# Analyzing the Quantitative Impact of Constituent Counts and Rebalancing Intervals on Ethereum Market Index Performance Metrics

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#### Abstract

In the rapidly evolving landscape of decentralized finance, the Ethereum market stands as a dynamic and multifaceted ecosystem. This research delineates a meticulous approach to unraveling the complexities of capitalization-weighted (CW) index configurations in the Ethereum market, offering a robust statistical foundation for navigating this vibrant financial arena. Through an indepth exploration of various rebalancing intervals and constituent counts, this study illuminates optimal strategies to enhance performance metrics in CW index constructions. The empirical results presented herein are grounded in rigorous statistical validation, revealing that configurations with higher constituent counts generally yield favorable total return outcomes while reducing the max drawdown value, thereby suggesting a potential for risk reduction through portfolio diversification. Furthermore, an eight-week rebalancing interval paired with a thirty-constituent strategy emerged as a potent configuration, promising a total return of 556.65% and a Sharpe ratio of 1.83, indicative of a robust risk-adjusted performance. This study bears substantial implications for investors, asset managers, and the broader cryptocurrency community.

# 1 Introduction

In recent years, the realm of decentralized finance (DeFi) has witnessed a meteoric rise, with the Ethereum market emerging as a nexus of innovation and opportunities [6]. In this sector, Capitalization-Weighted (CW) indices serve as a crucial instrument, facilitating a data-analytic method for stakeholders to steer through the intricate landscape of the Ethereum ecosystem, as seen with tools like the Defi Pulse Index (DPI) [4]. However, the optimal configuration of these indexes — a harmonious balance of constituent count and rebalancing intervals — remains a largely unexplored territory. This study embarks on a meticulous journey to unravel these intricacies, offering a robust statistical pathway to optimized index configurations.

The significance of this research is manifold. First and foremost, it seeks to fill a critical gap in the existing body of literature, by providing a comprehensive exploration of CW index configurations, grounded in rigorous statistical analysis. It is worth noting that while there have been efforts such as the CRIX study to conduct analyses on crypto indices broadly, no study has yet homed in specifically on the Ethereum market, marking this research as pioneering in its field [7]. Through a detailed scrutiny of rebalancing intervals and constituent counts, this study lays down a nuanced approach to indexing in the Ethereum market, paving the way for strategies that are both lucrative and risk-mitigated. The initiative hence stands as the inaugural deep-dive into Ethereum-specific indices.

Beyond its contribution to the academic discourse, this research opens up fertile ground for the development of new crypto index products. By unraveling the optimal strategies for CW index constructions, it offers a blueprint for products that are not only robust and efficient but also finely tuned to the pulse of the Ethereum market, thereby serving the needs of both retail and institutional participants.

# 2 Index Methodology

# 2.1 Data Sources

Backtesting of the CW Index requires high-quality data procured from two primary sources. The initial source is historical snapshots obtained from CoinMarketCap, predominantly employed to identify the tokens with the highest market capitalization [3]. These snapshots, captured exclusively on Sundays, facilitate a backtesting timeline commencing on January 5, 2020 (05.01.2020) and culminating on September 3, 2023 (03.09.2023). The second and more vital source leveraged is the Coingecko Pro API, a revered repository that furnishes precise historical data encompassing various metrics such as free-float market capitalization [2]. This data is instrumental in index rebalancing and reconstitution, serving as a cornerstone for the meticulous backtesting of diverse CW indices.

Engaging both data repositories not only ensures a resilient foundation for backtesting but also safeguards the reliability of the CW indices analyzed. However, it is essential to approach this data with a discerning eye, cognizant of its hypothetical nature. The backtested data delineates potential index performance prior to an official launch, bereft of a guarantee for future outcomes, thereby accentuating the necessity for informed and judicious interpretation of the results garnered.

# 2.2 Eligibility Criteria

To construct a Capitalization-Weighted (CW) Index that accurately reflects the Ethereum ecosystem, a stringent set of eligibility criteria is followed, rooted in the International Token Classification (ITC) framework developed by the International Token Standardization Association (ITSA) [1]. Establishing robust eligibility criteria is pivotal; it not only ensures that the index is built upon a foundation of tokens that hold genuine potential and align with the specified standards but also aids in averting risks associated with volatility and unpredictable market behaviors, thereby engendering a reliable and stable index. In the following subsections, the criteria are delineated, categorized into fundamental groups that address the distinct attributes of prospective tokens.

