USACO Notebook

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```
typedef pair<int, int> pii;
template <class T> using Tree = tree<T, null_type,</pre>
    less<T>,
    rb_tree_tag,tree_order_statistics_node_update>;
#define FOR(i, a, b) for (int i=a; i<(b); i++)</pre>
#define FOR(i, a) for (int i=0; i<(a); i++)
#define FORd(i,a,b) for (int i = (b)-1; i \ge a; i--)
#define FORd(i,a) for (int i = (a)-1; i >= 0; i--)
#define sz(x) (int)(x).size()
#define mp make_pair
#define pb push_back
#define f first
#define s second
#define lb lower_bound
#define ub upper_bound
#define all(x) x.begin(), x.end()
const int MOD = 1000000007;
int main() {
       ios_base::sync_with_stdio(0);cin.tie(0);
}
// read!read!read!read!read!read!
// 11 vs. int!
```

1.2 FastScanner

```
* Source: Matt Fontaine
class FastScanner {
   private InputStream stream;
   private byte[] buf = new byte[1024];
   private int curChar;
   private int numChars;
   public FastScanner(InputStream stream) {
       this.stream = stream;
   int read() {
       if (numChars == -1)
           throw new InputMismatchException();
       if (curChar >= numChars) {
           curChar = 0;
           try {
              numChars = stream.read(buf);
           } catch (IOException e) {
              throw new InputMismatchException();
           if (numChars <= 0) return -1;</pre>
       }
       return buf[curChar++];
   }
   boolean isSpaceChar(int c) {
```

```
return c == ' ' || c == '\n' || c == '\r' || c
           == '\t' || c == -1;
   }
   boolean isEndline(int c) {
       return c == '\n' || c == '\r' || c == -1;
   public int nextInt() {
       return Integer.parseInt(next());
   public long nextLong() {
       return Long.parseLong(next());
   public double nextDouble() {
       return Double.parseDouble(next());
   public String next() {
       int c = read();
       while (isSpaceChar(c)) c = read();
       StringBuilder res = new StringBuilder();
          res.appendCodePoint(c);
          c = read();
       } while (!isSpaceChar(c));
       return res.toString();
   }
   public String nextLine() {
       int c = read();
       while (isEndline(c))
          c = read();
       StringBuilder res = new StringBuilder();
       do {
          res.appendCodePoint(c);
           c = read();
       } while (!isEndline(c));
       return res.toString();
   }
}
```

1.3 Troubleshoot

Source: KACTL

Pre-submit:

- Write a few simple test cases, if sample is not enough.
- Are time limits close? If so, generate max cases.
- Is the memory usage fine?
- Could anything overflow?
- Make sure to submit the right file.

Wrong answer:

- Print your solution! Print debug output, as well.
- Are you clearing all datastructures between test cases?
- Can your algorithm handle the whole range of input?
- Read the full problem statement again.
- Do you handle all corner cases correctly?
- Have you understood the problem correctly?
- Any uninitialized variables?
- Any overflows?
- Confusing N and M, i and j, etc.?
- Are you sure your algorithm works?
- What special cases have you not thought of?
- Are you sure the STL functions you use work as you think?
- Add some assertions, maybe resubmit.
- Create some testcases to run your algorithm on.
- Go through the algorithm for a simple case.
- Go through this list again.
- Explain your algorithm to a team mate.
- Ask the team mate to look at your code.
- Go for a small walk, e.g. to the toilet.
- Is your output format correct? (including whitespace)
- Rewrite your solution from the start or let a team mate do it.

Runtime error:

- Have you tested all corner cases locally?
- Any uninitialized variables?
- Are you reading or writing outside the range of any vector?
- Any assertions that might fail?
- Any possible division by 0? (mod 0 for example)
- Any possible infinite recursion?
- Invalidated pointers or iterators?
- Are you using too much memory?
- Debug with resubmits (e.g. remapped signals, see Various).

Time limit exceeded:

- Do you have any possible infinite loops?
- What is the complexity of your algorithm?
- Are you copying a lot of unnecessary data? (References)
- How big is the input and output? (consider scanf)
- Avoid vector, map. (use arrays/unordered map)
- What do your team mates think about your algorithm?

Memory limit exceeded:

- What is the max amount of memory your algorithm should need?
- Are you clearing all data structures between test cases?

2 Data Structures

2.1 (2) Coordinate Compression

```
/**
 * Source: own
*/

void compress(vi& x) {
    map<int,int> m; for (int i: x) m[i] = 0;
    int co = 0; for (auto& a: m) a.s = co++;
    for (int& i: x) i = m[i];
}

// vi x = {2,4,3,6}; compress(x);
```

2.2 (2) STL Demo

2.3 (4) Matrix

```
* Source: KACTL
template<int SZ> struct mat {
   array<array<11,SZ>,SZ> d;
   mat() {
       FOR(i,SZ) FOR(j,SZ) d[i][j] = 0;
   mat operator+(const mat& m) {
       mat<SZ> a;
       FOR(i,SZ) FOR(j,SZ) a.d[i][j] =
            (d[i][j]+m.d[i][j]) % MOD;
       return a;
   }
   mat operator*(const mat& m) {
       mat<SZ> a;
       FOR(i,SZ) FOR(j,SZ) FOR(k,SZ)
           a.d[i][k] = (a.d[i][k]+d[i][j]*m.d[j][k]) %
       return a;
   }
   mat operator^(ll p) {
       mat<SZ> a, b(*this);
       FOR(i,SZ) a.d[i][i] = 1;
       while (p) {
          if (p&1) a = a*b;
           b = b*b;
           p /= 2;
       return a;
   }
   void print() {
       FOR(i,SZ) {
           FOR(j,SZ) cout << d[i][j] << " ";</pre>
           cout << "\n";
       cout << "----\n":
   }
};
mat<2> x; x.d[0][0] = 1, x.d[1][0] = 2, x.d[1][1] = 1,
    x.d[0][1] = 3;
mat<2> y = x*x;
mat<2> z = x^5;
x.print(), y.print(), z.print();
*/
```

2.4 1D Range Queries

2.4.1 (3) BIT

```
/**
 * Source: own
 * Description: 1D point update, range query
 */

template<class T, int SZ> struct BIT {
    T bit[SZ+1];

BIT() { memset(bit,0,sizeof bit); }

    void upd(int k, T val) { // add val to index k
        for(;k <= SZ; k += (k&-k)) bit[k] += val;
    }

T query(int k) {
    T temp = 0;
    for (;k > 0;k -= (k&-k)) temp += bit[k];
    return temp;
    }

T query(int l, int r) { return
        query(r)-query(l-1); } // range query [l,r]
};

// BIT<int,1<<17> b;
```

2.4.2 (3) RMQ

```
/**
* Source: own
* Description: 1D range query
template < class T, int SZ> struct RMQ {
   T stor[SZ][31-__builtin_clz(SZ)];
   T comb(T a, T b) {
       return min(a,b);
   void build(vector<T>& x) {
       FOR(i,sz(x)) stor[i][0] = x[i];
       FOR(j,1,31-__builtin_clz(SZ))
            FOR(i,SZ-(1<<(j-1)))
           stor[i][j] =
                comb(stor[i][j-1],stor[i+(1<<(j-1))][j-1]);</pre>
   }
   T query(int 1, int r) {
       int x = 31-\_builtin\_clz(r-l+1);
       return comb(stor[1][x],stor[r-(1<<x)+1][x]);</pre>
   }
};
// RMQ<int,100000> R;
```

2.4.3 (3) SegTree

```
/*
* Source: http://codeforces.com/blog/entry/18051
* Description: 1D point update, range query
template < class T, int SZ> struct Seg {
   T seg[2*SZ], MN = 0;
   Seg() {
       memset(seg,0,sizeof seg);
   T comb(T a, T b) { return a+b; } // easily change
        this to min or max
   void upd(int p, T value) { // set value at
       position p
       for (seg[p += SZ] = value; p > 1; p >>= 1)
           seg[p>>1] = comb(seg[p], seg[p^1]);
   }
   void build() {
       FORd(i,SZ) seg[i] = comb(seg[2*i],seg[2*i+1]);
   T query(int 1, int r) { // sum on interval [1, r]
       T res = MN; r++;
       for (1 += SZ, r += SZ; 1 < r; 1 >>= 1, r >>=
           1) {
           if (1&1) res = comb(res,seg[1++]);
           if (r\&1) res = comb(res, seg[--r]);
       return res;
   }
};
// Seg<int,1<<17> b;
```

2.4.4 (4) BIT with Range Update

2.4.5 (4) Lazy SegTree

```
* Source: USACO Counting Haybales
* 1D range update, range query
const ll INF = 1e18:
template<class T, int SZ> struct LazySegTree {
   T sum[2*SZ], mn[2*SZ], lazy[2*SZ]; // set SZ to a
       power of 2
   LazySegTree() {
       memset (sum,0,sizeof sum);
       memset (mn,0,sizeof mn);
       memset (lazy,0,sizeof lazy);
   void push(int ind, int L, int R) {
       sum[ind] += (R-L+1)*lazy[ind];
       mn[ind] += lazy[ind];
       if (L != R) lazy[2*ind] += lazy[ind],
           lazy[2*ind+1] += lazy[ind];
       lazy[ind] = 0;
   void pull(int ind) {
       sum[ind] = sum[2*ind] + sum[2*ind+1];
       mn[ind] = min(mn[2*ind], mn[2*ind+1]);
   void build() {
       FORd(i,SZ) pull(i);
   T qsum(int lo, int hi, int ind = 1, int L = 0, int
       R = SZ-1) \{
       push(ind,L,R);
       if (lo > R || L > hi) return 0;
       if (lo <= L && R <= hi) return sum[ind];</pre>
       int M = (L+R)/2;
```

```
return qsum(lo,hi,2*ind,L,M) +
            qsum(lo,hi,2*ind+1,M+1,R);
   }
    T qmin(int lo, int hi, int ind = 1, int L = 0, int
        R = SZ-1) {
       push(ind,L,R);
       if (lo > R || L > hi) return INF;
       if (lo <= L && R <= hi) return mn[ind];</pre>
       int M = (L+R)/2;
       return min(qmin(lo,hi,2*ind,L,M),
            qmin(lo,hi,2*ind+1,M+1,R));
   }
    void upd(int lo, int hi, ll inc, int ind = 1, int
        L = 0, int R = SZ-1) {
       push(ind,L,R);
       if (hi < L || R < lo) return;</pre>
       if (lo <= L && R <= hi) {</pre>
           lazy[ind] = inc;
           push(ind,L,R);
           return;
       }
       int M = (L+R)/2;
       upd(lo,hi,inc,2*ind,L,M);
            upd(lo,hi,inc,2*ind+1,M+1,R);
       pull(ind);
   }
};
// LazySegTree<11,1<<17> b;
```

2.4.6 (5) Lazy Persistent SegTree

