





Workbook v1.1

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### Unit 1

- Many important questions ("what's the best restaurant in town?", "is this law good for citizens?", etc.) are answered with data. Data Scientists try and answer these questions, by writing programs that ask questions of data.
- Data of all types can be organized into **Tables**
- Every Table has a **header row**, and some number of **data rows**
- **Quantitative data** is data usually numeric that measures *quantity*, such as a person's height, a score on test, a measure of distance, etc. A list of quantitative data can be ordered from smallest to largest.
- Categorical data is data that specifies categories, such as eye color, country of origin, etc. A list of categorical data has no notion of "smallest" or "largest", and cannot be ordered.
- **Programming languages** involves different *datatypes*, such as Numbers, Strings, Booleans and Images.
- Operators (like +, -, \*, <, etc.) are written between values. For example: 4 + 2
- Functions (like triangle, star, string-repeat, etc.) are written first, followed by a list of arguments in parentheses. For example: star(50, "solid", "red")
- **Examples** help programmers reason about their code. Every example contains two expressions, and the example "passes" if both expressions evaluate to the same thing. For example: 4 + 2 is 6, or "cat" == "dog" is false

### Numbers and Strings

Make sure you've loaded the Unit 1 Starter File, and clicked "Run".

- 1. Try typing 42 into the Interactions Area and hitting "Enter". What happens?
- 2. Try typing in other Numbers. What happens if you try a decimal like 0.5? A fraction like 1/3? Try really big Numbers, and really small ones.
- 3. String values are always in quotes. Try typing your name (in quotes!). What happens when you hit "Enter"?
- 4. Try typing your name with the opening quote, but without the closing quote. What happens? Now try typing it without any quotes.
- 5. Is 42 the same as "42"? Why or why not? Write your answer below:

### **Operators**

- 6. Just like in math, Pyret has operators like + and -. Try typing in 4 + 2, and then 4+2 (without the spaces). What can you conclude from this? Write your answer below:
- 7. Try typing in 4+2+6, 4+2\*6, and 4+(2\*6). What can you conclude from this? Write your answer below:
- 8. Try typing in 4 + "cat", and then "dog" + "cat". What can you conclude from this? Write your answer below:

### Booleans

Boolean expressions are yes-or-no questions, and will always evaluate to either true ("yes") or false ("no"). What will each of the expressions below evaluate to? Write down the result in the blanks provided, and type them into Pyret if you're not sure.

3 <= 4	 "a" > "b"	
3 == 2	 "a" <> "b"	
2 <> 4	 "a" == "b"	
3 <> 3	 "a" <> "a"	

### **Boolean Operators**

Pyret also has operators that work on *Booleans*. For each expression below, write down your guess about what it will evaluate to. Then type them in and see if you were right!

$$(3 \le 4)$$
 and  $(3 == 2)$ 
 $("a" == "b")$  and  $(3 <> 4)$ 
 $(3 <= 4)$  or  $(3 == 2)$ 
 $("a" == "b")$  or  $(3 <> 4)$ 

- How many different Number values are there in Pyret?
  \_\_\_\_\_\_
- 2. How many different String values are there in Pyret?
- 3. How many different Boolean values are there in Pyret? \_\_\_\_\_

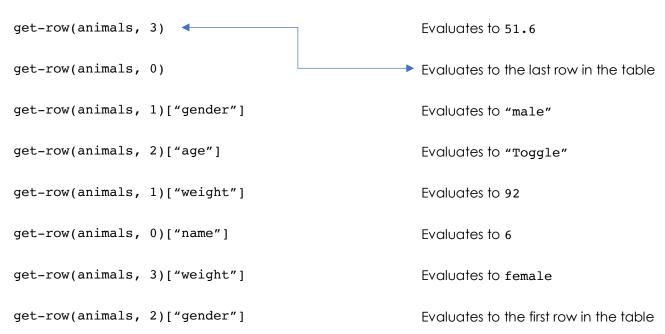
### Playing with Tables

The table below represents four animals at the shelter:

#### animals

name	gender	age	weight
"Toggle"	"female"	3	48
"Fritz"	"male"	4	92
"Nori"	"female"	6	35.3
"Maple"	"female"	3	51.6

1) Match each Pyret expression (left) to the description of what it does (right).



2) Fill in the blanks (left) with the Pyret code that will produce the value (right).

a. get-row(animals, 3)["name"]	"Mapie" —
b.	male
_c.	4
d.	48
e.	- "Nori"

### Writing Examples

In the examples block below, put an "X" next to the examples that will <u>fail</u>.
 Remember: examples only pass if the left- and right-hand expressions evaluate to the same thing!

```
examples:
    1 + 2 + 9
    num-sqrt(16)
    is 2 + 2
    3 > 99
        is true
    square(10, "solid", "red")
end

is rectangle(10, 10, "solid", "red")
end
```

2. In the examples block below, fill in the blank on the right-hand side so the example will <u>pass</u>.

3. The examples block below refers to the shapes table on the right, using row-accessors and the get-row function. For each example, fill in the blank so the example will pass.

name	corners	Is-round
"triangle"	3	false
"circle"	0	true
"ellipse"	0	true
"square"	4	false

# Unit 2

• Notes go here



### The Animals Dataset

- 1. This dataset is Animals from an animal shelter
- 2. The columns are....
  (For each column in this dataset, fill out the datatype, and whether it contains Qualitative or Categorical data in the table below)

name	species	gender	age	fixed	pounds	weeks
"Sasha"	"cat"	"female"	1	false	6.5	3
"Toggle"	"dog"	"female"	3	true	48	1
"Boo-boo"	"dog"	"male"	11	true	123	24
"Snuggles"	"tarantula"	"female"	2	false	.01	1
"Nori"	"dog"	"female"	6	true	35.3	1
"Snowcone"	"cat"	"female"	2	true	6.1	5
Datatype						
Quantitative or Categorical?						

3.	For the questions below, check the box next to the questions you <u>COULD</u> answer
	given this dataset:
	☐ How old is Boo-boo?
	☐ What color is Snowcone's fur?
	☐ What is the average age of all the animals in the shelter?
	Are there more fixed or unfixed animals at the shelter?
	Are families with children more likely to adopt kittens?
4.	Some questions I have about this dataset:

#### What Questions Can You Answer?

The following is a dataset of a bicycle rider's training rides.

date	miles	time	weather	average speed	max speed
04/10/2018	10	44	"cloudy"	13	30
05/30/2018	15	66	"sunny"	13.5	22
06/12/2018	12	61	"rainy"	11.2	25
06/22/2018	15	61	"cloudy"	13	28
07/04/2018	24	103	"sunny"	14	26
07/12/2018	24	120	"windy"	12.5	26

For the questions below, check the box next to the questions you <u>COULD</u> answer given this dataset:

What is the cyclist's average speed across all rides?
 How many miles did they ride in June?
 What is the tallest hill this cyclist climbed?
 Does this cyclist ride slower when it is rainy?
 Does this cyclist ride faster when they are late to an appointment?

For the questions below, check the box next to the questions you <u>COULD NOT</u> answer given this dataset:

- What tire pressure produces the highest average speed?
   What is the average time it takes this cyclist to ride one mile?
   Does this cyclist ride more in April or July?
- □ What is the average temperature while this cyclist is riding?
- ☐ How many flat tires did this cyclist fix in June?

### Threats to Validity

Some volunteers from the animal shelter surveyed a group of pet owners at a local park. They found that almost all of the owners were there with their dogs, and from this survey they concluded that dogs are the most popular pet in the region.

