
Bodensee: Version 1.0; Jacques Ambühl; 30 Juillet 2011

■ Directoire opérationnel

```
SetDirectory["~/Mathematica/Bodensee/Operation"]
FileNames[] // TableForm

/Users/jacques/Mathematica/Bodensee/Operation

11072900_905.dat
BodenseeCoord.csv
Bodensee_OP.nb
Polaire.csv
```

Géométrie et navigation

■ Elements géométriques de base

Convention: Longitude: Abscisse $x \rightarrow i \rightarrow \Theta$
 Latitude: Ordonnée $y \rightarrow j \rightarrow \Phi$

```
fleche[{{x1_, y1_}, {x2_, y2_}}] := Module[{L, F},
  L = 0.8 ;
  F = 0.05 ;
  Line[{
    {x1, y1},
    {x1 + L (x2 - x1), y1 + L (y2 - y1)},
    {x1 + L (x2 - x1) - F (y2 - y1), y1 + L (y2 - y1) + F (x2 - x1)},
    {x2, y2},
    {x1 + L (x2 - x1) + F (y2 - y1), y1 + L (y2 - y1) - F (x2 - x1)}, {x1 + L (x2 - x1), y1 + L (y2 - y1)}
  ]]; (* fleche *)
```

```

Horaire[H_] := Module[{HH, MM},
  HH = Floor[H];
  MM = Round[60 (H - HH)];
  "[ "<> ToString[HH] <> "h " <> ToString[MM] <> "mm "]" ;

DMS[x_] := Module[{D, M, , MS, Sec},
  D = Floor[x];
  MS = x - D;
  M = Floor[60 MS];
  Sec = Round[3600 MS - 60 M];
  ToString[M] <> "'";

```

■ Navigation orthodromique

```

Track12[{x1_, y1_}, {x2_, y2_}] := Module[{θ1, φ1, θ2, φ2},
  {θ1, φ1, θ2, φ2} =  $\frac{\pi}{180}$  {x1, y1, x2, y2};
  N[{Cos[φ2] Sin[θ2 - θ1], Cos[φ1] Sin[φ2] - Sin[φ1] Cos[φ2] Cos[θ1 - θ2]}] ] ; (* Track12 *)

Ortho[{x1_, y1_}, {x2_, y2_}] := Module[{θ1, φ1, θ2, φ2},
  {θ1, φ1, θ2, φ2} =  $\frac{\pi}{180}$  {x1, y1, x2, y2};
  (* Km 6371 // NM 3437.75 *)
   $\frac{360}{2\pi} \frac{60}{\text{ArcCos}[N[\text{Cos}[\phi_1] \text{Cos}[\phi_2] \text{Cos}[\theta_1 - \theta_2] + \text{Sin}[\phi_1] \text{Sin}[\phi_2]]]}$  ] ; (* Ortho *)

```

■ Carte du Lac

```

Coast = Import["BodenseeCoord.csv"];
CoastLine = Graphics[{RGBColor[1, 0.5, 0], Line[Coast]}}];
Marker = Graphics[{RGBColor[1, 0.5, 0], Point[Coast[[29]]]}}];

TrameLat = Graphics[Table[{RGBColor[0.95, 0.95, 0.7], Line[{{9, 47.40 + 0.05 i}, {9.8, 47.40 + 0.05 i}}]}, {i, 0, 9}]];
TrameLong = Graphics[Table[{RGBColor[0.95, 0.95, 0.7], Line[{{9.0 + 0.05 i, 47.40}, {9.0 + 0.05 i, 47.85}}]}, {i, 0, 16}]];

TexteCoordonnées[La_, Lo_] := Module[{TexteLat, TexteLong},

  TexteLat = Graphics[Table[{Text[Style[DMS[47.40001 + 0.05 i], Small, Bold, Orange], {Lo, 47.40 + 0.05 i}}]}, {i, 1, 9}]];
  TexteLong = Graphics[Table[{Text[Style[DMS[9.00001 + 0.05 i], Small, Bold, Orange], {9.0 + 0.05 i, La}}]}, {i, 1, 16}]];
  {TexteLong, TexteLat}]; (* TexteCoordonnées *)

Show[TrameLat, TrameLong, TexteCoordonnées[47.4, 9.0], CoastLine, Frame → True, FrameTicks → True]

(*
See=Import["BodenMap.jpg"];
Dimensions[See]
Show[See]
*)

```



Polaire

■ Lecture de la table de base et construction de la fonction Yacht

```
RawPol = Import["Polaire.csv"];

{DV, DA} = Dimensions[RawPol];
{MinW, MaxW, MinA, MaxA} = {RawPol[[2, 1]], RawPol[[DV, 1]], RawPol[[1, 2]], RawPol[[1, DA]]};
{Minr, Maxr} = {1, 7};
RawPolaire = Table[{RawPol[[j, 1]], RawPol[[1, i]], RawPol[[j, i]], {j, 2, DV}, {i, 2, DA}};

MinimumSpeed = 0.001; (* KT *)
Voilier = Interpolation[Flatten[RawPolaire, 1]];
Navigateur = "Marco Stoll";
Yacht[W_, A_] :=
  If[(A < MinA) || (W < MinW), MinimumSpeed,
    If[(W > MaxW), Voilier[MaxW, A],
      Voilier[W, A]]];
```