```
/**
* Source:
    http://codeforces.com/blog/entry/47108?#comment-315047
struct Node { // without lazy updates
   int val = 0;
   Node* c[2];
   Node* copy() {
       Node* x = new Node(); *x = *this;
       return x;
   }
   int query(int low, int high, int L, int R) {
       if (low <= L && R <= high) return val;</pre>
       if (R < low || high < L) return MOD;</pre>
       int M = (L+R)/2;
       return min(c[0]->query(low,high,L,M),
                 c[1]->query(low,high,M+1,R));
   }
   Node* upd(int ind, int v, int L, int R) {
       if (R < ind || ind < L) return this;</pre>
```

```
Node* x = copy();
        if (ind <= L && R <= ind) {</pre>
           x->val += v;
           return x;
        int M = (L+R)/2:
       x->c[0] = x->c[0]->upd(ind,v,L,M);
        x \rightarrow c[1] = x \rightarrow c[1] \rightarrow upd(ind, v, M+1, R);
        x-val = min(x-c[0]-val,x-c[1]-val);
        return x;
    void build(vi& arr, int L, int R) {
        if (L == R) {
           if (L < (int)arr.size()) val = arr[L];</pre>
            else val = 0;
           return;
        int M = (L+R)/2;
        c[0] = new Node();
        c[0]->build(arr,L,M);
        c[1] = new Node();
        c[1]->build(arr,M+1,R);
        val = min(c[0]->val,c[1]->val);
    }
};
struct node { // with lazy updates
    int val = 0, lazy = 0;
    node* c[2];
    node* copy() {
        node* x = new node(); *x = *this;
        return x;
    }
    void push() {
        if (!lazy) return;
        FOR(i,2) if (c[i]) {
           c[i] = new node(*c[i]);
           c[i]->lazy += lazy;
        }
        lazy = 0;
    int query(int low, int high, int L, int R) {
        if (low <= L && R <= high) return val;</pre>
        if (R < low || high < L) return MOD;</pre>
        int M = (L+R)/2;
        return lazy+min(c[0]->query(low,high,L,M),
                       c[1]->query(low,high,M+1,R));
    }
    node* upd(int low, int high, int v, int L, int R) {
       if (R < low || high < L) return this;</pre>
        node* x = copy();
        if (low <= L && R <= high) {</pre>
           x\rightarrowlazy += v, x\rightarrowval += v;
           return x;
```

```
push();
       int M = (L+R)/2;
       x - c[0] = x - c[0] - upd(low, high, v, L, M);
       x - c[1] = x - c[1] - upd(low, high, v, M+1, R);
       x-val = min(x-c[0]-val,x-c[1]-val);
       return x;
   }
    void build(vi& arr, int L, int R) {
       if (L == R) {
           if (L < sz(arr)) val = arr[L];</pre>
           else val = 0;
           return;
       }
       int M = (L+R)/2;
       c[0] = new node();
       c[0]->build(arr,L,M);
       c[1] = new node();
       c[1]->build(arr,M+1,R);
       val = min(c[0]->val,c[1]->val);
   }
};
template<int SZ> struct pers {
   node* loc[SZ+1]; // stores location of root after
        ith update
   int nex = 1;
   pers() { loc[0] = new node(); }
    void upd(int low, int high, int val) {
       loc[nex] =
            loc[nex-1]->upd(low,high,val,0,SZ-1);
       nex++;
    }
    void build(vi& arr) {
       loc[0]->build(arr,0,SZ-1);
    int query(int ti, int low, int high) {
       return loc[ti]->query(low,high,0,SZ-1);
};
pers<8> p;
int main() {
   vi arr = \{1,7,2,3,5,9,4,6\};
   p.build(arr);
   p.upd(1,2,2); // 1 9 4 3 5 9 4 6
   FOR(i,8) {
       FOR(j,i,8) cout << p.query(1,i,j) << " ";
       cout << "\n";
    cout << "\n";
    p.upd(4,7,5); // 1 9 4 3 10 14 9 11
    FOR(i,8) {
```

```
FOR(j,i,8) cout << p.query(2,i,j) << " ";
    cout << "\n";
}
cout << "\n";

FOR(i,8) {
    FOR(j,i,8) cout << p.query(1,i,j) << " ";
    cout << "\n";
}
cout << "\n";
}</pre>
```

2.5 2D Range Queries

2.5.1 (4) 2D BIT

```
/**
* Source: own
template<class T, int SZ> struct BIT2D {
   T bit[SZ+1][SZ+1];
   void upd(int X, int Y, T val) {
       for (; X <= SZ; X += (X&-X))</pre>
           for (int Y1 = Y; Y1 <= SZ; Y1 += (Y1&-Y1))</pre>
               bit[X][Y1] += val:
   T query(int X, int Y) {
       T ans = 0;
       for (; X > 0; X -= (X\&-X))
           for (int Y1 = Y; Y1 > 0; Y1 = (Y1&-Y1))
               ans += bit[X][Y1];
       return ans;
   }
   T query(int X1, int X2, int Y1, int Y2) {
       return query(X2,Y2)-query(X1-1,Y2)
           -query(X2,Y1-1)+query(X1-1,Y1-1);
   }
};
// BIT2D<int,1000> b;
```

2.5.2 (4) 2D Sparse SegTree

```
/**
 * Source: USACO Mowing the Field
 * Description: 2D Point Update, Range Query
 */

const int SZ = 1<<17;

// Sparse 1D SegTree
struct node {
  int val = 0;
  node* c[2];

  void upd(int ind, int v, int L = 0, int R = SZ-1)
  { // set an element equal to v</pre>
```

```
if (L == ind && R == ind) { val = v; return; }
       int M = (L+R)/2;
       if (ind <= M) {</pre>
           if (!c[0]) c[0] = new node();
           c[0] \rightarrow upd(ind, v, L, M);
       } else {
           if (!c[1]) c[1] = new node();
           c[1] \rightarrow upd(ind,v,M+1,R);
       val = 0;
       if (c[0]) val += c[0]->val;
       if (c[1]) val += c[1]->val;
   }
    int query(int low, int high, int L = 0, int R =
        SZ-1) { // query sum of segment
       if (low <= L && R <= high) return val;</pre>
       if (high < L || R < low) return 0;</pre>
       int M = (L+R)/2, t = 0;
       if (c[0]) t += c[0]->query(low,high,L,M);
       if (c[1]) t += c[1]->query(low,high,M+1,R);
       return t;
   }
};
// 2D SegTree, sparse segtree of sparse 1D segtrees
struct Node {
   node seg;
   Node* c[2];
    void upd(int x, int y, int v, int L = 0, int R =
        SZ-1) { // set an element equal to v
       seg.upd(y,v);
       if (L == x && R == x) return;
       int M = (L+R)/2;
       if (x <= M) {</pre>
           if (!c[0]) c[0] = new Node();
           c[0] \rightarrow upd(x,y,v,L,M);
       } else {
           if (!c[1]) c[1] = new Node();
           c[1] - vpd(x, y, v, M+1, R);
   }
    int query(int x1, int x2, int y1, int y2, int L =
        0, int R = SZ-1) { // query sum of rectangle
       if (x1 <= L && R <= x2) return</pre>
            seg.query(y1,y2);
       if (x2 < L || R < x1) return 0;</pre>
       int M = (L+R)/2, t = 0;
       if (c[0]) t += c[0]->query(x1,x2,y1,y2,L,M);
       if (c[1]) t += c[1]->query(x1,x2,y1,y2,M+1,R);
       return t;
   }
};
// SegTree + BIT
```

```
// Array of Sparse Segtrees
struct SegBit {
   node seg[SZ+1];
   void upd(int x, int y, int v) { // set an element
       for (x++;x \le SZ; x += (x\&-x)) seg[x].upd(y,v);
   int query(int x, int y1, int y2) {
       int ret = 0;
       for (;x > 0; x -= (x\&-x)) ret +=
           seg[x].query(y1,y2);
       return ret;
   }
   int query(int x1, int x2, int y1, int y2) { //
        query sum of rectangle
       return query(x2+1,y1,y2)-query(x1,y1,y2);
};
Node n;
SegBit s;
int main() {
   n.upd(5,7,2);
   n.upd(3,2,20);
   n.upd(5,8,200);
   cout << n.query(3,5,2,7) << "\n"; // 22
   s.upd(5,7,2);
   s.upd(3,2,20);
   s.upd(5,8,200);
   cout << s.query(3,5,2,7) << "\n"; // 22
```

2.5.3 (4) Merge-Sort Tree

```
/**
* Source: own
*/
template<int SZ> struct mstree {
   Tree<pii> val[SZ+1]; // for offline queries use
        vector with binary search instead
   void upd(int x, int y, int t = 1) { //
       x-coordinate between 1 and SZ inclusive
       for (int X = x; X <= SZ; X += X&-X) {</pre>
           if (t) val[X].insert({y,x});
           else val[X].erase({y,x});
       }
   }
   int query(int x, int y) {
       int t = 0;
       for (;x > 0; x -= x&-x) t +=
           val[x].order_of_key({y,MOD});
       return t;
```

2.6 BBST

2.6.1 (5) Link-Cut Tree

```
/**
* Source: Dhruv Rohatgi
int p[100001], pp[100001], c[100001][2], sum[100001];
int getDir(int x, int y) {
   return c[x][0] == y ? 0 : 1;
}
void setLink(int x, int y, int d) {
   c[x][d] = y, p[y] = x;
void rotate(int y, int d) {
   int x = c[y][d], z = p[y];
   setLink(y,c[x][d^1],d);
   setLink(x,y,d^1);
   setLink(z,x,getDir(z,y));
   sum[x] = sum[y];
   sum[y] = sum[c[y][0]] + sum[c[y][1]] + 1;
   pp[x] = pp[y]; pp[y] = 0;
void splay(int x) {
   while (p[x]) {
       int y = p[x], z = p[y];
       int dy = getDir(y,x), dz = getDir(z,y);
       if (!z) rotate(y,dy);
       else if (dy == dz) rotate(z,dz), rotate(y,dy);
       else rotate(y,dy), rotate(z,dz);
   }
}
void dis(int v, int d) {
   p[c[v][d]] = 0, pp[c[v][d]] = v;
   sum[v] -= sum[c[v][d]];
   c[v][d] = 0;
}
```

