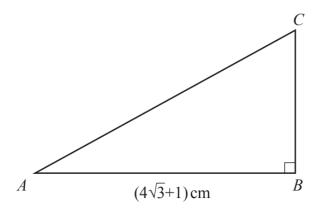


ADDITIONAL MATHEMATICS INDICES and SURDS

0606/11

Nov 2015 P13 - Qu 4

You are not allowed to use a calculator in this question.



The diagram shows triangle ABC with side $AB = (4\sqrt{3} + 1)$ cm. Angle B is a right angle. It is given that the area of this triangle is $\frac{47}{2}$ cm².

- (i) Find the length of the side BC in the form $(a\sqrt{3} + b)$ cm, where a and b are integers. [3]
- (ii) Hence find the length of the side AC in the form $p\sqrt{2}$ cm, where p is an integer. [2]

Nov 2015 P13 - Qu 12

(a) Given that $2^{2x-1} \times 4^{x+y} = 128$ and $\frac{9^{2y-x}}{27^{y-4}} = 1$, find the value of each of the integers x and y. [4]

(b) Solve
$$2(5)^{2z} + 5^z - 1 = 0$$
. [4]

Nov 2015 P23 - Qu 4

Solve the following simultaneous equations, giving your answers for both x and y in the form $a + b\sqrt{3}$, where a and b are integers.

$$2x + y = 9$$

$$\sqrt{3}x + 2y = 5$$
[5]



ADDITIONAL MATHEMATICS QUADRATICS

0606/11

Nov 2015 P11 - Qu 1

Find the range of values of k for which the equation $kx^2 + k = 8x - 2xk$ has 2 real distinct roots. [4]

Nov 2015 P13 - Qu 11

The line x-y+2=0 intersects the curve $2x^2-y^2+2x+1=0$ at the points A and B. The perpendicular bisector of the line AB intersects the curve at the points C and D. Find the length of the line CD in the form $a\sqrt{5}$, where a is an integer. [10]

Nov 2015 P23 - Qu 2

Find the values of k for which the line y = 2x + k + 2 cuts the curve $y = 2x^2 + (k+2)x + 8$ in two distinct points.

Nov 2015 P23 - Qu 2

Given that $f(x) = 3x^2 + 12x + 2$,

(i) find values of a, b and c such that
$$f(x) = a(x+b)^2 + c$$
, [3]

(ii) state the minimum value of
$$f(x)$$
 and the value of x at which it occurs, [2]

(iii) solve
$$f\left(\frac{1}{y}\right) = 0$$
, giving each answer for y correct to 2 decimal places. [3]



ADDITIONAL MATHEMATICS REMAINDER THEOREM

0606/11

Nov 2015 P21 - Qu 1

It is given that $f(x) = 4x^3 - 4x^2 - 15x + 18$.

(i) Show that
$$x + 2$$
 is a factor of $f(x)$. [1]

(ii) Hence factorise
$$f(x)$$
 completely and solve the equation $f(x) = 0$. [4]

Nov 2015 P23 - Qu 5

The roots of the equation $x^3 + ax^2 + bx + c = 0$ are 1, 3 and 3. Show that c = -9 and find the value of a and of b.



ADDITIONAL MATHEMATICS

0606/11

SETS

Nov 2015 P11 - Qu 6

It is given that $\mathscr{E} = \{x : 1 \le x \le 12, \text{ where } x \text{ is an integer} \}$ and that sets A, B, C and D are such that $A = \{\text{multiples of } 3\},$ $B = \{\text{prime numbers}\},$ $C = \{\text{odd integers}\},$ $D = \{\text{even integers}\}.$

Write down the following sets in terms of their elements.

(i)	$A \cap B$	[1]
(ii)	$A \cup C$	[1]
(iii)	$A'\cap C$	[1]
(iv)	$(D \cup B)^{'}$	[1]
(v)	Write down a set E such that $E \subset D$.	[1]

On the Venn diagrams below, shade the regions indicated.

