

Assignment 1: CS106L GraphViz

Due: Tuesday, 30th January, 11:59pm

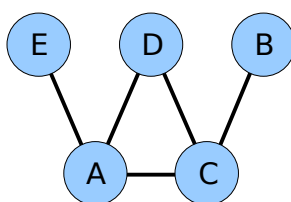
Introduction

One of the most useful abstractions in computer science is the *graph*, a means of expressing relationships between objects. Formally, a graph is a collection of *nodes* (also called *vertices*) joined together by *edges* (also called *arcs*), where each node represents some object and each edge connects two nodes that are somehow related. For example, Facebook represents people and friendships as a graph – each person is node, and two people are connected by edges if they are friends of one another. The Google search engine is powered by the PageRank algorithm, which treats webpages as nodes and has an edge between any two pages that have links to one another. Recent work into the *smart grid* treats the electrical grid as a graph by modeling power stations and substations as nodes and power lines as edges.

One advantage of using graphs to represent relationships is that graphs have a natural geometric interpretation. In particular, we can visualize the structure of a graph by drawing a dot for each node and a line between any two nodes joined by an edge. For example, suppose that we want to represent friendships in a small group of people using a graph. Let's name the people in this group Alice, Bob, Christine, David, and Evelyn and suppose that their friendships are as follows:

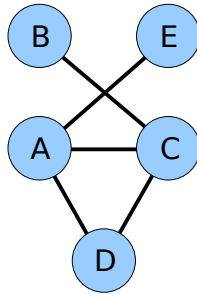
- Alice, Christine, and David are all friends of one another.
- Bob and Christine are friends.
- Evelyn and Alice are friends.

We could then draw these relationships in a graph as follows:

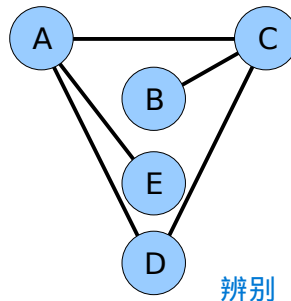


This picture makes it much easier to see who is friends with one another.

An important detail to notice, though, is that **this is not the only possible way that we could have drawn this graph**. Below is an entirely different rendering of the graph:

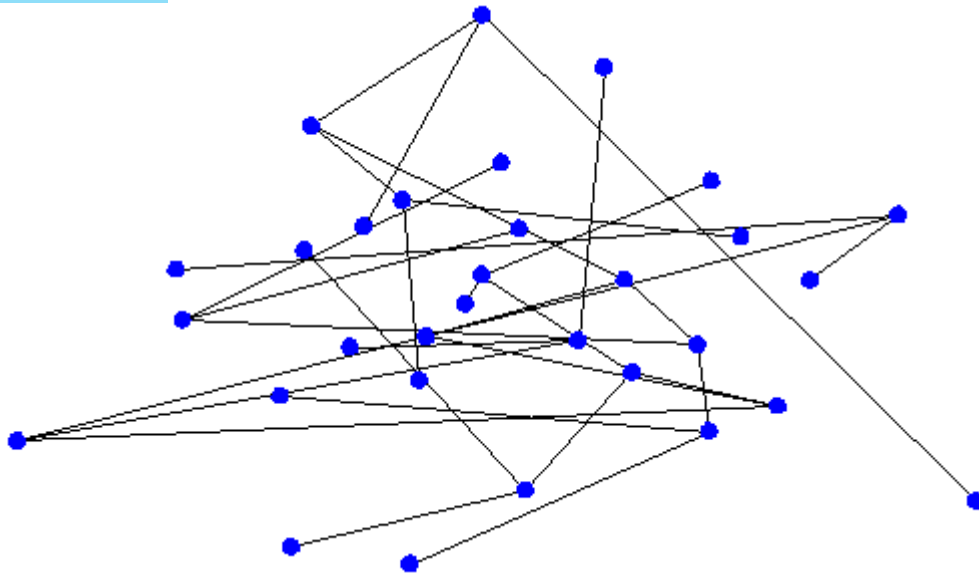


And here is yet another:

