Cuckoo Cycle: a graph-theoretic proof-of-work system

John Tromp April 7, 2014

Abstract

We introduce the first graph-theoretic proof-of-work system, based on finding cycles on large random graphs. Such problems are arbitrarily scalable trivially verifiable. Our implementation requires the use of 1 bit per edge. We hypothesize that using less causes superlinear slowdown.

1 Introduction

A "proof of work" (PoW) system allows a verifier to check with negligible effort that a prover has expended a large amount of computational effort. Originally introduced as a spam fighting measure, where the effort is the price paid by an email sender for demanding the recipient's attention, they now form one of the cornerstones of crypto-currencies.

As proof-of-work for new blocks of transactions, Bitcoin [1] uses hashcash [2]. This requires finding a nonce value such that twofold application of the cryptographic hash function SHA256 to this nonce (and the rest of the block header) results in a number with many leading 0s. The bitcoin protocol dynamically adjust this "difficulty" number so as to maintain a 10-minute average block interval. Starting out at 32 leading zeroes in 2009, the number has steadily climbed and is currently at 64, representing an incredible $2^{64}/10$ double-hashes per minute. This growth was enabled by the migration of hash computation from desktop processors (CPUs) to graphics-card processors (GPUs), to field-programmable gate arrays (FPGAs), and finally to custom designed chips (ASICs).

Downsides of this development include high investment costs, rapid obsolesence, centralization of mining power, and large power consumption. Although ASICs are the most energy-efficient way of computing hashes, the tiny amount of die-space needed for a single SHA256 circuit allows a huge number of them (e.g. 1440 on KnC's Neptune) to be crammed onto a single chip, consuming 100s of Watts and requiring ample cooling. Thus, energy costs dominate the economics of mining.

This has led people to look for alternative proof-of-work systems that, by requiring a nontrivial amount of memory, resist such massive parallelizability, and narrow the performance gap with commodity hardware. Memory chips, in the form of DRAM, have only a tiny portion of their circuitry active at any time, and thus require orders of magnitude less power.

Litecoin replaces the SHA256 hash function in hashcash by a single round version of the *scrypt* key derivation function. Its memory requirement of 128KB is a compromise between computation-hardness for the prover and verification efficiency for the verifier. Although designed to be GPU-resistant, GPUs are now at least an order of magnitude faster than CPUs for Litecoin mining. ASICs first appeared on the market in early 2014 and are expected to dominate Litecoin mining by the fourth quarter.

Primecoin [3] is an interesting design based on finding long Cunningham chains of prime numbers, using a two-step process of filtering candidates by *sieving*, and applying pseudo-primality tests to remaining candidates. GPU implementations that outperform CPU ones have recently appeared.

Downsides to this proof-of-work are its complexity and the scope for algorithmic improvements. Its memory requirements, while larger than Litecoin's, are still modest.

Momentum [4] proposes finding birthday collisions of hash outputs as proof-of-work, the simplest way to combine scalable memory usage with trivial verifiability. Its memory requirements are not very strict though. as Bloom filters or rainbow tables can identify collisions, and parallellizes well.

Adam Back [5] has a good overview of proof-of-work papers past and present.

2 Memory latency; the great equalizer

While cpu-speed and (sequential) memory bandwidth are highly variable across time and architectures, main memory latencies have remained relatively stable. This suggests making the proof-of-work system latency-bound to level the mining playing field. Ideally, it should have the following properties:

verify-trivial A proof can be checked in microseconds rather than milliseconds.

scalable The amount of memory needed is a parameter that can scale arbitrarily.

linear Amount of computational steps and memory accesses are linear in the amount of memory.

tmto-hard Using only half as much memory should incur several orders of magnitude slowdown.

random-access RAM is accessed randomly, making sequential bandwidth and caches mostly irrelevant.

parallel-hard The algorithm cannot be parallellized within a single instance, i.e. proof attempt).

simple The algorithm should be sufficiently simple that one can be convinced of its optimality.

Combined, these properties ensure that a proof-of-work system is entirely constrained by main memory latency and scales appropriately for any application.

We introduce the very first graph-theoretic proof-of-work system. which aims to satisfy most of the above properties, except for parallel-hardness (see the later section on parallelizability). Amazingly, it amounts to little more than enumerating nonces and storing them in a hashtable. While all hashtables break down when trying to store more items than it was designed to handle, in one hashtable design in particular this breakdown is of a special nature that can be turned into a concise and easily verified proof. Enter the cuckoo hashtable.