(i) & A

 $A \cap (B \cup C)$

[1]

(ii) \mathcal{E} $A \cup (B \cap C)$

[1]

 $(A \cup B)' \cap C$

[1]



ADDITIONAL MATHEMATICS BINOMIAL THEOREM

0606/11

Nov 2015 P13 - Qu 8

- (a) Given that the first 4 terms in the expansion of $(2 + kx)^8$ are $256 + 256x + px^2 + qx^3$, find the value of k, of p and of q. [3]
- **(b)** Find the term that is independent of x in the expansion of $\left(x \frac{2}{x^2}\right)^9$. [3]

Nov 2015 P21 - Qu 2

- (i) Find, in the simplest form, the first 3 terms of the expansion of $(2-3x)^6$, in ascending powers of x. [3]
- (ii) Find the coefficient of x^2 in the expansion of $(1+2x)(2-3x)^6$. [2]

ADDITIONAL MATHEMATICS CALCULUS

0606/11

Nov 2015 P11 - Qu 2

A curve, showing the relationship between two variables x and y, passes through the point P(-1,3).

The curve has a gradient of 2 at *P*. Given that
$$\frac{d^2y}{dx^2} = -5$$
, find the equation of the curve. [4]

Nov 2015 P11 - Qu 5

Variables x and y are such that $y = (x-3)\ln(2x^2+1)$.

(i) Find the value of
$$\frac{dy}{dx}$$
 when $x = 2$. [4]

(ii) Hence find the approximate change in y when x changes from 2 to 2.03. [2]

Nov 2015 P11 - Qu 8

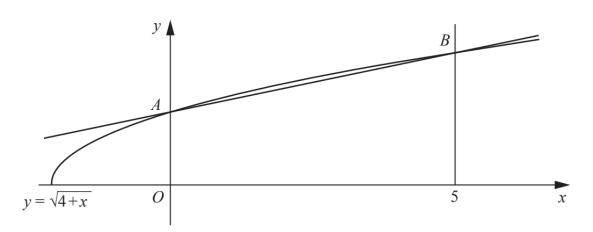
Find the equation of the tangent to the curve
$$y = \frac{2x-1}{\sqrt{x^2+5}}$$
 at the point where $x = 2$. [7]

Nov 2015 P11 - Qu 9

You are not allowed to use a calculator in this question.

(i) Find
$$\int \sqrt{4+x} \, dx$$
. [2]

(ii)



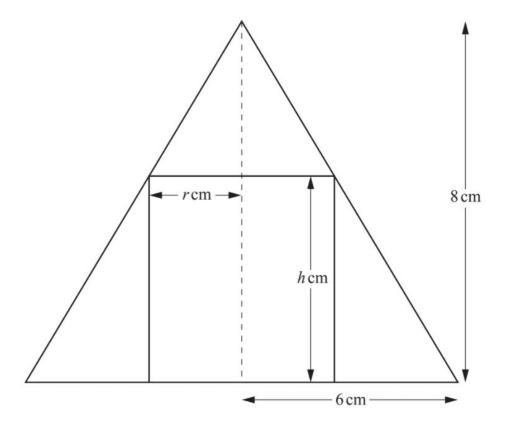
The diagram shows the graph of $y = \sqrt{4 + x}$, which meets the y-axis at the point A and the line x = 5 at the point B. Using your answer to part (i), find the area of the region enclosed by the curve and the straight line AB.

Find the equation of the normal to the curve $y = 5 \tan x - 3$ at the point where $x = \frac{\pi}{4}$. [5]

Nov 2015 P13 - Qu 7

A curve, showing the relationship between two variables x and y, is such that $\frac{d^2y}{dx^2} = 6\cos 3x$. Given that the curve has a gradient of $4\sqrt{3}$ at the point $\left(\frac{\pi}{9}, -\frac{1}{3}\right)$, find the equation of the curve. [6]

Nov 2015 P21 - Qu 7



A cone, of height 8 cm and base radius 6 cm, is placed over a cylinder of radius r cm and height h cm and is in contact with the cylinder along the cylinder's upper rim. The arrangement is symmetrical and the diagram shows a vertical cross-section through the vertex of the cone.