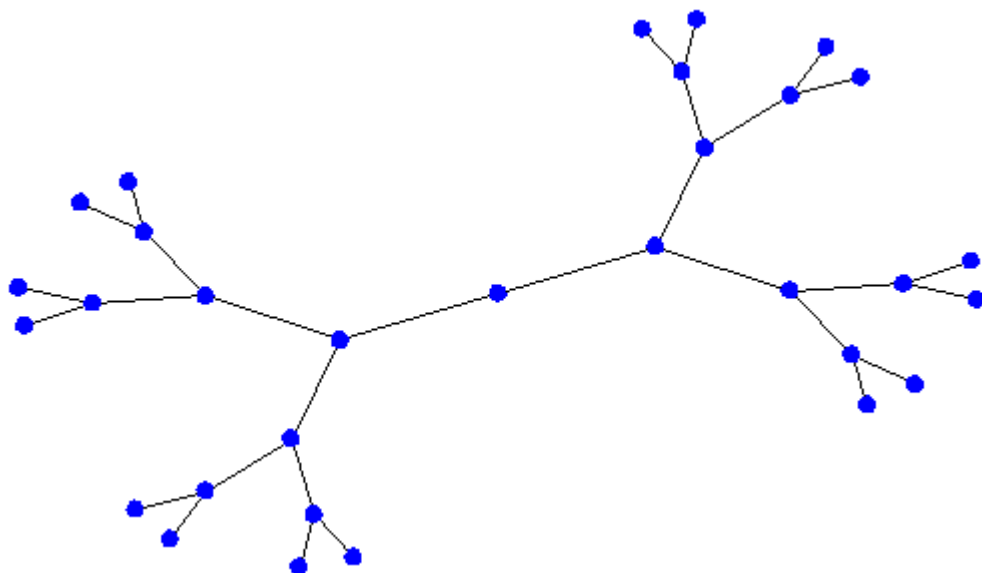


在极端情况下，可能会以完全掩盖
图形节点之间关系的方式布置图形

In all three of these cases, it is possible to discern the group's friendships, though some of these drawings are easier to interpret than others. In the extreme, it is possible to lay out graphs in ways that entirely obscure the relationships between the graph's nodes. For example, consider the following graph layout:



分散 This drawing is a mess! Many of the arcs cross one another, the nodes seem to be scattered around randomly, and the overall drawing is garbled. However, consider this alternative drawing below:



This drawing is for *exactly the same graph* as the previous image, but the structure is much more visible. The drawing is symmetric, the nodes are spaced apart in an aesthetically pleasing manner, and the edges do not cross one another.

审美

In general, it can be difficult to find aesthetically pleasing layouts for graphs. The question then arises – given an arbitrary graph, how can we produce a good drawing for that graph? This is called the *graph drawing problem* and has been studied extensively. Interestingly, while there are many good algorithms for drawing graphs, no one algorithm shines as “the” graph drawing algorithm. Every algorithm has its strengths and weaknesses, and many algorithms that work marvelously on certain graphs will produce poor layouts for other graphs. In this assignment, you'll learn about one particular type of algorithm called a *force-directed layout algorithm* and will get a chance to see its performance on a variety of graphs. In doing so, you'll cement your skills with the streams library and the STL `vector` class. Plus, you'll end up with an incredibly entertaining piece of software.

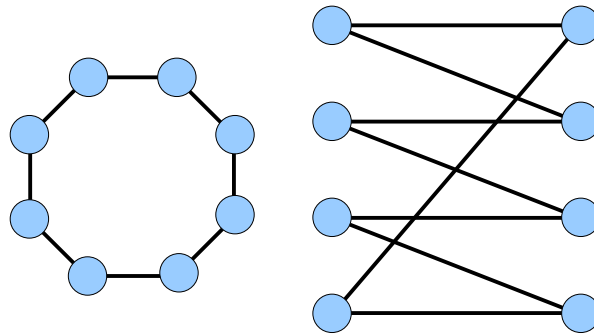
Graph Layout Heuristics

Before going into the details of how force-directed layouts work, we need to address the following question: how can a computer, which can only blindly crunch numbers, tell whether a particular graph drawing is aesthetically pleasing to its human masters? This question is both difficult to pose and difficult to answer – what one person finds intuitive might leave another baffled – and in this assignment we won't try to answer it directly. Instead, we will come up with a set of criteria that in general lead to nice graph layouts, then will design an algorithm to try to pick layouts meeting these criteria. This will not always result in ideal graph drawings, but will do a surprisingly good job laying out many graphs.

