Unsupervised Recurrent Neural Network Grammars

Yoon Kim[†] Alexander M. Rush[†] Lei Yu[⋄] Adhiguna Kuncoro^{‡,⋄} Chris Dyer[⋄] Gábor Melis[⋄]

†Harvard University ‡University of Oxford ◆DeepMind

{yoonkim,srush}@seas.harvard.edu {leiyu,akuncoro,cdyer,melisgl}@google.com

Abstract

Recurrent neural network grammars (RNNG) are generative models of language which jointly model syntax and surface structure by incrementally generating a syntax tree and sentence in a top-down, left-to-right order. Supervised RNNGs achieve strong language modeling and parsing performance, but require an annotated corpus of parse trees. In this work, we experiment with unsupervised learning of RNNGs. Since directly marginalizing over the space of latent trees is intractable, we instead apply amortized variational inference. To maximize the evidence lower bound, we develop an inference network parameterized as a neural CRF constituency parser. On language modeling, unsupervised RNNGs perform as well their supervised counterparts on benchmarks in English and Chinese. On constituency grammar induction, they are competitive with recent neural language models that induce tree structures from words through attention mechanisms.

1 Introduction

Recurrent neural network grammars (RNNGs) (Dyer et al., 2016) model sentences by first generating a nested, hierarchical syntactic structure which is used to construct a context representation to be conditioned upon for upcoming words. Supervised RNNGs have been shown to outperform standard sequential language models, achieve excellent results on parsing (Dyer et al., 2016; Kuncoro et al., 2017), better encode syntactic properties of language (Kuncoro et al., 2018), and correlate with electrophysiological responses in the human brain (Hale et al., 2018). However, these all require annotated syntactic trees for training. In this work, we explore unsupervised learning of recurrent neural network grammars for language modeling and grammar induction.

Work done while the first author was an intern at DeepMind. Code available at https://github.com/harvardnlp/urnng

The standard setup for unsupervised structure learning is to define a generative model $p_{\theta}(\mathbf{x}, \mathbf{z})$ over observed data x (e.g. sentence) and unobserved structure z (e.g. parse tree, part-of-speech sequence), and maximize the log marginal likelihood $\log p_{\theta}(\mathbf{x}) = \log \sum_{\mathbf{z}} p_{\theta}(\mathbf{x}, \mathbf{z})$. Successful approaches to unsupervised parsing have made strong conditional independence assumptions (e.g. context-freeness) and employed auxiliary objectives (Klein and Manning, 2002) or priors (Johnson et al., 2007). These strategies imbue the learning process with inductive biases that guide the model to discover meaningful structures while allowing tractable algorithms for marginalization; however, they come at the expense of language modeling performance, particularly compared to sequential neural models that make no independence assumptions.

Like RNN language models, RNNGs make no independence assumptions. Instead they encode structural bias through operations that compose linguistic constituents. The lack of independence assumptions contributes to the strong language modeling performance of RNNGs, but make unsupervised learning challenging. First, marginalization is intractable. Second, the biases imposed by the RNNG are relatively weak compared to those imposed by models like PCFGs. There is little pressure for non-trivial tree structure to emerge during unsupervised RNNG (URNNG) learning.

In this work, we explore a technique for handling intractable marginalization while also injecting inductive bias. Specifically we employ amortized variational inference (Kingma and Welling, 2014; Rezende et al., 2014; Mnih and Gregor, 2014) with a *structured* inference network. Variational inference lets us tractably optimize a lower bound on the log marginal likelihood, while employing a structured inference network encourages non-trivial structure. In particular, a con-

ditional random field (CRF) constituency parser (Finkel et al., 2008; Durrett and Klein, 2015), which makes significant independence assumptions, acts as a guide on the generative model to learn meaningful trees through regularizing the posterior (Ganchev et al., 2010).

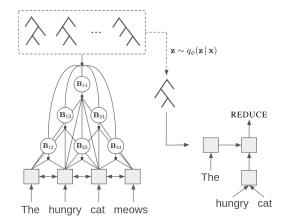
We experiment with URNNGs on English and Chinese and observe that they perform well as language models compared to their supervised counterparts and standard neural LMs. In terms of grammar induction, they are competitive with recently-proposed neural architectures that discover tree-like structures through gated attention (Shen et al., 2018). Our results, along with other recent work on joint language modeling/structure learning with deep networks (Shen et al., 2018, 2019; Wiseman et al., 2018; Kawakami et al., 2018), suggest that it is possible learn generative models of language that model the underlying data well (i.e. assign high likelihood to held-out data) and at the same time induce meaningful linguistic structure.

2 Unsupervised Recurrent Neural Network Grammars

We use $\mathbf{x} = [x_1, \dots, x_T]$ to denote a sentence of length T, and $\mathbf{z} \in \mathcal{Z}_T$ to denote an unlabeled binary parse tree over a sequence of length T, represented as a binary vector of length 2T - 1. Here 0 and 1 correspond to SHIFT and REDUCE actions, explained below. Figure 1 presents an overview of our approach.

2.1 Generative Model

An RNNG defines a joint probability distribution $p_{\theta}(\mathbf{x}, \mathbf{z})$ over sentences \mathbf{x} and parse trees \mathbf{z} . We consider a simplified version of the original RNNG (Dyer et al., 2016) by ignoring constituent labels and only considering binary trees. The RNNG utilizes an RNN to parameterize a stack data structure (Dyer et al., 2015) of partially-completed constituents to incrementally build the parse tree while generating terminals. Using the current stack representation, the model samples an action (SHIFT or REDUCE): SHIFT generates a terminal symbol, i.e. word, and shifts it onto the stack, 2 REDUCE pops the last two elements off



Inference Network $q_{\phi}(\mathbf{z} \mid \mathbf{x})$ Generative Model $p_{\theta}(\mathbf{x}, \mathbf{z})$

Figure 1: Overview of our approach. The inference network $q_{\phi}(\mathbf{z} \mid \mathbf{x})$ (left) is a CRF parser which produces a distribution over binary trees (shown in dotted box). \mathbf{B}_{ij} are random variables for existence of a constituent spanning i-th and j-th words, whose potentials are the output from a bidirectional LSTM (the global factor ensures that the distribution is only over valid binary trees). The generative model $p_{\theta}(\mathbf{x}, \mathbf{z})$ (right) is an RNNG which consists of a stack LSTM (from which actions/words are predicted) and a tree LSTM (to obtain constituent representations upon REDUCE). Training involves sampling a binary tree from $q_{\phi}(\mathbf{z} \mid \mathbf{x})$, converting it to a sequence of shift/reduce actions ($\mathbf{z} = [SHIFT, SHIFT,$ SHIFT, REDUCE, REDUCE, SHIFT, REDUCE] in the above example), and optimizing the log joint likelihood $\log p_{\theta}(\mathbf{x}, \mathbf{z})$. the stack, composes them, and shifts the composed representation onto the stack.

Formally, let $S = [(\mathbf{0}, \mathbf{0})]$ be the initial stack. Each item of the stack will be a pair, where the first element is the hidden state of the stack LSTM, and the second element is an input vector, described below. We use top(S) to refer to the top pair in the stack. The push and pop operations are defined imperatively in the usual way. At each time step, the next action z_t (SHIFT or REDUCE) is sampled from a Bernoulli distribution parameterized in terms of the current stack representation. Letting $(\mathbf{h}_{prev}, \mathbf{g}_{prev}) = top(S)$, we have

$$z_t \sim \text{Bernoulli}(p_t), \quad p_t = \sigma(\mathbf{w}^\top \mathbf{h}_{\text{prev}} + b).$$

Subsequent generation depend on z_t :

• If $z_t = 0$ (SHIFT), the model first generates a terminal symbol via sampling from a categorical distribution whose parameters come from an affine transformation and a softmax,

$$x \sim \operatorname{softmax}(\mathbf{W}\mathbf{h}_{\text{prev}} + \mathbf{b}).$$

Then the generated terminal is shifted onto the stack using a stack LSTM,

$$\mathbf{h}_{\text{next}} = \text{LSTM}(\mathbf{e}_x, \mathbf{h}_{\text{prev}}),$$

 $\text{push}(S, (\mathbf{h}_{\text{next}}, \mathbf{e}_x)),$

where e_x is the word embedding for x.

¹The cardinality of $\mathcal{Z}_T\subset\{0,1\}^{2T-1}$ is given by the (T-1)-th Catalan number, $|\mathcal{Z}_T|=\frac{(2T-2)!}{T!(T-1)!}$.