What are some possible threats to the validity of this conclusion?
The animal shelter noticed a large increase in pet adoptions between Thanksgiving and New Year's Eve. They conclude that at this current rate, there will be a huge demand for pets between January and April.  What are some possible threats to the validity of this conclusion?

### Threats to Validity

The animal shelter wanted to find out what kind of food to buy for their animals. They took a random sample of two animals and the food they eat, and found that spider and rabbit food was by far the most popular cuisine!

What are some possible threats to the validity of this conclusion?
A volunteer opens the shelter in the morning and walks all the dogs. At mid-day, another volunteer feeds all the dogs and walks them again. In the evening, a third volunteer walks the dogs a final time, and closes the shelter. The volunteers report that the dogs are much friendlier and more active at mid-day, so the shelter staff assume the second volunteer must be better with animals then the others.  What are some possible threats to the validity of this conclusion?

## My Dataset

1. My dataset is \_\_\_\_\_

2.	(Cop	e of my columns y six columns from y ains Qualitative or C	our dataset, a			s datatype, aı	nd whether	it
		Datatype						
		Quantitative or Categorical?						
3.	Som	e questions I hav	ve about this	s dataset:				
4.	Wha	t are some poss	ible threats t	o validity yo	u may enc	ounter in yo	our analys	isŞ

### Unit 3

- Programming languages let us define our own function.
- We use the **Design Recipe** to help us define functions without making mistakes.
- The first step is to write a **Contract** and **Purpose Statement** for the function, which specify the Name, Domain and Range of the function and give a summary of what it does.
- The second step is to **write at least two examples**, which show how the function should work for specific inputs. These examples help us see patterns, and we express those patterns by **circling and labeling** what changes.
- The final step is to **define the function**, which generalizes our examples.

### The Design Recipe

Define a function called is-fixed, which tells us whether or not an animal is fixed

	is-fixed	::	(animal :: Row)		Boolean
	name		domain		range
# <u>Co</u>	nsumes an animo	al, and produ	ces the value in th	e fixed column	<del> </del>
exan	mples:				
	is-fixed	(sasi	na) is	sasha["f	ixed"]
		(	) is		
end					
fun		(	) :		
end					
	e a function cal ender of that ar		which consumes	a Row of the an	imals table tells us
		::		$\rightarrow$	
#	name		domain		range
exan	mples:				
		(	) is		
-		(	) is		
end					
fun		(	) :		
end					

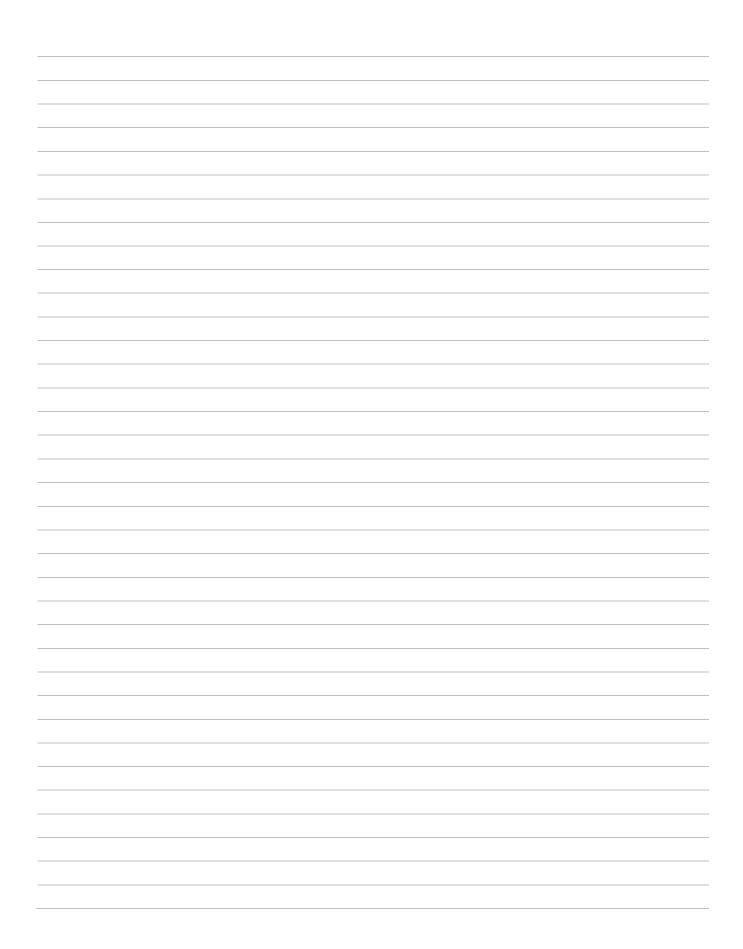
Define a function called is-cat,	which consumes a	Row of the	animals t	table d	and
produces true if it's a cat.					

	is-cat	<b>::</b>	(animal :: Row)		Boolean
	name		domain		range
# Col	nsumes an anim	al, and returi	n true if the species	is "cat"	
exam	ples:				
	is-cat	(sash	<u>a</u> ) is		
		(	) is		
end					
fun		(	) :		
end					
			ag, which consumes at is less than two yo	ears old.	iliiliidis lable alla
		::		<del>-</del>	
#	name		domain		range
exam	ples:				
		(	) is		
		(	) is		
end					
fun	· <del></del>	(	) :		
end					

Def	ne a function cal	led nameta	g, prints out each anin	nal's name in	big red letters.
	nametag	::	(animal :: Row)	>	Image
	name		domain		range
# (	Consumes an anima	al, and produ	uces an image of their i	name in big, re	ed letters
ex	amples:				
	nametag	( <i>sas</i>	<u>'ha</u> ) <b>is</b>		
		(	) is		
en	đ				
fu	n	(	) :		
en	đ				
			ten, which consumes er than two years old.	a Row of the	animals table and
		::		$\rightarrow$	
#	name		domain		range
ex	amples:				
		(	) is		
		(	) is		
en					
fu	n	(	) :		
en	đ				

### Unit 4

- Methods are special functions that are attached to pieces of data. We use them to manipulate Tables.
- They are different from functions in several ways:
  - 1. Their names can't be used alone: they can only be used as part of data, separated by a dot. (For example, animals.order-by)
  - 2. Their contracts are different: they include the type of the data as part of their names. (eg, .order-by :: (column :: String) > Table)
  - 3. They have a "secret" argument, which is the data they are attached to
- We will use three **Table Methods** to manipulate our datasets:
  - 1. <Table>.order-by order the rows of a table based on a column
  - 2. <Table>.filter create a subset of the data, with only certain rows
  - 3. <Table>.build-column use the columns of a table to compute a new one



# Reviewing Functions

١.	One of the examples for the last function is broken! Fix this examples for the last function is broken! Fix this examples for the last function is broken! Fix this examples for the last function is broken!	mple in the
2.	How many values are defined in this file?	
3.	How many functions are defined in this file?	
4.	What is the name of the last function?	
5.	What is the Domain of the last function?	
6.	What is the Range of the last function?	
7.	What is the variable name that the last function uses?	
8.	Which function will tell us if an animal is a kitten?	
9.	Which function will print out " <name> the <species>"?</species></name>	
10	.Which function will tell us if an animal is a dog older than 10?	
11	.Which function will tell us if an animal has been fixed?	
12	.Which function will draw a nametag for an animal?	

