





Workbook v1.1

Brought to you by the Bootstrap team:

- Emmanuel Schanzer
- Kathi Fisler
- Shriram Krishnamurthi
- Sam Dooman
- Ed Campos

Bootstrap is licensed under a Creative Commons 3.0 Unported License. Based on a work from www.BootstrapWorld.org. Permissions beyond the scope of this license may be available at schanzer@BootstrapWorld.org.

### Unit 1

- Many important questions ("what's the best restaurant in town?", "is this law good for citizens?", etc.) are answered with data. Data Scientists try and answer these questions, by writing programs that ask questions of data.
- Data of all types can be organized into **Tables**
- Every Table has a header row, and some number of data rows
- **Quantitative data** is data usually numeric that measures *quantity*, such as a person's height, a score on test, a measure of distance, etc. A list of quantitative data can be ordered from smallest to largest.
- Categorical data is data that specifies categories, such as eye color, country of origin, etc. A list of categorical data has no notion of "smallest" or "largest", and cannot be ordered.
- **Programming languages** involves different *datatypes*, such as Numbers, Strings, Booleans and Images.
- Operators (like +, -, \*, <, etc.) are written between values. For example: 4 + 2
- **Functions** (like triangle, star, string-repeat, etc.) are written first, followed by a list of **arguments** in parentheses. For example: star(50, "solid", "red")
- **Examples** help programmers reason about their code. Every example contains two expressions, and the example "passes" if both expressions evaluate to the same thing. For example: 4 + 2 is 6, or "cat" == "dog" is false

# Numbers and Strings

Make sure you've loaded the Unit 1 Starter File, and clicked "Run".

- 1. Try typing 42 into the Interactions Area and hitting "Enter". What happens?
- 2. Try typing in other Numbers. What happens if you try a decimal like 0.5? A fraction like 1/3? Try really big Numbers, and really small ones.
- 3. String values are always in quotes. Try typing your name in quotes, and see what happens when you hit "Enter".
- 4. Try typing your name without the closing quote. What happens? Now try typing it without any quotes.
- 5. Is 42 the same as "42"? Why or why not? Write your answer below:

# **Operators**

- 6. Just like in math, Pyret has operators like + and -. Try typing in 4 + 2, and then 4+2 (without the spaces). What can you conclude from this? Write your answer below:
- 7. Try typing in 4+2+6, 4+2\*6, and 4+(2\*6). What can you conclude from this? Write your answer below:
- 8. Try typing in 4 + "cat", and then "dog" + "cat". What can you conclude from this? Write your answer below:

#### Booleans

Boolean expressions are yes-or-no questions, and you probably already know some Boolean operators from math class, which compare Numbers. What will each of the shaded expressions below evaluate to? Type them into Pyret if you're not sure.

3 <= 4	 "a" > "b"	
3 == 2	 "a" <> "b"	
2 <> 4	 "a" == "b"	
3 <> 3	 "a" <> "a"	

## **Boolean Operators**

Pyret also has operators that work on *Booleans*. For each expression below, write down your guess about what it will evaluate to. Then type them in and see if you were right!

$$(3 \le 4)$$
 and  $(3 == 2)$ 
 $("a" == "b")$  and  $(3 <> 4)$ 
 $(3 <= 4)$  or  $(3 == 2)$ 
 $("a" == "b")$  or  $(3 <> 4)$ 

- 2. How many different String values are there in Pyret?
- 3. How many different Boolean values are there in Pyret?

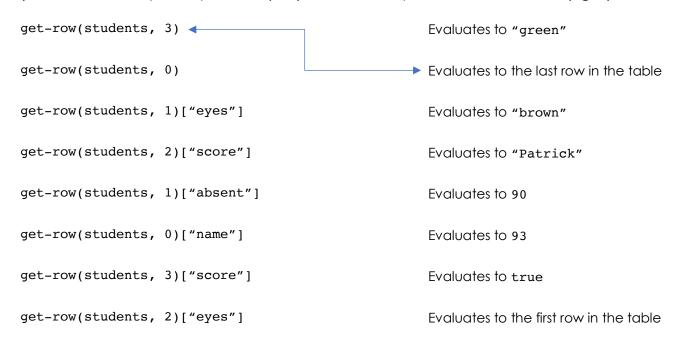
# Playing with Tables

The students table below represents four students in Ms. Phillip's history class:

#### students

name	eyes	score	absent
"Patrick"	"brown"	82	false
"Syd"	"green"	65	true
"Asha"	"brown"	93	false
"Berri"	"blue"	90	false

1) Match each Pyret expression (left) to the description of what it does (right).



2) Fill in the blanks (left) with the Pyret code that will produce the value (right).

a. get-row(students, 3)["eyes"]	"blue"
b.	65
С.	"Asha"
d.	82
e.	"Berri"

# Writing Examples

In the examples block below, put an "X" next to the examples that will <u>fail</u>.
 Remember: examples only pass if the left- and right-hand expressions evaluate to the same thing!

```
examples:
    1 + 2 + 9
    num-sqrt(16)
    is 2 + 2
    3 > 99
    is true
    square(10, "solid", "red")
end

is 19
is 2 + 2
is true
is rectangle(10, 10, "solid", "red")
end
```

2. In the examples block below, fill in the blank on the right-hand side so the example will pass.

3. The examples block below refers to the shapes table on the right, using row-accessors and the get-row function. For each example, fill in the blank so the example will pass.

name	corners	Is-round
"triangle"	3	false
"circle"	0	true
"ellipse"	0	true
"square"	4	false

### Unit 2

- Programming languages let us **define our own function**.
- We use the **Design Recipe** to help us define functions without making mistakes.
- The first step is to write a **Contract** and **Purpose Statement** for the function, which specify the Name, Domain and Range of the function and give a summary of what it does.
- The second step is to **write at least two examples**, which show how the function should work for specific inputs. These examples help us see patterns, and we express those patterns by **circling and labeling** what changes.
- The final step is to **define the function**, which generalizes our examples.



# The Animals Dataset

1.	This dataset	is Animals from a	pet store					
2.	. Four of my columns are (choose four columns, and for each one fill out the name, datatype, and whether it contains Qualitative or Categorical data in the table below)							
N	ame							
D	atatype							
	uantitative or ategorical?							
3.	Three quest  1.  2.	ions I have about	my dataset:					
	3.							