#### 2.2.1 Basic Token Characteristics

Tokens must satisfy the following fundamental attributes:

- Affiliation to the Ethereum ecosystem.
- Non-classification as a security by regulatory authorities in the US and EU territories.
- Alignment with specific Economic Purpose (ITC) dimensions, notably:
  - 1. Utility Token, which includes:
    - Governance Token
    - Ownership Token
    - Settlement and Governance Token
- Exclusion from certain Economic Purpose (ITC) dimensions such as:
  - 1. Payment Token
  - 2. Certain Utility Tokens, specifically:
    - Settlement Token
    - Access Token
    - Settlement and Access Token
  - 3. Investment Token
  - 4. Tokens with other economic purposes

#### 2.2.2 Token Supply Features

Tokens must meet the following supply criteria:

- Predictable supply over a four-year period.
- A minimum of 10% of the projected four-year supply in current circulation.
- Absence of locking mechanisms that significantly disadvantage index investors.

#### 2.2.3 Project Traction Features

Project-related criteria include:

- Wide recognition for developing a substantial protocol or product.
- Non-affiliation with Ponzi schemes or other fraudulent activities.
- Significant protocol usage demonstrated through metrics such as total value locked (TVL) or user engagement.
- Operational history of at least 180 days.

#### 2.2.4 Protocol Safety Features

Safety protocols dictate the following:

- Security verification through a smart contract audit.
- Effective and transparent resolution of safety incidents.
- Adequate liquidity across diverse trading platforms.

These criteria, rooted in the ITSA's ITC framework, facilitate the selection of secure and viable tokens, fostering transparency and safety in the ever-evolving Ethereum market landscape.

#### 2.3 Index Calculation

Central to this study is the application of the mathematical principles underlying the Laspeyres index, traditionally employed to monitor relative price changes over a stipulated timeline involving a fixed basket of goods. Leveraging this mathematical framework affords a rigorous approach to computing the index level in the Ethereum market, as delineated by the formula:

$$Index Level = \frac{(\sum (P_i \times Q_i))}{Divisor}$$

Here,  $P_i$  and  $Q_i$  stand for the price and the free-float quantity of the *i*th constituent at a given point in time, respectively. The denominator, termed the "Divisor," is instrumental in maintaining the index's integrity across diverse market conditions and structural configurations, accounting for adjustments rooted in the base period of the Laspeyres index [5].

The role of the Divisor transcends a mere constant; it undergoes recalibrations to sustain the index's continuity and consistency, adapting to shifts in the market dynamics, including alterations in the constituent counts and rebalancing intervals. The recalibration process adheres to the following mathematical representation, where the Divisor at a specific time period i (Divisor<sub>i</sub>) is recalculated grounded on the total market capitalization at the current and preceding time periods, t and t-1 respectively [5]:

$$Divisor_i = \frac{\left(\sum (P_{it} \times Q_{it})\right)}{\left(\sum (P_{i(t-1)} \times Q_{i(t-1)})\right)}$$

The analytical endeavor encompasses a deep-seated exploration of the intricate processes of index calculation and divisor adjustment within the Ethereum ecosystem, steering towards a comprehensive analysis that embodies the multifaceted nature of the Ethereum market. This approach intends to pinpoint the optimal constituent count and rebalancing frequency, thus offering a mathematical blueprint for a robust Ethereum-based Capitalisation-Weighted Index grounded in precision and analytical rigor.

# 2.4 Experimental Design

The experimental design aims to facilitate in-depth insights into the diverse performances of the CW Index across different configurations, focusing on constituent variability and rebalancing intervals.

Constituent Variability: The investigation commenced with a meticulous exploration to ascertain the ideal number of constituents, starting with a minimal ensemble of merely 5 tokens to glean an understanding of the dynamics of a more concentrated index. Subsequently, larger sets comprising 10, 20, and ultimately 30 tokens were examined, engendering a comprehensive perception of the performance trade-offs between an index with a narrow focus and one characterized by broader inclusion based on capitalization weights.