Champ de vent

■ Lecture du Fichier COSMO-2

```
MarcoField = Import["11072900_905.dat", "Table"];
LatitudeSteps = 12; (* 12 steps in Latitude in Marco's File *)
EchéancesPrévi = 24; (* 24 échéances de prévision *)
LastTabWnd = 337; (* Tête de la dernière table de vent *)
{Nwest, Nnorth} = {First[Dimensions[MarcoField[[1]]]] - 1, LatitudeSteps}
{Mmax, Nmax} = {Nwest, Nnorth}

{31, 12}

{31, 12}

MarcoField[[1, 1]]

2011JUL2900
```

■ Coordonnées de base du champ de vent

```
{δlat, δlong} = {MarcoField[[1, 4]] - MarcoField[[1, 3]], - MarcoField[[4, 1]] + MarcoField[[3, 1]]};
{LongMin, LatMax} = {MarcoField[[1, 2]], MarcoField[[2, 1]]};
{LongMax, LatMin} = {Last[MarcoField[[1]]], MarcoField[[LatitudeSteps + 1, 1]]};

Coordinates = Table[{LongMin + δlong i, LatMax - δlat j}, {j, 0, Nnorth - 1}, {i, 0, Nwest - 1}];
```

■ Construction du champ de vent (20 pas dans le fichier entre chaque échéance !!)

```
WindLenghtFactor = 0.005;
```

```
WindField[ech_] := Module[{ForecastStep, Wls, Wle, W, TZero},
  ForecastStep = 1 + (LatitudeSteps + 2) ech;
  {Wls, Wle} = {ForecastStep, ForecastStep + LatitudeSteps};
  W = Table[MarcoField[[i]], {i, Wls, Wle}];

  {W[[1, 1]], Table[ $\frac{3600}{1852}$  {W[[i, j - 1]], W[[i, j]]}, {i, 2, Nnorth + 1}, {j, 3, 2 Nwest, 2}]}
];
```

Préparation du Graphe

■ Structure et orientation du Graphe

```

GrapheGeneration[{θ1_, ϕ1_}, {θ2_, ϕ2_}, {m_, n_, ρ_}] := Module[{Bornes, Coord, MiLo, MaLo, MiLa, MaLa, CoordLong, CoordLat, e, c, s, M},
  e =  $\sqrt{(\theta_2 - \theta_1)^2 + (\phi_2 - \phi_1)^2}$ ;
  {c, s} =  $\left\{\frac{\theta_2 - \theta_1}{e}, \frac{\phi_2 - \phi_1}{e}\right\}$ ;
  M :=  $\begin{pmatrix} c & -s \\ +s & c \end{pmatrix}$ ;

  Coord = Table[N[M. $\left\{\frac{e}{m}i, \rho \frac{e}{m}j\right\}$  + {θ1, ϕ1}], {i, 0, m}, {j, -n, n}];

  CoordLong = Table[Coord[[k, 1, 1]], {k, 1, m + 1}, {l, 1, 2 n + 1}];
  CoordLat = Table[Coord[[k, 1, 2]], {k, 1, m + 1}, {l, 1, 2 n + 1}];
  {MiLo, MaLo, MiLa, MaLa} = {Min[CoordLong], Max[CoordLong], Min[CoordLat], Max[CoordLat]};
  Bornes =  $\left\{\left\{MiLo - \frac{MaLo - MiLo}{20}, MaLo + \frac{MaLo - MiLo}{20}\right\}, \left\{MiLa - \frac{MaLa - MiLa}{20}, MaLa + \frac{MaLa - MiLa}{20}\right\}\right\}$ ;
  {Coord, Bornes}
]; (* GrapheGeneration *)

```

Interpolation des vitesses de vent aux sommets du graphe

```

BuildWindTable[Ech_] := Module[{Wind, WindInterpolation},

  WindInterpolation[{x_, y_}] := Module[{WindInterpolationFull, Vide, A, MinA, Refi, Refj, Refx, Refy},

    WindInterpolationFull[{xi_, yi_}] :=
      Module[{SquareCoordinates, Void, Csw, Cse, Cne, Cnw, CordSW, CordSE,
        CordNW, CordNE, αZonal, αMeridional, WndSW, WndSE, WndNE, WndNW, WndW, WndE, Boat, grapheWindBoat},