# The Design Recipe

Define a function called is-fixed, which tells us whether or not an animal is fixed

	is-fixed	::	(animal :: Row)	$\rightarrow$	Boolean
	name		domain		range
# <u>Col</u>	nsumes an anima	al, and produc	es the value in the fi	xed column	
exam	ples:				
	is-fixed	( sashi	a ) <b>is</b>	true	
		(			
		(	) is		
end					
fun		(	) :		· · · · · · · · · · · · · · · · · · ·
end					
0110					
	e a function cal ender of that ar		which consumes a R	ow of the anir	nals table tells us
			which consumes a R	ow of the anir	nals table tells us
		nimal	which consumes a R		nals table tells us
	ender of that ar	nimal			
#	ender of that ar	nimal			
#	name	nimal			
#	name	nimal::	domain) <b>is</b>	>	
#exam	name	nimal::	domain	>	
#exam	name	nimal::	domain) <b>is</b>	>	
#exam	name	nimal::	domain) <b>is</b>	>	

Define a function called is-cat, which consumes a Row of the animals table and produces true if it's a cat.

	is-cat		(animal :: Row)		Boolean
	name	::	domain	<del>-</del> -	range
# Co		nal, and return	n true if the species is	s "cat"	5 0
`` —	mples:				
	is-cat	(sasha	<u></u> ) is		
		(	) is		
end					
fun		(	) :		
end					
0110					
Defin	e a function co	alled i a_voun	~ which consumes	a Pow of the a	nimals table and
			g, which consumes o		nimals table and
					nimals table and
					nimals table and
produ		an animal the			nimals table and
	JCes true if it's	an animal the	at is less than two ye		
#	JCes true if it's	an animal the	at is less than two ye		
#	name	an animal the	domain	ars old >	range
#	name	an animal the	domain) is	ars old >	range
#	name  nples:	an animal the	domain) is	ars old >	range
# _ exa	name  nples:	an animal the	domain) is	ars old >	range

Define a function called nametag, prints out each animal's name in big red letters.

	nametag	::	(animal :: Row)	$\rightarrow$	Image
	name		domain		range
#	Consumes an animo	al, and produc	es an image of their	name in big, re	ed letters
ex	amples:				
	nametag	(sash	<u>a</u> ) <b>is</b>		
		(	) is		
en	d				
fu	n	(	) :		<del> </del>
en	ď				
	ine a function ca duces true if it's a		en, which consumes	a Row of the	animals table and
			en, which consumes	a Row of the	animals table and
			en, which consumes  domain		animals table and
	duces true if it's a				
#	duces true if it's a				
#	name				
#	name	::	domain	>	range
# #	name amples:	::	domain	>	range
# ex	name amples:		domain	>	range

# My Dataset

(choose four	columns are columns, and for Categorical dat	each one fill out that in the table belo	ne name, datatype w)	e, and whether it contains
ame				
atatype				
uantitative or ategorical?				
1.		oout my datase		
1.				
1.				
1.				

### Unit 3

- Methods are special functions that are attached to pieces of data. We use them to manipulate Tables.
- They are different from functions in several ways:
  - 1. Their names can't be used alone: they can only be used as part of data, separated by a dot. (For example, animals.order-by)
  - 2. Their contracts are different: they include the type of the data as part of their names. (eg, .order-by :: (column :: String) → Table)
  - 3. They have a "secret" argument, which is the data they are attached to
- We will use three **Table Methods** to manipulate our datasets:
  - 1. <Table>.order-by order the rows of a table based on a column
  - 2. <Table>.filter create a **subset** of the data, with only certain rows
  - 3. <Table>.build-column use the columns of a table to compute a new one
- We use Table Plans to help us use these methods correctly, without making mistakes

# Reviewing Functions

1.	How many functions are defined in this file?	
2.	What is the name of the last function?	
3.	What is the Domain of the last function?	
4.	What is the Range of the last function?	
5.	What is the Range of the last function?	
6.	What is the variable name that the last function uses?	
7.	Which function will tell us if an animal is a kitten?	
8.	Which function will print out " <name> the <species>"?</species></name>	
9.	Which function will tell us if an animal is a dog older than 10?	
10	.Which function will tell us if an animal has been fixed?	
11	.Which function will draw a nametag for an animal?	

12. One of the examples for the last function is broken. Fix this example in the Definitions Area.

# Plans for the Animals Dataset

What are two ways you might want to order the animals dataset?
1)
2)
What are two subsets into which you might filter the animals dataset?
1)
2)
What are two new columns you might want to build from the animals dataset?
1)
2)

#### Methods

Methods are a lot like functions, but they differ in three important ways:

- They can only be called as **part of a value**, using the **dot-accessor**. For example: **animals.**row-n(2)
- Their Contracts are different, because they contain a **Type** as part of their name. For example: <**Table>.**row-n :: (index :: Number) -> Row
- They have a "secret argument", which is the value they are attached to. In the examples above, the row-n method consumes only a Number as part of its Domain, but it also consumes a Table.

Here is the Contract for a method, which consumes the name of a food and produces True if the person likes that food:

Person>.likes :: (food :: String) -> Boolean
1. What Type of data is the method attached to?
2. What is the name of this method?
3. How many things are in its Domain?
4. What is the name of the argument in its Domain?
5. What is the Type of the argument in its Domain?
6. What Type of data will this method will produce?
7. Below are 3 expressions. Based on the contract above, circle the correct one.
emma.likes("pizza")
likes("pizza")
likes(emma, pizza)

8. On the line below, write your own expression that uses this method, replacing emma and "pizza" with your own name and a food you like.

On Kitten Day, the shelter prints up a list of all the cats in their database that are less than 2 years old, and makes nametags for them. They need a function that will help them out! Define a function called get-kittens-tags, which takes in the dataset and produces the correct table.