3 Cuckoo hashing

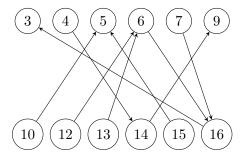
Introduced by Rasmus Pagh and Flemming Friche Rodler [6], a cuckoo hashtable consists of two same-sized tables each with its own hash function mapping a key to a table location, providing two possible locations for each key. Upon insertion of a new key, if both locations are already occupied by keys, then one is kicked out and inserted in its alternate location, possibly displacing yet another key, repeating the process until either a vacant location is found, or some maximum number of iterations is reached. The latter can only happen once cycles have formed in the *Cuckoo graph*. This is a bipartite graph with a node for each location and an edge for every key, connecting the two locations it can reside at. This naturally suggests a proof-of-work problem, which we now formally define.

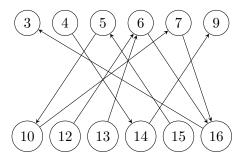
4 The proof-of-work function

Fix an (even) number of nodes $8 \le N < 2^{64}$, a number of edges $N/4 < E \le N$, and an (even) cycle length $4 \le L < N$. Function cuckoo maps any 128-bit key k (the header digest) to a bipartite graph $G = (V_0 \cup V_1, E)$, where V_0 and V_1 are disjoint set of integers modulo N/2, and E has an edge between siphash $(k, 2 * n) \mod \frac{N}{2}$ in V_0 and siphash $(k, n) \mod \frac{N}{2}$ in V_1 for every nonce $0 \le n < E$. A proof for G is a subset of E nonces whose corresponding edges form an E-cycle in G.

5 Solving the proof-of-work problem

We enumerate the E nonces, but instead of storing the nonce itself as a key in the Cuckoo hashtable, we store the alternate key location at the key location, and forget about the nonce. We thus maintain the directed cuckoo graph, in which the edge for a key is directed from the location where it resides to its alternate location. Moving a key to its alternate location thus corresponds to reversing its edge. The outdegree of every node in this graph is either 0 or 1. When there are no cycles yet, the graph is a forest, a disjoint union of trees. In each tree, all edges are directed, directly, or indirectly, to its root, the only node in the tree with outdegree 0. Initially there are just N singleton trees consisting of individual nodes which are all roots. Addition of a new key causes a cycle if and only if its two endpoints are nodes in the same tree, which we can test by following the path from each endpoint to its root. In case of different roots, we reverse all edges on the shorter of the two paths, and finally create the edge for the new key itself, thereby joining the two trees into one. The left diagram below shows the directed cuckoo graph for header 'header' on N=9+7 nodes after adding edges (3,16), (5,15), (6,16), (7,16), (5,10), (6,13), (6,12), (9,14) and (4,14) (nodes with no incident edges are omitted for clarity). In order to add the 10th edge (7,10), we follow the paths $7 \to 16 \to 3$ and $10 \to 5$ to find different roots 3 and 5. Since the latter path is shorter, we reverse it to $5 \to 10$ so we can add the new edge as $(10 \rightarrow 7)$, resulting in the right diagram.





When adding the 11th edge (3,15), we find the singleton path 3 and the path $15 \rightarrow 5 \rightarrow 10 \rightarrow 7 \rightarrow 16 \rightarrow 3$ with equal roots. In this case, we can compute the length of the resulting cycle as 1 plus the sum of the path-lengths to the node where the two paths first join. In the diagram, the paths first join at the root, and the cycle length is computed as 1+0+5=6. If the cycle length equals L, then we solved the problem, and recover the proof by enumerating nonces once more and checking which ones formed the cycle. If not, then we keep the graph acyclic by ignoring the edge. There is some probability of overlooking other L-cycles through that edge, but in the important case of having few cycles in the cuckoo graph to begin with, it hardly affects the rate of solution finding.

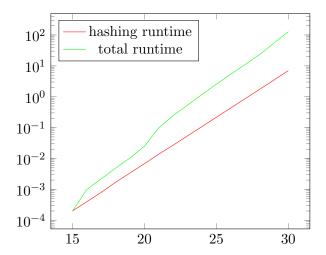
6 Union-find

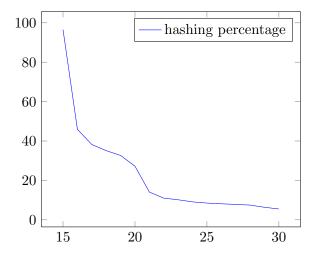
The above representation of the directed cuckoo graph is an example of a disjoint-set data structure [7], and our algorithm is closely related to the well known union-find algorithm, where the find operation

determines which subset an element is in, and the union operation joins two subsets into a single one. For each edge addition to the cuckoo graph we perforn the equivalent of two find operations and one union operation. The difference is that the union-find algorithm is free to add directed edges between arbitrary elements. Thus it can join two subsets by adding an edge from one root to another, with no need to reverse any edges. Conversely, our algorithm can be seen as the first one that solves the union-find problem by maintaining a direction on all union operations while keeping the maximum outdegree at 1.

