

Lukas Steindl

All the scripts and notes i took before github got cool.

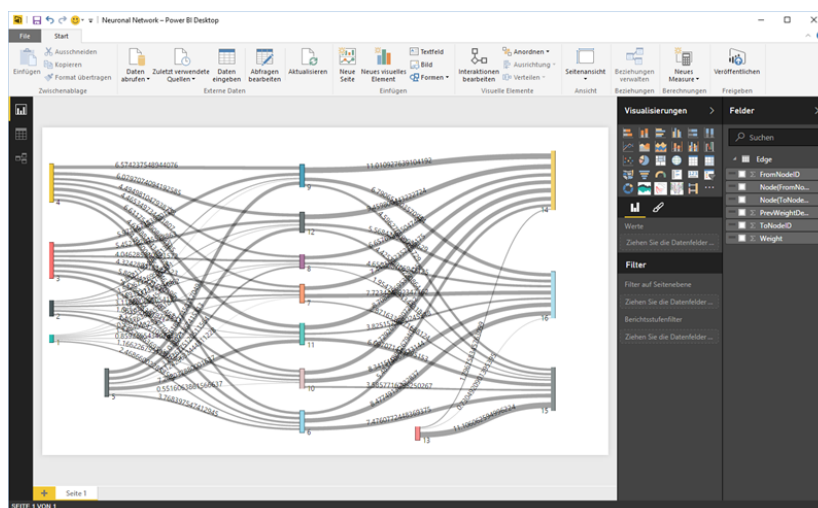
Uncategorized

# Neural Networks in T-SQL

*Posted On February 28, 2016*

it might not be the fastest option to train a neural network but it seems to be a quite elegant approach to use T-SQL to implement the backpropagation algorithm. In order to learn and better understand the algorithm I decided to port the C# neural network example from Dr. James McCaffrey(MSR) to Sql Server. The goal of the network is to classify three different types of flowers based on four input features (sepal length, height etc.).

This is how the trained model looks like in the end:



(Its a nice sideeffect that you can easily visualize the network using Power BI when the

Search this site Search

## Recent Posts

How to Call a Machine Learning Model deployed with azure ML from Python

Remove all Jobs from an Azure Batch Account with Powershell

How to get the status of an Azure Batch Job with Node.js

Submit a simple Job to Azure Batch with Node js (minimal example)

Connect Node.js to SQL Azure with Tedious

## Recent Comments

Malcom on SQL Server 2016 (CTP3) R Integration

data is stored in SQL Server. )

The high level steps to train a neural network model are described briefly first:

1. Normalize the input data
2. Define the network structure (Number of Input Nodes, Number of Output Nodes are given by the problem, Number of Hidden nodes are up to you.)
3. Take a random training example and set the input and desired output state
4. Calculate the error for the training example
5. Change the weights so that the error decreases
6. Repeat Steps 3 to 5 until the error on the training data goes below a threshold or stop after a finite number of training iterations

You will find the complete executable script at the end of this post. Here are some of the highlights I wanted to point out.

### Doing Step 1 in T-sql is just a single line of code:

```
Insert Into NormalizedIrisData
Select (x1-mue_x1)/std_x1,(x2-mue_x2)/std_x2,(x3-mue_x3)/std_x3, (x4-
mue_x4)/std_x4, class
from IrisData i cross join (
Select AVG(x1) as mue_x1, STDEVP(x1) as std_x1, AVG(x2) as mue_x2,
STDEVP(x2) as std_x2,
AVG(x3) as mue_x3, STDEVP(x3) as std_x3, AVG(x4) as mue_x4, STDEVP(x4)
as std_x4
from IrisData) d
```

Darron on SQL Server  
2016 (CTP3) R  
Integration

Fausto on SQL Server  
2016 (CTP3) R  
Integration

Sylvester on SQL Server  
2016 (CTP3) R  
Integration

Haley on SQL Server  
2016 (CTP3) R  
Integration

## Archives

October 2019

June 2018

May 2018

April 2018

March 2018

June 2017

June 2016

May 2016

April 2016

February 2016

December 2015

November 2015

October 2015

## Step 2 is simple using two tables you can encode your network structure:

Create Table Node (ID int primary key identity, NodeType char(2), WeightedInputSum float, ActivationOutput float, ExpectedOutput float, Delta float, Gradient float)

Create Table Edge (FromNodeID int references Node, ToNodeID int references Node, [Weight] float, PrevWeightDelta float)

```
--3 input Nodes
Insert Into Node VALUES ('I',null,null,null,null,null),('I',null,null,null,null,null),
('I',null,null,null,null,null),('I',null,null,null,null,null),('BI',null,1,null,null,null)

--7 hidden Nodes
Insert Into Node VALUES ('H',null,null,null,null,null),
('H',null,null,null,null,null),('H',null,null,null,null,null),
('H',null,null,null,null,null),('H',null,null,null,null,null),
('H',null,null,null,null,null),('H',null,null,null,null,null),('BH',null,1,null,null,null)

--3 output nodes
Insert Into Node VALUES ('O',null,null,null,null,null),
('O',null,null,null,null,null),('O',null,null,null,null,null)
```

