

Problem G

Matrix

Input: Standard Input
Output: Standard Output
Time Limit: 2 Seconds

[Preliminaries]

(He who has already studied linear algebra may skip this part)

A matrix is composed of $n \times n$ elements. Formally,

$$A = \begin{bmatrix} a_{11} & a_{12} & \cdots & a_{1n} \\ a_{21} & a_{22} & \cdots & a_{2n} \\ \vdots & & & \vdots \\ a_{n1} & a_{n2} & \cdots & a_{nn} \end{bmatrix} \text{ is an } n \times n \text{ matrix.}$$

for example, $A = \begin{bmatrix} 1 & 2 \\ 3 & 4 \end{bmatrix}$ is a 2×2 matrix.

Two operations on matrices will be used in this problem:

1. $A + k$ (A is an $n \times n$ matrix, k is an integer)

all the elements in the MAIN diagonal is added by k . that is

$$A + k = \begin{bmatrix} a_{11} & a_{12} & \cdots & a_{1n} \\ a_{21} & a_{22} & \cdots & a_{2n} \\ \vdots & & & \vdots \\ a_{n1} & a_{n2} & \cdots & a_{nn} \end{bmatrix} = \begin{bmatrix} a_{11} + k & a_{12} & \cdots & a_{1n} \\ a_{21} & a_{22} + k & \cdots & a_{2n} \\ \vdots & & & \vdots \\ a_{n1} & a_{n2} & \cdots & a_{nn} + k \end{bmatrix}$$

For example,

$$\begin{bmatrix} 1 & 2 \\ 3 & 4 \end{bmatrix} + 5 = \begin{bmatrix} 6 & 2 \\ 3 & 9 \end{bmatrix}. \text{ } A - k \text{ is defined } A + (-k), \text{ so } \begin{bmatrix} 1 & 2 \\ 3 & 4 \end{bmatrix} - 5 = \begin{bmatrix} -4 & 2 \\ 3 & -1 \end{bmatrix}$$

2. $A * B$ (both A and B are $n \times n$ matrices)

$$\text{let } A = \begin{bmatrix} a_{11} & a_{12} & \cdots & a_{1n} \\ a_{21} & a_{22} & \cdots & a_{2n} \\ \vdots & & & \vdots \\ a_{n1} & a_{n2} & \cdots & a_{nn} \end{bmatrix}, B = \begin{bmatrix} b_{11} & b_{12} & \cdots & b_{1n} \\ b_{21} & b_{22} & \cdots & b_{2n} \\ \vdots & & & \vdots \\ b_{n1} & b_{n2} & \cdots & b_{nn} \end{bmatrix},$$

$$\text{and } C = A \times B = \begin{bmatrix} c_{11} & c_{12} & \cdots & c_{1n} \\ c_{21} & c_{22} & \cdots & c_{2n} \\ \vdots & & & \vdots \\ c_{n1} & c_{n2} & \cdots & c_{nn} \end{bmatrix},$$

then we have:

$$c_{ij} = \sum_{k=1}^n a_{ik} b_{kj} = a_{i1} b_{1j} + a_{i2} b_{2j} + \cdots + a_{in} b_{nj}$$

For example,

$$\begin{bmatrix} 1 & 2 \\ 3 & 4 \end{bmatrix} \times \begin{bmatrix} 5 & 6 \\ 7 & 8 \end{bmatrix} = \begin{bmatrix} 5+14 & 6+16 \\ 15+28 & 18+32 \end{bmatrix} = \begin{bmatrix} 19 & 22 \\ 43 & 50 \end{bmatrix}$$

Well, I have no time to explain why matrix multiplication is defined like this. Please just remember it.

[Problem]

Find a matrix root of this equation:

$(A + k_1)(A+k_2)(A+k_3)...(A+k_m) = O$ where $k_1, k_2...k_m$ are distinct integers.

That is, EVERY ELEMENT OF the matrix computed from the left is zero.

for example,

$A = \begin{bmatrix} 1 & 4 \\ 2 & 3 \end{bmatrix}$ is a matrix root of the equation $(A+1)(A-5) = O$, since

$$(A+1)(A-5) = \begin{bmatrix} 2 & 4 \\ 2 & 4 \end{bmatrix} \times \begin{bmatrix} -4 & 4 \\ 2 & -2 \end{bmatrix} = \begin{bmatrix} -8+8 & 8-8 \\ -8+8 & 8-8 \end{bmatrix} = \begin{bmatrix} 0 & 0 \\ 0 & 0 \end{bmatrix}$$

It can be proven that there are infinitely many solutions, however, I do not like trivial answer, so your answer must have at least $(n*n)/2$ non-zero elements.

Input

The first line contains the number of tests $t(1 \leq t \leq 15)$. Each case contains two lines. The first line contains an integer $m(1 \leq m \leq 30)$. The second line contains m integers, representing $k_1, k_2...k_m$ respectively. Absolute values of the integers are no greater than 100.

Output

For each test case, if no answer can be found, print -1. otherwise print n , indicating that you found an $n*n$ matrix root. the following n lines should be the matrix. It is guaranteed that if there is an answer, the smallest possible n is not greater than 50, so your n should also NOT be greater than 50. The absolute value of integers you gave should not be larger than 1000.

Sample Input

```
2
2
1 -5
2
1 -5
```

Output for Sample Input

```
2
1 4
2 3
2
1 4
2 3
```

Problemsetter: Rujia Liu, Member of Elite Problemsetters' Panel
Special thanks to Monirul Hasan