### Plans for the Animals Dataset

What are two ways you might want to order the animals dataset?
1)
2)
What are two subsets into which you might filler the animal adapted?
What are two subsets into which you might filter the animals dataset?
1)
2)
What are two new columns you might want to build from the animals dataset?
1)
2)

#### Methods

Methods are a lot like functions, but they differ in three important ways:

- They can only be called as **part of a value**, using the **dot-accessor**. For example: **animals.**row-n(2)
- Their Contracts are different, because they contain a **Type** as part of their name. For example: <**Table>.**row-n :: (index :: Number) -> Row
- They have a "secret argument", which is the value they are attached to. In the examples above, the row-n method consumes only a Number as part of its Domain, but it also consumes the Table to which it is attached.

Here is the Contract for a method, which consumes the name of a food and produces True if the person likes that food:

	<person>.likes :: (food :: String) → Boolean</person>
1.	What Type of data is the method attached to?
2.	What is the name of this method?
3.	How many things are in its Domain?
4.	What is the name of the argument in its Domain?
5.	What is the Type of the argument in its Domain?
6.	What Type of data will this method will produce?
7.	Below are 3 expressions. Based on the contract above, circle the correct one
	emma.likes("pizza") likes("pizza") likes(emma, pizza)

8. On the line below, write your own expression that uses this method, replacing emma and "pizza" with your own name and a food you like.

### Playing with Methods

You have the following functions defined below (read them carefully!):

```
fun is-fixed(animal): animal["fixed"] end
fun is-young(animal): animal["age"] < 4 end
fun nametag(animal): text(animal["name"], 20, "red") end</pre>
```

The table **t** below represents four animals at the shelter:

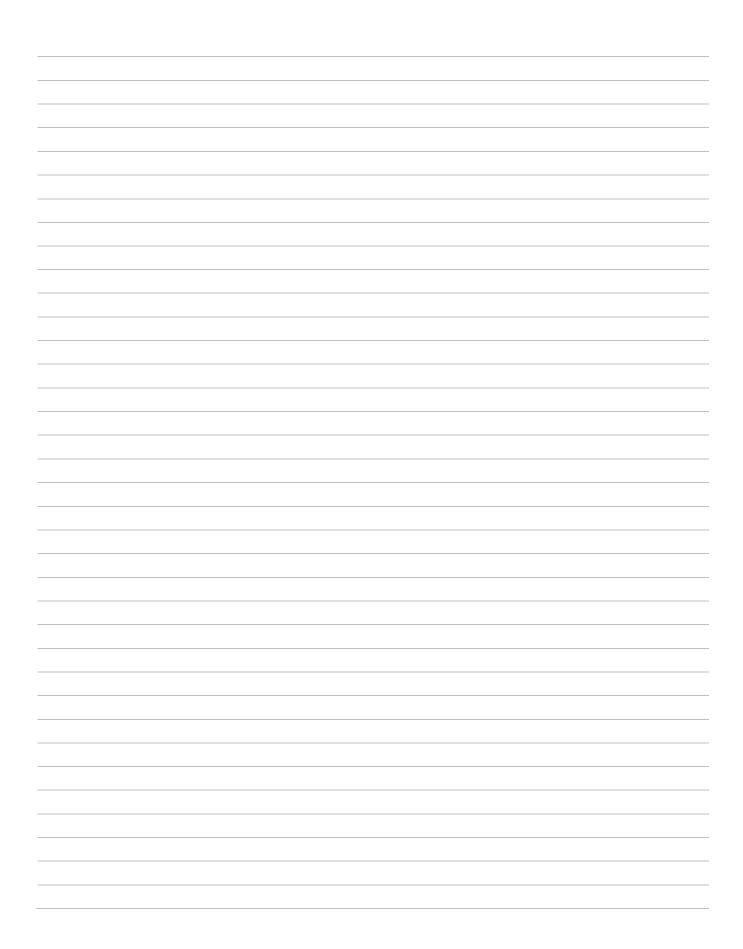
name	gender	age	fixed	weight
"Toggle"	"female"	3	true	48
"Fritz"	"male"	4	true	92
"Nori"	"female"	6	true	35.3
"Maple"	"female"	3	true	51.6

Match each Pyret expression (left) to the description of what it does (right).

t.order-by("age", true)	Produces a table containing <i>only</i> Toggle and Maple
t.filter(is-fixed)	Produces a table, sorted oldest-to- youngest.
<pre>t.build-column("sticker", nametag)</pre>	Produces a table, sorted youngest-to- oldest
t.filter(is-young)	Produces a table with an extra column, named "sticker"
t.order-by("age", false)	Produces a table containing Maple and Toggle, in that order.
<pre>t .filter(is-young) .order-by("weight", false)</pre>	Produces a table containing the same four animals.
<pre>t .order-by("age", true) .build-column("sticker", nametag)</pre>	Produces a table with an extra "sticker" column, sorted youngest-to-oldest

### Unit 5

- Functions can contain value definitions
- We use **Table Plans** to help us use table methods correctly, without making mistakes



### Review

2.	If a researcher is looking at a dataset of students, they might want to divide the
	data into separate populations of boys and girls. A veterinarian might want to look
	at only the cats at a shelter. Copy one of your "filtering" answers from Page 18
	<b>below</b> , to define the filtering criteria you want to use.

3.	In the space below, use the Design Recipe to write a function that checks if a row in
	your dataset fits that criteria. Whatever criteria you choose, it should be true for
	some rows and false for others. Type this function into the Definitions Area.

		::	_	
#	name	domain		range
examp	ples:			
-		(sample1) <b>is</b>		
		(sample2) <b>is</b>		
end				
fun _		() :		<del></del>
and				

4. Use the function to filter your dataset.

5. Instead of using the function you wrote to *filter* your dataset, **use another table method to build a new column** that shows whether or not each row meets the criteria.

On Kitten Day, the shelter prints up a list of all the cats in their database that are less than 2 years old, and makes nametags for them. They need a function that will help them out! Define a function called get-kittens-tags, which takes in the dataset and produces the correct table.