```
void con(int v, int d) {
   c[pp[v]][d] = v;
   sum[pp[v]] += sum[v];
   p[v] = pp[v], pp[v] = 0;
void access(int v) {
   // v is brought to the root of auxiliary tree
   // modify preferred paths
   splay(v);
   dis(v,1);
   while (pp[v]) {
       int w = pp[v]; splay(w);
       dis(w,1), con(v,1);
       splay(v);
int find_root(int v) {
   access(v);
   while (c[v][0]) v = c[v][0];
   access(v);
   return v;
int find_depth(int v) {
   access(v);
   return sum[c[v][0]];
}
void cut(int v) {
   // cut link between v and par[v]
   access(v);
   pp[c[v][0]] = p[c[v][0]] = 0; // fix
   sum[v] -= sum[c[v][0]];
   c[v][0] = 0;
}
void link(int v, int w) {
   // v, which is root of another tree, is now child
        of w
   access(v), access(w);
   pp[w] = v; con(w,0);
int anc(int v, int num) {
   if (find_depth(v) < num) return 0;</pre>
   access(v);
   v = c[v][0];
   while (1) {
       if (sum[c[v][1]] >= num) v = c[v][1];
       else if (sum[c[v][1]]+1 == num) return v;
       else num -= (sum[c[v][1]]+1), v = c[v][0];
}
int main() {
   FOR(i,1,100001) sum[i] = 1;
```

```
link(2,1);
   link(3,1);
   link(4,1);
   link(5,4);
   link(10,4);
   link(7,6);
   link(8,7);
   link(9,8);
   FOR(i,1,11) cout << i << " " << find_root(i) << "
       " << find_depth(i) << " " << anc(i,2) << "\n";
   cout << "\n";
   cut(4);
   link(4,8);
   FOR(i,1,11) cout << i << " " << find_root(i) << "
        " << find_depth(i) << " " << anc(i,2) << "\n";
}
```

2.6.2 (5) Splay Tree

```
* Description: based off treap code
struct snode {
   int val;
   snode *p, *c[2];
    snode (int v) {
       val = v;
       c[0] = c[1] = p = NULL;
    void inOrder(bool f = 0) {
       if (c[0]) c[0]->inOrder();
       cout << val << " ";
       if (c[1]) c[1]->inOrder();
       if (f) cout << "\n----\n";</pre>
   }
};
void setLink(snode* x, snode* y, int d) {
   if (x) x\rightarrow c[d] = y;
    if (y) y \rightarrow p = x;
}
int getDir(snode* x, snode* y) {
    if (!x) return -1;
   return x - > c[0] == y ? 0 : 1;
void rot(snode* x, int d) {
    snode *y = x->c[d], *z = x->p;
    setLink(x, y->c[d^1], d);
    setLink(y, x, d^1);
    setLink(z, y, getDir(z, x));
snode* splay(snode* x) {
```

```
while (x && x->p) {
       snode* y = x->p, *z = y->p;
       int dy = getDir(y, x), dz = getDir(z, y);
       if (!z) rot(y, dy);
       else if (dy == dz) rot(z, dz), rot(y, dy);
       else rot(y, dy), rot(z, dz);
   return x;
}
pair<snode*,snode*> find(snode *cur, int v) { // x.f
    is result, x.s is lowest
   if (!cur) return {cur,cur};
   pair<snode*,snode*> x;
   if (cur->val >= v) {
       x = find(cur->c[0],v);
       if (!x.f) x.f = cur;
   } else x = find(cur->c[1],v);
   if (!x.s) x.s = cur;
   return x;
snode* getmx(snode* x) {
   return x->c[1]?getmx(x->c[1]):x;
pair<snode*,snode*> split(snode* x, int v) {
   if (!x) return {x,x};
   auto y = find(x,v); y.s = splay(y.s);
   if (!y.f) return {y.s,NULL};
   y.f = splay(y.f);
   auto z = y.f->c[0]; setLink(y.f,NULL,0),
       setLink(NULL,z,0);
   return {z,y.f};
}
snode* merge(snode* x, snode* y) {
   if (!x) return y;
   x = splay(getmx(x));
   setLink(x,y,1);
   return x;
}
snode* ins(snode* x, int v) { // insert value v
   auto a = split(x,v);
   return merge(merge(a.f, new snode(v)),a.s);
snode* del(snode* x, int v) { // delete all values
    equal to v
   auto a = split(x,v), b = split(a.s,v+1);
   return merge(a.f,b.s);
snode* root;
int main() {
   root = ins(root,1);
   root = ins(root,9);
   root = ins(root,3);
```

```
root->inOrder(1);

root = ins(root,7);
root = ins(root,4);
root = del(root,9);

root->inOrder(1);
}
```

2.6.3 (5) Treap

```
* Source: own?
* Description: Easiest BBST
* Note: Also see lazy persistent treap.
struct tnode {
   int val, pri;
   tnode *c[2];
    tnode (int v) {
       val = v, pri = rand()+(rand()<<15);</pre>
       c[0] = c[1] = NULL;
    void inOrder(bool f = 0) {
       if (c[0]) c[0]->inOrder();
       cout << val << " ";
       if (c[1]) c[1]->inOrder();
       if (f) cout << "\n----\n";</pre>
   }
};
pair<tnode*,tnode*> split(tnode* t, int v) { // >= v
    goes to the right
    if (!t) return {t,t};
   if (v <= t->val) {
       auto p = split(t->c[0], v); t->c[0] = p.s;
       return {p.f, t};
    } else {
       auto p = split(t->c[1], v); t->c[1] = p.f;
       return {t, p.s};
    }
}
tnode* merge(tnode* 1, tnode* r) {
   if (!1) return r;
   if (!r) return 1;
   if (1->pri > r->pri) {
       1->c[1] = merge(1->c[1],r);
       return 1;
   } else {
       r - c[0] = merge(1, r - c[0]);
       return r;
   }
}
```

```
tnode* ins(tnode* x, int v) { // insert value v
   auto a = split(x,v);
   return merge(merge(a.f, new tnode(v)),a.s);
}
tnode* del(tnode* x, int v) { // delete all values
    equal to v
   auto a = split(x,v), b = split(a.s,v+1);
   return merge(a.f,b.s);
tnode *root;
int main() {
   root = ins(root,1);
   root = ins(root,9);
   root = ins(root,3);
   root->inOrder(1);
   root = ins(root,7);
   root = ins(root,4);
   root = del(root,9);
   root->inOrder(1);
```

3 Flows

3.1 (5) Dinic

```
/**
* Source: GeeksForGeeks
*/
struct Edge {
   int v, flow, C, rev;
};
template<int SZ> struct Dinic {
   int level[SZ], start[SZ];
   vector<Edge> adj[SZ];
   void addEdge(int u, int v, int C) {
       Edge a{v, 0, C, sz(adj[v])};
       Edge b{u, 0, 0, sz(adj[u])};
       adj[u].pb(a), adj[v].pb(b);
   bool BFS(int s, int t) {
       FOR(i,SZ) level[i] = -1;
       level[s] = 0;
       queue<int> q; q.push(s);
       while (!q.empty()) {
           int u = q.front(); q.pop();
           for (auto e: adj[u])
              if (level[e.v] < 0 && e.flow < e.C) {</pre>
                  level[e.v] = level[u] + 1;
```

```
q.push(e.v);
              }
       }
       return level[t] >= 0;
   }
   int sendFlow(int u, int flow, int t) {
       if (u == t) return flow;
       for ( ; start[u] < adj[u].size(); start[u] ++)</pre>
           Edge &e = adj[u][start[u]];
           if (level[e.v] == level[u]+1 && e.flow <</pre>
               int curr_flow = min(flow, e.C - e.flow);
               int temp_flow = sendFlow(e.v,
                   curr_flow, t);
               if (temp_flow > 0) {
                  e.flow += temp_flow;
                  adj[e.v][e.rev].flow -= temp_flow;
                  return temp_flow;
           }
       }
       return 0;
   }
   int maxFlow(int s, int t) {
       if (s == t) return -1;
       int total = 0:
       while (BFS(s, t)) {
           FOR(i,SZ) start[i] = 0;
           while (int flow = sendFlow(s, INT_MAX, t))
               total += flow;
       return total;
   }
};
Dinic<1000> D;
int main() {
   D.addEdge(0, 1, 16 );
   D.addEdge(0, 2, 13);
   D.addEdge(1, 2, 10);
   D.addEdge(1, 3, 12);
   D.addEdge(2, 1, 4 );
   D.addEdge(2, 4, 14);
   D.addEdge(3, 2, 9 );
   D.addEdge(3, 5, 20);
   D.addEdge(4, 3, 7);
   D.addEdge(4, 5, 4);
   cout << "Maximum flow " << D.maxFlow(0, 5);</pre>
}
```

3.2 (5) MinCostFlow

```
/**
* Source: GeeksForGeeks
struct Edge {
   int v, flow, C, rev, cost;
template<int SZ> struct mcf {
   pii pre[SZ];
   int cost[SZ], num[SZ], SC, SNC;
   11 flo, ans, ccost;
   vector<Edge> adj[SZ];
   void addEdge(int u, int v, int C, int cost) {
       Edge a{v, 0, C, sz(adj[v]), cost};
       Edge b{u, 0, 0, sz(adj[u]), -cost};
       adj[u].pb(a), adj[v].pb(b);
   void reweight() {
       FOR(i,SZ) {
          for (auto& p: adj[i]) p.cost +=
               cost[i]-cost[p.v];
       }
   }
   bool spfa() {
       FOR(i,SZ) cost[i] = MOD, num[i] = 0;
       cost[SC] = 0, num[SC] = MOD;
       priority_queue<pii,vector<pii>,greater<pii>>
           todo; todo.push({0,SC});
       while (todo.size()) {
          pii x = todo.top(); todo.pop();
           if (x.f > cost[x.s]) continue;
          for (auto a: adj[x.s]) if (x.f+a.cost <</pre>
               cost[a.v] && a.flow < a.C) {</pre>
              pre[a.v] = {x.s,a.rev};
              cost[a.v] = x.f+a.cost;
              num[a.v] = min(a.C-a.flow,num[x.s]);
              todo.push({cost[a.v],a.v});
       }
       ccost += cost[SNC];
       return num[SNC] > 0;
   void backtrack() {
       flo += num[SNC], ans += (11)num[SNC]*ccost;
       for (int x = SNC; x != SC; x = pre[x].f) {
          adj[x][pre[x].s].flow -= num[SNC];
           int t = adj[x][pre[x].s].rev;
           adj[pre[x].f][t].flow += num[SNC];
   }
   pii mincostflow(int sc, int snc) {
```