²A better name for SHIFT would be GENERATE (as in Dyer et al. (2016)), but we use SHIFT to emphasize similarity with the shift-reduce parsing.

• If $z_t = 1$ (REDUCE), we pop the last two elements off the stack,

$$(\mathbf{h}_r, \mathbf{g}_r) = \text{pop}(S), \quad (\mathbf{h}_l, \mathbf{g}_l) = \text{pop}(S),$$

and obtain a new representation that combines the left/right constituent representations using a tree LSTM (Tai et al., 2015; Zhu et al., 2015),

$$\mathbf{g}_{\text{new}} = \text{TreeLSTM}(\mathbf{g}_l, \mathbf{g}_r).$$

Note that we use \mathbf{g}_l and \mathbf{g}_r to obtain the new representation instead of \mathbf{h}_l and \mathbf{h}_r .³ We then update the stack using \mathbf{g}_{new} ,

$$\begin{split} &(\mathbf{h}_{prev}, \mathbf{g}_{prev}) = top(S), \\ &\mathbf{h}_{new} = LSTM(\mathbf{g}_{new}, \mathbf{h}_{prev}), \\ &push(S, (\mathbf{h}_{new}, \mathbf{g}_{new})). \end{split}$$

The generation process continues until an end-ofsentence symbol is generated. The parameters θ of the generative model are $\mathbf{w}, b, \mathbf{W}, \mathbf{b}$, and the parameters of the stack/tree LSTMs. For a sentence $\mathbf{x} = [x_1, \dots, x_T]$ of length T, the binary parse tree is given by the binary vector $\mathbf{z} = [z_1, \dots, z_{2T-1}]$.⁴ The joint log likelihood decomposes as a sum of terminal/action log likelihoods,

$$\log p_{\theta}(\mathbf{x}, \mathbf{z}) = \underbrace{\sum_{t=1}^{T} \log p_{\theta}(x_t \mid \mathbf{x}_{< t}, \mathbf{z}_{< n(t)})}_{\log p_{\theta}(\mathbf{x} \mid \mathbf{z})} + \underbrace{\sum_{j=1}^{2T-1} \log p_{\theta}(z_j \mid \mathbf{x}_{< m(j)}, \mathbf{z}_{< j})}_{\log p_{\theta}(\mathbf{z} \mid \mathbf{x}_{< \mathbf{z}})}$$
(1)

where $\mathbf{z}_{< n(t)}$ refers to all actions before generating the t-th word, and similarly $\mathbf{x}_{< m(j)}$ refers to all words generated before taking the j-th action. For brevity, from here on we will use $\log p_{\theta}(\mathbf{x} \mid \mathbf{z})$ to refer to the first term (terminal log likelihood) and $\log p_{\theta}(\mathbf{z} \mid \mathbf{x}_{<\mathbf{z}})$ to refer to the second term (action log likelihood) in the above decomposition.⁵

In the supervised case where ground-truth \mathbf{z} is available, we can straightforwardly perform gradient-based optimization to maximize the joint log likelihood $\log p_{\theta}(\mathbf{x}, \mathbf{z})$. In the unsupervised case, the standard approach is to maximize the log marginal likelihood,

$$\log p_{\theta}(\mathbf{x}) = \log \sum_{\mathbf{z}' \in \mathcal{Z}_T} p_{\theta}(\mathbf{x}, \mathbf{z}').$$

However this summation is intractable because z_t fully depends on all previous actions $[z_1,\ldots,z_{t-1}]$. Even if this summation were tractable, it is not clear that meaningful latent structures would emerge given the lack of explicit independence assumptions in the RNNG (e.g. it is clearly not context-free). We handle these issues with amortized variational inference.

2.2 Amortized Variational Inference

Amortized variational inference (Kingma and Welling, 2014) defines a trainable inference network ϕ that parameterizes $q_{\phi}(\mathbf{z} \mid \mathbf{x})$, a variational posterior distribution, in this case over parse trees \mathbf{z} given the sentence \mathbf{x} . This distribution is used to form an evidence lower bound (ELBO) on the log marginal likelihood,

$$\mathrm{ELBO}(\theta, \phi; \mathbf{x}) = \mathbb{E}_{q_{\phi}(\mathbf{z} \mid \mathbf{x})} \left[\log \frac{p_{\theta}(\mathbf{x}, \mathbf{z})}{q_{\phi}(\mathbf{z} \mid \mathbf{x})} \right].$$

We maximize the ELBO with respect to both model parameters θ and inference network parameters ϕ . The ELBO is still intractable to calculate exactly, but this formulation will allow us to obtain unbiased gradient estimators based on Monte Carlo sampling.

Observe that rearranging the ELBO gives the following optimization problem,

$$\max_{\theta, \phi} \log p_{\theta}(\mathbf{x}) - \mathrm{KL}[q_{\phi}(\mathbf{z} \mid \mathbf{x}) \parallel p_{\theta}(\mathbf{z} \mid \mathbf{x})].$$

Thus, ϕ is trained to match the variational posterior $q_{\phi}(\mathbf{z} \mid \mathbf{x})$ to the true posterior $p_{\theta}(\mathbf{z} \mid \mathbf{x})$, but θ is also trained to match the true posterior to the variational posterior. Indeed, there is some evidence to suggest that generative models trained with amortized variational inference (i.e. variational autoencoders) learn posterior distributions that are close to the variational family (Cremer et al., 2018).

We can use this to our advantage with an inference network that injects inductive bias. We propose to do this by using a context-free model for the inference network, in particular, a neural CRF parser (Durrett and Klein, 2015). This choice

³The update equations for the tree LSTM (and the stack LSTM) also involve *cell* states in addition to the hidden states. To reduce notational clutter we do not explicitly show the cell states and instead subsume them into g. If one (or both) of the inputs to the tree LSTM is a word embedding, the associated cell state is taken to be zero. See Tai et al. (2015) for the exact parameterization.

⁴As it stands, the support of \mathbf{z} is $\{0,1\}^{2T-1}$, all binary vectors of length 2T-1. To restrict our distribution to \mathcal{Z}_T (binary vectors which describe valid trees), we constrain z_t to be valid at each time step, which amounts to deterministically choosing $z_t = 0$ (SHIFT) if there are fewer than two elements (not counting the initial zero tuple) on the stack.

⁵The action log likelihood is the sum of log *conditional* priors, which is obviously different from the unconditional log prior $\log p_{\theta}(\mathbf{z}) = \log \sum_{\mathbf{x}} p_{\theta}(\mathbf{x}, \mathbf{z})$.

can seen as a form of posterior regularization that limits posterior flexibility of the overly powerful RNNG generative model.^{6,7}

The parameterization of span scores is similar to recent works (Wang and Chang, 2016; Stern et al., 2017; Kitaev and Klein, 2018): we add position embeddings to word embeddings and run a bidirectional LSTM over the input representations to obtain the forward $[\overrightarrow{\mathbf{h}}_1, \dots, \overrightarrow{\mathbf{h}}_T]$ and backward $[\overleftarrow{\mathbf{h}}_1, \dots, \overleftarrow{\mathbf{h}}_T]$ hidden states. The score $s_{ij} \in \mathbb{R}$ for a constituent spanning x_i to x_j is given by,

$$s_{ij} = \text{MLP}([\overrightarrow{\mathbf{h}}_{i+1} - \overrightarrow{\mathbf{h}}_i; \overleftarrow{\mathbf{h}}_{i-1} - \overleftarrow{\mathbf{h}}_j]).$$

Letting **B** be the binary matrix representation of a tree ($\mathbf{B}_{ij} = 1$ means there is a constituent spanning x_i and x_j), the CRF parser defines a distribution over binary trees via the Gibbs distribution,

$$q_{\phi}(\mathbf{B} \mid \mathbf{x}) = \frac{1}{Z_T(\mathbf{x})} \exp\left(\sum_{i < j} \mathbf{B}_{ij} s_{ij}\right),$$

where $Z_T(\mathbf{x})$ is the partition function,

$$Z_T(\mathbf{x}) = \sum_{\mathbf{B}' \in \mathcal{B}_T} \exp\left(\sum_{i \le j} \mathbf{B}'_{ij} s_{ij}\right),$$

and ϕ denotes the parameters of the inference network (i.e. the bidirectional LSTM and the MLP). Calculating $Z_T(\mathbf{x})$ requires a summation over an exponentially-sized set $\mathcal{B}_T \subset \{0,1\}^{T\times T}$, the set of all binary trees over a length T sequence. However we can perform the summation in $O(T^3)$ using the inside algorithm (Baker, 1979), shown in

⁷In preliminary experiments, we also attempted to learn latent trees with a transition-based parser (which does not make explicit independence assumptions) that looks at the entire sentence. However we found that under this setup, the inference network degenerated into a local minimum whereby it always generated left-branching trees despite various optimization strategies. Williams et al. (2018) observe a similar phenomenon in the context of learning latent trees for classification tasks. However Li et al. (2019) find that it is possible use a transition-based parser as the inference network for dependency grammar induction, if the inference network is constrained via posterior regularization (Ganchev et al., 2010) based on universal syntactic rules (Naseem et al., 2010).