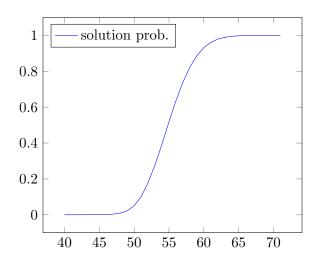
7 Implementation and performance

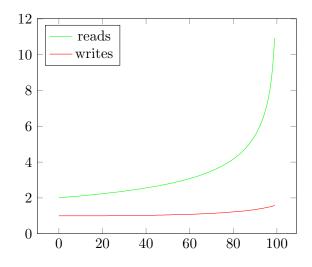
The C-program listed in the Appendix is also available online at https://github.com/tromp/cuckoo together with a Makefile, proof verifier and the latest version of this paper. 'make test' tests everything. 'make example' reproduces the example shown above. The main program uses 32 bits per node to represent the directed cuckoo graph, plus about 56KB per thread for 3 auxiliary arrays. The us and vs arrays not only record traversed paths, but also double as a mini cuckoo table used for storing edges of a solution cycle, allowing easy recovery of the proof nonces. The uvpre array precomputes edges in blocks of 1024, which was found (inexplicably) to save up to 30% runtime. The left plot below shows both the total runtime in seconds and the runtime of just the hash computation, as a function of (log)size. The latter is purely linear, while the former is superlinear due to increasing memory latency as the nodes no longer fit in cache. The right plot show this more clearly as the percentage of hashing to total runtime, ending up around 5%.





On a 3.2GHz Intel Core i5, size 2^{20} takes 4MB and 0.025s, size 2^{25} takes 128MB and 2.5s, and size 2^{30} takes 4GB and 128s, or roughly half a minute per GB. The left plot below shows the probability of finding a 42-cycle as a function of the percentage edges/nodes (relative easiness), while the right plot shows the average number of memory reads and writes per edge as a function of the percentage nonce/easiness (progress through main loop). Both were determined from 10000 runs at size 2^{20} ; results at size 2^{25} look almost identical. In total the program averages 3.3 reads and 1.1 writes per edge.





8 Difficulty control

Relative easiness (the ratio E/N) determines a base level of difficulty, which may suffice for applications where difficulty is to remain fixed. The ratio E/N=1 is suitable when a practically guaranteed solution is desired, For crypto currencies, where difficulty must scale in precisely controlled manner across a huge range, adjusting easiness is not suitable. The implementation default E/N=1/2 gives a solution probability of roughly 2.2%, while the average number of cycles found increases slowly with size; from 2 at 2^{20} to 3 at 2^{30} . For further control, a difficulty target $0 < T < 2^{256}$ is introduced, and we impose the additional constraint that the sha256 digest of the cycle nonces in ascending order be less than T, thus reducing the success probability by a factor $2^{256}/T$.

9 Memory-hardness

I conjecture that this problem doesn't allow for a time-memory trade-off. If one were to store only a fraction p of V_0 and V_1 , then one would have to reject a fraction p^2 of generated edges, drastically reducing the odds of finding cycles for $p < 1/\sqrt{2}$ (the reduction being exponential in cycle length).

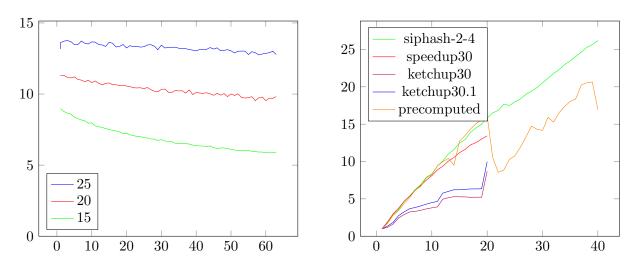
10 Parallelization

The implementation allows the number of threads to be set with option -t. For $0 \le t < T$, thread t processes all nonces t mod T. Parallelization presents some algorithmic challenges. Paths from an edge's two endpoints are not well-defined when other edge additions and path reversals are still in progress. One example of such a path conflict is the check for duplicate edges yielding a false negative, if in between checking the two endpoints, another thread reverses a path through those nodes. Another is the addition of edges (7,10) and (3,15) in the example diagrams. If these were to happen in parallel, then the path from 15 will likely end at 5 because edge $(10 \to 5)$ hasn't been reversed yet. As a result, $(3 \to 15)$ will be added, not realizing it creates a cyle. Thus, in a parallel implementation, path following can no longer be assumed to terminate. Instead of using a cycle detection algorithm such as [8], our implementation notices when the path length exceeds MAXPATHLEN (4096 by default), and reports wether this is due to a path conflict. The left plot below shows the average number of times that either of the two roots for a nonce occurred a given number of nonces ago, showing that there are potentially about 10T such conflicts. Despite these conflicts, and the complete lack of synchronization between threads (apart from a solution recording mutex), the cuckoo array at any