Make a Start Table and a result based on that table.    Sanimals	3	Table	7		$\rightarrow$		le)	: Tabi	nimals .	(ar	<b>:</b>	:	ags	ns-ti	t-kitte	ger
Make a Start Table and a result based on that table.    animals-table	пате	d by na	, sorted	tags,	name	with:	kittens	taining	able cor	uce a t	nd prod	ls, an	anima	le of	ne a tabi	# Consun
name     species     age     fixed     legs     weight     adopt       Sasha     cat     1     FALSE     4     6.5     4       Toggle     dog     3     TRUE     4     48     3       Buddy     lizard     2     FALSE     4     0.3     12       Wade     cat     1     FALSE     4     3.2     4       Mittens     cat     2     TRUE     4     7.4     5     Define the function  Jse the relevant methods (circle your helper functions!), then produce a result with the new form the personal methods (circle your helper functions!), then produce a result with the new form the personal methods (circle your helper functions!) is the personal method of the persona																
Sasha   Cat   1   FALSE   4   6.5																
name     species     age     fixed     legs     weight     adopt       Sasha     cat     1     FALSE     4     6.5     4       Toggle     dog     3     TRUE     4     48     3       Buddy     lizard     2     FALSE     4     0.3     12       Wade     cat     1     FALSE     4     3.2     4       Mittens     cat     2     TRUE     4     7.4     5    Define the function  Jac       Jse the relevant methods (circle your helper functions!), then produce a result with the new functions!) is the produce a result with the new functions. The produce is the produce of the produce o								_		on the	based	esult	nd a re			
Sasha         cat         1         FALSE         4         6.5         4           Toggle         dog         3         TRUE         4         48         3           Buddy         lizard         2         FALSE         4         0.3         12           Wade         cat         1         FALSE         4         3.2         4           Mittens         cat         2         TRUE         4         7.4         5     Define the function  Jack there  Sasha cat 1 FALSE 4 6.5 4  Gard 1 FALSE 4 6.5  Wade cat 1 FALSE 4 3.2  I FALSE 4 3.2  Wade cat 1 FALSE 4 3.2  FALSE 4 3.2  A 3.2  A 3.2  A 3.2  A 3.2  A 3.2  A 4  Sasha cat 1 FALSE 4 6.5  Wade cat 1 FALSE 4 3.2  A 3.2  A 3.2  A 3.2  A 3.2  A 4  Sasha cat 1 FALSE 4 6.5  A 1 FALSE 4 3.2  A 4  Sasha cat 1 FALSE 4 6.5  A 6.5  A 4 6.5  A 4 6.5  A	-table	<u>nals-</u>	(anir	ags	ns-t	tte:	et-ki	<b>→</b> g	_					<u>le</u>	s-tab	<u>animal</u>
Sasha         Cat         1         FALSE         4         6.5         4           Toggle         dog         3         TRUE         4         48         3           Buddy         lizard         2         FALSE         4         0.3         12           Wade         cat         1         FALSE         4         3.2         4           Mittens         cat         2         TRUE         4         7.4         5     Define the function  Jack the relevant methods (circle your helper functions!), then produce a result with the new formation of the relevant methods (circle your helper functions!) is the produce of the relevant methods (circle your helper functions!) is the produce of the relevant methods (circle your helper functions!) is the relevant methods (circle your helper functions!) is the produce of the relevant methods (circle your helper functions!) is the relevant method (circle your	ot tag	adopt	weight	legs	fixed	age	species	name		adopt				age	species	name
Buddy lizard 2 FALSE 4 0.3 12  Wade cat 1 FALSE 4 3.2 4  Mittens cat 2 TRUE 4 7.4 5   Define the function  Use the relevant methods (circle your helper functions!), then produce a result with the new to the second secon	Sascho		6.5	4	FALSE	1	cat	Sasha								
Wade cat 1 FALSE 4 3.2 4  Mittens cat 2 TRUE 4 7.4 5   Define the function  Use the relevant methods (circle your helper functions!), then produce a result with the new to the second s															ŭ	
Define the function  Use the relevant methods (circle your helper functions!), then produce a result with the new to the second method (circle your helper functions!), then produce a result with the new to the second method (circle your helper functions!), then produce a result with the new to the second method (circle your helper functions!), then produce a result with the new to the second method (circle your helper functions!), then produce a result with the new to the second method (circle your helper functions!), then produce a result with the new to the second method (circle your helper functions!), then produce a result with the new to the second method (circle your helper functions!), then produce a result with the new to the second method (circle your helper functions!), then produce a result with the new to the second method (circle your helper functions!), then produce a result with the new to the second method (circle your helper functions!), then produce a result with the new to the second method (circle your helper functions!), then produce a result with the new to the second method (circle your helper functions!), then produce a result with the new to the second method (circle your helper functions!), then produce a result with the new to the second method (circle your helper functions!), the sec	Wade	4	3.2	4	FALSE	1	cat	Wade				·				
Define the function  Use the relevant methods (circle your helper functions!), then produce a result with the new to the function of the funct												4				
fun         get-kittens-tags         ( pets ):         Define           t = pets         .build-column(         )         Are there money           _filter(         )         Are there									· ·							
t = pets build-column(	lable.	new to	th the i	JIT WI	a resu	luce	en prod	,		helper	·					Jse the re
t = pets	the table	fine t	Des				:	<u>5</u> )	pet.	_ (_	195	15-10	litter	iet-k	9	fun
				_											ets	<u>† = p</u>
				)									<u></u>	<u>'umn</u>	<u> iild-col</u>	bu
.order-by( ) Are the ro	fewer rows.	there fe	Are t	_)											Iter(	fi
	ws ordered.	the row	Are 1	)										(	der-by	or
† Produce 1	he resul	uce th	Produ	_												<i>†</i>

The first weekend of every month, the shelter holds a "meet the dogs" picnic, to encourage families to adopt their dogs. Write a function called get-dogs-by-age, that takes their database and produces a table of all the dogs in the shelter, sorted from youngest to oldest.

	-dogs-b	y-ag	ре	<b>::</b> _		(anima	als :: Tabl	le)	>	·		Та	ble	
# Consum	e a table	of ai	nimals, d	nd pi	roduce	a table	containing	only the	dogs, so	rted	by ag	re		
xample: Make a St		e and	d a resul	t has	sed on	that ta	ble							
animals					.00 011		<b>→</b>	get-d	og-by	-ag	e(an	<u>ima</u>	ls-ta	able
name	species	age	fixed	legs	weight	adopt								
Snowcone	cat	2	TRUE	4	6.1	5		name	species	age	fixed	legs	weight	adopt
Wade	cat	1	FALSE	4	3.2	4		Toggle	dog	3	TRUE	4	48	3
Hercules	cat	3	FALSE	4	13.4	7	-	Fritz	dog	4	TRUE	4	92	6
Toggle	dog	3	TRUE	4	48	3	L		l					I
Fritz	dog	4	TRUE	4	92	6								
Define th	e funct	ion												
							مائد المصمئاء	1		\	vith th	e ne	w table	
	ievant m	netho	ods (circ	de yo	our help	er tund	CHONS!), ING	en proau	ce a res	OII V	VIII II I	0	W IGDI	€.
	ievant m	netho	ods (circ	le yc	our help	er tund	Chonsi), ine	en proau	ice a res	OII V	VIII II I	0110	W IGDI	∋.
Jse the re	ievant m	netho	ods (circ	ile yc	our help (	er tund	) :	en produ	ice a res	SOII V	VIII II II I	0110	W IGDI	Э.
	levant m	netho	ods (circ	cle yc	our help	er tund		en produ	ice a res	SOII V			ne the	
Ise the re  Fun				cle yc	our help (	er tund		en produ			<u></u>	efir	ne the	tabl
Sun	ild-colu			ele yo	our help ( 	er tund		en produ 			<u>D</u>	<u>efir</u> there	more c	table table
se the re Fun				cle yo	our help (	per fund		en produ	ce a res		Are:	<b>)efir</b> there e the	ne the more co	tabl
Se the re	ild-colu	mn(		cle yo	(	per fund		en produ	ce a res		Are:	<b>)efir</b> there e the	more c	table table

It's important for animals to stay healthy, especially when they get older. The veterinarians at the shelter want to put some of the dogs on a diet! They need a regular report of all the older dogs, sorted from heaviest-to-lightest. Define a function old-dogs-diet, which does just that!