```

```

SquareCoordinates[{xa_, ya_}] := Module[{se, sw, nw, ne, type},
  If[ ((xa ≥ Refx) && (ya ≥ Refy)),
    {type, sw, se, ne, nw} = {"a", {Refi, Refj}, {Refi, Refj + 1}, {Refi - 1, Refj + 1}, {Refi - 1, Refj}},
    If[ ((xa ≥ Refx) && (ya ≤ Refy)), {type, sw, se, ne, nw} = {"b", {Refi + 1, Refj}, {Refi + 1, Refj + 1}, {Refi, Refj + 1}, {Refi, Refj}},
    If[ ((xa ≤ Refx) && (ya ≤ Refy)), {type, sw, se, ne, nw} =
      {"c", {Refi + 1, Refj - 1}, {Refi + 1, Refj}, {Refi, Refj}, {Refi, Refj - 1}}, If[ ((xa ≤ Refx) && (ya ≥ Refy)),
      {type, sw, se, ne, nw} = {"d", {Refi, Refj - 1}, {Refi, Refj}, {Refi - 1, Refj}, {Refi - 1, Refj - 1}}]]];
]; (* End Module SquareCoordinates *)

{Void, Csw, Cse, Cne, Cnw} = SquareCoordinates[{xi, yi}];

CordSW = Coordinates[First[Csw], Last[Csw]]; (* turquoise *)
CordSE = Coordinates[First[Cse], Last[Cse]]; (* bleu *)
CordNE = Coordinates[First[Cne], Last[Cne]]; (* vert *)
CordNW = Coordinates[First[Cnw], Last[Cnw]]; (* rouge *)

{αZonal, αMeridional} = {

$$\frac{xi - First[CordSW]}{First[CordSE] - First[CordSW]}, \frac{yi - Last[CordSE]}{Last[CordNE] - Last[CordSE]}$$

};

WndSW = Wind[First[Csw], Last[Csw]];
WndSE = Wind[First[Cse], Last[Cse]];
WndNE = Wind[First[Cne], Last[Cne]];
WndNW = Wind[First[Cnw], Last[Cnw]];

WndW = αMeridional WndNW + (1 - αMeridional) WndSW;
WndE = αMeridional WndNE + (1 - αMeridional) WndSE;

αZonal WndE + (1 - αZonal) WndW]; (* WindInterpolationFull *)

A = Table[N[Ortho[{x, y}, Coordinates[{i, j}]]], {i, 1, Nmax}, {j, 1, Mmax}];

MinA = Min[A];
{Refi, Refj} = First[Position[A, MinA]];
{Refx, Refy} = Coordinates[{Refi, Refj}];

If[MinA < 0.1 δlat, Wind[{Refi, Refj}], WindInterpolationFull[{x, y}]]
]; (* End Module WindInterpolation *)

Wind = Last[WindField[Ech]];

Table[If[InTruth[{i, j}], WindInterpolation[Locations[{i, j}], {MinimumSpeed, MinimumSpeed}], {i, 1, Maxi}, {j, 1, Maxj}]