time represents some, possibly cyclic, directed cuckoo graph on a subset of processed nonces. On 2^{20} nodes, aborts happened 0.03% of the time with 2 threads, 0.1% with 4 threads, 0.27% with 8 threars, and 0.2% with 12 threads. They overlooked 0.13%, 0.31%, 0.57%, and 0.17%, respectiverly, of the 42-cycles found by the single-threaded runs. Empirically then, path conflicts have negligable effect on multi-threaded performance. The percentage of hashing to total runtime shows the same behaviour as in the single-threaded case, with a dual Xeon X5670 machine spending only 5.5% of wallclock time on hashing with 2^{28} nodes.

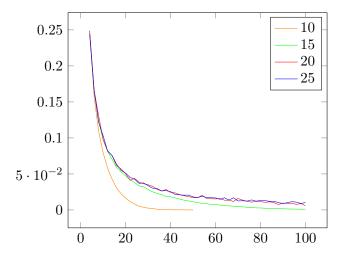
The right plot shows in green the speedup achieved by up to 40 threads on a system with two Intel Xeon E5-2690 cpus, each which 10 hyperthreaded cores running at 3GHz. Each datapoint represents 10 runs on 2³⁰ nodes with headers "0" through "9". Although the speedup is sublinear at 26 for 40 threads, it doesn't look like the memory interface is saturated yet. Since we don't have access to more than 40 threads, we tried two alternative approaches to see happens when the memory access frequency increases further, In the second approach we precompute all the hashes, shown in orange. This shows some sort of breakdown of the memory interface starting from 21 threads, which is presumably where hyperthreading starts to kick in. It is perhaps odd that such a hyperthreading transition is completely absent from the green line. Since the hash precomputation showed a significant speedup, the implementation was changed to make it the default. Reproducing the other curves requires compilation with -DPRESIP=0 for C or setting CuckooSolve.PRESIP=1 for java.

UPDATE: We added 3 curves for the new implementation with 21x reduced memory, tested up to 20 threads. This shows some really weird boost at the thread maximum.



11 Choice of cycle length

Extremely small cycle lengths risk the feasability of alternative datastructures that are more memory-efficient. For example, for L=2 the problem reduces to finding a birthday collision as in the Momentum proof-of-work. It is conceivable however that the Cuckoo representation is already optimal for L=4. Such small values still harm the TMTO resistance though, as mentioned in the previous paragraph, and may reduce parallelization resistance. In order to keep proof size manageable, the cycle length should not be too large either. We consider 20-64 to be a healthy range, which averages to 42. The plot below shows the distribution of cycle lengths found for sizes 2^{10} , 2^{15} , 2^{20} , 2^{25} , as determined from 100000,100000,100000, and 10000 runs respectively. The tails of the distributions beyond L=100 are not shown. For reference, the longest cycle found was of length 2120.



12 Choice of memory size

The memory requirement should exceed that of the largest available single-chip memory to enforce offchip latencies. It should also be a significant fraction of the typical memory of a botnet computer, With a significant risk of sending machines into swap-hell and likely alerting its owner, botnet operators will refrain from deploying Cuckoo Cycle, prefering other proof-of-work schemes whose smaller memory footprint allows them to stay under the radar. With memory sizes doubling roughly every 18 months, 16GB will become commonplace in a few years. While the current algorithm can accomodate up to $N = 2^{33} - 2$ nodes (32GB) by separately keeping track of which partition a vertex is in, a different idea is needed to scale beyond that. To that end, we propose to use K-partite graphs with edges only between partition k and partition k and partition consisting of at most k is fed into the hash function along with the header and nonce. With each partition consisting of at most k is fed into the hash function along with the header and nonce. With each partition consisting of at most k is fed into the hash function along with the header and nonce. With each partition consisting of at most k is fed into the hash function along with the header and nonce. With each partition consisting of at most k is fed into the hash function along with the header and nonce. With each partition consisting of at most k is fed into the hash function along with the header and nonce. With each partition consisting of at most k is fed into the hash function along with the header and nonce with each partition significant bit is then available to distinguish edges to the two neighbouring partitions. Setting the size of partition 0 to be relatively prime to k is relatively prime.

13 Conclusion

Cuckoo Cycle is an elegant proof-of-work design emphasizing memory latency over computation. This promotes investment in low-power general purpose hardware (RAM) rather than investment in single purpose hardware coupled with high operational costs, making mining more sustainable. More research is needed to determine the limits of parallelizability.