There are many heuristics that could be used to determine how good a graph drawing is. For example, we could try to minimize the number of arcs crossing one another, or try to maximize the symmetry of the drawing. In this assignment, however, we'll limit ourselves to the following two heuristics, which work remarkably well in practice:

将连接的节点彼此靠近。在布置图形时，最好将边连接的节点彼此靠近放置。该指标背后的想法是，如果连接的节点彼此靠近，读者可以专注于图形的某一部分，并在该区域看到图形的局部结构。例如，以下是同一图表的两个演绎版，其中左侧的图表具有彼此靠近放置的已连接节点，而右侧的已连接节点间距相距很远：

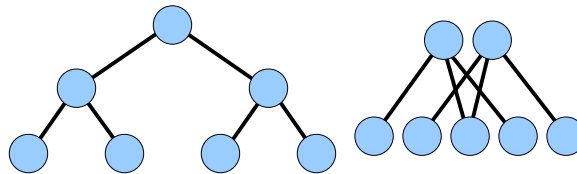
- **Position connected nodes near one another.** When laying out a graph, it is often a good idea to place nodes that are joined by an edge near one another. The idea behind this metric is that if connected nodes are near each other, a reader can focus on one part of the graph and see the local structure of the graph in that region. For example, below are two renditions of the same graph, where the graph on the left-hand side has connected nodes placed near each other and the right-hand side has connected nodes spaced far apart:



As you can see, the left-hand graph is much easier to interpret.

- **Maximize the distance between unconnected nodes.** If two unconnected nodes are placed near one another, the reader can be confused into thinking that they are somehow related when in fact there is no connection between them. For example, consider the two drawings below:

最大化未连接节点之间的距离。如果两个未连接的节点彼此靠近放置，读者可能会混淆认为它们以某种方式相关，而实际上它们之间没有联系。例如，考虑下面的两个图：在左侧图中，未连接的节点彼此隔开，从而可以深入了解图形的结构。在右侧，没有连接两个水平相邻的节点，并且图形的结构更难直观



In the left-hand graph, nodes that are not connected are spaced apart from one another, providing insight into the structure of the graph. In the right-hand side, no two horizontally adjacent nodes are connected, and the structure of the graph is much harder to intuit.

Now that we have a set of heuristics for elegant graphs, how do we go about placing nodes according to those heuristics? In general, this problem is difficult. The position of each node influences the position of each other node, so picking a layout that balances the heuristics requires solving a large, complicated system of equations.* Fortunately, there is a clever strategy that lets us avoid this complexity.

* Later on when we cover the actual math behind node placement, it's a fun exercise to think about solving the system of equations manually. This is very difficult because, as you'll see, the equations governing node

我们不是直接求解答案，而是从随机猜测开始，然后不断调整节点的位置以改进启发式方法。随着时间的推移，节点将达到平衡启发式的方法，我们最终会得到一个美观的图形绘图。该算法的关键步骤是引入某种方法来更新节点位置，为此，我们将从物理学中汲取灵感。在图形布局的每个步骤中，我们都会让节点相互施加力。这些力将推拉处于次优位置的节点，直到它们最终停在稳定的位置。因为我们希望未连接的节点彼此相距较远，所以我们将让每个节点用一定的力排斥其他节点。同样，由于我们希望连接的节点彼此靠近，因此我们将在 tract 的端点处使节点之间的每条边都位于其端点处。当这些力移动节点时，节点的位置将趋向于连接，其中每个节点上的净力最小；也就是说，当 Forces 之间存在平衡时，将未连接的节点隔开并保持在在一起的节点。

Rather than solving for the answer directly, we'll instead start off with a random guess, then continuously refine the positions of the nodes to improve upon the heuristics. Over time, the nodes will reach a positions that balance the heuristics, and we'll end up with an aesthetically pleasing graph drawing.

The key step in this algorithm is finding some way to update the node positions, and to do this we'll take a cue from physics. At each step of the graph layout, we'll have the nodes exert *forces* on one another. These forces will push and pull nodes that are in suboptimal positions until they eventually come to rest in a stable location. Because we want unconnected nodes to be far apart from one another, we'll have each node repel each other node with some force. Similarly, because we want connected nodes to remain near one another, we'll have each edge between nodes attract its endpoints. As these forces move the nodes around, the positions of the nodes will tend toward configurations where the net force on each node is minimized; that is, when there is a balance between the forces spacing out unconnected nodes and keeping together connected nodes.

