

In[1]:= **Remove["Global`*"]**

Please see

<http://www.sci.utah.edu/~gerig/CS7960-S2010/handouts/04%20Gaussian%20derivatives.pdf>

and

http://www.cse.yorku.ca/~kosta/CompVis_Notes/fourier_transform_Gaussian.pdf

In[3]:= **gaussian[x_, sigma_] := Exp[-x^2 / (2 * sigma^2)]**

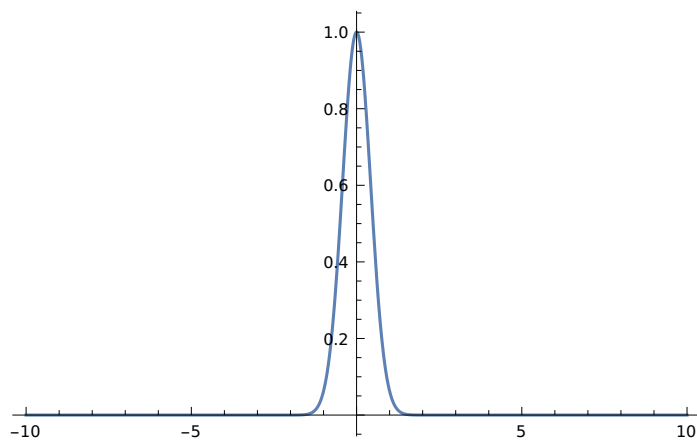
In[4]:= **normalizedGaussian [x_, sigma_] = Evaluate[gaussian[x, sigma]/gaussian[0, sigma]]**

Plot[Evaluate[normalizedGaussian [x, 1.0 / 2.355]], {x, -10, 10}, PlotRange -> All]

normalizedGaussian [0.5, 1.0 / 2.355]

Out[4]=
$$e^{-\frac{x^2}{2 \sigma^2}}$$

Out[5]=



Out[6]= **0.499947**

In[7]:=

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In[8]:= order = 1
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gaussianderivative [x_, sigma_] := Evaluate[D[gaussian[x, sigma], {x, order}]]
maxValue[sigma_] := Solve[{Evaluate[D[gaussianderivative [x, sigma], {x, 1}]] == 0}, {x}]
normalizedGaussianDerivative [x_, sigma_] :=
  gaussianderivative [x, sigma]/(-gaussianderivative [x, sigma] /. maxValue[sigma][[1]])
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Evaluate[Simplify[normalizedGaussianDerivative [x, sigma]]]
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Out[8]= 1
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Out[12]= 
$$\frac{e^{\frac{1}{2} - \frac{x^2}{2 \sigma^2}} x}{\sigma}$$

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Maxima of a gaussian derivative is

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Solve[{Evaluate[D[gaussian[x,sigma],{x,2}]]==0},{x}],
```

in this case maximum is sigma.

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Out[62]= {{x → -sigma}, {x → sigma}}
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In[13]:=
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In[14]:= Plot[Evaluate[normalizedGaussianDerivative [x, 1.0/2.355]],
  {x, -10, 10}, PlotRange → All]
```