```



```
]; (* BuildWindTable *)
```

Présentation Graphique

```
Arbre := Module[{G4, G5},
  G4 = Table[Graphics[{RGBColor[1, 0.7, 0.3], Point[Locations[[i, j]]]}], {i, 1, Maxi}, {j, 1, Maxj}];
  G5 = Table[Graphics[{RGBColor[0.9, 0.7, 0.7], Line[{
    Locations[[First[Analyse[[i, 1, 1]]], Last[Analyse[[i, 1, 1]]]]],
    Locations[[First[Analyse[[i, 1, 2]]], Last[Analyse[[i, 1, 2]]]]]}]}], {i, 1, DimD}];
  {{(*G4,*)G5}}; (* Arbre *)

Isochr[Z_] := Module[{Selec, DimS, Iso, e},
  e = 0.01;
  Selec = Select[Analyse, (#[[2]] < Z) && (Z < #[[3]]) &];
  DimS = First[Dimensions[Selec]];

  Iso[z_, i_] := Module[{a, S1, S2},
    a = 
$$\frac{z - \text{Selec}[[i, 2]]}{\text{Selec}[[i, 3]] - \text{Selec}[[i, 2]]};$$

    S1 = Locations[[First[Selec[[i, 1, 1]]], Last[Selec[[i, 1, 1]]]]];
    S2 = Locations[[First[Selec[[i, 1, 2]]], Last[Selec[[i, 1, 2]]]]];

    (1 - a) S1 + a S2]; (* Iso *)

{Table[Graphics[{RGBColor[1, 0, 0], Point[Iso[Z, i]]}], {i, 1, DimS}], (* Graphics[
  Text[Style[Z, Small, Bold, Red], Iso[Z, 1] - {e, e}]], *)Graphics[Text[Style[Z, Small, Bold, Red], Iso[Z, 1 (* DimS *)] - {e, e}]]}
]; (* Isochr *)
```

```

GrapheFieldStatique[ech_] :=
Module[{ Ech, W3, T1, T2, VerifTime, grapheGrid, grapheWind1, grapheWind2, TitreSimple},

TitreSimple := Module[{TCoord, Texte0, Texte1, Texte2, Texte3, Texte4, Texte5, Texte6, Echeances, DimHeading, S,  $\epsilon$ },
 $\epsilon$  = 0.015;

TCoord = BormesLocations;
Echeances = ToString[CosmoStart] <> " - " <> ToString[CosmoEnd];

Texte1 = Graphics[{Text[Style["Prévision: COSMO-2", Medium, Bold, Blue], {TCoord[[1, 1]] + 5  $\epsilon$ , TCoord[[2, 1]] + 5  $\epsilon$ }}]];
Texte2 =
Graphics[{Text[Style["Echéances: " <> Echeances <> " UTC", Medium, Bold, Blue], {TCoord[[1, 1]] + 5  $\epsilon$ , TCoord[[2, 1]] + 4  $\epsilon$ }}]];
Texte3 = Graphics[{Text[Style["Date: " <> ForecastDay, Medium, Bold, Blue], {TCoord[[1, 1]] + 5  $\epsilon$ , TCoord[[2, 1]] + 3  $\epsilon$ }}]];
Texte4 = Graphics[{Text[Style["©Routage 2011: J. Ambühl", Small, Bold, Blue], {TCoord[[1, 1]] + 5  $\epsilon$ , TCoord[[2, 1]] + 0.45  $\epsilon$ }}]];

{TexteCoordonnées[TCoord[[2, 1]] +  $\epsilon$ , TCoord[[1, 1]] +  $\epsilon$ ], Texte1, Texte2, Texte3, Texte4}];

Ech = Round[ech] - CosmoStart;
W3 = WindField[Ech];
VerifTime = Graphics[{Text[Style[First[W3], Medium, Bold, Blue], {9.68, 47.77}]]];
grapheGrid =
Graphics[{PointSize[0.003], RGBColor[0.4, 0.4, 0.7], Table[Point[Coordinates[[j, i]]], {j, Nmax, 1, -1}, {i, 1, Mmax}]]];

T1 = Table[{Coordinates[[i, j]], Coordinates[[i, j]] + WindLenghtFactor Last[W3][[i, j]]}, {i, 1, Nnorth - 1}, {j, 1, Nwest - 1}];
grapheWind1 = Graphics[{RGBColor[0.2, 0.6, 1], Thickness[0.001], Table[fleche[T1[[i, j]]], {i, 1, Nmax - 1}, {j, 1, Mmax - 1}]]];

T2 = Table[{Locations[[i, j]], Locations[[i, j]] + WindLenghtFactor ContinuousWind[i, j, ech]}, {i, 1, Maxi}, {j, 1, Maxj}];
grapheWind2 = Graphics[{RGBColor[0.4, 0.2, 1], Thickness[0.001], Table[fleche[T2[[i, j]]], {i, 1, Maxi}, {j, 1, Maxj}]]];

Show[TrameLong, TrameLat, CoastLine, TexteCoordonnées[47.4, 9.0],
grapheGrid, grapheWind1, grapheWind2, VerifTime, TitreSimple,
(*Arbre,Isochr[ech],*) Frame → True, PlotRange → BormesLocations]
]; (* GraphFieldStatique *)

```

```

Titres := Module[{TCoord, Texte0, Texte1, Texte2, Texte3, Texte4, Texte5, Texte6, Echeances, DimHeading, S, e},
  e = 0.015;

  TCoord = BormesLocations;
  Echeances = ToString[CosmoStart] <> " - " <> ToString[CosmoEnd];
  Texte0 = Graphics[{Text[Style["Voilier: " <> Navigateur, Medium, Bold, Blue], {TCoord[[1, 1]] + 5 e, TCoord[[2, 1]] + 6 e}]}];
  Texte1 = Graphics[{Text[Style["Prévision: COSMO-2", Medium, Bold, Blue], {TCoord[[1, 1]] + 5 e, TCoord[[2, 1]] + 5 e}]}];
  Texte2 = Graphics[{Text[Style["Echéances: " <> Echeances <> " UTC", Medium, Bold, Blue], {TCoord[[1, 1]] + 5 e, TCoord[[2, 1]] + 4 e}]}];
  Texte3 = Graphics[{Text[Style["Date: " <> ForecastDay, Medium, Bold, Blue], {TCoord[[1, 1]] + 5 e, TCoord[[2, 1]] + 3 e}]}];
  Texte4 = Graphics[{Text[Style["@Routage 2011: J. Ambühl", Small, Bold, Blue], {TCoord[[1, 1]] + 5 e, TCoord[[2, 1]] + 0.45 e}]}];

  DimHeading = First[Dimensions[Heading]];
  Texte5 = Graphics[Table[{Text[Style[Heading[[S, 1, 2]], Small, Bold, Blue], {e, e} + Heading[[S, 1, 1]]}], {S, 1, DimHeading}]];
  Texte6 =
    Graphics[{Text[Style["Départ [GMT]: " <> Horaire[DepartureTime], Medium, Bold, Blue], {TCoord[[1, 1]] + 5 e, TCoord[[2, 1]] + 2 e}]}];

  {TexteCoordonnées[TCoord[[2, 1]] + e, TCoord[[1, 1]] + e], Texte0, Texte1, Texte2, Texte3, Texte4, Texte5, Texte6}];