The general skeleton of our algorithm is as follows:

```
Assign each node in the graph an initial location.
While the layout is not yet finished:
    Have each node exert a repulsive force on each other node.
    Have each edge exert an attractive force on its endpoints.
    Move the nodes according to the net force acting on them.
```

The details of each of these steps are quite customizable: we can initialize the positions of the nodes however we choose, decide when to stop based on multiple criteria, and use almost any function to determine the strengths of the attractive and repulsive forces between nodes. In this assignment, you'll implement one particular version of a force-directed layout algorithm, but I highly encourage you to try out your own variations; I've suggested several ideas at the end of this handout.

Let's now go over the specifics of how each of the above steps work.

Assigning initial node positions. There is no one “correct way” to initially lay out the nodes in the graph. Because the algorithm takes an initial guess and improves over time, pretty much any initial layout will do. In this assignment, however, you'll initially position the nodes so that they are evenly spaced apart on the unit circle. In particular, in a graph with n nodes, node k should be placed at

$$\left(\cos \frac{2\pi k}{n}, \sin \frac{2\pi k}{n} \right)$$

Here, angles are represented in radians. In C++, you can compute sine and cosine using the `sin` and `cos` functions exported by the `<cmath>` header file. There is no predefined C++ constant for π , but you should be fine with

```
const double kPi = 3.14159265358979323;
```

Determining whether to continue iterating. The heart of the force-directed algorithm is the iteration. If the iteration cuts off too early, then the nodes may not

positions are nonlinear.

have moved into good positions; if the iteration runs too long, then the computer will waste time trying to improve upon an already perfect layout. Although there are ways to automatically detect whether to continue or cut off the iteration,* in this assignment we'll adopt a simple approach – asking the user to control how long the algorithm runs. In particular, before running the algorithm, you should prompt the user for a number of seconds, then run the algorithm until that many seconds have elapsed.

In C++, you can retrieve the current time by using the `time` function, exported by `<ctime>`. The `time` function returns a value of type `time_t` which holds some unique value identifying the current time. In order to track how much time has elapsed in the simulation, you can use the `difftime` function. `difftime` takes as arguments two `time_t`s, then reports the number of seconds that have elapsed between the two time points. For example, the following illustrates one way to use `difftime` to measure how long a computation takes:

```
time_t startTime = time(NULL);

/* ... some complex operation ... */

double elapsedTime = difftime(time(NULL), startTime);
```

Here, the first line invokes the `time` function to get the start time, and the last line uses `difftime` to compute the difference in time between now and the start time.

Computing forces. The particular approach we will use to compute forces is based off of the *Fruchterman-Reingold algorithm*, an early but effective force-directed layout algorithm. In Fruchterman-Reingold, every node exerts a repulsive force on every other node that is inversely proportional to the distance between those nodes, and each arc exerts an attractive force on its endpoints proportional to the *square* of the distance between those nodes. This means that as connected nodes grow more distant to one another, the attractive force rises quickly and the repulsive force drops off, so connected nodes will have a tendency to “snap back” toward one another. Similarly, as the nodes draw increasingly close, the repulsive force grows rapidly while the attractive force diminishes, so the nodes will move away from each other. Only when the nodes are at a perfect distance from one another will the forces balance and the nodes cease to move.

To keep track of the net forces on each node, you'll maintain a Δx and Δy value for each node which stores the net forces on that node along the x and y axes. It's important to track both, since it's possible that a node might be repelled entirely vertically (in which case it will have a strong force in the y direction but no force in the x direction) or horizontally (strong force in the x direction, no force in the y direction). The net forces in each direction begin at zero, but will be adjusted by the interactions of each node with each other node.

我们将用于计算力的特定方法基于 Fruchterman-Reingold 算法，这是一种早期但有效的 force-directed 布局算法。在 Fruchterman-Reingold 中，每个节点都对其他每个节点施加一个排斥力，该排斥力与这些节点之间的距离成反比，并且每个圆弧对其端点施加的吸引力与这些节点之间距离的平方成正比。这意味着，随着连接的节点彼此之间的距离越来越远，吸引力迅速上升，排斥力下降，因此连接的节点将有相互“弹回”的趋势。同样，随着节点越来越靠近，排斥力迅速增加，而吸引力减小，因此节点将彼此远离。只有当节点彼此处于完美距离时，力才会平衡，节点才会停止移动。

