

# ZKU – Cohort 4 (Jul-Aug 2022)

## Week 1: Introduction to ZKP

### Assignment #1

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**Abstract**—This document is for answering ZKUC04, Week-1, Introduction to ZKP Assignment. It consists of three main parts.

**Part 1:** Theoretical background of zk-SNARKs and zk-STARKS.

**Part 2:** Getting started with circom and snarkjs.

**Part 3:** Reading and designing circuits with Circom.

The total number of questions and points is 13, including the bonus questions.

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#### I. PART 1: THEORETICAL BACKGROUND OF ZK-SNARKS AND ZK-STARKS

A. 1.1 Explain in 2-4 sentences why SNARK requires a trusted setup while STARK doesn't.

zkSTARKs requires a trusted setup because it requires an initial creation event of the keys, which are used to create proofs for private transactions, and used in the verification of those proofs.

On the other hand, zkSTARKs does not require a trusted-setup for utilizing the network because it is transparent which means that they use publicly verifiable randomness to create a trustless verifiable computing system. [?][?]

B. 1.2 Name two more differences between SNARK and STARK proofs.

- 1) zkSTARKs rely on hash functions, so it would be a quantum resistant, on the other hand zkSNARKs are not quantum resistant so the privacy of SNARKs could be broken. [?]
- 2) zkSTARKs have larger proof sizes than zkSNARKs, which means that the verification in STARKs takes more time than in SNARKs. [?]

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#### II. PART 2: GETTING STARTED WITH CIRCOM AND SNARKJS:

A. Question (1)

1) 2.1 What does the circuit in `HelloWorld.circom` do?

It implements a Circom circuit to prove the multiplication of two private inputs signal identifiers a, and b, and calculate the result in a public output signal identifier c.

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B. Question (2)

1) 2.2.1 What is a Powers of Tau ceremony?

The Power of Tau ( $\tau$ ) is a secure multi-party computation (MPC) ceremony. It is used in generating the parameters of the first phase (1) in zkSNARK which consists of two phases. It can generate parameters for all the circuits up to a depth of  $2^{21}$ . It proceeds in turns, one turn for each party, and the result of the computation of each party is then added to a public transcript, which will allow all the system be verified. The result parameters of the system then becomes secure if one party was able to destroy the random toxic waste. [?]

2) 2.2.2 Explain why this is important in the setup of zk-SNARK applications.

In order to deploy a zkSNARK circuits, a developer must perform a computation for generating the "Proving Key", and the "Verifying key", and this process called a "Trusted Setup". There is a downside for this process because it produces bad numbers called "toxic waste" file that needs to be destroyed otherwise it will produce fake proofs which will violate the security of the system. So to resolve that, the "Trusted Setup" can be setup using specific Cryptographic ceremony like the "Powers of Tau" ceremony, which will be used only in generating the first phase of parameter generation of all the projects, since zk-SNARKs requires two phases of parameter generation. [?]

Power of Tau ceremony is helping in creating what is called a "Chain of trusted-setup", through allowing multiple parties to setup a trusted setup and then adding the results to a public transcript, and the system can be verified by publishing the results. Moreover, the system will be considered secure, if only one of the parties has successfully destroying the "toxic waste" file. [?]

3) 2.2.3 How are Phase 1 and Phase 2 trusted setup ceremonies different from each other?

zkSNARK projects consists of two phases of parameter generation, The Power of Tau can be only used in the first phase for all the projects. While the second phase if a circuit-specific that needs to be done for each circuit, and the individual teams are responsible on it.

Phase-one is a universal phase ceremony for the entire community, while to start phase-two, any zkSNARK projects can pick any point of the ceremony to begin their circuit-specific second phase. [?] [?]

