

A point $x=c$ is a local maximum (minimum) of $f(x)$ if there exists an open interval (a,b) such that for a point c in (a,b) , and for all x in (a,b) :

- $f(x) \leq f(c)$
- (Or, for minimums, $f(x) \geq f(c)$)

Something can be both a local and a *global* maximum

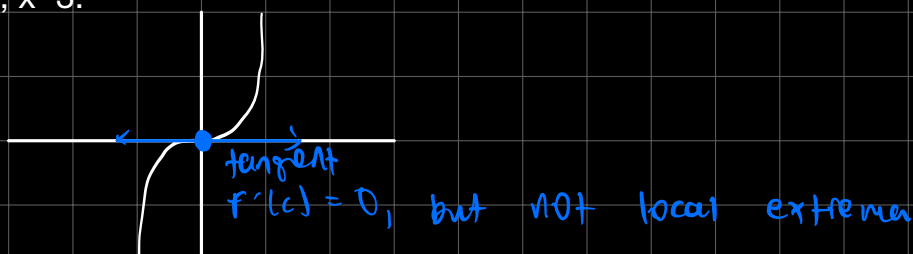
Endpoints can't be local minimums or maximums because they are not defined on open intervals

Local Extrema Theorem

If $x=c$ is a local extrema of $f(x)$ and $f'(c)$ exists, then $f'(c) = 0$

Note that the converse is not true: if $f'(c) = 0$, then c is not necessarily a local extrema

For example, x^3 :



If $x=c$ is a local extrema, it is not necessarily continuous or differentiable at $x=c$