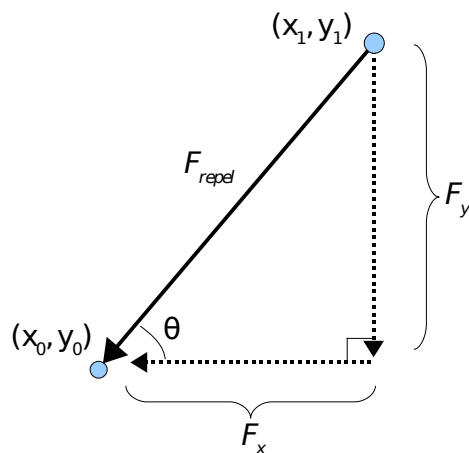
- * One common approach is to compute the *kinetic energy* of the system, which is given by the sum of the squares of the Δx and Δy terms of each of the nodes. When the kinetic energy drops below some particular threshold, the algorithm can assume that the graph is more or less in its final configuration and can stop the iteration.

The first source of force acting on each node is the repulsive force exerted by every node against every other node. For each pair of nodes (x_0, y_0) and (x_1, y_1) , the magnitude of the repulsive force F_{repel} between these nodes is

$$F_{repel} = \frac{k_{repel}}{\sqrt{(x_1 - x_0)^2 + (y_1 - y_0)^2}}$$

Where k_{repel} is a constant that controls the strength of the repulsive attraction. If the magnitude of this constant increases, then nodes repel each other more strongly; if it has a small magnitude, then nodes hardly repel each other at all. I advise using a value of 10^{-3} for this constant, but you are free to experiment with this value if you wish.

Once you have computed the magnitude of the repulsive force, you will need to determine how much of that force is in the y direction and how much of it is in the x direction. To see how this force splits up, consider the following diagram:



Here, F_x and F_y are the forces in the x and y directions exerted on the node (x_0, y_0) . Using some simple trigonometry, we get that

$$\begin{aligned} F_{x_0} &= -F_{repel} \cos \theta \\ F_{y_0} &= -F_{repel} \sin \theta \end{aligned}$$

By Newton's laws, the force exerted against the node (x_1, y_1) are thus

$$\begin{aligned} F_{x_1} &= +F_{repel} \cos \theta \\ F_{y_1} &= +F_{repel} \sin \theta \end{aligned}$$

Here, we've been using the angle θ to represent the angle indicated in the above drawing. Again, simple trigonometry tells us that

$$\theta = \tan^{-1} \frac{y_1 - y_0}{x_1 - x_0}$$

In C++, you can compute this arctangent using the `atan2` function, also in `<cmath>`. `atan2` takes in two arguments – the first representing $y_1 - y_0$ and the second $x_1 - x_0$ – and returns the value of the above expression in radians. For example:

在 C++ 中，您可以使用 `atan2` 函数计算此反正切函数，同样在 `<cmath>` 接受两个参数（first 表示 $y_1 - y_0$ ，第二个 $x_1 - x_0$ ）并返回上述表达式的值（以弧度为单位）。例如：

```
double theta = atan2(y1 - y0, x1 - x0);
```

To summarize, the logic for computing repulsive forces is as follows:

```
For each pair of nodes (x0, y0), (x1, y1):
    Compute F_repel = k_repel / sqrt((y1 - y0)^2 + (x1 - x0)^2)
    Compute theta = atan2(y1 - y0, x1 - x0)
    Δx0 -= F_repel cos(theta)
    Δy0 -= F_repel sin(theta)
    Δx1 += F_repel cos(theta)
    Δy1 += F_repel sin(theta)
```

The second source of force acting on each node is the attractive forces between nodes joined together by edges. In this case, the attractive force $F_{attract}$ is proportional to the square of the distance between the nodes:

$$F_{attract} = k_{attract}((x_1 - x_0)^2 + (y_1 - y_0)^2)$$

Again, $k_{attract}$ is a constant controlling the strength of the attractive force. As with k_{repel} I suggest using the value 10^{-3} , but you should feel free to experiment with this value as well.

Using logic similar to the above reasoning with repulsive forces, we can compute how this force divides over the x and y components as follows:

```
For each edge:
    Let the first endpoint be (x0, y0)
    Let the second endpoint be (x1, y1)
    Compute F_attract = k_attract * ((y1 - y0)^2 + (x1 - x0)^2)
    Compute theta = atan2(y1 - y0, x1 - x0)
    Δx0 += F_attract cos(theta) // Note that this is a += and not a -=!
    Δy0 += F_attract sin(theta)
    Δx1 -= F_attract cos(theta) // Note that this is a -= and not a +=!
    Δy1 -= F_attract sin(theta)
```

Moving Nodes According to the Forces. Once you've computed the net Δx and Δy for each node, moving the nodes is an easy step – simply increment each node's x coordinate by its Δx and each node's y coordinate by its Δy . Note that in a true physical simulation the forces on each object would change the *velocity* of the object rather than directly modifying its position, but for our simplified example changing position alone is sufficient. If you'd like to experiment with each node having a velocity and a position, feel free to do so.