- (i) Use similar triangles to express h in terms of r. [2]
- (ii) Hence show that the volume, $V \text{ cm}^3$, of the cylinder is given by $V = 8\pi r^2 \frac{4}{3}\pi r^3$. [1]
- (iii) Given that r can vary, find the value of r which gives a stationary value of V. Find this stationary value of V in terms of π and determine its nature. [6]

Nov 2015 P23 - Qu 1

Find the equation of the tangent to the curve $y = x^3 + 3x^2 - 5x - 7$ at the point where x = 2. [5]

Nov 2015 P23 - Qu 3

(a) Given that
$$y = \frac{x^3}{2 - x^2}$$
, find $\frac{dy}{dx}$. [3]

(b) Given that
$$y = x\sqrt{4x+6}$$
, show that $\frac{dy}{dx} = \frac{k(x+1)}{\sqrt{4x+6}}$ and state the value of k . [3]

Nov 2015 P23 - Qu 10

(i) Given that
$$\frac{d}{dx}(e^{2-x^2}) = kxe^{2-x^2}$$
, state the value of k . [1]

(ii) Using your result from part (i), find
$$\int 3xe^{2-x^2}dx$$
. [2]

(iii) Hence find the area enclosed by the curve
$$y = 3xe^{2-x^2}$$
, the x-axis and the lines $x = 1$ and $x = \sqrt{2}$. [2]

(iv) Find the coordinates of the stationary points on the curve
$$y = 3xe^{2-x^2}$$
. [4]



ADDITIONAL MATHEMATICS COORDINATE GEOMETRY

0606/11

Nov 2015 P11 - Qu 12

The line 2x - y + 1 = 0 meets the curve $x^2 + 3y = 19$ at the points A and B. The perpendicular bisector of the line AB meets the x-axis at the point C. Find the area of the triangle ABC.

Nov 2015 P21 - Qu 8

Solutions to this question by accurate drawing will not be accepted.

Two points A and B have coordinates (-3, 2) and (9, 8) respectively.

- (i) Find the coordinates of C, the point where the line AB cuts the y-axis. [3]
- (ii) Find the coordinates of D, the mid-point of AB. [1]
- (iii) Find the equation of the perpendicular bisector of AB. [2]

The perpendicular bisector of AB cuts the y-axis at the point E.

- (iv) Find the coordinates of E. [1]
- (v) Show that the area of triangle ABE is four times the area of triangle ECD. [3]



ADDITIONAL MATHEMATICS EXPONENTIALS and LOGARITHMS

0606/11

Nov 2015 P11 - Qu 7

Two variables, x and y, are such that $y = Ax^b$, where A and b are constants. When $\ln y$ is plotted against $\ln x$, a straight line graph is obtained which passes through the points (1.4, 5.8) and (2.2, 6.0).

- (i) Find the value of A and of b. [4]
- (ii) Calculate the value of y when x = 5. [2]

Nov 2015 P21 - Qu 5

(a) Solve the following equations to find p and q.

$$8^{q-1} \times 2^{2p+1} = 4^7$$

$$9^{p-4} \times 3^q = 81$$
[4]

(b) Solve the equation
$$\lg(3x-2) + \lg(x+1) = 2 - \lg 2$$
. [5]

Nov 2015 P23 - Qu 6

Solve the following equation.

$$\log_2(29x - 15) = 3 + \frac{2}{\log_x 2}$$
 [5]

The trees in a certain forest are dying because of an unknown virus.

