

Problem Set 10, due May 25, 2018 **(Accelerated Gradient Descent)**

Restart

Prove the following theorem as given in the lecture slides:

Theorem 1. *By repeatedly restarting the AGD algorithm, we can find an ε -optimal solution in $\mathcal{O}(1/\sqrt{\varepsilon})$ updates.*

Convergence in Iterate

Prove the following theorem as given in the lecture slides:

Theorem 2. *By repeatedly starting the AGD algorithm, for a μ -strongly convex and L -smooth function, we can find an ε -optimal solution in the value of iterate in $\mathcal{O}(\log(1/\varepsilon))$ updates where the constant in the big- \mathcal{O} is $\sqrt{\frac{L}{\mu}}$ compared to vanilla GD where the constant is $\frac{L}{\mu}$.*