The Assignment

Your assignment is to implement a simple program which reads in a graph from a file, then runs the force-directed layout algorithm described above to find an appealing layout for the graph. In particular, your program should do the following:

1. Prompt the user for the name of a file containing the graph to visualize. (The graph file format is discussed below.)

2. Prompt the user for the number of seconds to run the algorithm, which should be positive.
3. Place each node into its initial configuration.
- 当指定的秒数尚未过去时：1. 计算每个节点上的净力。2. 按指定的数量移动每个节点。3. 使用提供的库显示图形的当前状态
4. While the specified number of seconds has not elapsed:
 1. Compute the net forces on each node.
 2. Move each node by the specified amount.
 3. Display the current state of the graph using the provided library.
5. (optional) Ask the user if they want to display another graph and loop accordingly.

In the provided starter code, I have provided you a header file, `SimpleGraph.h`, which exports a set of types for representing a graph. In particular, you're given:

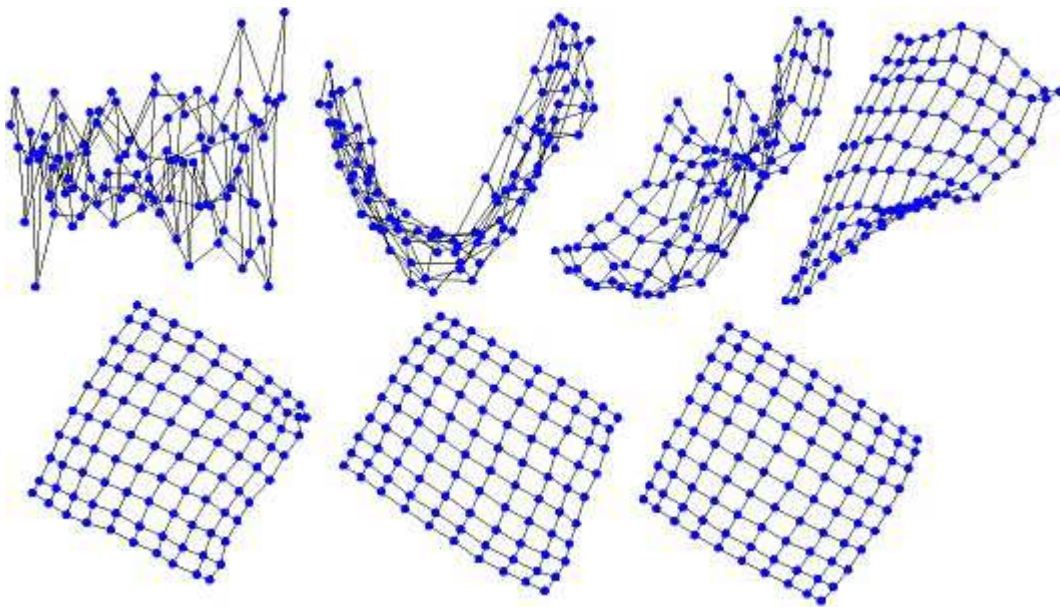
- `Node`, a struct representing a node in a graph. It simply stores an x and y position.
- `SimpleGraph`, which stores two vectors, one of `Nodes` and one of `Edges`.
- `Edge`, a struct representing an edge in the graph. Each `Edge` has two fields, `start` and `end`, which correspond to the indexes of the edge's endpoints in the `Node` vector.

The provided starter code also contains many sample graphs you can run your program on. Each graph is represented as a file, where the first line contains the number of nodes and each remaining line defines an edge. For example, here is a graph file where the nodes and edges represent the corners and edges of a cube:

```
8
0 1
1 2
2 3
3 0
4 5
5 6
6 7
7 4
0 4
1 5
2 6
3 7
```

Here, the first line of the file indicates that there are eight nodes in the graph, and the remainder of the lines consist of two numbers denoting which nodes are connected by edges. For example, the line 0 1 indicates that there is an edge from node 0 to node 1, the line 3 7 that there is an edge from node 3 to node 7, etc. You can assume that every file the user opens is well-formed, though if you wanted to make this program more resilient you may want to add some code to check that this is the case.

