

# Problem A

## Not the Best

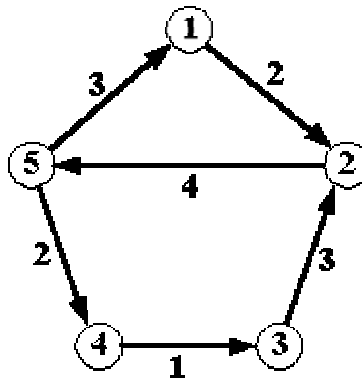
**Input:** standard input

**Output:** standard output

**Time Limit:** 1 second

*Abul* is not the best student in his class; neither is he the best player in his team. Not that he is bad; he is really good, but unfortunately not the best.

Last semester our “not quite the best” *Abul* took a course on algorithms. In one of the assignments he was required to find the shortest path from a given vertex  $x$  to another vertex  $y$  in a weighted directed graph. As you have probably already guessed, he rarely managed to find the shortest path; instead he always ended up finding the  $k^{\text{th}}$  ( $2 \leq k \leq 10$ ) shortest path from  $x$  to  $y$ . If he was fortunate enough and the shortest  $k$  paths from  $x$  to  $y$  had the same length, he was given credit for his solution.



For example, for the graph above, *Abul* was asked to find the shortest path from vertex 5 to vertex 2. The shortest 7 paths from vertex 5 to vertex 2 are listed below in non-decreasing order of length. For this graph *Abul* was able to find the 5<sup>th</sup> shortest path which could be either  $5 \rightarrow 4 \rightarrow 3 \rightarrow 2 \rightarrow 5 \rightarrow 1 \rightarrow 2$  or  $5 \rightarrow 1 \rightarrow 2 \rightarrow 5 \rightarrow 4 \rightarrow 3 \rightarrow 2$ , each with length 15.

<i>Path</i>	<i>Length</i>
$5 \rightarrow 1 \rightarrow 2$	5
$5 \rightarrow 4 \rightarrow 3 \rightarrow 2$	6
$5 \rightarrow 1 \rightarrow 2 \rightarrow 5 \rightarrow 1 \rightarrow 2$	14
$5 \rightarrow 4 \rightarrow 3 \rightarrow 2 \rightarrow 5 \rightarrow 1 \rightarrow 2$	15
$5 \rightarrow 1 \rightarrow 2 \rightarrow 5 \rightarrow 4 \rightarrow 3 \rightarrow 2$	15
$5 \rightarrow 4 \rightarrow 3 \rightarrow 2 \rightarrow 5 \rightarrow 4 \rightarrow 3 \rightarrow 2$	16
$5 \rightarrow 1 \rightarrow 2 \rightarrow 5 \rightarrow 1 \rightarrow 2 \rightarrow 5 \rightarrow 1 \rightarrow 2$	23

Given a description of the graph, source vertex  $x$ , target vertex  $y$ , and the value of  $k$ , you need to find out the length of the path *Abul* computed. You may assume that there exists at least one path from  $x$  to  $y$  in the given graph.

## Input

The input may contain multiple test cases.

The first line of each test case contains two integers  $n$  ( $2 \leq n \leq 100$ ) and  $m$  ( $1 \leq m \leq 1000$ ) giving respectively the number of vertices, and the number of edges in the graph. Each vertex in the graph is identified by a unique integer in  $[1, n]$ . The second line of the test case contains the values of  $x, y$  and  $k$  ( $1 \leq x, y \leq 100, x \neq y, 2 \leq k \leq 10$ ). Each of the next  $m$  lines contains three integers  $u, v$  and  $l$  ( $1 \leq u, v \leq 100, 0 \leq l \leq 10000$ ) specifying a directed edge of length  $l$  from vertex  $u$  to vertex  $v$ .

The input terminates with two zeros for  $n$  and  $m$ .

## Output

For each test case in the input output a line containing an integer giving the length of the  $k^{\text{th}}$  shortest path in the graph. If the graph does not have at least  $k$  paths from  $x$  to  $y$ , output a  $-1$  instead.

### Sample Input

```
3 3
1 3 4
1 3 3
1 2 4
2 3 5
5 6
5 2 5
1 2 2
2 5 4
3 2 3
4 3 1
5 1 3
5 4 2
2 2
1 2 3
1 2 5
2 2 2
0 0
```

### Output for Sample Input

```
-1
15
9
```

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