```
SC = sc, SNC = snc;
       flo = ans = ccost = 0;
       spfa();
       while (1) {
           reweight();
           if (!spfa()) return {flo,ans};
           backtrack();
       }
   }
};
mcf<100> m;
int main() {
   m.addEdge(0, 1, 16, 5);
   m.addEdge(1, 2, 13, 7);
   m.addEdge(1, 2, 13, 8);
   pii x = m.mincostflow(0,2);
   cout << x.f << " " << x.s;
}
```

3.3 (5) Push-Relabel

```
* Source: http://codeforces.com/blog/entry/14378
 * Unused
 */
struct Edge {
   int v, flow, C, rev;
};
template <int SZ> struct PushRelabel {
   vector<Edge> adj[SZ];
   int excess[SZ], dist[SZ], count[SZ+1], b = 0;
   bool active[SZ];
   vi B[SZ];
   void addEdge(int u, int v, int C) {
       Edge a{v, 0, C, sz(adj[v])};
       Edge b{u, 0, 0, sz(adj[u])};
       adj[u].pb(a), adj[v].pb(b);
   }
   void enqueue (int v) {
       if (!active[v] && excess[v] > 0 && dist[v] <</pre>
           SZ) {
           active[v] = 1;
           B[dist[v]].pb(v);
           b = max(b, dist[v]);
       }
   }
   void push (int v, Edge &e) {
       int amt = min(excess[v], e.C-e.flow);
       if (dist[v] == dist[e.v]+1 && amt > 0) {
           e.flow += amt, adj[e.v][e.rev].flow -= amt;
           excess[e.v] += amt, excess[v] -= amt;
```

```
enqueue(e.v);
       }
   }
   void gap (int k) {
       FOR(v,SZ) if (dist[v] >= k) {
           count[dist[v]] --;
           dist[v] = SZ;
           count[dist[v]] ++;
           enqueue(v);
       }
   }
   void relabel (int v) {
       count[dist[v]] --; dist[v] = SZ;
       for (auto e: adj[v]) if (e.C > e.flow) dist[v]
           = min(dist[v], dist[e.v] + 1);
       count[dist[v]] ++;
       enqueue(v);
   void discharge(int v) {
       for (auto &e: adj[v]) {
           if (excess[v] > 0) push(v,e);
           else break;
       if (excess[v] > 0) {
           if (count[dist[v]] == 1) gap(dist[v]);
           else relabel(v);
       }
   }
   int maxFlow (int s, int t) {
       for (auto &e: adj[s]) excess[s] += e.C;
       count[0] = SZ;
       enqueue(s); active[t] = 1;
       while (b >= 0) {
           if (sz(B[b])) {
              int v = B[b].back(); B[b].pop_back();
              active[v] = 0; discharge(v);
           } else b--;
       return excess[t];
};
PushRelabel<1000> D;
int main() {
   D.addEdge(0, 1, 16 );
   D.addEdge(0, 2, 13);
   D.addEdge(1, 2, 10);
   D.addEdge(1, 3, 12 );
   D.addEdge(2, 1, 4 );
   D.addEdge(2, 4, 14);
   D.addEdge(3, 2, 9);
   D.addEdge(3, 5, 20);
   D.addEdge(4, 3, 7);
   D.addEdge(4, 5, 4);
```

```
cout << "Maximum flow " << D.maxFlow(0, 5);
}</pre>
```

f 4 Geometry

4.1 (3) Pair Operators

```
/**
* Source: own
template<class T> pair<T,T> operator+(const pair<T,T>&
    1, const pair<T,T>& r) {
   return {1.f+r.f,1.s+r.s};
}
template<class T> pair<T,T> operator-(const pair<T,T>&
    1, const pair<T,T>& r) {
   return {1.f-r.f,1.s-r.s};
}
template<class T> pair<T,T> operator*(const pair<T,T>&
    1, T r) {
   return {1.f*r,1.s*r};
}
template<class T> pair<T,T> operator/(const pair<T,T>&
   return {1.f/r,1.s/r};
template<class T> double mag(pair<T,T> p) {
   return sqrt(p.f*p.f+p.s*p.s);
template<class T> pair<T,T> operator*(const pair<T,T>&
    1, const pair<T,T>& r) {
   // l.f+l.s*i, r.f+r.s*i
   return {1.f*r.f-l.s*r.s,l.s*r.f+l.f*r.s};
}
template < class T > pair < T, T > operator / (const pair < T, T > &
    1, const pair<T,T>& r) {
   // l.f+l.s*i, r.f+r.s*i
   pair<T,T>z =
        {r.f/(r.f*r.f+r.s*r.s),-r.s/(r.f*r.f+r.s*r.s)};
   return 1*z;
}
template<class T> double area(pair<T,T> a, pair<T,T>
    b, pair<T,T> c) {
   b = b-a, c = c-a;
   return (b.f*c.s-b.s*c.f)/2;
}
template<class T> double dist(pair<T,T> 1, pair<T,T>
   return mag(r-1);
}
```

```
template<class T> double dist(pair<T,T> o, pair<T,T>
    x, pair<T,T> d) { // signed distance
    return 2*area(o,x,x+d)/mag(d);
}
```

4.2 (4) Closest Pair

```
/**
* Source: GeeksForGeeks
* Description: Nlog^2N, can be improved
* Use: https://open.kattis.com/problems/closestpair2
*/
pair<double,pair<pdd,pdd>> MN = {INF,{{0,0},{0,0}}};
int n;
bool cmp(pdd a, pdd b) {
   return a.s < b.s;</pre>
double dist(pdd a, pdd b) {
   b.f -= a.f, b.s -= a.s;
   return sqrt(b.f*b.f+b.s*b.s);
pair<double,pair<pdd,pdd>> strip(vector<pdd> v, double
    pair<double,pair<pdd,pdd>> ans = MN;
   FOR(i,v.size()) FOR(j,i+1,v.size()) {
       if (v[i].s+di <= v[j].s) break;</pre>
       ans = min(ans,{dist(v[i],v[j]),{v[i],v[j]}});
   return ans;
}
pair<double,pair<pdd,pdd>> bes (vector<pdd> v) {
   if (v.size() == 1) return MN;
    int M = v.size()/2;
    vector<pdd> v1(v.begin(),v.begin()+M),
        v2(v.begin()+M,v.end());
    auto a = bes(v1), b = bes(v2);
    double di = min(a.f,b.f);
   vector<pdd> V;
   FOR(i,v.size()) if (v[i].f > v[M].f-di && v[i].f <</pre>
        v[M].f+di) V.pb(v[i]);
    sort(V.begin(), V.end(), cmp);
    auto z = strip(V,di);
   return min(min(a,b),z);
}
int main() {
       ios_base::sync_with_stdio(0);cin.tie(0);
       cout << fixed << setprecision(2);</pre>
       while (cin >> n) {
           if (n == 0) break;
           vector<pdd> v(n);
```

4.3 (4) Convex Hull

```
/**
* Source: Wikibooks
* Usage: https://open.kattis.com/problems/convexhull
11 cross(pii 0, pii A, pii B) {
    return
        (11)(A.f-0.f)*(B.s-0.s)-(11)(A.s-0.s)*(B.f-0.f);
}
vector<pii> convex_hull(vector<pii> P) {
    sort(P.begin(),P.end());
        P.erase(unique(P.begin(),P.end()),P.end());
    if (P.size() == 1) return P;
    int n = P.size();
    vector<pii> bot = {P[0]};
   FOR(i,1,n) {
       while (bot.size() > 1 &&
            cross(bot[bot.size()-2], bot.back(), P[i])
            <= 0) bot.pop_back();
       bot.pb(P[i]);
    bot.pop_back();
    vector<pii> up = \{P[n-1]\};
    FORd(i,n-1) {
       while (up.size() > 1 && cross(up[up.size()-2],
            up.back(), P[i]) <= 0) up.pop_back();
       up.pb(P[i]);
   }
    up.pop_back();
    bot.insert(bot.end(),all(up));
    return bot;
int main() {
    while (cin >> n) {
       if (n == 0) break;
       vector<pii> P(n); FOR(i,n) cin >> P[i].f >>
            P[i].s;
       vector<pii> hull = convex_hull(P);
       cout << hull.size() << "\n";</pre>
       for (auto a: hull) cout << a.f << " " << a.s</pre>
            << "\n";
   }
```

4.4 (4) LineContainer

```
* Source: KACTL
* Unused
bool Q;
struct Line {
       mutable ll k, m, p; // slope, y-intercept,
           last optimal x
       bool operator<(const Line& o) const {</pre>
               return Q ? p < o.p : k < o.k;</pre>
       }
};
struct LineContainer : multiset<Line> {
       const ll inf = LLONG_MAX;
       11 div(ll a, ll b) { // floored division
           if (b < 0) a *= -1, b *= -1;
           if (a >= 0) return a/b;
           return -((-a+b-1)/b);
       }
       // updates x->p, determines if y is unneeded
       bool isect(iterator x, iterator y) {
               if (y == end()) { x->p = inf; return 0;
               if (x->k == y->k) x->p = x->m > y->m ?
                   inf : -inf;
               else x->p = div(y->m - x->m, x->k -
                   y->k);
               return x->p >= y->p;
       }
       void add(ll k, ll m) {
               auto z = insert(\{k, m, 0\}), y = z++, x
                   = y;
               while (isect(y, z)) z = erase(z);
               if (x != begin() && isect(--x, y))
                   isect(x, y = erase(y));
               while ((y = x) != begin() \&\& (--x)->p
                   >= y->p) isect(x, erase(y));
       }
       11 query(11 x) {
               assert(!empty());
               Q = 1; auto 1 = *lb({0,0,x}); Q = 0;
               return 1.k * x + 1.m;
       }
};
int main() {
```

4.5 (4) MaxCollinear

```
/**
* Usage: https://open.kattis.com/problems/maxcolinear
int n, mx, ans;
map<pair<pii,int>,int> m;
pii p[1000];
pair<pii,int> getline(pii a, pii b) {
   pii z = \{b.f-a.f,b.s-a.s\};
   swap(z.f,z.s); z.f *= -1;
   int g = \_gcd(z.f,z.s); z.f /= g, z.s /= g;
   if (z.f < 0 \mid | (z.f == 0 \&\& z.s < 0)) z.f *= -1,
        z.s *= -1:
   return {z,z.f*a.f+z.s*a.s};
}
void solve() {
   mx = ans = 0; m.clear();
   FOR(i,n) cin >> p[i].f >> p[i].s;
   FOR(i,n) FOR(j,i+1,n) m[getline(p[i],p[j])] ++;
   for (auto a: m) mx = max(mx,a.s);
   FOR(i,1,n+1) if (i*(i-1)/2 \le mx) ans = i;
   cout << ans << "\n";
}
```

4.6 (4) Point in Polygon