```

```

GrapheFieldDynamique[IsoStart_] := Module[{Ech, T3, T4, T5, grapheWind3, grapheWind4, grapheDépart, grapheArrivée, grapheRoute, e},

  e = 0.002;
  T3 = Table[{
    Locations[First[Analyse[[i, 1, 1]]], Last[Analyse[[i, 1, 1]]]],
    Locations[First[Analyse[[i, 1, 1]]], Last[Analyse[[i, 1, 1]]]] +
    WindLenghtFactor ContinuousWind[First[Analyse[[i, 1, 1]]], Last[Analyse[[i, 1, 1]]], Analyse[[i, 2]]], {i, 1, DimD}];

  grapheWind3 = Graphics[{RGBColor[0.7, 0.7, 1], Thickness[0.001], Table[fleche[T3[[i]]], {i, 1, DimD}]}];

  T4 = Table[{
    Locations[First[Analyse[[i, 1, 2]]], Last[Analyse[[i, 1, 2]]]],
    Locations[First[Analyse[[i, 1, 2]]], Last[Analyse[[i, 1, 2]]]] +
    WindLenghtFactor ContinuousWind[First[Analyse[[i, 1, 2]]], Last[Analyse[[i, 1, 2]]], Analyse[[i, 3]]], {i, 1, DimD}];

  grapheWind4 = Graphics[{RGBColor[0.7, 0.7, 1], Thickness[0.001], Table[fleche[T4[[i]]], {i, 1, DimD}]}];

  T5 =
    Table[{Locations[Route[[i + 1, 1]], Route[[i + 1, 2]]], Locations[Route[[i, 1]], Route[[i, 2]]]}, {i, 1, GraphAttributes[[1]]}];

  grapheRoute = Graphics[{RGBColor[0.0, 0.0, 1], Thickness[0.003], Table[fleche[T5[[j]]], {j, 1, GraphAttributes[[1]]}]}];

  grapheDépart = Graphics[{Blue, Rectangle[DepartureLocation - {e, e}, DepartureLocation + {e, e}]}];
  grapheArrivée = Graphics[{Blue, Rectangle[ArrivalLocation - {e, e}, ArrivalLocation + {e, e}]}];

  Show[TrameLong, TrameLat, CoastLine, Arbre,
    grapheWind3, grapheWind4, grapheRoute, grapheDépart, grapheArrivée,
    Isochr[Ceiling[IsoStart] + 0],
    Isochr[Ceiling[IsoStart] + 1],
    Isochr[Ceiling[IsoStart] + 2],
    Isochr[Ceiling[IsoStart] + 3],
    Isochr[Ceiling[IsoStart] + 4],
    Titres, PlotRange -> BormesLocations, Frame -> True, FrameTicks -> None]

];(* GrapheFieldDynamique *)

```

Algorithme de décision: programmation dynamique

■ Préparation

```
TimeTuning := Module[{FDay, HS, HE, DS, DE, CE},

  (* Time settings *)

  FDay = StringDrop[MarcoField[[1, 1]], -2];

  HS = ToExpression[StringDrop[MarcoField[[1, 1]], 9]]; (* Tête de la première table de vents *)
  HE = ToExpression[StringDrop[MarcoField[[LastTabWnd, 1]], 9]]; (* Tête de la dernière table de vents *)

  DS = ToExpression[StringTake[MarcoField[[1, 1]], {8, 9}]];
  DE = ToExpression[StringTake[MarcoField[[267, 1]], {8, 9}]];

  {FDay, HS, HS + EchéancesPrévi}}; (* 24 Echéances de prévision, Timestep 1 h. *)

TimeTuning

{2011JUL29, 0, 24}

ContinuousWind[i_, j_, t_] := Module[{Ech, δEch, WindAnte, WindPost},
  If[(t < CosmoStart) || (CosmoEnd < t), {MinimumSpeed, MinimumSpeed}, (* vérifier !! *)
    Ech = IntegerPart[t] - CosmoStart;
    δEch = t - (Ech + CosmoStart);
    WindAnte = WindinTime[[Ech + 1, i, j]];
    WindPost = WindinTime[[Ech + 2, i, j]];
    (1 - δEch) WindAnte + δEch WindPost]
];
```

