

$$f(x) = \begin{cases} 3x+5, & x \neq 1 \\ 10^7, & x = 1 \end{cases}$$

Here, $\lim_{x \rightarrow 1} f(x)$ exists (8), even if there is a jump discontinuity at $x=1$.