Algorithm 1 Inside algorithm for calculating $Z_T(\mathbf{x})$

```
1: procedure INSIDE(s)
                                                 \triangleright scores s_{ij} for i \leq j
                                                       ⊳ length-1 spans
       for i := 1 to T do
3:
           \beta[i,i] = s_{ii}
4:
       for \ell := 1 to T - 1 do
                                                           ⊳ span length
5:
           for i := 1 to T - \ell do
                                                              ⊳ span start
6:
              j = i + \ell
                                                               ⊳ span end
              \beta[i,j] = \sum_{k=i}^{j-1} s_{ij} \cdot \beta[i,k] \cdot \beta[k+1,j]
7:
       return \beta[1,T]
                                 \triangleright return partition function Z_T(\mathbf{x})
```

Algorithm 1. This computation is itself differentiable and amenable to gradient-based optimization. Finally, letting $f: \mathcal{B}_T \to \mathcal{Z}_T$ be the bijection between the binary tree matrix representation and a sequence of SHIFT/REDUCE actions, the inference network defines a distribution over \mathcal{Z}_T via $q_{\phi}(\mathbf{z} \mid \mathbf{x}) \triangleq q_{\phi}(f^{-1}(\mathbf{z}) \mid \mathbf{x})$.

2.3 Optimization

For optimization, we use the following variant of the ELBO,

$$\mathbb{E}_{q_{\phi}(\mathbf{z} \mid \mathbf{x})}[\log p_{\theta}(\mathbf{x}, \mathbf{z})] + \mathbb{H}[q_{\phi}(\mathbf{z} \mid \mathbf{x})],$$

where $\mathbb{H}[q_{\phi}(\mathbf{z} \mid \mathbf{x})] = \mathbb{E}_{q_{\phi}(\mathbf{z} \mid \mathbf{x})}[-\log q_{\phi}(\mathbf{z} \mid \mathbf{x})]$ is the entropy of the variational posterior. A Monte Carlo estimate for the gradient with respect to θ is

$$\nabla_{\theta} \operatorname{ELBO}(\theta, \phi; \mathbf{x}) \approx \frac{1}{K} \sum_{k=1}^{K} \nabla_{\theta} \log p_{\theta}(\mathbf{x}, \mathbf{z}^{(k)}),$$

with samples $\mathbf{z}^{(1)},\dots,\mathbf{z}^{(K)}$ from $q_{\phi}(\mathbf{z}\,|\,\mathbf{x})$. Sampling uses the intermediate values calculated during the inside algorithm to sample split points recursively (Goodman, 1998; Finkel et al., 2006), as shown in Algorithm 2. The gradient with respect to ϕ involves two parts. The entropy term $\mathbb{H}[q_{\phi}(\mathbf{z}\,|\,\mathbf{x})]$ can be calculated exactly in $O(T^3)$, again using the intermediate values from the inside algorithm (see Algorithm 3). Since each step of this dynamic program is differentiable, we can obtain the gradient $\nabla_{\phi}\mathbb{H}[q_{\phi}(\mathbf{z}\,|\,\mathbf{x})]$ using automatic differentation. An estimator for the gradient with respect to $\mathbb{E}_{q_{\phi}(\mathbf{z}\,|\,\mathbf{x})}[\log p_{\theta}(\mathbf{x},\mathbf{z})]$ is obtained via the score function gradient estimator (Glynn, 1987; Williams, 1992),

$$\nabla_{\phi} \mathbb{E}_{q_{\phi}(\mathbf{z} \mid \mathbf{x})} [\log p_{\theta}(\mathbf{x}, \mathbf{z})]$$

$$= \mathbb{E}_{q_{\phi}(\mathbf{z} \mid \mathbf{x})} [\log p_{\theta}(\mathbf{x}, \mathbf{z}) \nabla_{\phi} \log q_{\phi}(\mathbf{z} \mid \mathbf{x})]$$

$$\approx \frac{1}{K} \sum_{k=1}^{K} \log p_{\theta}(\mathbf{x}, \mathbf{z}^{(k)}) \nabla_{\phi} \log q_{\phi}(\mathbf{z}^{(k)} \mid \mathbf{x}).$$

⁶While it has a similar goal, this formulation differs the from posterior regularization as formulated by Ganchev et al. (2010), which constrains the distributional family via linear constraints on posterior expectations. In our case, the conditional independence assumptions in the CRF lead to a *curved* exponential family where the vector of natural parameters has fewer dimensions than the vector of sufficient statistics of the full exponential family. This curved exponential family is a subset of the marginal polytope of the full exponential family, but it is an intersection of both linear and nonlinear manifolds, and therefore cannot be characterized through linear constraints over posterior expectations.

⁸We adapt the algorithm for calculating tree entropy in PCFGs from Hwa (2000) to the CRF case.

 $^{^9}abla_\phi\mathbb{H}[q_\phi(\mathbf{z}\,|\,\mathbf{x})]$ can also be computed using the insideoutside algorithm and a second-order expectation semiring (Li and Eisner, 2009), which has the same asymptotic runtime complexity but generally better constants.

```
procedure SAMPLE(\beta)
                                                                                                                                           \triangleright \beta from running INSIDE(s)
                              \mathbf{B} = \mathbf{0}

    binary matrix representation of tree

    3:
                              Q = [(1, T)]

    prepare property prop
    4:
                              while Q is not empty do
    5:
                                         (i,j) = pop(Q)
    6:
                                         \tau = \sum_{k=i}^{j-1} \beta[i,k] \cdot \beta[k+1,j]
     7:
                                        for k := i to j - 1 do \triangleright get distribution over splits
    8:
                                                    w_k = (\beta[i, k] \cdot \beta[k+1, j])/\tau
    9:
                                          k \sim \operatorname{Cat}([w_i, \dots, w_{j-1}]) \quad \triangleright \text{ sample a split point }
10:
                                        \mathbf{B}_{i,k} = 1, \ \mathbf{B}_{k+1,j} = 1
                                                                                                                                                                                                                   ⊳ update B
                                        if k > i then
                                                                                                                                            ⊳ if left child has width > 1
11:
12:
                                                    \operatorname{push}(Q,(i,k))
                                                                                                                                                                                                     ⊳ add to queue
13:
                                        if k+1 < j then
                                                                                                                                     \triangleright if right child has width > 1
14:
                                                    \operatorname{push}(Q,(k+1,j))

    add to queue

15:
                                                                                          \triangleright f: \mathcal{B}_T \to \mathcal{Z}_T maps matrix represen-
                                                                                                    tation of tree to sequence of actions.
16:
                              return z
```

The above estimator is unbiased but typically suffers from high variance. To reduce variance, we use a control variate derived from an average of the other samples' joint likelihoods (Mnih and Rezende, 2016), yielding the following estimator,

$$\frac{1}{K} \sum_{k=1}^{K} (\log p_{\theta}(\mathbf{x}, \mathbf{z}^{(k)}) - r^{(k)}) \nabla_{\phi} \log q_{\phi}(\mathbf{z}^{(k)} | \mathbf{x}),$$

where $r^{(k)} = \frac{1}{K-1} \sum_{j \neq k} \log p_{\theta}(\mathbf{x}, \mathbf{z}^{(j)})$. This control variate worked better than alternatives such as estimates of baselines from an auxiliary network (Mnih and Gregor, 2014; Deng et al., 2018) or a language model (Yin et al., 2018).