## Step 3 just loads a random training example into the input nodes and sets the desired output at the output nodes

```
Update InputNodes set ActivationOutput = (Select x1 from TrainingData where i
= @SampleID) where InputNodes.ID = 1
Update InputNodes set ActivationOutput = (Select x2 from TrainingData where i
= @SampleID) where InputNodes.ID = 2
Update InputNodes set ActivationOutput = (Select x3 from TrainingData where i
= @SampleID) where InputNodes.ID = 3
Update InputNodes set ActivationOutput = (Select x4 from TrainingData where i
= @SampleID) where InputNodes.ID = 4
Update OutputNodes set ExpectedOutput = (Select class1 from TrainingData
where i = @SampleID) where OutputNodes.ID = 14
Update OutputNodes set ExpectedOutput = (Select class2 from TrainingData
where i = @SampleID) where OutputNodes.ID = 15
Update OutputNodes set ExpectedOutput = (Select class3 from TrainingData
where i = @SampleID) where OutputNodes.ID = 16
```

## Step 4 passes the inputs through the network and calculates the error

```
Update h set h.WeightedInputSum = x.WeightedInputSum
from HiddenNodes h
join (Select ToNodeID, SUM(i.ActivationOutput*e.Weight) as
```

June 2015

July 2014

February 2014

November 2013

June 2013

April 2013

## Categories

Uncategorized

## Meta

Log in

Entries feed

Comments feed

WordPress.org

```

'WeightedInputSum' from InputNodes i join Edge e on i.ID = e.FromNodeID
group by ToNodeID) x on h.ID = x.ToNodeID

--calculate activation of the hidden nodes using the hyperbolic tangent activation
function:
Update HiddenNodes set ActivationOutput = dbo.tanh(WeightedInputSum)
where NodeType = 'H'

-- calculate the weighted input sum of the output nodes
Update o set o.WeightedInputSum = x.WeightedInputSum
from OutputNodes o
join (Select ToNodeID, SUM(h.ActivationOutput*e.Weight) as
'WeightedInputSum' from HiddenNodes h join Edge e on h.ID = e.FromNodeID
group by ToNodeID) x on o.ID = x.ToNodeID

--calculate activation of the output nodes using Soft Max activation function:
declare @MaxOutput float
declare @Scale float
Select @MaxOutput = Max(WeightedInputSum) from OutputNodes
Select @Scale = SUM(EXP(WeightedInputSum - (@MaxOutput))) from
OutputNodes
Update OutputNodes set ActivationOutput = EXP(WeightedInputSum-
@MaxOutput)/@Scale
--Calculate the error for this one training example:
Update OutputNodes set Delta = ExpectedOutput - ActivationOutput

```

**Step 5 calculates the change of the error for the change of a weight and changes the weight so that the error gets smaller. this is the core of the backpropagation algorithm.**

```

--Calculate OutputLayer Gradient = (SoftMax Derivative * Delta)
Update OutputNodes set Gradient = (1-ActivationOutput)*ActivationOutput *
Delta

--Calculate HiddenLayer Deltas (= Sum of the weighted Output Layer gradients)
Update h set Delta = x.Delta
from HiddenNodes h join (
Select e.FromNodeID, SUM(o.Gradient*e.Weight) as 'Delta'
from OutputNodes o join Edge e on o.ID = e.ToNodeID group by
e.FromNodeID) x
on h.ID = x.FromNodeID

```

```

--calculate HiddenLayer Gradient = (tanh Derivative * Delta)
Update HiddenNodes set Gradient = (1-ActivationOutput)*
(1+ActivationOutput) * Delta

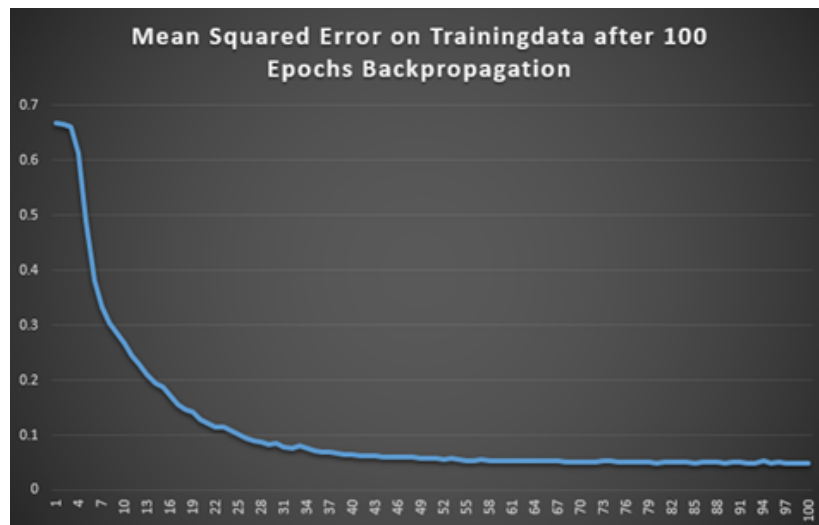
-- Update weights between input and hidden layer
Update e set PrevWeightDelta = @learningrate * h.Gradient*
i.ActivationOutput,
[Weight] = [Weight] * 0.9999 + @learningrate * h.Gradient* i.ActivationOutput
+ @momentum * PrevWeightDelta
from HiddenNodes h join Edge e on e.ToNodeID = h.ID join InputNodes i on
e.FromNodeID = i.ID

--Update weights between hidden and output layer ->
Update e set PrevWeightDelta = @learningrate * o.Gradient*
h.ActivationOutput,
[Weight] = [Weight]* 0.9999 + @learningrate * o.Gradient* h.ActivationOutput
+ @momentum * PrevWeightDelta
from HiddenNodes h join Edge e on e.FromNodeID = h.ID join OutputNodes o
on e.ToNodeID = o.ID

