Introducing the Roman Senatorial Debate

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Successful implementation proposal

Here we present the rules of a round of Roman Senatorial Debate.

- 1. **Number of debaters.** The standard number of debaters is 8. Speaking time is 7 minutes.
 - The Roman Sentorial Debate format should work from 4 debaters to any number of debaters, even beyond 8, but for the purpose of a tournament, rooms should be assumed to accommodate 8 debaters, so the pace would mirror that of the British Parliamentary style.
- 2. In the beginning of the debate, each debater must reveal in their hand a number of coins. If they add up to 1\$ it means they support the motion. If they add up to 2\$ it means they're against the motion. This is supposed to be biased for the motion for it to pass. The sums are then pooled into the common pot. And they start to debate.
- 3. Each debater makes a speech. During any time of their speech, they may add money to the pot.
- 4. At the end of all speeches, votes are counted. The number of votes must reach the 1/2 + 1 number of votes threshold to pass.
- 5. Points are distributed thus:

	留	轉軚	棄權
贏輸和	$\begin{array}{c} 3 \\ 2 \\ 0 \end{array}$	1 0 0	0 0 0

1. The pot money is split thus:

- (a) s is the total sum in the pot, which always abides by the following: $s=w_{\rm fl}+w_{\rm iff}$
- (b) v is the total number of votes on the winning side, which always abides by the following: $v = v_{\text{fl}} + v_{\text{fl}}$
- (c) $w_{\widehat{\mathbf{a}}}$ and $w_{\widehat{\mathbf{p}}}$ are defined as such:

i.
$$w_{\widehat{\mathbb{H}}} = s \cdot \frac{v_{\widehat{\mathbb{H}}} + 1}{v + 1}$$
 ii. $w_{\widehat{\mathbb{H}}} = s \cdot \frac{v_{\widehat{\mathbb{H}}}}{v + 1}$

- (d) To say this without justification, this creates a quasi-prisoner's dilemma situation in the following box, where those who switch sides and win, win money but lose out relatively on points.
- (e) the split of the $w_{\mathbb{H}}$ and $w_{\mathbb{H}}$ leave a weird case where everyone switched sides and that side won. In such a case, there'd be nobody to claim the virtual \mathbb{H} share. That share can go to many places: (1) the poorest member, (2) the hosting tournament, (3) divided equally amongst all players...(4) taken by the winning side as well...

I	留	轉軚
贏輸	$\frac{3}{2}$	$\begin{array}{c} 1 \\ 0 \end{array}$

The point of the dynamic is: some people care about the money, some people care about passing the motion.

Payout structure by debater count

$n_{ m debaters}$	v_{win}	$v_{\mathrm{@}}$	$v_{ m ee}$	$w_{\widehat{\mathbf{H}}} = 100 \cdot \frac{v_{\widehat{\mathbf{H}}} + 1}{v_{win} + 1}$	$w_{\ensuremath{\scriptscriptstyle{f \#}}} = 100 \cdot rac{v_{\ensuremath{\scriptscriptstyle{f \#}}}}{v+1}$	w _{留/人}	w _{轉/人}
6	4	0	4	20.0	80.0	n/a^a	20.0
6	4	1	$\frac{3}{2}$	40.0	60.0	40.0	20.0
6	4	$\frac{2}{3}$	2	60.0	40.0	30.0	20.0
$\overset{\circ}{6}$	4	3	1	80.0	20.0	26.67	20.0
6	$\frac{4}{5}$	4	0	100.0	0.0	25.0_{2}	0.0_
6		0	5	16.67	83.33	n/a ^a	16.67
6	5	1	$\frac{4}{3}$	33.33	66.67	33.33	16.67
6	5	$\frac{\bar{2}}{3}$	3	50.0	50.0	25.0	16.67
6	þ	3	2	66.67	$\frac{33.33}{2}$	22.22	16.67
$\stackrel{\circ}{6}$	555555	$\frac{4}{5}$	Ų.	$83.33 \\ 100.0$	$^{16.67}_{0.0}$	$\frac{20.83}{20.0}$	$^{16.67}_{0.0}$
6	$\overset{5}{6}$	$\overset{\circ}{0}$	6	14.29	85.71	/ a	14.29
6	6	1	5	$\frac{14.29}{28.57}$	71.43	$^{ m n/a^a}_{28.57}$	14.29 14.29
6		2		$\frac{20.37}{42.86}$	57.14	$\frac{26.37}{21.43}$	$14.29 \\ 14.29$
$\overset{\circ}{6}$	$\frac{6}{6}$	$\frac{\bar{2}}{3}$	$\frac{4}{3}$	57.14	42.86	$\frac{21.45}{19.05}$	$14.29 \\ 14.29$
6	ĕ		$\frac{3}{2}$	71.43	$\frac{42.00}{28.57}$	17.86	14.29
6 6 6	6 6 6	$\frac{4}{5}$	1	85.71	$\bar{1}4.29$	17.14	$14.\overline{29}$
6	6	6	0	100.0	0.0	16.67	0.0^{-}

a n/a, because there are literally no participants who won who stayed on the position that they started with. Obviously this is a degenerate and highly unlikely case. But we still need to figure out how to handle the payout which has no one to receive it. It can either (1) be distributed amongst those who won, (2) go to anyone on the losing side who stuck to their guns, or (3) go to the poorest member, or (4) to the tournament organizer. We are not too interested in the details.