The code in SimpleGraph.h also contains two functions: InitGraphVisualizer, which accepts a SimpleGraph sets up the internal state of the visualizer, and DrawGraph, which accepts a SimpleGraph and displays it on screen. At the start of your program, you should call the InitGraph, and after each iteration of the main algorithm should call DrawGraph on the current graph configuration. This will let you watch as the computer incrementally finds a good layout for the graph. For example, here is a time-lapse view of the computer drawing a grid graph (a 10 x 10 array of nodes connected to their neighbors in the cardinal directions), done using a slight modification to the base algorithm:

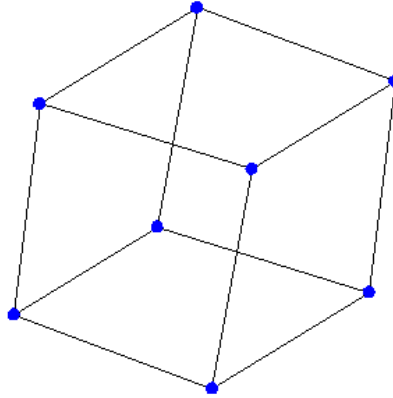


When writing this program, **you should not use any of the CS106B/X libraries**. That is, you should not use anything from the `strlib.h`, `scanner.h`, `simpio.h`, `filelib.h` headers. However, you are free to use anything off of the CS106L course website, including the implementations of the functions contained in these headers. This may seem like an arbitrary restriction, but the idea is to get you to write your entire program using purely portable C++ code.

Task Breakdown

Although this handout is fairly lengthy, *don't panic* – you don't need to write very much code to complete this assignment. To help you get started, I've constructed one possible breakdown of the required tasks. You should feel free to implement the assignment in any way you see fit, so don't worry if this ordering sounds unusual.

- *Implement code to read a graph from disk.* As a first step, I suggest writing a set of functions that will prompt the user for the name of a graph file and then read that file from disk. The actual file reading should not be particularly difficult, and depending on how you go about reading the file it may actually require more code to prompt the user for a valid filename than to actually read in the graph. You should be sure to use `getline` (or a wrapper function) to read input from the user.
- *Implement the logic to initially position the nodes.* Before you can run the force-directed algorithm, you will need to position all of the nodes in the graph in a circle. I suggest getting this step working before writing the iterative part of the algorithm since it's easy to check whether it's working. In particular, you can always call `DrawGraph` and check whether all of the nodes are arranged in a circle.
- *Implement the force-directed layout algorithm.* This is the core of the assignment, but fortunately the code necessary to get it working is not too daunting. You will ultimately need to prompt the user for how long to run the algorithm, but initially I suggest just putting the iteration in a `while (true)` loop and just letting the algorithm run forever. As a test of whether your code is working, if you run the algorithm on the graph `10line`, your algorithm should eventually end up arranging the points in a straight line. Similarly, running the algorithm on the file `cube` should arrange the points in a way that looks like a 3D perspective drawing of a cube, as shown here:



- *Implement the code to time the simulation.* Once you have all the rest of the program working, add in the code to prompt the user for the length of time to run the algorithm, and then update your iteration to terminate once that amount of time has passed. Feel free to use the `GetInteger` code from the CS106L website to read a number of seconds from the user.

Advice, Tips, and Tricks

Here are a few specific pointers that might make your life a lot easier as you go through this assignment:

- *Don't hesitate to ask questions!* **The point of this assignment is to give you a chance to play around with C++ and build cool software, not to punish you for not understanding a particular library or language detail.** If you're having trouble understanding the starter code, run into inexplicable runtime errors, or can't seem to get some part of the assignment working, please send me an email, talk to me after lecture, or come to office hours. I genuinely love this material and want to help you learn it, so don't hesitate to ask questions if you need to.
- *Make sure to read the graph files correctly.* When reading in the graph data from each file, make sure that you *don't* write the loop to read the edges as follows:

```
while (!infile.fail()) { // Error: Don't do this!!
    /* ... read another edge ... */
}
```

This loop structure will incorrectly detect when you have read all of the lines from the file, since if in the body of the loop you read data and find that none exists, the error will not be detected until the current loop iteration finishes. This will cause your program to add garbage data to the edge list. To avoid this, use a different loop structure, such as the one suggested in Chapter 3 of the online course reader.