The number of trees, N, surviving t years after the onset of the virus is shown in the table below.

t	1	2	3	4	5	6
N	2000	1300	890	590	395	260

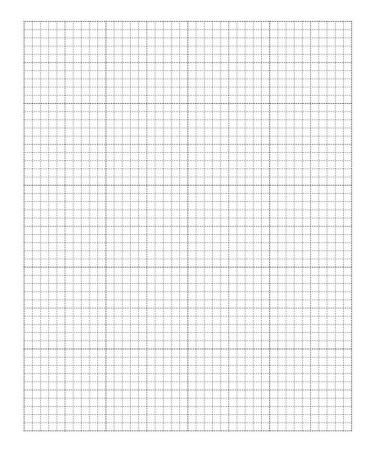
The relationship between N and t is thought to be of the form $N = Ab^{-t}$.

(i) Transform this relationship into straight line form.

[1]

(ii) Using the given data, draw this straight line on the grid below.

[3]



(iii) Use your graph to estimate the value of A and of b.

[3]

If the trees continue to die in the same way, find

(iv) the number of trees surviving after 10 years,

[1]

(v) the number of years taken until there are only 10 trees surviving.

[2]

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ADDITIONAL MATHEMATICS FUNCTIONS (incl MODULUS FUNCTIONS)

0606/11

Nov 2015 P11 - Qu 11

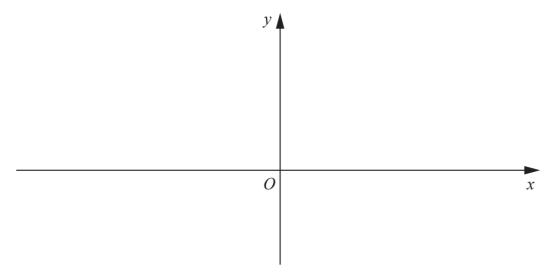
- (a) A function f is such that $f(x) = x^2 + 6x + 4$ for $x \ge 0$.
 - (i) Show that $x^2 + 6x + 4$ can be written in the form $(x + a)^2 + b$, where a and b are integers. [2]
 - (ii) Write down the range of f. [1]
 - (iii) Find f^{-1} and state its domain. [3]
- **(b)** Functions g and h are such that, for $x \in \mathbb{R}$,

$$g(x) = e^x$$
 and $h(x) = 5x + 2$.

Solve
$$h^2g(x) = 37$$
. [4]

Nov 2015 P13 - Qu 6

(i) On the axes below, sketch the graph of $y = |x^2 - 4x - 12|$ showing the coordinates of the points where the graph meets the axes. [3]



- (ii) Find the coordinates of the stationary point on the curve $y = |x^2 4x 12|$. [2]
- (iii) Find the values of k such that the equation $|x^2 4x 12| = k$ has only 2 solutions. [2]



ADDITIONAL MATHEMATICS KINEMATICS

0606/11

Nov 2013 P21 - Qu 10

A particle is moving in a straight line such that its velocity, $v \,\text{ms}^{-1}$, t seconds after passing a fixed point O is $v = e^{2t} - 6e^{-2t} - 1$.

- (i) Find an expression for the displacement, s m, from O of the particle after t seconds. [3]
- (ii) Using the substitution $u = e^{2t}$, or otherwise, find the time when the particle is at rest. [3]
- (iii) Find the acceleration at this time. [2]

Nov 2013 P23 - Qu 7

The velocity, $v \text{ ms}^{-1}$, of a particle travelling in a straight line, t seconds after passing through a fixed point O, is given by $v = \frac{10}{(2+t)^2}$.

- (i) Find the acceleration of the particle when t = 3.
- (ii) Explain why the particle never comes to rest. [1]
- (iii) Find an expression for the displacement of the particle from O after time ts. [3]
- (iv) Find the distance travelled by the particle between t = 3 and t = 8. [2]

ADDITIONAL MATHEMATICS MATRICES

0606/11

Nov 2015 P13 - Qu 3

(a) Matrices **A** and **B** are such that
$$\mathbf{A} = \begin{bmatrix} 2 & 1 \\ 4 & 3 \end{bmatrix}$$
 and $\mathbf{B} = \begin{bmatrix} 3 & 8 & 1 \\ 6 & 0 & 2 \end{bmatrix}$. Find \mathbf{AB} .