表 1: Payout structure for different numbers of debaters and voting scenarios

$n_{ m debaters}$	$v_{ m win}$	$v_{\widehat{f a}}$	$v_{ m e}$	$w_{\widehat{\mathbf{a}}} = 100 \cdot \frac{v_{\widehat{\mathbf{a}}} + 1}{v_{win} + 1}$	$w_{ ext{\tiny eff}} = 100 \cdot rac{v_{ ext{\tiny eff}}}{v+1}$	w _{留/人}	w _{轉/人}
7	4	0	4	20.0	80.0	n/a^a	20.0
7				40.0	60.0	40.0	20.0
7	4 4 4 5 5 5 5 5 6	$\begin{array}{c} 1\\2\\3\\4 \end{array}$	$\begin{array}{c} 3 \\ 2 \\ 1 \end{array}$	60.0	40.0	$\begin{array}{c} 40.0 \\ 30.0 \\ 26.67 \end{array}$	$\frac{\bar{20.0}}{20.0}$
7	4	3	1	80.0	20.0	26.67	20.0
7	4	$_{4}$	0	100.0	[0.0]	25.0	0.0_{-}
7	5	0	5	16.67	83.33	n/a^a	16.67
7	5	1	$\frac{4}{2}$	33.33	66.67	33.33	16.67
7	5	$\frac{2}{3}$	3	50.0	50.0 $ 33.33$	$\frac{25.0}{22.22}$	$\frac{16.67}{16.67}$
1/7	5	<u>ئ</u>	2	50.0 66.67 83.33	33.33 16.67	$\frac{22.22}{20.83}$	16.67
$\frac{1}{7}$	၌	$\begin{array}{c} 1\\2\\3\\4\\5\end{array}$	$\begin{array}{c} 4 \\ 3 \\ 2 \\ 1 \\ 0 \end{array}$	$\frac{63.33}{100.0}$	0.07	$\frac{20.83}{20.0}$	$\substack{16.67\\0.0}$
7	6	ő	$\overset{0}{6}$	14.29	85.71	n/a^a	14.29
7				28 57	71.43	28.57	14.29
7	ĕ	5	7	28.57 42.86	57.14	$\frac{20.37}{21.43}$	14.29
7	<u>ĕ</u>	$\bar{3}$	5 4 3 2 1	57.14	$\begin{array}{c} 42.86 \\ 28.57 \end{array}$	19.05	$14.29 \\ 14.29$
7	Ğ.	$\check{4}$	$\check{2}$	71.43	28.57	$\bar{17.86}$	14.29
7	6	$ \begin{array}{c} 1 \\ 2 \\ 3 \\ 4 \\ 5 \\ 6 \end{array} $		85.71	14.29	17.14	14.29
7	$\begin{array}{c} 6 \\ 6 \\ 6 \\ 6 \\ 6 \\ 7 \end{array}$	6	$\underline{0}$	100.0	0.0	16.67	0.0
7		Ō	7	12.5	87.5	n/a^a	12.5
7	$\frac{7}{7}$	1	6	25.0	75.0	25.0	12.5
7	7	2	$ \begin{array}{c} 6 \\ 5 \\ 4 \\ 3 \\ 2 \end{array} $	37.5 50.0	62.5	18.75	12.5
7	$\frac{7}{7}$	3	4	50.0	50.0	16.67	12.5 12.5 12.5
47	4	4	၌	$\begin{array}{c} 62.5 \\ 75.0 \end{array}$	$\begin{array}{c} 37.5 \\ 25.0 \end{array}$	$\frac{15.62}{15.0}$	12.5
$\frac{i}{7}$	$\frac{1}{7}$	$\begin{array}{c} 1 \\ 2 \\ 3 \\ 4 \\ 5 \\ 6 \\ 7 \end{array}$		87.5	$12.5 \\ 12.5$	14.58	$12.5 \\ 12.5$
7	7	7	Ö	100.0	0.0	14.29	0.0

a n/a indicates no 留 voters to receive the payout.

