# **PyNomo Documentation**

Release 0.3.0

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pyNomo is a python library for making nomographs (or nomograms) that are graphical calculators. Nomographs are defined as a python script that consists in most part of dictionaries.

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**CHAPTER** 

ONE

#### **INSTALLATION**

pyNomo is a python2 library and thus requires working python installation on the computer. pyNomo stands on the shoulders of (read: requires) the python packages: numpy, scipy and pyx that requires LaTeX-installation.

For editing pyNomo scripts any text browser works but integrated development environment (IDE) for python can speed up developments. Good free IDE alternatives are for example PyCharm community edition and spyder.

# 1.1 OSX Installation

In OSX Macports is an effective tool to manage open-source software. In the following a Mac-Ports environment is set for Python and pyNomo. *sudo* runs the commands as super-user and requires it's password to be given.

First install python 2.7

```
$ sudo port install python27
```

One can list available python versions on the system with command

```
$ sudo port select --list python
```

Select MacPorts python 2.7

```
$ sudo port select --set python python27
```

Install python package index tool (pip)

```
$ sudo port install py27-pip
```

and set it active

```
$ port select --set pip pip27
```

Now python environment should be correct to be run from /opt/local/Library/.... Now install other required packages.

```
$ sudo port install py27-numpy
$ sudo port install py27-scipy
$ sudo port install py27-pyx
$ sudo pip install pynomo
```

#### 1.2 Linux installation

In Debian Linux distribution and in its derivatives (for example Ubuntu and Raspbian) pynomo can be installed using *apt-get* with the following commands. *sudo* runs the commands as superuser and requires it's password to be given.

```
$ sudo apt-get -y install python
$ sudo apt-get -y install python-pyx
$ sudo apt-get -y install python-pip
$ sudo apt-get -y install python-numpy
$ sudo apt-get -y install python-scipy
$ sudo pip install pynomo
```

#### 1.3 Windows installation

- 1. Download and install python 2.7.x from www.python.org/downloads/ . pyNomo is not yet compatible with python 3.x.x
- 2. Download and install MIKTeX LaTeX -distribution from http://miktex.org/download.
- 3. Download and install numpy from sourceforge.net/projects/numpy.
- 4. Download and install scipy from sourceforge.net/projects/scipy.
- 5. Download and install PIL (python imaging library) from http://effbot.org/downloads/. PIL is required by some pyx packages. pynomo might work without PIL.

pyx (python graphics package) installation is more tricky. Either

- Download pyx 0.12.1 (python graphics package) from http://sourceforge.net/projects/pyx/files/pyx/0.12.1/PyX-0.12.1.tar.gz/download
- Uncompress the file *PyX-0.12.1.tar.gz* using for example 7-zip.
- Open command prompt (cmd) and go to the uncompressed folder that contains file *setup.py*.
- run command python setup.py install

or cross your fingers and just run:

```
> pip install --allow-external pyx pyx
```

on command prompt with administrative rights.

Finally pyNomo is installed either by downloading installer from http://sourceforge.net/projects/pynomo/ and by running it. Other choice to try is to run:

```
> pip install pynomo
```

on command line. Tedious, huh! If you find simpler Windows recipe, please email it to the maintainer of the project.

#### 1.4 Docker installation

Docker is a platform to create a sandboxed virtualized environments. In the following example

Dockerfile a virtualized Ubuntu is created that has pyNomo installed with all requirements:

```
FROM ubuntu
# Install required packages:
# python, pyx, pip, numpy, scipy, pynomo and their requirements
RUN apt-get update
RUN apt-get -y upgrade
RUN DEBIAN_FRONTEND=noninteractive apt-get -y install python
RUN DEBIAN_FRONTEND=noninteractive apt-get -y install python-pyx
RUN DEBIAN_FRONTEND=noninteractive apt-get -y install python-pip
{\tt RUN\ DEBIAN\_FRONTEND=} noninteractive\ apt-get\ -y\ install\ python-numpy
RUN DEBIAN_FRONTEND=noninteractive apt-get -y install python-scipy
RUN DEBIAN_FRONTEND=noninteractive pip install pynomo
# Add /app directory and make it working dir
RUN mkdir -p /app
ADD . /app
WORKDIR /app
# Set the default command to execute -> "python my_pynomo_file.py"
CMD ["python", "my_pynomo_file.py"]
```

Docker container (environment) *my\_pynomo\_docker* is built in the directory */my\_directory\_path* that has the file *Dockerfile* with command

```
$ docker build -t my_pynomo_docker .
```

Once environment is built and *my\_pynomo\_file.py* is in *directory* '/my\_directory\_path/pdf\_py\_dir/ one can run

```
$ docker run -i -v /my_directory_path/pdf_py_dir:/app my_pynomo_docker
```

that runs command python <code>my\_pynomo\_file.py</code> inside <code>/app directory</code> of container that is mapped to directory <code>/my\_directory\_path/pdf\_py\_dir</code> of the host system. That way a folder is used to share the script file and the generated pdf file between host system and the container (virtualized Linux environment).

# SOFTWARE DOCUMENTATION

Nomographs of PyNomo are constructed by writing a python script that defines the nomograph and calls class Nomographer to build the nomograph.

Nomograph is constructed by defining axis parameters that are used to build a block. Many blocks are possibly aligned with each other and construct the nomograph.

A simple example of pseudocode of typical PyNomo structure is the following:

```
from pynomo.nomographer import * # this loads the needed pynomo class
# define block 1
axis_params_1_for_block_1 = {...}
axis_params_2_for_block_1 = {...}
axis_params_3_for_block_1 = {...}
block_1 = {...}
# define block 2
axis_params_1_for_block_2 = {...}
axis_params_2_for_block_2 = {...}
axis_params_3_for_block_2 = {...}
block_2 = {...}
# define nomograph
main_params={
                \verb|'filename':'filename_of_nomograph.pdf', # filename of output|\\
               'block_params':[block_1,block_2],  # the blocks make the nomograph
'transformations':[('scale paper',)],  # these make (projective) transformations for the canves
# create nomograph
Nomographer(main_params)
```

It is to be noted that nomograph is defined as python dicts that constitute one dict that is passed to Nomographer class.

#### 2.1 Basic blocks

The following blocks are the core of PyNomo. These are used as easy building blocks for nomograph construction. If these do not suffice one can build as complex nomograph as one wishes by using determinants in type 9.

Туре 1	$F_1(u_1) + F_2(u_2) + F_3(u_3) = 0$	Three parallel lines
Type 2	$F_1(u_1) = F_2(u_2)F_3(u_3)$	"N" or "Z"
Туре 3	$F_1(u_1) + F_2(u_2) + \dots + F_N(u_N) = 0$	N parallel lines
Type 4	$\frac{F_1(u_1)}{F_2(u_2)} = \frac{F_3(u_3)}{F_4(u_4)}$	"Proportion"
Туре 5	$F_1(v) = F_2(x, u).$	"Contour"
Туре 6	u = u	"Ladder"
Type 7	$\frac{1}{F_1(u_1)} + \frac{1}{F_2(u_2)} = \frac{1}{F_3(u_3)}$	"Angle"
Туре 8	y = F(u)	"Single"
Туре 9	$ \begin{vmatrix} F_1(u_1[,v_1]) & G_1(u_1[,v_1]) & H_1(u_1[,v_1]) \\ F_2(u_2[,v_2]) & G_2(u_2[,v_2]) & H_2(u_2[,v_2]) \\ F_3(u_3[,v_3]) & G_3(u_3[,v_3]) & H_3(u_3[,v_3]) \end{vmatrix} = 0 $	"General"
Type 10	$F_1(u) + F_2(v)F_3(w) + F_4(w) = 0$	One curved line

# 2.2 Axes

Defining axes and their appearance is major work in nomograph construction. Different possibilities are illustrated in examples of axes parameters.

# 2.3 Combination of blocks

If a nomograph consists of many equations that are aligned, a compound nomograph is constructed.

# 2.4 Transformations

Scales shall be transformed in order to tune the appearance.

# 2.5 Manual

Article "Creating Nomograms with the PyNomo Software" by Ron Doerfler is a detailed manual for using PyNomo.

# **THREE**

# **AXES**

# 3.1 Common axis params

Table 3.1: Common axis params

parameter	default value	explanation
'ID'	'none'	String. To identify the axis.
'tag'	'none'	<b>String.</b> To align blocks w.r.t each other along axes with same tag.
'dtag'	'none'	<b>String.</b> To double-align blocks w.r.t each other along axes with same tag.
'title'	, ,	String. Axis title.
'title_x_shift'	0.0	<b>Float.</b> Title shift in x-direction.
'title_y_shift'	0.25	<b>Float.</b> Title shift in y-direction.
'scale_type'	'linear'	String. Scale type. Can be 'linear': linear scale. 'log': logarithmic scale. 'smart linear': linear scale with equal spacings. 'smart log': logarithmic scale with equal spacings, can also have negative values. 'manual point': Points and corresponding text positions are given manually in 'manual axis data'. No line is drawn. 'manual line': Ticks and corresponding text positions are given manually in 'manual axis data'.
'tick_levels'	4	Integer. How many levels (minor, minorminor, etc.) of ticks are drawn. Largest effect to 'linear' scale.
'tick_text_levels'	'3'	<b>Integer.</b> How many levels (minor, minorminor, etc.) of texts are drawn. Largest effect to 'linear' scale.
'tick_side'	'right'	String. Tick and text side in final paper. Can be: 'right'' or '''left'
'reference'	False	<b>Boolean.</b> If axis is treated as reference line that is a turning point.
'reference_padding'	'0.2'	<b>Float.</b> Fraction of reference line over other lines.
		Continued on next page

Table 3.1 – continued from previous page

parameter	default value	explanation
'manual_axis_data'	{}	<b>Dict.</b> Manually set tick/point positions
		and text positions. Could be for example:"{1:'1',3.14:r'\$pi\$',5:'5',7:'seven',10:'10
'title_draw_center'	False	<b>Boolean.</b> Title is drawn to center of line.
'title_distance_cente		String. To double-align blocks w.r.t each
01010_01000100_00000		other along axes with same tag.
'title_opposite_tick'	True	<b>Boolean.</b> Title in opposite direction w.r.t ticks.
'align_func'	lambda u:u	<b>func(u).</b> function to align different scales.
'align_x_offset'	0.0	<b>Float.</b> If axis is aligned with other axis, this value x offsets final scale.
'align_y_offset'	0.0	<b>Float.</b> If axis is aligned with other axis, this value y offsets final scale.
'text_format'	r'\$%4.4g\$'	<b>String.</b> Format for numbers in scale.
'extra_params'	[{},]	<b>Array of Dicts.</b> List of dictionary of params to be drawn additionally.
'text_distance_#'	x.x	<b>Float.</b> where $\#=0,1,2,3$ or 4. Distance of text from scale line. Number corresponds to the level, where 0 is the major tick and 4 is the most minor ticks.
'grid_length_#'	x.x	<b>Float.</b> where $\#=0,1,2,3$ or 4. Length of the tick. Number corresponds to the level, where 0 is the major tick and 4 is the most minor ticks.
'text_size_#'	x.x	Float. where #=0,1,2,3 or 4. Text size. For example: text.size.small, text.size.scriptsize or text.size.tiny. Number corresponds to the level, where 0 is the major tick and 4 is the most minor ticks.
'text_size_log_#'	x.x	Float. where #=0,1 or 2. Text size. For example: text.size.small, text.size.scriptsize or text.size.tiny. Number corresponds to the level, where 0 is the major tick and 2 is the most minor ticks.
'full_angle'	False	Boolean. If true, text can be upside down, otherwise +- 90 degrees from horizontal. Good foor example for full circle scales.
'extra_angle'	0.0	<b>Boolean.</b> Title is drawn to center of line.
'title_draw_center'	False	<b>Float.</b> Angle to rotate tick text from horizontal along tick.
'text_horizontal_alig	n_Eamser'	<b>Boolean.</b> Aligns tick text horizontally to center. Good when text rotated 90 degrees.
	•	Continued on next page

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Table 3.1 – continued from previous page

parameter	default value	explanation
'turn_relative'	False	Boolean. Side left or right is relative ac-
		cording to traveling of scale from min to
		max.
'arrow_size'	0.2	Float. Used with arrow scale.
'arrow_length'	1.0	Float. Used with arrow scale
'arrow_color'	color.rgb.black	Color. Used with arrow scale.
'axis_color'	color.rgb.black	Color. Color of axis.
'text_color'	color.rgb.black	Color. Color of tick texts.
'extra_titles'	[]	Array. List of extra title dicts for
		scale. Could be i.e."[{'dx':1.0,
		'dy':1.0, 'text':'extra title 1',
		'width':5, 'pyx_extra_defs':
		[color.rgb.red,text.size.Huge]}, {'text':
		'extra title 2'}]".
'base_start'	None	None/Float. Defines number with
		'base_stop' (instead of 'u_min' or
		'u_max') to find major tick decades.
'base_stop'	None	None/Float. Defines number with
		'base_start' (instead of 'u_min' or
		'u_max') to find major tick decades.

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# **FOUR**

# **MAIN PARAMS**

Main params define the top level properties of the nomograph.