References

- [1] S. Nakamoto, "Bitcoin: A peer-to-peer electronic cash system," Tech. Rep., May 2009. [Online]. Available: http://www.bitcoin.org/bitcoin.pdf
- [2] A. Back, "Hashcash a denial of service counter-measure," Tech. Rep., Aug. 2002, (implementation released in mar 1997).
- [3] S. King, "Primecoin: Cryptocurrency with prime number proof-of-work," Tech. Rep., Jul. 2013. [Online]. Available: http://primecoin.org/static/primecoin-paper.pdf

- [4] D. Larimer, "Momentum a memory-hard proof-of-work via finding birthday collisions," Tech. Rep., Oct. 2013. [Online]. Available: http://invictus-innovations.com/s/MomentumProofOfWork-hok9.pdf
- [5] A. Back, "Hashcash.org," Feb. 2014. [Online]. Available: http://www.hashcash.org/papers/
- [6] R. Pagh and F. F. Rodler, "Cuckoo hashing," *J. Algorithms*, vol. 51, no. 2, pp. 122–144, May 2004. [Online]. Available: http://dx.doi.org/10.1016/j.jalgor.2003.12.002
- [7] Wikipedia, "Disjoint-set data structure wikipedia, the free encyclopedia," 2014, [Online; accessed 23-March-2014]. [Online]. Available: http://en.wikipedia.org/w/index.php?title=Disjoint-set_data_structure&oldid=600366584
- [8] R. P. Brent, "An improved Monte Carlo factorization algorithm," BIT, vol. 20, pp. 176–184, 1980.

14 Appendix A: cuckoo.h

```
// Cuckoo Cycle, a memory-hard proof-of-work
// Copyright (c) 2013-2014 John Tromp
#include <stdint.h>
#include <string.h>
#include copenssl/sha.h> // if openssl absent, use #include "sha256.c"
// proof-of-work parameters
#ifndef SIZESHIFT
#define SIZESHIFT 25
#endif
#ifndef PROOFSIZE
#define PROOFSIZE 42
#endif
#define SIZE (1UL<<SIZESHIFT)
#define HALFSIZE (SIZE/2)
#define NODEMASK (HALFSIZE-1)
typedef uint32_t u32;
typedef uint64_t u64;
typedef u64 nonce_t;
#ifdef TRIMEDGES
typedef u64 node_t;
#else
\mathbf{typedef} \ \ \mathbf{u32} \ \ \mathbf{node\_t} \ ;
#endif
typedef struct {
  u64 v [4];
} siphash_ctx;
#define U8TO64_LE(p) \
  (((u64)((p)[0])
                         ) | ((u64)((p)[1]) \ll 8)
   ((u64)((p)[2]) \ll 16) | ((u64)((p)[3]) \ll 24)
   ((u64)((p)[4]) \iff 32) \mid ((u64)((p)[5]) \iff 40) \mid \
   ((u64)((p)[6]) \ll 48) \mid ((u64)((p)[7]) \ll 56))
// derive siphash key from header
void setheader(siphash_ctx *ctx, const char *header) {
```

```
unsigned char hdrkey [32];
  SHA256((unsigned char *) header, strlen(header), hdrkey);
  u64 k0 = U8TO64_LE(hdrkey);
  u64 k1 = U8TO64\_LE(hdrkey+8);
  ctx \rightarrow v[0] = k0 \quad 0x736f6d6570736575ULL;
  ctx \rightarrow v[1] = k1 \hat{0}x646f72616e646f6dULL;
  ctx \rightarrow v[2] = k0 \quad 0x6c7967656e657261ULL;
  ctx \rightarrow v[3] = k1 \quad 0x7465646279746573ULL;
#define ROTL(x,b) (u64)( ((x) << (b)) | ((x) >> (64 - (b))) )
#define SIPROUND \
  do { \
    v0 += v1; v2 += v3; v1 = ROTL(v1, 13); \setminus
    v3 = ROTL(v3, 16); v1 = v0; v3 = v2;
    v0 = ROTL(v0, 32); v2 += v1; v0 += v3;
    v1 = ROTL(v1, 17); v3 = ROTL(v3, 21);
    v1 = v2; v3 = v0; v2 = ROTL(v2, 32); \
  } while(0)
// SipHash-2-4 specialized to precomputed key and 8 byte nonces
u64 siphash24(siphash_ctx *ctx, u64 nonce) {
  u64 \ v0 = ctx - v[0], \ v1 = ctx - v[1], \ v2 = ctx - v[2], \ v3 = ctx - v[3] \ \hat{} \ nonce;
  SIPROUND; SIPROUND;
  v0 = nonce;
  v2 = 0xff;
  SIPROUND; SIPROUND; SIPROUND;
  return v0 \hat{v}1 \hat{v}2 \hat{v}3;
}
void sipedge(siphash_ctx *ctx, nonce_t nonce, node_t *pu, node_t *pv) {
  *pu = siphash24(ctx, 2*nonce) & NODEMASK;
  *pv = siphash24(ctx, 2*nonce+1) & NODEMASK;
// generate edge endpoint in cuckoo graph
node_t sipedge_u(siphash_ctx *ctx, nonce_t nonce) {
  return siphash24(ctx, 2*nonce) & NODEMASK;
}
// generate edge endpoint in cuckoo graph
node_t sipedge_v(siphash_ctx *ctx, nonce_t nonce) {
  return siphash24(ctx, 2*nonce+1) & NODEMASK;
// verify that (ascending) nonces, all less than easiness, form a cycle in header-generated graph
int verify(nonce_t nonces[PROOFSIZE], const char *header, u64 easiness) {
  siphash_ctx ctx;
  setheader(&ctx, header);
  node_t us[PROOFSIZE];
  unsigned i = 0, n;
  for (n = 0; n < PROOFSIZE; n++) {
    if (nonces[n] >= easiness || (n && nonces[n] <= nonces[n-1]))
      return 0;
    sipedge(\&ctx, nonces[n], \&us[n], \&vs[n]);
  \mathbf{do} { // follow cycle until we return to i=0; n edges left to visit
    unsigned j = i;
    for (unsigned k = 0; k < PROOFSIZE; k++) // find unique other j with same vs[j]
      if (k != i \&\& vs[k] == vs[i]) {
```

```
if (j != i)
        return 0;
      j = k;
  if (j == i)
   return 0;
  i = j;
  for (unsigned k = 0; k < PROOFSIZE; k++) // find unique other i with same us[i]
    if (k != j \&\& us[k] == us[j]) {
      if (i != j)
        return 0;
      i = k;
  if (i == j)
    return 0;
 n = 2;
} while (i);
return n = 0;
```