3 Experimental Setup

3.1 Data

For English we use the Penn Treebank (Marcus et al., 1993, PTB) with splits and preprocessing from Dyer et al. (2016) which retains punctuation and replaces singleton words with Berkeley parser's mapping rules, resulting in a vocabulary of 23,815 word types. Notably this is much larger than the standard PTB LM setup from Mikolov et al. (2010) which uses 10K types. Also different from the LM setup, we model each sentence separately instead of carrying information across sentence boundaries, as the RNNG is a generative model of sentences. Hence our perplexity numbers are not comparable to the PTB LM results (Melis et al., 2018; Merity et al., 2018; Yang et al., 2018).

Since the PTB is rather small, and since the URNNG does not require annotation, we also test our approach on a subset of the one billion word

Algorithm 3 Calculating the tree entropy $\mathbb{H}[q_{\phi}(\mathbf{z} \mid \mathbf{x})]$

```
procedure ENTROPY(\beta) \triangleright \beta from running INSIDE(s)
 2:
         for i := 1 to T do
                                               ⊳ initialize entropy table
 3:
            H[i,i] = 0
         for l := 1 to T - 1 do
 4:
                                                              ⊳ span length
 5:
            for i := 1 to T - l do
                                                                 ⊳ span start
 6:
                j = i + l
                                                                 ⊳ span end
                \tau = \sum_{u=i}^{j-1} \beta[i, u] \cdot \beta[u+1, j] for u := i to j-1 do
 7:
 8:
 9:
                   w_u = (\beta[i, u] \cdot \beta[u+1, j])/\tau
                H[i,j] = \sum_{u=i}^{j-1} (H[i,u] + H[u+1,j])
10:
11:
                              -\log w_u) \cdot w_u
12:
         return H[1,T]
                                   \triangleright return tree entropy \mathbb{H}[q_{\phi}(\mathbf{z} \mid \mathbf{x})]
```

corpus (Chelba et al., 2013). We randomly sample 1M sentences for training and 2K sentences for validation/test, and limit the vocabulary to 30K word types. While still a subset of the full corpus (which has 30M sentences), this dataset is two orders of magnitude larger than PTB. Experiments on Chinese utilize version 5.1 of the Chinese Penn Treebank (CTB) (Xue et al., 2005), with the same splits as in Chen and Manning (2014). Singleton words are replaced with a single \(\lambda UNK \rangle \) token, resulting in a vocabulary of 17,489 word types.

3.2 Training and Hyperparameters

The stack LSTM has two layers with input/hidden size equal to 650 and dropout of 0.5. The tree LSTM also has 650 units. The inference network uses a one-layer bidirectional LSTM with 256 hidden units, and the MLP (to produce span scores s_{ij} for $i \leq j$) has a single hidden layer with a ReLU nonlinearity followed by layer normalization (Ba et al., 2016) and dropout of 0.5. We share word embeddings between the generative model and the inference network, and also tie weights between the input/output word embeddings (Press and Wolf, 2016).

Optimization of the model itself required standard techniques for avoiding posterior collapse in VAEs. We warm-up the ELBO objective by linearly annealing (per batch) the weight on the conditional prior $\log p_{\theta}(\mathbf{z} \mid \mathbf{x}_{<\mathbf{z}})$ and the entropy $\mathbb{H}[q_{\phi}(\mathbf{z} \mid \mathbf{x})]$ from 0 to 1 over the first two epochs (see equation (1) for definition of $\log p_{\theta}(\mathbf{z} \mid \mathbf{x}_{<\mathbf{z}})$). This is analogous to KL-annealing in VAEs with continuous latent variables (Bowman et al., 2016; Sønderby et al., 2016). We train for 18 epochs (enough for convergence for all models) with a batch size of 16 and K=8 samples for the Monte Carlo gradient estimators. The generative model is optimized with SGD with learning rate equal to 1,

¹⁰https://github.com/clab/rnng

¹¹Both versions of the PTB data can be obtained from http://demo.clab.cs.cmu.edu/cdyer/ptb-lm.tar.gz.

¹²Posterior collapse in our context means that $q_{\phi}(\mathbf{z} \mid \mathbf{x})$ always produced trivial (always left or right branching) trees.

except for the affine layer that produces a distribution over the actions, which has learning rate 0.1. Gradients of the generative model are clipped at 5. The inference network is optimized with Adam (Kingma and Ba, 2015) with learning rate 0.0001, $\beta_1 = 0.9, \beta_2 = 0.999$, and gradient clipping at 1. As Adam converges significantly faster than SGD (even with a much lower learning rate), we stop training the inference network after the first two epochs. Initial model parameters are sampled from $\mathcal{U}[-0.1, 0.1]$. The learning rate starts decaying by a factor of 2 each epoch after the first epoch at which validation performance does not improve, but this learning rate decay is not triggered for the first eight epochs to ensure adequate training. We use the same hyperparameters/training setup for both PTB and CTB. For experiments on (the subset of) the one billion word corpus, we use a smaller dropout rate of 0.1. The baseline RNNLM also uses the smaller dropout rate.

All models are trained with an end-of-sentence token, but for perplexity calculation these tokens are not counted to be comparable to prior work (Dyer et al., 2016; Kuncoro et al., 2017; Buys and Blunsom, 2018). To be more precise, the inference network does not make use of the end-of-sentence token to produce parse trees, but the generative model is trained to generate the end-of-sentence token after the final REDUCE operation.

3.3 Baselines

We compare the unsupervised RNNG (URNNG) against several baselines: (1) RNNLM, a standard RNN language model whose size is the same as URNNG's stack LSTM; (2) Parsing Reading Predict Network (PRPN) (Shen et al., 2018), a neural language model that uses gated attention layers to embed soft tree-like structures into a neural network (and among the current state-of-the-art in grammar induction from words on the full corpus); (3) RNNG with trivial trees (left branching, right branching, random); (4) supervised RNNG trained on unlabeled, binarized gold trees. 13 Note that the supervised RNNG also trains a discriminative parser $q_{\phi}(\mathbf{z} \mid \mathbf{x})$ (alongside the generative model $p_{\theta}(\mathbf{x}, \mathbf{z})$ in order to sample parse forests for perplexity evaluation (i.e. importance sampling). This discriminative parser has the same ar-

	PTB		СТВ	
Model	PPL	F_1	PPL	F_1
RNNLM	93.2	_	201.3	_
PRPN (default)	126.2	32.9	290.9	32.9
PRPN (tuned)	96.7	41.2	216.0	36.1
Left Branching Trees	100.9	10.3	223.6	12.4
Right Branching Trees	93.3	34.8	203.5	20.6
Random Trees	113.2	17.0	209.1	17.4
URNNG	90.6	40.7	195.7	29.1
RNNG	88.7	68.1	193.1	52.3
$\text{RNNG} \rightarrow \text{URNNG}$	85.9	67.7	181.1	51.9
Oracle Binary Trees	_	82.5	_	88.6

Table 1: Language modeling perplexity (PPL) and grammar induction F_1 scores on English (PTB) and Chinese (CTB) for the different models. We separate results for those that make do not make use of annotated data (top) versus those that do (mid). Note that our PTB setup from Dyer et al. (2016) differs considerably from the usual language modeling setup (Mikolov et al., 2010) since we model each sentence independently and use a much larger vocabulary (see §3.1).

chitecture as URNNG's inference network. For all models, we perform early stopping based on validation perplexity.

4 Results and Discussion

4.1 Language Modeling

Table 1 shows perplexity for the different models on PTB/CTB. As a language model URNNG outperforms an RNNLM and is competitive with the supervised RNNG.14 The left branching baseline performs poorly, implying that the strong performance of URNNG/RNNG is not simply due to the additional depth afforded by the tree LSTM composition function (a left branching tree, which always performs REDUCE when possible, is the "deepest" model). The right branching baseline is essentially equivalent to an RNNLM and hence performs similarly. We found PRPN with default hyperparameters (which obtains a perplexity of 62.0 in the PTB setup from Mikolov et al. (2010)) to not perform well, but tuning hyperparameters improves performance.¹⁵ The supervised RNNG performs well as a language model, despite being trained on the joint (rather than marginal) likelihood objective. 16 This indicates that explicit

¹³We use right branching binarization—Matsuzaki et al. (2005) find that differences between various binarization schemes have marginal impact. Our supervised RNNG therefore differs the original RNNG, which trains on non-binarized trees and does not ignore constituent labels.