■ Calcul direct des options possibles

```
ProgrammationDynamique[Start_, Time_, Spread_] := Module[{Graphe, DimGraphe, Duration, ProgrDyn, G0, G1, DimG1, G2, G3, G4},

  Duration[i1_, j1_, i2_, j2_] :=
    Module[{t1, t2, Lx, Ly, Compute, FixPoint, Route}, {Lx, Ly} = Track12[Locations[[i1, j1]], Locations[[i2, j2]]];

    {t1, t2} = {Graphe[[i1, j1, 3]], Graphe[[i2, j2, 3]]};

    Compute[t1_, t2_] := Module[{Wu, Wv, WSpeedArrival, AllureArrival, WSpeedStart, AllureStart, YArrival, YStart, Leg},
```

```

{Wu, Wv} = ContinuousWind[i1, j1, tt1];
WSpeedStart =  $\sqrt{Wu^2 + Wv^2}$ ;

AllureStart =  $180 \left( 1 - \frac{1}{\pi} \text{ArcCos} \left[ \frac{\{Wu, Wv\} \cdot \{Lx, Ly\}}{WSpeedStart \sqrt{Lx^2 + Ly^2}} \right] \right)$ ;

YStart = Yacht[WSpeedStart, AllureStart];

{Wu, Wv} = ContinuousWind[i2, j2, tt2];
WSpeedArrival =  $\sqrt{Wu^2 + Wv^2}$ ;

AllureArrival =  $180 \left( 1 - \frac{1}{\pi} \text{ArcCos} \left[ \frac{\{Wu, Wv\} \cdot \{Lx, Ly\}}{WSpeedArrival \sqrt{Lx^2 + Ly^2}} \right] \right)$ ;

YArrival = Yacht[WSpeedArrival, AllureArrival];

Leg = {
  (WSpeedStart + WSpeedArrival) / 2,
  (AllureStart + AllureArrival) / 2,
  (YStart + YArrival) / 2};

(*
If[RandomInteger[{1,10000}]>9950,
  Print[" " Cap du Vent: ",(CapVentStart+CapVentArrival)/2,
    " Vitesse du vent: ",(WSpeedStart+WSpeedArrival)/2,
    " Allure: ",(AllureStart+AllureArrival)/2,
    " Vitesse du voilier: ",(YStart+YArrival)/2]];
*)

{
 $\frac{2 \text{Ortho}[\text{Locations}[[i1, j1]], \text{Locations}[[i2, j2]]]}{YStart + YArrival}$ , Leg}
]; (* Compute *)

(*
FixPoint[t_]:=Module[{D0,D1,DD1,D2,ϵ},
  D0=Compute[t,t];

```

```

Do[ { D1=Compute[t,t+D0];
      ε= 0.01D1;
      DD1=
$$\frac{\text{Compute}[t,t+D1+\epsilon]-\text{Compute}[t,t+D1-\epsilon]}{2\epsilon};$$

      D2=D0-
$$\frac{D1-D0}{DD1-1};$$

      D0=D2},
  {i,1,2}];D2];

FixPoint[t1]
*)

Compute[t1, t1 + First[Compute[t1, t1 + First[Compute[t1, t1]]]] ] ]

]; (* Duration *)

ProgrDyn[r_] := Module[{Etabli, Posi, Wahl, MinEtabli},

  Do[
    Wahl = Table[Duration[r-1, j, r, k], {j, 1, Maxj}];
    Etabli = Table[Graphe[[r-1, j, 3]] + First[Wahl[[j]]], {j, 1, Maxj}];
    MinEtabli = Min[Etabli];
    {{Posi}} = Position[Etabli, MinEtabli];

    If[Abs[k - Posi] ≤ Spread, Graphe[[r, k]] =
      {{ {r-1, Posi}, {r, k}}, Graphe[[r-1, Posi, 3]], MinEtabli, Last[Wahl[[Posi]]] }},
      {k, 1, Maxj}]

  ]; (* ProgrDyn *)

Graphe = Table[{0, 0, 106, 106}, {i, 1, Maxi}, {j, 1, Maxj}];
Graphe[[1, Start]] = {1, 0, Time};

Do[ProgrDyn[r], {r, 2, Maxi}];

G0 = Table[Drop[Graphe[[i, j]], -1], {i, 1, Maxi}, {j, 1, Maxj}];
G1 = Select[Flatten[Transpose[G0], 1], (Last[#] < 1000 000) && (Last[#] > Time) &];
DimG1 = First[Dimensions[G1]];

G2 = Table[First[G1[[i]]], {i, 1, DimG1}];
G3 = Table[{First[G2[[i]]][[1]], First[G2[[i]]][[2]]}, {Last[G2[[i]]][[1]], Last[G2[[i]]][[2]]}, {i, 1, DimG1}];
G4 = Table[{G3[[i]], G1[[i, 2]], G1[[i, 3]]}, {i, 1, DimG1}];

```

```

{Graphe, G4 }

```

```

]; (* Programmation Dynamique *)