# 4.1 List of main params

Table 4.1: General params

parameter	default value	explanation
'filename'	'pynomo_default.pdf'	String. Filename of generated filepdf
		and .eps formats supported.
'paper_height'	20.0	<b>String.</b> Height of paper (roughly, ticks
		and texts extend this).
'paper_width'	20.0	<b>String.</b> Width of paper (roughly, ticks and
		texts extend this).
'block_params'		Array of Blocks. List of blocks that make
		the nomograph.
'transformations'	[('rotate', 0.01),	Array of tuples. List of transformations
	('scale paper')]	to transform nomograph.
'title_str'	, ,	<b>String.</b> Title string of nomograph.
'title_x'	paper_width/2.0	<b>Float.</b> Title x-position.
'title_y'	paper_height	Float. Title y-position.
'title_box_width'	paper_width/2.2	<b>Float.</b> Title box width.
'title_color'	'color.rgb.black'	Color. Title color.
'make_grid'	False	<b>Boolean.</b> If True, draws grid to help posi-
		tion texts, etc.
'pre_func'	None	func(context). PyX function(canvas) to
		draw under nomograph. Function defini-
		tion could be:
'post_func'	None	func(context). PyX function(canvas) to
		draw over nomograph. Definiton same as
		for 'pre_func'.
'debug'	False	<b>Boolean.</b> If True, prints dicts of definions.
'extra_texts'	[]	<b>List of Dicts defining texts.</b> Defines extra
		texts. Could be for example:
'isopleth_params'	[{}]	List of Dicts. Defines appearance of iso-
		pleths. Could be for example:

**CHAPTER** 

**FIVE** 

# **TYPE REFERENCE**

In the following is a reference for the types used in pyNomo.

# 5.1 Type 1

Type 1 is three parallel lines that have functional relationship:

$$F_1(u_1) + F_2(u_2) + F_3(u_3) = 0$$

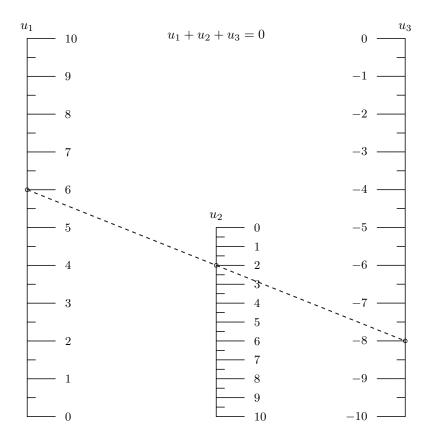
Note, that this kind of function can be transformed to many forms by using type 8 that is a equation given in determinant form. Use of this nomograph is given by the following simple example.

# 5.1.1 Simple example

This simple example plots nomograph for equation:

$$u_1 + u_2 + u_3 = 0.$$

# Generated nomograph



# Source code of simple example of type 1

```
1
2
          ex_type1_nomo_1.py
3
         Simple nomogram of type 1: F1+F2+F3=0
4
5
     import sys
6
     sys.path.insert(0, "..")
#sys.path[:0] = [".."]
8
     \textbf{from pynomo.nomographer import} ~*
9
10
11
     N_params_1={
              'u_min':0.0,
12
              'u_max':10.0,
13
              'function':lambda u:u,
'title':r'$u_1$',
14
15
              'tick_levels':2,
16
              'tick_text_levels':1,
17
18
19
     N_params_2={
20
21
              'u_min':0.0,
              'u_max':10.0,
22
              'function':lambda u:u,
23
              'title':r'$u_2$',
24
              'tick_levels':2,
25
              'tick_text_levels':1,
26
27
                       }
28
29
     N_params_3={
               u_min':0.0,
30
               'u_max':-10.0,
31
32
              'function':lambda u:u,
              'title':r'$u_3$',
33
```

```
'tick_levels':2,
34
             'tick_text_levels':1,
35
36
37
38
    block_1_params={
39
                  'block_type':'type_1',
40
41
                  'width':10.0,
                  'height':10.0,
42
                  'f1_params':N_params_1,
43
44
                  'f2_params':N_params_2,
                  'f3_params':N_params_3,
45
                  'isopleth_values':[[6,2,'x']],
46
47
48
    main_params={
                   'filename':'ex_type1_nomo_1.pdf',
50
                   'paper_height':10.0,
51
52
                   'paper_width':10.0,
                   'block_params':[block_1_params],
53
                   'transformations':[('rotate',0.01),('scale paper',)],
54
                   'title_str':r'$u_1+u_2+u_3=0$',
55
                   'debug':False,
56
57
    Nomographer(main_params)
58
```

# 5.1.2 Parameters for type 1

# **Axis parameters**

Table 5.1: Specific axis parameters for type 1

parameter key	default value	type, explanation
'function'	_	<b>func(u).</b> Function in equation For exam-
		ple lambda u: u
'u_min'	_	Float. Minimum value of function vari-
		able.
'u_max'	_	Float. Maximum value of function vari-
		able.

See Common axis params for other parameters.

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# **Block parameters**

Table 5.2: Specific block parameters for type 9

parameter	default value	explanation
'block_type'	'type_1'	<b>String.</b> This is type 1 block
'width'	10.0	Float. Block width (to be scaled)
'height'	10.0	Float. Block height (to be scaled)
'f1_params'	_	Axis params Dict. Axis params for func-
		tion f1
'f2_params'	_	Axis params Dict. Axis params for func-
		tion f2
'f3_params'	_	Axis params Dict. Axis params for func-
		tion f3
'mirror_x'	False	<b>Boolean.</b> If x-axis is mirrored
'mirror_y'	False	Boolean. If y-axis is mirrored
'proportion'	1.0	Float. Factor for spacings between lines
'isopleth_values'	[[]]	** List of list of isopleth values.** Un-
		known values are given with strings, e.g.
		'x'. An example:[[0.8, 0.1, 'x'], ['x',
		0.2, 1.0]]

# **General parameters**

See *List of main params* for top level main parameters.

# 5.2 Type 2

Type 1 is "N" or "Z" nomograph that have functional relationship:

$$F_1(u_1) = F_2(u_2)F_3(u_3)$$

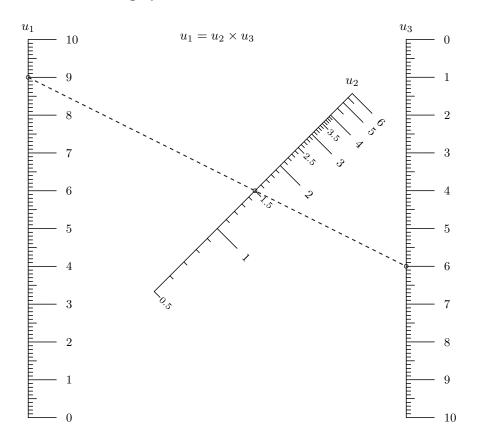
Use of this nomograph is given by the following simple example.

# 5.2.1 Simple example

This simple example plots nomograph for equation:

$$u_1 = u_2 u_3$$

#### Generated nomograph



# Source code of simple example of type 2

```
1
2
         ex_type2_nomo_1.py
3
         Simple nomogram of type 2: F1=F2*F3
4
5
    import sys
6
     sys.path.insert(0, "..")
8
     from pynomo.nomographer import \ast
9
10
    N_params_1={
             'u_min':0.0,
11
             'u_max':10.0,
12
             'function':lambda u:u,
13
             'title':r'$u_1$',
14
             'tick_levels':3,
15
             'tick_text_levels':1,
16
                     }
17
18
    N_params_2={
19
             'u_min':0.5,
20
21
             'u_max':6.0,
             'function':lambda u:u,
22
             'title':r'$u_2$',
23
24
             'tick_levels':3,
             'tick_text_levels':2,
25
             'scale_type':'linear smart',
26
27
28
29
    N_params_3={
              'u_min':0.0,
30
             'u_max':10.0,
31
32
             'function':lambda u:u,
             'title':r'$u_3$',
33
```

5.2. Type 2

```
'tick_levels':3,
34
             'tick_text_levels':1,
35
36
37
38
    block\_1\_params = \{
39
                  'block_type':'type_2',
40
41
                  'width':10.0,
                  'height':10.0,
42
                  'f1_params':N_params_1,
43
44
                  'f2_params':N_params_2,
                  'f3_params':N_params_3,
45
                  'isopleth_values':[[9,1.5,'x']],
46
47
48
    main_params={
                   'filename':'ex_type2_nomo_1.pdf',
50
                   'paper_height':10.0,
51
52
                   'paper_width':10.0,
                   'block_params':[block_1_params],
53
                   'transformations':[('rotate',0.01),('scale paper',)],
54
                   'title_str':r'u_1=u_2\times u_3'
55
56
    Nomographer(main_params)
```

# 5.2.2 Parameters for type 2

#### **Axis parameters**

Table 5.3: Specific axis parameters for type 2

parameter key	default value	type, explanation
'function'	_	func(u). Function in equation For exam-
		ple lambda u: u
'u_min'	_	Float. Minimum value of function vari-
		able.
'u_max'	_	Float. Maximum value of function vari-
		able.

See Common axis params for other parameters.

# **Block parameters**

Table 5.4: Specific block parameters for type 2

parameter	default value	explanation
'block_type'	'type_2'	<b>String.</b> This is type 2 block
'width'	10.0	Float. Block width (to be scaled)
'height'	10.0	Float. Block height (to be scaled)
'f1_params'	_	Axis params Dict. Axis params for func-
		tion f1
'f2_params'	_	Axis params Dict. Axis params for func-
		tion f2
'f3_params'	_	Axis params Dict. Axis params for func-
		tion f3
'mirror_x'	False	Boolean. If x-axis is mirrored
'mirror_y'	False	Boolean. If y-axis is mirrored
'proportion'	1.0	Float. Factor for spacings between lines
'isopleth_values'	[[]]	** List of list of isopleth values.** Un-
		known values are given with strings, e.g.
		'x'. An example:[[0.8, 0.1, 'x'], ['x',
		0.2, 1.0]]

# **General parameters**

See *List of main params* for top level main parameters.

# 5.3 Type 3

Type 3 has N parallel lines that have functional relationship:

$$F_1(u_1) + F_2(u_2) + \dots + F_N(u_N) = 0$$

Use of this nomograph is given by the following simple example.

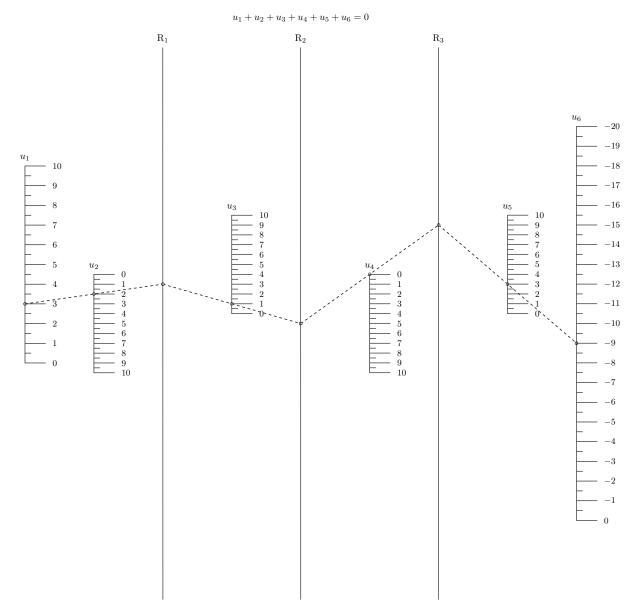
# 5.3.1 Simple example

This simple example plots nomograph for equation:

$$u_1 + u_2 + u_3 + u_4 + u_5 + u_6 = 0$$

5.3. Type 3 21

# Generated nomograph



# Source code of simple example of type 2

```
1
2
          ex_type3_nomo_1.py
3
          Simple nomogram of type 3: F1+F2+...+FN=0
4
          You should have received a copy of the GNU General Public License \,
5
6
         along with this program. If not, see <a href="http://www.gnu.org/licenses/">http://www.gnu.org/licenses/</a>.
7
     import sys
9
     sys.path.insert(0, "..")
     from pynomo.nomographer import \star
10
11
12
     N\_params\_1 = \{
              'u_min':0.0,
13
14
              'u_max':10.0,
              'function':lambda u:u,
15
              'title':r'$u_1$',
16
              'tick_levels':2,
17
              'tick_text_levels':1,
18
19
     N_params_2={
20
```

```
'u_min':0.0,
21
             'u_max':10.0,
22
             'function':lambda u:u,
23
             'title':r'$u_2$',
24
25
             'tick_levels':2,
             'tick_text_levels':1,
26
27
                     }
28
    N_params_3={
             'u_min':0.0.
29
             'u_max':10.0,
30
31
             'function':lambda u:u,
             'title':r'$u_3$',
32
             'tick_levels':2,
33
             'tick_text_levels':1,
34
                     }
35
    N_params_4={
             'u_min':0.0,
37
             'u_max':10.0,
38
39
             'function':lambda u:u,
             'title':r'$u_4$',
40
41
             'tick_levels':2,
             'tick_text_levels':1,
42
                     }
43
44
    N_params_5={
             'u_min':0.0,
45
46
             'u_max':10.0,
47
             'function':lambda u:u,
             'title':r'$u_5$',
48
             'tick_levels':2,
49
50
             'tick_text_levels':1,
51
                     }
52
    N_params_6={
             'u_min':-20.0,
53
             'u_max':0.0,
54
             'function':lambda u:u,
55
             'title':r'$u_6$',
56
             'tick_levels':2,
57
             'tick_text_levels':1,
58
             'tick_side':'right',
59
60
                     }
61
62
    block_1_params={
63
                   'block_type':'type_3',
                  'width':10.0.
64
65
                  'height':10.0,
                   'f_params':[N_params_1,N_params_2,N_params_3,
66
                               N_params_4,N_params_5,N_params_6],
67
68
                  'isopleth_values':[[3,2,1,0,3,'x']],
69
                  }
70
71
     main_params={
                    'filename':'ex_type3_nomo_1.pdf',
72
                    'paper_height':20.0,
73
                   'paper_width':20.0,
74
75
                    'block_params':[block_1_params],
76
                    'transformations':[('rotate',0.01),('scale paper',)],
                   'title_str':r'$u_1+u_2+u_3+u_4+u_5+u_6=0$',
77
                    'title_y':21.0,
78
79
    Nomographer(main_params)
80
```

5.3. Type 3

# 5.3.2 Parameters for type 3

#### **Axis parameters**

Table 5.5: Specific axis parameters for type 3

parameter key	default value	type, explanation
'function'	_	func(u). Function in equation For exam-
		ple lambda u: u
'u_min'	_	Float. Minimum value of function vari-
		able.
'u_max'	_	Float. Maximum value of function vari-
		able.

