

Algorithmic C (AC) Math Release Notes

Software Version v3.2.0

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Release 3.1.2

The following topics describes the changes that were made to the *ac_math* library since the last release. This release provides new functionality and bug fixes. This version of *ac_math* was included in Catapult release 10.3a.

Improved Bitwidth Calculation

The following PWL functions had the calculations for parameterized bitwidths of *ac_fixed* variables improved in order to eliminate redundant bits and reduce area:

- *ac_inverse_sqrt_pwl.h*
- *ac_log_pwl.h*
- *ac_pow_pwl.h*
- *ac_reciprocal_pwl.h*
- *ac_sqrt_pwl.h*
- *ac_tan_pwl.h*

Cleanup Sine/Cosine Cordic

The *ac_sincos_cordic.h* file was updated to rename a typedef so as to avoid a redeclaration conflict.

Removed Direct Access to AC Float Member Data

The *ac_reciprocal_pwl()*, *ac_inverse_sqrt_pwl()* and *ac_sqrt_pwl()* functions now no longer directly access the mantissa and exponent data members in the *ac_float* class for inputs. Instead, the functions use the *.mantissa()* and *.exp()* member functions to indirectly access (read-only) the data members of the input floating point variables.

Added New Power Function

A generic *ac_pow_pwl()* function was which accepted variable bases as well as exponents.

Default Template Parameter Changed

ac_exp_pwl() function now uses more fractional bits by default for an intermediate variable, to minimize error.

Corrected Issues

The following user-reported problems were fixed in this release:

- **(no bug #):** File: `ac_matrix.h` – `Transpose()` member function was incorrect.
- **(no bug #):** File `ac_sqrt_pwl.h` – Fixed bug in output near normalized 1 by adding extra bit to account for upward shifting of segments against the direction of concavity for `ac_float` types.
- **(no bug #):** File `ac_sincos_cordic.h` – Renamed the typedef to avoid redeclaration conflict with `ac_atan2_cordic.h`

Release 3.1.0

The following topics describes the changes that were made to the *ac_math* library since the last release. This release provides new functionality and bug fixes. This version of *ac_math* was included in Catapult release 10.3.

Hyperbolic Tangent File Renamed

The file `ac_hyperbolic_tan_pwl.h` was renamed to `ac_tanh_pwl.h` for consistency with the other header files.

Improved AC Complex Support

The file `ac_reciprocal_pwl.h` was changed to use better bitwidth calculation for intermediate variables in the `ac_complex<ac_float>` version.

Corrected Issues

The following user-reported problems were fixed in this release:

- **(bug #51400):** File: `ac_abs.h` – Function for `ac_int` values results in hardware that uses an $XW + 1$ bit adder instead of an $XW + 2$ bit adder, where XW is the input bitwidth, thereby reducing area and improving QofR.
- **(bug #51145):** Files: `ac_inverse_sqrt_pwl.h`, `ac_reciprocal_pwl.h` and `ac_sqrt_pwl.h` – Fixed expressions that directly manipulated the mantissa and exponent for `ac_float` outputs, replacing it with an `ac_float` constructor that performed normalization first and then modified the mantissa and exponent.
- **(no bug #):** File: `ac_sqrt.h` – Fixed expression that could cause overflow.
- **(no bug #):** Files: `ac_arccos_cordic.h` and `ac_arcsin_cordic.h` – Used different names for the class, function and variable in both the files to avoid name conflicts.

Release 2.0.10

This is the first official open-source release of the *ac_math* library. The following table lists the functions available in this release. For details about how to use the *ac_math* library consult the AC Math Reference Manual. This version of *ac_math* was included in Catapult release 10.2d.

