

Definition

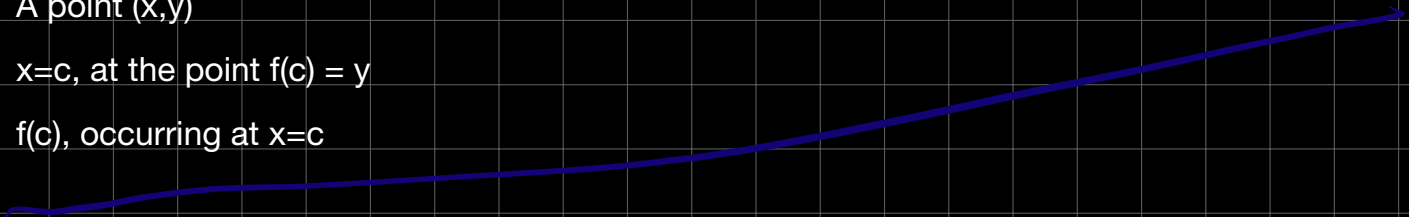
If $f: I \rightarrow \mathbb{R}$ (interval \rightarrow real numbers) then:

- c in I is a global maximum for f on I if $f(c) \geq f(x)$ for all x in I
- c in I is a global minimum for f on I if $f(c) \leq f(x)$ for all x in I
- c in I is a global extremum if it is either a global maximum or a global minimum

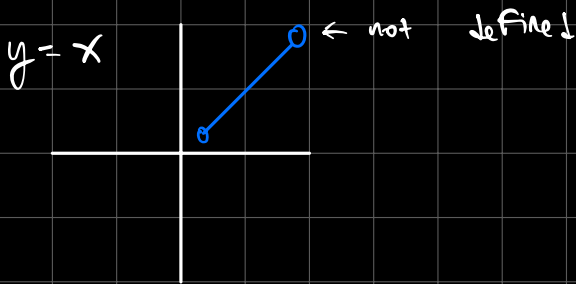
Also called *absolute* minimums/maximums

Refers to the x -coordinate (c , or $x=c$), but can also be written as:

- A point (x, y)
- $x=c$, at the point $f(c) = y$
- $f(c)$, occurring at $x=c$



If f is defined on an open interval (a, b) , it does not necessarily have a global min/max



If f is defined on a closed interval $[a, b]$ it also does not necessarily have a global min/max

Extreme Value Theorem

If f is continuous on a closed interval $[a, b]$, then there exists a c_1 and c_2 in $[a, b]$ such that

$$f(c_1) \leq f(x) \leq f(c_2)$$

\Leftarrow global min $\quad \quad \quad \Leftarrow$ global max

For all x in $[a, b]$

Converse is false