Contract	and Purpo	ose												
			::						>	<b>&gt;</b> _				
Example														
Make a St	art Table ar	nd a	result be	ased	I on the	at tab	le.							
animals	-table					•	$\rightarrow$	old-	dogs-	<u>die</u>	t(an	<u>imal</u>	s-tal	ole)
name	species	age	fixed	legs	weight	adopt		n amo		- 70	fixed	logo	weight	-dont
Snowcone	cat	2	TRUE	4	6.1	5		name Lucky	species dog	age 3	fixed TRUE	legs	weight 45.4	adopt 9
Lucky	dog	3	TRUE	3	45.4	9		Snowcone	cat	2	TRUE	4	6.1	5
Hercules	cat	3	FALSE	4	13.4	7		Toggle	dog	3	TRUE	4	48	3
Toggle	dog	3	TRUE	4	48	3		109910	409		11.02		10	
Snuggles	tarantula	2	FALSE	8	0.1	1								
			_	_		_								
Define th	e function													
			(circle	your	helper	funct	ions!),	then produ	ice a re	sult v	vith the	e new	/ table.	,
fun					_ (		_)	:			_	·	. 1	
											<u>D</u>	etine	e the t	able
											Are t	here n	more col	umns?
	ter(									 	Are	e there	e fewer	rows?
											Are	e the r	rows ora	dered?
ord	der-by(													
											Pro	duce	the re	esult
end														

The shelter is tracking birth-years for all the animals who've been fixed. They need a function that takes in their database and returns a table that contains the birth-year for each one. Define get-fixed-birth that will do this for them.

Contract	and Purpo	ose													
			::							_ =	<b>&gt;</b>				
Examples															
Make a St	art Table ar	nd a	result b	asec	I on the	at tabl	le.								
	- +-blo						_`	<b>&gt;</b>	- : a	L	7 - ~ ~	′ - m i	·	⊥oh	- 7 - N
animals							_	→ get-f	:1xea-	-py-	tegs	(anı	_mars	-tab	теу
name	species	age	fixed	legs				name	species	age	fixed	legs	weight	adopt	year
Snowcone	cat	2	TRUE	4	6.1	5		Snowcone	cat	2	TRUE	4	6.1	5	2015
Lucky	dog	3	TRUE	3	45.4	9		Lucky	dog	3	TRUE	3	45.4	9	2014
Hercules	cat	3	FALSE	4	13.4	7		Toggle	dog	3	TRUE	4	48	3	2014
Toggle	dog	3	TRUE	4	48	3		109910	409		11102		10		2 4 -
Snuggles	tarantula	2	FALSE	8	0.1	1									
					.1	<u> </u>	1								
							_								_
	e function		/ sincle		اء ماره در	· £ a k						U- H		-:   -   -	
use me re	levant meth	100s	(Circle )	your	neipei	TUNCII	1OI	ns!), men p	roduce	; a re	SUIT WII	n me	new i	dbie.	
					,										
fun					_ (			):				De	efine 1	the to	nhla
<u>† =</u>															
	ild-column										)	Are th	here moi	re colu	ımns?
	ter(											Are	there f	ewer i	70WS?
												Are	the rou	vs orde	ered?
orc	der-by(														
												Proc	duce ti	he re	:SU/1
end															

# My Dataset

What are two ways you might want to order this dataset?
1)
2)
What are two subsets into which you might filter this dataset?
_1)
2)
What are two new columns you might want to build from this dataset?
2)

### Unit 4

- Bar charts show the absolute quantity of each row in a dataset. The larger the
  quantity, the longer the bar. Bar charts provide a visual representation of values
  in a dataset.
- **Pie charts** show the *relative* quantity of each row in a dataset. The greater the percentage, the larger the pie slice. Pie charts provide a visual representation of proportions in a dataset.
- **Choosing a Sample Table** is important when coming up with small examples for Table Plans. A good sample table has:
  - 1. At least all the relevant columns
  - 2. Enough rows to accurately represent the dataset
  - 3. Rows that are randomly-ordered

### Statements about Columns

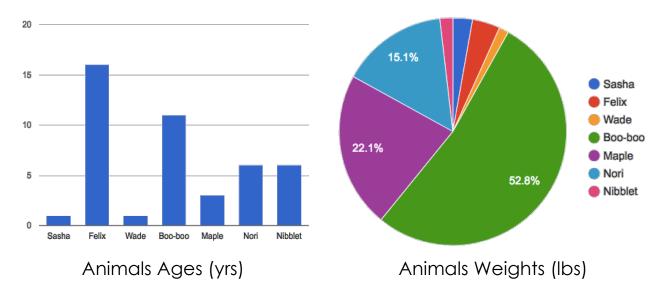
Use the Table below to help you answer the questions.

name	species	age	pounds
Sasha	cat	1	6.5
Felix	cat	16	9.2
Wade	cat	1	3.2
Boo-boo	dog	11	123
Maple	dog	3	51.6
Nori	dog	6	35.3
Nibblet	rabbit	6	4.3

Which animal(s) is/are the heaviest?
 Which animal(s) is/are the youngest?
 How much of the total weight comes from Maple?
 How much of the combined age comes from Nori?
 Would these questions be harder to answer if the table had 100 rows? If so, why?

# Visualizing Quantity

In the table below, there are two observations drawn from the following charts. Add two more.



Based on a chart of	I notice that
Based on a <b>bar chart</b> of 7 animals' ages	Felix is by far the oldest
Based on a <b>pie chart</b> of 7 animals' weights	Boo-boo weighs more than the other six animals combined!
Based on a bar chart of 7 animals' ages	
Based on a <b>pie chart</b> of 7 animals' weights	

Dogs are generally a lot bigger heavier than cats, so the shelter wants to look at a chart of *only* the dogs to determine who needs more exercise time. Define a function pie-dog-weight, which will make a pie chart showing the relative weights of all the dogs in the shelter.

Contract a	nd Pur	oose							
			::				$\rightarrow$		
			_••						
Examples									
	† Table	and a res	ult based on	that table.					
animals-	table	<u>!</u>		$\rightarrow$	pie	e-dog-w	eight	(animal	s-table)
name		weight							
Snowcone		6.1							
Lucky		45.4							
Hercules	•••	13.4							
Toggle	•••	48							
Snuggles		0.1							
Define the	functio	n _							
			cle your help	per function	s!), then pro	oduce a i	result wit	th the new	/ table.
fun			(		):			- 6.	4
<i>t =</i>					<u> </u>			Define	e the table
·								Are there n	nore columns?
								Are there	e fewer rows?
								Are the r	rows ordered?
						<del></del>			
								Produce	the result
end									

## Bad Sample Tables!

For each word problem, a Sample Table must have (1) all the columns that matter, (2) a representative sample of the rows, and be in (3) random order. For each problem below, check the boxes to determine if the Sample Table meets those criteria.