¹⁴For RNNG and URNNG we estimate the log marginal likelihood (and hence, perplexity) with K=1000 importance-weighted samples, $\log p_{\theta}(\mathbf{x}) \approx \log \left(\frac{1}{K} \sum_{k=1}^{K} \frac{\log p(\mathbf{x}, \mathbf{z}^{(k)})}{q_{\phi}(\mathbf{z}^{(k)}|\mathbf{x})}\right)$. During evaluation only, we also flatten $q_{\phi}(\mathbf{z}|\mathbf{x})$ by dividing span scores s_{ij} by a temperature term 2.0 before feeding it to the CRF.

¹⁵Using the code from https://github.com/yikangshen/ PRPN, we tuned model size, initialization, dropout, learning rate, and use of batch normalization.

¹⁶RNNG is trained to maximize $\log p_{\theta}(\mathbf{x}, \mathbf{z})$ while URNNG is trained to maximize (a lower bound on) the language modeling objective $\log p_{\theta}(\mathbf{x})$.

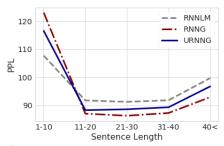


Figure 2: Perplexity of the different models grouped by sentence length on PTB.

modeling of syntax helps generalization even with richly-parameterized neural models. Encouraged by these observations, we also experiment with a hybrid approach where we train a supervised RNNG first and continue fine-tuning the model (including the inference network) on the URNNG objective (RNNG \rightarrow URNNG in Table 1).¹⁷ This approach results in nontrivial perplexity improvements, and suggests that it is potentially possible to improve language models with supervision on parsed data. In Figure 2 we show perplexity by sentence length. We find that a standard language model (RNNLM) is better at modeling short sentences, but underperforms models that explicitly take into account structure (RNNG/URNNG) when the sentence length is greater than 10. Table 2 (top) compares our results against prior work on this version of the PTB, and Table 2 (bottom) shows the results on a 1M sentence subset of the one billion word corpus, which is two orders of magnitude larger than PTB. On this larger dataset URNNG still improves upon the RNNLM. We also trained an RNNG (and RNNG → URNNG) on this dataset by parsing the training set with the self-attentive parser from Kitaev and Klein (2018). These models improve upon the RNNLM but not the URNNG, potentially highlighting the limitations of using predicted trees for supervising RNNGs.

4.2 Grammar Induction

Table 1 also shows the F_1 scores for grammar induction. Note that we induce latent trees directly from words on the full dataset.¹⁹ For

PTB	PPL
KN 5-gram (Dyer et al., 2016)	169.3
RNNLM (Dyer et al., 2016)	113.4
Original RNNG (Dyer et al., 2016)	102.4
Stack-only RNNG (Kuncoro et al., 2017)	101.2
Gated-Attention RNNG (Kuncoro et al., 2017)	100.9
Generative Dep. Parser (Buys and Blunsom, 2015)	138.6
RNNLM (Buys and Blunsom, 2018)	100.7
Sup. Syntactic NLM (Buys and Blunsom, 2018)	107.6
Unsup. Syntactic NLM (Buys and Blunsom, 2018)	125.2
PRPN [†] (Shen et al., 2018)	96.7
This work:	
RNNLM	93.2
URNNG	90.6
RNNG	88.7
$RNNG \rightarrow URNNG$	85.9
1M Sentences	PPL
PRPN [†] (Shen et al., 2018)	77.7
RNNLM	77.4
URNNG	71.8
$RNNG^{\ddagger}$	72.9
$RNNG^{\ddagger} o URNNG$	72.0

Table 2: (Top) Comparison of this work as a language model against prior works on sentence-level PTB with preprocessing from Dyer et al. (2016). Note that previous versions of RNNG differ from ours in terms of parameterization and model size. (Bottom) Results on a subset (1M sentences) of the one billion word corpus. PRPN † is the model from Shen et al. (2018), whose hyperparameters were tuned by us. RNNG ‡ is trained on predicted parse trees from the self-attentive parser from Kitaev and Klein (2018).

RNNG/URNNG we obtain the highest scoring tree from $q_{\phi}(\mathbf{z} \mid \mathbf{x})$ through the Viterbi inside (i.e. CKY) algorithm.²⁰ We calculate unlabeled F_1 using evalb, which ignores punctuation and discards trivial spans (width-one and sentence spans).²¹ Since we compare F_1 against the original, non-binarized trees (per convention), F_1 scores of models using oracle binarized trees constitute the upper bounds.

We confirm the replication study of Htut et al. (2018) and find that PRPN is a strong model for grammar induction. URNNG performs on par with PRPN on English but PRPN does better on Chinese; both outperform right branching base-

 $^{^{17}}$ We fine-tune for 10 epochs and use a smaller learning rate of 0.1 for the generative model.

 $^{^{18}}$ To parse the training set we use the benepar_en2 model from https://github.com/nikitakit/self-attentive-parser, which obtains an F_1 score of 95.17 on the PTB test set.

¹⁹Past work on grammar induction usually train/evaluate on short sentences and also assume access to gold POS tags (Klein and Manning, 2002; Smith and Eisner, 2004; Bod, 2006). However more recent works do train directly words (Jin et al., 2018; Shen et al., 2018; Drozdov et al., 2019).

²⁰Alternatively, we could estimate $\arg \max_{\mathbf{z}} p_{\theta}(\mathbf{z} \mid \mathbf{x})$ by sampling parse trees from $q_{\phi}(\mathbf{z} \mid \mathbf{x})$ and using $p_{\theta}(\mathbf{x}, \mathbf{z})$ to rerank the output, as in Dyer et al. (2016).

 $^{^{21}}$ Available at https://nlp.cs.nyu.edu/evalb/. We evaluate with COLLINS.prm parameter file and LABELED option equal to 0. We observe that the setup for grammar induction varies widely across different papers: lexicalized vs. unlexicalized; use of punctuation vs. not; separation of train/test sets; counting sentence-level spans for evaluation vs. ignoring them; use of additional data; length cutoff for training/evaluation; corpus-level F_1 vs. sentence-level F_1 ; and, more. In our survey of twenty or so papers, almost no two papers were identical in their setup. Such variation makes it difficult to meaningfully compare models across papers. Hence, we report grammar induction results mainly for the models and baselines considered in the present work.

Tree	PTB	СТВ	Label	URNNG	PRPN
Gold	40.7	29.1	SBAR	74.8%	28.9%
Left	9.2	8.4	NP	39.5%	63.9%
Right	68.3	51.2	VP	76.6%	27.3%
Self	92.3	87.3	PP	55.8%	55.1%
RNNG	55.4	47.1	ADJP	33.9%	42.5%
PRPN	41.0	47.2	ADVP	50.4%	45.1%

Table 3: (Left) F_1 scores of URNNG against other trees. "Self" refers to another URNNG trained with a different random seed. (Right) Recall of constituents by label for URNNG and PRPN. Recall for a particular label is the fraction of ground truth constituents of that label that were identified by the model (as in Htut et al. (2018)).

	F_1	+PP
PRPN-UP [‡]	39.8	45.4
PRPN-LM [‡]	42.8	42.4
ON-LSTM [‡] (Shen et al., 2019)	49.4	_
DIORA [‡] (Drozdov et al., 2019)	49.6	56.2
PRPN (tuned)	49.0	49.9
URNNG	52.4	52.4

Table 4: PTB F_1 scores using the same evaluation setup as Drozdov et al. (2019), which evaluates against binarized trees, counts punctuation and trivial spans, and uses sentence-level F_1 . +PP indicates a post-processing heuristic which directly attaches trailing punctuation to the root. This does not change URNNG results since it learns to do so anyway. Results with ‡ are copied from Table 1 of Drozdov et al. (2019).

lines. Table 3 further analyzes the learned trees and shows the F_1 score of URNNG trees against other trees (left), and the recall of URNNG/PRPN trees against ground truth constituents (right). We find that trees induced by URNNG and PRPN are quite different; URNNG is more sensitive to SBAR and VP, while PRPN is better at identifying NP. While left as future work, this naturally suggests a hybrid approach wherein the intersection of constituents from URNNG and PRPN is used to create a corpus of partially annotated trees, which can be used to guide another model, e.g. via posterior regularization (Ganchev et al., 2010) or semisupervision (Hwa, 1999). Finally, Table 4 compares our results using the same evaluation setup as in Drozdov et al. (2019), which differs considerably from our setup.

