# **Project Euler #57: Square root convergents**



This problem is a programming version of Problem 57 from projecteuler.net

It is possible to show that the square root of two can be expressed as an infinite continued fraction.

$$\sqrt{2} = 1 + \frac{1}{2 + \frac{1}{2 + \frac{1}{2 + \dots}}} = 1.414213 \cdots$$

By expanding this for the first four iterations, we get:

$$1 + \frac{1}{2} = \frac{3}{2} = 1.5$$

$$1 + \frac{1}{2 + \frac{1}{2}} = \frac{7}{5} = 1.4$$

$$1 + \frac{1}{2 + \frac{1}{2 + \frac{1}{2}}} = \frac{17}{12} = 1.41666 \cdots$$

$$1 + \frac{1}{2 + \frac{1}{2 + \frac{1}{2 + \frac{1}{2}}}} = \frac{41}{29} = 1.41379 \cdots$$

The next three expansions are  $\frac{99}{70}$ ,  $\frac{239}{169}$ , and  $\frac{577}{408}$ , but the eighth expansion,  $\frac{1393}{985}$ , is the first example where the number of digits in the numerator exceeds the number of digits in the denominator.

Given N. In the first N expansions, print the iteration numbers where the fractions contain a numerator with more digits than denominator.

#### **Input Format**

Input contains an integer N

#### **Output Format**

Print the answer corresponding to the test case.

## **Constraints**

 $8 < N < 10^4$ 

# **Sample Input**

14

## **Sample Output**

8 13