15 Appendix B: cuckoo_miner.h

```
// Cuckoo Cycle, a memory-hard proof-of-work
// Copyright (c) 2013-2014 John Tromp
#include "cuckoo.h"
#ifdef __APPLE__
#include "osx_barrier.h"
#endif
#include <stdio.h>
#include <stdlib.h>
#include <pthread.h>
#include <assert.h>
#include <vector>
#include <atomic>
#include <set>
// ok for size up to 2^32
#define MAXPATHLEN 8192
#ifdef TRIMEDGES
#include "trim_edge_data.h"
#else
#ifndef PRESIP
#define PRESIP 1024
#endif
#define CUCKOOSET(key, val)
                                cuckoo [key] = val
#define CUCKOOHASH
                        node_t *
class graph_data {
public:
  node_t *cuckoo;
  graph_data(nonce_t easiness, int nthreads) {
    assert(cuckoo = (node_t *)calloc(1+SIZE, sizeof(node_t)));
   graph_data() {
    free (cuckoo);
```

```
};
#endif
class cuckoo_ctx {
public:
  siphash_ctx sip_ctx;
  nonce_t easiness;
  graph_data data;
  nonce_t (*sols)[PROOFSIZE];
  unsigned maxsols;
  std::atomic<unsigned> nsols;
  int nthreads;
  \mathbf{int} \quad \mathtt{ntrims} \, ;
  pthread_barrier_t barry;
  cuckoo_ctx(const char* header, nonce_t easy_ness, int n_threads, int n_trims, int max_sols)
  : data(easy_ness, n_threads) {
    setheader(&sip_ctx , header);
    easiness = easy_ness;
    nthreads = n_{threads};
    ntrims = n_trims;
    assert (pthread_barrier_init(&barry, NULL, nthreads) == 0);
    assert(sols = (nonce_t (*)[PROOFSIZE])calloc(maxsols = max_sols, PROOFSIZE*sizeof(nonce_t)));
    nsols = 0;
  }
};
typedef struct {
  int id;
  pthread_t thread;
  cuckoo_ctx *ctx;
} thread_ctx;
#ifdef TRIMEDGES
void barrier(pthread_barrier_t *barry) {
  int rc = pthread_barrier_wait(barry);
  if (rc != 0 && rc != PTHREAD_BARRIER_SERIAL_THREAD) {
    printf("Could_not_wait_on_barrier\n");
    pthread_exit(NULL);
}
#define FORALL_LIVE_NONCES(NONCE) \
  for (nonce_t block = tp->id *32; block < ctx.easiness; block += ctx.nthreads *32) {\
    for (nonce_t NONCE = block; NONCE < block+32 && NONCE < ctx.easiness; NONCE++) {\
      if (alive.test(NONCE))
void trim_edges(thread_ctx *tp, unsigned part) {
  cuckoo_ctx &ctx = *tp->ctx;
  graph_data &data = ctx.data;
  shrinkingset &alive = *data.alive;
  twice_set &nonleaf = *data.nonleaf;
  if (tp \rightarrow id = 0)
    nonleaf.reset();
  barrier(&ctx.barry);
  FORALL_LIVE_NONCES(nonce) {
    node_t u = sipedge_u(&ctx.sip_ctx, nonce);
    if ((u & PART_MASK) == part)
      nonleaf.set(u >> PART_BITS);
```

```
}}}
  barrier(&ctx.barry);
  FORALL_LIVE_NONCES(nonce) {
     node_t u = sipedge_u(&ctx.sip_ctx, nonce);
     if ((u & PART_MASK) == part && !nonleaf.test(u >> PART_BITS))
     alive.reset(nonce, tp->id);
  }}}
  barrier(&ctx.barry);
  if (tp \rightarrow id = 0)
     nonleaf.reset();
  barrier(&ctx.barry);
  FORALL_LIVE_NONCES(nonce) {
     node_t v = sipedge_v(\&ctx.sip_ctx, nonce);
     if ((v & PART_MASK) == part)
       nonleaf.set(v >> PART_BITS);
  }}}
  barrier(&ctx.barry);
  FORALL_LIVE_NONCES(nonce) {
     node_t v = sipedge_v(&ctx.sip_ctx, nonce);
     if ((v & PART_MASK) == part && !nonleaf.test(v >> PART_BITS))
       alive.reset (nonce, tp->id);
  }}}
  barrier(&ctx.barry);
#endif
int path(CUCKOOHASH cuckoo, node_t u, node_t *us) {
  int nu;
  for (nu = 0; u; u = cuckoo[u]) {
     if (++nu >= MAXPATHLEN) {
       while (nu— && us[nu] != u) ;
       if (nu < 0)
          printf("maximum_path_length_exceeded\n");