4.3 Distributional Metrics

Table 5 shows some standard metrics related to the learned generative model/inference network. The "reconstruction" perplexity based on $\mathbb{E}_{q_{\phi}(\mathbf{z}\,|\,\mathbf{x})}[\log p_{\theta}(\mathbf{x}\,|\,\mathbf{z})]$ is much lower than regular perplexity, and further, the Kullback-Leibler divergence between the conditional prior and the variational posterior, given by

$$\mathbb{E}_{q_{\phi}(\mathbf{z} \mid \mathbf{x})} \left[\log \frac{q_{\phi}(\mathbf{z} \mid \mathbf{x})}{p_{\theta}(\mathbf{z} \mid \mathbf{x}_{<\mathbf{z}})} \right],$$

	PTB		CTB	
	RNNG	URNNG	RNNG	URNNG
PPL	88.7	90.6	193.1	195.7
Recon. PPL	74.6	73.4	183.4	151.9
KL	7.10	6.13	11.11	8.91
Prior Entropy	7.65	9.61	9.48	15.13
Post. Entropy	1.56	2.28	6.23	5.75
Unif. Entropy	26.07	26.07	30.17	30.17

Table 5: Metrics related to the generative model/inference network for RNNG/URNNG. For the supervised RNNG we take the "inference network" to be the discriminative parser trained alongside the generative model (see §3.3). Recon. PPL is the reconstruction perplexity based on $\mathbb{E}_{q_{\phi}(\mathbf{z} \mid \mathbf{x})}[\log p_{\theta}(\mathbf{x} \mid \mathbf{z})]$, and KL is the Kullback-Leibler divergence. Prior entropy is the entropy of the conditional prior $p_{\theta}(\mathbf{z} \mid \mathbf{x}_{<\mathbf{z}})$, and uniform entropy is the entropy of the uniform distribution over all binary trees. The KL/entropy metrics are averaged across sentences.

is highly nonzero. (See equation (1) for definitions of $\log p_{\theta}(\mathbf{x} \mid \mathbf{z})$ and $\log p_{\theta}(\mathbf{z} \mid \mathbf{x}_{<\mathbf{z}})$). This indicates that the latent space is being used in a meaningful way and that there is no posterior collapse (Bowman et al., 2016). As expected, the entropy of the variational posterior is much lower than the entropy of the conditional prior, but there is still some uncertainty in the posterior.

4.4 Syntactic Evaluation

We perform a syntactic evaluation of the different models based on the setup from Marvin and Linzen (2018): the model is given two minimally different sentences, one grammatical and one ungrammatical, and must identify the grammatical sentence by assigning it higher probability.²² Table 6 shows the accuracy results. Overall the supervised RNNG significantly outperforms the other models, indicating opportunities for further work in unsupervised modeling. While the URNNG does slightly outperform an RNNLM, the distribution of errors made from both models are similar, and thus it is not clear whether the outperformance is simply due to better perplexity or learning different structural biases.

4.5 Limitations

There are several limitations to our approach. For one, the URNNG takes considerably more time/memory to train than a standard language model due to the ${\cal O}(T^3)$ dynamic program in the inference network, multiple samples to obtain low-variance gradient estimators, and dynamic

²²We modify the publicly available dataset from https://github.com/BeckyMarvin/LM.syneval to only keep sentence pairs that did not have any unknown words with respect to our vocabulary, resulting in 80K sentence pairs for evaluation. Further, we train on a much smaller corpus, and hence our results are not directly comparable.

	RNNLM	PRPN	RNNG	URNNG
PPL	93.2	96.7	88.7	90.6
Overall	62.5%	61.9%	69.3%	64.6%
Subj.	63.5%	63.7%	89.4%	67.2%
Obj. Rel.	62.6%	61.0%	67.6%	65.7%
Refl.	60.7%	68.8%	57.3%	60.5%
NPI	58.7%	39.5%	46.8%	55.0%

Table 6: Syntactic evaluation based on the setup from Marvin and Linzen (2018). Subj. is subject-verb agreement in sentential complement, across prepositional phrase/subjective relative clause, and VP coordination; Obj. Rel. refers to subject-verb agreement in/across an objective relative clause; Refl. refers to reflexive pronoun agreement with antecedent; NPI is negative polarity items.

computation graphs that make efficient batching nontrivial.²³ The model is sensitive to hyperparameters and required various optimization strategies (e.g. separate optimizers for the inference network and the generative model) to avoid posterior collapse. Finally, the URNNG also seemed to rely heavily on punctuation to identify constituents and we were unable to improve upon a right-branching baseline when training the URNNG on a version of PTB where punctuation is removed.²⁴

5 Related Work

There has been much work on incorporating tree structures into deep models for syntax-aware language modeling, both for unconditional (Emami and Jelinek, 2005; Buys and Blunsom, 2015; Dyer et al., 2016) and conditional (Yin and Neubig, 2017; Alvarez-Melis and Jaakkola, 2017; Rabinovich et al., 2017; Aharoni and Goldberg, 2017; Eriguchi et al., 2017; Wang et al., 2018; Gū et al., 2018) cases. These approaches generally rely on annotated parse trees during training and maximizes the joint likelihood of sentence-tree pairs. Prior work on combining language modeling and unsupervised tree learning typically embed soft, tree-like structures as hidden layers of a deep net-

work (Cho et al., 2014; Chung et al., 2017; Shen et al., 2018, 2019). In contrast, Buys and Blunsom (2018) make Markov assumptions and perform exact marginalization over latent dependency trees. Our work is also related to the recent line of work on learning latent trees as part of a deep model through supervision on other tasks, typically via differentiable structured hidden layers (Kim et al., 2017; Bradbury and Socher, 2017; Liu and Lapata, 2018; Tran and Bisk, 2018; Peng et al., 2018; Niculae et al., 2018; Liu et al., 2018), policy gradient-based approaches (Yogatama et al., 2017; Williams et al., 2018; Havrylov et al., 2019), or differentiable relaxations (Choi et al., 2018; Maillard and Clark, 2018).

The variational approximation uses amortized inference (Kingma and Welling, 2014; Mnih and Gregor, 2014; Rezende et al., 2014), in which an inference network is used to obtain the variational posterior for each observed x. Since our inference network is structured (i.e., a CRF), it is also related to CRF autoencoders (Ammar et al., 2014) and structured VAEs (Johnson et al., 2016; Krishnan et al., 2017), which have been used previously for unsupervised (Cai et al., 2017; Drozdov et al., 2019; Li et al., 2019) and semi-supervised (Yin et al., 2018; Corro and Titov, 2019) parsing.

6 Conclusion

It is an open question as to whether explicit modeling of syntax significantly helps neural models. Strubell et al. (2018) find that supervising intermediate attention layers with syntactic heads improves semantic role labeling, while Shi et al. (2018) observe that for text classification, syntactic trees only have marginal impact. Our work suggests that at least for language modeling, incorporating syntax either via explicit supervision or as latent variables does provide useful inductive biases and improves performance.

Finally, in modeling child language acquisition, the complex interaction of the parser and the grammatical knowledge being acquired is the object of much investigation (Trueswell and Gleitman, 2007); our work shows that apparently grammatical constraints can emerge from the interaction of a constrained parser and a more general grammar learner, which is an intriguing but underexplored hypothesis for explaining human linguistic biases.

Acknowledgments

We thank the members of the DeepMind language team for helpful feedback. YK is supported by a Google Fellowship. AR is supported by NSF Career 1845664.

²³The main time bottleneck is the dynamic compution graph, since the dynamic programming algorithm can be batched (however the latter is a significant memory bottleneck). We manually batch the SHIFT and REDUCE operation as much as possible, though recent work on auto-batching (Neubig et al., 2017) could potentially make this easier/faster.

²⁴Many prior works that induce trees directly from words often employ additional heuristics based on punctuation (Seginer, 2007; Ponvert et al., 2011; Spitkovsky et al., 2013; Parikh et al., 2014), as punctuation (e.g. comma) is usually a reliable signal for start/end of constituent spans. The URNNG still has to *learn* to rely on punctuation, similar to recent works such as depth-bounded PCFGs (Jin et al., 2018) and DIORA (Drozdov et al., 2019). In contrast, PRPN (Shen et al., 2018) and Ordered Neurons (Shen et al., 2019) induce trees by directly training on corpus without punctuation. We also reiterate that punctuation is used during training but ignored during evaluation (except in Table 4).