Rebalancing Intervals: Recognizing the considerable influence of rebalancing frequency on both the index performance and the upkeep costs, six distinct intervals were analyzed: weekly (1 week), biweekly (2 weeks), monthly (4 weeks), bi-monthly (8 weeks), quarterly (12 weeks), and semi-annually (24 weeks). This step-wise strategy facilitated an acute scrutiny of the complex interaction between market responsiveness and potential costs arising from index turnover, thereby enriching the understanding of the impact of rebalancing timings on performance and efficiency within the Ethereum ecosystem.

# 3 Empirical Results

## 3.1 Performance Overview

This section provides a meticulous analysis dissecting the Capitalization-Weighted (CW) Index in the Ethereum market. The analysis unravels the intricate dynamics between varying rebalancing intervals (Wks) and constituent counts (Cons.), focusing on a range of metrics including Total Return, Mean Return, and Median Return, along with volatility measures such as Standard Deviation (Std Dev). Risk-adjusted performance metrics such as the Sharpe Ratio (S. Ratio) and Sortino Ratio (So. Ratio) are employed, coupled with the Max Drawdown (Max D.D.) to articulate potential worst-case scenarios in investment downturns.

| Rank | Wks | Cons. | Total Ret. | Mean Ret. | Median Ret. | Std Dev | S. Ratio | So. Ratio | Max D.D. |
|------|-----|-------|------------|-----------|-------------|---------|----------|-----------|----------|
| 1    | 8   | 30    | 556.65     | 1.99      | 1.54        | 14.02   | 1.83     | 2.83      | -84.11   |
| 2    | 1   | 30    | 536.28     | 1.96      | 1.72        | 13.83   | 1.82     | 2.76      | -83.04   |
| 3    | 2   | 30    | 510.77     | 1.93      | 1.70        | 13.79   | 1.79     | 2.72      | -83.03   |
| 4    | 4   | 30    | 506.04     | 1.95      | 1.71        | 14.02   | 1.79     | 2.74      | -83.81   |
| 5    | 1   | 20    | 464.79     | 1.90      | 1.37        | 13.89   | 1.75     | 2.65      | -82.63   |
| 6    | 2   | 20    | 447.63     | 1.88      | 1.37        | 13.89   | 1.73     | 2.62      | -82.59   |
| 7    | 4   | 20    | 429.10     | 1.89      | 1.33        | 14.11   | 1.71     | 2.62      | -83.30   |
| 8    | 24  | 30    | 393.59     | 1.82      | 1.44        | 13.91   | 1.66     | 2.54      | -84.19   |
| 9    | 8   | 20    | 381.72     | 1.83      | 1.33        | 14.07   | 1.65     | 2.53      | -83.72   |
| 10   | 2   | 5     | 346.34     | 1.86      | 0.75        | 14.73   | 1.61     | 2.56      | -85.98   |
| 11   | 12  | 30    | 321.87     | 1.74      | 1.41        | 13.86   | 1.57     | 2.37      | -83.53   |
| 12   | 1   | 10    | 310.94     | 1.76      | 1.42        | 14.13   | 1.56     | 2.39      | -84.99   |
| 13   | 2   | 10    | 306.82     | 1.74      | 1.24        | 14.10   | 1.55     | 2.38      | -84.76   |
| 14   | 24  | 20    | 281.32     | 1.69      | 1.38        | 13.95   | 1.51     | 2.29      | -85.78   |
| 15   | 12  | 20    | 271.69     | 1.68      | 1.34        | 13.95   | 1.49     | 2.26      | -83.16   |
| 16   | 8   | 10    | 267.20     | 1.71      | 1.17        | 14.27   | 1.49     | 2.30      | -87.09   |
| 17   | 4   | 10    | 249.25     | 1.70      | 1.33        | 14.40   | 1.46     | 2.27      | -85.48   |
| 18   | 8   | 5     | 246.77     | 1.69      | 0.75        | 14.38   | 1.46     | 2.28      | -87.77   |
| 19   | 1   | 5     | 228.31     | 1.70      | 0.75        | 14.66   | 1.44     | 2.26      | -88.17   |
| 20   | 24  | 5     | 216.44     | 1.66      | 0.75        | 14.48   | 1.42     | 2.18      | -86.51   |
| 21   | 24  | 10    | 214.93     | 1.64      | 1.09        | 14.32   | 1.40     | 2.16      | -88.06   |
| 22   | 4   | 5     | 199.24     | 1.70      | 0.74        | 15.12   | 1.39     | 2.23      | -89.01   |
| 23   | 12  | 5     | 105.73     | 1.46      | 0.74        | 14.65   | 1.18     | 1.81      | -88.42   |
| 24   | 12  | 10    | 94.29      | 1.38      | 1.20        | 14.28   | 1.12     | 1.70      | -87.79   |

Table 1: Performance ranking based on various metrics with different rebalancing intervals and number of constituents.