**Xample Tables** Make a Start Table and a result based on that table.  **nimals-table**  **Jame		t and P t-kitte			:	<b>:</b>	(aı	nimals :	: Tabi	le)		· ->			Table	
Adake a Start Table and a result based on that table.  Inimals—table    Table   Table   Table   Table   Table   Table   Table	t Consun	ne a tabi	le of	anima	ls, ar	nd proa	luce a t	able con	taining	kittens	with	name	tags,	. sorte	d by na	те
Adake a Start Table and a result based on that table.  Inimals—table    Table   Table   Table   Table   Table   Table   Table																
name         species         age         fixed         legs         weight         adopt           Sasha         cat         1         FALSE         4         6.5         4           Toggle         dog         3         TRUE         4         48         3           Buddy         lizard         2         FALSE         4         0.3         12           Wade         cat         1         FALSE         4         3.2         4	xample	e Tables	S													
name         species         age         fixed         legs         weight         adopt           Sasha         cat         1         FALSE         4         6.5         4           Toggle         dog         3         TRUE         4         48         3           Buddy         lizard         2         FALSE         4         0.3         12           Wade         cat         1         FALSE         4         3.2         4    Wade  Cat  1  FALSE  4  3.2  4  Wade				nd a r	esult	based	on the	at table.	,							
Sasha         Cat         1         FALSE         4         6.5         4           Toggle         dog         3         TRUE         4         48         3           Buddy         lizard         2         FALSE         4         0.3         12           Wade         cat         1         FALSE         4         3.2         4             Wade         cat         1         FALSE         4         3.2         4	nimal	s-tab	<u>le</u>					-	<b>→</b> g	et-ki	tte	ns-t	ags	(anir	mals-	table
Sasha         Cat         1         FALSE         4         6.5         4           Toggle         dog         3         TRUE         4         48         3           Buddy         lizard         2         FALSE         4         0.3         12           Wade         cat         1         FALSE         4         3.2         4             Wade         cat         1         FALSE         4         3.2         4	name	species	age	fixed	legs	weight	adopt		namo	species	999	fixed	logs	woight	adont	łaa
Toggle         dog         3         TRUE         4         48         3           Buddy         lizard         2         FALSE         4         0.3         12           Wade         cat         1         FALSE         4         3.2         4             Wade         cat         1         FALSE         4         3.2         4	Sasha	cat	1	FALSE	4	6.5	4			-	_			_	_	
Wade         cat         1         FALSE         4         3.2         4	Toggle	dog	3	TRUE	4	48	3		303110	Cai	'	TALSE	7	0.5	7	Sasn
	Buddy	lizard	2		4	0.3	12		Wade	cat	1	FALSE	4	3.2	4	Wac
Mittens   cat   2   TRUE   4   74   5																
	Mittens	cat	2	IRUE	4	7.4	5									
	se the r	elevant	meth	nods (	circle	e your	helper	tunctio	ns!), th	en proc	luce	a resu	ilt wi	th the	new to	ble.
									,							
se the relevant methods (circle your helper functions!), then produce a result with the new table.	un _	9	ret-k	Kittei	15-10	195	_ (_	anıma	7/5	:				De	fine t	he tak
se the relevant methods (circle your helper functions!), then produce a result with the new table.  Fun get-kittens-tags ( animals ):	<u>† = 0</u>	nimals												De	1110 11	ic rub
se the relevant methods (circle your helper functions!), then produce a result with the new table.	.bi	uild-col	lumn	(									)	Are the	ere mor	e columr
se the relevant methods (circle your helper functions!), then produce a result with the new table.  Funget-kittens-tags (animals) :  Define the table.	fi	Iter(												Are 1	there fe	wer rou
se the relevant methods (circle your helper functions!), then produce a result with the new table.  fun			/										)	Are	the rows	s ordere
se the relevant methods (circle your helper functions!), then produce a result with the new table.  fun <u>get-kittens-tags</u> ( <u>animals</u> ): <u>t = animals</u> build-column(filter(	+													Produ	ice th	e resi
t = animals build-column(filter(	<del>'</del> ——												_	, , out	100 111	0 1 031

The first weekend of every month, the shelter holds a "meet the dogs" picnic, to encourage families to adopt their dogs. Write a function called get-dogs-by-age, that takes their database and produces a table of all the dogs in the shelter, sorted from youngest to oldest.

Contract	and Pu	rpos	е											
get	-dogs-b	y-ag	ge	::_		(anima	als :: Tab	le)	>	·		Tai	ble	
# Consum	e a table	of ai	nimals, a	and pi	roduce	a table	containing	only the	dogs, sa	rtea	by ag	re		
Examples Make a St		e and	d a resul	t has	sed on	that to	able							
animals			<i>a</i> 10301	1 000	000	iiiai ie	<b>→</b>	get-d	og-by	-ag	e(an	ima	ls-ta	able)
name	species	age	fixed	legs	weight	adopt								
Snowcone	cat	2	TRUE	4	6.1	5		name	species	age	fixed	legs	weight	adopt
Wade	cat	1	FALSE	4	3.2	4		Toggle	dog	3	TRUE	4	48	3
Hercules	cat	3	FALSE	4	13.4	7		Fritz	dog	4	TRUE	4	92	6
Toggle	dog	3	TRUE	4	48	3				l.		ı	1	
Fritz	dog	4	TRUE	4	92	6								
Define th	o funct	ion												
Use the re			ods (circ	le yc	our help	oer fun	ctions!), th	en produ	ce a re	sult v	vith th	e ne	w table	∋.
							):				<u></u>	efir	ne the	table
										)	Are	there	more c	olumns?
											Ar	e the	re fewe	er rows?
	der-by(										Ar	e the	rows of	rdered?
											Pro	duce	e the	result

It's important for animals to stay healthy, especially when they get older. The veterinarians at the shelter want to put some of the dogs on a diet! They need a regular report of all the older dogs, sorted from heaviest-to-lightest. Define a function old-dogs-diet, which does just that!

Contract	and Purpo	ose												
			::							<b>&gt;</b> _				
Example	S													
Make a St	art Table a	nd a	result b	asec	on the	at tab	le.							
animals	-table						$\rightarrow$	old-	-dogs-	-die	t(ani	mal	s-ta	ble)
name	species	age	fixed	legs	weight	adopt	1							
Snowcone	cat	2	TRUE	4	6.1	5		name	species	_	fixed		weight	
Lucky	dog	3	TRUE	3	45.4	9		Mr. PB	dog	10	FALSE	4	161	6
Mr. PB	dog	10	FALSE	4	161	6		Boo-boo	dog	11	TRUE	4	123	24
Boo-boo	dog	11	TRUE	4	123	24								
Snuggles	tarantula	2	FALSE	8	0.1	1								
	l						1							
Define th	e function													
	levant met	hods	(circle	your	helper	funct	tions!),	then produ	uce a re	sult v	with the	new	/ table	
fun					(		)	:						
<i>t =</i>											De	efine	the i	table
	ild-column										Are th	here n	nore col	umns?
	_										Are	there	e fewer	rows?
fil										/			rows ord	
ord	der-by(													
											Proc	<u>luce</u>	the r	esult
end														

The shelter is tracking birth-years for all the animals who've been fixed. They need a function that takes in their database and returns a table that contains the birth-year for each one. Define get-fixed-birth that will do this for them.

Contract	and Purpo	ose													
			::							-	<b>&gt;</b>				
										_					
Example	S														
	art Table a	nd a	result b	asec	on the	at tabl	le.							•	
animals	-table						$\rightarrow$	get-f	ixed-	-by-	-legs	(ani	mals	-tab	le)
name	species	age	fixed	legs	weight	adopt	1 ,	name	species	999	fixed	logs	weight	adoni	Lyggr
Snowcone	cat	2	TRUE	4	6.1	5	1	Snowcone	species cat	age 2	TRUE	legs 4	6.1	<b>5</b>	2015
Lucky	dog	3	TRUE	3	45.4	9		Lucky	dog	3	TRUE	3	45.4	9	2013
Hercules	cat	3	FALSE	4	13.4	7	]	Toggle	dog	3	TRUE	4	43.4	3	2014
Toggle	dog	3	TRUE	4	48	3	į L	109916	aog	J	IKOE	4	40	J	2014
Snuggles	tarantula	2	FALSE	8	0.1	1									
	l						_								
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ord	der-by(											Are	the rov	vs orde	red?
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end															

# My Dataset

What are two ways you might want to order this dataset?
1)
2)
What are two subsets into which you might filter this dataset?
1)
2)
What are two new columns you might want to build from this dataset?
1)
2)

#### Unit 6

- **Bar charts** show the *absolute* quantity of each row in a dataset. The larger the quantity, the longer the bar. Bar charts provide a visual representation of values in a dataset.
- **Pie charts** show the *relative* quantity of each row in a dataset. The greater the percentage, the larger the pie slice. Pie charts provide a visual representation of proportions in a dataset.
- **Choosing a Sample Table** is important when coming up with small examples for Table Plans. A good sample table has:
  - 1. At least all the relevant columns
  - 2. Enough rows to accurately represent the dataset
  - 3. Rows that are randomly-ordered

#### Statements about Columns

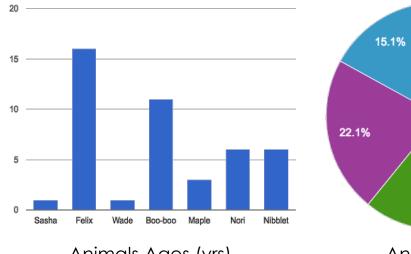
Use the Table below to help you answer the questions.

name	species	age	pounds
Sasha	cat	1	6.5
Felix	cat	16	9.2
Wade	cat	1	3.2
Boo-boo	dog	11	123
Maple	dog	3	51.6
Nori	dog	6	35.3
Nibblet	rabbit	6	4.3

Which animal(s) is/are the heaviest?
 Which animal(s) is/are the youngest?
 How much of the total weight comes from Maple?
 How much of the combined age comes from Nori?
 Would these questions be harder to answer if the table had 100 rows? If so, why?