表 2: Payout structure for different numbers of debaters and voting scenarios

$n_{ m debaters}$	v_{win}	$v_{\mathrm{ ilde{B}}}$	$v_{ m e}$	$w_{\widehat{\mathbf{H}}} = 100 \cdot \frac{v_{\widehat{\mathbf{H}}} + 1}{v_{win} + 1}$	$w_{ ext{\tiny \#}} = 100 \cdot rac{v_{ ext{\tiny \#}}}{v+1}$	$w_{lpha/igwedge}$	w _{轉/人}
8	5	0	5	16.67	83.33	n/a^a	16.67
8	5 555556	1		33 33	$\begin{array}{c} 66.67 \\ 50.0 \\ 33.33 \end{array}$	33.33 25.0 22.22 20.83	16.67
8	5	$\begin{array}{c} 1 \\ 2 \\ 3 \\ 4 \\ 5 \\ 0 \end{array}$	$\begin{array}{c} 4 \\ 3 \\ 2 \\ 1 \\ 0 \\ 6 \end{array}$	50.0 66.67 83.33	50.0	25.0	16.67
8	5	3	2	66.67	<u> 33.32</u>	22.22	16.67
8	þ	$\frac{4}{2}$	Ţ	83.33	16.67	20.83	16.67
8	5	Ö	Ü	100.0	$\begin{array}{c} 0.0 \\ 85.71 \end{array}$	20.0 n/a^a	$0.0 \\ 14.29$
0	O C		õ	14.29		n/a^a	14.29
Ş	6	1) 4	28.37 42.86	71.43	$28.57 \\ 21.43$	$\frac{14.29}{14.29}$
8	6 6 6 6 6 7	$\begin{array}{c} 1 \\ 2 \\ 3 \\ 4 \\ 5 \\ 6 \\ 0 \end{array}$	5 4 3 2 1 0	28.57 42.86 57.14	57.14 42.86 28.57 14.29	19.05	14.29
8	6	4	$\frac{3}{2}$	71.43	28.57	$\frac{19.05}{17.86}$	14.29 14.29
<u>8</u>	ĕ	$\bar{5}$	$\bar{1}$	85.71	$\bar{1}4.29$	17.14	14.29
8	6	6	0	100.0	0.0	16.67	0.0
8	7		7	12.5	87.5	n/a^a	12.5
8	7	1	6	$\begin{array}{c} 25.0 \\ 37.5 \end{array}$	$\begin{array}{c} 75.0 \\ 62.5 \end{array}$	25.0	12.5
8	7	2	5	37.5	62.5	18.75	12.5
8	7	3	$\frac{4}{2}$	50.0	50.0	16.67	12.5
8	$\frac{i}{7}$	5	ગુ	$\begin{array}{c} 50.0 \\ 62.5 \\ 75.0 \end{array}$	37.3 25.0	$\frac{15.62}{15.0}$	15.5
8	7	6	ī	87.5	$\begin{array}{c} 37.5 \\ 25.0 \\ 12.5 \end{array}$	$15.0 \\ 14.58$	12.5 12.5 12.5 12.5 12.5 12.5
<u>8</u>	Ż	$\begin{array}{c} 1 \\ 2 \\ 3 \\ 4 \\ 5 \\ 6 \\ 7 \end{array}$	$ \begin{array}{c} 6 \\ 5 \\ 4 \\ 3 \\ 2 \\ 1 \\ 0 \end{array} $	100.0	0.0	14.29	0.0
8	8	Ó	8	11.11	$ \begin{array}{c} 0.0 \\ 88.89 \end{array} $	n/a^a	11.11
8	8	1	7	22.22	77.78	22.22	11.11
8	8	$\overline{2}$	6	33.33	66.67	$\overline{16}.\overline{67}$	11.11
8	8	3	5	44.44	55.56	14.81 13.89 13.33	11.11
8	8	4	4	55.5 <u>6</u>	44.44	13.89	11.11
Ş	777777888888888888888888888888888888888	9 6	8 76 5 4 3 2 1 0	55.56 66.67 77.78	$\frac{33.33}{22.22}$	13.33 12.96	$\frac{11.11}{11}$
8	8	7	1	88.89	11.11	$\frac{12.90}{12.7}$	11:11
2 222222 22 222222 22 22222222222222222	8	1 2 3 4 5 6 7 8	Ō	100.0	0.0°	$\frac{12.7}{12.5}$	0.0^{-1}
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^a n/a indicates no 留 voters to receive the payout.