The overarching landscape exhibited in the table showcases a substantial divergence in the performances at different ranks based on a diverse set of metrics. Evident from the data, higher rebalancing intervals (Wks) paired with a greater number of constituents (Cons.) generally foster more favorable Total Return outcomes. Additionally, it is observed that an increase in the number of constituents

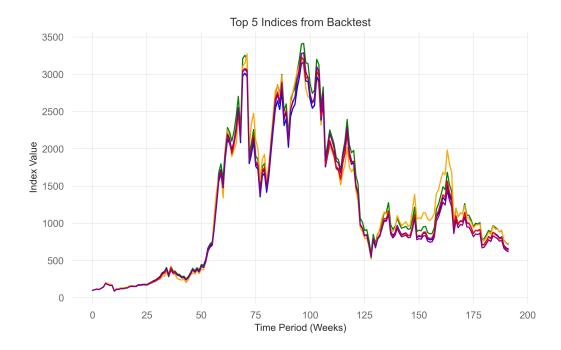


Figure 1: Comparative Analysis of the Top 5 Backtested Indices. The depiction articulates the performance of the top five backtested indices over a specified period, highlighting the variations in key metrics such as Total Return, Mean Return, and Standard Deviation. It is pertinent to note the superior performance exhibited by configurations with shorter rebalancing intervals and diverse constituent counts.

tends to alleviate the Max Drawdown value, hinting at a potential reduction in risk through a diversified portfolio.

The top performers in the CW indices predominantly favor a constituent count of 30, with rebalancing intervals fluctuating between 1 and 8 weeks. The index securing the first rank notably achieved the highest Total Return of 556.65% coupled with commendable Mean and Median Returns. Furthermore, it registered impressive Sharpe and Sortino Ratios, which depict a strong risk-adjusted performance.

Delving into the intricacies of standard deviation, it varies broadly from 13.79 to 15.12 across distinct configurations, with the portfolio ranked 22 showcasing the highest figure. This metric significantly denotes the volatility harbored by the portfolios, suggesting that a diminished value could represent a less risky portfolio.

The metric of maximum drawdown also presents itself as a critical player in the analytical narrative, revealing its apex at an 89.01% dip in the 22nd rank. A comprehensive analysis would extend to coupling Max Drawdown with other pivotal metrics to delineate the worst-case scenarios and gauge the resilience ingrained in varying strategies.

A notable trend that surfaces is the harmony between the S. Ratio and So. Ratio, illustrating a consistent appraisal of risk-adjusted performance across both parameters. The higher values in these ratios, especially as seen in the first rank, affirm a superior risk-adjusted performance.

To augment this analysis, Figure 1 delineates the comparative performances of various configurations, elucidating the nuanced relationship between rebalancing intervals and constituent counts. The portrayal underscores the superior performances attained through higher constituent counts paired with diverse rebalancing intervals.

In advancing the research, a detailed examination of the parameters of Total Return, Standard Deviation, and Sharpe Ratio is undertaken to unravel the fundamental dynamics steering the Ethereum market's CW Index performance. Preliminary observations suggest the efficacy of strategies that employ larger constituent counts and moderate rebalancing intervals. This endeavor seeks to pave a path balancing return and risk optimally, beckoning a closer inspection of individual metrics to facilitate informed strategic decisions.

# 3.2 Total Return Analysis

The premier position in total returns is held by the configuration that leverages an 8-week rebalancing interval coupled with a constituent count of 30, thereby recording a staggering total return of 556.65%. Following closely, the configurations employing rebalancing intervals of 1, 2, and 4 weeks, all with 30 constituents, exhibit total returns exceeding 500%. It is pertinent to note that the configuration standing at rank 5 exhibits a 20 constituent count and a 1-week rebalancing interval, marking a total return of 464.79%, thereby underlining the significant return potential even with a reduced constituent count.

