

$$\textcircled{27} \textcircled{I} D_a(ab + aab) =$$

$$D_a(ab) + D_a(aab) =$$

$$= b + ab$$

$$D_a(abaab) = baab$$

But also

$$D_a(abaab) = D_a(ab \cdot aab)$$

$$= D_a(ab) \cdot aab + \delta(ab) \cdot D_a(aab)$$

$$= baab + \emptyset \cdot ab = baab$$

$$\textcircled{II} \overline{Dab(a \cdot a^* \cdot b \cdot b^*)} =$$

$$= Db(Da(a \cdot a^* \cdot b \cdot b^*)) =$$

$$Db(a^*bb^*) = Db(a^* \cdot bb^*)$$

$$= Db(a^*) \cdot bb^* + \delta(a^*) Db(bb^*) =$$

$$= \emptyset \cdot bb^* + \lambda \cdot b^* = b^*$$

Note that  $Db(a^*) = Db(a)a^* =$

$$= \emptyset a^* = \emptyset$$

Q8

$$a + b = R$$

$$\begin{aligned} Da(a+b) &= Da(a) + Da(b) = \\ &= \lambda + \emptyset = \lambda \end{aligned}$$

$$\begin{aligned} Db(a+b) &= Db(a) + Db(b) = \\ &= \emptyset + \lambda = \lambda \end{aligned}$$

$$\begin{aligned} Daa(R) &= Da(Da(R)) = \\ &= Da(\lambda) = \emptyset \end{aligned}$$

$\Rightarrow$  We don't need considering  $Daa \dots (R)$  anymore

$$\begin{aligned} Dab(R) &= Db(Da(R)) = Db(\lambda) = \emptyset \\ \Rightarrow \text{no need to consider } Dab \dots (R) \end{aligned}$$

$$\begin{aligned} Dba(R) &= Da(Db(R)) = Da(\lambda) = \emptyset \\ \Rightarrow \text{no need to consider } Dba \dots (R) \end{aligned}$$

$$Dbb(R) = Db(Db(R)) = Db(\lambda) = \emptyset$$

We have finished

We have  $R_0 = (a+b)$   $R_1 = \lambda$  } only two expressions (different)

Now

$$\left[ \begin{array}{ll} Da(R_0) = \lambda & Db(R_0) = \lambda \\ Da(R_1) = \emptyset & Db(R_1) = \emptyset \\ \delta(Da(R_0)) = \lambda & \delta(Db(R_0)) = \lambda \\ \rightarrow R_0 \rightarrow a\lambda & R_0 \rightarrow b\lambda \end{array} \right]$$

$$S \rightarrow a|b$$