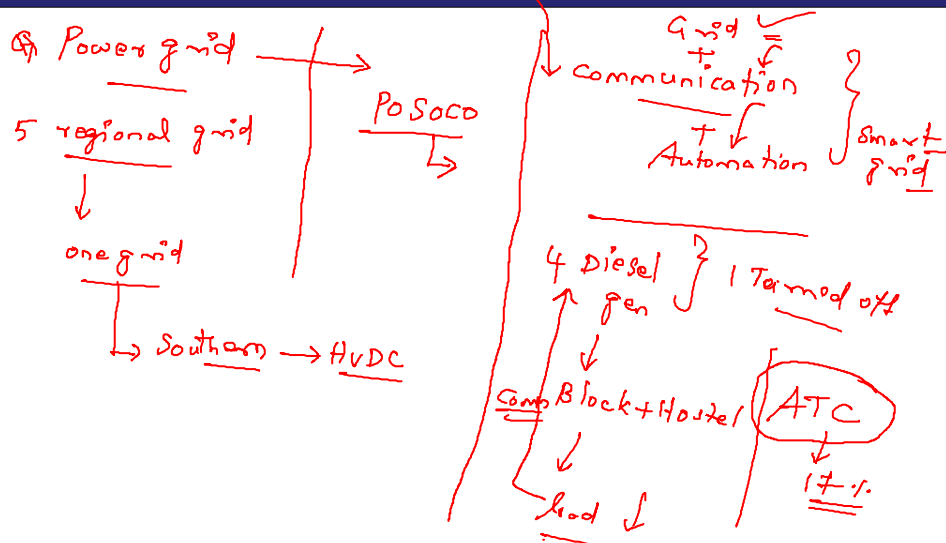


## Unit - I

### 1.7 Electrostatics

Dr.Santhosh.T.K.

## Smart Grid



## Syllabus

### UNIT – I

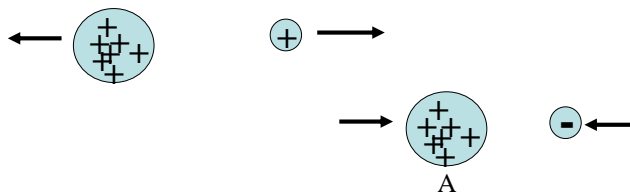
**10 Periods**

**Introduction and Basic Concepts:** Concept of Potential difference, voltage, current - Fundamental linear passive and active elements to their functional current-voltage relation - Terminology and symbols in order to describe electric networks - Concept of work, power, energy and conversion of energy- Principle of batteries and application.

**Principles of Electrostatics:** Electrostatic field - electric field intensity - electric field strength - absolute permittivity - relative permittivity - capacitor composite – dielectric capacitors - capacitors in series & parallel - energy stored in capacitors - charging and discharging of capacitors.

## The Electric Field

Between two charged bodies there is a force,  $F$ , of attraction or repulsion:

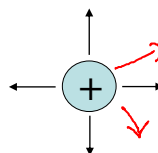


We don't understand why; we can only say this is what happens.

We can think of a charged body as *changing the nature of the space surrounding it*.

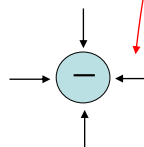
## Direction of the Electric Field

Outward (away) from a positive charge



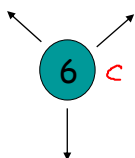
*These are called "field arrows"*

Inward (towards) a negative charge



## Direction of the Electric Field

We draw the number of arrows proportional to the charge...more charge, more arrows. Say the charges are in " $\mu\text{Coulombs}$ " (that's micro-coulombs, or  $10^{-6}$  Coulombs)

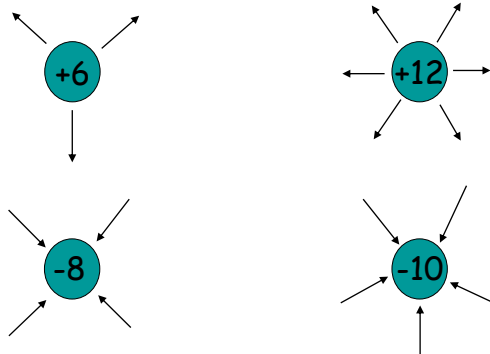




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## Direction of the Electric Field