```
/**
* Source: own
* Usage:
    https://open.kattis.com/problems/pointinpolygon
int n,m;
pii p[1000];
int area(pii x, pii y, pii z) {
   return (y.f-x.f)*(z.s-x.s)-(y.s-x.s)*(z.f-x.f);
bool on(pii x, pii y, pii z) {
   if (area(x,y,z) != 0) return 0;
   return min(x,y) \le z && z \le max(x,y);
double get(pii x, pii y, int z) {
   return double((z-x.s)*y.f+(y.s-z)*x.f)/(y.s-x.s);
void test(pii z) {
   int ans = 0;
   FOR(i,n) {
       pii x = p[i], y = p[(i+1)%n];
       if (on(x,y,z)) {
```

```
cout << "on\n";</pre>
           return;
       }
       if (x.s > y.s) swap(x,y);
       if (x.s <= z.s && y.s > z.s) {
           double t = get(x,y,z.s);
           if (t > z.f) ans++;
   }
   if (ans \% 2 == 1) cout << "in\n";
    else cout << "out\n";</pre>
}
void solve() {
   FOR(i,n) cin >> p[i].f >> p[i].s;
    cin >> m;
   FOR(i,m) {
       pii z; cin >> z.f >> z.s;
       test(z);
}
```

4.7 (4) Polygon Area

```
/**
 * Description: Shoelace Formula
 * Usage: https://open.kattis.com/problems/polygonarea
 */

double area(vector<pii> v) {
    double x = 0;
    FOR(i,sz(v)) {
        int j = (i+1)%sz(v);
        x += (l1)v[i].f*v[j].s;
        x -= (l1)v[j].f*v[i].s;
    }
    return x/2;
}
```

4.8 (5) LiChao Segment Tree

```
/**
  * Source:
    http://codeforces.com/blog/entry/51275?#comment-351413
  * Unused
  */

const int N = 100000 + 5;

int n, m;
int vis[N << 1];
char op[100];

struct line {
    double k, b;
    line(double _k = 0, double _b = 0) { k = _k; b =
    _b; }</pre>
```

```
double get(double x) { return k * x + b; }
} c[N << 1];
void modify(int x, int 1, int r, line v) {
    if (!vis[x]) { vis[x] = 1, c[x] = v; return; }
    if (c[x].get(1) > v.get(1) && c[x].get(r) >
        v.get(r)) return;
    if (c[x].get(1) < v.get(1) && c[x].get(r) <</pre>
        v.get(r)) { c[x] = v; return;}
    int m = (1 + r) >> 1;
    if (c[x].get(1) < v.get(1)) swap(c[x], v);
    if (c[x].get(m) > v.get(m)) modify(x<<1|1, m + 1,</pre>
        r, v);
    else {swap(c[x], v); modify(x<<1, 1, m, v);}</pre>
}
double get(int x, int 1, int r, int pos) {
   if (1 == r) return c[x].get(1);
    int m = (l + r) \gg 1; double ans = c[x].get(pos);
    if (pos <= m) ans = max(ans, get(x<<1, 1, m, pos));</pre>
    else ans = max(ans, get(x<<1|1, m + 1, r, pos));
    return ans;
}
int main() {
    cin >> n;
   FOR(i,n) {
       cin >> op;
       if (op[0] == 'Q') {
           int x; cin >> x;
           cout << get(1, 1, n, x) << "\n";
           double k, b; cin >> b >> k;
           line l = line(k, b);
           modify(1, 1, n, 1);
       }
   }
}
```

4.9 (5) Line Segment Intersection

```
/**
 * Source:
    https://open.kattis.com/problems/segmentintersection
 * If numbers are small enough, fractions are
    recommended.
 */

typedef pair<double,double> pdd;

pii A,B,C,D;

pdd operator*(int x, pdd y) {
    return {x*y.f,x*y.s};
}

pdd operator/(pdd y, int x) {
    return {y.f/x,y.s/x};
}
```

```
pdd operator+(pdd 1, pdd r) {
   return {1.f+r.f,1.s+r.s};
}
int sgn(pii a, pii b, pii c) {
   return (b.s-a.s)*(c.f-a.f)-(b.f-a.f)*(c.s-a.s);
pdd get(pii a, pii b, pii c, pii d) {
    return (abs(sgn(a,b,c))*d+abs(sgn(a,b,d))*c)
     /(abs(sgn(a,b,c))+abs(sgn(a,b,d)));
}
void solve() {
   cin >> A.f >> A.s >> B.f >> B.s >> C.f >> C.s >>
        D.f >> D.s;
   if (A > B) swap(A,B);
   if (C > D) swap(C,D);
   int a1 = sgn(A,B,C), a2 = sgn(A,B,D);
   if (a1 > a2) swap(a1,a2);
   if (!(a1 <= 0 && a2 >= 0)) {
       cout << "none\n";</pre>
       return:
   if (a1 == 0 && a2 == 0) {
       if (sgn(A,C,D) != 0) {
           cout << "none\n";</pre>
           return:
       pii x1 = max(A,C), x2 = min(B,D);
       if (x1 > x2) cout << "none\n";
       else if (x1 == x2) cout << (double)x1.f << " "</pre>
            << (double)x1.s << "\n";
       else cout << (double)x1.f << " " <<
            (double)x1.s << " " << (double)x2.f << " "
            << (double)x2.s << "\n";
       return;
    pdd z = get(A,B,C,D);
    if (mp((double)A.f,(double)A.s) <= z && z <=</pre>
        mp((double)B.f,(double)B.s)) cout << z.f << "</pre>
        " << z.s << "\n";
    else cout << "none\n";</pre>
}
int main() {
       ios_base::sync_with_stdio(0);cin.tie(0);
       int n; cin >> n;
       cout << fixed << setprecision(2);</pre>
       FOR(i,n) solve();
}
```

4.10 (6) KD Tree

```
int t = 0, cur = 0;
struct point {
    11 d[2];
   point(ll x, ll y) {
       d[0] = x, d[1] = y;
   point() {
       d[0] = 0, d[1] = 0;
};
11 distance(point a, point b) {
    11 d = 0;
    FOR(i,2) d += (a.d[i]-b.d[i])*(a.d[i]-b.d[i]);
    return d;
}
bool comp(point a, point b) {
    return a.d[cur] < b.d[cur];</pre>
struct node {
   point* pt = NULL;
   point lo, hi;
   node* c[2];
   int ax = 0;
   11 dist(point p) {
       11 d = 0;
       FOR(i,2) {
           if (p.d[i] < lo.d[i]) d +=</pre>
                (p.d[i]-lo.d[i])*(p.d[i]-lo.d[i]);
           else if (p.d[i] > hi.d[i]) d +=
                (p.d[i]-hi.d[i])*(p.d[i]-hi.d[i]);
       return d;
   node(int axis, point low, point high,
        vector<point> p) {
       lo = low, hi = high, ax = axis;
       if (p.size() > 1) {
           cur = ax;
           sort(p.begin(),p.end(),comp);
           int M = p.size()/2;
           while (M > 0 \&\& p[M].d[ax] == p[M-1].d[ax])
           point lo1 = lo; lo1.d[ax] = p[M].d[ax];
           point hi1 = hi; hi1.d[ax] = p[M].d[ax]-1;
           if (M) c[0] = new node((ax+1)\%2, lo, hi1,
                {p.begin(),p.begin()+M});
           c[1] = new node((ax+1)\%2,lo1,hi,
               {p.begin()+M,p.end()});
       } else if (p.size() == 1) {
           pt = new point(p[0]);
       }
   }
```

```
point get(point p) {
       if (pt) return *pt;
       if (!c[0]) return c[1]->get(p);
       int t = c[0] - dist(p) < c[1] - dist(p) ? 0 : 1;
       point z = c[t] - set(p);
       if (distance(p,z) <= c[t^1]->dist(p)) return z;
       point z1 = c[t^1]-\gcd(p);
       if (distance(p,z) < distance(p,z1)) return z;</pre>
       return z1;
};
node* root;
int main() {
       ios_base::sync_with_stdio(0);cin.tie(0);
       vector<point> x;
       FOR(i,100000) x.pb(point(rand() % 1000000000,
           rand() % 100000000));
       root = new
           node(0,point(-MOD,-MOD),point(MOD,MOD),x);
       FOR(i,100000) {
           point y(rand() % 1000000000, rand() %
               100000000);
           cout << y.d[0] << " " << y.d[1] << " " <<
               root->get(y).d[0] << " " <<
               root->get(y).d[1] << "\n";
       }
```

5 Graphs

5.1 (5) Biconnected Components

```
/**
* Source:
    http://www.geeksforgeeks.org/biconnected-components/
struct BCC {
   int V, ti = 0;
   vector<vi> adj;
   vi par, disc, low;
   vector<vector<pii>> fin;
   vector<pii> st;
   void init(int _V) {
       V = V;
       par.resize(V), disc.resize(V), low.resize(V),
           adj.resize(V);
       FOR(i,V) par[i] = disc[i] = low[i] = -1;
   void addEdge(int u, int v) {
       adj[u].pb(v), adj[v].pb(u);
```

```
void BCCutil(int u) {
       disc[u] = low[u] = ti++;
       int child = 0;
       for (int i: adj[u]) if (i != par[u]) {
           if (disc[i] == -1) {
               child ++; par[i] = u;
               st.pb({u,i});
               BCCutil(i);
               low[u] = min(low[u],low[i]);
               if ((disc[u] == 0 && child > 1) ||
                   (disc[u] != 0 && disc[u] <=
                   low[i])) { // checks for
                   articulation point
                  vector<pii> tmp;
                  while (st.back() != mp(u,i))
                       tmp.pb(st.back()),
                       st.pop_back();
                  tmp.pb(st.back()), st.pop_back();
                  fin.pb(tmp);
               }
           } else if (disc[i] < low[u]) {</pre>
               low[u] = disc[i];
               st.pb({u,i});
           }
       }
   }
   void bcc() {
       FOR(i,V) if (disc[i] == -1) {
           BCCutil(i);
           if (st.size()) fin.pb(st);
           st.clear();
       }
   }
};
int main() {
       ios_base::sync_with_stdio(0);cin.tie(0);
       BCC g; g.init(12);
       g.addEdge(0,1);
   g.addEdge(1,2);
   g.addEdge(1,3);
   g.addEdge(2,3);
   g.addEdge(2,4);
   g.addEdge(3,4);
   g.addEdge(1,5);
   g.addEdge(0,6);
   g.addEdge(5,6);
   g.addEdge(5,7);
   g.addEdge(5,8);
   g.addEdge(7,8);
   g.addEdge(8,9);
   g.addEdge(10,11);
   g.bcc();
   for (auto a: g.fin) {
       for (pii b: a) cout << b.f << " " << b.s << "</pre>
           | ";
       cout << "\n";
```