       \textbf{else} \hspace{0.2cm} \texttt{printf} \hspace{0.1cm} (\texttt{"illegal\_\%\_4d-cycle} \hspace{0.1cm} \backslash \texttt{n"} \hspace{0.1cm}, \hspace{0.1cm} \texttt{MAXPATHLEN-nu}) \hspace{0.1cm} ;
       pthread_exit(NULL);
     us[nu] = u;
  }
  return nu;
typedef std::pair<node_t,node_t> edge;
void solution(cuckoo_ctx &ctx, node_t *us, int nu, node_t *vs, int nv) {
  std::set<edge> cycle;
  unsigned n;
  cycle.insert(edge(*us, *vs));
  while (nu--)
     cycle.insert(edge(us[(nu+1)&^{1}], us[nu|1])); // u's in even position; v's in odd
  while (nv--)
     {\tt cycle.insert} \, (\, {\tt edge} \, (\, {\tt vs} \, [\, {\tt nv} \, | \, 1] \, , \ {\tt vs} \, [\, (\, {\tt nv} \, + \, 1) \, \& \, \tilde{} \, 1] \, )); \ /\!/ \ u \, {\it 's in odd position} \, ; \ v \, {\it 's in even} \, .
  unsigned soli = std::atomic_fetch_add_explicit(&ctx.nsols, 1U, std::memory_order_relaxed);
  for (nonce_t nonce = n = 0; nonce < ctx.easiness; nonce++)
#ifdef TRIMEDGES
    if (ctx.data.alive -> test (nonce))
#endif
       edge e(1+sipedge_u(&ctx.sip_ctx, nonce), 1+HALFSIZE+sipedge_v(&ctx.sip_ctx, nonce));
       if (cycle.find(e) != cycle.end()) {
          ctx.sols[soli][n++] = nonce;
```

```
cycle.erase(e);
      }
    }
}
void *worker(void *vp) {
  thread_ctx *tp = (thread_ctx *)vp;
  cuckoo_ctx &ctx = *tp->ctx;
  graph_data &data = ctx.data;
#ifdef TRIMEDGES
  shrinkingset &alive = *data.alive;
  int load = 100;
  for (int round=1; round <= ctx.ntrims; round++) {
    for (unsigned part = 0; part <= PART_MASK; part++)
      trim_edges(tp, part);
    if (tp\rightarrow id = 0) {
      load = (int)(100 * alive.count() / CUCKOO_SIZE);
      printf("%d_trims:_load_%d%%\n", round, load);
    }
  if (tp->id == 0) {
    if (load >= 90) {
      printf("overloaded!_exiting...");
      exit(0);
    delete data.nonleaf;
    data.nonleaf = 0;
    data.cuckoo = new cuckoo_hash();
  barrier(&ctx.barry);
  cuckoo_hash &cuckoo = *data.cuckoo;
  node_t us [MAXPATHLEN] , vs [MAXPATHLEN] ;
  FORALL_LIVE_NONCES(nonce) {
    node_t u0, v0;
    sipedge(&ctx.sip_ctx, nonce, &u0, &v0);
  node_t *cuckoo = data.cuckoo;
  {\tt node\_t} \;\; us \, [\texttt{MAXPATHLEN}] \;, \;\; vs \, [\texttt{MAXPATHLEN}] \;, \;\; uvpre \, [2*PRESIP] \;, \;\; npre \; = \; 0;
  for (node_t nonce = tp->id; nonce < ctx.easiness; nonce += ctx.nthreads) {{{
    node_t u0, v0;
    if (!npre) {
      for (unsigned n = nonce; npre < PRESIP; npre++, n += ctx.nthreads)
        sipedge(\&ctx.sip\_ctx, n, \&uvpre[2*npre], \&uvpre[2*npre+1]);
    }
    unsigned i = PRESIP - npre--;
    u0 = uvpre[2*i];
    v0 = uvpre[2*i+1];
#endif
                    ; // make non-zero
    \mbox{v0 += 1 + HALFSIZE;} \quad // \  \mbox{\it make v's different from u's}
    node_t u = cuckoo[u0], v = cuckoo[v0];
    if (u = v0 | v = u0)
      continue; // ignore duplicate edges
    us[0] = u0;
    vs[0] = v0;
    int nu = path(cuckoo, u, us), nv = path(cuckoo, v, vs);
    if (us[nu] = vs[nv]) {
      int min = nu < nv ? nu : nv;
```

```
int len = nu + nv + 1;
    printf("%_4d-cycle_found_at_%d:%d%%\n", len, tp->id, (int)(nonce*100L/ctx.easiness));
    if (len == PROOFSIZE && ctx.nsols < ctx.maxsols)
        solution(ctx, us, nu, vs, nv);
    continue;
}
if (nu < nv) {
    while (nu--)
        CUCKOOSET(us[nu+1], us[nu]);
    CUCKOOSET(u0, v0);
} else {
    while (nv--)
        CUCKOOSET(vs[nv+1], vs[nv]);
    CUCKOOSET(v0, u0);
}
}
pthread_exit(NULL);
}</pre>
```