References

- Roee Aharoni and Yoav Goldberg. 2017. Towards String-to-Tree Neural Machine Translation. In *Proceedings of ACL*.
- David Alvarez-Melis and Tommi S. Jaakkola. 2017. Tree-structured Decoding with Doubly-Recurrent Neural Networks. In *Proceedings of ICLR*.
- Waleed Ammar, Chris Dyer, and Noah A. Smith. 2014. Conditional Random Field Autoencoders for Unsupervised Structured Prediction. In *Proceedings of NIPS*.
- Jimmy Lei Ba, Jamie Ryan Kiros, and Geoffrey E. Hinton. 2016. Layer Normalization. In *Proceedings of NIPS*.
- James K. Baker. 1979. Trainable Grammars for Speech Recognition. In Proceedings of the Spring Conference of the Acoustical Society of America.
- Rens Bod. 2006. An All-Subtrees Approach to Unsupervised Parsing. In *Proceedings of ACL*.
- Samuel R. Bowman, Luke Vilnis, Oriol Vinyal, Andrew M. Dai, Rafal Jozefowicz, and Samy Bengio. 2016. Generating Sentences from a Continuous Space. In *Proceedings of CoNLL*.
- James Bradbury and Richard Socher. 2017. Towards Neural Machine Translation with Latent Tree Attention. In Proceedings of the 2nd Workshop on Structured Prediction for Natural Language Processing.
- Jan Buys and Phil Blunsom. 2015. Generative Incremental Dependency Parsing with Neural Networks. In *Proceedings of ACL*.
- Jan Buys and Phil Blunsom. 2018. Neural Syntactic Generative Models with Exact Marginalization. In *Proceedings of NAACL*.
- Jiong Cai, Yong Jiang, and Kewei Tu. 2017. CRF Autoencoder for Unsupervised Dependency Parsing. In *Proceed*ings of EMNLP.
- Ciprian Chelba, Tomas Mikolov, Mike Schuster, Qi Ge, Thorsten Brants, Phillipp Koehn, and Tony Robinson. 2013. One Billion Word Benchmark for Measuring Progress in Statistical Language Modeling. arXiv:1312.3005.
- Danqi Chen and Christopher D. Manning. 2014. A Fast and Accurate Dependency Parser using Neural Networks. In *Proceedings of EMNLP*.
- Kyunghyun Cho, Bart van Merrienboer, Dzmitry Bahdanau, and Yoshua Bengio. 2014. On the Properties of Neural Machine Translation: Encoder-Decoder Approaches. In *Proceedings of Eighth Workshop on Syntax, Semantics and Structure in Statistical Translation*.
- Jihun Choi, Kang Min Yoo, and Sang goo Lee. 2018. Learning to Compose Task-Specific Tree Structures. In *Proceedings of AAAI*.
- Junyoung Chung, Sungjin Ahn, and Yoshua Bengio. 2017. Hierarchical Multiscale Recurrent Neural Networks. In *Proceedings of ICLR*.
- Caio Corro and Ivan Titov. 2019. Differentiable Perturb-and-Parse: Semi-Supervised Parsing with a Structured Variational Autoencoder. In *Proceedings of ICLR*.

- Chris Cremer, Xuechen Li, and David Duvenaud. 2018. Inference Suboptimality in Variational Autoencoders. In *Proceedings of ICML*.
- Yuntian Deng, Yoon Kim, Justin Chiu, Demi Guo, and Alexander M. Rush. 2018. Latent Alignment and Variational Attention. In *Proceedings of NIPS*.
- Andrew Drozdov, Patrick Verga, Mohit Yadev, Mohit Iyyer, and Andrew McCallum. 2019. Unsupervised Latent Tree Induction with Deep Inside-Outside Recursive Auto-Encoders. In *Proceedings of NAACL*.
- Greg Durrett and Dan Klein. 2015. Neural CRF Parsing. In *Proceedings of ACL*.
- Chris Dyer, Miguel Ballesteros, Wang Ling, Austin Matthews, and Noah A. Smith. 2015. Transition-Based Dependency Parsing with Stack Long Short-Term Memory. In *Proceedings of ACL*.
- Chris Dyer, Adhiguna Kuncoro, Miguel Ballesteros, and Noah A. Smith. 2016. Recurrent Neural Network Grammars. In *Proceedings of NAACL*.
- Ahmad Emami and Frederick Jelinek. 2005. A Neural Syntactic Language Model. *Machine Learning*, 60:195–227.
- Akiko Eriguchi, Yoshimasa Tsuruoka, and Kyunghyun Cho. 2017. Learning to Parse and Translate Improves Neural Machine Translation. In *Proceedings of ACL*.
- Jenny Rose Finkel, Alex Kleeman, and Christopher D. Manning. 2008. Efficient, Feature-based, Conditional Random Field Parsing. In *Proceedings of ACL*.
- Jenny Rose Finkel, Christopher D. Manning, and Andrew Y. Ng. 2006. Solving the Problem of Cascading Errors: Approximate Bayesian Inference for Linguistic Annotation Pipelines. In *Proceedings of EMNLP*.
- Kuzman Ganchev, João Graça, Jennifer Gillenwater, and Ben Taskar. 2010. Posterior Regularization for Structured Latent Variable Models. *Journal of Machine Learning Re*search, 11:2001–2049.
- Peter Glynn. 1987. Likelihood Ratio Gradient Estimation: An Overview. In *Proceedings of Winter Simulation Conference*.
- Joshua Goodman. 1998. Parsing Inside-Out. *PhD thesis, Harvard University*.
- Jetic Gū, Hassan S. Shavarani, and Anoop Sarkar. 2018. Topdown Tree Structured Decoding with Syntactic Connections for Neural Machine Translation and Parsing. In Proceedings of EMNLP.
- John Hale, Chris Dyer, Adhiguna Kuncoro, and Jonathan R. Brennan. 2018. Finding Syntax in Human Encephalography with Beam Search. In *Proceedings of ACL*.
- Serhii Havrylov, Germán Kruszewski, and Armand Joulin. 2019. Cooperative Learning of Disjoint Syntax and Semantics. In *Proceedings of NAACL*.
- Phu Mon Htut, Kyunghyun Cho, and Samuel R. Bowman. 2018. Grammar Induction with Neural Language Models: An Unusual Replication. In *Proceedings of EMNLP*.
- Rebecca Hwa. 1999. Supervised Grammar Induction Using Training Data with Limited Constituent Information. In *Proceedings of ACL*.

- Rebecca Hwa. 2000. Sample Selection for Statistical Grammar Induction. In *Proceedings of EMNLP*.
- Lifeng Jin, Finale Doshi-Velez, Timothy Miller, William Schuler, and Lane Schwartz. 2018. Unsupervised Grammar Induction with Depth-bounded PCFG. In *Proceed-ings of TACL*.
- Mark Johnson, Thomas L. Griffiths, and Sharon Goldwater. 2007. Bayesian Inference for PCFGs via Markov chain Monte Carlo. In *Proceedings of NAACL*.
- Matthew Johnson, David K. Duvenaud, Alex Wiltschko, Ryan P. Adams, and Sandeep R. Datta. 2016. Composing Graphical Models with Neural Networks for Structured Representations and Fast Inference. In *Proceedings* of NIPS.
- Kazuya Kawakami, Chris Dyer, and Phil Blunsom. 2018. Unsupervised Word Discovery with Segmental Neural Language Models. arXiv:1811.09353.
- Yoon Kim, Carl Denton, Luong Hoang, and Alexander M. Rush. 2017. Structured Attention Networks. In *Proceedings of ICLR*.
- Diederik P. Kingma and Jimmy Ba. 2015. Adam: A Method for Stochastic Optimization. In *Proceedings of ICLR*.
- Diederik P. Kingma and Max Welling. 2014. Auto-Encoding Variational Bayes. In *Proceedings of ICLR*.
- Nikita Kitaev and Dan Klein. 2018. Constituency Parsing with a Self-Attentive Encoder. In *Proceedings of ACL*.
- Dan Klein and Christopher Manning. 2002. A Generative Constituent-Context Model for Improved Grammar Induction. In *Proceedings of ACL*.
- Rahul G. Krishnan, Uri Shalit, and David Sontag. 2017. Structured Inference Networks for Nonlinear State Space Models. In *Proceedings of AAAI*.
- Adhiguna Kuncoro, Miguel Ballesteros, Lingpeng Kong, Chris Dyer, Graham Neubig, and Noah A. Smith. 2017. What Do Recurrent Neural Network Grammars Learn About Syntax? In *Proceedings of EACL*.
- Adhiguna Kuncoro, Chris Dyer, John Hale, Dani Yogatama, Stephen Clark, and Phil Blunsom. 2018. LSTMs Can Learn Syntax-Sensitive Dependencies Well, But Modeling Structure Makes Them Better. In *Proceedings of ACL*.
- Bowen Li, Jianpeng Cheng, Yang Liu, and Frank Keller. 2019. Dependency Grammar Induction with a Neural Variational Transition-based Parser. In *Proceedings of AAAI*.
- Zhifei Li and Jason Eisner. 2009. First- and Second-Order Expectation Semirings with Applications to Minimum-Risk Training on Translation Forests. In *Proceedings of EMNLP*.
- Yang Liu, Matt Gardner, and Mirella Lapata. 2018. Structured Alignment Networks for Matching Sentences. In Proceedings of EMNLP.
- Yang Liu and Mirella Lapata. 2018. Learning Structured Text Representations. In *Proceedings of TACL*.

