

We know

- $(\sin x)' = \cos x$
- $(\cos x)' = -\sin x$
- $(\sec x)' = \sec x \tan x$

$$f(x) = \tan x = \frac{\sin x}{\cos x}$$

$$f'(x) = \frac{\cos x \cdot \cos x - \sin x (-\sin x)}{\cos^2 x} = \frac{\sin^2 x + \cos^2 x}{\cos^2 x} = \frac{1}{\cos^2 x}$$
$$= \sec^2 x$$

$$\cot x' = -\csc^2 x$$

$$\sec x' = \sec x \tan x$$

$$\csc x' = -\csc x \cot x$$