See Common axis params for other parameters.

# **Block parameters**

Table 5.6: Specific block parameters for type 3

parameter	default value	explanation
'block_type'	'type_3'	String. This is type 3 block
'width'	10.0	Float. Block width (to be scaled)
'height'	10.0	Float. Block height (to be scaled)
'f_params'	-	List of Axis params Dict. List of Axis
		params.
'mirror_x'	False	Boolean. If x-axis is mirrored
'mirror_y'	False	Boolean. If y-axis is mirrored
'reference_padding'	0.2	Float. Additional length to reference
		axes.
'reference_titles'		Array of Strings. List of ref-
		erence line titles. For example
		['\$R_1\$','\$R_2\$','\$R_3\$']'.
'reference_color'	color.rgb.black	<b>Color.</b> Color of reference lines.
'isopleth_values'	[[]]	** List of list of isopleth val-
		ues.** Unknown values are given
		with strings, e.g. 'x'. An exam-
		ple:[[0.8,'x',0.7,7.0,9.0],[0.7,0.8,'x',5.0,4.44

# **General parameters**

See *List of main params* for top level main parameters.

# 5.4 Type 4

Type 4 is proportion nomograph that have functional relationship:

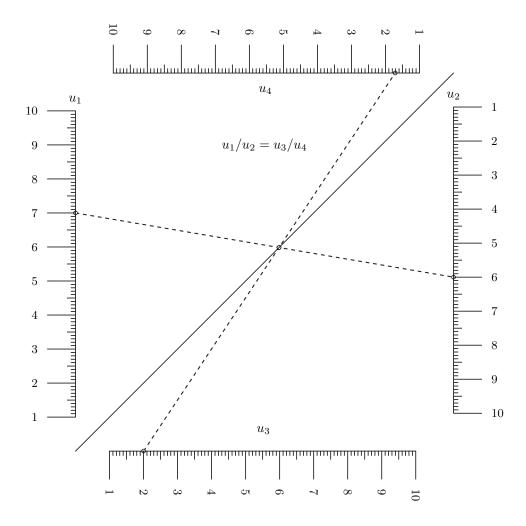
$$\frac{F_1(u_1)}{F_2(u_2)} = \frac{F_3(u_3)}{F_4(u_4)}$$

# 5.4.1 Simple example

This simple example plots nomograph for equation:

$$u_1/u_2 = u_3/u_4$$

# Generated nomograph



# Source code of simple example of type 4

```
2
          ex_type4_nomo_1.py
3
          Simple nomogram of type 4: F1/F2=F3/F4
4
5
6
     import sys
     sys.path.insert(0, "..")
     from pynomo.nomographer import *
8
10
     N_params_1={
               'u_min':1.0,
11
               'u_max':10.0,
12
               'function':lambda u:u,
'title':r'$u_1$',
13
14
               'tick_levels':3,
15
               'tick_text_levels':1,
'tick_side':'left',
16
17
```

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```
18
     N_params_2={
19
20
             'u_min':1.0,
              'u_max':10.0,
21
             \verb|'function': \textbf{lambda} u: u, \\
22
             'title':r'$u_2$',
23
             'tick_levels':3,
24
25
             'tick_text_levels':1,
             'tick_side':'right',
26
27
                      }
28
     N_params_3={
              'u_min':1.0,
29
             'u_max':10.0,
30
31
             'function':lambda u:u,
             'title':r'$u_3$',
32
             'tick_levels':3,
33
34
             'tick_text_levels':1,
             'tick_side':'right',
35
36
             'title_draw_center':True,
             'title_opposite_tick':False,
37
38
39
     N_params_4={
             'u_min':1.0,
40
             'u_max':10.0,
41
             'function':lambda u:u,
42
             'title':r'$u_4$',
43
44
             'tick_levels':3,
             'tick_text_levels':1,
45
             'tick_side':'left',
46
47
             'title_draw_center':True,
             'title_opposite_tick':False,
48
49
50
51
     block_1_params={
                      'block_type':'type_4',
52
                      'f1_params':N_params_1,
53
                      'f2_params':N_params_2,
54
                      'f3_params':N_params_3,
                      'f4_params':N_params_4,
56
                      'isopleth_values':[[7,6,2,'x']],
57
58
59
60
     main_params={
                    'filename':'ex_type4_nomo_1.pdf',
61
62
                    'paper_height':10.0,
63
                    'paper_width':10.0,
                    'block_params':[block_1_params],
64
                    'transformations':[('rotate',0.01),('scale paper',)],
65
66
                    'title_str':r'$u_1/u_2=u_3/u_4$',
                    'title_y':8.0,
67
     Nomographer(main_params)
69
```

# 5.4.2 Parameters for type 4

# **Axis parameters**

Table 5.7: Specific axis parameters for type 4

parameter key	default value	type, explanation
'function'	_	func(u). Function in equation For exam-
		ple lambda u: u
'u_min'	_	Float. Minimum value of function vari-
		able.
'u_max'	_	Float. Maximum value of function vari-
		able.

See *Common axis params* for other parameters.

# **Block parameters**

Table 5.8: Specific block parameters for type 4

parameter	default value	explanation
'block_type'	'type_4'	<b>String.</b> This is type 4 block
'width'	10.0	Float. Block width (to be scaled)
'height'	10.0	Float. Block height (to be scaled)
'f1_params'	_	Axis params Dict. Axis params for func-
		tion f1
'f2_params'	_	Axis params Dict. Axis params for func-
		tion f2
'f3_params'	_	Axis params Dict. Axis params for func-
		tion f3
'f4_params'	_	Axis params Dict. Axis params for func-
		tion f4
'mirror_x'	False	<b>Boolean.</b> If x-axis is mirrored
'mirror_y'	False	<b>Boolean.</b> If y-axis is mirrored
'padding'	0.9	Float. How much axis extend w.r.t.
		width/height.
'float_axis'	'F1 or F2'	<b>Strings.</b> If given 'F1 or F2', then scaling
		is according to them, otherwise according
		to F3 and F4.
'reference_color'	color.rgb.black	<b>Color.</b> Color of reference lines.
'isopleth_values'	[[]]	** List of list of isopleth val-
		ues.** Unknown values are given
		with strings, e.g. 'x'. An exam-
		ple:[[0.8,'x',0.7,0.5],[0.7,0.8,'x',0.3]]

# **General parameters**

See *List of main params* for top level main parameters.

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# 5.5 Type 5

Type 5 is graphing block that has functional relationship:

$$F_1(u) = F_2(x, v).$$

This type of block is used commonly in nomographs that have an equation in form

$$f_a(a_1, a_2, a_3, ...) = f_b(u, v)$$

and :math: 'f\_b(u,v) cannot be represented as line-nomograph. Typically equation above is written as pair of equations:

$$f_a(a_1, a_2, a_3, ...) = x$$

and

$$f_b(u,v) = x.$$

This equation is written in form

$$F_1(u) = F_2(x, v).$$

in order to construct this contour block. In reality block consists of horizontal lines:

$$F_1(u) = y$$

and contour lines

$$F_2(x,v) = y,$$

where x and y are the coordinates of canvas. Coordinate x is reference with name wd in block parameters and it holds

$$x = f_{wd}(wd)$$
.

**Note:** Type 5 is a very complex (say stupid) way to make basic graphs. In the future versions of pynomo a more simple way for graphs will be implemented.

# 5.5.1 Simple example

In the following example

$$F_1(u) = u$$

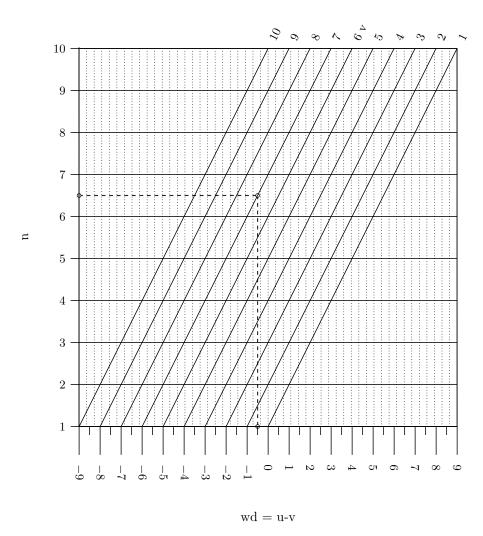
and

$$F_2(wd, v) = wd + v.$$

Thus the original equation is

$$wd = u - v$$
.

#### Generated nomograph



# Source code of simple example of type 5

```
1
2
         ex_type5_nomo_1.py
3
         Simple nomogram of type 5.
4
    import sys
6
     sys.path.insert(0, "..")
    from pynomo.nomographer import *
9
10
11
    block_params={
12
13
        'block_type':'type_5',
        'u_func':lambda u:u,
14
        v_func': \mathbf{lambda} \ x, v: x+v,
15
16
        'u_values':[1.0,2.0,3.0,4.0,5.0,6.0,7.0,8.0,9.0,10.0],
        'v_values':[1.0,2.0,3.0,4.0,5.0,6.0,7.0,8.0,9.0,10.0],
17
        'wd_tick_levels':2,
        'wd_tick_text_levels':1,
19
        'wd_tick_side':'right',
20
21
        'wd_title':'wd = u-v',
        'u_title':'u',
22
        'v_title':'v',
23
24
        'wd_title_opposite_tick':True,
        'wd_title_distance_center':2.5,
25
```

5.5. Type 5