```

**Thats it!**

**Visualizing the Training Error shows a smooth learning curve:**



**Here is the entire Script for your convenience:**

[use master](#)

GO

Alter Database NeuralNetwork set single\_user with rollback immediate

go

Drop Database NeuralNetwork

GO

Create Database NeuralNetwork

go

use NeuralNetwork

GO

Create Table IrisData (x1 float, x2 float, x3 float, x4 float, class varchar(255))

GO

Insert Into IrisData Values (5.1,3.5,1.4,0.2,'Iris-setosa')

Insert Into IrisData Values (4.9,3.0,1.4,0.2,'Iris-setosa')

Insert Into IrisData Values (4.7,3.2,1.3,0.2,'Iris-setosa')

Insert Into IrisData Values (4.6,3.1,1.5,0.2,'Iris-setosa')

Insert Into IrisData Values (5.0,3.6,1.4,0.2,'Iris-setosa')

Insert Into IrisData Values (5.4,3.9,1.7,0.4,'Iris-setosa')

Insert Into IrisData Values (4.6,3.4,1.4,0.3,'Iris-setosa')

Insert Into IrisData Values (5.0,3.4,1.5,0.2,'Iris-setosa')

Insert Into IrisData Values (4.4,2.9,1.4,0.2,'Iris-setosa')

Insert Into IrisData Values (4.9,3.1,1.5,0.1,'Iris-setosa')

Insert Into IrisData Values (5.4,3.7,1.5,0.2,'Iris-setosa')

Insert Into IrisData Values (4.8,3.4,1.6,0.2,'Iris-setosa')

Insert Into IrisData Values (4.8,3.0,1.4,0.1,'Iris-setosa')

Insert Into IrisData Values (4.3,3.0,1.1,0.1,'Iris-setosa')

Insert Into IrisData Values (5.8,4.0,1.2,0.2,'Iris-setosa')

Insert Into IrisData Values (5.7,4.4,1.5,0.4,'Iris-setosa')

Insert Into IrisData Values (5.4,3.9,1.3,0.4,'Iris-setosa')

Insert Into IrisData Values (5.1,3.5,1.4,0.3,'Iris-setosa')

Insert Into IrisData Values (5.7,3.8,1.7,0.3,'Iris-setosa')

Insert Into IrisData Values (5.1,3.8,1.5,0.3,'Iris-setosa')

Insert Into IrisData Values (5.4,3.4,1.7,0.2,'Iris-setosa')

Insert Into IrisData Values (5.1,3.7,1.5,0.4,'Iris-setosa')

Insert Into IrisData Values (4.6,3.6,1.0,0.2,'Iris-setosa')

Insert Into IrisData Values (5.1,3.3,1.7,0.5,'Iris-setosa')

Insert Into IrisData Values (4.8,3.4,1.9,0.2,'Iris-setosa')

Insert Into IrisData Values (5.0,3.0,1.6,0.2,'Iris-setosa')

Insert Into IrisData Values (5.0,3.4,1.6,0.4,'Iris-setosa')

Insert Into IrisData Values (5.2,3.5,1.5,0.2,'Iris-setosa')

Insert Into IrisData Values (5.2,3.4,1.4,0.2,'Iris-setosa')

Insert Into IrisData Values (4.7,3.2,1.6,0.2,'Iris-setosa')

Insert Into IrisData Values (4.8,3.1,1.6,0.2,'Iris-setosa')

Insert Into IrisData Values (5.4,3.4,1.5,0.4,'Iris-setosa')

Insert Into IrisData Values (5.2,4.1,1.5,0.1,'Iris-setosa')