Basic Math Functions

Function Type	Function Call	Approximation Method	Supported Data Types		
			ac_fixed	ac_float	ac_complex
Absolute Value	<i>ac_abs()</i>	N/A	Yes	Yes	No
Division	<i>ac_div()</i>	N/A	Yes	Yes	Yes
Normalization	<i>ac_normalize()</i>	N/A	Yes	No	Yes
Reciprocal	<i>ac_reciprocal_pwl()</i>	PWL	Yes	Yes	Yes
Logarithm Base e	<i>ac_log_pwl()</i>	PWL	Yes	No	No
	<i>ac_log_cordic()</i>	CORDIC	Yes	No	No
Logarithm Base 2	<i>ac_log2_pwl()</i>	PWL	Yes	No	No
	<i>ac_log2_cordic()</i>	CORDIC	Yes	No	No
Exponent Base e	<i>ac_exp_pwl()</i>	PWL	Yes	No	No
	<i>ac_exp_cordic()</i>	CORDIC	Yes	No	No
Exponent Base 2	<i>ac_pow2_pwl()</i>	PWL	Yes	No	No
	<i>ac_exp2_cordic()</i>	CORDIC	Yes	No	No
Generic Exponent	<i>ac_pow_pwl()</i>	PWL	Yes	No	No
	<i>ac_pow_cordic()</i>	CORDIC	Yes	No	No
Square Root	<i>ac_sqrt_pwl()</i>	PWL	Yes	Yes	Yes
	<i>ac_sqrt()</i>	N/A	Yes	No	No
Inverse Square Root	<i>ac_inverse_sqrt_pwl()</i>	PWL	Yes	Yes	Yes
Sine/Cosine	<i>ac_sincos()</i>	LUT	Yes	No	No
	<i>ac_cos_cordic()</i>	CORDIC	Yes	No	No
	<i>ac_sin_cordic()</i>	CORDIC	Yes	No	No
	<i>ac_sincos_cordic()</i>	CORDIC	Yes	No	No
Tangent	<i>ac_tan_pwl()</i>	PWL	Yes	No	No
Inverse Trig	<i>ac_atan_pwl()</i>	PWL	Yes	No	No
	<i>ac_arccos_cordic()</i>	CORDIC	Yes	No	No

Function Type	Function Call	Approximation Method	Supported Data Types		
			ac_fixed	ac_float	ac_complex
	<i>ac_arcsin_cordic()</i>	CORDIC	Yes	No	No
	<i>ac_arctan_cordic()</i>	CORDIC	Yes	No	No
Shift Left/Right	<i>ac_shift_left</i>	N/A	Yes	No	Yes
	<i>ac_shift_right</i>	N/A	Yes	No	Yes
Hyperbolic Tangent	<i>ac_tanh_pwl</i>	PWL	Yes	No	No
Sigmoid	<i>ac_sigmoid_pwl</i>	PWL	Yes	No	No
Softmax	<i>ac_softmax_pwl</i>	PWL	Yes	No	No

AC Matrix Class

The class `ac_matrix` implements a 2-D container class with a template parameter to specify the data type of the internal storage.

The class has member functions to implement some common operations including

- Assignment: `operator=()`
- Read-Only and Read-Write Element Access: `*this(<row>,<col>)`
- Comparison: `operator!=()`, `operator==()`
- Piecewise Addition: `operator+()`, `operator+=()`
- Piecewise Subtraction: `operator-()`, `operator-=()`
- Piecewise Multiplication: `pwisemult()`
- Matrix Multiplication (nested loops): `operator*()`
- Matrix Transpose: `transpose()`
- Sum All Elements: `sum()`
- Scale All Elements: `scale(value)`
- Formatted Stream Output: `ostream &operator<<()`

When using the computational functions with AC Datatypes, the form that returns a value is designed in such a way as to determine the full precision required in the output type in order to preserve accuracy during the operation. So using `operator+` between two 10 bit `ac_fixed` matrices will return an 11 bit `ac_fixed` matrix. If you wish to prevent the bit growth and accept the truncation, you can use the compound operators `+=`, `-=`, etc. so that the target object receives the truncated values.

In addition to the built-in member functions, the `ac_math` library also includes stand-alone functions for more complicated linear algebra operations as described in the next section.

Linear Algebra Functions

The `ac_math` library includes several linear algebra functions that operate on either `ac_matrix` or plain C-style arrays. These functions, when used with AC Datatypes, are designed to give the user greater control over the bit precision of internal variables and the return value.

- Matrix Multiplication
- Matrix Determinant
- Cholesky Decomposition
- Cholesky Inverse
- QR Decomposition

Supported Compilers

The PWL functions use default template arguments. This requires using a C++ compiler that support the C++11 or newer standard.