We draw the number of arrows proportional to the charge...more charge, more arrows. Say the charges are in “ $\mu\text{Coulombs}$ ” (that’s micro-coulombs, or  $10^{-6}$  Coulombs)



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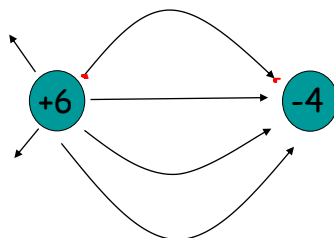


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## Direction of the Electric Field

When charges get near each other, these fields interact

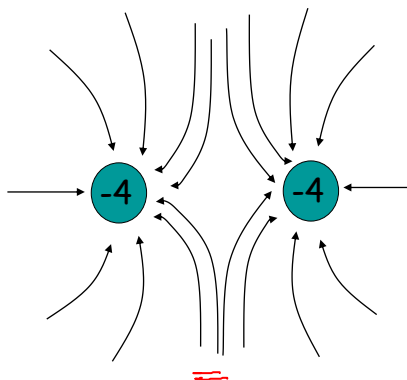
For unlike charges, the arrows go from the positive charge to the negative charge:



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For like particles the arrows are repelled:



The field arrows never cross in either case

## Electric Field Intensity (Cont'd)

It becomes convenient to define electric field intensity  $E_1$  or force per unit charge as:

$$E_1 = \frac{F_{12}}{Q_2}$$

This field from charge  $Q_1$  fixed at origin results from the force vector  $F_{12}$  for any arbitrarily chosen value of  $Q_2$



## Electric Field Intensity (Cont'd)

Coulomb's law can be rewritten as

$$\vec{E} = \frac{Q}{4\pi\epsilon_0 |\vec{R}|^2} \vec{a}_R$$

$$F = \frac{Q_1 Q_2}{4\pi\epsilon_0 r^2}$$

$$E = \frac{F}{Q} = \frac{Q}{4\pi\epsilon_0 r^2}$$

to find the electric field intensity at any point in space resulting from a fixed charge  $Q$ .



## Example 2



Find  $\vec{E}$  at (0,3,4) m in cartesian coordinates due to a point charge  $Q = 0.5\mu\text{C}$  at the origin.

### Solution to Example 2

$$\vec{R} = 3\vec{a}_y + 4\vec{a}_z$$

$$\vec{a}_R = (3\vec{a}_y + 4\vec{a}_z) / 5$$

$$R = 5$$

$$= 0.6\vec{a}_y + 0.8\vec{a}_z$$

$$\vec{E} = \frac{0.5 \times 10^{-6}}{4\pi(10^{-9}/36\pi)(5)^2} (0.6\vec{a}_y + 0.8\vec{a}_z)$$

Thus  $[\vec{E}] = 180\text{V/m}$  <sup>unit vector</sup> in the direction  $\vec{a}_R = 0.6\vec{a}_y + 0.8\vec{a}_z$



## Electric Field Intensity (Cont'd)

If there are N charges,  $Q_1, Q_2 \dots Q_N$  located respectively at point with position vectors  $r_1, r_2 \dots r_N$  the electric field intensity at point  $r$  is:

$$\mathbf{E} = \frac{Q_1}{4\pi\epsilon_0 |\mathbf{r} - \mathbf{r}_1|^2} \frac{(\mathbf{r} - \mathbf{r}_1)}{|\mathbf{r} - \mathbf{r}_1|} + \dots \frac{Q_N}{4\pi\epsilon_0 |\mathbf{r} - \mathbf{r}_N|^2} \frac{(\mathbf{r} - \mathbf{r}_N)}{|\mathbf{r} - \mathbf{r}_N|}$$