1	The shelter wan	to to know	the median	ago of all	the cate
	me mener wan	IIS IO KIIOW	me median	age or all	me cais,

name	species	age	fixed	legs	pounds	weeks	Relevant columns
Sasha	cat	1	FALSE	4	6.5	3	Representative sample of rows
Mittens	cat	2	TRUE	4	7.4	5	Random order
Sunfower	cat	5	TRUE	4	8.1	10	

#### 2. The shelter wants a pie chart showing all the dogs' weight

name	species	age	ge		
Fritz	dog	4	4		
Wade	cat	2	2		
Nibblet	rabbit	6	6		
Daisy	dog	5	5		

#### 3. Sort all the animals alphabetically by name

name	species	age	fixed	legs	pounds	weeks	Delevent selven
Ada	dog	2	TRUE	4	32	3	<ul><li>Relevant columns</li><li>Representative sample of rows</li></ul>
Во	dog	4	TRUE	4	76.1	10	Representative sample of rows     □ Random order
Boo-boo	dog	11	TRUE	4	123	10	Random oraci

#### 4. Make a bar chart for all the fixed animals

name	species	age	fixed	legs	pounds	weeks	П	Relevant columns
Sasha	cat	1	FALSE	4	6.5	3	П	Representative sample of rows
								Random order

Define a function bar-kitten-adoption, which takes in a Table of animals and creates a bar chart showing how many weeks it took for each kitten to be adopted

Contract and Purpose			
			$\rightarrow$
Examples			
Make a Start Table and a result bo	ased on that table.		
	<i>→</i>		
<b>Define the function</b> Use the relevant methods (circle y	your helper function	nsl) then produce	a result with the new table
ose me relevant memous (enele y	correspondence	ns.,, mon produce	a result with the flew lable.
fun	(	):	
<i>† =</i>			Define the table
·			Are there more columns?
			Are there fewer rows?
	··		Are the rows ordered?
			 Produce the result
end			,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,

Contract and Purpos	е					
	::				<i>&gt;</i>	
<b>Examples</b> Make a Start Table and	d a rosult base	d on that	table			
Make a start table and	a resuit base	a on mai	idble.			
			$\rightarrow$			
Define the function						
Use the relevant metho	ods (circle you	r helper fu	nctions!)	, then proc	luce a resul	t with the new table.
		/	,	`		
_						Define the table
<u>† =</u>						_ Are there more columns?
						_ Are there fewer rows?
						_ Are the rows ordered?
						Produce the result
 end						_ Froduce The result
= =						

Contract and Purp	ose					
	* * *				_ > _	
Examples						
Make a Start Table c	and a result bas	sed on that to	able.			
			<b>→</b>			
Define the function						
Use the relevant me		our helper fur	nctions!),	then produc	ce a result	with the new table.
fun		(	)	:		Define the table
<u>† =</u>						
						Are there more columns?
						Are there fewer rows?
						Are the rows ordered?
						Produce the result
end						

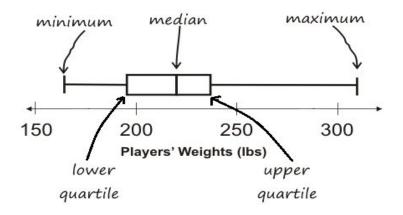
# Visualizing My Dataset

What quantity charts did you make, and what do you notice? Fill in the table below.

Based on a chart of	I notice that
·	

#### Unit 5

- There are three ways to measure the "center" of a dataset, to talk about a whole column of data using just one number:
  - 1. The **mean** of a dataset is the average of all the numbers
  - 2. The **median** of a dataset is a value that is smaller than half the dataset, and larger than the other half
  - 3. The **modes** of a dataset are the numbers that appear the most often.
- Data Scientists can also measure the "variation" of a dataset using a **five number summary:** 
  - 1. The **minimum** the smallest value in the dataset
  - 2. The **first**, **or** "**lower**" **quartile (Q1)** the median value that separates the first quarter of the values in the dataset from the second quarter
  - 3. The **second quartile (Q2)** the median value which separates the entire dataset into "top" and "bottom" halves.
  - 4. The **third**, **or "upper" quartile (Q3)** the median value that separates the third quarter of the values in the dataset from the fourth quarter
  - 5. The **maximum** the largest value in the dataset
- The five number summary can be used to draw a box-and-whisker plot.



# Summarizing Columns in Animals

The column I cho	ose to measure i	s <u>weeks</u>					
Measures of Center The three measures for this column are:							
Mean (Ave	rage)	Median	٨	Mode(s)			
Based on the diffe	erences betwee	n mean and medic	an, I conclude :				
		easures of Variati					
Minimum	Q1	Q2 (Median)	Q3	Maximum			
A box plot can be drawn from this summary on the number line below:							
From this summary and box-plot, I conclude:							

#### Table Plan

The shelter wants a summary of the variation in ages among the dogs. Write a function called variation-dog-age that will take in a table of animals produce a box-plot that shows this variation.

Contract	and Purpo	ose																
			::								$\rightarrow$	•						
											_							
Example	\$																	
Make a St	art Table a	nd a	result b	asec	on the	at tab	ole.											
animals	-table						$\rightarrow$	vai	riati	ion-	-dog	-ag	e (	an	ima	ls-	<u>tabl</u>	e)
name	species	age	fixed	legs	weight	adopt	t											
Snowcone	cat	2	TRUE	4	6.1	5												
Lucky	dog	3	TRUE	3	45.4	9												
Hercules	cat	3	FALSE	4	13.4	7												
Toggle	dog	3	TRUE	4	48	3												
Snuggles	tarantula	2	FALSE	8	0.1	1												
	e function							1) 11		1		- 11	• • • •					
Use the re	levant met	hods	(circle	your	helper	tunct	tions	!), the	en prod	duce	e a re	sult v	∕∕ITI	n th	e ne	w tak	ole.	
					,			`										
					_ (			_):						D	efii	ne th	ne tak	ole
<u>† =</u>																		
bu	ild-column	<u> </u>											1	1re	there	more	colum	ns?
.fil	ter(											)		Ar	e the	re fev	ver roi	NS?
	der-by(													Ar	e the	rows	ordere	2d?
														Pro	duc	e the	e resi	u/t
end	-																	

#### Interpreting Variation

Consider the following list dataset, representing the annual income of ten people:

\$65k, \$12k, \$14k, \$280k, \$15k, \$22k, \$45k, \$34k, \$45k, \$175k

1. In the space below, rewrite this dataset in **sorted order**.

2. In the table below, compute the measures of center for this dataset.

Mean (Average)	Median	Mode(s)

3. In the table below, compute the **five number summary** of this dataset.

Minimum	Q1	Q2 (Median)	Q3	Maximum

4. On the number line below, draw a **box plot** for this dataset.

5. The following statements are correct...but misleading. Write down the reason why.

### Statement Why it's misleading

"The average person makes more than \$70k dollars!"

"The most common salary is \$45k/yr!"

"This group is really diverse, with people making as little as 12k and as much as \$280k!"