### Perpetual Powers of Tau (phase 1)

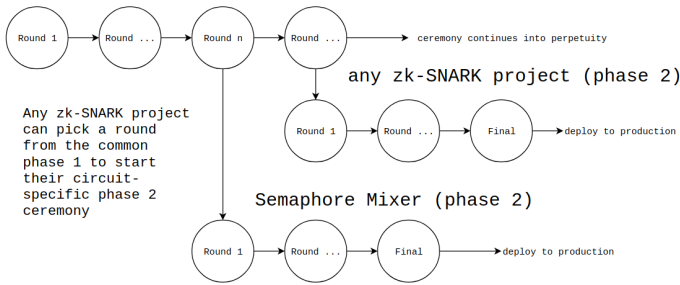


Fig. 1. Image borrowed from Wei Jie Koh's post. [?]

### C. Question (3)

1) **2.3.2** Try to run `compile-Multiplier3-groth16.sh`. You should encounter an `error[T3001]` with the circuit as is. Explain what the error means and how it arises.

`error[T3001]` means that the constraint is Non-quadratic expression, because it should be one of those constraints: [?]

**Constant values**

**Linear expression**  $2 * x + 3 * y + 2$

**Quadratic expression**  $(2 * x + 3 * y + 2) * (x + y) + 6 * x + y - 2$

### D. Question (4)

1) **2.4.1** What are the practical differences between Groth16 and PLONK? Hint: compare and contrast the resulted contracts and running time of unit tests from the two protocols.

- Groth16 requires a trusted ceremony to each circuit, while PLONK does not require it, its just enough to use The Power of Tau universal setup ceremony. [?]
- After running the `test/test.js` in Question (5), it turns out that Groth16 proofing system took shorter time than PLONK proofing system, where Groth16 took 1132ms, and PLONK took 1462ms.
- The `verifyProof` in `Multiplier3Verifier.sol` of Groth16 is simpler than The `verifyProof` in `Multiplier3-plonkVerifier.sol` of PLONK

### E. Question (5)

1) **2.5.3** In `test/test.js`, add the unit tests for **Multiplier3** for both the Groth16 and PLONK versions. Include a screenshot of all the tests (for **HelloWorld**, **Multiplier3 with Groth16**, and **Multiplier3 with PLONK**) passing in your PDF file.

Look at Fig, [2].

```
[@archlinux ~] / /zku/week1/Q2$ npm run test
> test
> node scripts/bump-solidity.js && npx hardhat test

Bump Solidity contract: HelloWorldVerifier
Bump Solidity contract: Multiplier3-plonkVerifier
Bump Solidity contract: Multiplier3Verifier

HelloWorld
✓ Circuit should multiply two numbers correctly (884ms)
✓ Should return true for correct proof (2136ms)
✓ Should return false for invalid proof (290ms)

Multiplier3 with Groth16
✓ Circuit should multiply three numbers correctly
✓ Should return true for correct proof (1132ms)
✓ Should return false for invalid proof (334ms)

Multiplier3 with PLONK
✓ Should return true for correct proof (1462ms)
✓ Should return false for invalid proof

8 passing (35s)
```

Fig. 2. All tests are passing.

2) **3.1.2** What are the possible outputs for the `LessThan` template and what do they mean respectively?

The expected outputs are either 0 or 1 which is a boolean return datatype, so if the number  $n1$  is not less than number  $n2$  the output will be 0 which means false  $n1 > n2$ . Otherwise the output will be 1 which means true  $n1 < n2$ .

### B. Question (2)

1) **3.2.2** You can run `npm run test:fullProof` while inside the `zkPuzzles` directory to test your modified circuit. You are expected to encounter an error. Record the error, resolve it by modifying `project/zkPuzzles/scripts/compile-circuits.sh`, and explain why it has occurred and what you did to solve the error?

The error was `[ERROR] snarkJS: circuit too big for this power of tau ceremony. 97588 > 216`. It means that the current circuit requires a bigger power of tau ceremony, because the current one is a 16 ceremony  $2^{16} < 97588$ , which is less than the expected from the circuit 97588. To resolve this error, just change the downloaded Power of Tau ceremony file to be bigger than 16, so I downloaded Power of Tau with the power of 20 therefore,  $2^{20} > 97588$ .

```
1 # ./zku/week1/Q3/projects/zkPuzzles/scripts
2 if [ -f ./powersOfTau28_hez_final_20.ptau ]; then
3   echo "powersOfTau28_hez_final_20.ptau already
4   exists. Skipping."
5 else
6   echo 'Downloading powersOfTau28_hez_final_20.
7   ptau'
8   wget https://hermez.s3-eu-west-1.amazonaws.com/
9   powersOfTau28_hez_final_20.ptau
10 fi
```

Listing 1. Expected solution

## III. PART 3: READING AND DESIGNING CIRCUITS WITH CIRCOM

### A. Question (1)

1) **3.1.1** What does the 32 in Line 9 stand for?