Insert Into IrisData Values (5.5,4.2,1.4,0.2,'Iris-setosa')

```
Insert Into IrisData Values (4.9,3.1,1.5,0.2,'Iris-setosa')
Insert Into IrisData Values (5.0,3.2,1.2,0.2,'Iris-setosa')
Insert Into IrisData Values (5.5,3.5,1.3,0.2,'Iris-setosa')
Insert Into IrisData Values (4.9,3.6,1.4,0.1,'Iris-setosa')
Insert Into IrisData Values (4.4,3.0,1.3,0.2,'Iris-setosa')
Insert Into IrisData Values (5.1,3.4,1.5,0.2,'Iris-setosa')
Insert Into IrisData Values (5.0,3.5,1.3,0.3,'Iris-setosa')
Insert Into IrisData Values (4.5,2.3,1.3,0.3,'Iris-setosa')
Insert Into IrisData Values (4.4,3.2,1.3,0.2,'Iris-setosa')
Insert Into IrisData Values (5.0,3.5,1.6,0.6,'Iris-setosa')
Insert Into IrisData Values (5.1,3.8,1.9,0.4,'Iris-setosa')
Insert Into IrisData Values (4.8,3.0,1.4,0.3,'Iris-setosa')
Insert Into IrisData Values (5.1,3.8,1.6,0.2,'Iris-setosa')
Insert Into IrisData Values (4.6,3.2,1.4,0.2,'Iris-setosa')
Insert Into IrisData Values (5.3,3.7,1.5,0.2,'Iris-setosa')
Insert Into IrisData Values (5.0,3.3,1.4,0.2,'Iris-setosa')
Insert Into IrisData Values (7.0,3.2,4.7,1.4,'Iris-versicolor')
Insert Into IrisData Values (6.4,3.2,4.5,1.5,'Iris-versicolor')
Insert Into IrisData Values (6.9,3.1,4.9,1.5,'Iris-versicolor')
Insert Into IrisData Values (5.5,2.3,4.0,1.3,'Iris-versicolor')
Insert Into IrisData Values (6.5,2.8,4.6,1.5,'Iris-versicolor')
Insert Into IrisData Values (5.7,2.8,4.5,1.3,'Iris-versicolor')
Insert Into IrisData Values (6.3,3.3,4.7,1.6,'Iris-versicolor')
Insert Into IrisData Values (4.9,2.4,3.3,1.0,'Iris-versicolor')
Insert Into IrisData Values (6.6,2.9,4.6,1.3,'Iris-versicolor')
Insert Into IrisData Values (5.2,2.7,3.9,1.4,'Iris-versicolor')
Insert Into IrisData Values (5.0,2.0,3.5,1.0,'Iris-versicolor')
Insert Into IrisData Values (5.9,3.0,4.2,1.5,'Iris-versicolor')
Insert Into IrisData Values (6.0,2.2,4.0,1.0,'Iris-versicolor')
Insert Into IrisData Values (6.1,2.9,4.7,1.4,'Iris-versicolor')
Insert Into IrisData Values (5.6,2.9,3.6,1.3,'Iris-versicolor')
Insert Into IrisData Values (6.7,3.1,4.4,1.4,'Iris-versicolor')
Insert Into IrisData Values (5.6,3.0,4.5,1.5,'Iris-versicolor')
Insert Into IrisData Values (5.8,2.7,4.1,1.0,'Iris-versicolor')
Insert Into IrisData Values (6.2,2.2,4.5,1.5,'Iris-versicolor')
Insert Into IrisData Values (5.6,2.5,3.9,1.1,'Iris-versicolor')
Insert Into IrisData Values (5.9,3.2,4.8,1.8,'Iris-versicolor')
Insert Into IrisData Values (6.1,2.8,4.0,1.3,'Iris-versicolor')
Insert Into IrisData Values (6.3,2.5,4.9,1.5,'Iris-versicolor')
Insert Into IrisData Values (6.1,2.8,4.7,1.2,'Iris-versicolor')
Insert Into IrisData Values (6.4,2.9,4.3,1.3,'Iris-versicolor')
Insert Into IrisData Values (6.6,3.0,4.4,1.4,'Iris-versicolor')
Insert Into IrisData Values (6.8,2.8,4.8,1.4,'Iris-versicolor')
Insert Into IrisData Values (6.7,3.0,5.0,1.7,'Iris-versicolor')
Insert Into IrisData Values (6.0,2.9,4.5,1.5,'Iris-versicolor')
Insert Into IrisData Values (5.7,2.6,3.5,1.0,'Iris-versicolor')
Insert Into IrisData Values (5.5,2.4,3.8,1.1,'Iris-versicolor')
Insert Into IrisData Values (5.5,2.4,3.7,1.0,'Iris-versicolor')
Insert Into IrisData Values (5.8,2.7,3.9,1.2,'Iris-versicolor')
```

```
Insert Into IrisData Values (6.0,2.7,5.1,1.6,'Iris-versicolor')
Insert Into IrisData Values (5.4,3.0,4.5,1.5,'Iris-versicolor')
Insert Into IrisData Values (6.0,3.4,4.5,1.6,'Iris-versicolor')
Insert Into IrisData Values (6.7,3.1,4.7,1.5,'Iris-versicolor')
Insert Into IrisData Values (6.3,2.3,4.4,1.3,'Iris-versicolor')
Insert Into IrisData Values (5.6,3.0,4.1,1.3,'Iris-versicolor')
Insert Into IrisData Values (5.5,2.5,4.0,1.3,'Iris-versicolor')
Insert Into IrisData Values (5.5,2.6,4.4,1.2,'Iris-versicolor')
Insert Into IrisData Values (6.1,3.0,4.6,1.4,'Iris-versicolor')