表 3: Payout structure for different numbers of debaters and voting scenarios

$n_{ m debaters}$	$v_{ m win}$	$v_{\mathrm{ ilde{a}}}$	$v_{ m e}$	$w_{\widehat{\mathbf{u}}} = 100 \cdot \frac{v_{\widehat{\mathbf{u}}} + 1}{v_{win} + 1}$	$w_{ ext{\tiny #\#}} = 100 \cdot rac{v_{ ext{\tiny #\#}}}{v+1}$	w _{留/人}	w _{轉/人}
9	5	0	5	16.67	83.33	n/a ^a 33.33 25.0 22.22 20.83 20.0	16.67
9	5	$\frac{1}{2}$	$\frac{4}{2}$	33.33	66.67 50.0 33.33	33.33	$\frac{16.67}{16.67}$
9	9 5	3	3	50.0 66.67 83.33	30.0 33.33	$\frac{25.0}{22.22}$	$\frac{16.67}{16.67}$
9	$\check{5}$	$\overset{\circ}{4}$	$\bar{1}$	83.33	10.07	20.83	16.67
9	5	5	0	100.0	$\begin{array}{c} 0.0 \\ 85.71 \end{array}$	20.0_{a}	0.0
9	6	0	6	14.29	85.71	20.0 n/a ^a 28.57 21.43 19.05 17.86 17.86	14.29
9	6	$\frac{1}{2}$	$\frac{9}{4}$	28.57 42.86 57.14	71.43 57.14 42.86 28.57 14.29	28.57 21.43	14.29 14.29 14.29 14.29 14.29
ğ	$\ddot{6}$	$\bar{3}$	$\bar{3}$	$\frac{42.00}{57.14}$	42.86	19.05	14.29
9	6	$\underline{4}$	2	71.43	28.57	17.86	14.29
9	6	5 6	Ü	$\begin{array}{c} 85.71 \\ 100.0 \end{array}$	14.29	$\frac{17.14}{16.67}$	14.29
9	7	Ŏ	7	12.5	87.5	n/a^a	12.5
9	$\dot{7}$	ĭ	6	25.0	75.0	25.0	$12.5 \\ 12.5$
9	7	2	5	37.5	62.5	18.75	12.5
9	$\frac{7}{7}$	3	$\frac{4}{2}$	50.0 62.5	50.0 37.5	25.0 18.75 16.67 15.62	$\frac{12.5}{12.5}$
9	$\frac{1}{7}$	$\frac{4}{5}$	$\frac{3}{2}$	25.0 37.5 50.0 62.5 75.0 87.5	75.0 62.5 50.0 37.5 25.0 12.5	15.02	$\begin{array}{c} 0.0 \\ 12.5 \\ 12.5 \\ 12.5 \\ 12.5 \\ 12.5 \\ 12.5 \\ 12.5 \\ 12.5 \\ 12.5 \\ \end{array}$
ğ	$\dot{7}$	<u>6</u>	$\bar{1}$	87.5	$\overline{1}2.5$	14.58	$\bar{1}\bar{2}.\bar{5}$
9	7	7	Ö	100.0	0.0 88.89 77.78 66.67 55.56	15.0 14.58 14.29 n/a ^a 22.22 16.67 14.81 13.33 12.96 12.7 12.5 n/a ^a	$0.0 \\ 11.11$
9	8	1	8	11.11	88.89 77.78	n/a	11.11
9	8	$\frac{1}{2}$	6	22.22 33.33 44.44 55.56	66.67	16.67	11.11
ğ	8	$\bar{3}$	Š.	44.44	55.56	14.81	11.11
9	8	4	$\frac{4}{2}$	55.56	$\begin{array}{c} 44.44 \\ 33.33 \\ 22.22 \end{array}$	13.89	$\frac{11.11}{11.11}$
8	8	6 6	3	$\frac{66.67}{77.78}$	33.33 22.22	13.33 12.96	11.11
9	8	$\ddot{7}$	$\bar{1}$	$\begin{array}{c} 66.67 \\ 77.78 \\ 88.89 \end{array}$	11.11	12.7	11.11
9	8	8	0	100.0	0.0	12.5_{a}	0.0
9	9	0	9	10.0	90.0	$^{ m n/a^{a}}_{20.0}$	10.0
9	9	$\frac{1}{2}$	7	$\frac{20.0}{30.0}$	$\frac{80.0}{70.0}$	20.0 15.0	$\frac{10.0}{10.0}$
ğ	\S	$\bar{3}$	6	40.0	60.0	$ \begin{array}{c} \overline{15.0} \\ 13.33 \\ 12.5 \end{array} $	10.0
9	9	4	5	50.0	50.0	$\frac{12.5}{12.0}$	$\frac{10.0}{10.0}$
9	9	5 6	$\frac{4}{3}$	$\frac{60.0}{70.0}$	$\frac{40.0}{30.0}$	$\frac{12.0}{11.67}$	$\frac{10.0}{10.0}$
ğ	ğ	7	$\overset{\circ}{2}$	80.0	20.0	11.43	10.0
9 99999 9 999999 9 99999999 9 99999999 9999	5 55555 6 66666667 777777778 888888889 9999999999	$\frac{1}{2345} \\ 0 \\ 1 \\ 23456 \\ 0 \\ 1 \\ 23456 \\ 7 \\ 0 \\ 1 \\ 23456 \\ 7 \\ 89$	5432106543210765432108765432109876543210	90.0	10.0	11.25	10.0
9	9	9	U	100.0	0.0	11.11	0.0

a n/a indicates no 留 voters to receive the payout.