```

■ Calcul rétrograde de l'option choisie et rédaction du logbook

```

WohinDesWegs := Module[{Vorgänger, Weg, nn, LB},
  Vorgänger[{i_, j_}] := Réseau[{i, j, 1, 1}];
  Weg = {ArrivalPoint};
  nn = Maxi - 1; While[nn ≥ 1, Weg = Append[Weg, Vorgänger[Last[Weg]]]; nn--];
  LB = Table[{i, Réseau[Weg[{i, 1}], Weg[{i, 2}]]], {i, 1, Maxi - 1}];
  {Weg, LB}
]; (* CalculRoute *)

LogBook := Module[{LB},

  LB[S_] := Module[{ALong, ALat, BLong, BLat, LocLong, LocLat, ButLong, ButLat, DMS, Komp, Kompass, Heure, Flottheit},

    DMS[x_] := Module[{D, M, , MS, Sec},
      D = Floor[x];
      MS = x - D;
      M = Floor[60 MS];
      Sec = Round[3600 MS - 60 M];
      "[ "<> ToString[D] <> "° " <> ToString[M] <> "m " <> ToString[Sec] <> "s ]";

    Heure = Logbuch[{S, 2, 2}];
    {ALong, ALat} = Logbuch[{S, 2, 1, 1}];
    {BLong, BLat} = Logbuch[{S, 2, 1, 2}];
    {LocLong, LocLat} = Locations[{ALong, ALat}];
    {ButLong, ButLat} = Locations[{BLong, BLat}];
    Komp = ToString[Round[GeoDirection[{LocLat, LocLong}, {ButLat, ButLong}]]];
    Kompass = "[ Kompass: " <> Komp <> "° ]";
    Flottheit = "[ Speed: " <> ToString[Logbuch[{S, 2, 4, 3}]] <> " Kt ]";
    {{LocLong, LocLat}, Komp}, {Horaire[Heure], DMS[LocLat], DMS[LocLong], Kompass, Flottheit}}
  ]; (* LB *)

  {
    Table[{First[LB[Maxi - i]], {i, 1, Maxi - 1}}, Table[{i, Last[LB[Maxi - i]], {i, 1, Maxi - 1}}]
  }
]; (* LogBook *)

```


Action

■ Initialisation et construction du graphe

```

Bregenz = N[{FromDMS[{9, 44, 57}], FromDMS[{47, 30, 18}]}];
Konstanz = N[{FromDMS[{9, 11, 00}], FromDMS[{47, 39, 48}]}];
Start = N[{FromDMS[{9, 36, 00}], FromDMS[{47, 30, 00}]}];
Arrival = N[{FromDMS[{9, 21, 00}], FromDMS[{47, 39, 00}]}];

AncreArr = Arrival; (* Ancre de départ: Longitude, Latitude *)
AncreDep = Start; (* Ancre d'arrivée: Longitude, Latitude *)
GraphAttributes = {16, 6, 0.25}; (* # Pas, # Options, Ratio  $\delta$  Options /  $\delta$  Pas *)

{Locations, BormesLocations} = GrapheGeneration[AncreDep, AncreArr, GraphAttributes];
{Maxi, Maxj, v} = Dimensions[Locations];

DeparturePoint = {1, 6}; (* #, # *)
ArrivalPoint = {Maxi, 4}; (* #, # *)

{DepartureLocation, ArrivalLocation} =
  {Locations[[DeparturePoint[[1]], DeparturePoint[[2]]]], Locations[[ArrivalPoint[[1]], ArrivalPoint[[2]]]]};
InDomain[{ $\theta$ _,  $\phi$ _}] := (LongMin +  $\delta$ long  $\leq$   $\theta$ ) && ( $\theta \leq$  LongMax -  $\delta$ long) && (LatMin +  $\delta$ lat  $\leq$   $\phi$ ) && ( $\phi \leq$  LatMax -  $\delta$ lat);
InTruth = Table[InDomain[Locations[[i, j]]], {i, 1, Maxi}, {j, 1, Maxj}];

{ForecastDay, CosmoStart, CosmoEnd} = TimeTuning; (* String, GMT, GMT *)
{Spread, DepartureTime} = {3, 12.20}; (* #, CosmoStart < GMT < CosmoEnd *)

```

■ Construction de la matrices des champs de vent sur le graphe

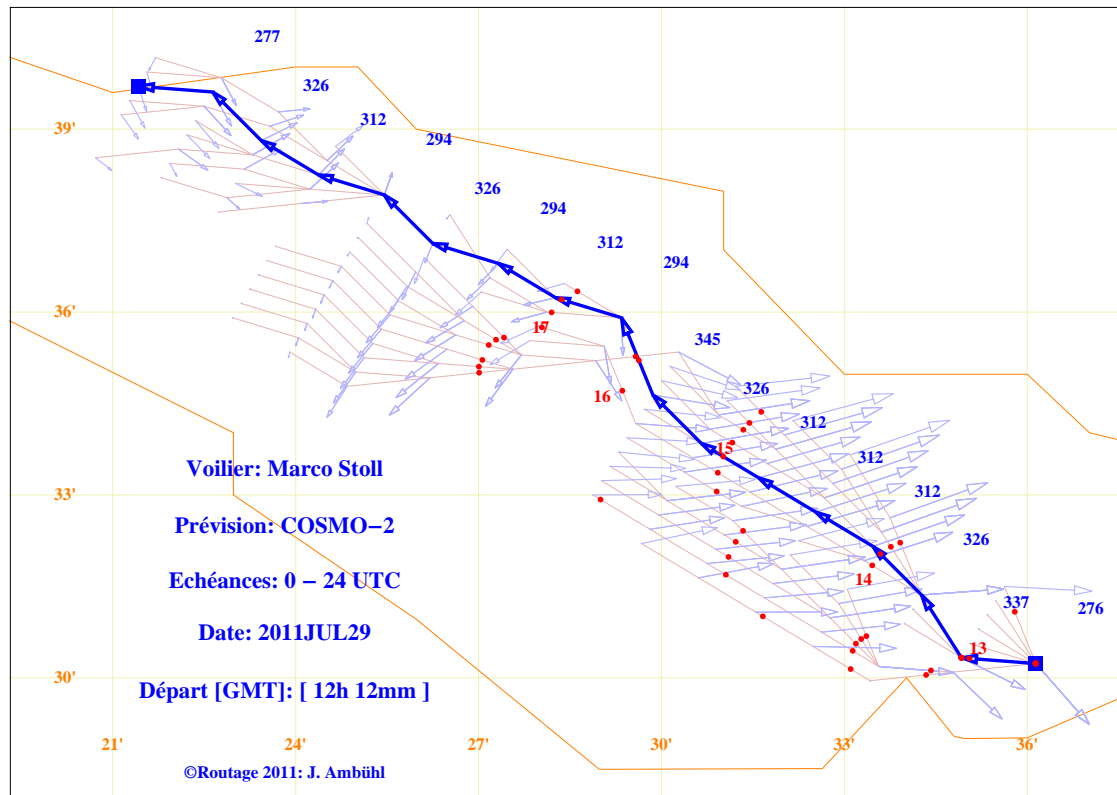
```

WindinTime = Table[BuildWindTable[Ech], {Ech, 0, 24}];