Insert Into IrisData Values (5.8,2.6,4.0,1.2,'Iris-versicolor')
Insert Into IrisData Values (5.0,2.3,3.3,1.0,'Iris-versicolor')
Insert Into IrisData Values (5.6,2.7,4.2,1.3,'Iris-versicolor')
Insert Into IrisData Values (5.7,3.0,4.2,1.2,'Iris-versicolor')
Insert Into IrisData Values (5.7,2.9,4.2,1.3,'Iris-versicolor')
Insert Into IrisData Values (6.2,2.9,4.3,1.3,'Iris-versicolor')
Insert Into IrisData Values (5.1,2.5,3.0,1.1,'Iris-versicolor')
Insert Into IrisData Values (5.7,2.8,4.1,1.3,'Iris-versicolor')
Insert Into IrisData Values (6.3,3.3,6.0,2.5,'Iris-virginica')
Insert Into IrisData Values (5.8,2.7,5.1,1.9,'Iris-virginica')
Insert Into IrisData Values (7.1,3.0,5.9,2.1,'Iris-virginica')
Insert Into IrisData Values (6.3,2.9,5.6,1.8,'Iris-virginica')
Insert Into IrisData Values (6.5,3.0,5.8,2.2,'Iris-virginica')
Insert Into IrisData Values (7.6,3.0,6.6,2.1,'Iris-virginica')
Insert Into IrisData Values (4.9,2.5,4.5,1.7,'Iris-virginica')
Insert Into IrisData Values (7.3,2.9,6.3,1.8,'Iris-virginica')
Insert Into IrisData Values (6.7,2.5,5.8,1.8,'Iris-virginica')
Insert Into IrisData Values (7.2,3.6,6.1,2.5,'Iris-virginica')
Insert Into IrisData Values (6.5,3.2,5.1,2.0,'Iris-virginica')
Insert Into IrisData Values (6.4,2.7,5.3,1.9,'Iris-virginica')
Insert Into IrisData Values (6.8,3.0,5.5,2.1,'Iris-virginica')
Insert Into IrisData Values (5.7,2.5,5.0,2.0,'Iris-virginica')
Insert Into IrisData Values (5.8,2.8,5.1,2.4,'Iris-virginica')
Insert Into IrisData Values (6.4,3.2,5.3,2.3,'Iris-virginica')
Insert Into IrisData Values (6.5,3.0,5.5,1.8,'Iris-virginica')
Insert Into IrisData Values (7.7,3.8,6.7,2.2,'Iris-virginica')
Insert Into IrisData Values (7.7,2.6,6.9,2.3,'Iris-virginica')
Insert Into IrisData Values (6.0,2.2,5.0,1.5,'Iris-virginica')
Insert Into IrisData Values (6.9,3.2,5.7,2.3,'Iris-virginica')
Insert Into IrisData Values (5.6,2.8,4.9,2.0,'Iris-virginica')
Insert Into IrisData Values (7.7,2.8,6.7,2.0,'Iris-virginica')
Insert Into IrisData Values (6.3,2.7,4.9,1.8,'Iris-virginica')
Insert Into IrisData Values (6.7,3.3,5.7,2.1,'Iris-virginica')
Insert Into IrisData Values (7.2,3.2,6.0,1.8,'Iris-virginica')
Insert Into IrisData Values (6.2,2.8,4.8,1.8,'Iris-virginica')
Insert Into IrisData Values (6.1,3.0,4.9,1.8,'Iris-virginica')
Insert Into IrisData Values (6.4,2.8,5.6,2.1,'Iris-virginica')
Insert Into IrisData Values (7.2,3.0,5.8,1.6,'Iris-virginica')
Insert Into IrisData Values (7.4,2.8,6.1,1.9,'Iris-virginica')
Insert Into IrisData Values (7.9,3.8,6.4,2.0,'Iris-virginica')
```



```

Insert Into IrisData Values (6.4,2.8,5.6,2.2,'Iris-virginica')
Insert Into IrisData Values (6.3,2.8,5.1,1.5,'Iris-virginica')
Insert Into IrisData Values (6.1,2.6,5.6,1.4,'Iris-virginica')
Insert Into IrisData Values (7.7,3.0,6.1,2.3,'Iris-virginica')
Insert Into IrisData Values (6.3,3.4,5.6,2.4,'Iris-virginica')
Insert Into IrisData Values (6.4,3.1,5.5,1.8,'Iris-virginica')
Insert Into IrisData Values (6.0,3.0,4.8,1.8,'Iris-virginica')
Insert Into IrisData Values (6.9,3.1,5.4,2.1,'Iris-virginica')
Insert Into IrisData Values (6.7,3.1,5.6,2.4,'Iris-virginica')
Insert Into IrisData Values (6.9,3.1,5.1,2.3,'Iris-virginica')
Insert Into IrisData Values (5.8,2.7,5.1,1.9,'Iris-virginica')
Insert Into IrisData Values (6.8,3.2,5.9,2.3,'Iris-virginica')
Insert Into IrisData Values (6.7,3.3,5.7,2.5,'Iris-virginica')
Insert Into IrisData Values (6.7,3.0,5.2,2.3,'Iris-virginica')
Insert Into IrisData Values (6.3,2.5,5.0,1.9,'Iris-virginica')
Insert Into IrisData Values (6.5,3.0,5.2,2.0,'Iris-virginica')
Insert Into IrisData Values (6.2,3.4,5.4,2.3,'Iris-virginica')
Insert Into IrisData Values (5.9,3.0,5.1,1.8,'Iris-virginica')