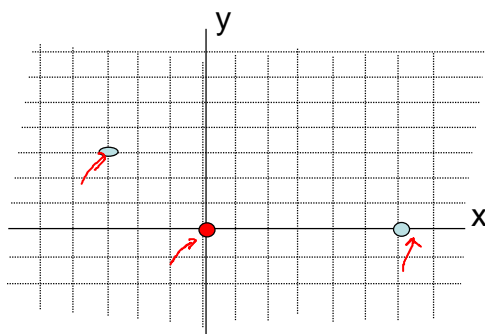
$$\mathbf{E} = \frac{1}{4\pi\epsilon_0} \sum_{k=1}^N \frac{Q_k (\mathbf{r} - \mathbf{r}_k)}{|\mathbf{r} - \mathbf{r}_k|^3}$$



## Superposition of forces from two charges

**Blue charges fixed , negative, equal charge (-q)**

What is force on positive red charge +q ?





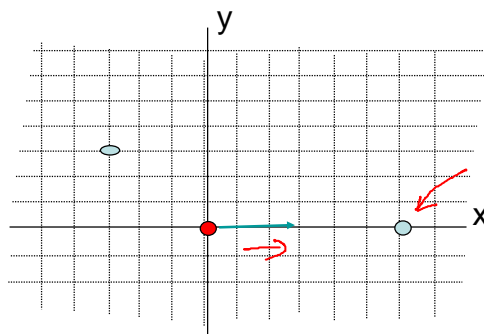
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## Superposition of forces from two charges

**Blue charges fixed , negative, equal charge  $(-q)$**

What is force on positive red charge  $+q$  ?

Consider effect of each charge separately:



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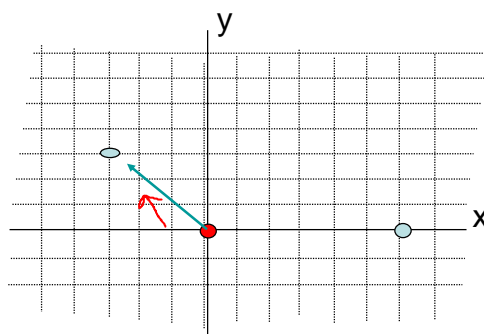
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## Superposition of forces from two charges

**Blue charges fixed , negative, equal charge  $(-q)$**

What is force on positive red charge  $+q$  ?

Take each charge in turn:



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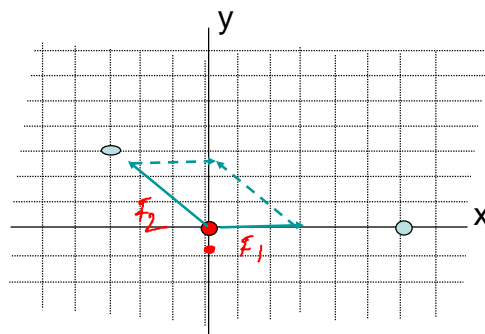
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## Superposition of forces from two charges

### Blue charges fixed , negative, equal charge $(-q)$

What is force on positive red charge  $+q$  ?

Create vector sum:



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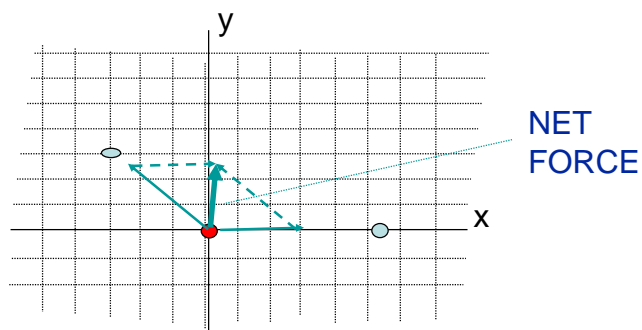
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## Superposition of forces from two charges

### Blue charges fixed , negative, equal charge $(-q)$

What is force on positive red charge  $+q$  ?