$n$  variable in the template `LessThan(n)` function refers to the number of bits for the input signal, and 32 stands for the unsigned integers, non-negative integer in the range [0 to 4294967295].

### C. Question (3) [Bonus]

1) **3.3** Run `npm run test` to prove that the solution to the following system of equations is  $x = 15$ ,  $y = 17$ ,  $z = 19$ .

Look at fig, [3].

```

[ @archlinux ~/ / /zku/week1/Q3]$ npm run test
> test
> . scripts/bonus-compile.sh && node scripts/bonus-bump-solidity.js && npx hardhat test

mkdir: cannot create directory 'SystemOfEquations': File exists
powersOfTau28_hez_final_10.ptau already exists. Skipping.
Compiling SystemOfEquations.circom...
template instances: 2
non-linear constraints: 2
linear constraints: 0
public inputs: 12
public outputs: 1
private inputs: 3
private outputs: 0
wires: 16
labels: 29
Written successfully: SystemOfEquations/SystemOfEquations.r1cs
Written successfully: SystemOfEquations/SystemOfEquations.sym
Written successfully: SystemOfEquations/SystemOfEquations_js/SystemOfEquations.wasm
Everything went okay, circom safe
[INFO] snarkJS: Curve: bn-128
[INFO] snarkJS: # of Wires: 16
[INFO] snarkJS: # of Constraints: 2
[INFO] snarkJS: # of Private Inputs: 3
[INFO] snarkJS: # of Public Inputs: 12
[INFO] snarkJS: # of Labels: 29
[INFO] snarkJS: # of Outputs: 1
[INFO] snarkJS: Reading r1cs
[INFO] snarkJS: Reading tauG1
[INFO] snarkJS: Reading tauG2
[INFO] snarkJS: Reading alphatauG1
[INFO] snarkJS: Reading betatauG1
[INFO] snarkJS: Circuit hash:
0ccb345a ed31807d 1dea9101 68e04922
f80213ef c35c1ed8 3d599e2a df05d7ef
0e663578 2e3a5674 6f7562e4 cb1531ba
ce7dcdad 94b7d507 aai44bae 4a13cf35
[DEBUG] snarkJS: Applying key: L Section: 0/2
[DEBUG] snarkJS: Applying key: H Section: 0/16
[INFO] snarkJS: Circuit Hash:
0ccb345a ed31807d 1dea9101 68e04922
f80213ef c35c1ed8 3d599e2a df05d7ef
0e663578 2e3a5674 6f7562e4 cb1531ba
ce7dcdad 94b7d507 aai44bae 4a13cf35
[INFO] snarkJS: Contribution Hash:
189dc3d2 352de94e 81ab2fe6 218380d9
a914e40b 7865ef54 d3aaf3fb 2d57e079
6ce046ef 38928eec 8cc4fd4 c8f6f9e2
6169205b d3c3fe61 4e0d13fb 66689066
Compiled 1 Solidity file successfully

SystemOfEquations circuit test
✓ Bonus question (49ms)

SystemOfEquations verifier test
✓ Should return true for correct proof (2377ms)
✓ Should return false for invalid proof (359ms)

3 passing (3s)

```

Fig. 3. All tests are passing.

#### D. Question (4) [Bonus]

1) 3.4 what other libraries do you think could be created to help foster the growth of ZK applications?

I think it would be better if there is a support for strings in the debugging log() library, that would be useful to separate between the printed logs, for exmaple: `log("Single input in", in);`. Also, it would be useful if there are a static typing system for the templates and the functions, typing the data-types of the expected inputs and the expected return.

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## REFERENCES

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