表 4: Payout structure for different numbers of debaters and voting scenarios

$n_{ m debaters}$	$v_{ m win}$	$v_{\mathrm{ ilde{a}}}$	$v_{ m e}$	$w_{\widehat{\mathbf{H}}} = 100 \cdot \frac{v_{\widehat{\mathbf{H}}} + 1}{v_{win} + 1}$	$w_{ extstyle ij} = 100 \cdot rac{v_{ extstyle ij}}{v+1}$	w _{留/人}	$w_{ ext{\tiny e}/ackslash}$
10	6	0	6	14.29	85.71	$^{ m n/a^a}_{28.57}$	14.29
$^{10}_{10}_{10}$	6	$\frac{1}{2}$	$ \begin{array}{c} 6 \\ 5 \\ 4 \\ 3 \\ 2 \\ 1 \\ 0 \\ 7 \end{array} $	28.57 42.86 57.14 71.43 85.71	71.43 57.14 42.86 28.57	$\frac{28.57}{21.43}$	14.29 14.29 14.29 14.29 14.29 0.0
10	6	$\frac{2}{3}$	$\frac{4}{3}$	$\frac{42.80}{57.14}$	$\frac{37.14}{42.86}$	$\frac{21.45}{19.05}$	$14.29 \\ 14.29$
$\overset{\bar{1}\check{0}}{10}$	Ğ	$\frac{3}{4}$	$\tilde{2}$	71.43	$\frac{28.57}{2}$	$\frac{19.05}{17.86}$	14.29
$\frac{10}{10}$	6	5 6	Ų.	$\begin{array}{c} 85.71 \\ 100.0 \end{array}$	$\begin{array}{c} 14.29 \\ 0.0 \end{array}$	$17.14 \\ 16.67$	14.29
10	$\frac{3}{7}$	ŏ	$\frac{9}{7}$	12.5	87.5	n/a^a	12.5
$^{10}_{10}$	7	1	6	$\frac{25.0}{37.5}$	$\begin{array}{c} 75.0 \\ 62.5 \end{array}$	$\frac{25.0}{18.75}$	12.5 12.5 12.5 12.5 12.5 12.5
$\overset{10}{10}$	$\frac{7}{7}$	$\frac{2}{3}$	$\frac{5}{4}$	37.5 50.0	62.5 50.0	$\frac{18.75}{16.67}$	$\frac{12.5}{12.5}$
10	$\dot{7}$	$\frac{3}{4}$	3	50.0 62.5 75.0 87.5	50.0 37.5 25.0	15.62	12.5
10	$\frac{7}{7}$	5	2	$\frac{75.0}{27.5}$	$\begin{array}{c} 25.0 \\ 12.5 \end{array}$	15.0	$\frac{12.5}{12.5}$
$\overset{\bar{10}}{10}$	$\dot{7}$	7	Ö	100.0	0.0	$14.58 \\ 14.29$	0.0
10	8	0	8	11.11	88.89	n/a^a	11.11
$^{10}_{10}$	8	$\frac{1}{2}$	6	$\begin{array}{c} 22.22 \\ 33.33 \end{array}$	77.78 66.67	$\frac{22.22}{16.67}$	$\frac{11.11}{11.11}$
10	8	$\bar{3}$	5	44.44	66.67 55.56	14.81	11.11
$\overset{\bar{1}\overset{\circ}{0}}{10}$	8	$\frac{4}{5}$	$\frac{4}{3}$	55.56 66.67	$\frac{44.44}{22.22}$	$\frac{13.89}{13.33}$	$\frac{11.11}{11.11}$
10	8	$\ddot{6}$	$\overset{3}{2}$	$\overset{66.67}{77.78}$	$\begin{array}{c} 44.44 \\ 33.33 \\ 22.22 \end{array}$	12.96	11.11
$\frac{10}{10}$	6666667777777788888888899999999999	7	65432108765432109876543210	88.89 100.0	$\substack{11.11\\0.0}$	n/a ^a 22.22 16.67 14.81 13.89 13.33 12.96 12.7 12.5 n/a ^a	$^{11.11}_{0.0}$
10	9	0	9	100.0	90.0	n/a ^a	10.0
10	$\tilde{9}$	ĭ	8	20.0	80.0	20.0	10.0
10	9	$\frac{2}{3}$	7	$\frac{30.0}{40.0}$	$70.0 \\ 60.0$	$15.0 \\ 13.33$	$\frac{10.0}{10.0}$
$\begin{array}{c} 10 \\ 10 \end{array}$	9	$\overset{3}{4}$	5	50.0	50.0	$12.5 \\ 12.0$	10.0
$\begin{array}{c} 10 \\ 10 \end{array}$	9	5	$\frac{4}{2}$	$\frac{60.0}{70.0}$	$\frac{40.0}{30.0}$	$\frac{12.0}{11.67}$	$\frac{10.0}{10.0}$
10 10 10	9	7	$\frac{3}{2}$	80.0	20.0	11.43	$10.0 \\ 10.0$
10	9	8	1	90.0	$\overline{10.0}$	$\frac{11.25}{11.11}$	10.0
$\begin{array}{c} 10 \\ 10 \end{array}$	9 10	0	10	$100.0 \\ 9.09$	$0.0 \\ 90.91$	$\frac{11.11}{n/a}$	$0.0 \\ 9.09$
10	10	ĭ		18.18	$\begin{array}{c} 81.82 \\ 72.73 \end{array}$	18.18	9.09
$\begin{array}{c} 10 \\ 10 \end{array}$	$^{10}_{10}$	$\frac{2}{2}$	8	$\frac{27.27}{36.36}$	$\frac{72.73}{62.64}$	$\frac{13.64}{12.12}$	$9.09 \\ 9.09$
10	$\frac{10}{10}$	$\overset{\mathfrak{d}}{4}$	6	45.45	$63.64 \\ 54.55$	11.36	$9.09 \\ 9.09$
$\overset{\bar{1}}{\overset{\bar{0}}{0}}$	10	$\frac{5}{c}$	5	54.55	45.45	10.91	9.09
$\overset{10}{10}$	$^{10}_{10}$	$\frac{0}{7}$	$\frac{4}{3}$	$\begin{array}{c} 63.64 \\ 72.73 \end{array}$	$\frac{36.36}{27.27}$	$\frac{10.61}{10.39}$	$\frac{9.09}{9.09}$
10	10	8	$\tilde{2}$	81.82	18.18	10.23	9.09
$^{10}_{10}$	$^{10}_{10}$	$\frac{1}{234} \\ 560 \\ 1234 \\ 567 \\ 01234 \\ 567 \\ 801 \\ 234 \\ 567 \\ 8901 \\ 234 \\ 567 \\ 8910$	9876543210	$90.91 \\ 100.0$	$\frac{9.09}{0.0}$	$\frac{10.1}{10.0}$	$\frac{9.09}{0.0}$
			~	=00.0	0.0	-0.0	

 $[\]frac{1}{a}$ n/a indicates no \cong voters to receive the payout.