## Visualizing Quantity

In the table below, there are two observations drawn from the following charts. Add two more.



Sasha Felix Wade Boo-boo Maple Nori 52.8% Nibblet

Animals Ages (yrs)

Animals Weights (lbs)

Based on a chart of	I notice that
Based on a bar chart of 7 animals' ages	Felix is by far the oldest
Based on a <b>pie chart</b> of 7 animals' weights	Boo-boo weighs more than the other six animals combined!
Based on a bar chart of 7 animals' ages	
Based on a pie chart of 7 animals' weights	

Dogs are generally a lot bigger heavier than cats, so the shelter wants to look at a chart of *only* the dogs to determine who needs more exercise time. Define a function pie-dog-weight, which will make a pie chart showing the relative weights of all the dogs in the shelter.

Contract a	nd Pur	pose				
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Examples	t Table	and a result	harad on t	hat table		
			basea on i			
animals-	table	<u> </u>		$\rightarrow$		<pre>pie-dog-weight(animals-table)</pre>
name	•••	weight				
Snowcone		6.1				
Lucky		45.4				
Hercules Toggle		13.4				
Snuggles		0.1				
onaggico	•••	0.1				
Define the					1) 11	
use the rele	vant m	etnoas (circi	e your neip	er functior	ns!), the	n produce a result with the new table.
			,		`	
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<u>† =</u>						Are there more columns?
						Are there fewer rows?
						Are the rows ordered?
						Produce the result
end						

## Bad Sample Tables!

For each word problem, a Sample Table must have (1) all the columns that matter, (2) a representative sample of the rows, and be in (3) random order. For each problem below, check the boxes to determine if the Sample Table meets those criteria.

1.	The shelter wan	ts to know the	median age	of all the cats

name	species	age	fixed	legs	pounds	weeks	Relevant columns
Sasha	cat	1	FALSE	4	6.5	3	Representative sample of rows
Mittens	cat	2	TRUE	4	7.4	5	Random order
Sunfower	cat	5	TRUE	4	8.1	10	

#### 2. The shelter wants a pie chart showing all the dogs' weight

name	species	age
Fritz	dog	4
Wade	cat	2
Nibblet	rabbit	6
Daisy	dog	5

#### 3. Sort all the animals alphabetically by name

name	species	age	fixed	legs	pounds	weeks	Dalay and a alympia
Ada	dog	2	TRUE	4	32	3	<ul><li>Relevant columns</li><li>Representative sample of rows</li></ul>
Во	dog	4	TRUE	4	76.1	10	☐ Random order
Boo-boo	dog	11	TRUE	4	123	10	Random order

#### 4. Make a bar chart for all the fixed animals

name	species	age	fixed	legs	pounds	weeks	Relevant columns
Sasha							Representative sample of rows
							Random order

Define a function bar-kitten-adoption, which takes in a Table of animals and creates a bar chart showing how many weeks it took for each kitten to be adopted

Contract and Purpose				
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				Are the rows ordered?
				Produce the result
end				

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end						

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Make a Start Table	and a result base	ed on that to	able.			
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		ır helper fun	ctions!),	then produc	ce a result	with the new table.
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						Are there fewer rows?
						Are the rows ordered?
						Produce the result
end						

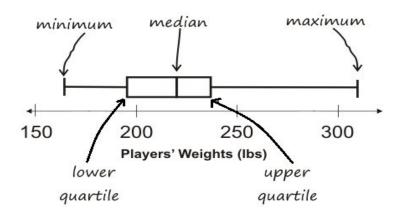
# Visualizing My Dataset

What quantity charts did you make, and what do you notice? Fill in the table below.

Based on a	_ chart of	I notice that
-		
		·
		· <del></del>
-		
-		
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## Unit 7

- There are three ways to measure the "center" of a dataset, to talk about a whole column of data using just one number:
  - 1. The **mean** of a dataset is the average of all the numbers
  - 2. The **median** of a dataset is a value that is smaller than half the dataset, and larger than the other half
  - 3. The **modes** of a dataset are the numbers that appear the most often.
- Data Scientists can also measure the "variation" of a dataset using a five number summary:
  - 1. The **minimum** the smallest value in the dataset
  - 2. The **first**, **or "lower" quartile (Q1)** the median value that separates the first quarter of the values in the dataset from the second quarter
  - 3. The **second quartile (Q2)** the median value which separates the entire dataset into "top" and "bottom" halves.
  - 4. The **third**, **or** "**upper**" **quartile (Q3)** the median value that separates the third quarter of the values in the dataset from the fourth quarter
  - 5. The **maximum** the largest value in the dataset
- The five number summary can be used to draw a box-and-whisker plot.



# Summarizing Columns in Animals

The column I choose to measure is <u>weeks</u>									
Measures of Center  The three measures for this column are:									
Mean (Ave	rage)	Median		Mode(s)					
Based on the diffe	erences betwe	en mean and medic	an, I conclude :						
	Му	<b>Measures of Variat</b> five-number summa	ary is:						
Minimum	Q1	Q2 (Median)	Q3	Maximum					
A box plot can be	e drawn from th	nis summary on the r	number line belov	v: <b>→</b>					
From this summar	y and box-plot	, I conclude:							

The shelter wants a summary of the variation in ages among the dogs. Write a function called variation-dog-age that will take in a table of animals and produce a boxplot that shows this variation.

Contract	and Purpo	ose																			
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														_							
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	art Table a	nd a	result b	asec	on the	at tab	le.														
animals	-table						$\rightarrow$	<u> </u>	var	iat	ior	n-c	log	-ag	ge	( a	nin	nals	s-t	ab]	Le)
name	species	age	fixed	legs	weight	adopt															
Snowcone	cat	2	TRUE	4	6.1	5															
Lucky	dog	3	TRUE	3	45.4	9															
Hercules	cat	3	FALSE	4	13.4	7															
Toggle	dog	3	TRUE	4	48	3															
Snuggles	tarantula	2	FALSE	8	0.1	1															
Define th	a function																				
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end																					

## Interpreting Variation

Consider the following list dataset, representing the annual income of ten people:

\$65k, \$12k, \$14k, \$280k, \$15k, \$22k, \$45k, \$34k, \$45k, \$175k

1. In the space below, rewrite this dataset in **sorted order**.

2. In the table below, compute the **measures of center** for this dataset.

Mean (Average)	Median	Mode(s)

3. In the table below, compute the **five number summary** of this dataset.

Minimum	Q1	Q2 (Median)	Q3	Maximum

4. On the number line below, draw a **box plot** for this dataset.

5. The following statements are correct...but misleading. Write down the reason why.

"They're rich! The average person makes more than \$70k dollars!"