```

```

Create Table NormalizedIrisData (x1 float, x2 float, x3 float, x4 float, class
varchar(255))

```

```

Insert Into NormalizedIrisData
Select (x1-mue_x1)/std_x1,(x2-mue_x2)/std_x2,(x3-mue_x3)/std_x3, (x4-
mue_x4)/std_x4, class
from IrisData i cross join (
Select AVG(x1) as mue_x1, STDEVP(x1) as std_x1,AVG(x2) as mue_x2,
STDEVP(x2) as std_x2,
AVG(x3) as mue_x3, STDEVP(x3) as std_x3,AVG(x4) as mue_x4,STDEVP(x4)
as std_x4
from IrisData) d

```

```

--Select * from NormalizedIrisData

```

```

Create Table TrainingData (i int primary key identity, x1 float, x2 float, x3 float,
x4 float, class1 bit,class2 bit,class3 bit)
Create Table ValidationData (i int primary key identity, x1 float, x2 float, x3
float, x4 float, class1 bit,class2 bit,class3 bit)

```

```

Truncate Table TrainingData
Truncate Table ValidationData

```

```

Insert into TrainingData
Select x1,x2,x3,x4,CASE class WHEN ('Iris-virginica') THEN 1 ELSE 0
END,CASE class WHEN ('Iris-versicolor') THEN 1 ELSE 0 END,CASE class
WHEN ('Iris-setosa') THEN 1 ELSE 0 END
from (

```

```
Select ROW_NUMBER() over (order by class)%10 as 'Bucket' ,* from
NormalizedIrisData)x where Bucket < 7
```

```
Insert into ValidationData
Select x1,x2,x3,x4,CASE class WHEN ('Iris-virginica') THEN 1 ELSE 0
END,CASE class WHEN ('Iris-versicolor') THEN 1 ELSE 0 END,CASE class
WHEN ('Iris-setosa') THEN 1 ELSE 0 END
from (
Select ROW_NUMBER() over (order by class)%10 as 'Bucket' ,* from
NormalizedIrisData)x where Bucket >= 7
```

```
use NeuralNetwork
go
```

```
--helperfunction as sql doesn't offer a hyperbolic tangent function
```

```
Create Function tanh (@x float) Returns float
as
begin
```

```
    -- Declare the return variable here
    declare @Result float
    -- Add the T-SQL statements to compute the return value here
    set @Result = (exp(@x) - exp(-@x)) / (exp(@x) + exp(-@x))
    -- Return the result of the function
    return @Result
```

```
end
go
```

```
Create Table Error (MSE float)
```

```
--structure the neural network:
```

```
Create Table Node (ID int primary key identity, NodeType char(2),
WeightedInputSum float, ActivationOutput float, ExpectedOutput float, Delta
float, Gradient float)
```

```
Create Table Edge (FromNodeID int references Node, ToNodeID int references
Node, [Weight] float, PrevWeightDelta float)
```

```
--3 input Nodes
```

```
Insert Into Node VALUES ('I',null,null,null,null,null),
('T',null,null,null,null,null),('T',null,null,null,null,null),
('T',null,null,null,null,null),('BI',null,1,null,null,null)
```

```
--7 hidden Nodes
```

```
Insert Into Node VALUES ('H',null,null,null,null,null),
('H',null,null,null,null,null),('H',null,null,null,null,null),
('H',null,null,null,null,null),('H',null,null,null,null,null),
('H',null,null,null,null,null),('BH',null,1,null,null,null)
```

```
--3 output nodes
```

```
Insert Into Node VALUES ('O',null,null,null,null,null),
('O',null,null,null,null,null),('O',null,null,null,null,null)
```

```

go
Create View HiddenNodes as Select * from Node where NodeType = 'H' or
NodeType = 'BH'
go
Create View InputNodes as Select * from Node where NodeType = 'I' or
NodeType = 'BI'
go
Create View OutputNodes as Select * from Node where NodeType = 'O'
go

--Initialize Weights and Biases
Insert Into Edge
Select i.ID,h.ID,0.02*RAND(CHECKSUM(NEWID()))-0.01,0 from InputNodes
i cross join HiddenNodes h
where h.NodeType != 'BH' -- no input weight into the hidden bias fake neuron

Insert Into Edge
Select h.ID,o.ID,0.02*RAND(CHECKSUM(NEWID()))-0.01,0 from
HiddenNodes h cross join OutputNodes o

--calculate forward pass

go
Create Procedure CalculateErrorForSample (@SampleID int)
as
begin
    -- take a training example and save it as activation of the input neurons and
    the labels as expected output of the output neurones
    Update InputNodes set ActivationOutput = (Select x1 from TrainingData
    where i = @SampleID) where InputNodes.ID = 1
    Update InputNodes set ActivationOutput = (Select x2 from TrainingData
    where i = @SampleID) where InputNodes.ID = 2
    Update InputNodes set ActivationOutput = (Select x3 from TrainingData
    where i = @SampleID) where InputNodes.ID = 3
    Update InputNodes set ActivationOutput = (Select x4 from TrainingData
    where i = @SampleID) where InputNodes.ID = 4
    Update OutputNodes set ExpectedOutput = (Select class1 from
    TrainingData where i = @SampleID) where OutputNodes.ID = 14
    Update OutputNodes set ExpectedOutput = (Select class2 from
    TrainingData where i = @SampleID) where OutputNodes.ID = 15
    Update OutputNodes set ExpectedOutput = (Select class3 from
    TrainingData where i = @SampleID) where OutputNodes.ID = 16

    -- calculate the weighted input sum of the hidden nodes
    Update h set h.WeightedInputSum = x.WeightedInputSum
    from HiddenNodes h
    join (Select ToNodeID, SUM(i.ActivationOutput*e.Weight) as
    'WeightedInputSum' from InputNodes i join Edge e on i.ID = e.FromNodeID