```
'isopleth_values':[[6.5,7,'x']],
26
27
28
29
30
     \verb|main_params={|}|
                    'filename':'ex_type5_nomo_1.pdf',
31
                    'paper_height':10.0,
32
33
                    'paper_width':10.0,
                    'block_params':[block_params],
34
                    'transformations':[('rotate',0.01),('scale paper',)]
35
36
37
    Nomographer(main_params)
```

# 5.5.2 Parameters for type 5

# Axis parameters

No specific axis parameters. Everything is defined in block.

# **Block parameters**

Table 5.9: Specific block parameters for type 4

parameter	default value	explanation
'block_type'	'type_5'	<b>String.</b> This is type 5 block.
'width'	10.0	<b>Float.</b> Block width (to be scaled)
'height'	10.0	Float. Block height (to be scaled)
'mirror_x'	False	Boolean. If x-axis is mirrored
'mirror_y'	False	Boolean. If y-axis is mirrored
'u_func'	_	func(u). u function. For example
		"lambda u:u'
'v_func'	_	func(u,v). v function. For example
		lambda x,v: x+v
'wd_func'	_	func(wd). wd func. For example lambda
		wd: wd
'wd_func_inv'	_	func(wd). Inverse of wd-func. For exam-
		ple lambda wd: wd
'u_values'	_	List of Floats. List of plot-
		ted u values. For example
		[1.0,2.0,3.0,4.0,5.0,6.0,7.0,8.0,9.0,10.0]'.
'u_tag'	'none'	String. To align blocks w.r.t each other
		along axes with same tag.
'u_title'	,,	String. Axis title.
'u_title_x_shift'	0.0	<b>Float.</b> Title shift in x-direction.
'u_title_y_shift'	0.25	<b>Float.</b> Title shift in y-direction.
		Continued on next page

Table 5.9 – continued from previous page

parameter	default value	explanation
•	'linear'	•
'u_scale_type'	inear	String. Scale type. Can be 'linear':
		linear scale. 'log': logarithmic scale.
		'smart linear': linear scale with equal
		spacings. 'smart log': logarithmic scale
		with equal spacings, can also have nega-
		tive values. 'manual point': Points and
		corresponding text positions are given
		manually in 'manual axis data'. No line
		is drawn. 'manual line': Ticks and cor-
		responding text positions are given manu-
		ally in 'manual axis data'.
'u_tick_levels'	4	Integer. How many levels (minor, minor-
		minor, etc.) of ticks are drawn. Largest
		effect to 'linear' scale.
'u_tick_text_levels'	'3'	Integer. How many levels (minor, minor-
a_fick_fevf_TeAGT2		minor, etc.) of texts are drawn. Largest
		effect to 'linear' scale.
1 ## al 2 d - 1	1 m i mln # 2	
'u_tick_side'	'right'	<b>String.</b> Tick and text side in final paper.
		Can be: 'right'''or '''left'
'u_reference'	False	<b>Boolean.</b> If axis is treated as reference
		line that is a turning point.
'u_reference_padding'	'0.2'	<b>Float.</b> Fraction of reference line over
		other lines.
'u_manual_axis_data'	{}	<b>Dict.</b> Manually set tick/point positions
		and text positions. Could be for exam-
		ple:"{1:'1',3.14:r'\$pi\$',5:'5',7:'seven',10:'10'
'u_title_draw_center'	False	<b>Boolean.</b> Title is drawn to center of line.
'u_title_distance_cent		<b>String.</b> To double-align blocks w.r.t each
d_trere_dretato_co		other along axes with same tag.
'u_title_opposite_tick	, True	<b>Boolean.</b> Title in opposite direction w.r.t
u_title_opposite_tier	Truc	ticks.
'u_align_func'	lambda u:u	<b>func(u).</b> function to align different scales.
'u_align_x_offset'	0.0	<b>Float.</b> If axis is aligned with other axis,
		this value x offsets final scale.
'u_align_y_offset'	0.0	<b>Float.</b> If axis is aligned with other axis,
		this value y offsets final scale.
'u_text_format'	r'\$%4.4g\$'	<b>String.</b> Format for numbers in scale.
'u_extra_params'	[{},]	Array of Dicts. List of dictionary of
		params to be drawn additionally.
'u_text_distance_#'	X.X	<b>Float.</b> where $\#=0,1,2,3$ or 4. Distance of
		text from scale line. Number corresponds
		to the level, where 0 is the major tick and
		4 is the most minor ticks.
'u_grid_length_#'	X.X	Float. where $\#=0,1,2,3$ or 4. Length of
u_61 1u_1c11g t11_π	^.^	the tick. Number corresponds to the level,
		=
		where 0 is the major tick and 4 is the most
f .	1	minor ticks.
		Continued on next page

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Table 5.9 – continued from previous page

parameter	default value	explanation
'u_text_size_#'	X.X	Float. where $\#=0,1,2,3$ or
u_text_512e_#	A. A	4. Text size. For example:
		-
		text.size.small, text.size.scriptsize
		or text.size.tiny. Number corresponds
		to the level, where 0 is the major tick and
		4 is the most minor ticks.
'u_text_size_log_#'	X.X	<b>Float.</b> where $\#=0,1$ or
		2. Text size. For example:
		text.size.small, text.size.scriptsize
		or text.size.tiny . Number corresponds
		to the level, where 0 is the major tick and
		2 is the most minor ticks.
'u_full_angle'	False	<b>Boolean.</b> If true, text can be upside down,
		otherwise +- 90 degrees from horizontal.
		Good foor example for full circle scales.
'u_extra_angle'	0.0	<b>Boolean.</b> Title is drawn to center of line.
'u_text_horizontal_al	igħ <u>a</u> demter'	<b>Boolean.</b> Aligns tick text horizontally to
		center. Good when text rotated 90 de-
		grees.
'u_axis_color'	color.rgb.black	Color. Color of axis.
'u_text_color'	color.rgb.black	<b>Color.</b> Color of tick texts.
'v_values'	_	List of Floats. List of plot-
		ted v values. For example
		[1.0,2.0,3.0,4.0,5.0,6.0,7.0,8.0,9.0,10.0]'.
'v_title'	, ,	String. Axis title.
'v_title_draw_center'	False	<b>Boolean.</b> Title is drawn to center of line.
'v_title_distance_cen	tertype_9'	<b>String.</b> To double-align blocks w.r.t each
		other along axes with same tag.
1		· ·
'v_title_opposite_tic	k'True	<b>Boolean.</b> Little in opposite direction w.r.t
'v_title_opposite_tic	k'True	<b>Boolean.</b> Title in opposite direction w.r.t ticks.
		ticks.
'v_title_opposite_tic  'wd_tag'	k'True 'none'	ticks.  String. To align blocks w.r.t each other
'wd_tag'		ticks. <b>String.</b> To align blocks w.r.t each other along axes with same tag.
<pre>'wd_tag' 'wd_title'</pre>	'none'	ticks.  String. To align blocks w.r.t each other along axes with same tag.  String. Axis title.
<pre>'wd_tag' 'wd_title' 'wd_title_x_shift'</pre>	'none' '' 0.0	ticks.  String. To align blocks w.r.t each other along axes with same tag.  String. Axis title.  Float. Title shift in x-direction.
<pre>'wd_tag' 'wd_title' 'wd_title_x_shift' 'wd_title_y_shift'</pre>	'none' '' 0.0 0.25	ticks.  String. To align blocks w.r.t each other along axes with same tag.  String. Axis title.  Float. Title shift in x-direction.  Float. Title shift in y-direction.
<pre>'wd_tag' 'wd_title' 'wd_title_x_shift'</pre>	'none' '' 0.0	ticks.  String. To align blocks w.r.t each other along axes with same tag.  String. Axis title.  Float. Title shift in x-direction.  Float. Title shift in y-direction.  String. Scale type. Can be 'linear':
<pre>'wd_tag' 'wd_title' 'wd_title_x_shift' 'wd_title_y_shift'</pre>	'none' '' 0.0 0.25	ticks.  String. To align blocks w.r.t each other along axes with same tag.  String. Axis title.  Float. Title shift in x-direction.  Float. Title shift in y-direction.  String. Scale type. Can be 'linear': linear scale. 'log': logarithmic scale.
<pre>'wd_tag' 'wd_title' 'wd_title_x_shift' 'wd_title_y_shift'</pre>	'none' '' 0.0 0.25	ticks.  String. To align blocks w.r.t each other along axes with same tag.  String. Axis title.  Float. Title shift in x-direction.  Float. Title shift in y-direction.  String. Scale type. Can be 'linear': linear scale. 'log': logarithmic scale. 'smart linear': linear scale with equal
<pre>'wd_tag' 'wd_title' 'wd_title_x_shift' 'wd_title_y_shift'</pre>	'none' '' 0.0 0.25	ticks.  String. To align blocks w.r.t each other along axes with same tag.  String. Axis title.  Float. Title shift in x-direction.  Float. Title shift in y-direction.  String. Scale type. Can be 'linear': linear scale. 'log': logarithmic scale. 'smart linear': linear scale with equal spacings. 'smart log': logarithmic scale
<pre>'wd_tag' 'wd_title' 'wd_title_x_shift' 'wd_title_y_shift'</pre>	'none' '' 0.0 0.25	ticks.  String. To align blocks w.r.t each other along axes with same tag.  String. Axis title.  Float. Title shift in x-direction.  Float. Title shift in y-direction.  String. Scale type. Can be 'linear': linear scale. 'log': logarithmic scale. 'smart linear': linear scale with equal spacings. 'smart log': logarithmic scale with equal spacings, can also have nega-
<pre>'wd_tag' 'wd_title' 'wd_title_x_shift' 'wd_title_y_shift'</pre>	'none' '' 0.0 0.25	ticks.  String. To align blocks w.r.t each other along axes with same tag.  String. Axis title.  Float. Title shift in x-direction.  Float. Title shift in y-direction.  String. Scale type. Can be 'linear': linear scale. 'log': logarithmic scale. 'smart linear': linear scale with equal spacings. 'smart log': logarithmic scale with equal spacings, can also have negative values. 'manual point': Points and
<pre>'wd_tag' 'wd_title' 'wd_title_x_shift' 'wd_title_y_shift'</pre>	'none' '' 0.0 0.25	ticks.  String. To align blocks w.r.t each other along axes with same tag.  String. Axis title.  Float. Title shift in x-direction.  Float. Title shift in y-direction.  String. Scale type. Can be 'linear': linear scale. 'log': logarithmic scale. 'smart linear': linear scale with equal spacings. 'smart log': logarithmic scale with equal spacings, can also have negative values. 'manual point': Points and corresponding text positions are given
<pre>'wd_tag' 'wd_title' 'wd_title_x_shift' 'wd_title_y_shift'</pre>	'none' '' 0.0 0.25	ticks.  String. To align blocks w.r.t each other along axes with same tag.  String. Axis title.  Float. Title shift in x-direction.  Float. Title shift in y-direction.  String. Scale type. Can be 'linear': linear scale. 'log': logarithmic scale. 'smart linear': linear scale with equal spacings. 'smart log': logarithmic scale with equal spacings, can also have negative values. 'manual point': Points and corresponding text positions are given manually in 'manual axis data'. No line
<pre>'wd_tag' 'wd_title' 'wd_title_x_shift' 'wd_title_y_shift'</pre>	'none' '' 0.0 0.25	ticks.  String. To align blocks w.r.t each other along axes with same tag.  String. Axis title.  Float. Title shift in x-direction.  Float. Title shift in y-direction.  String. Scale type. Can be 'linear': linear scale. 'log': logarithmic scale. 'smart linear': linear scale with equal spacings. 'smart log': logarithmic scale with equal spacings, can also have negative values. 'manual point': Points and corresponding text positions are given manually in 'manual axis data'. No line is drawn. 'manual line': Ticks and cor-
<pre>'wd_tag' 'wd_title' 'wd_title_x_shift' 'wd_title_y_shift'</pre>	'none' '' 0.0 0.25	ticks.  String. To align blocks w.r.t each other along axes with same tag.  String. Axis title.  Float. Title shift in x-direction.  Float. Title shift in y-direction.  String. Scale type. Can be 'linear': linear scale. 'log': logarithmic scale. 'smart linear': linear scale with equal spacings. 'smart log': logarithmic scale with equal spacings, can also have negative values. 'manual point': Points and corresponding text positions are given manually in 'manual axis data'. No line is drawn. 'manual line': Ticks and corresponding text positions are given manual
<pre>'wd_tag' 'wd_title' 'wd_title_x_shift' 'wd_title_y_shift'</pre>	'none' '' 0.0 0.25	ticks.  String. To align blocks w.r.t each other along axes with same tag.  String. Axis title.  Float. Title shift in x-direction.  Float. Title shift in y-direction.  String. Scale type. Can be 'linear': linear scale. 'log': logarithmic scale. 'smart linear': linear scale with equal spacings. 'smart log': logarithmic scale with equal spacings, can also have negative values. 'manual point': Points and corresponding text positions are given manually in 'manual axis data'. No line is drawn. 'manual line': Ticks and cor-

Table 5.9 – continued from previous page

narameter	default value	
parameter		explanation
'wd_tick_levels'	4	Integer. How many levels (minor, minor-
		minor, etc.) of ticks are drawn. Largest
		effect to 'linear' scale.
'wd_tick_text_levels'	'3'	Integer. How many levels (minor, minor-
		minor, etc.) of texts are drawn. Largest
		effect to 'linear' scale.
'wd_tick_side'	'right'	<b>String.</b> Tick and text side in final paper.
		Can be: 'right'''or '''left'
'wd_reference'	False	<b>Boolean.</b> If axis is treated as reference
		line that is a turning point.
'wd_reference_padding'	'0.2'	<b>Float.</b> Fraction of reference line over
		other lines.
'wd_manual_axis_data'	{}	<b>Dict.</b> Manually set tick/point positions
a_mandat_axt3_data		and text positions. Could be for exam-
		ple:"{1:'1',3.14:r'\$pi\$',5:'5',7:'seven',10:'10'
2 md + i + l o draw aart 1	Falso	Boolean. Title is drawn to center of line.
'wd_title_draw_center'		
'wd_title_distance_cer	ite <b>r</b> type_9'	<b>String.</b> To double-align blocks w.r.t each
	<u></u>	other along axes with same tag.
'wd_title_opposite_tic	:kTrue	<b>Boolean.</b> Title in opposite direction w.r.t
		ticks.
'wd_align_func'	lambda u:u	<b>func(u).</b> function to align different scales.
'wd_align_x_offset'	0.0	<b>Float.</b> If axis is aligned with other axis,
		this value x offsets final scale.
'wd_align_y_offset'	0.0	Float. If axis is aligned with other axis,
		this value y offsets final scale.
'wd_text_format'	r'\$%4.4g\$'	<b>String.</b> Format for numbers in scale.
'wd_extra_params'	[{},]	Array of Dicts. List of dictionary of
,	-(3,/ -	params to be drawn additionally.
'wd_text_distance_#'	X.X	<b>Float.</b> where $\#=0,1,2,3$ or 4. Distance of
		text from scale line. Number corresponds
		to the level, where 0 is the major tick and
		4 is the most minor ticks.
'wd_grid_length_#'	V V	Float. where $\#=0,1,2,3$ or 4. Length of
wu_gi tu_teligtii_#	X.X	
		the tick. Number corresponds to the level,
		where 0 is the major tick and 4 is the most
		minor ticks.
'wd_text_size_#'	X.X	<b>Float.</b> where $\#=0,1,2,3$ or
		4. Text size. For example:
		text.size.small, text.size.scriptsize
		or text.size.tiny. Number corresponds
		to the level, where 0 is the major tick and
		4 is the most minor ticks.
		Continued on next page
		2

5.5. Type 5 33

Table 5.9 – continued from previous page

parameter	default value	explanation
'wd_text_size_log_#'	x.x	<b>Float.</b> where $\#=0,1$ or
		2. Text size. For example:
		text.size.small, text.size.scriptsize
		or text.size.tiny. Number corresponds
		to the level, where 0 is the major tick and
		2 is the most minor ticks.
'wd_full_angle'	False	<b>Boolean.</b> If true, text can be upside down,
		otherwise +- 90 degrees from horizontal.
		Good foor example for full circle scales.
'wd_extra_angle'	0.0	<b>Boolean.</b> Title is drawn to center of line.
'wd_text_horizontal_al	i <b>ga<u>l</u>se</b> nter'	Boolean. Aligns tick text horizontally to
		center. Good when text rotated 90 de-
		grees.
'wd_axis_color'	color.rgb.black	Color. Color of axis.
'wd_text_color'	color.rgb.black	Color. Color of tick texts.
'isopleth_values'		** List of list of isopleth val-
		ues.** Unknown values are given
		with strings, e.g. 'x'. An exam-
		ple:[[0.8,'x',0.7],[0.7,0.8,'x']]

# **General parameters**

See List of main params for top level main parameters.

# 5.6 Type 6

Type 6 is ladder nomograph:

$$u = u$$
.

In practice this means that if one axis has for example y-position as

$$y = f_1(u)$$

and it was desirable to have

$$y = f_2(u)$$

in order to connect blocks together, one uses ladder to make the transformation.

Note: Ladders are not beautiful and should be used only when no other solution exist.

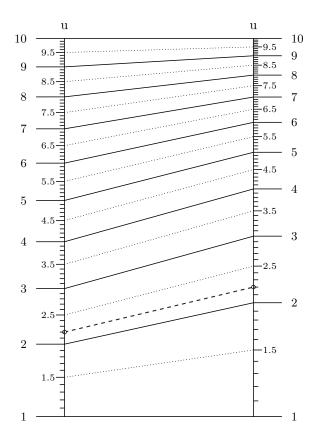
### 5.6.1 Simple example

This simple example plots nomograph for equation:

$$u = u$$
,

where linear scale is converted to a logarithmic scale.

### **Generated nomograph**



### Source code of simple example of type6