"It's a middle-income list: the most common salary is \$45k/yr!"

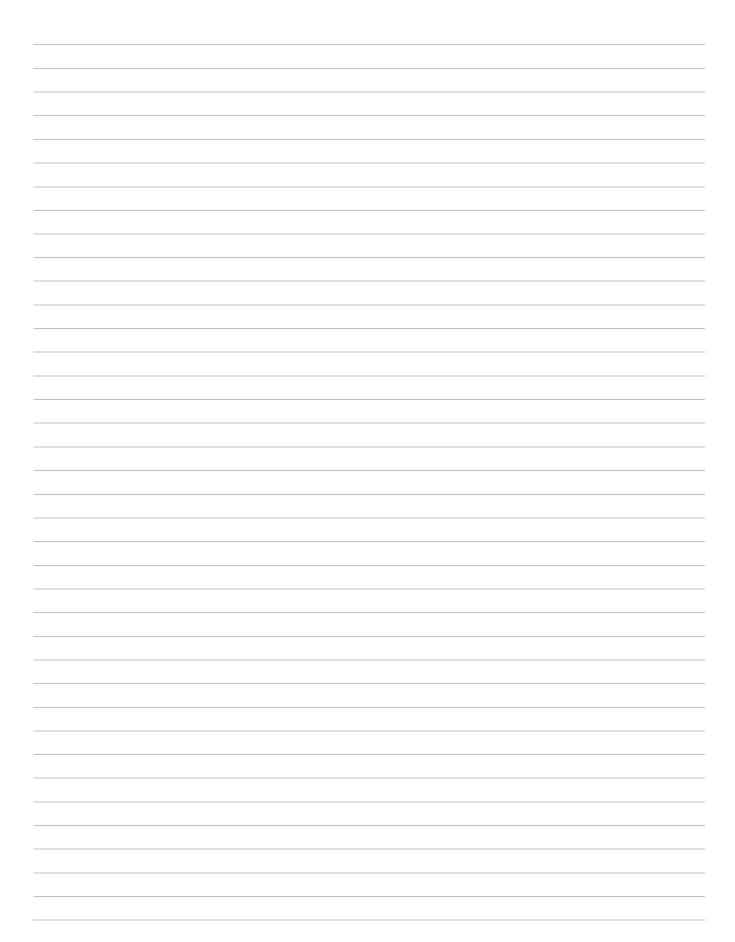
"This group is really diverse, with people making as little as 12k and as much as \$280k!"

# Summarizing a Column in My Dataset

The column I cho	The column I choose to measure is								
Measures of Center The three measures for this column are:									
Mean (Ave	rage)	Median	٨	Node(s)					
Based on the diffe	erences betv	veen mean and medic	an, I conclude :						
Minimum	Measures of Variation  My five-number summary is:								
Millimom	Q1	Q2 (Median)	Q3	Maximum					
A box plot can be drawn from this summary on the number line below:									
From this summar	y and box-pl	ot, I conclude:							

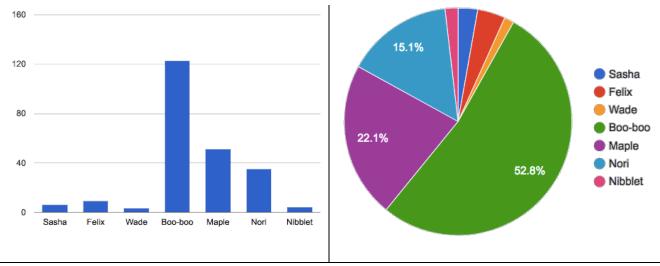
#### Unit 8

- Frequency Bar charts show the number of rows belonging to a given category. The more rows in each category, the longer the bar. Frequency bar charts provide a visual representation of the frequency of values in a categorical column. Since categorical data cannot be ordered, there is no strict ordering of bars in a frequency bar chart.
- Histograms show the number of rows that fall within certain ranges, or "bins" of a
  dataset. The more rows that that fall within a particular "bin", the longer the bar.
  Histograms provide a visual representation of the frequency of values in a
  quantitative column. Quantitative data can be ordered, so the bars of a
  histogram are always sorted.
- When dealing with histograms, it's important to select a good **bin size**. If the bins are too small or too large, it is difficult to see the distribution in the dataset.



## Visualizing Quantity (Review)

Use the charts below to help you answer the questions.



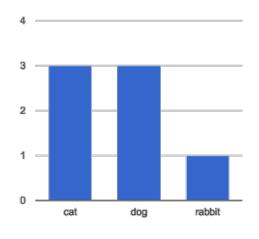
Animals Weights (lbs)

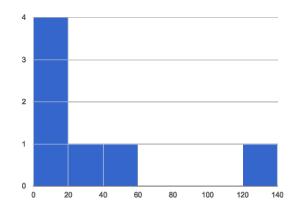
- 1. Which animal is the heaviest?
- 2. Which animal is the lightest?
- 3. How much of the total weight comes from Maple?
- 4. How much of the total weight comes from Nori?
- 5. Which chart did you use for questions 1 and 2?
- 6. Which chart did you use for questions 3 and 4?
- 7. Why are some questions easier to answer with one kind of chart or another?

## Visualizing Frequency

name	species	age	pounds
"Sasha"	"cat"	1	6.5
"Boo-boo"	"dog"	11	123
"Felix"	"cat"	16	9.2
"Nori"	"dog"	6	35.3
"Wade"	"cat"	1	3.2
"Nibblet"	"rabbit"	6	4.3
"Maple"	"dog"	3	51.6

- 1. How many cats are there?
- 2. How many dogs are there?
- 3. How many animals are between 3-6 years old?
- 4. How many weigh between 0-5 pounds?
- 5. Are there more animals weighing 0-5 than 6-10 pounds?
- 6. The charts below are based on the Sample Table above. What is each one measuring? Write down your guess underneath each one.





Define a function freq-bar-gender, which takes in a Table of animals and creates a frequency bar chart showing how many animals are male v. female.

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Make a Start Table and (	a result based on tho	at table.		
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Define the function				
	ls (circle your helper	functions!), tl	nen produce a	result with the new table.
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				Are the rows ordered?
				Produce the result
end				

Define a function histogram-adoption, which takes in a Table of animals and creates a histogram showing how long it took for animals to get adopted

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Define the function	Loirela vour halpar	functional	than produce	a result with the new table.
ose me relevam memoa:	s (circle your neiper	ioriciioris:),	men produce (	areson with the new table.
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·				Are there more columns?
				Are there fewer rows?
				Are the rows ordered?
				Produce the result
end				

# Visualizing My Dataset

What frequency charts did you make, and what do you notice? Fill in the table below.

Based on a	_ chart of	I notice that
,		
	· · · · · · · · · · · · · · · · · · ·	

## Matching Charts to Questions

For each of the questions below, draw a line to the chart that will best answer it. (You may find that more than one question is best answered by the same chart!)

	Are there more of the animals at the shelter fixed or unfixed?	1.
Pie Chart	How many weeks did each cat wait to be adopted?	2.
Bar Chart	How many male v. female dogs are there?	3.
Bui Chair	How many animals have 4 legs? 8? 3?	4.
Frequency Bar Chart	What percent of the total weight at the shelter is made up by Boo-boo?	5.
	What is the distribution of weights across all the animals older than 3?	6.
Histogram	How many animals are there of each species?	7.
	Who waited the longest to be adopted?	8.