| Rank | Wks | Cons. | Total Ret. | Mean Ret. | Median Ret. | Std Dev | S. Ratio | So. Ratio | Max D.D. |
|------|-----|-------|------------|-----------|-------------|---------|----------|-----------|----------|
| 1    | 8   | 30    | 556.65     | 1.99      | 1.54        | 14.02   | 1.83     | 2.83      | -84.11   |
| 2    | 1   | 30    | 536.28     | 1.96      | 1.72        | 13.83   | 1.82     | 2.76      | -83.04   |
| 3    | 2   | 30    | 510.77     | 1.93      | 1.70        | 13.79   | 1.79     | 2.72      | -83.03   |
| 4    | 4   | 30    | 506.04     | 1.95      | 1.71        | 14.02   | 1.79     | 2.74      | -83.81   |
| 5    | 1   | 20    | 464.79     | 1.90      | 1.37        | 13.89   | 1.75     | 2.65      | -82.63   |

Table 2: Top 5 indices by Total Return.

While the top ranks are predominantly adorned by configurations with a 30 constituent count, it brings forth the compelling argument that a diversified portfolio, represented here by a higher constituent count, holds the potential to accrue substantially higher total returns. Concurrently, a striking observation is the prominence of shorter rebalancing intervals, under 8 weeks, in securing superior total returns, showcasing the favorable impact of more frequent rebalances in navigating the dynamic Ethereum market landscape.

The decline in total return from rank 1 to rank 5 exhibits a non-linear pattern, emphasizing a more pronounced decrease initially that levels off to some degree further down the ranks. This suggests that although the leading configurations present considerable return opportunities, the disparity in returns starts to level out, indicating a diminishing return on total yield when navigating down the top five rankings.

Drawing interpretations from the analyzed data, it surfaces that a strategy encapsulating a larger constituent count tends to harbor a higher propensity for optimal total returns, arguably due to the diversified nature mitigating undue exposures and fostering a resilient portfolio structure. Moreover, the pivotal role of rebalancing intervals in sculpting the total return landscape cannot be overlooked, indicating a tendency for shorter intervals to harness greater returns in the turbulent waters of the Ethereum market, perhaps owing to the agile response to market fluctuations that frequent rebalancing affords.

Furthermore, the data suggests a diminishing disparity in total returns as one progresses through the top five ranks. This alludes to a scenario where investors seeking slightly conservative strategies might not compromise extensively on potential total return, provided they align with configurations within the top performance echelon.

#### 3.3 Sharpe Ratio Analysis

The Sharpe Ratio, a benchmark for risk-adjusted returns, presents a narrative where the 8-week rebalancing interval paired with 30 constituents emerges victorious with a ratio of 1.83. This stellar performance is closely followed by configurations with shorter rebalancing intervals of 1 and 2 weeks, both maintaining the 30 constituent benchmark and achieving Sharpe Ratios of 1.82 and 1.79, respectively. Cascading down the top rankings, the 4-week interval with 30 constituents and the 1-week interval with 20 constituents complete the top 5 with ratios of 1.79 and 1.75 respectively, painting a picture of high risk-adjusted returns coupled with diversified constituent counts.

| Rank | Wks | Cons. | Total Ret. | Mean Ret. | Median Ret. | Std Dev | S. Ratio | So. Ratio | Max D.D. |
|------|-----|-------|------------|-----------|-------------|---------|----------|-----------|----------|
| 1    | 8   | 30    | 556.65     | 1.99      | 1.54        | 14.02   | 1.83     | 2.83      | -84.11   |
| 2    | 1   | 30    | 536.28     | 1.96      | 1.72        | 13.83   | 1.82     | 2.76      | -83.04   |
| 3    | 2   | 30    | 510.77     | 1.93      | 1.70        | 13.79   | 1.79     | 2.72      | -83.03   |
| 4    | 4   | 30    | 506.04     | 1.95      | 1.71        | 14.02   | 1.79     | 2.74      | -83.81   |
| 5    | 1   | 20    | 464.79     | 1.90      | 1.37        | 13.89   | 1.75     | 2.65      | -82.63   |

Table 3: Top 5 indices by Sharpe Ratio.

Delving deeper, it is apparent that the top performers in terms of Sharpe ratio largely mirror those leading in total returns, suggesting a strong correlation between high total returns and favorable risk-adjusted outcomes, as assessed by the Sharpe ratio. The core inference drawn here is the pronounced efficacy of higher constituent counts, a strategy vindicated across both total and risk-adjusted return analyses, reinforcing the hypothesis of diversity being a potent tool in risk mitigation and performance enhancement.

