# Ch 14 Oscillations (cont.'d)

**Key words:** simple harmonic motion (SHM), Hooke's Law, spring constant, spring-mass, pendulum, position function, displacement from equilibrium, frequency, period.

## Objective:

- I. Solve a problem that involves a **pendulum** in SHM
  - $\square$  By using the same approach for a **spring-mass** in SHM
- II. Solve for the velocity and acceleration for an object in SHM
  - $\square$  By solving for x(t) and then finding its **derivatives**.
  - $\square$  By using Conservation of Energy

#### Content Review:

 $\blacksquare$  Recall: for an object in SHM, the **position function** x(t) is generally given by

$$x(t) = A\cos(\omega t + \phi)$$

where the variables are

A = amplitude

 $\omega = angular frequency$ 

 $\phi = \text{phase shift}$ 

■ Taking the derivative (with respect to time) of x(t) gives us the **velocity function** v(t)

$$v(t) = \frac{dx}{dt} =$$

■ Taking the derivative of v(t) gives us the **acceleration function** a(t)

$$a(t) = \frac{dv}{dt} =$$

■ The angular frequency  $\omega$  has 2 forms: spring-mass and pendulum

$$\omega_{
m spr} = \sqrt{\frac{k}{m}}$$
  $\omega_{
m pen} =$ 

where the variables are

 $k = \text{spring constant}, \quad m = \text{mass of object}, \quad \ell = \text{length of string}, \quad g = \text{acc. due to gravity}$ 

■ The **total energy** of the oscillating spring-mass system is given by

$$E_{\text{tot}} = U + K = \frac{1}{2}kx^2 + \frac{1}{2}mv^2$$

where the variables are

U =spring potential energy

K =kinetic energy

## **Guided Practice**

A pendulum has a period of  $1.35\,\mathrm{s}$  on Earth. Suppose the same pendulum is now on Mars, where the acceleration of gravity is about 0.37 that on Earth.

- (i) Determine its period on Mars.
- (ii) How should the pendulum be modified so that its period is the same as on Earth?

Solution

- (i)  $T = 2.2 \,\mathrm{s}$
- (ii) By decreasing the length of the pendulum string.

## **Group Activity**

An object with mass  $2.7\,\mathrm{kg}$  is executing SHM, attached to a spring with  $k=280\,\mathrm{N/m}$ . When the object is  $0.020\,\mathrm{m}$  from its equilibrium position, it is moving with a speed of  $0.55\,\mathrm{m/s}$ .

- Determine the amplitude of the motion.
- Find the maximum speed of the object as it's oscillating.

#### Solution

(i) 
$$A = 5.8 \times 10^{-2} \,\mathrm{m}$$

(ii) 
$$v_{\text{max}} = 0.59 \,\text{m/s}$$