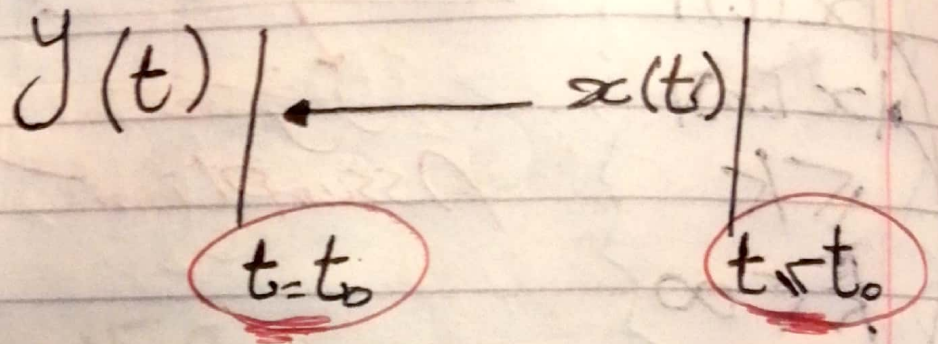


Lec. 7

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[3] Causality:-



ex:- $y[n] = x[n] + 3x[n+1]$

System equation

$$y[0] = x[0] + 3x[1]$$

↑

↑

0

1

∴ the system is Not Causal.

ex: $y(t) = x(t) - \cos(t+3)$

∴ the system is Memoryless.

∴ the system is Causal.

[4] Stability:- $BIBO$

Complex

$$|x(t)|$$

$$|x[n]|$$

$$\leq k$$

$$k < \infty$$

$$\forall t$$

$$\forall n$$

Bounded input

Bounded output

Assumption

Trial Check

$$\text{ex- } y(t) = t \cdot x(t)$$

Let $|x(t)| \leq k, k < \infty, \forall t$.

$$|y(t)| = |t \cdot x(t)|$$

Recall $|A \cdot B| = |A| \cdot |B|$

$$\therefore |y(t)| = |t| \cdot |x(t)|$$

$$\leq k \cdot |t|$$

$$\text{at } t = \pm \infty \implies |y(t)| = \infty$$

\therefore the system is not stable.

ex: $y(t) = e^{x(t)}$

Let $|x(t)| \leq k, k < \infty; \forall t$.

$$|y(t)| = |e^{x(t)}| = e^{x(t)} \leq e^{|x(t)|} \leq e^k < \infty$$

\therefore the output is Bounded.

then the system is stable.

[5] Time-Invariance:-

$$y(t) \rightarrow x(t)$$

$$y(t+t_0) \leftarrow x(t+t_0)$$

Time-shift for I/P

Same " " " O/P

ex:-

$$y(t) = \sin(x(t))$$

$$\text{Let } x_1(t) \xrightarrow{S} y_1(t) = \sin(x_1(t))$$

$$\text{and let } x_2(t) = x_1(t-t_0) \xrightarrow{S} y_2(t) = \sin(x_2(t)) \quad \text{--- (1)}$$

$$\therefore y_2(t) = \sin(x_1(t-t_0)) \quad \text{--- (2')}$$

$$y_1(t-t_0) = \sin(x_1(t-t_0)) \quad \text{--- (3)}$$

$$\therefore y_2(t) = y_1(t-t_0)$$

\therefore the system is time-Invariance

ex1-

$$y[n], n \geq x[n]$$

$$\text{Let } x_1[n] \xrightarrow{S} y_1[n] = n x_1[n] \rightarrow \textcircled{1}$$

$$\text{and Let } x_2[n] = x_1[n-n_0] \xrightarrow{S} y_2[n] = n x_2[n] \rightarrow \textcircled{2}$$

$$\therefore y_2[n] = n x_1[n-n_0] \rightarrow \textcircled{2'}$$

$$y_1[n-n_0] = (n-n_0) x_1[n-n_0] \rightarrow \textcircled{3}$$

$$\therefore y_2[n] \neq y_1[n-n_0]$$

\therefore the system is not time Invariant