- *Be careful when reading input from the user.* As mentioned in class, directly reading data from `cin` is dangerous and can completely break input in the program. You should instead use a wrapper around `cin` along the lines of the

`GetLine` or `GetInteger` functions we wrote in class. If you'd like to use lecture code in your program, that's completely fine, but you should be sure to cite it.

- **DO NOT** make copies of your `SimpleGraph`. It will mess up the graphics and give you a whole mess of problems. You should have one copy that is passed in as a parameter everywhere

Extensions

This assignment implements one of many algorithms that can be used to draw graphs. Here are a few possible extensions you may want to experiment with. I hope that you try at least one of these changes out, since most of them require only a few lines of code and can yield noticeable changes in the resulting graphs:

1. *Change the relative strength of the attractive and repulsive forces.* The aforementioned algorithm uses two constants, k_{repel} and $k_{attract}$, which control how strong the attractive and repulsive forces are. My suggestion is to set both of these values to 10^{-3} , but there's no reason that they stay at this value, or that they even stay in a 1:1 ratio. Try changing these values independently of one another. What do you notice happening to the graph layouts? Do any values cause the algorithm to completely fail to work?
2. *Add random perturbations.* One potential problem with this force-directed algorithm is that the graph can get stuck in a *local minimum*, a configuration in which all of the forces are balanced but which is not the optimal configuration. Often, this manifests itself in a situation in which if any of the nodes were to move even a slight amount, the graph would collapse into a much better configuration. For example, consider a graph in which three nodes are each connected to one another in a triangle. One possible layout for the graph would be to put them all in a straight line. If this happens, then the repulsive and attractive forces on the nodes would always push and pull along that line, and so the nodes would always be collinear. However, if one of the nodes were to get bumped slightly out of place, then the forces between the nodes would no longer be along a line and the nodes will quickly arrange themselves in a triangle. Try modifying the current algorithm by giving each node a slight "push" in a random direction at each step of the process. Does this result in better layouts in any cases?
3. *Add node velocities.* In this particular force-directed algorithm, the amount each node moves on each iteration is completely independent of the amount that the node moved on the previous steps. That is, if a node moves a great distance on one step, it has no "memory" of this and on the next step it will move based solely on the current configuration. In an actual physical system, each node would have an associated velocity which would keep it moving in a particular direction until the net forces slowed it down. Consider modifying the algorithm to incorporate information about the previous iteration's velocities into the current step. One way to do this would be to track the Δx and Δy of each object from one iteration to the next, rather than resetting it to zero each time. What do you notice about the graph layouts?

4. *Add penalties for crossing edges.* One aspect of graph drawings we did not take into account when computing forces is the number of edges that are crossing in a particular drawing. A graph drawing without crossings is more likely to be aesthetically pleasing than a graph drawing with crossings. Modify the algorithm to detect these crossings and adjust the layout accordingly. One common approach for doing this is to pretend that there is an invisible node at the center of each edge that exerts a repulsive force against the center of each other edge, thus pushing edges apart from one another.
5. *Add penalties for low resolution.* The *resolution* of a graph drawing is the smallest angle between any two edges incident to a single node. Graphs that have low resolution can be hard to understand, since the edges emanating from a source node will all be bunched together. Modify the algorithm to try to avoid low resolution. One way to do this might be to add a repulsive force between the endpoints of arcs that have a small angle between them.
6. *Generalize the definition of an attractive force.* In our current algorithm, only nodes directly connected by edges have an attractive force between them. The rationale behind this was that nodes that are connected to one another ought to be close to each other. However, given this same reasoning, it also makes sense to have nodes that are *almost* connected to one another exert a force on each other. For example, if node A is connected to node B and node B is connected to node C, then A and C are likely to be near each other in the final graph layout. Similarly, if C is then connected to D, perhaps A and D should be near each other as well. Update the algorithm so that nodes that are more than one hop away from each other still exert an attractive force. One option might be to have each node exert an attractive force on each other node proportional to how “close” they are to one another in the initial graph.

There are a whole host of extensions you could try out, so don't be limited just by these. If you come up with something impressive, I'll gladly show it off to the rest of the class.

Deliverables

To submit the assignment, please submit your assignment on paperless (located at paperless.stanford.edu). Then pat yourself on the back – you've just completed the first assignment of the quarter!

Good luck!