表 5: Payout structure for different numbers of debaters and voting scenarios

$ \begin{array}{c ccccccccccccccccccccccccccccccccccc$								
$\begin{array}{cccccccccccccccccccccccccccccccccccc$	$n_{ m debaters}$	$v_{ m win}$	v_{B}	$v_{ m ee}$	$w_{\widehat{\mathbf{a}}} = 100 \cdot \frac{v_{\widehat{\mathbf{a}}} + 1}{v_{win} + 1}$	$w_{ ext{\tiny \#}} = 100 \cdot rac{v_{ ext{\tiny \#}}}{v+1}$		w _{轉/人}
$\begin{array}{cccccccccccccccccccccccccccccccccccc$	11	6			$\frac{14.29}{28.57}$	85.71	$\frac{n}{a^a}$	14.20
$\begin{array}{cccccccccccccccccccccccccccccccccccc$	11	6	$\frac{1}{2}$	4	42.86 57.14	57.14 42.86	21.43	14.29 14.29
$\begin{array}{cccccccccccccccccccccccccccccccccccc$	11	6	$\frac{3}{4}$	2	$\begin{array}{c} 37.14 \\ 71.43 \end{array}$	$\frac{42.50}{28.57}$	$\frac{19.05}{17.86}$	14.29 14.29
$\begin{array}{cccccccccccccccccccccccccccccccccccc$	11 11	6	$\overset{5}{6}$	0	100.0	$0.0^{14.29}$	10.07	0.0
$\begin{array}{cccccccccccccccccccccccccccccccccccc$	11	7 7		7 6	$\begin{array}{c} 12.5 \\ 25.0 \end{array}$	87.5	$\frac{n}{a^a}$	$\frac{12.5}{12.5}$
$\begin{array}{cccccccccccccccccccccccccccccccccccc$	11	$\frac{\dot{7}}{7}$	$\frac{1}{2}$	$\frac{5}{4}$	$\frac{57.5}{50.0}$	62.5	$\frac{18.75}{16.67}$	$\frac{12.5}{12.5}$
$\begin{array}{cccccccccccccccccccccccccccccccccccc$	11	$\frac{1}{7}$	$\frac{3}{4}$	3	$\frac{62.5}{75.0}$	$\frac{37.5}{35.5}$	15.62	$12.5 \\ 12.5$
$\begin{array}{cccccccccccccccccccccccccccccccccccc$	11	$\frac{7}{7}$	$\frac{5}{6}$	1	87.5	12.5	14.58	$12.5 \\ 12.5$
$\begin{array}{cccccccccccccccccccccccccccccccccccc$	11	8	0	8	11.11	88.89	$\frac{14.29}{\text{n/a}}$	11.11
$\begin{array}{cccccccccccccccccccccccccccccccccccc$	11 11	8	$\frac{1}{2}$	$\frac{7}{6}$	$\frac{22.22}{33.33}$	$77.78 \\ 66.67$	$\frac{22.22}{16.67}$	$\frac{11.11}{11.11}$
$\begin{array}{cccccccccccccccccccccccccccccccccccc$	11 11	8 8	$\bar{3}_4$	$\frac{5}{4}$	44.44 55.56	55.56 44.44	$\frac{14.81}{13.89}$	11.11
$\begin{array}{cccccccccccccccccccccccccccccccccccc$	11 11	8	5	3	66.67	33.33 22.22	13.33	11.11
$\begin{array}{cccccccccccccccccccccccccccccccccccc$	11	8	$\frac{6}{7}$	1	88.89 100.0	11.11	12.7 12.7	11.11
$\begin{array}{cccccccccccccccccccccccccccccccccccc$	11	9	0	9	10.0	90.0	n / 2"	10.0
$\begin{array}{cccccccccccccccccccccccccccccccccccc$	11 11	9 9	$\frac{1}{2}$	$\frac{8}{7}$	$\frac{20.0}{30.0}$	$\frac{80.0}{70.0}$	$\frac{20.0}{15.0}$	10.0
$\begin{array}{cccccccccccccccccccccccccccccccccccc$	11 11	9 9	$\frac{3}{4}$	$\frac{6}{5}$	50.0	60.0	$\frac{13.33}{12.5}$	
$\begin{array}{cccccccccccccccccccccccccccccccccccc$	11	9	5 6	$\frac{4}{3}$	60.0	40.0	$\frac{12.0}{11.67}$	
$\begin{array}{cccccccccccccccccccccccccccccccccccc$	11 11	9 9	7 8	$\frac{3}{1}$	80.0 90.0	20.0 10.0	11.43 11.25	10.0
$\begin{array}{cccccccccccccccccccccccccccccccccccc$	11 11	9 10	9	0	100.0	0.0	11.11	0.0
$\begin{array}{cccccccccccccccccccccccccccccccccccc$	11 11	10	1	9	10 10	$\frac{90.91}{81.82}$	18.18	9.09
$\begin{array}{cccccccccccccccccccccccccccccccccccc$	11 11	$\frac{10}{10}$	$\frac{2}{3}$	8 7	$\frac{27.27}{36.36}$	$\begin{array}{c} 72.73 \\ 63.64 \end{array}$	$\frac{13.64}{12.12}$	9.09
$\begin{array}{cccccccccccccccccccccccccccccccccccc$	11 11	10	$\frac{4}{5}$	$\frac{6}{5}$	$45.45 \\ 54.55$	45.45	$\frac{11.36}{10.91}$	9.09
$\begin{array}{cccccccccccccccccccccccccccccccccccc$	11 11	$\frac{10}{10}$	$\frac{6}{7}$	$\frac{4}{3}$	63.64	36.36	$\frac{10.61}{10.39}$	$9.09 \\ 9.09$
$\begin{array}{cccccccccccccccccccccccccccccccccccc$	11 11	10	8	$\frac{2}{1}$	81.82 90.91	18.18	10.23	9.09 9.09
$\begin{array}{cccccccccccccccccccccccccccccccccccc$	11 11			1.1	100.0	0.0	10.0	0.0
$\begin{array}{cccccccccccccccccccccccccccccccccccc$	11	11			16 67	83 33	16.67	8.33 8.33
$\begin{array}{cccccccccccccccccccccccccccccccccccc$	11	11	$\frac{2}{3}$	9 <u>8</u>	33.33	$\begin{array}{c} 75.0 \\ 66.67 \end{array}$	11.11	8.33 8.33
$\begin{array}{cccccccccccccccccccccccccccccccccccc$	11 11	11 11	$\frac{4}{5}$	$\overset{7}{6}$	$\frac{41.67}{50.0}$	$\begin{array}{c} 58.33 \\ 50.0 \end{array}$	$\frac{10.42}{10.0}$	$ \begin{array}{c} 8.33 \\ 8.33 \end{array} $
$\begin{array}{cccccccccccccccccccccccccccccccccccc$	11 11	$^{11}_{11}$	$\frac{6}{7}$	$\frac{5}{4}$	58.33	41.67	$9.72 \\ 9.52$	$\frac{8.33}{8.33}$
$egin{array}{cccccccccccccccccccccccccccccccccccc$	$1\overline{1}$	11	$\frac{\dot{8}}{9}$	$\frac{\bar{3}}{2}$	83 33	25.0_{-}	$\frac{9.3\bar{8}}{9.26}$	$\frac{8.33}{8.33}$
	11 11		$\frac{10}{11}$	$\bar{1} \\ 0$	$91.67 \\ 100.0$	8.33 0.0	$\frac{9.17}{9.09}$	$\begin{array}{c} 8.33 \\ 0.0 \end{array}$