#### Unit 9

- **Scatter Plots** show the relationship between two quantitative columns. Each row in the dataset is represented by a point, with one column providing the x-value and the other providing the y-value. The resulting "point cloud" makes it possible to look for a relationship between those two columns.
- If the points in a scatter plot appear to follow a pattern, it is possible that a relationship or **correlation** exists between those two columns.
- If there is a pattern to the points in a scatter plot, points that are far away from the pattern are called **outliers**.
- We can express this correlation by drawing line through the data cloud, so that
  the distance between the line and each of the points is as small as possible. This
  line is called the line of best fit or predictor function and allows us to make
  predictions based on the dataset.

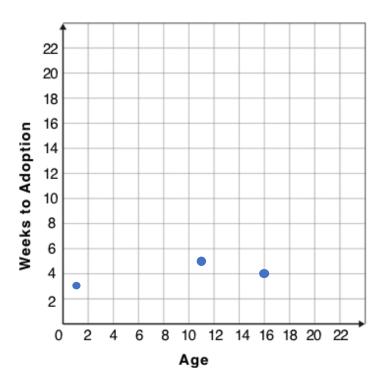
# (Dis)Proving a Claim

### "Younger animals are cuter, so they get adopted faster."

Do you agree? If so, why?
I hypothesize
What would you look for in the dataset to see if you are right?

## Creating a Scatter Plot

name	species	age	weeks
"Sasha"	"cat"	1	3
"Boo-boo"	"dog"	11	5
"Felix"	"cat"	16	4
"Buddy"	"lizard"	2	24
"Nori"	"dog"	6	9
"Wade"	"cat"	1	2
"Nibblet"	"rabbit"	6	12
"Maple"	"dog"	3	2



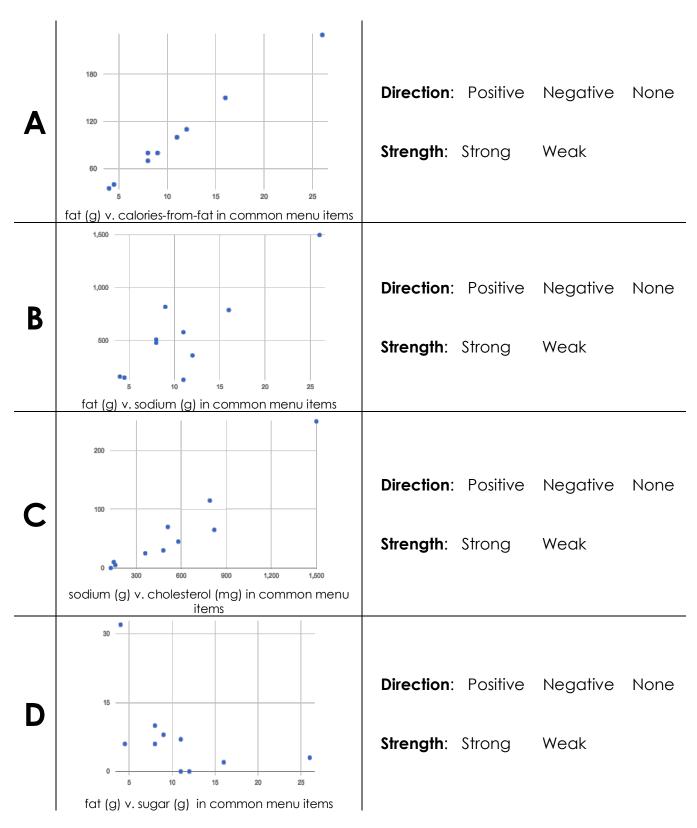
- 1. For each row in the Sample Table on the left, add a point to the scatter plot on the right. The first 3 rows have been completed for you. Use the values from the age column for the x-axis, and values from the weeks column for the y-axis.
- 2. Do you see a pattern? Do the points seem to shift up or down as age increases? **Draw a line on the scatter plot to show this pattern**.
- 3. Does the line slope upwards or downwards?
- 4. Are the points mostly close to the line?

Define a function <code>dogs-age-weeks</code>, which takes in a Table of animals and creates a scatter plot of all the dogs, tracking their <code>age</code> on the x-axis and the number of <code>weeks</code> it took for them to be adopted on the y-axis.

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	s (circle your helpe	er functions!)	, then produce	a result with the new table.
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<u>† =</u>				
				Are there more columns?
				Are there fewer rows?
				Are the rows ordered?
				Produce the result
end				

## **Drawing Predictors**

For each of the scatter plots below, draw a **predictor line** that fits best.



# Correlations in My Dataset

1) There may be a correlation between		and
	column	
1.11.1.1.1.11.11.1.		
I think it is a	strong / weak	
Column	sciong / weak	positive / negative
correlation, because		
	ال يميير ال	d bootropper if I looked
	II WOUR	a be stronger it i looked
a subset		
a subset	or extension of my da	ata
There may be a correlation between		and
T) There may be a conelation between	column	and
I think it is a		
COLUMN	strong / weak	positive / negative
correlation, because		
	11 - 1	-1  1
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a subset	or extension of my da	ata
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T) There may be a conelation between	column	and
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correlation, because		
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a subset	or extension of my da	ata

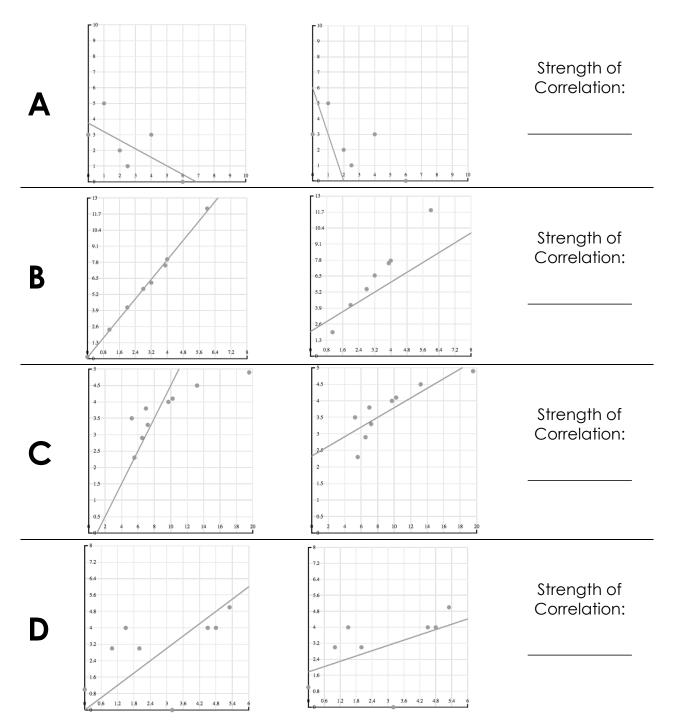
### Unit 10

- Given a **predictor function** and a scatter plot, we can compute the error by adding the squares of all the distances between the function and each point in the plot. The error is called the **r**<sup>2</sup> **statistic**, which tells us how much of the variation in the y-axis can be explained by the x-axis.
- A strong correlation will have a large r<sup>2</sup>. A weak correlation will have a small r<sup>2</sup>.
- A **positive correlation** means the slope of the line of best fit is positive. A **negative correlation** means the slope is negative.
- **Linear Regression** is a way of computing the **line of best fit**, by taking a scatter plot and deriving the slope and y-intercept for a line that has the smallest possible r<sup>2</sup>.
- <u>Correlation is not causation!</u> Correlation only suggests that two measures are related, but does not tell us if one causes the other. For example, hot days are correlated with people running their air conditioners, air conditioners do not cause hot days!