# Summarizing a Column in My Dataset

The column I cho	ose to measure	is		
		Measures of Center measures for this c		
Mean (Ave	rage)	Median	٨	Mode(s)
Based on the diffe	erences betwee	en mean and medic	an, I conclude :	
		<b>Neasures of Variat</b> five-number summe		
Minimum	Q1	Q2 (Median)	Q3	Maximum
A box plot can be	e drawn from th	is summary on the r	number line belov	v: •
From this summar	y and box-plot,	I conclude:		

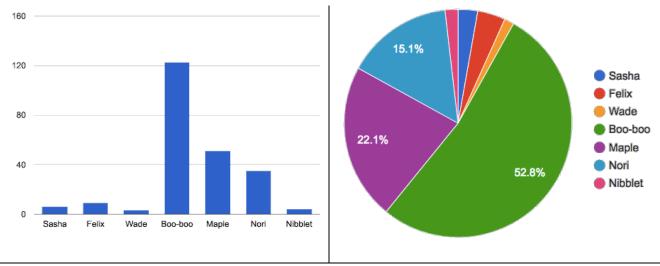
#### Unit 6

- Frequency Bar charts show the number of rows belonging to a given category. The more rows in each category, the longer the bar. Frequency bar charts provide a visual representation of the frequency of values in a categorical column. Since categorical data cannot be ordered, there is no strict ordering of bars in a frequency bar chart.
- Histograms show the number of rows that fall within certain ranges, or "bins" of a
  dataset. The more rows that that fall within a particular "bin", the longer the bar.
  Histograms provide a visual representation of the frequency of values in a
  quantitative column. Quantitative data can be ordered, so the bars of a
  histogram are always sorted.
- When dealing with histograms, it's important to select a good **bin size**. If the bins are too small or too large, it is difficult to see the distribution in the dataset.



## Visualizing Quantity (Review)

Use the charts below to help you answer the questions.



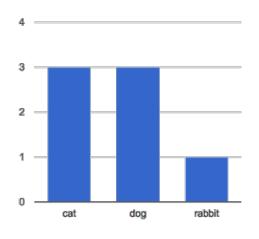
Animals Weights (lbs)

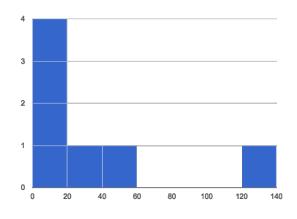
- 1. Which animal is the heaviest?
- 2. Which animal is the lightest?
- 3. How much of the total weight comes from Maple? \_\_\_\_\_\_
- 4. How much of the total weight comes from Nori?
- 5. Which chart did you use for questions 1 and 2?
- 6. Which chart did you use for questions 3 and 4?
- 7. Why are some questions easier to answer with one kind of chart or another?

#### Visualizing Frequency

name	species	age	pounds
"Sasha"	"cat"	1	6.5
"Boo-boo"	"dog"	11	123
"Felix"	"cat"	16	9.2
"Nori"	"dog"	6	35.3
"Wade"	"cat"	1	3.2
"Nibblet"	"rabbit"	6	4.3
"Maple"	"dog"	3	51.6

- 1. How many cats are there?
- 2. How many dogs are there?
- 3. How many animals are between 3-6 years old?
- 4. How many weigh between 0-5 pounds?
- 5. Are there more animals weighing 0-5 than 6-10 pounds?
- 6. The charts below are based on the Sample Table above. What is each one measuring? Write down your guess underneath each one.





#### Table Plan

Define a function freq-bar-gender, which takes in a Table of animals and creates a frequency bar chart showing how many animals are male v. female.

Contract and Purpose				
	::		$\rightarrow$	
		<del></del>	<del></del>	
Examples				
Make a Start Table and c	result based on tha	t table.		
	-	_		
	_			
Define the function				
Use the relevant method	s (circle your helper t	functions!), ther	n produce a resu	ult with the new table.
fun	(	):		Define the table
<u>† =</u>				_
				Are there more columns?
				Are there fewer rows?
				Are the rows ordered?
				Produce the result
end				

#### Table Plan

Define a function histogram-adoption, which takes in a Table of animals and creates a histogram showing how long it took for animals to get adopted

<b>Contract and Purpo</b>	se					
	::				$\rightarrow$	
Examples						
Make a Start Table ar	nd a result based	on that tak	ole.			
			<b>→</b> _			
<b>Define the function</b> Use the relevant meth	nods (circle vour	helper func	ctions!), th	nen produc	e a result v	with the new table.
fun		(	):			
						Define the table
						Are there more columns?
						Are there fewer rows?
						Are the rows ordered?
						Produce the result
end						

Visualizing My Dataset

What frequency charts did you make, and what do you notice? Fill in the table below.

Based on a chart of	I notice that

# Matching Charts to Questions

For each of the questions below, draw a line to the chart that will best answer it.

	Are there more of the animals at the shelter fixed or unfixed?	1.
Pie Chart	How many weeks did each cat wait to be adopted?	2.
Bar Chart	How many male v. female dogs are there?	3.
bui Ciluii	How many animals have 4 legs? 8? 3?	4.
Frequency Bar Chart	What percent of the total weight at the shelter is made up by Boo-boo?	5.
	What is the distribution of weights across all the animals older than 3?	6.
Histogram	How many animals are there of each species?	7.
	Who waited the longest to be adopted?	8.

#### Unit 7

- **Scatter Plots** show the relationship between two quantitative columns. Each row in the dataset is represented by a point, with one column providing the x-value and the other providing the y-value. The resulting "point cloud" makes it possible to look for a relationship between those two columns.
- If the points in a scatter plot appear to follow a pattern, it is possible that a relationship or **correlation** exists between those two columns.
- If there is a pattern to the points in a scatter plot, points that are far away from the pattern are called **outliers**.
- We can express this correlation by drawing line through the data cloud, so that
  the distance between the line and each of the points is as small as possible. This
  line is called the line of best fit or predictor function and allows us to make
  predictions based on the dataset.

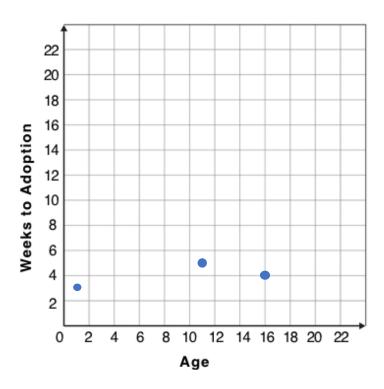
# (Dis)Proving a Claim

## "Younger animals are cuter, so they get adopted faster."

Do you agree? If so, why?
I hypothesize
What would you look for in the dataset to see if you are right?

#### Creating a Scatter Plot

name	species	age	weeks
"Sasha"	"cat"	1	3
"Boo-boo"	"dog"	11	5
"Felix"	"cat"	16	4
"Buddy"	"lizard"	2	24
"Nori"	"dog"	6	9
"Wade"	"cat"	1	2
"Nibblet"	"rabbit"	6	12
"Maple"	"dog"	3	2



- 1. For each row in the Sample Table on the left, add a point to the scatter plot on the right. The first 3 rows have been completed for you. Use the values from the age column for the x-axis, and values from the weeks column for the y-axis.
- 2. Do you see a pattern? Do the points seem to shift up or down as age increases? **Draw a line on the scatter plot to show this pattern**.
- 3. Does the line slope upwards or downwards?
- 4. Are the points mostly close to the line?