```
}
```

5.2 (5) Kosaraju

```
/**
* Source: Wikipedia
* Description: generates SCC in topological order
const int MX = 100001;
struct scc {
   vi adj[MX], radj[MX], todo;
   int comp[MX], N, M;
   bool visit[MX];
   scc() {
       memset(comp,0,sizeof comp);
       memset(visit,0,sizeof visit);
   void dfs(int v) {
       visit[v] = 1;
       for (int w: adj[v]) if (!visit[w]) dfs(w);
       todo.pb(v);
   void dfs2(int v, int val) {
       comp[v] = val;
       for (int w: radj[v]) if (!comp[w]) dfs2(w,val);
   void addEdge(int a, int b) {
              adj[a].pb(b), radj[b].pb(a);
   void genSCC() {
       FOR(i,1,N+1) if (!visit[i]) dfs(i);
       reverse(all(todo)); // toposort
       for (int i: todo) if (!comp[i]) dfs2(i,i);
};
scc S;
int main() {
       cin >> S.N >> S.M;
       FOR(i,S.M) {
              int a,b; cin >> a >> b;
              S.addEdge(a,b);
       S.genSCC();
```

5.3 (6) Euler Tour

```
* Description: extra log factor
* Usage: https://open.kattis.com/problems/eulerianpath
vi circuit;
multiset<int> adj[10000], adj1[10000];
int N,M, out[10000], in[10000];
void find_circuit(int x) { // directed graph, possible
    that resulting circuit is not valid
   while (adj[x].size()) {
       int j = *adj[x].begin();
            adj[x].erase(adj[x].begin());
       find_circuit(j);
   }
   circuit.pb(x);
}
int a,b,start;
void solve() {
   FOR(i,N) {
       adj[i].clear(), adj1[i].clear();
       out[i] = in[i] = 0;
   circuit.clear();
   FOR(i,M) {
       cin >> a >> b;
       adj[a].insert(b), adj1[a].insert(b);
       out[a] ++, in[b] ++;
   start = a;
   FOR(i,N) if (out[i]-in[i] == 1) start = i;
   find_circuit(start);
   reverse(circuit.begin(),circuit.end());
   if (circuit.size() != M+1) {
       cout << "Impossible\n";</pre>
       return:
   }
   FOR(i,M) {
       if (adj1[circuit[i]].find(circuit[i+1]) ==
           adj1[circuit[i]].end()) {
           cout << "Impossible\n";</pre>
           return;
       int t = circuit[i];
       adj1[t].erase(adj1[t].find(circuit[i+1]));
   FOR(i,M+1) cout << circuit[i] << " ";
   cout << "\n";
}
int main() {
   ios_base::sync_with_stdio(0);cin.tie(0);
   while (cin >> N >> M) {
       if (N+M == 0) break;
       solve();
   }
```

5.4 Shortest Path

5.4.1 (3) Bellman-Ford

```
/**
* Source: own
* Description: can be useful with linear programming
* Usage: https://open.kattis.com/problems/shortestpath3
*/
const ll INF = 1e18:
int n,m,q,s,bad[1000];
vector<pair<pii,int>> edge;
ll dist[1000];
void solve() {
   edge.clear();
   FOR(i,n) dist[i] = INF, bad[i] = 0;
   dist[s] = 0;
   FOR(i,m) {
       int u,v,w; cin >> u >> v >> w;
       edge.pb(\{\{u,v\},w\});
   FOR(i,n) for (auto a: edge) if (dist[a.f.f] < INF)</pre>
        dist[a.f.s] = min(dist[a.f.s],
        dist[a.f.f]+a.s);
   for (auto a: edge) if (dist[a.f.f] < INF) if</pre>
        (dist[a.f.s] > dist[a.f.f]+a.s) bad[a.f.s] = 1;
   FOR(i,n) for (auto a: edge) if (bad[a.f.f])
        bad[a.f.s] = 1;
   FOR(i,q) {
       int x; cin >> x;
       if (bad[x]) cout << "-Infinity\n";</pre>
       else if (dist[x] == INF) cout <<</pre>
            "Impossible\n";
       else cout << dist[x] << "\n";</pre>
   cout << "\n";
```

5.4.2 (3) Dijkstra

```
/**
  * Source: own
  */

template<int SZ> struct Dijkstra {
    int dist[SZ];
    vector<pii> adj[SZ];
    priority_queue<pii,vector<pii>,greater<pii>> q;

    void gen() {
        fill_n(dist,SZ,MOD); dist[0] = 0;
}
```

```
q.push({0,0});
       while (q.size()) {
               pii x = q.top(); q.pop();
               if (dist[x.s] < x.f) continue;</pre>
               for (pii y: adj[x.s]) if (x.f+y.s <</pre>
                    dist[y.f]) {
                       dist[y.f] = x.f+y.s;
                       q.push({dist[y.f],y.f});
               }
       }
    }
};
Dijkstra<100> D;
int main() {
       FOR(i,100) FOR(j,100) if (rand() % 10 == 0)
            D.adj[i].pb({j,rand() % 10+1});
       D.gen();
       FOR(i,100) cout << D.dist[i] << "\n";</pre>
}
```

5.4.3 (3) Floyd-Warshall

```
* Source: own
* Usage: https://open.kattis.com/problems/allpairspath
const 11 INF = 1e18;
int n,m,q; // vertices, edges, queries
ll dist[150][150], bad[150][150];
void solve() {
   FOR(i,n) FOR(j,n) dist[i][j] = INF, bad[i][j] = 0;
   FOR(i,n) dist[i][i] = 0;
   FOR(i,m) {
       int u,v,w; cin >> u >> v >> w;
       dist[u][v] = min(dist[u][v],(l1)w);
   FOR(k,n) FOR(i,n) FOR(j,n) if (dist[i][k] != INF
        && dist[k][j] != INF)
       dist[i][j] =
           min(dist[i][j],dist[i][k]+dist[k][j]);
   FOR(k,n) FOR(i,n) FOR(j,n) if (dist[i][k] != INF
        && dist[k][j] != INF)
       if (dist[i][j] > dist[i][k]+dist[k][j])
           bad[i][j] = 1;
   FOR(k,n) FOR(i,n) FOR(j,n) {
       if (dist[i][k] < INF && bad[k][j]) bad[i][j] =</pre>
       if (bad[i][k] && dist[k][j] < INF) bad[i][j] =</pre>
   }
   FOR(i,q) {
       int u,v; cin >> u >> v;
```

6 Math

6.1 (5) Chinese Remainder Theorem

```
/**
* Source: Own
* Usage: Kattis generalchineseremainder
ll n,m,a,b;
map<ll,pii> M;
bool bad;
ll inv(ll a, ll b) { // 0 < a < b, gcd(a,b) = 1
   a %= b;
   if (a <= 1) return a:</pre>
   11 i = inv(b\%a,a);
   ll tmp = -((b/a)*i+((b\%a)*i)/a) \% b;
   while (tmp < 0) tmp += b;
   return tmp;
}
ll naive(ll n, ll m, ll a, ll b) {
   11 x = (a-b)*inv(m,n) % n;
   11 ans = (m*x+b) \% (m*n);
   while (ans < 0) ans += (m*n);
   return ans;
void process(ll a, ll n) {
   vector<pii> z;
   for (int i = 2; i*i <= n; ++i) if (n % i == 0) {
       int co = 0;
       while (n \% i == 0) n /= i, co++;
       z.pb({i,co});
   if (n != 1) z.pb({n,1});
   for (auto A: z) {
       if (M.count(A.f)) {
           pii p1 = M[A.f];
           pii p2 = {A.s,a%(11)pow(A.f,A.s)};
           if (p1 > p2) swap(p1,p2);
           if (p2.s%(ll)pow(A.f,p1.f) != p1.s) bad = 1;
           M[A.f] = p2;
       } else M[A.f] = {A.s,a%(11)pow(A.f,A.s)};
   }
}
ll po(ll b, ll p) {
   11 z = 1;
   FOR(i,p) z *= b;
```

```
return z;
}
void solve() {
    bad = 0, M.clear();
    long long aa,nn,bb,mm; cin >> aa >> nn >> bb >> mm;
    a = aa, n = nn, b = bb, m = mm;
    process(a,n), process(b,m);
    if (bad) {
       cout << "no solution\n";</pre>
       return;
    11 a1 = 0, a2 = 1;
    for (auto& x: M) {
       a1 = naive(a2,po(x.f,x.s.f),a1,x.s.s);
       a2 *= po(x.f,x.s.f);
    }
    cout << (long long)a1 << " " << (long long)a2 <<</pre>
}
int main() {
    ios_base::sync_with_stdio(0);cin.tie(0);
    int T; cin >> T;
    FOR(i,T) solve();
```

6.2 (5) Combinations

```
/**
* Source: Own
template<int SZ> struct Combo {
   11 fac[SZ+1], ifac[SZ+1];
   Combo() {
       fac[0] = ifac[0] = 1;
       FOR(i,1,SZ+1) {
           fac[i] = i*fac[i-1] % MOD;
           ifac[i] = inv(fac[i]);
   }
   ll po (ll b, ll p) {
       return !p?1:po(b*b%MOD,p/2)*(p&1?b:1)%MOD;
   11 inv (11 b) { return po(b,MOD-2); }
   11 comb(ll a, ll b) {
       if (a < b) return 0;</pre>
       11 tmp = fac[a]*ifac[b] % MOD;
       tmp = tmp*ifac[a-b] % MOD;
       return tmp;
   }
};
```

6.3 (5) Eratosthenes' Sieve

6.4 (6) FFT, NTT