```
1
2
         ex_type6_nomo_1.py
3
         Simple nomogram of type 6.
4
5
    import sys
6
    sys.path.insert(0, "..")
8
     from pynomo.nomographer import *
9
10
    N_params_1={
11
              'u_min':1.0,
             'u_max':10.0,
12
13
             'function':lambda u:u**0.5,
             'title':'u',
14
             'tick_levels':3,
15
             'tick_text_levels':2,
16
             'tick_side':'left',
17
18
19
    N_params_2={
20
21
             'u_min':1.0,
             'u_max':10.0,
22
             'function':lambda u:log(u),
23
24
             'title':'u',
             'tick_levels':3,
25
             'tick_text_levels':2,
26
27
28
29
    block_params={
                    'block_type':'type_6',
30
                    'f1_params':N_params_1,
31
                   'f2_params':N_params_2,
32
                    'width':5.0,
33
```

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```
'height':10.0,
34
                   'isopleth_values':[[2.2,'x']],
35
36
                   #'curve_const':0.01
37
                          }
38
    main_params={
39
                   'filename':'ex_type6_nomo_1.pdf',
40
                   'paper_height':10.0,
41
                   'paper_width':5.0,
42
                   'block_params':[block_params],
43
44
                   'transformations':[('rotate',0.01),('scale paper',)]
45
46
    Nomographer(main_params)
```

# 5.6.2 Parameters for type 6

### **Axis parameters**

Table 5.10: Specific axis parameters for type 6

parameter key	default value	type, explanation
'function'	_	func(u). Function in equation For exam-
		ple lambda u: u
'u_min'	_	Float. Minimum value of function vari-
		able.
'u_max'	_	Float. Maximum value of function vari-
		able.

See Common axis params for other parameters.

# **Block parameters**

Table 5.11: Specific block parameters for type 6

parameter	default value	explanation
'block_type'	'type_6'	<b>String.</b> This is type 6 block.
'type'	'parallel'	String. Can be either 'parallel'''or
		'''orthogonal'.
'x_empty'	0.2	<b>Float.</b> If orthogonal, how much fractional
		space before start of x-axis.
'y_empty'	0.2	<b>Float.</b> If orthogonal, how much fractional
		space before start of y-axis.
'curve_const'	0.0	Float. Sets the lenght of angle of Bezier
		curve. low value = straigh line, high
		value = curved line.
'width'	10.0	Float. Block width (to be scaled)
'height'	10.0	Float. Block height (to be scaled)
'f1_params'	_	Axis params Dict. Axis params for func-
		tion f1
'f2_params'	_	Axis params Dict. Axis params for func-
		tion f2
'mirror_x'	False	Boolean. If x-axis is mirrored
'mirror_y'	False	Boolean. If y-axis is mirrored
'ladder_color'	color.rgb.black	Color. Ladder color.
'isopleth_values'	[[]]	** List of list of isopleth values.** Un-
		known values are given with strings, e.g.
		'x'. An example:[[0.8,'x'],[0.7,'x']]

### **General parameters**

See *List of main params* for top level main parameters.

# 5.7 Type 7

Type 7 is "angle" nomograph that has functional relationship:

$$\frac{1}{F_1(u_1)} + \frac{1}{F_2(u_2)} = \frac{1}{F_3(u_3)}$$

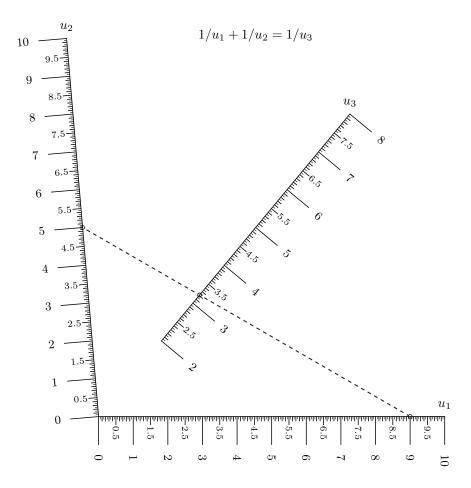
# 5.7.1 Simple example

This simple example plots nomograph for equation:

$$1/u_1 + 1/u_2 = 1/u_3$$

5.7. Type 7 37

# **Generated nomograph**



# Source code of simple example of type 2

# 5.7.2 Parameters for type 7

### **Axis parameters**

Table 5.12: Specific axis parameters for type 7

parameter key	default value	type, explanation
'function'	_	func(u). Function in equation For exam-
		ple lambda u: u
'u_min'	_	Float. Minimum value of function vari-
		able.
'u_max'	_	Float. Maximum value of function vari-
		able.

See Common axis params for other parameters.

# **Block parameters**

Table 5.13: Specific block parameters for type 7

parameter	default value	explanation
'block_type'	'type_4'	<b>String.</b> This is type 7 block
'width'	10.0	Float. Block width (to be scaled)
'height'	10.0	Float. Block height (to be scaled)
'f1_params'	_	Axis params Dict. Axis params for func-
		tion f1
'f2_params'	_	Axis params Dict. Axis params for func-
		tion f2
'f3_params'	_	Axis params Dict. Axis params for func-
		tion f3
'mirror_x'	False	<b>Boolean.</b> If x-axis is mirrored
'mirror_y'	False	Boolean. If y-axis is mirrored
'angle_u'	45.0	Float. Angle between u1 and u3. Note:
		later transformations may alter the angle.
'angle_v'	45.0	Float. Angle between u2 and u3. Note:
		later transformations may alter the angle.
'isopleth_values'	[[]]	** List of list of isopleth val-
		ues.** Unknown values are given
		with strings, e.g. 'x'. An exam-
		ple:[[0.8,'x',0.7],[0.7,0.8,'x']]

### **General parameters**

See *List of main params* for top level main parameters.

# 5.8 Type 8

Type 8 is single nomograph:

$$y = F(u)$$

or

$$x = F_x(u),$$

$$y = F_y(u)$$
.

 ${\bf x}$  and  ${\bf y}$  are coordinates of canvas. Often this block is used for construction of dual-scales to existing scales.

# 5.8.1 Simple example

This simple example plots single vertical scale.

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### **Generated nomograph**



### Source code of simple example of type 8

```
1
2
         ex\_type8\_nomo\_1.py
3
        Simple nomogram of type 8.
4
5
    import sys
6
    sys.path.insert(0, "..")
7
8
     from pynomo.nomographer import *
10
    N\_params\_1 = \{
11
             'u_min':1.0,
             'u_max':10.0,
12
13
             'function':lambda u:u,
             'title':'u',
14
             'tick_levels':3,
15
             'tick_text_levels':2,
17
             'tick_side':'left',
18
19
20
    block_params={
                    'block_type':'type_8',
21
                   'f_params':N_params_1,
22
                   'width':5.0,
23
24
                   'height':10.0,
                   'isopleth_values':[[5]]
25
26
                          }
27
28
    main_params={
                   'filename':'ex_type8_nomo_1.pdf',
29
                    'paper_height':10.0,
30
                    'paper_width':5.0,
31
                   'block_params':[block_params],
32
                    'transformations':[]
33
34
                   }
35
    Nomographer(main_params)
36
```

# 5.8.2 Parameters for type 8

# **Axis parameters**

Table 5.14: Specific axis parameters for type 8

parameter key	default value	type, explanation
'function'	_	func(u). Function in equation. For exam-
		ple lambda u: u.
'u_min'	_	Float. Minimum value of function vari-
		able.
'u_max'	_	Float. Maximum value of function vari-
		able.
'function_x'	_	func(u). x-position in function. If used
		'function_y' must be defined. For example
		lambda u: u.
'function_y'	_	func(u). y-position in function. If used
		'function_x' must be defined. Overrides
		'function'. For example lambda u: u.

See Common axis params for other parameters.

# **Block parameters**

Table 5.15: Specific block parameters for type 8

parameter	default value	explanation
'block_type'	'type_8'	<b>String.</b> This is type 8 block
'width'	10.0	Float. Block width (to be scaled)
'height'	10.0	Float. Block height (to be scaled)
'f1_params'	_	Axis params Dict. Axis params for func-
		tion f1
'f2_params'	_	Axis params Dict. Axis params for func-
		tion f2
'f3_params'	_	Axis params Dict. Axis params for func-
		tion f3
'f4_params'	-	Axis params Dict. Axis params for func-
		tion f4
'mirror_x'	False	<b>Boolean.</b> If x-axis is mirrored
'mirror_y'	False	<b>Boolean.</b> If y-axis is mirrored
'padding'	0.9	<b>Float.</b> How much axis extend w.r.t.
		width/height.
'float_axis'	'F1 or F2'	<b>Strings.</b> If given 'F1 or F2', then scaling
		is according to them, otherwise according
		to F3 and F4.
'reference_color'	color.rgb.black	<b>Color.</b> Color of reference lines.
'isopleth_values'	[[]]	** List of list of isopleth values.** Un-
		known values are given with strings, e.g.
		'x'. An example:[[0.8, 'x', 0.7, 0.5],
		[0.7,0.8,'x',0.3]]

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#### **General parameters**

See *List of main params* for top level main parameters.

# 5.9 Type 9

Type 9 is "general determinant" nomograph that has functional relationship:

$$\begin{vmatrix} F_1(u_1[, v_1]) & G_1(u_1[, v_1]) & H_1(u_1[, v_1]) \\ F_2(u_2[, v_2]) & G_2(u_2[, v_2]) & H_2(u_2[, v_2]) \\ F_3(u_3[, v_3]) & G_3(u_3[, v_3]) & H_3(u_3[, v_3]) \end{vmatrix} = 0.$$

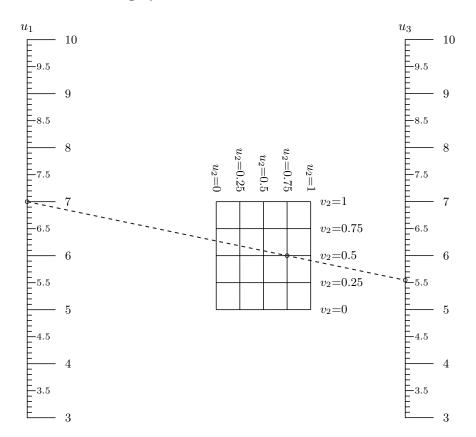
This is the basic building block for line nomographs. Notation u[,v] is to be understood such that if v is defined ', a grid is constructed for the row, otherwise a normal scale with variable u.