16 Appendix C: cuckoo_miner.cpp

```
// \  \, \textit{Cuckoo} \  \, \textit{Cycle} \;, \; \; \textit{a} \; \; \textit{memory-hard} \; \; \textit{proof-of-work}
// Copyright (c) 2013-2014 John Tromp
#include "cuckoo_miner.h"
#include <unistd.h>
int main(int argc, char **argv) {
  int nthreads = 1;
  int maxsols = 8;
  int ntrims = 12;
  const char *header = "";
  int c, easipet = 50;
  \mathbf{while} \ ((\, c \ = \ getopt \ (\, argc \, , \ argv \, , \ "e\, : \, h\, : m\, : \, n\, : \, t\, : \, "\,)) \ != \ -1) \ \{
     switch (c) {
       case 'e':
          easipct = atoi(optarg);
          break;
       case 'h':
          header = optarg;
          break;
       case 'm':
          maxsols = atoi(optarg);
          break;
       case 'n':
          ntrims = atoi(optarg);
          break;
       case 't':
          nthreads = atoi(optarg);
          break;
  assert (easipct \geq 0 && easipct \leq 100);
  printf("Looking\_for\_\%d-cycle\_on\_cuckoo\%d(\"\%s\")\_with\_\%d\%\%\_edges\ , \_\%d\_trims\ , \_and\_\%d\_threads\", \\
                  PROOFSIZE, SIZESHIFT, header, easipct, ntrims, nthreads);
  u64 easiness = easipct * SIZE / 100;
  \verb"cuckoo-ctx" ctx(header, easiness", nthreads", ntrims", maxsols");
  thread_ctx *threads = (thread_ctx *)calloc(nthreads, sizeof(thread_ctx));
  assert (threads);
  for (int t = 0; t < nthreads; t++) {
```

```
threads[t].id = t;
    threads[t].ctx = &ctx;
    assert(pthread_create(&threads[t].thread, NULL, worker, (void *)&threads[t]) == 0);
}
for (int t = 0; t < nthreads; t++)
    assert(pthread_join(threads[t].thread, NULL) == 0);
free(threads);
for (unsigned s = 0; s < ctx.nsols; s++) {
    printf("Solution");
    for (int i = 0; i < PROOFSIZE; i++)
        printf("\n", ctx.sols[s][i]);
    printf("\n");
}
return 0;
}</pre>
```