```

```
group by ToNodeID) x on h.ID = x.ToNodeID
```

–calculate activation of the hidden nodes using the hyperbolic tangent activation function:

```
Update HiddenNodes set ActivationOutput = dbo.tanh(WeightedInputSum)
where NodeType = 'H'
```

— calculate the weighted input sum of the output nodes

```
Update o set o.WeightedInputSum = x.WeightedInputSum
from OutputNodes o
join (Select ToNodeID, SUM(h.ActivationOutput*e.Weight) as
'WeightedInputSum' from HiddenNodes h join Edge e on h.ID = e.FromNodeID
group by ToNodeID) x on o.ID = x.ToNodeID
```

–calculate activation of the output nodes using Soft Max activation function:

```
declare @MaxOutput float
declare @Scale float
Select @MaxOutput = Max(WeightedInputSum) from OutputNodes
Select @Scale = SUM(EXP(WeightedInputSum - (@MaxOutput))) from
OutputNodes
Update OutputNodes set ActivationOutput = EXP(WeightedInputSum-
@MaxOutput)/@Scale
```

–Calculate the error for this one training example:

```
Update OutputNodes set Delta = ExpectedOutput - ActivationOutput
end
```

```
go
```

```
Create Procedure UpdateWeights (@learningrate float, @momentum float)
```

```
as
```

```
begin
```

–Calculate OutputLayer Gradient = (SoftMax Derivative \* Delta)

```
Update OutputNodes set Gradient = (1-ActivationOutput)*ActivationOutput *
Delta
```

–Calculate HiddenLayer Deltas (= Sum of the weighted Output Layer gradients)

```
Update h set Delta = x.Delta
from HiddenNodes h join (
Select e.FromNodeID, SUM(o.Gradient*e.Weight) as 'Delta'
from OutputNodes o join Edge e on o.ID = e.ToNodeID group by
e.FromNodeID) x
on h.ID = x.FromNodeID
```

–calculate HiddenLayer Gradient = (tanh Derivative \* Delta)

```
Update HiddenNodes set Gradient = (1-ActivationOutput)*
(1+ActivationOutput) * Delta
```

— Update weights between input and hidden layer

```
Update e set PrevWeightDelta = @learningrate * h.Gradient*
```

```

i.ActivationOutput,
[Weight] = [Weight] * 0.9999 + @learningrate * h.Gradient * i.ActivationOutput
+ @momentum * PrevWeightDelta
from HiddenNodes h join Edge e on e.ToNodeID = h.ID join InputNodes i on
e.FromNodeID = i.ID

```

–Update weights between hidden and output layer ->

```

Update e set PrevWeightDelta = @learningrate * o.Gradient *
h.ActivationOutput,
[Weight] = [Weight] * 0.9999 + @learningrate * o.Gradient * h.ActivationOutput
+ @momentum * PrevWeightDelta
from HiddenNodes h join Edge e on e.FromNodeID = h.ID join OutputNodes o
on e.ToNodeID = o.ID
end

