

## Problem D. Professor Lazy, Ph.D.

Input file:        `standard input`  
Output file:      `standard output`

Professors are very motivated when they have to travel abroad for a conference (of course, if fees are paid by the university), but they don't have the same attitude when the moment to grade exams arrives.

Professor Lazy, Ph.D., has a particular way to grade exams (and very unfair, by the way). He puts all his exams in a box and then starts getting them out one by one in a totally random fashion. He assigns grade  $\alpha$  to the first exam that he gets out of the box, and grade  $\beta$  to the second exam that he gets out of the box. From that point on, he assigns a grade to each of the exams based on the grades of the previous two exams. What he does is that he takes the grade of the immediately previous exam, adds 1 and divides by the grade of the exam before the previous one.

For example, let's imagine that  $\alpha = 2$  and  $\beta = 3$ . This is what happens:

- The first exam gets  $\alpha = 2$ .
- The second exam gets  $\beta = 3$ .
- The previous two grades are  $\alpha$  and  $\beta$ , so the third exam gets  $\frac{(1 + \beta)}{\alpha} = \frac{(1 + 3)}{2} = 2$ .
- The previous two grades are  $\beta$  and  $\frac{(1 + \beta)}{\alpha}$ , so the fourth exam gets  $\frac{1 + \frac{(1 + \beta)}{\alpha}}{\beta} = \frac{1 + 2}{3} = 1$ .
- The procedure continues until he's done with all exams.

More formally, we can define the grade  $Q_n$  of the  $n$ th exam with a recurrence like this:

$$Q_n = \begin{cases} \alpha & \text{if } n = 0, \\ \beta & \text{if } n = 1, \\ \frac{1 + Q_{n-1}}{Q_{n-2}} & \text{if } n \geq 2. \end{cases}$$

Even this simple procedure is a lot of work for Professor Lazy, Ph.D., so he asks you to write a program to do it for him. He wants to spend all day long drinking coffee in the cafeteria with other professors. Given  $\alpha$ ,  $\beta$  and  $n$  find the value of  $Q_n$ .

Note that the grades do not necessarily lie inside a fixed range. They are just arbitrary integers.

### Input

The input contains several test cases (at most 1000). Each test case is described by three integer numbers  $\alpha$ ,  $\beta$  and  $n$  on a single line ( $1 \leq \alpha, \beta \leq 10^9$  and  $0 \leq n \leq 10^{15}$ ).

The last line of the input contains three zeros and should not be processed.

### Output

For each test case, write the value of  $Q_n$  in a single line. The input will be such that the value of  $Q_n$  is always an integer. Furthermore,  $Q_i$  will never be zero for  $0 \leq i \leq n$  (in other words, division by zero will never arise when evaluating the recurrence).

**Sample input and output**

standard input	standard output
1 1 0	1
1 2 1	2
5 9 2	2
2 3 3	1
7 4 4	2
2109 650790 344341899059516	650790
45861686 57 594261603792314	804591
2309734 21045930 808597262407955	2309734
0 0 0	