#### Table Plan

Define a function <code>dogs-age-weeks</code>, which takes in a Table of animals and creates a scatter plot of all the dogs, tracking their <code>age</code> on the x-axis and the number of <code>weeks</code> it took for them to be adopted on the y-axis.

Contract and Purpose				
	::			$\rightarrow$
Examples				
Make a Start Table and	a result based on	that table.		
		,		
		→		
Define the function				
	ds (circle your help	per functions!)	, then produce (	a result with the new table.
fun	(	)	) :	Define the table
				<u>Define the table</u>
				Are there more columns?
				Are there fewer rows?
				Are the rows ordered?
				Produce the result
end				

## **Drawing Predictors**

For each of the scatter plots below, draw a **predictor line** that fits best.



# Correlations in My Dataset

1) There may be a correlation between		and
•	column	
I think it is a		
Column	strong / weak	positive / negative
correlation, because		
	It would	d be stronger it I looked
at		
a     subset	or extension of my da	ata
1) There may be a correlation between		and
	column	arra
I think it is a		
column	strong / weak	positive / negative
correlation, because		
	It would	d be stronger if I looked
at		
ata subset	or extension of my da	ata
1) There may be a correlation between		and
T) There may be a concidion between	column	and
I think it is a		
I think it is a	strong / weak	positive / negative
correlation because		
correlation, because		
	It would	d be stronger if I looked
at		
ata subset	or extension of mv da	ata

#### Unit 8

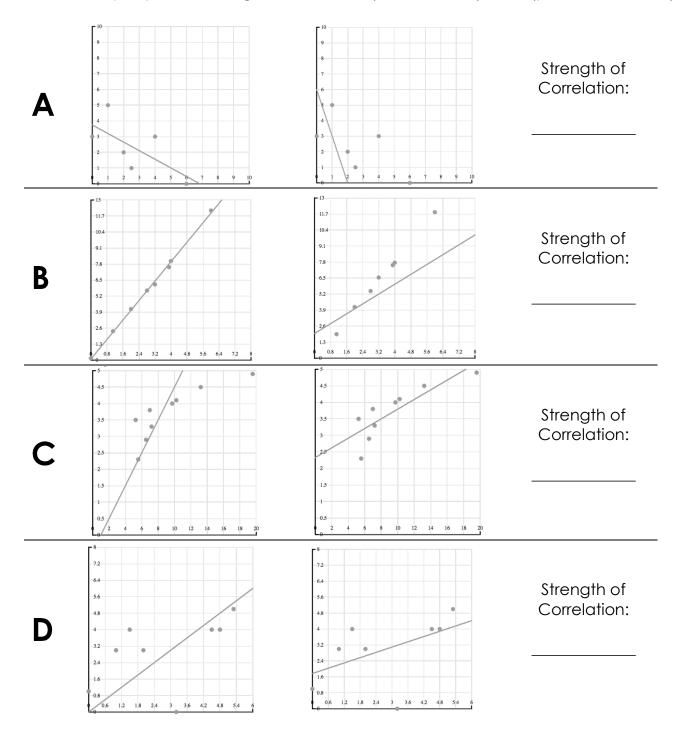
- Given a **predictor function** and a scatter plot, we can compute the error by adding the squares of all the distances between the function and each point in the plot. The error is called the **r**<sup>2</sup> **statistic**, which tells us how much of the variation in the y-axis can be explained by the x-axis.
- A strong correlation will have a large r<sup>2</sup>. A weak correlation will have a small r<sup>2</sup>.
- A **positive correlation** means the slope of the line of best fit is positive. A **negative correlation** means the slope is negative.
- **Linear Regression** is a way of computing the **line of best fit**, by taking a scatter plot and deriving the slope and y-intercept for a line that has the smallest possible r<sup>2</sup>.
- <u>Correlation is not causation!</u> Correlation only suggests that two measures are related, but does not tell us if one causes the other. For example, hot days are correlated with people running their air conditioners, air conditioners do not cause hot days!

_
_
_
_
_
_
_
_
_
_
_
_
_
_
_
_
_

## **Grading Predictors**

Below are the scatter plots for data sets A-D, with two different lines predictor lines drawn on top. For plots A-D:

- 1. Circle the plot with the line that fits better
- 2. Give the plot you circled a grade between 0 (no correlation) and 1 (perfect correlation)



# Findings in the animals Dataset

I performed a linear	r regression on	dog	is at the shelter	, and
•	-		dataset or subset	
found	a weak (r²=	0.25), positive	correlation I	petween
	_	weak ( $r^2=$ ), posit	_	
		and <b>number</b>	of weeks to be adopted	$\underline{\underline{I}}$ . From this, I
conclude that	25% of the	variability in ad	<pre>[y-axis] option time is explained is explained by [x-axis]</pre>	
	r <sup>2</sup> % of the varia	tion in [y-axis]	is explained by [x-axis]	
by the age of the	e dog			
I performed a linear	r regression on			, and
•	· —		dataset or subset	
found			correlation I	between
			correlation I	
		and	[y-axis]	From this, I
[x-a	ixis]		[y-axis]	
conclude that			is explained by [x-axis]	
	$r^2$ % of the varia	tion in [y-axis]	is explained by [x-axis]	
I performed a linear	r regression on			, and
•			dataset or subset	
found			correlation I	between
	a strong/	weak $(r^2=)$ , posit	cive/negative	
		and	[y-axis]	From this, I
[x-a	axis]		[y-axis]	
conclude that			is explained by [x-axis]	
	r <sup>2</sup> % of the varia	tion in [y-axis]	is explained by [x-axis]	

# Correlations in My Dataset

I performed a line	ear regressi	on on					, and
					dataset o	or subset	
found						_ correlation	between
		a strong/weak	$(r^2=)$ ,	positive	/negative		
		ar	nd				From this
[:	x-axis]			[ À-9	axis]		
conclude that _							
	r² % of	the variation	in [y-ax	kis] is e	xplained	by [x-axis]	
I performed a line	ear rearessi	on on					. and
. 10 0	· · · · · · · · · · · · · · · · · ·					or subset	,
found						correlation	between
found		a strong/weak	(r <sup>2</sup> =),	positive	/negative		
		ar	nd				From this
[:	x-axis]			[ À-9	axis]		
conclude that _							
conclude that _	r <sup>2</sup> % of	the variation	in [y-ax	kis] is e	xplained	by [x-axis]	
I performed a lin	ear rearessi	on on					and
r perrennea a mi	o an 10 gi o ssi				dataset o		, and
found						_ correlation	between
		a strong/weak	(r <sup>2</sup> =),	positive	/negative	001101011011	201110011
		ar	nd				. From this
[:	x-axis]			[y-a	axis]		From this
conclude that							
conclude that _	r² % of	the variation	in [y-ax	kis] is e	xplained	by [x-axis]	

# Unit 9

#### Fake News!

**Every claim below is wrong!** Your job is to figure out why, by looking at the data.

	Data	Claim	Why it's wrong
1	The average player on a basketball team is 6'1".	"Most of the players on the team are taller than 6'."	Wily it's wiong
2	After performing linear regression on census data, a positive correlation (r <sup>2</sup> =0.18) was found between people's height and salary.	"Taller people get paid more."	
3	y=12.234x + -17.089; r-sq: 0.636	"According to the predictor function indicated here, the value on the x-axis is will predict the value on the y-axis 63.6% of the time."	
4	15  Sasha Felix Wade Boo-boo Maple Nori Bar Chart of Pet Ages	"According to this bar chart, Felix makes up a little more than 15% of the total ages of all the animals in the dataset."	
5	4	"According to this histogram, most animals weigh between 40 and 60 pounds."	
6	After performing linear regression, a negative correlation (r <sup>2</sup> =0.91) was found between the number of hairs on a person's head and their likelihood of owning a wig.	"Owning wigs causes people to go bald."	