```
* Sources: KACTL, https://pastebin.com/3Tnj5mRu
typedef complex<double> cd;
typedef vector<cd> vcd;
typedef vector<ll> vl;
namespace Poly {
   int get(int s) {
       return s > 1 ? 32 - __builtin_clz(s - 1) : 0;
   namespace FFT {
       vcd fft(vcd& a) {
           int n = a.size(), x = get(n);
           vcd res, RES(n), roots(n);
           FOR(i,n) roots[i] =
               cd(cos(2*M_PI*i/n),sin(2*M_PI*i/n));
           res = a;
           FOR(i,1,x+1) {
              int inc = n>>i;
              FOR(j,inc) for (int k = 0; k < n; k +=
                   inc) {
                  int t = 2*k%n+j;
                  RES[k+j] =
                      res[t]+roots[k]*res[t+inc];
               swap(res,RES);
           }
           return res;
       }
       vcd fft_rev(vcd& a) {
```

```
vcd res = fft(a);
       FOR(i,sz(res)) res[i] /= a.size();
       reverse(res.begin() + 1, res.end());
       return res;
   }
   vcd brute(vcd& a, vcd& b) {
       vcd c(sz(a)+sz(b)-1);
       FOR(i,sz(a)) FOR(j,sz(b)) c[i+j] +=
           a[i]*b[j];
       return c;
   }
   vcd conv(vcd a, vcd b) {
       int s = sz(a)+sz(b)-1, L = get(s), n = 1 << L;
       if (s <= 0) return {};</pre>
       if (s <= 200) return brute(a,b);</pre>
       a.resize(n); a = fft(a);
       b.resize(n); b = fft(b);
       FOR(i,n) a[i] *= b[i];
       a = fft_rev(a);
       a.resize(s);
       return a;
   }
}
namespace NTT {
   const 11 mod = (119 << 23) + 1, root = 3; // =</pre>
        998244353
   // For p < 2^30 there is also e.g. (5 << 25,
        3), (7 << 26, 3),
   // (479 << 21, 3) and (483 << 21, 5). The last
        two are > 10^9.
   11 modpow(ll b, ll p) { return
        !p?1:modpow(b*b\mod,p/2)*(p\lambda1?b:1)\mod; }
   11 inv (11 b) { return modpow(b,mod-2); }
   vl ntt(vl& a) {
       int n = a.size(), x = get(n);
       vl res, RES(n), roots(n);
       roots[0] = 1, roots[1] =
           modpow(root, (mod-1)/n);
       FOR(i,2,n) roots[i] = roots[i-1]*roots[1] %
           mod:
       res = a;
       FOR(i,1,x+1) {
           int inc = n>>i;
           FOR(j,inc) for (int k = 0; k < n; k +=
               inc) {
              int t = 2*k%n+j;
              RES[k+j] =
                   (res[t]+roots[k]*res[t+inc]) %
           swap(res,RES);
```

```
return res;
       }
       vl ntt_rev(vl& a) {
           vl res = ntt(a);
           11 in = inv(a.size());
           FOR(i,sz(res)) res[i] = res[i]*in % mod;
           reverse(res.begin() + 1, res.end());
           return res;
       }
       vl brute(vl& a, vl& b) {
           vl c(sz(a)+sz(b)-1);
           FOR(i,sz(a)) FOR(j,sz(b)) c[i+j] =
                (c[i+j]+a[i]*b[j])%mod;
           return c;
       }
       vl conv(vl a, vl b) {
           int s = sz(a)+sz(b)-1, L = get(s), n = 1 << L;
           if (s <= 0) return {};</pre>
           if (s <= 200) return brute(a,b);</pre>
           a.resize(n); a = ntt(a);
           b.resize(n); b = ntt(b);
           FOR(i,n) a[i] = a[i]*b[i] % mod;
           a = ntt_rev(a);
           a.resize(s);
           return a;
   }
}
int main() {
    ios_base::sync_with_stdio(0);cin.tie(0);
   vcd x =
        Poly::FFT::conv({1,2,3,4,5,6,7,8},{1,2,3,4,5,6,7,8});
   for (auto a: x) cout << a << "\n";</pre>
   cout << "\n";
        Poly::NTT::conv({1,2,3,4,5,6,7,8},{1,2,3,4,5,6,7,8});
   for (auto a: X) cout << a << "\n";</pre>
```

7 Strings

7.1 (3) Hashing

```
/**
* Source: own
*/

typedef pair<ll, ll> pll;
```

```
template<class T> pair<T,T> operator+(const pair<T,T>&
    1, const pair<T,T>& r) {
   return {(1.f+r.f)%MOD,(1.s+r.s)%MOD};
}
template<class T> pair<T,T> operator-(const pair<T,T>&
    1, const pair<T,T>& r) {
   return {(1.f-r.f+MOD)%MOD,(1.s-r.s+MOD)%MOD);
}
template<class T> pair<T,T> operator*(const pair<T,T>&
    1, const T& r) {
   return {1.f*r%MOD,1.s*r%MOD};
template<class T> pair<T,T> operator*(const pair<T,T>&
    1, const pair<T,T>& r) {
   return {1.f*r.f%MOD,1.s*r.s%MOD};
}
struct hsh {
   string S;
   vector<pll> po, ipo, cum;
   pll base = mp(948392576,573928192);
   11 modpow(ll b, ll p) {
       return !p?1:modpow(b*b%MOD,p/2)*(p&1?b:1)%MOD;
   }
   ll inv(ll x) {
       return modpow(x,MOD-2);
   void gen(string _S) {
       S = _S;
       po.resize(sz(S)), ipo.resize(sz(S)),
           cum.resize(sz(S)+1);
       po[0] = ipo[0] = \{1,1\};
       FOR(i,1,sz(S)) {
           po[i] = po[i-1]*base;
           ipo[i] = {inv(po[i].f),inv(po[i].s)};
       FOR(i,sz(S)) cum[i+1] =
           cum[i]+po[i]*(l1)(S[i]-'a'+1);
   }
   pll get(int 1, int r) {
       return ipo[l]*(cum[r+1]-cum[l]);
};
int lcp(hsh& a, hsh& b) {
   int lo = 0, hi = min(sz(a.S), sz(b.S));
   while (lo < hi) {</pre>
       int mid = (lo+hi+1)/2;
       if (a.get(0,mid-1) == b.get(0,mid-1)) lo = mid;
       else hi = mid-1;
   }
   return lo;
int main() {
```

7.2 (4) Bitset Trie

```
/**
* Source: own?
*/
template<int MX> struct tri {
   int nex = 0, ans = 0;
   int trie[MX][2]; // easily changed to character
   tri() {
       memset(trie,0,sizeof trie);
   void ins(int x) {
       int cur = 0;
       FORd(i,30) {
           int t = (x&(1<<i))>>i;
           if (!trie[cur][t]) trie[cur][t] = ++nex;
           cur = trie[cur][t];
   }
   void test(int x) {
       int cur = 0;
       FORd(i,30) {
           int t = ((x&(1<<i))>>i) ^ 1;
           if (!trie[cur][t]) t ^= 1;
           cur = trie[cur][t];
           if (t) x ^= (1<<i);</pre>
       ans = max(ans,x);
   }
};
int main() {
```

7.3 (5) Aho-Corasick

```
/**
 * Source: GeeksForGeeks
 * also see https://ideone.com/OcMjZJ
 */
string arr[200];
```

```
int val[200], states = 1;
queue<int> update;
const int MAXS = 201;
const int MAXC = 26;
int n, out[MAXS], f[MAXS], g[MAXS][MAXC];
int buildMatchingMachine() {
   memset(out, 0, sizeof out);
   memset(g, -1, sizeof g);
   FOR(i,n) {
       string word = arr[i];
       int currentState = 0;
       FOR(j,word.size()) {
           int ch = word[j] - 'a';
           if (g[currentState][ch] == -1)
               g[currentState][ch] = states++;
           currentState = g[currentState][ch];
       out[currentState] += val[i];
   FOR(ch, MAXC) if (g[0][ch] == -1) g[0][ch] = 0;
   memset(f, -1, sizeof f);
   queue<int> q;
   FOR(ch,MAXC)
       if (g[0][ch] != 0) {
           f[g[0][ch]] = 0;
           q.push(g[0][ch]);
   while (q.size()) {
       int state = q.front();
       q.pop();
       FOR(ch,MAXC) {
           if (g[state][ch] != -1) {
               int failure = f[state];
               while (g[failure][ch] == -1) failure =
                   f[failure];
               failure = g[failure][ch];
               f[g[state][ch]] = failure;
               out[g[state][ch]] += out[failure];
              q.push(g[state][ch]);
       }
   }
   return states;
}
int findNextState(int currentState, char nextInput) {
   int answer = currentState;
   int ch = nextInput - 'a';
```

```
while (g[answer][ch] == -1){
    update.push(answer);
    answer = f[answer];
}
if (update.size()){
    while (update.size()){
        int k = update.front(); update.pop();
        g[k][nextInput-'a'] = g[answer][ch];
        //cache state transitions: often
        necessary if we don't want to
        explicitly compute all of them
    }
}
return g[answer][ch];
}
int main() {
```

7.4 (5) Manacher

```
* Source: http://codeforces.com/blog/entry/12143
* Description: Calculates length of largest palindrome
    centered at each character of string
vi manacher(string s) {
   string s1 = "0";
   for (char c: s) s1 += c, s1 += "#";
   s1[s1.length()-1] = '&';
   vi ans(s1.length()-1);
   int lo = 0, hi = 0;
   FOR(i,1,s1.length()-1) {
       ans[i] = min(hi-i,ans[hi-i+lo]);
       while (s1[i-ans[i]-1] == s1[i+ans[i]+1])
            ans[i] ++;
       if (i+ans[i] > hi) lo = i-ans[i], hi =
            i+ans[i]:
   ans.erase(ans.begin());
   FOR(i,ans.size()) if ((i&1) == (ans[i]&1)) ans[i]
        ++; // adjust lengths
   return ans;
}
int main() {
       ios_base::sync_with_stdio(0);cin.tie(0);
       vi a1 = manacher("abacaba");
       for (int i: a1) cout << i << " ";</pre>
       cout << "\n";
       vi a2 = manacher("aabbaaccaabbaa");
       for (int i: a2) cout << i << " ";</pre>
```

7.5 (5) Z