A nuanced observation reveals a minor decrement in the Sharpe ratio when transitioning from an 8-week to a 1-week rebalancing strategy, hinting at a scenario where longer rebalancing intervals might slightly edge out in risk-adjusted performance. This could potentially be attributed to lower exposure to short-term market volatilities, thereby offering a more stable and risk-averse investment pathway.

The analysis, therefore, advocates for a harmonized strategy leveraging longer rebalancing intervals and higher constituent counts, thereby promising not only substantial returns but also a risk-mitigated pathway. It beckons a strategy that envisions a broader market spectrum, capitalizing on market synergies through diversified portfolios that stand resilient in a fluctuating market, promising a strategy that is both lucrative and risk-mitigated.

# 3.4 Standard Deviation Analysis

Delving into the analysis of standard deviation (Std Dev), a key indicator of investment risk that measures the variance or dispersion of a set of values, a landscape emerges where configurations with the least standard deviation stand out prominently.

|   | Rank | Wks | Cons. | Total Ret. | Mean Ret. | Median Ret. | Std Dev | S. Ratio | So. Ratio | Max D.D. |
|---|------|-----|-------|------------|-----------|-------------|---------|----------|-----------|----------|
|   | 1    | 2   | 30    | 510.77     | 1.93      | 1.70        | 13.79   | 1.79     | 2.72      | -83.03   |
|   | 2    | 1   | 30    | 536.28     | 1.96      | 1.72        | 13.83   | 1.82     | 2.76      | -83.04   |
|   | 3    | 12  | 30    | 321.87     | 1.74      | 1.41        | 13.86   | 1.57     | 2.37      | -83.53   |
|   | 4    | 1   | 20    | 464.79     | 1.90      | 1.37        | 13.89   | 1.75     | 2.65      | -82.63   |
| İ | 5    | 2   | 20    | 447.63     | 1.88      | 1.37        | 13.89   | 1.73     | 2.62      | -82.59   |

Table 4: Top 5 indices by Standard Deviation.

Leading the table is the configuration with a 2-week rebalancing interval and 30 constituents, exhibiting the lowest standard deviation of 13.79. This is followed closely by the 1-week rebalancing strategy, also with 30 constituents, demonstrating a standard deviation of 13.83. Progressing further, the 12-week strategy with 30 constituents takes the third position, reflecting a marginally elevated standard deviation of 13.86. The fourth and fifth ranks are held by configurations with 20 constituents, coupled with 1 and 2-week rebalancing intervals, both portraying a standard deviation of 13.89.

Upon close inspection, it is apparent that the configurations with 30 constituents dominate the lower spectrum of standard deviation, barring the configurations holding the fourth and fifth positions. This underlines a potent strategy where a higher constituent count potentially fosters a reduction in standard deviation, thereby mitigating investment risks through a diversified portfolio that cushions against market volatilities.

An astute observation reveals a narrow range of standard deviation values across the top ranks, hinting at a landscape where the standard deviation does not drastically fluctuate across different configurations in the top echelon. This suggests a compact space where the differences in risk as gauged through standard deviation are nuanced rather than starkly contrasted, offering investors a range of options that do not substantially diverge in terms of risk profiles.

In retrospect, the analysis elucidates a delicate balance where both the constituent count and rebalancing intervals play pivotal roles in sculpting the standard deviation landscape. The data propels the inference that a strategy anchored in higher constituent counts paired with either short or moderately long rebalancing intervals stands to offer a resilient and risk-mitigated pathway in the investment arena.

## 3.5 Statistical Validation

In this section, the empirical results are validated statistically, analyzing the influence of varying rebalancing intervals (Wks) and constituent counts (Cons.) on the Capitalisation-Weighted (CW) Index's total return in the Ethereum market. The Ordinary Least Squares (OLS) regression model is leveraged to unravel the underlying statistical narratives in the dataset.