### 5.9.1 Simple example

This simple example plots nomograph for equation in determinant form:

$$\begin{vmatrix} 0 & u_1 & 1 \\ u_2 + 2 & 2v_2 + 5 & 1 \\ 4 & u_3 & 1 \end{vmatrix} = 0$$

#### Generated nomograph



#### Source code of simple example of type 9

```
1
2
         ex_type9_nomo_1.py
3
 4
         Simple nomogram of type 9: determinant
5
 6
     import sys
     sys.path.insert(0, "..")
8
     from pynomo.nomographer import *
     N_params_1={
10
                  'u_min':3.0,
11
                  'u_max':10.0,
12
                  'f':lambda u:0,
13
                  'g':lambda u:u,
14
15
                  'h':lambda u:1.0,
                 'title' r'$u_1$',
16
17
                  'scale_type':'linear',
18
                  'tick_levels':3,
                  'tick_text_levels':2,
19
20
                  'grid':False}
21
     N\_params\_2 = \{
22
23
             'u_min':0.0, # for alignment
             'u_max':1.0, # for alignment
24
             'f_grid':lambda u,v:u+2.0,
25
             'g_grid':lambda u,v:2*v+5.0,
26
             'h_grid':lambda u,v:1.0,
27
             'u_start':0.0,
28
             'u_stop':1.0,
29
             'v_start':0.0,
30
31
             'v_stop':1.0,
             'u_values':[0.0,0.25,0.5,0.75,1.0],
32
33
             'v_values':[0.0,0.25,0.5,0.75,1.0],
              'grid':True,
34
35
             'text_prefix_u':r'$u_2$=',
             'text_prefix_v':r'$v_2$=',
36
37
38
39
     N_params_3={
                  'u_min':3.0,
40
                  'u_max':10.0,
41
                  'f':lambda u:4.0,
42
                  'g':lambda u:u,
43
44
                  'h':lambda u:1.0,
                 'title':r'$u_3$',
45
                  'scale_type':'linear',
46
                  'tick_levels':3,
47
                  'tick_text_levels':2,
48
                  'grid':False
49
50
51
52
     block_params={
                   'block_type':'type_9',
53
                   'f1_params':N_params_1,
54
                   'f2_params':N_params_2,
55
                   'f3_params':N_params_3,
56
                   'transform_ini':False,
57
                   'isopleth_values':[[7,[0.75,0.5],'x']]
58
59
60
     main_params={
61
                    'filename':'ex_type9_nomo_1.pdf',
62
63
                    'paper_height':10.0,
                    'paper_width':10.0,
64
                    'block_params':[block_params],
65
66
                    'transformations':[('rotate',0.01),('scale paper',)]
67
     Nomographer(main_params)
```

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# 5.9.2 Parameters for type 9

# Axis parameters

Table 5.16: Specific axis parameters for type 9 grid axis

parameter key	default value	type, explanation
'grid'	_	<b>Bool.</b> True because this is grid.
'f'	_	func(u,v). F function in determinant. For
		example lambda u,v:u+v
'g'	_	func(u,v). G function in determinant. For
		example lambda u,v:u+v
'h'	_	func(u,v). H function in determinant. For
		example lambda u,v:u+v
'u_start'	_	u start when drawing v=const line
'u_stop'	_	u stop when drawing v=const line
'v_start'	_	v start when drawing u=const line
'v_stop'	_	v stop when drawing u=const line
'u_values'	_	List of grid lines u=const. For example
		[0.0,0.25,0.5,0.75,1.0]
'v_values'	_	List of grid lines v=const. For example
		"[0.0,0.25,0.5,0.75,1.0]"
'text_prefix_u'	_	Text prefix for u before value
'text_prefix_v'	_	Text prefix for v before value
'v_texts_u_start'	False	If v-texts are in u start side
'v_texts_u_stop'	True	If v-texts are in u stop side
'u_texts_v_start'	False	If u-texts are in v start side
'u_texts_v_stop'	True	If u-texts are in v stop side
'u_line_color'	color.rgb.black	Color. u line color
'v_line_color'	color.rgb.black	Color. v line color
'u_text_color'	color.rgb.black	Color. u text color
'v_text_color'	color.rgb.black	Color. v text color
'text_distance'	0.25	Float. Text distance
'circles'	False	Boolean. If marker circles to crossings
'extra_params'	_	<b>List of Dicts.</b> List of params to be drawn.

See Common axis params for other parameters.

# **Block parameters**

Table 5.17: Specific block parameters for type 9

parameter	default value	explanation
'block_type'	'type_9'	<b>String.</b> This is type 9 block
'width'	10.0	Float. Block width (to be scaled)
'height'	10.0	Float. Block height (to be scaled)
'f1_params'	_	Axis params Dict. Axis params for func-
		tion f1
'f2_params'	_	Axis params Dict. Axis params for func-
		tion f2
'f3_params'	_	Axis params Dict. Axis params for func-
		tion f3
'mirror_x'	False	<b>Boolean.</b> If x-axis is mirrored
'mirror_y'	False	Boolean. If y-axis is mirrored
'transform_ini'	False	<b>Boolean.</b> If row 1 and row 3 end and start
		are to be transformed to be in rectangle
		corners. If True, be sure that 'u_min_trafo'
		and 'u_max_trafo' are defined.
'isopleth_values'	[[]]	** List of list of isopleth values.**
		Grid values are given with tuple (a,b)
		and are not solved. Unknown val-
		ues are given with strings, e.g. 'x'.
		An example:[[0.8,(0.1,0.2),'x'],
		['x',(0.1,0.2),1.0]]

### **General parameters**

See *List of main params* for top level main parameters.

# 5.10 Type 10

Type 10 is nomograph that has one curved line. It has functional relationship:

$$F_1(u) + F_2(v)F_3(w) + F_4(w) = 0.$$

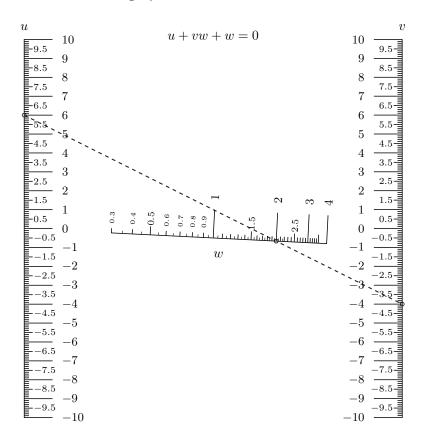
# 5.10.1 Simple example

This simple example plots nomograph for equation:

$$u + vw + w = 0.$$

5.10. Type 10 45

#### Generated nomograph



#### Source code of simple example of type 10

```
1
2
          ex_type10_nomo_1.py
3
          Simple nomogram of type 7: F1(u)+F2(v)*F3(w)+F4(w)=0
4
5
          along with this program. If not, see <a href="http://www.gnu.org/licenses/">http://www.gnu.org/licenses/</a>.
6
     import sys
8
     sys.path.insert(0, "..")
     from pynomo.nomographer import \ast
9
10
11
     N_params_1={
              'u_min':-10.0,
12
              'u_max':10.0,
13
              'function':lambda u:u,
14
              'title':r'$u$',
15
              'tick_levels':3,
16
              'tick_text_levels':2,
17
18
19
     N\_params\_2 = \{
20
21
              'u_min':-10.0,
              'u_max':10.0,
22
23
              'function':lambda u:u,
24
              'title':r'$v$',
              'tick_levels':3,
25
              'tick_text_levels':2,
26
              'tick_side':'left',
27
28
                       }
29
30
     N_params_3={
               'u_min':0.3,
31
32
              'u_max':4.0,
              'function_3':lambda u:u,
33
```

```
'function_4':lambda u:u,
34
             'title':r'$w$',
35
             'tick_levels':4,
36
             'tick_text_levels':3,
37
38
              'scale_type':'linear smart',
             'title_draw_center':True,
39
40
                     }
41
     block_1_params={
42
                   'block_type':'type_10',
43
44
                   'width':10.0,
                  'height':10.0,
45
                  'f1_params':N_params_1,
46
                  'f2_params':N_params_2,
47
                  'f3_params':N_params_3,
48
                  'isopleth_values':[[6,-4,'x']]
50
51
52
     \verb|main_params| = \{
                    \verb|'filename':'ex_type10_nomo_1.pdf'|,\\
53
54
                    'paper_height':10.0,
                    'paper_width':10.0,
55
                    'block_params':[block_1_params],
56
57
                    'transformations':[('rotate',0.01),('scale paper',)],
                    'title_str':r'$u+vw+w=0$'
58
59
                    }
     Nomographer(main_params)
```

### 5.10.2 Parameters for type 10

### **Axis parameters**

Table 5.18: Specific axis parameters for type 10

parameter key	default value	type, explanation
'function'	_	<b>func(u).</b> Function in the equation for $F_1$
		and $F_2$ . For example "lambdau : u"
'function_3'	-	<b>func(u).</b> Function in the equation for $F_3$ .
		For example lambda u: u
'function_4'	_	<b>func(u).</b> Function in the equation for $F_4$ .
		For example lambda u: u
'u_min'	_	Float. Minimum value of function vari-
		able.
'u_max'	_	Float. Maximum value of function vari-
		able.

See Common axis params for other parameters.

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# **Block parameters**

Table 5.19: Specific block parameters for type 10

parameter	default value	explanation
'block_type'	'type_10'	<b>String.</b> This is type 10 block
'width'	10.0	Float. Block width (to be scaled)
'height'	10.0	<b>Float.</b> Block height (to be scaled)
'f1_params'	-	<b>Axis params Dict.</b> Axis params for function f1
'f2_params'	_	Axis params Dict. Axis params for func-
		tion f2
'f3_params'	_	Axis params Dict. Axis params for func-
		tion f3
'f4_params'	_	Axis params Dict. Axis params for func-
		tion f4
'mirror_x'	False	<b>Boolean.</b> If x-axis is mirrored
'mirror_y'	False	Boolean. If y-axis is mirrored
'padding'	0.9	<b>Float.</b> How much axis extend w.r.t. width/height.
'float_axis'	'F1 or F2'	<b>Strings.</b> If given 'F1 or F2', then scaling
		is according to them, otherwise according
		to F3 and F4.
'reference_color'	color.rgb.black	<b>Color.</b> Color of reference lines.
'isopleth_values'	[[]]	** List of list of isopleth val-
		ues.** Unknown values are given
		with strings, e.g. 'x'. An exam-
		ple:[[0.8,'x',0.7,0.5],[0.7,0.8,'x',0

# **General parameters**

See *List of main params* for top level main parameters.

#### **EXAMPLES**

In the following are listed examples to show nomographs possibilities. Also is explained the background for the cases and underlying math for the nomograph construction. Source code shows the implementation.

# 6.1 Example: Amortized loan calculator

### 6.1.1 Theory and background

This approach of constructing an amortized loan calculator is similar to one in Ref. [1]\_ Equation for amortized loan [2] is:

$$\frac{a}{A} = \frac{\frac{p}{100 \times 12}}{1 - \frac{1}{(1 + \frac{p}{100 \times 13})^{12n}}},$$

where A is the amount of loan, a is monthly payment amount, p interest rate per year (monthly interest rate is taken as p/12)  $^1$  and p is number of years for payment.

This equation of four variables is probably impossible to present with line and grid nomographs. For this reason a "Type 5" contour nomogram is constructed of the right hand side of the equation and left hand equation is just N-nomogram (Type 2). The two equations for nomogram construction are:

$$x = \frac{a}{A}$$

and

$$x = \frac{\frac{p}{100 \times 12}}{1 - \frac{p}{(1 + \frac{p}{100 \times 12})^{12n}}}.$$

In practice x is the x-coordinate of the canvas where nomogram is constructed.

#### Right hand side of equation

By defining coordinates x and y:

$$x = \frac{\frac{p}{100 \times 12}}{1 - \frac{1}{(1 + \frac{p}{100 \times 12})^{12n}}},$$

y = 12n, we may solve y in terms of x and n:

<sup>&</sup>lt;sup>1</sup> http://en.wikipedia.org/wiki/Annual percentage rate#Does not represent the total cost of borrowing

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$$y = \frac{\log(\frac{x}{x - \frac{p}{100 \times 12}})}{\log(1 + \frac{p}{100 \times 12})}$$

The previous two equations are of correct form

$$y = f_1(v)$$

and

$$y = f_2(x, u)$$

for type 5 nomogram. For compressing time axis (y-axis), we transform  $y \to \log y$  and find

$$y = \log \left( \frac{\log(\frac{x}{x - \frac{p}{100 \times 12}})}{\log(1 + \frac{p}{100 \times 12})} \right)$$