- Jean Maillard and Stephen Clark. 2018. Latent Tree Learning with Differentiable Parsers: Shift-Reduce Parsing and Chart Parsing. In Proceedings of the Workshop on the Relevance of Linguistic Structure in Neural Architectures for NLP.
- Mitchell P. Marcus, Mary Ann Marcinkiewicz, and Beatrice Santorini. 1993. Building a Large Annotated Corpus of English: The Penn Treebank. *Computational Linguistics*, 19:313–330.
- Rebecca Marvin and Tal Linzen. 2018. Targeted Syntactic Evaluation of Language Models. In *Proceedings of EMNLP*.
- Takuya Matsuzaki, Yusuke Miyao, and Junichi Tsujii. 2005. Probabilistic CFG with Latent Annotations. In *Proceedings of ACL*.
- Gábor Melis, Chris Dyer, and Phil Blunsom. 2018. On the State of the Art of Evaluation in Neural Language Models. In *Proceedings of ICLR*.
- Stephen Merity, Nitish Shirish Keskar, and Richard Socher. 2018. Regularizing and Optimizing LSTM Language Models. In *Proceedings of ICLR*.
- Tomas Mikolov, Martin Karafiat, Lukas Burget, Jan Cernocky, and Sanjeev Khudanpur. 2010. Recurrent Neural Network Based Language Model. In *Proceedings of IN-TERSPEECH*.
- Andriy Mnih and Karol Gregor. 2014. Neural variational inference and learning in belief networks. In *Proceedings of ICML*.
- Andriy Mnih and Danilo J. Rezende. 2016. Variational Inference for Monte Carlo Objectives. In *Proceedings of ICML*.
- Tahira Naseem, Harr Chen, Regina Barzilay, and Mark Johnson. 2010. Using Universal Linguistic Knowledge to Guide Grammar Induction. In *Proceedings of EMNLP*.
- Graham Neubig, Yoav Goldberg, and Chris Dyer. 2017. On-the-fly Operation Batching in Dynamic Computation Graphs. arXiv:1705.07860.
- Vlad Niculae, André F. T. Martins, and Claire Cardie. 2018. Towards Dynamic Computation Graphs via Sparse Latent Structure. In *Proceedings of EMNLP*.
- Ankur P. Parikh, Shay B. Cohen, and Eric P. Xing. 2014. Spectral Unsupervised Parsing with Additive Tree Metrics. In *Proceedings of ACL*.
- Hao Peng, Sam Thomson, and Noah A. Smith. 2018. Backpropagating through Structured Argmax using a SPIGOT. In *Proceedings of ACL*.
- Elis Ponvert, Jason Baldridge, and Katrin Erk. 2011. Simpled Unsupervised Grammar Induction from Raw Text with Cascaded Finite State Methods. In *Proceedings of ACL*.
- Ofir Press and Lior Wolf. 2016. Using the Output Embedding to Improve Language Models. In *Proceedings of EACL*.
- Maxim Rabinovich, Mitchell Stern, and Dan Klein. 2017. Abstract Syntax Networks for Code Generation and Semantic Parsing. In *Proceedings of ACL*.

- Danilo J. Rezende, Shakir Mohamed, and Daan Wierstra. 2014. Stochastic Backpropagation and Approximate Inference in Deep Generative Models. In *Proceedings of ICML*.
- Yoav Seginer. 2007. Fast Unsupervised Incremental Parsing. In *Proceedings of ACL*.
- Yikang Shen, Zhouhan Lin, Chin-Wei Huang, and Aaron Courville. 2018. Neural Language Modeling by Jointly Learning Syntax and Lexicon. In *Proceedings of ICLR*.
- Yikang Shen, Shawn Tan, Alessandro Sordoni, and Aaron Courville. 2019. Ordered Neurons: Integrating Tree Structures into Recurrent Neural Networks. In *Proceedings of ICLR*.
- Haoyue Shi, Hao Zhou, Jiaze Chen, and Lei Li. 2018. On Tree-based Neural Sentence Modeling. In *Proceedings of EMNLP*.
- Noah A. Smith and Jason Eisner. 2004. Annealing Techniques for Unsupervised Statistical Language Learning. In *Proceedings of ACL*.
- Casper Kaae Sønderby, Tapani Raiko, Lars Maaløe, Søren Kaae Sønderby, and Ole Winther. 2016. Ladder Variational Autoencoders. In *Proceedings of NIPS*.
- Valentin I. Spitkovsky, Hiyan Alshawi, and Daniel Jurafsky. 2013. Breaking Out of Local Optima with Count Transforms and Model Recombination: A Study in Grammar Induction. In *Proceedings of EMNLP*.
- Mitchell Stern, Jacob Andreas, and Dan Klein. 2017. A Minimal Span-Based Neural Constituency Parser. In Proceedings of ACL.
- Emma Strubell, Patrick Verga, Daniel Andor, David Weiss, and Andrew McCallum. 2018. Linguistically-Informed Self-Attention for Semantic Role Labeling. In *Proceedings of EMNLP*.
- Kai Sheng Tai, Richard Socher, and Christopher D. Manning. 2015. Improved Semantic Representations From Tree-Structured Long Short-Term Memory Networks. In Proceedings of ACL.
- Ke Tran and Yonatan Bisk. 2018. Inducing Grammars with and for Neural Machine Translation. In *Proceedings of the 2nd Workshop on Neural Machine Translation and Generation*.
- John C. Trueswell and Lila R. Gleitman. 2007. Learning to Parse and its Implications for Language Acquisition. *The* Oxford Handbook of Psycholinguistics.
- Wenhui Wang and Baobao Chang. 2016. Graph-based Dependency Parsing with Bidirectional LSTM. In *Proceedings of ACL*.
- Xinyi Wang, Hieu Pham, Pengcheng Yin, and Graham Neubig. 2018. A Tree-based Decoder for Neural Machine Translation. In *Proceedings of EMNLP*.
- Adina Williams, Andrew Drozdov, and Samuel R. Bowman. 2018. Do Latent Tree Learning Models Identify Meaningful Structure in Sentences? In *Proceedings of TACL*.
- Ronald J. Williams. 1992. Simple Statistical Gradientfollowing Algorithms for Connectionist Reinforcement Learning. *Machine Learning*, 8.

- Sam Wiseman, Stuart M. Shieber, and Alexander M. Rush. 2018. Learning Neural Templates for Text Generation. In *Proceedings of EMNLP*.
- Naiwen Xue, Fei Xia, Fu dong Chiou, and Marta Palmer. 2005. The Penn Chinese Treebank: Phrase Structure Annotation of a Large Corpus. *Natural Language Engineer*ing, 11:207–238.
- Zhilin Yang, Zihang Dai, Ruslan Salakhutdinov, and William W. Cohen. 2018. Breaking the Softmax Bottleneck: A High-Rank RNN Language Model. In *Proceed*ings of ICLR.
- Pengcheng Yin and Graham Neubig. 2017. A Syntactic Neural Model for General-Purpose Code Generation. In *Proceedings of ACL*.
- Pengcheng Yin, Chunting Zhou, Junxian He, and Graham Neubig. 2018. StructVAE: Tree-structured Latent Variable Models for Semi-supervised Semantic Parsing. In Proceedings of ACL.
- Dani Yogatama, Phil Blunsom, Chris Dyer, Edward Grefenstette, and Wang Ling. 2017. Learning to Compose Words into Sentences with Reinforcement Learning. In *Proceedings of ICLR*.
- Xiaodan Zhu, Parinaz Sobhani, and Hongyu Guo. 2015. Long Short-Term Memory Over Tree Structures. In Proceedings of ICML.