```

■ Décision: construction de l'arbre des options et choix de la route; présentations graphiques

```
(* Calcul direct *)
{Réseau, Analyse} = ProgrammationDynamique[DeparturePoint[[2]], DepartureTime, Spread];
DimD = First[Dimensions[Analyse]];
(* Calcul rétrograde *)
{Route, Logbuch} = WohinDesWegs;
{Heading, Book} = LogBook;
(* Présentation graphique*)
GrapheFieldDynamique[DepartureTime]
(*Impression du logbook*)
Print[Book];
```



```

{{1, {[ 12h 12mm ], [ 47° 30m 14s ], [ 9° 36m 8s ], [ Kompass: 276° ], [ Speed: 0.928207 Kt ]}},
{2, {[ 13h 6mm ], [ 47° 30m 20s ], [ 9° 34m 55s ], [ Kompass: 337° ], [ Speed: 1.97055 Kt ]}},
{3, {[ 13h 40mm ], [ 47° 31m 22s ], [ 9° 34m 16s ], [ Kompass: 326° ], [ Speed: 2.40628 Kt ]}},
{4, {[ 14h 4mm ], [ 47° 32m 9s ], [ 9° 33m 28s ], [ Kompass: 312° ], [ Speed: 2.42695 Kt ]}},
{5, {[ 14h 25mm ], [ 47° 32m 43s ], [ 9° 32m 32s ], [ Kompass: 312° ], [ Speed: 2.37224 Kt ]}},
{6, {[ 14h 46mm ], [ 47° 33m 17s ], [ 9° 31m 36s ], [ Kompass: 312° ], [ Speed: 2.25754 Kt ]}},
{7, {[ 15h 9mm ], [ 47° 33m 51s ], [ 9° 30m 39s ], [ Kompass: 326° ], [ Speed: 2.1379 Kt ]}},
{8, {[ 15h 36mm ], [ 47° 34m 38s ], [ 9° 29m 52s ], [ Kompass: 345° ], [ Speed: 1.43988 Kt ]}},
{9, {[ 16h 30mm ], [ 47° 35m 54s ], [ 9° 29m 21s ], [ Kompass: 294° ], [ Speed: 1.46715 Kt ]}},
{10, {[ 17h 3mm ], [ 47° 36m 14s ], [ 9° 28m 16s ], [ Kompass: 312° ], [ Speed: 1.52018 Kt ]}},
{11, {[ 17h 36mm ], [ 47° 36m 48s ], [ 9° 27m 20s ], [ Kompass: 294° ], [ Speed: 1.38088 Kt ]}},
{12, {[ 18h 11mm ], [ 47° 37m 7s ], [ 9° 26m 15s ], [ Kompass: 326° ], [ Speed: 1.15438 Kt ]}},
{13, {[ 19h 1mm ], [ 47° 37m 55s ], [ 9° 25m 27s ], [ Kompass: 294° ], [ Speed: 1.4016 Kt ]}},
{14, {[ 19h 35mm ], [ 47° 38m 15s ], [ 9° 24m 22s ], [ Kompass: 312° ], [ Speed: 1.56249 Kt ]}},
{15, {[ 20h 7mm ], [ 47° 38m 49s ], [ 9° 23m 26s ], [ Kompass: 326° ], [ Speed: 0.820925 Kt ]}},
{16, {[ 21h 18mm ], [ 47° 39m 37s ], [ 9° 22m 38s ], [ Kompass: 277° ], [ Speed: 1.28654 Kt ]}}

```

GrapheFieldStatique[CosmoStart + 22.05]