The analysis commences with an Analysis of Variance (ANOVA) to scrutinize the total return concerning the rebalancing intervals and the number of constituents, the results of which are tabulated below:

Table 5: ANOVA Results

| Source   | sum_sq     | df   | F      | PR(¿F)    |
|----------|------------|------|--------|-----------|
| Wks      | 119432.817 | 5.0  | 16.907 | 1.076e-05 |
| Cons.    | 249293.236 | 3.0  | 58.818 | 1.586e-08 |
| Residual | 21192.028  | 15.0 | NaN    | NaN       |

The ANOVA uncovers a significant impact of both the rebalancing intervals and the number of constituents on the total return, as evidenced by the extremely low p-values  $(1.076 \times 10^{-5})$  for Wks and  $1.586 \times 10^{-8}$  for Cons.).

Subsequent to this, the results of the OLS regression analysis are presented:

Table 6: OLS Regression Results

|           | coef     | std err | t      | P¿—t— | [0.025, 0.975]     |
|-----------|----------|---------|--------|-------|--------------------|
| Intercept | 186.8904 | 38.870  | 4.808  | 0.000 | [105.809, 267.972] |
| Wks       | -3.4152  | 3.356   | -1.018 | 0.321 | [-10.415, 3.585]   |
| Cons.     | 11.9114  | 2.059   | 5.784  | 0.000 | [7.616, 16.207]    |
| Wks:Cons. | -0.1648  | 0.178   | -0.927 | 0.365 | [-0.536, 0.206]    |

The regression analysis, boasting a significant R-squared value of 0.778, demonstrates that the model can account for approximately 77.8% of the variance in the total return, underscoring the robustness of the model. The significant coefficient for the number of constituents (Cons.) solidifies the argument for a strategy favoring a higher constituent count. However, the weeks (Wks) show a negative yet statistically insignificant coefficient, suggesting a potential area for further research to understand its nuanced role in determining total returns. The interaction term between Wks and Cons. also requires a more intricate analysis, given its statistically insignificant p-value.

In conclusion, this validation accentuates the criticality of adopting a statistically grounded strategy in navigating the dynamic Ethereum market landscape, underscoring a strategy that capitalizes on a higher constituent count to enhance the CW Index's total return. The regression analysis substantiates the empirical findings, fostering a foundational base for deeper exploration in succeeding sections of the paper.

# 4 Conclusion

In the fast-paced and continually evolving landscape of decentralized finance, this research embarked on an unprecedented journey to untangle the intricacies of the capitalization-weighted (CW) index within the Ethereum ecosystem. Through meticulous exploration of varying rebalancing intervals and constituent counts, a robust groundwork has been established that paves the way for a nuanced approach to indexing in the Ethereum market, a domain characterized by its dynamic nature and rich diversity.

The empirical findings highlight a critical interplay between the rebalancing intervals and the number of constituents in determining the optimal configuration for the CW index. An 8-week rebalancing interval harmonized with a 30 constituents strategy surfaced as a potent configuration, promising a stellar total return of 556.65% and a remarkable Sharpe ratio of 1.83. The study underscores the necessity of a balanced strategy that leverages a higher constituent count to foster superior outcomes, advocating for a harmonized strategy that optimizes returns while mitigating substantial risks. These insights are pivotal, holding substantial implications for investors, asset managers, and the broader cryptocurrency community, guiding them towards informed decision-making and fostering the birth of new crypto index products.

However, it is imperative to approach these results with a discerning eye, considering the potential risks underscored by the Max Drawdown metric, which advocates for a cautious approach that balances the allure of high returns with risk mitigation strategies. The statistical validation further reinforced

these findings, with the regression analysis elucidating a substantial 77.8% of the variance in total returns, thereby validating the robustness of the model and emphasizing a strategy favoring a higher constituent count to enhance the CW index's total return.

Advancing further, this research establishes a foundation for in-depth investigations rooted in statistical precision. Critical dynamics have been elucidated, yet the Ethereum market, with its volatility and intricacies, demands ongoing research to foster a more comprehensive understanding. Future endeavors could delve deeper into understanding the nuanced role of rebalancing intervals in determining total returns, exploring the potential interaction effects in greater detail, and possibly unearthing innovative methodologies that could revolutionize indexing in the Ethereum market.

In conclusion, this research marks a significant stride in understanding the Ethereum market's complex dynamics. Through rigorous analysis, a pathway to optimized index configuration has been illuminated, fostering a landscape ripe with opportunities for both retail and institutional participants. The insights gleaned from this study intend to serve as a beacon, guiding stakeholders towards informed and strategically sound decisions, thereby contributing to shaping a more robust, efficient, and insightful future for Ethereum market indexing.

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