## **Grading Predictors**

Below are the scatter plots for data sets A-D, with two different lines predictor lines drawn on top. For plots A-D:

- 1. Circle the plot with the line that fits better
- 2. Give the plot you circled a grade between 0 (no correlation) and 1 (perfect correlation)



# Findings in the animals Dataset

I performed a linear regression on dogs at the s		gs at the shelter	, and	
•	•		dataset or subset	
found	a weak (r²	=0.25), positive	correlation be	tween
age of the	dogs (in weeks) [x-axis]	and numbe	r of weeks to be adopted [y-axis]	$_{-\!-\!-}$ . From this, I
conclude that _	25% of th	e variability in ac	doption time is explained is explained by [x-axis]	
		ation in [y-axis]	is explained by [x-axis]	
by the age of	the dog			
I performed a lin	near regression on			and
i penomica a iii	icai regression on		dataset or subset	, and
found			correlation be	atween
100110	a strong	/weak (r²=), posi	correlation be	
		and		From this I
	[x-axis]	and	[y-axis]	110111 11113, 1
conclude man_	r² % of the vari	ation in [y-axis]	is explained by [x-axis]	
I performed a lir	near regression on		dataset or subset	, and
found	a strong	/weak (r2= ) nosi	correlation be	etween
	[v-avie]	and	[y-axis]	From this, I
conclude that _	$r^2$ % of the wari	ation in [w-awicl	is explained by [x-axis]	
	I .º OI CHE VALI	acton in [y-axis]	19 Cybrathen by [x-axi2]	

## Correlations in My Dataset

I performed a linea	ır regression on				, and
	-		dataset o	r subset	
found	a strong/we	22k (r²= ) 200	itivo/pogativo	_ correlation be	tween
	axis]	_ and	[v-avia]		From this, I
conclude that	r <sup>2</sup> % of the variati	ion in [v-axis]	is explained	hv [x-axis]	
	1 0 01 che variaci	ion in [y anio]	is explained	ey (n anio)	
					·
I performed a linea	ır regression on		dataset o	r subset	, and
touna	a strong/we	eak $(r^2=)$ , pos	itive/negative	_ correlation be:	rween
	axis]	_ and	[y-axis]		HOIII IIIIS, I
conclude that					
	r <sup>2</sup> % of the variati	ion in [y-axis]	is explained	by [x-axis]	
I performed a linea	ır regression on				, and
			dataset o		,
found	a strong/we			correlation be	tween
<del>, , , , , , , , , , , , , , , , , , , </del>	a strong/we	eak $(r^2=)$ , pos	itive/negative	_	
	axis]	_ and			From this, I
[x-	axis]		[y-axis]		
conclude that	$r^2$ % of the variati				
	r' % of the variati	lon in [y-axis]	ıs explained	by [x-axis]	
					·

# Unit 11

#### Fake News!

**Every claim below is wrong!** Your job is to figure out why, by looking at the data.

	D1	OI	WI
	Data	Claim	Why it's wrong
1	The average player on a basketball team is 6'1".	"Most of the players on the team are taller than 6'."	
2	After performing linear regression on census data, a positive correlation (r <sup>2</sup> =0.18) was found between people's height and salary.	"Taller people get paid more."	
3	y=12.234x + -17.089; r-sq: 0.636	"According to the predictor function indicated here, the value on the x-axis is will predict the value on the y-axis 63.6% of the time."	
4	15  Sasha Felix Wade Boo-boo Maple Nori Bar Chart of Pet Ages	"According to this bar chart, Felix makes up a little more than 15% of the total ages of all the animals in the dataset."	
5	20 40 60 80 100 120 140 160 180 Weight (pounds)	"According to this histogram, most animals weigh between 40 and 60 pounds."	
6	After performing linear regression, a negative correlation (r <sup>2</sup> =0.91) was found between the number of hairs on a person's head and their likelihood of owning a wig.	"Owning wigs causes people to go bald."	

# Blank Recipes, Table Plans, and References

## Design Recipes

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#### Table Plan

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				Produce the result
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#### Table Plan

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						Are the rows ordered?
						Produce the result
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### Contracts

Name	Domain		Range
triangle	:: (side :: Number, style :: String, color :: String)	$\rightarrow$	Image
circle	:: (radius :: Number, style :: String, color :: String)	$\rightarrow$	Image
star	:: (radius :: Number, style :: String, color :: String)	$\rightarrow$	Image
rectangle	:: (width :: Num, height :: Num, style :: Str, color :: Str)	$\rightarrow$	Image
ellipse	:: (width :: Num, height :: Num, style :: Str, color :: Str)	$\rightarrow$	Image
square	:: (size :: Number, style :: String, color :: String)	$\rightarrow$	Image
text	:: (str :: String, size :: Number, color :: String)	$\rightarrow$	Image
overlay	:: (img1 :: <i>Image</i> , img2 :: <i>Image</i> )	$\rightarrow$	Image
rotate	:: (degree :: Number, img :: Image)	$\rightarrow$	Image
scale	:: (factor :: Number, img :: Image)	$\rightarrow$	Image
string-repeat	:: (text :: String, repeat :: Number)	$\rightarrow$	String
string-contains	:: (text :: String, search-for :: String)	$\rightarrow$	Boolean
num-sqr	:: (n :: Number)	$\rightarrow$	Number
num-sqrt	:: (n :: Number)	$\rightarrow$	Number
num-min	:: (a :: Number, b:: Number)	$\rightarrow$	Number
num-max	:: (a :: Number, b:: Number)	$\rightarrow$	Number
get-row	:: (t :: Table, index :: Number)	$\rightarrow$	Row

#### Contracts

Name	Domain		Range
<table>.row-n</table>	:: (n :: Number)	$\rightarrow$	Row
<table>.order-by</table>	:: (col :: String, increasing :: Boolean)	$\rightarrow$	Table
<table>.filter</table>	:: (test :: (Row → Boolean) )	$\rightarrow$	Table
<table>.build-column</table>	:: (col :: String, builder :: (Row → Value) )	$\rightarrow$	Table
mean	:: ( <u>t</u> :: Table, col :: String)	$\rightarrow$	Number
median	:: (t :: Table, col :: String)	$\rightarrow$	Number
modes	:: (t :: Table, col :: String)	$\rightarrow$	List <number></number>
bar-chart	:: (t :: Table, labels :: String, values :: String)	$\rightarrow$	Image
pie-chart	:: (t :: Table, labels :: String, values :: String)	$\rightarrow$	Image
box-plot	:: (t :: Table, col:: String)	$\rightarrow$	Image
freq-bar-chart	:: (t :: Table, values :: String)	$\rightarrow$	Image
histogram	:: (t :: Table, values :: String, bin-width :: Number)	$\rightarrow$	Image
scatter-plot	:: (t :: Table, xs :: String, ys :: String)	$\rightarrow$	Image
labeled-scatter-plot	:: (t :: Table, labels :: String, xs :: String, ys :: String)	$\rightarrow$	Image
lr-plot	:: (t :: Table, xs :: String, ys :: String)	$\rightarrow$	Image
labeled-lr-plot	:: (t :: Table, labels :: String, xs :: String, ys :: String)	$\rightarrow$	Image