- (b) Given that matrix $\mathbf{X} = \begin{pmatrix} 4 & 6 \\ 2 & -8 \end{pmatrix}$, find the integer value of m and of n such that $\mathbf{X}^2 = m\mathbf{X} + n\mathbf{I}$, where \mathbf{I} is the identity matrix. [5]
- (c) Given that matrix $\mathbf{Y} = \begin{pmatrix} a & 2 \\ 3 & a \end{pmatrix}$, find the values of a for which det $\mathbf{Y} = 0$. [2]

Nov 2015 P21 - Qu 4

(a) Given that
$$\mathbf{A} = \begin{pmatrix} 2 & -1 \\ 3 & 5 \\ 7 & 4 \end{pmatrix}$$
 and $\mathbf{B} = \begin{pmatrix} 1 & -2 & 4 \\ -2 & 3 & 0 \end{pmatrix}$, calculate **2BA**. [3]

(b) The matrices **C** and **D** are given by $\mathbf{C} = \begin{pmatrix} 1 & 2 \\ -1 & 6 \end{pmatrix}$ and $\mathbf{D} = \begin{pmatrix} 3 & -2 \\ 1 & 4 \end{pmatrix}$.

(i) Find
$$C^{-1}$$
. [2]

(ii) Hence find the matrix \mathbf{X} such that $\mathbf{CX} + \mathbf{D} = \mathbf{I}$, where \mathbf{I} is the identity matrix. [3]



ADDITIONAL MATHEMATICS PERMUTATIONS and COMBINATIONS

0606/11

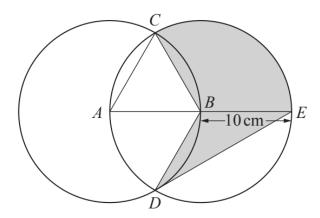
NOV	2015	PTI - Qu 4				
(a)	a) 6 books are to be chosen from 8 different books.					
	(i)	Find the number of different selections of 6 books that could be made.	[1]			
	A clock is to be displayed on a shelf with 3 of the 8 different books on each side of it. Fin number of ways this can be done if					
	(ii)	there are no restrictions on the choice of books,	[1]			
	(iii)	3 of the 8 books are music books which have to be kept together.	[2]			
(b)	(b) A team of 6 tennis players is to be chosen from 10 tennis players consisting of 7 men and 3 women. Find the number of different teams that could be chosen if the team must include least 1 woman.					
Nov	2015	P13 - Qu 9				
(a)	Five different books are to be arranged on a shelf. There are 2 Mathematics books and 3 Histo books. Find the number of different arrangements of books if					
	(i)	the Mathematics books are next to each other,	[2]			
	(ii)	the Mathematics books are not next to each other.	[2]			
(b)	b) To compete in a quiz, a team of 5 is to be chosen from a group of 9 men and 6 women. Fin number of different teams that can be chosen if					
	(i)	there are no restrictions,	[1]			
	(ii)	at least two men must be on the team.	[3]			



ADDITIONAL MATHEMATICS RADIAN MEASURE

0606/11

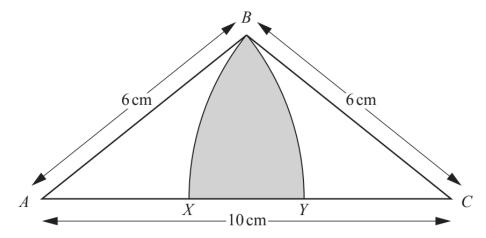
Nov 2015 P11 - Qu 10



The diagram shows two circles, centres A and B, each of radius 10 cm. The point B lies on the circumference of the circle with centre A. The two circles intersect at the points C and D. The point E lies on the circumference of the circle centre B such that ABE is a diameter.