# Blank Recipes, Table Plans, and References

# Design Recipes

name       domain       rang         amples:       () is		::		$\rightarrow$	
() is() is d n() :	name		domain		range
() is	mples:				
d() is		(	) is		
d () :		(			
	<b>d</b>	<b>\</b>			
d	n	(	) :		
	d				
		::			
	name		domain		range
name domain rang	amples:	<del> </del>			<del></del>
name domain rang	•		_		
name domain rang		(	) is		
name domain rang		(	) is		
name domain rang	d				
name domain rang  amples:() is	ın	(	) :		
name domain rang  amples:() is() is d					
name       domain       range         amples:       () is	nd				

# Design Recipes

	::		$\rightarrow$	
name		domain		range
mples:				
	(	) is		
	(			
	· · · · · · · · · · · · · · · · · · ·			
	(	) :		
	<b>::</b>		>	
name		domain		range
mples:				
	,	) is		
	\	) is		
	(	) is		
	(	) :		
l				
A.				

# Design Recipes

	::		$\rightarrow$	
name		domain		range
mples:				
	(	) is		
	(			
	· · · · · · · · · · · · · · · · · · ·			
	(	) :		
	<b>::</b>		>	
name		domain		range
mples:				
	,	) is		
	\	) is		
	(	) is		
	(	) :		
l				
A.				

#### Table Plan

Contract and Purpose				
	::			$\rightarrow$
Examples				
Make a Start Table and c	result based on tho	at table.		
		$\rightarrow$		
		_ ′		
Define the function				
Use the relevant method	s (circle your helper	functions!)	, then produce	a result with the new table.
	,			
	(		):	Define the table
<u>† =</u>				 Are there more columns?
				Are there fewer rows?
				Are the rows ordered?
				<del></del>
				<u>Produce the result</u>
end				

Table Plan

Contract and Purpose				$\rightarrow$	
	··			_ ~ -	
<b>Examples</b> Make a Start Table and c	result based on the	at table			
Make a start table and c	rresun basea on inc	ai iable.			
		_ >			
Define the function					
Use the relevant method	s (circle your helper	functions!),	then produ	ce a result	with the new table.
fun	(	)	•		
<u>† =</u>					Define the table
					Are there more columns?
					Are there fewer rows?
					Are the rows ordered?
					Produce the result
end					

## Table Plan

Contract and Purpose				
Confider and Forpose	::			$\rightarrow$
				_ ,
<b>Examples</b> Make a Start Table and c	result based on tha	t table		
Make a start table and e	rreson basea on ma	riddic.		
		_ <b>→</b>		
		_		
Define the function				
Use the relevant method:	s (circle your helper f	functions!),	then produce	e a result with the new table.
	(			Define the table
<u>† =</u>				Are there more columns
				Are there fewer rows
				Are the rows ordered
end				<u>Produce the resul</u>

## Contracts

Name	Domain		Range
triangle	:: (side :: Number, style :: String, color :: String)	$\rightarrow$	Image
circle	:: (radius :: Number, style :: String, color :: String)	$\rightarrow$	Image
star	:: (radius :: Number, style :: String, color :: String)	$\rightarrow$	Image
rectangle	:: (width :: Num, height :: Num, style :: Str, color :: Str)	$\rightarrow$	Image
ellipse	:: (width :: Num, height :: Num, style :: Str, color :: Str)	$\rightarrow$	Image
square	:: (size :: Number, style :: String, color :: String)	$\rightarrow$	Image
text	:: (str :: String, size :: Number, color :: String)	$\rightarrow$	Image
overlay	:: (img1 :: <i>Image</i> , img2 :: <i>Image</i> )	$\rightarrow$	Image
rotate	:: (degree :: Number, img :: Image)	$\rightarrow$	Image
scale	:: (factor :: Number, img :: Image)	$\rightarrow$	Image
string-repeat	:: (text :: String, repeat :: Number)	$\rightarrow$	String
string-contains	:: (text :: String, search-for :: String)	$\rightarrow$	Boolean
num-sqr	:: (n :: Number)	$\rightarrow$	Number
num-sqrt	:: (n :: Number)	$\rightarrow$	Number
num-min	:: (a :: Number, b:: Number)	$\rightarrow$	Number
num-max	:: (a :: Number, b:: Number)	$\rightarrow$	Number
get-row	:: (t :: Table, index :: Number)	$\rightarrow$	Row

## Contracts

Name	Domain		Range
<table>.row-n</table>	:: (n :: Number)	$\rightarrow$	Row
<table>.order-by</table>	:: (col :: String, increasing :: Boolean)	$\rightarrow$	Table
<table>.filter</table>	:: (test :: (Row → Boolean) )	$\rightarrow$	Table
<table>.build-column</table>	:: (col :: String, builder :: (Row → Value) )	$\rightarrow$	Table
mean	$:: (\underline{t} :: Table, col :: String)$	$\rightarrow$	Number
median	:: (t :: Table, col :: String)	$\rightarrow$	Number
modes	:: (t :: Table, col :: String)	$\rightarrow$	List <number></number>
bar-chart	:: (t :: Table, labels :: String, values :: String)	$\rightarrow$	Image
pie-chart	:: (t :: Table, labels :: String, values :: String)	$\rightarrow$	Image
box-plot	:: (t :: Table, col:: String)	$\rightarrow$	Image
freq-bar-chart	:: (t :: Table, values :: String)	$\rightarrow$	Image
histogram	:: (t :: Table, values :: String, bin-width :: Number)	$\rightarrow$	Image
scatter-plot	:: (t :: Table, xs :: String, ys :: String)	$\rightarrow$	Image
labeled-scatter-plot	:: (t :: Table, labels :: String, xs :: String, ys :: String)	$\rightarrow$	Image
lr-plot	:: (t :: Table, xs :: String, ys :: String)	$\rightarrow$	Image
labeled-lr-plot	:: (t :: Table, labels :: String, xs :: String, ys :: String)	$\rightarrow$	Image