$$y = \log(12n).$$

# Left hand side of equation

Left hand side of equation

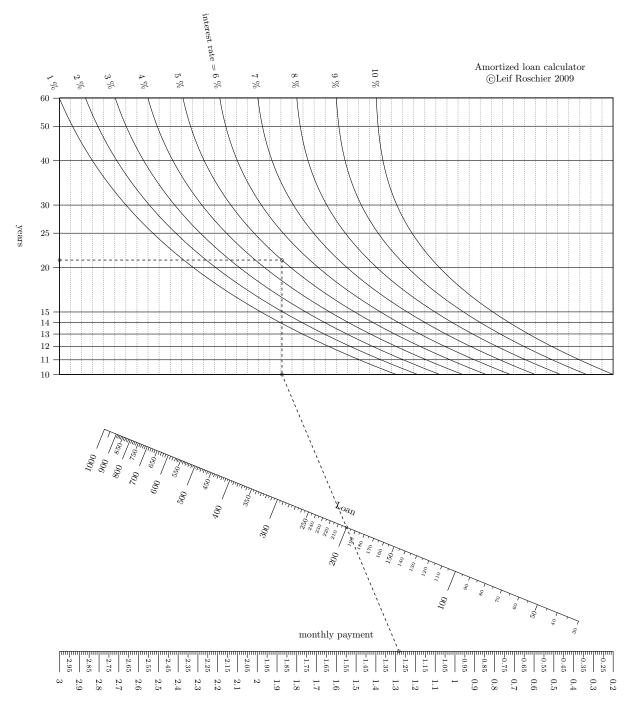
$$x = \frac{a}{A}$$

is just N-nomogram

$$F_1(u_1) = F_2(u_2)F_3(u_3)$$

#### References

# 6.1.2 Generated nomograph



### 6.1.3 Source code

```
def f1(x,u):
11
         return log(log(x/(x-u/(100.0*12.0)))/log(1+u/(100.0*12.0)))
12
13
     block_1_params={
14
15
                 'width':10.0,
                'height':5.0,
16
                'block_type':'type_5',
17
18
                'u_func':lambda u:log(u*12.0),
                'v_func':f1,
19
                'u_values':[10.0,11.0,12.0,13.0,14.0,15.0,20.0,25.0,30.0,40.0,50.0,60.0],
20
21
                'v_values':[1.0,2.0,3.0,4.0,5.0,6.0,7.0,8.0,9.0,10.0],
                'wd_tag':'A',
22
23
                'u_title':'years',
                 'v_title':r'interest rate = ',
24
                'u_text_format':r"$%3.0f$ ",
25
                'v_text_format':r"$%3.0f$ \%% ",
                'isopleth_values':[[21,5,'x']]
27
28
29
    \# this is non-obvious trick to find bottom edge coordinates of the grid in order
30
31
     # to align it with N nomogram
    block1_dummy=Nomo_Block_Type_5(mirror_x=False)
32
    block1_dummy.define_block(block_1_params)
33
34
    block1_dummy.set_block()
35
36
     # Let's define the N-nomogram
37
     N_params_3={
             'u_min':block1_dummy.grid_box.params_wd['u_min'],
38
39
             'u_max':block1_dummy.grid_box.params_wd['u_max'],
40
             'function':lambda u:u,
             'title':'',
41
             'tag':'A',
42
             'tick_side':'right',
43
             'tick_levels':2,
44
             'tick_text_levels':2,
45
             'reference':False,
46
             'tick_levels':0,
47
             'tick_text_levels':0,
48
             'title_draw_center':True
49
50
    N_params_2={
51
             'u_min':30.0,
52
53
             'u_max':1000.0,
             'function':lambda u:u,
54
55
             'title':'Loan',
             'tag': 'none',
56
             'tick_side':'left',
57
             'tick_levels':4,
58
59
             'tick_text_levels':3,
             'title_draw_center':True,
60
             #'text_format':r"$%3.0f$ '
61
             'scale_type':'linear smart',
62
63
64
    N_params_1={
             'u_min':0.2,
65
66
             'u_max':3.0,
             'function':lambda u:u,
67
             'title':'monthly payment',
68
             'tag':'none',
69
             'tick_side':'right',
70
             'tick_levels':3,
71
             'tick_text_levels':2,
72
             'title_draw_center':True
73
74
75
    block_2_params={
76
                  'block_type':'type_2',
77
                   'width':10.0.
78
                   'height':20.0,
79
80
                  'f1_params':N_params_1,
                   'f2_params':N_params_2,
81
82
                   'f3_params':N_params_3,
```

```
'isopleth_values':[['x',200,'x']]
83
84
85
     \verb|main_params| = \{
86
                    'filename':'amortized_loan.pdf',
87
                    'paper_height':20.0,
88
                    'paper_width':20.0,
89
                    'block_params':[block_1_params,block_2_params],
90
                    'transformations':[('rotate',0.01),('scale paper',)],
91
                                                                                  Leif Roschier 2009',
92
                      'title_str':r'Amortized loan calculator
                                                                   \copyright
93
                      'title_x': 17,
                      'title_y': 21,
94
                      'title_box_width': 5
95
96
     Nomographer(main_params)
```

# 6.2 Example Photography exposure

### 6.2.1 Theory and background

This example illustrates how exposure in photography depends on factors: latitude, time of day, day of year, weather, composition. It relates these to camera settings: film speed (e.g. ISO 100), aperture and shutter speed. The mathematical approach and model is taken from book written by V. Setälä. [1] This book illustrates the approach as nomographs but they are different compared with the one generatated here. Book uses shadow length, but we break shadow length into time, date and latitude via solar zenith angle.

The basic equation in Setälä (pp.492-494) can be extracted and written as

$$FS - L - A - W + C + T = 0 ag{6.1}$$

where parameters of (6.1) are listed below:

FS Film speed		DIN value that equals $10\log(S)+1$ ,where S is ISO FILM speed
T	shutter time	$10\log\left(\frac{t}{1/10}\right)$
A	aperture	$10\log\left(\frac{N^2}{3.2^2}\right)$
L	shadow	two times (shadow length)/(person length) = $2\arctan(\phi)$ , where $\phi$ is
	length (in	solar zenith angle.
	steps)	
W	weather	Clear sky, Cumulus clouds: 0, Clear sky: 1, Sun through clouds: 3, Sky
		light gray: 6, Sky dark gray: 9, Thunder-clouds cover sky: 12
C	Composi-	Person under trees: -6, Inside forest : -4, Person in shadow of wall : -1,
	tion	Person at open place; alley under trees: 2, Buildings; street: 5,
		Landscape and front matter: 7, Open landscape: 9, Snow landscape
		and front matter; beach: 11,Snow field; open sea: 13, Clouds: 15

It is to be noted that Setälä has stops ten times base-10 logarithmic. Today we think stops in base-2 logarithmic.

#### **Shadow lenght**

Calculation of shadow length as a function of day of year, time of day and latitude is according to [2] . Following equations are used. For fractional year (without time information) we take

```
\gamma = (day - 1 + 0.5)2\pi/365.
```

For time offset (eqtime) we use equation (in minutes)

$$TO = 229.18(0.000075 + 0.001868\cos(\gamma) - 0.032077\sin(\gamma) - 0.014615\cos(2\gamma) - 0.040849\sin(2\gamma))$$

to calculate that error is below 17 minutes for time axis. We assume that sun is at heightest point at noon and this is the error and approximation. We calculate stops in logarithmic scale and in this case we do not need very accurate equations for time. For declination we use equation

and for hour angle

$$ha = (60h + \overline{TO})/4 - 180.$$

Solar zenith angle ( $\phi$ ), latitude (LAT), declination (D) and hour angle (ha) are connected with equation:

$$\cos(\phi) = \sin(LAT)\sin(D) + \cos(LAT)\cos(D)\cos(ha).$$

This is in our desired form as a function of hour (h), day (day), latitude (LAT), solar zenith angle ( $\phi$ ):

$$\cos(\phi) = \sin(LAT)\sin(D(\gamma(day))) + \cos(LAT)\cos(D(\gamma(day)))\cos(ha(h)).$$

In practice illuminance of flat surface on earth depends on solar zenith angle as  $\cos(\phi)$ . Setälä uses shadow length that is easily measurable, but scales incorrectly, as value is proportional to  $\tan(\phi)$ . Also Setälä sums linear value with logarithmic ones as a practical approximation. To correct these assumptions, here we assume that values for shadow length 1 and 10 for Setälä are reasonable, and an equation that scales logarithmically is found:

```
L = 0.33766 - 13.656 \log 10(\cos(\phi))
that gives L = 1 for \phi = 26.565 = \arctan(1/2) and L = 10 for \phi = 78.69 = \arctan(10/2).
```

#### 6.2.2 Construction of the nomograph

The presented equation is the following:

$$FS - \{0.33766 - 13.656 \log_{10}[\sin(LAT)\sin(D(\gamma(day))) + \cos(LAT)\cos(D(\gamma(day)))\cos(ha(h))]\} - A - W + C + T = 0.$$

In order to construct the nomograph, we split the equation into four blocks and an additional block to present values as EV100.

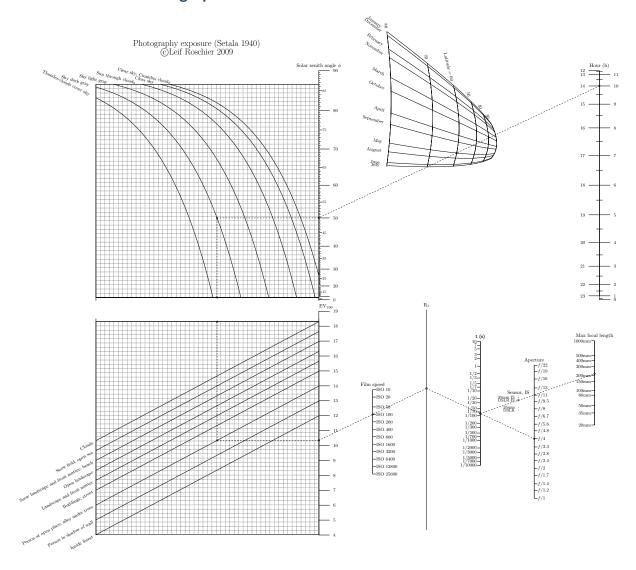
Table 6.1: Main equation split into blocks for the nomograph.

Explanation	Туре
	Type 9
$x_1 \equiv \cos(\phi) = \sin(LAT)\sin(D(\gamma(day))) + \cos(LAT)\cos(D(\gamma(day)))\cos(\theta)$	ha(h))
formed into determinant:	
$\begin{vmatrix} 0 & \cos(\phi) & 1\\ \frac{\cos(LAT)\cos(D(\gamma(day)))}{1+(\cos(LAT)\cos(D(\gamma(day))))} & \frac{\sin(LAT)\sin(D(\gamma(day)))}{1+(\cos(LAT)\cos(D(\gamma(day))))} & 1\\ 1 & -\cos(ha(h)) & 1 \end{vmatrix} = 0$	
	Type 5
$C_1 \equiv L + W = 0.006918 - 13.656 \log_{10}(x_1) + W$	
split into two equations for contour construction:	
$y_1 = C_1$	
$y_1 = 0.006918 - 13.656 \log_{10}(x_1) + W$	
	Type 5
$C_2 \equiv L + W + C = C_1 + C$	
anlit into true aquations for contour construction.	
split into two equations for contour construction:	
$y_2 = C_2$	
$y_2 = C_1 + C$	
	Type 3
$C_2 = FS - A + T$	
equals	
$C_2 - (10\log_{10}(S) + 1.0) + 10\log_{10}\left(\frac{N^2}{3.2^2}\right) - 10\log_{10}\left(\frac{1/t_i}{1/10}\right) = 0$	,
where	
$t_i \equiv 1/t$	
is inverse shutter time.	
	Continued on next page

Table 6.1 – continued from previous page

Explanation	Туре
Additional EV100 scale by using relation	Type 8
$C_2 = (-EV_{100} + 13.654)/0.3322$	
Maximum focal length calculator according to equation	Type 1
$t_i/f = FL$	
written as	
$-10\log_{10}\left(\frac{1/t_i}{1/10}\right) - 10\log_{10}\left(\frac{f}{10}\right) - 10\log_{10}\left(FL\right) = 0$	
in order to align correctly with previous equation. The values for the factor f are: DSLR (3/2), 35mm (1), DSLR image stabilization (3/8) and 35mm image stabilization (1/8).	