a n/a indicates no 留 voters to receive the payout.

表 6: Payout structure for different numbers of debaters and voting scenarios

$n_{ m debaters}$	v_{win}	$v_{\mathrm{\widehat{B}}}$	$v_{ m ee}$	$w_{\widehat{\mathbf{H}}} = 100 \cdot \frac{v_{\widehat{\mathbf{H}}} + 1}{v_{win} + 1}$	$w_{ ext{\tiny eff}} = 100 \cdot rac{v_{ ext{\tiny eff}}}{v+1}$	w _{留/人}	w _{轉/人}
12	$\frac{7}{7}$	0	7	$\frac{12.5}{25.0}$	87.5 75.0	n/a ^a 25.0 18.75 16.67 15.62 14.58	$\frac{12.5}{12.5}$
12 12 12 12 12 12 12 12 12 12	$\frac{1}{7}$	1 2 3 4 5 6 7 0	5	25.0 37.5 50.0 62.5 75.0 87.5	75.0 62.5 50.0 37.5 25.0 12.5	18.75	12.5 12.5 12.5 12.5 12.5 12.5
$\frac{12}{12}$	$\frac{1}{7}$	$\frac{3}{4}$	3	$\frac{50.0}{62.5}$	37.5 37.5	15.62	$12.5 \\ 12.5$
$\frac{12}{12}$	$\frac{7}{7}$	$\frac{5}{6}$	$\frac{2}{1}$	87.5 100.0	$12.5 \\ 12.5$	13.0 14.58	$12.5 \\ 12.5$
$\frac{12}{12}$	8		8	100.0 11 11	88.89	$\frac{14.29}{\text{n/a}^{\text{a}}}$	$0.0 \\ 11.11$
$\frac{12}{12}$	8 8	$\frac{1}{2}$	$\frac{7}{6}$	$\frac{22.22}{33.33}$	$77.78 \\ 66.67$	$\frac{22.22}{16.67}$	11.11 11.11 11.11
$^{12}_{12}$	8 8	$\frac{3}{4}$	$\frac{5}{4}$	$44.44 \\ 55.56$	0.0 88.89 77.78 66.67 55.56 44.44	$\frac{14.81}{13.89}$	11.11
$^{12}_{12}$	8 8	$ \begin{array}{c} 1 \\ 2 \\ 3 \\ 4 \\ 5 \\ 6 \\ 7 \\ 8 \\ 0 \end{array} $	$\frac{3}{2}$	22.22 33.33 44.44 55.56 66.67 77.78 88.89	33.33 22.22 11.11 0.0	14.29 n/a ^a 22.22 16.67 14.81 13.89 13.33 12.96 12.7 12.5 n/a ^a	11.11 11.11
$\begin{array}{c} 12 \\ 12 \end{array}$	8 8	$\frac{7}{8}$	$\stackrel{1}{0}$	$88.89 \\ 100.0 \\ 10.0$	$\begin{array}{c} 11.11 \\ 0.0 \end{array}$	$\frac{12.7}{12.5}$	$\begin{array}{c} 11.11 \\ 0.0 \end{array}$
$\frac{12}{12}$	9 9	0 1	9 8	$\frac{10.0}{20.0}$	90.0	$\frac{n}{a}^{a}$ 20.0	$\frac{10.0}{10.0}$
$\frac{12}{12}$	9 9	$\frac{\bar{2}}{3}$	$\frac{7}{6}$	20.0 30.0 40.0	80.0 70.0 60.0	$15.0 \\ 13.33$	$10.0 \\ 10.0$
$\overline{12}$	9 9	$\frac{4}{5}$	$\frac{5}{4}$	$\begin{array}{c} 50.0 \\ 60.0 \end{array}$	$\begin{array}{c} 50.0 \\ 40.0 \end{array}$	$\frac{12.5}{12.0}$	$\frac{10.0}{10.0}$
$\frac{12}{12}$	9 9	$\frac{6}{7}$	$\frac{3}{2}$	70.0 80.0	$\frac{30.0}{20.0}$	$\frac{11.67}{11.43}$	$10.0 \\ 10.0$
12 12 12 12 12 12 12 12 12 12 12 12 12 1	77777778888888889999999999	1 23 4 5 6 7 89	65432108765432109876543210	90.0 100.0	$ar{1}\overset{\bullet}{0}\overset{\bullet}{.}\overset{\bullet}{0}$	20.0 15.0 13.33 12.5 12.0 11.67 11.43 11.25 11.11	$10.0 \\ 0.0$
$\frac{12}{12}$	10 10	0	10	0.00	00.01	n/a ^a 18.18 13.64 12.12 11.36 10.91 10.61 10.39 10.23 10.1 10.0	9.09 9.09