Find resultant:



*When a number of charges are present, the total force on a given charge is equal to the vector sum of the forces due to the remaining other charges on the given charge.*

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## Superposition Principle

$F \leftarrow$   
 $E = \frac{F}{Q} \leftarrow$

Forces add vectorially

$$\underline{F} = (F_{21x} + F_{31x}) \underline{x} + (F_{21y} + F_{31y}) \underline{y}$$

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Just as we defined a gravitational field, we define an "electric field" in a similar manner:

$$F = \frac{GmM}{r^2}$$

$$mg = \frac{GmM}{r^2}$$

$$g = \frac{GM}{r^2}$$

Practical Applications

- Microwave ovens
- Motor
- Storage (capacitor)
- Heating (IR)
- Identification

This is the gravitational field (Earth =  $9.8 \text{ m/s}^2$  or  $9.8 \text{ N/kg}$ )

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Just as we defined a gravitational field, we define an "electric field" in a similar manner:

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$$F = \frac{k|qQ|}{r^2}$$

This is the gravitational field (Earth = 9.8 m/s<sup>2</sup> or 9.8 N/kg)

Just as we defined a gravitational field, we define an "electric field" in a similar manner:

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$$mg = \frac{GmM}{r^2}$$

$$g = \frac{GM}{r^2}$$

$$F = \frac{k|qQ|}{r^2}$$

$$q(?) = \frac{k|qQ|}{r^2}$$

$$E = \frac{F}{q}$$

$$F = qE$$

This is the gravitational field (Earth = 9.8 m/s<sup>2</sup> or 9.8 N/kg)

Just as we defined a gravitational field, we define an "electric field" in a similar manner:

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$$F = \frac{k|qQ|}{r^2}$$

$$q(E) = \frac{k|qQ|}{r^2}$$

$$E = \frac{k|Q|}{r^2}$$

✓ Electric field

This is the gravitational field (Earth = 9.8 m/s<sup>2</sup> or 9.8 N/kg)

The general equation for an ELECTRIC FIELD is:

$$E = \frac{k|Q|}{r^2}$$

$$\frac{\text{Newtons}}{\text{Coulomb}} = \frac{N}{C}$$

(compare this to the equation for the gravitational field)

Notice that for gravity,  $F = mg$

We see that in electrostatics,  $F = qE$

$$F = \frac{GmM}{r^2}$$

$$\downarrow$$

$$mg = \frac{GmM}{r^2}$$

$$g = \frac{GM}{r^2}$$

$$F = \frac{k|qQ|}{r^2}$$

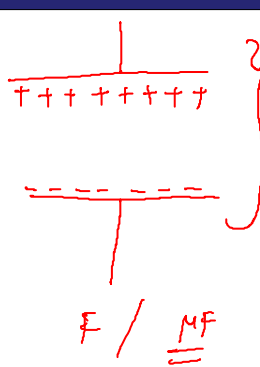
$$\downarrow$$

$$q(E) = \frac{k|qQ|}{r^2}$$

$$E = \frac{k|Q|}{r^2}$$

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## Capacitors.



Ultracapacitors } F 10F/50F  
 → Energy  
 → ↓ power  
Discharge

→ Energy Storage → gadgets

---

Energy Buffer → Electric vehicle  
 → Domestic

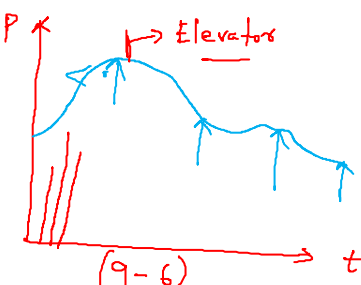
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## Hybrid

→ HEV → Engine + Battery  
 → PHEV → Engine + Battery + (PHEV) grid

Apartment  
 ↳ 20 homes → Power demand (month)

Peak → FN (6-9)  
 → AN (6-9)



Swan } Solar power  
 + OC  
 ↓

3L → 6pm  
 1F →  
 1 Mixer → 7am  
 1 AC → 10pm  
 1 Refrigerator → x  
 1 TV → 6pm  
 1 Water heater → 7am  
 1 Mobile charger → 6pm

EV } Li-ion  
 Battery } kona  
 +  
 UC x



## Summary

Electrostatics

→ F

→ E

→ Capacitor

→ Tradition } E.V.

→ uc

EV → Zero emission

↓  
→ Well to wheel