```
/**
* Source: http://codeforces.com/blog/entry/3107
* similar to KMP
vi z(string s) {
    int N = s.length(); s += '#';
    vi ans(N); ans[0] = N;
    while (s[1+ans[1]] == s[ans[1]]) ans[1] ++;
    int L = 1, R = ans[1];
    FOR(i,2,N) {
       if (i <= R) ans[i] = min(R-i+1,ans[i-L]);</pre>
       while (s[i+ans[i]] == s[ans[i]]) ans[i] ++;
       if (i+ans[i]-1 > R) L = i, R = i+ans[i]-1;
    return ans;
}
vi get(string a, string b) { // find prefixes of a in b
    string s = a + "0" + b;
    vi t = z(s);
    return vi(t.begin()+a.length()+1,t.end());
}
int main() {
       ios_base::sync_with_stdio(0);cin.tie(0);
       vi x = z("abcababcabcaba");
       for (int i: x) cout << i << " ";</pre>
       cout << "\n";
       x = get("abcab","uwetrabcerabcab");
       for (int i: x) cout << i << " ";</pre>
}
```

7.6 (6) Suffix Array

```
/**
 * Source: SuprDewd CP Course
 * Task: https://open.kattis.com/problems/suffixsorting
 */

struct suffix_array {
   int N;
   vector<vi> P;
   vector<pair<pii,int>> L;
   vi idx;
   string str;

suffix_array(string _str) {
    str = _str; N = str.length();
    P.pb(vi(N)); L.resize(N);
   FOR(i,N) P[O][i] = str[i];

   for (int stp = 1, cnt = 1; cnt < N; stp ++,
        cnt *= 2) {
        P.pb(vi(N));
   }
}</pre>
```

```
FOR(i,N) L[i] = \{\{P[stp-1][i], i+cnt < N ?\}\}
               P[stp-1][i+cnt] : -1},i};
           sort(L.begin(),L.end());
           FOR(i,N) {
               if (i && L[i].f == L[i-1].f)
                   P[stp][L[i].s] = P[stp][L[i-1].s];
               else P[stp][L[i].s] = i;
           }
       }
       idx.resize(N);
       FOR(i,P[P.size()-1].size())
            idx[P[P.size()-1][i]] = i;
   int lcp(int x, int y) {
       int res = 0;
       if (x == y) return N-x;
       for (int k = P.size() - 1; k >= 0 && x < N &&
           v < N; k--) {
           if (P[k][x] == P[k][y]) {
              x += 1 << k;
               y += 1 << k;
               res += 1 << k;
       }
       return res;
   }
};
int main() {
       ios_base::sync_with_stdio(0);cin.tie(0);
       string s;
       while (getline(cin,s)) {
           if (s[s.length()-1] == '\r')
               s.erase(s.end()-1);
           suffix_array sa = suffix_array(s);
           int z; cin >> z;
           FOR(i,z) {
               int x; cin >> x;
               cout << sa.idx[x] << " ";</pre>
           cout << "\n";
           getline(cin,s);
       }
```

8 Trees

8.1 (3) DSU, Kruskal

```
DSU() {
       FOR(i,SZ) par[i] = i, sz[i] = 1;
    int get(int x) { // path compression
       if (par[x] != x) par[x] = get(par[x]);
       return par[x];
   bool unite(int x, int y) { // union-by-rank
       x = get(x), y = get(y);
       if (x == y) return 0;
       if (sz[x] < sz[y]) swap(x,y);
       sz[x] += sz[y], par[y] = x;
       return 1;
    }
};
int ans = 0;
vector<pair<int,pii>> edge;
DSU<100> D;
void kruskal() {
       sort(edge.begin(),edge.end());
       for (auto a: edge) if (D.unite(a.s.f,a.s.s))
            ans += a.f:
}
int main() {
       FOR(i,100) FOR(j,i+1,100) if (rand() % 5 == 0)
            edge.pb({rand() % 100+1,{i,j}});
       cout << D.sz[D.get(5)] << " " << ans;</pre>
}
```

8.2 (4) Centroid Decomposition

```
* Source: own
*/
const int MX = 100001;
int N, visit[MX], sub[MX], par[MX];
vi adj[MX];
void dfs (int no) {
   sub[no] = 1;
   for (int i: adj[no]) if (!visit[i] && i !=
       par[no]) {
       par[i] = no;
       dfs(i);
       sub[no] += sub[i];
   }
}
int get_centroid(int x) {
   par[x] = 0;
   dfs(x);
```

```
int sz = sub[x];
   while (1) {
       pii mx = {0,0};
       for (int i: adj[x]) if (!visit[i] && i !=
           par[x]) mx = max(mx, {sub[i], i});
       if (mx.f*2 > sz) x = mx.s;
       else return x;
}
void solve (int x) {
   x = get_centroid(x); visit[x] = 1;
   // do stuff
   cout << x << "\n":
   for (int i: adj[x]) if (!visit[i]) solve(i);
}
int main() {
       ios_base::sync_with_stdio(0);cin.tie(0);
       cin >> N;
       FOR(i,N-1) {
           int a,b; cin >> a >> b;
           adj[a].pb(b), adj[b].pb(a);
       solve(1);
```

8.3 (4) HLD

```
* Source: http://codeforces.com/blog/entry/22072
* Task: USACO Grass Planting
// insert LazySegTree Template
vector<vi> graph;
template <int V> struct HeavyLight { // sum queries,
    sum updates
   int parent[V], heavy[V], depth[V];
   int root[V], treePos[V];
   LazySegTree<V> tree;
   void init() {
       int n = graph.size();
       FOR(i,1,n+1) heavy[i] = -1;
       parent[1] = -1, depth[1] = 0;
       dfs(1);
       for (int i = 1, currentPos = 0; i <= n; ++i)</pre>
                      if (parent[i] == -1 ||
                          heavy[parent[i]] != i)
                             for (int j = i; j != -1;
                                  j = heavy[j]) {
                                    root[j] = i;
                                    treePos[j] =
                                         currentPos++;
                             }
   }
```

```
int dfs(int v) {
       int size = 1, maxSubtree = 0;
       for (auto u : graph[v]) if (u != parent[v]) {
           parent[u] = v;
           depth[u] = depth[v] + 1;
           int subtree = dfs(u);
           if (subtree > maxSubtree) heavy[v] = u,
               maxSubtree = subtree:
           size += subtree;
       }
       return size;
   }
   template <class BinaryOperation>
   void processPath(int u, int v, BinaryOperation op)
       for (; root[u] != root[v]; v =
           parent[root[v]]) {
           if (depth[root[u]] > depth[root[v]])
               swap(u, v);
           op(treePos[root[v]], treePos[v]);
       }
       if (depth[u] > depth[v]) swap(u, v);
       op(treePos[u]+1, treePos[v]); // assumes
            values are stored in edges, not vertices
   void modifyPath(int u, int v, int value) {
       processPath(u, v, [this, &value](int 1, int r)
            { tree.upd(1, r, value); });
   }
   11 queryPath(int u, int v) {
       11 \text{ res} = 0;
       processPath(u, v, [this, &res](int 1, int r) {
            res += tree.qsum(1, r); });
       return res;
   }
HeavyLight<1<<17> H;
int N,M;
int main() {
       cin >> N >> M;
       graph.resize(N+1);
       FOR(i,N-1) {
           int a,b; cin >> a >> b;
           graph[a].pb(b), graph[b].pb(a);
       H.init();
       FOR(i,M) {
           char c; int A,B;
           cin >> c >> A >> B;
           if (c == 'P') H.modifyPath(A,B,1);
           else cout << H.queryPath(A,B) << "\n";</pre>
       }
}
```

8.4 (4) LCA with Binary Jumps

```
/**
* Source: USACO Camp
const int MAXN = 100001, MAXK = 17;
int Q;
struct LCA {
   int V;
   vi edges[MAXN];
   int parK[MAXK][MAXN];
   int depth[MAXN];
   void addEdge(int u, int v) {
       edges[u].pb(v), edges[v].pb(u);
   void dfs(int u, int prev){
       parK[0][u] = prev;
       depth[u] = depth[prev]+1;
       for (int v: edges[u]) if (v != prev) dfs(v, u);
   void construct() {
       dfs(1, 0);
       FOR(k,1,MAXK) FOR(i,1,V+1)
           parK[k][i] = parK[k-1][parK[k-1][i]];
   }
   int lca(int u, int v){
       if (depth[u] < depth[v]) swap(u,v);</pre>
       FORd(k,MAXK) if (depth[u] >= depth[v]+(1<<k))</pre>
           u = parK[k][u];
       FORd(k,MAXK) if (parK[k][u] != parK[k][v]) u =
           parK[k][u], v = parK[k][v];
       if(u != v) u = parK[0][u], v = parK[0][v];
       return u;
   }
   int dist(int u, int v) {
       return depth[u]+depth[v]-2*depth[lca(u,v)];
};
LCA L;
int main(){
   cin >> L.V >> Q;
   FOR(i,L.V-1) {
       int u,v; cin >> u >> v;
       L.addEdge(u,v);
   L.construct();
   FOR(i,Q) {
       int u,v; cin >> u >> v;
```

```
cout << L.dist(u,v) << "\n";
}</pre>
```

8.5 (4) LCA with RMQ

```
/**
* Description: Euler Tour LCA w/ O(1) query
* Source: own
const int MAXN = 100001, MAXK = 17;
int Q;
struct RMQ2 {
   vi edges[MAXN];
   pii rmq[MAXK][2*MAXN];
   int depth[MAXN], pos[MAXN];
   int N, nex=0;
   void addEdge(int u, int v) {
       edges[u].pb(v), edges[v].pb(u);
    void dfs(int u, int prev){
       pos[u] = nex; depth[u] = depth[prev]+1;
       rmq[0][nex++] = {depth[u],u};
       for (int v: edges[u]) if (v != prev) {
           dfs(v, u);
           rmq[0][nex++] = {depth[u],u};
   }
   void construct() {
       dfs(1, 0);
       FOR(k,1,MAXK) FOR(i,nex) if (i+(1<<(k-1)) <
           nex) rmq[k][i] =
           min(rmq[k-1][i],rmq[k-1][i+(1<<(k-1))]);
   }
    int lca(int u, int v){
       u = pos[u], v = pos[v];
       if (u > v) swap(u,v);
       int x = 31-__builtin_clz(v-u+1);
       return min(rmq[x][u],rmq[x][v-(1<<x)+1]).s;</pre>
   }
    int dist(int u, int v) {
       return depth[u]+depth[v]-2*depth[lca(u,v)];
   }
};
RMQ2 R;
int main(){
   cin >> R.N >> Q;
   FOR(i,R.N-1) {
       int u,v; cin >> u >> v;
```

```
R.addEdge(u,v);
}
R.construct();

FOR(i,Q) {
    int u,v; cin >> u >> v;
    cout << R.dist(u,v) << "\n";
}
</pre>
```