```

go

–Calculate Training Set Error

```

Create Procedure CalculateMSEforTrainingData
as
begin
    -- cannot be a function as it changes a table 😞 not nice i know!
    set nocount on
    declare @id int = 1
    declare @squarederror decimal(32,5) = 0
    declare @numberofobservations int
    Select @numberofobservations = COUNT(*) from TrainingData
    while @id <= @numberofobservations
    begin
        exec CalculateErrorForSample @id
        Select @squarederror = @squarederror + SUM(delta*delta) from
OutputNodes
        set @id += 1
    end
    Select @squarederror/@numberofobservations
end
go

```

–stochastic gradient descent

```

Create Procedure Train (@learningrate float, @momentum float)
as
begin
    set nocount on
    declare @numberofsamples int = 105
    declare @x int = 0
    while @x < @numberofsamples
    begin
        declare @trainingsample int
        Select @trainingsample = CAST(RAND()*105 as int)+1
    end
end

```

```

--print @trainingsample
exec CalculateErrorForSample @trainingsample
exec UpdateWeights @learningrate, @momentum
set @x += 1
end
end
go

```

```

Create Procedure Learn
as
begin
set nocount on
declare @error float
declare @epoch int = 0
while @epoch < 20
begin
Insert Into Error
exec CalculateMSEforTrainingData
Select @error = MSE from Error
--Training while MSE > Threshold
if (@error < 0.02)
begin
break
end
exec Train 0.05, 0.01
print @error
--calculate the new error
Truncate Table Error
Insert Into Error
exec CalculateMSEforTrainingData
Select @error = MSE from Error
set @epoch +=1
end
end
go

```

--this will start the backpropagation algorithm until the errorfunction converges.

--you can also run a single step of back propagation calling the next two lines!

```
exec Learn
```

```
--exec CalculateMSEforTrainingData
```

```
--exec Train 0.05, 0.01
```

```
--Select * from InputNodes
```

```
--Select * from HiddenNodes
```

```
--Select * from OutputNodes
```

```
--Select * from Edge
```

```

Use NeuralNetwork
--VALIDATION:

GO

Create Procedure CalculateErrorForValidationSample (@SampleID int)
as
begin
    Update InputNodes set ActivationOutput = (Select x1 from ValidationData
    where i = @SampleID) where InputNodes.ID = 1
    Update InputNodes set ActivationOutput = (Select x2 from ValidationData
    where i = @SampleID) where InputNodes.ID = 2
    Update InputNodes set ActivationOutput = (Select x3 from ValidationData
    where i = @SampleID) where InputNodes.ID = 3
    Update InputNodes set ActivationOutput = (Select x4 from ValidationData
    where i = @SampleID) where InputNodes.ID = 4
    Update OutputNodes set ExpectedOutput = (Select class1 from
    ValidationData where i = @SampleID) where OutputNodes.ID = 14
    Update OutputNodes set ExpectedOutput = (Select class2 from
    ValidationData where i = @SampleID) where OutputNodes.ID = 15
    Update OutputNodes set ExpectedOutput = (Select class3 from
    ValidationData where i = @SampleID) where OutputNodes.ID = 16

    Update h set h.WeightedInputSum = x.WeightedInputSum
    from HiddenNodes h
    join (Select ToNodeID, SUM(i.ActivationOutput*e.Weight) as
    'WeightedInputSum' from InputNodes i join Edge e on i.ID = e.FromNodeID
    group by ToNodeID) x on h.ID = x.ToNodeID

    Update HiddenNodes set ActivationOutput =
    dbo.TANH(WeightedInputSum) where NodeType = 'H'

    Update o set o.WeightedInputSum = x.WeightedInputSum
    from OutputNodes o
    join (Select ToNodeID, SUM(h.ActivationOutput*e.Weight) as
    'WeightedInputSum' from HiddenNodes h join Edge e on h.ID = e.FromNodeID
    group by ToNodeID) x on o.ID = x.ToNodeID

    declare @MaxOutput float
    declare @Scale float
    Select @MaxOutput = Max(WeightedInputSum) from OutputNodes
    Select @Scale = SUM(EXP(WeightedInputSum - (@MaxOutput))) from
    OutputNodes
    Update OutputNodes set ActivationOutput = EXP(WeightedInputSum-
    @MaxOutput)/@Scale
    Update OutputNodes set Delta = ExpectedOutput - ActivationOutput
END

```

GO

```
CREATE Procedure CalculateMSEforValidationData
AS
BEGIN
    -- Declare the return variable here
    DECLARE @Result float
    set nocount on
    declare @id int = 1
    declare @squareerror decimal(32,5) = 0
    declare @numberofobservations int
    Select @numberofobservations = COUNT(*) from ValidationData
    while @id <= @numberofobservations
    begin
        exec CalculateErrorForValidationSample @id
        Select @squareerror = @squareerror + SUM(delta*delta) from
        OutputNodes
        set @id += 1
    end

    Select @squareerror/@numberofobservations
END
GO
```

```
exec CalculateMSEforValidationData
```



## Add a Comment

*Comment*

Add Comment

© 2020 Lukas Steindl