$\frac{12}{12}$	$\frac{10}{10}$	1 23 4 5 6 7 8 9 10	9 87 65 4 32 10	18.18 27.27 36.36 45.45 54.55	81.81 81.82 72.73 63.64 54.55 45.45	13.64	9.09 9.09 9.09
$\frac{12}{12}$	$\frac{10}{10}$	$\frac{3}{4}$	6	45.45 54.55	54.55 45.45	11.36	$9.09 \\ 9.09$
$\frac{12}{12}$	10 10 10 10	$\frac{6}{7}$	$\frac{3}{3}$	63.64 72.73 81.82 90.91	36.36 27.27 18.18 9.09	10.61	$\frac{9.09}{9.09}$
$\frac{12}{12}$	$\frac{10}{10}$	8	$\frac{3}{1}$	81.82 90.91	18.18	10.23	$\frac{9.09}{9.09}$
$\frac{12}{12}$	10 11	$\frac{10}{0}$	0 11	100.0	0.0	10.0 n/2ª	$0.0 \\ 8.33$
12	11	1	10	8.33 16.67 25.0 33.33 41.67 50.0 58.33	91.67 83.33 75.0 66.67 58.33 50.0 41.67 33.33	n/a ^a 16.67 12.5	8.33
$\frac{12}{12}$	11 11 11	$\frac{2}{3}$	9 8	$\begin{array}{c} 25.0 \\ 33.33 \\ 41.67 \end{array}$	$\frac{75.0}{66.67}$	$12.0 \\ 11.11 \\ 10.42$	8.33 8.33
$\frac{12}{12}$	11 11 11	5	6	50.0 50.2	50.55 50.0 41.67	10.42 10.0	8.33 8.33
$\frac{12}{12}$	11 11	2 3 4 5 6 7 8 9 10	9 8 7 6 5 4 3 2 1	66.67 75.0		11.11 10.42 10.0 9.72 9.52 9.38 9.26 9.17 9.09	8.33 8.33 8.33 8.33 8.33 8.33 8.33 8.33
$\frac{12}{12}$	11 11	9	$\frac{3}{2}$	66.67 75.0 83.33 91.67 100.0	16.67 8.33 0.0 92.31	$9.26 \\ 9.17$	8.33 8.33
$\frac{12}{12}$	$\begin{array}{c} 11 \\ 11 \\ 12 \end{array}$	11	$\frac{1}{0}$ 12	$100.0 \\ 7.60$	0.00	$9.09 \\ n/a^{a}$	$0.0 \\ 7.60$
$\frac{12}{12}$	$\frac{12}{12}$	0 1	11	$\frac{7.09}{15.38}$	84.62 86.00	15.38	7 60
$\frac{12}{12}$	$\frac{12}{12}$	$\frac{2}{3}$	$\frac{10}{9}$	$\frac{23.08}{30.77}$	69.23	$\frac{11.54}{10.26}$	7.69 7.69 7.69
$\frac{12}{12}$	$\frac{12}{12}$	1 2 3 4 5 6 7 8 9	8 7	7.69 15.38 23.08 30.77 38.46 46.15 53.85 61.54 69.23 76.92	92.31 84.62 76.92 69.23 61.54 53.85 46.15 38.46 30.77	$9.62 \\ 9.23$	$7.69 \\ 7.69 \\ 7.69$
$\frac{12}{12}$	$\frac{12}{12}$	6 7	5 5	$\begin{array}{c} 53.85 \\ 61.54 \\ 20.03 \end{array}$	$\frac{46.15}{38.46}$	$\frac{8.97}{8.79}$	7.69
$\frac{12}{12}$	$\frac{12}{12}$	8 9	$\frac{4}{3}$	69.23 76.92	$\begin{array}{c} 30.77 \\ 23.08 \\ 15.38 \end{array}$	8.55 8.55	$\frac{7.69}{7.69}$
12 12 12 12 12 12 12 12 12 12 12 12 12 1	12 12 12 12 12 12 12 12 12 12 12 12	10 11 11	9 87 65 4 32 1 0	$ \begin{array}{r} 10.92 \\ 84.62 \\ 92.31 \\ 100.0 \end{array} $	7.69	15.38 11.54 10.26 9.62 9.23 8.97 8.79 8.65 8.55 8.46 8.39 8.33	7.69 7.69 7.69
12	12	12	U	100.0	0.0	8.33	0.0

a n/a indicates no 留 voters to receive the payout.

表 7: Payout structure for different numbers of debaters and voting scenarios