- (i) Explain why triangle ABC is equilateral. [1] (ii) Write down, in terms of π , angle CBE. [1]
- (iii) Find the perimeter of the shaded region. [5]
- (iv) Find the area of the shaded region. [3]

Nov 2015 P13 - Qu 10



The diagram shows an isosceles triangle ABC such that AC = 10 cm and AB = BC = 6 cm. BX is an arc of a circle, centre C, and BY is an arc of a circle, centre A.

- (i) Show that angle ABC = 1.970 radians, correct to 3 decimal places. [2]
- (ii) Find the perimeter of the shaded region. [4]
- (iii) Find the area of the shaded region. [3]

ADDITIONAL MATHEMATICS TRIGONOMETRY

0606/11

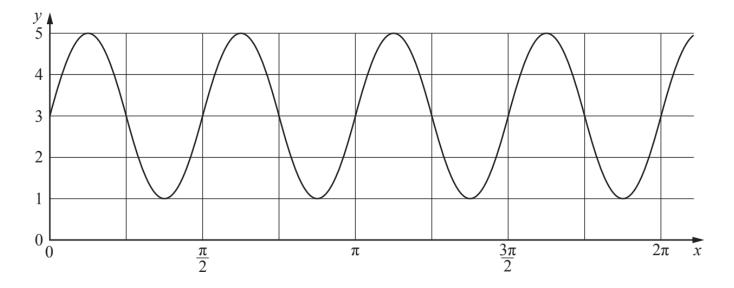
Nov 2015 P11 - Qu 3

Show that
$$\sqrt{\sec^2 \theta - 1} + \sqrt{\csc^2 \theta - 1} = \sec \theta \csc \theta$$
. [5]

Nov 2015 P13 - Qu 2

Solve
$$2\cos^2(3x - \frac{\pi}{4}) = 1$$
 for $0 \le x \le \frac{\pi}{3}$. [4]

Nov 2015 P21 - Qu 6



The figure shows part of the graph of $y = a + b \sin cx$.

(i) Find the value of each of the integers
$$a$$
, b and c . [3]

Using your values of a, b and c find

(ii)
$$\frac{\mathrm{d}y}{\mathrm{d}x}$$
, [2]

(iii) the equation of the normal to the curve at
$$(\frac{\pi}{2}, 3)$$
. [3]

Nov 2015 P21 - Qu 9

Solve the following equations.

(i)
$$4\sin 2x + 5\cos 2x = 0$$
 for $0^{\circ} \le x \le 180^{\circ}$

(ii)
$$\cot^2 y + 3 \csc y = 3$$
 for $0^{\circ} \le y \le 360^{\circ}$ [5]

(iii)
$$\cos\left(z + \frac{\pi}{4}\right) = -\frac{1}{2}$$
 for $0 \le z \le 2\pi$ radians, giving each answer as a multiple of π [4]

Nov 2015 P23 - Qu 8

(i) Prove that
$$\sec^2 x + \csc^2 x = \sec^2 x \csc^2 x$$
. [4]

(ii) Hence, or otherwise, solve
$$\sec^2 x + \csc^2 x = 4\tan^2 x$$
 for $90^\circ < x < 270^\circ$. [4]



ADDITIONAL MATHEMATICS VECTORS

0606/11

Nov 2015 P21 - Qu 3

Relative to an origin O, points A, B and C have position vectors $\binom{5}{4}$, $\binom{-10}{12}$ and $\binom{6}{-18}$ respectively. All distances are measured in kilometres. A man drives at a constant speed directly from A to B in 20 minutes.

(i) Calculate the speed in kmh^{-1} at which the man drives from A to B. [3]

He now drives directly from B to C at the same speed.

(ii) Find how long it takes him to drive from B to C. [3]

Nov 2015 P23 - Qu 12

A plane that can travel at $250 \,\mathrm{kmh^{-1}}$ in still air sets off on a bearing of 070° . A wind with speed $w \,\mathrm{kmh^{-1}}$ from the south blows the plane off course so that the plane actually travels on a bearing of 060° .

Find, in kmh $^{-1}$, the resultant speed V of the plane and the windspeed w. [5]