# 6.2.3 Generated nomograph



### 6.2.4 Source code

```
2
         ex_photo_exposure.py
3
         Photgraph exposure.
5
6
    import sys
    sys.path.insert(0, "..")
    from pynomo.nomographer import *
8
     functions for solartime taken from solaregns.pdf from
10
    http://www.srrb.noaa.gov/highlights/sunrise/solareqns.PDF
11
12
    # fractional year
13
14
    def gamma(day):
15
         return 2*pi/365.0*(day-1+0.5)
    # equation of time
16
17
    def eq_time(day):
         gamma0=gamma(day)
18
         return 229.18*(0.000075+0.001868*cos(gamma0)-0.032077*sin(gamma0)\
19
20
                         -0.014615*cos(2*gamma0)-0.040849*sin(2*gamma0))
21
    \mbox{\#} mean correction, with constant correction we make less than 17 minutes \mbox{\ error}
22
23
    temp_a=arange(0,365.0,0.1)
24
```

```
25
     temp b=eq time(temp a)
     correction=mean(temp_b) # this is 0.0171885 minutes
26
     #print "maximum time errors: %g %g"%(min(temp_b),max(temp_b))
27
28
29
     # declination
     def eq_declination(day):
30
31
         g0=gamma(day)
32
         return 0.006918-0.399912*cos(g0)+0.070257*sin(g0)-0.006758*cos(2*g0)\
                  +0.000907*sin(2*g0)-0.002697*cos(3*g0)+0.00148*sin(3*g0)
33
34
35
     def f1(dummy):
         return 0.0
36
37
     def g1(fii):
38
         return cos(fii*pi/180.0)
39
40
     def f2(lat,day):
         dec=eq_declination(day)
41
         \textbf{return} \ (\cos(\text{lat*pi/180.0})*\cos(\text{dec}))/(\text{1.0+}(\cos(\text{lat*pi/180.0})*\cos(\text{dec})))
42
     def g2(lat,day):
43
         dec=eq_declination(day) # in radians
44
45
         return (sin(lat*pi/180.0)*sin(dec))/(1.0+(cos(lat*pi/180.0)*cos(dec)))
46
     def f3(dummy):
47
48
         return 1
     def g3(h):
49
50
         hr=(h*60.0+correction)/4.0-180.0
51
         return -1.0*cos(hr*pi/180.0)
52
53
     days_in_month = (31,28,31,30,31,30,31,30,31,30,31)
54
     times1=[]
     for idx in range(0,12):
55
56
         times1.append(sum(days_in_month[0:idx])+1)
57
58
     #times=linspace(0,350,10)
59
     #times=arange(0.0,360.0,10.0,dtype=double).tolist()
60
     time_titles=['January','February','March','April','May','June',
61
                   'July', 'August', 'September', 'October', 'November', 'December']
62
63
64
     phi_params={
              'u_min':0.0,
65
              'u_max':90.0,
66
67
              'u_min_trafo':0.0,
             'u_max_trafo':90.0,
68
             'f':f1,
69
70
              'g':g1,
             'h':lambda u:1.0,
71
             'title':r'Solar zenith angle $\phi$',
72
73
              'title_x_shift':0.0,
             'title_y_shift':0.25,
74
             'scale_type':'linear smart',
75
              'tick_levels':4,
76
              'tick_text_levels':2,
77
             'tick_side':'right',
78
              'tag':'phi',
79
80
              'grid':False,
               'extra_params':[{'u_min':20.0,
81
82
                                 'u max':90.0.
83
                                 'tick_levels':4,
                                 'tick_text_levels':2,
84
85
                                 }]
86
             }
87
88
     time_params={
              'u_min':0.0,
89
              'u_max':23.0,
90
91
             'u_min_trafo':0.0,
92
              'u_max_trafo':12.0,
              'f':f3,
93
94
             'g':g3,
              'h':lambda u:1.0,
95
              'title':r'Hour (h)',
96
```

```
'title_x_shift':0.0,
97
              'title_y_shift':0.25,
98
              'scale_type':'linear',
 99
              'tick_levels':2,
100
101
              'tick_text_levels':1,
              'tick_side':'right',
102
              'tag':'none',
103
104
              'grid':False,
              }
105
106
107
      lat_day_params={
          'ID':'none', # to identify the axis
108
          'tag':'none', # for aligning block wrt others
109
          'title':'Grid',
110
          'title_x_shift':0.0,
111
          'title_y_shift':0.25,
112
          'title_distance_center':0.5,
113
          'title_opposite_tick':True,
114
115
          'u_min':20.0, # for alignment
          'u_max':80.0, # for alignment
116
117
          'f_grid':f2,
          'g_grid':g2,
118
          'h_grid':lambda u,v:1.0,
119
120
          'u_start':30.0,
          'u_stop':80.0,
121
122
          'v_start':times1[0], # day
          'v_stop':times1[-1],
123
          'u_values':[30.0,40.0,50.0,60.0,70.0,80.0],
124
          'u_texts':['30','40','50','Latitude = 60','70','80'],
125
126
          'v_values':times1,
          'v_texts':time_titles,
127
128
          'grid':True,
           'text_prefix_u':r''
129
          'text_prefix_v':r''
130
          'text_distance':0.5,
131
          'v_texts_u_start':False,
132
          'v_texts_u_stop':True,
133
          'u_texts_v_start':False,
134
135
          'u_texts_v_stop':True,
136
137
138
      block_params={
139
                    'block_type':'type_9',
                   'f1_params':phi_params,
140
                   'f2_params':lat_day_params,
141
                    'f3_params':time_params,
142
                   'transform_ini':True,
143
                   'isopleth_values':[['x',[60,times1[4]],14.0]],
144
145
146
      # limiting functions are to avoid NaN in contour construction that uses optimization
147
      def limit_xx(x):
148
149
          x1=x
           if x1>1.0:
150
              x1=1.0
151
152
           if x1<-1.0:
              x1=-1.0
153
154
          return x1
155
     def limit_x(x):
156
157
          x1=x
           if not x1>0.0:
158
               x1=0.0001
159
160
          return x1
161
     const_A=0.33766
162
      const_B=-13.656
163
164
165
     block_params_weather={
166
         'block_type':'type_5',
         'u_func':lambda u:u,
167
168
         'v_func':lambda x,v:const_A+const_B*log10(limit_x(x))+v,
```

```
#'u_values':[1.0,2.0,3.0,4.0,5.0,6.0,7.0,8.0,9.0,10.0,15.0,20,25],
169
         'u_values':[1.0,25.0],
170
         'u_manual_axis_data':{1.0:''
171
                                25.0:''},
172
173
         'v_values':[0.0,1.0,3.0,6.0,9.0,12.0],
         'v_manual_axis_data': {0.0:['Clear sky, Cumulus clouds',{'x_corr':0.5,
174
                                                                       'y_corr':0.0.
175
176
                                                                      'draw_line':False}],
                            1.0: 'Clear sky',
177
178
                            3.0: 'Sun through clouds',
179
                            6.0: 'Sky light gray',
                            9.0: 'Sky dark gray',
180
181
                            12.0: 'Thunder-clouds cover sky',
182
                            },
         'v text distance':0.5.
183
         'wd_tick_levels':0,
          'wd_tick_text_levels':0,
185
         'wd_tick_side':'right',
186
187
         'wd_title':'',
         'manual_x_scale':True,
188
189
         'x_min':0.06,
         'x_max':0.99,
190
         'u_title':'',
191
         'v_title':'',
192
         'wd_title_opposite_tick':True,
193
194
         'wd_title_distance_center':2.5,
         'wd_align_func':lambda L:acos(limit_xx(10.0**((L-const_A)/const_B)))*180.0/pi, # phi as L
195
         'wd_func':lambda L:10.0**((L-const_A)/const_B), # x as L
196
197
         'wd_func_inv':lambda x:const_A+const_B*log10(x), # L as x
198
         'wd_tag':'phi',
         'mirror_y':True,
199
         'mirror_x':False,
200
         'width':10.0,
201
         'height':10.0,
202
         'u_scale_opposite':True,
203
         'u_tag':'AA',
204
205
         'horizontal_guides':True,
         'isopleth_values':[['x',9.0,'x']],
206
207
208
209
      block_params_scene={
         'block_type':'type_5',
210
211
         'u_func':lambda u:u,
         'v_func':lambda x,v:x+v,
212
213
         'u_values':[1.0,25.0],
         'u_manual_axis_data':{1.0:''
214
                                25.0:''},
215
216
         'u_tag':'AA',
217
         'wd_tag':'EV'
         'v_values':[-4.0,-1.0,2.0,5.0,7.0,9.0,11.0,13.0,15.0],
218
         'v_manual_axis_data': {-6.0:'Person under trees',
219
                                  -4.0: 'Inside forest',
220
                                  -1.0: 'Person in shadow of wall',
221
                                  2.0: 'Person at open place; alley under trees',
222
                                  5.0: 'Buildings; street',
223
224
                                  7.0: 'Landscape and front matter',
                                  9.0: 'Open landscape',
225
226
                                  11.0: 'Snow landscape and front matter; beach',
227
                                  13.0: 'Snow field; open sea',
                                  15.0: 'Clouds',
228
229
         'wd_tick_levels':0,
230
         'wd tick text levels':0.
231
         'wd_tick_side':'right',
232
         'wd_title':'',
233
         'u_title':''
234
         'u_title':'',
'v_title':'',
235
         'wd_title_opposite_tick':True,
236
237
         'wd_title_distance_center':2.5,
238
         'mirror_x':True,
         'horizontal_guides':True,
239
240
         'u_align_y_offset':-0.9,
```

```
'isopleth_values':[['x',2.0,'x']],
241
242
       }
243
244
245
      camera_params_1={
               'u_min':-10.0,
246
               'u_max':15.0,
247
248
               'function':lambda u:u,
              'title':r''.
249
               'tick_levels':0,
250
251
               'tick_text_levels':0,
               'tag':'EV',
252
253
254
      camera_params_2={
               'u_min':10.0.
255
256
              'u_max':25600.0,
               'function': lambda S:-(10*log10(S)+1.0),
257
               'title':r'Film speed',
258
259
               'manual_axis_data': {10.0:'ISO 10',
                                      20.0:'ISO 20',
260
                                      #40.0:'ISO 40',
261
                                      50.0:'ISO 50',
262
                                      100.0:'ISO 100',
263
264
                                      200.0:'ISO 200',
                                      400.0:'ISO 400',
265
266
                                      800.0:'ISO 800'
267
                                      1600.0: 'ISO 1600',
                                      3200.0:'ISO 3200',
268
269
                                      6400.0: 'ISO 6400',
270
                                      12800.0: 'ISO 12800',
                                      25600.0:'ISO 25600',
271
272
               'scale_type':'manual line'
273
274
      camera_params_3={
275
               'u_min':0.1,
276
277
               'u_max':10000.0,
               'function': lambda t:-10*log10((1.0/t)/(1.0/10.0))-30,
278
               'manual_axis_data': {1/10.0:'10',
279
280
                                      1/7.0:'7',
                                      1/5.0:'5',
281
                                      1/3.0:'3',
282
283
                                      1/2.0:'2',
                                      1.0:'1'.
284
285
                                     2.0: '1/2',
286
                                      3.0: '1/3',
                                      5.0: '1/5',
287
288
                                      7.0: '1/7',
289
                                      10.0: '1/10',
                                      20.0:'1/20',
290
291
                                      30.0: '1/30',
                                      50.0:'1/50',
292
                                     70.0:'1/70'
293
                                      100.0: '1/100',
294
                                      200.0:'1/200',
295
296
                                      300.0:'1/300',
                                      500.0: '1/500',
297
                                      700.0: '1/700',
298
299
                                      1000.0: '1/1000',
                                      2000.0:'1/2000',
300
                                      3000.0:'1/3000',
301
302
                                      5000.0:'1/5000',
                                      7000.0: '1/7000',
303
304
                                      10000.0:'1/10000',
305
               'scale_type':'manual line',
306
307
              'title':r't (s)',
308
               'text_format':r"1/%3.0f s",
               'tag':'shutter',
309
310
              'tick_side':'left',
                       }
311
312
```

```
313
      camera_params_4={
               'u_min':1.0,
314
              'u_max':22.0,
315
              'function':lambda N:10*log10((N/3.2)**2)+30,
316
317
               'manual_axis_data': {1.0:'$f$/1'
                                      1.2:'$f$/1.2',
318
                                     1.4:'$f$/1.4',
319
                                     1.7:'$f$/1.7',
320
                                     2.0:'$f$/2',
321
                                     2.4:'$f$/2.4',
322
323
                                     2.8:'$f$/2.8',
                                     3.3:'$f$/3.3',
324
325
                                     4.0:'$f$/4'
326
                                     4.8:'$f$/4.8',
                                     5.6:'$f$/5.6',
327
                                     6.7:'$f$/6.7',
328
329
                                     8.0:'$f$/8',
                                     9.5:'$f$/9.5',
330
331
                                     11.0:'$f$/11',
                                     13.0:'$f$/13',
332
                                     16.0:'$f$/16',
333
                                     19.0:'$f$/19',
334
                                     22.0:'$f$/22',
335
336
              'scale_type':'manual line',
337
               'title':r'Aperture',
338
339
340
341
     block_params_camera={
342
                    'block_type':'type_3',
                    'width':10.0.
343
344
                    'height':10.0,
345
                    'f_params':[camera_params_1,camera_params_2,camera_params_3,
346
                                 camera_params_4],
                    'mirror_x':True,
347
                    'isopleth_values':[['x',100.0,'x',4.0]],
348
349
350
      def old_EV(EV): # C2(EV100) in wiki
351
352
          return (-EV+13.654)/0.3322
353
     EV_para={
354
355
               'tag':'EV'
              'u_min':4.0,
356
              'u_max':19.0,
357
358
              'function': lambda u:old_EV(u),
              'title':r'EV$_{100}$',
359
              'tick_levels':1,
360
361
              'tick_text_levels':1,
              'align_func':old_EV,
362
363
              'title_x_shift':0.5,
              'tick_side':'right',
364
365
366
     EV_block={
                'block_type':'type_8',
367
                'f_params':EV_para,
368
               'isopleth_values':[['x']],
369
370
371
      # maximum focal length
372
373
     FL_t_para={
374
              'u_max':10000.0,
375
376
              'function':lambda t:-10*log10((1.0/t)/(1.0/10.0))-30,
              'scale_type':'linear',
377
              'tick_levels':0,
378
              'tick_text_levels':0,
379
              'title':r't (s)',
'text_format':r"1/%3.0f s",
380
381
382
              'tag':'shutter',
383
                       }
384
```

```
FL_factor_params_2={
385
              'u_min':1.0/4.0,
386
              'u_max':3.0/2.0,
387
              'function':lambda factor:-10*log10(factor/10.0)+0,
388
389
              'title':r'Sensor, IS'
              'scale_type':'manual point',
390
              'manual_axis_data': {1.0/(2.0/3.0):'DSLR',
391
392
                            1.0/(1.0): '35mm',
                            1.0/(8.0/3.0): 'DSLR IS',
393
394
                            1.0/(4.0):'35mm IS',
395
                            },
              'tick_side':'left',
396
397
              'text_size_manual':text.size.footnotesize, # pyx directive
398
399
      FL_fl_params={
400
              'u_min':20.0,
401
              'u_max':1000.0,
402
403
              'function':lambda FL:-10*log10(FL)+30,
              'title':r'Max focal length',
404
405
              'tick_levels':3,
              'tick_text_levels':2,
406
              'tick_side':'left',
407
408
              'scale_type':'manual line',
              'manual_axis_data': {20.0:'20mm',
409
410
                                     35.0:'35mm',
                                     50.0:'50mm',
411
                                     80.0:'80mm',
412
413
                                     100.0:'100mm',
                                     150.0: '150mm',
414
                                     200.0:'200mm',
415
416
                                     300.0:'300mm',
                                     400.0:'400mm',
417
                                     500.0:'500mm',
418
                                     1000.0:'1000mm'}
419
              }
420
421
422
423
424
      FL_block_params={
                    'block_type':'type_1',
425
                    'width':12.0,
426
427
                    'height':10.0,
                   'f1_params':FL_t_para,
428
                    'f2_params':FL_factor_params_2,
429
                    'f3_params':FL_fl_params,
430
                    'mirror_x':True,
431
432
                   'proportion':0.5,
                    'isopleth_values':[['x',1.0/(8.0/3.0),'x']],
433
434
435
436
437
      main_params={
                     'filename':['ex_photo_exposure.pdf','ex_photo_exposure.eps'],
438
                     'paper_height':35.0,
439
440
                     'paper_width':35.0,
                     'block_params':[block_params,block_params_weather,block_params_scene,block_params_camera,EV_block,FL_block_params],
441
                    \verb| #'block_params':[block_params_weather,block_params_scene,block_params_camera,EV_block,FL_block_params]|,
442
                     'transformations':[('rotate',0.01),('scale paper',)],
443
                     'title_x': 7,
444
                     'title_y': 34,
445
                     'title_box_width': 10,
446
                     'title_str':r'\LARGE Photography exposure (Setala 1940) \par \copyright Leif Roschier 2009 '
447
448
      b=Nomographer(main_params)
449
```

C	CHAPTER
	CEV/ENI

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