





Workbook v1.1

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Unit 1

- Many important questions ("what's the best restaurant in town?", "is this law good for citizens?", etc.) are answered with data. Data Scientists try and answer these questions, by writing programs that ask questions of data.
- Data of all types can be organized into **Tables**
- Every Table has a **header row**, and some number of **data rows**
- **Quantitative data** is data usually numeric that measures *quantity*, such as a person's height, a score on test, a measure of distance, etc. A list of quantitative data can be ordered from smallest to largest.
- Categorical data is data that specifies categories, such as eye color, country of origin, etc. A list of categorical data has no notion of "smallest" or "largest", and cannot be ordered.
- **Programming languages** involves different *datatypes*, such as Numbers, Strings, Booleans and Images.
- Operators (like +, -, *, <, etc.) are written between values. For example: 4 + 2
- **Functions** (like triangle, star, string-repeat, etc.) are written first, followed by a list of **arguments** in parentheses. For example: star(50, "solid", "red")
- **Examples** help programmers reason about their code. Every example contains two expressions, and the example "passes" if both expressions evaluate to the same thing. For example: 4 + 2 is 6, or "cat" == "dog" is false

Numbers and Strings

Make sure you've loaded the Unit 1 Starter File, and clicked "Run".

- 1. Try typing 42 into the Interactions Area and hitting "Enter". What happens?
- 2. Try typing in other Numbers. What happens if you try a decimal like 0.5? A fraction like 1/3? Try really big Numbers, and really small ones.
- 3. String values are always in quotes. Try typing your name (in quotes!). What happens when you hit "Enter"?
- 4. Try typing your name with the opening quote, but without the closing quote. What happens? Now try typing it without any quotes.
- 5. Is 42 the same as "42"? Why or why not? Write your answer below:

Operators

- 6. Just like in math, Pyret has operators like + and -. Try typing in 4 + 2, and then 4+2 (without the spaces). What can you conclude from this? Write your answer below:
- 7. Try typing in 4+2+6, 4+2*6, and 4+(2*6). What can you conclude from this? Write your answer below:
- 8. Try typing in 4 + "cat", and then "dog" + "cat". What can you conclude from this? Write your answer below:

Booleans

Boolean expressions are yes-or-no questions, and will always evaluate to either true ("yes") or false ("no"). What will each of the expressions below evaluate to? Write down the result in the blanks provided, and type them into Pyret if you're not sure.

3 <= 4	 "a" > "b"	
3 == 2	 "a" <> "b"	
2 <> 4	 "a" == "b"	
3 <> 3	 "a" <> "a"	

Boolean Operators

Pyret also has operators that work on *Booleans*. For each expression below, write down your guess about what it will evaluate to. Then type them in and see if you were right!

- How many different Number values are there in Pyret?

- 2. How many different String values are there in Pyret?
- 3. How many different Boolean values are there in Pyret? _____

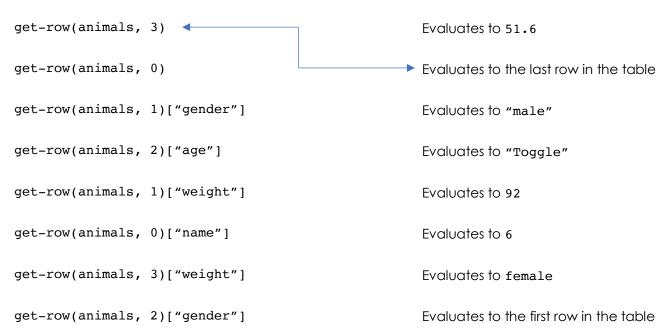
Playing with Tables

The table below represents four animals at the shelter:

animals

name	gender	age	weight
"Toggle"	"female"	3	48
"Fritz"	"male"	4	92
"Nori"	"female"	6	35.3
"Maple"	"female"	3	51.6

1) Match each Pyret expression (left) to the description of what it does (right).



2) Fill in the blanks (left) with the Pyret code that will produce the value (right).

a. get-row(animals, 3)["name"]	"Map⊥e" -
b.	male
С.	4
_d.	48
e.	"Nori"

Writing Examples

In the examples block below, put an "X" next to the examples that will <u>fail</u>.
 Remember: examples only pass if the left- and right-hand expressions evaluate to the same thing!

```
examples:
    1 + 2 + 9
    num-sqrt(16)
    is 2 + 2
    3 > 99
        is true
    square(10, "solid", "red")
end

is rectangle(10, 10, "solid", "red")
end
```

2. In the examples block below, fill in the blank on the right-hand side so the example will <u>pass</u>.

3. The examples block below refers to the shapes table on the right, using row-accessors and the get-row function. For each example, fill in the blank so the example will pass.

name	corners	Is-round
"triangle"	3	false
"circle"	0	true
"ellipse"	0	true
"square"	4	false

Unit 2

Answering Questions from Data can take many forms. Here are a few types of questions, each requiring a different kind of analysis:

- Lookup Questions can be answered just by finding the right row and column a table. (e.g. – "How old is Toggle?")
- Comparison Questions can be answered by comparing a single row or column to all the rest of the table. (e.g. – "What is the heaviest animal at the shelter?")
- **Pattern Questions** require looking for trends across multiple rows or columns. (e.g. "Do cats tend to be adopted sooner than dogs?")

Threats to Validity can undermine a conclusion, even if the analysis was done correctly. Some examples of threats are:

- Sample size averaging the age of only three animals won't tell us anything reliable about the age of animals at the shelter!
- **Selection bias** identifying the favorite food of the rabbits won't tell us anything reliable about what all the animals eat.
- **Sample error** surveying dogs when they are puppies won't tell us anything reliable about overall dog behavior, since their behavior changes as they age.
- Confounding variables if they person surveying the animals has a piece of bacon in their pocket, they will incorrectly find that all dogs are friendly!



The Animals Dataset

- 1. This dataset is **Animals from an animal shelter**
- 2. The columns are....
 (For each column in this dataset, fill out the datatype, and whether it contains Qualitative or Categorical data in the table below)

name	species	gender	age	fixed	pounds	weeks
"Sasha"	"cat"	"female"	1	false	6.5	3
"Toggle"	"dog"	"female"	3	true	48	1
"Boo-boo"	"dog"	"male"	11	true	123	24
"Snuggles"	"tarantula"	"female"	2	false	.01	1
"Nori"	"dog"	"female"	6	true	35.3	1
"Snowcone"	"cat"	"female"	2	true	6.1	5
Datatype						
Quantitative or Categorical?						

3 .	For the questions below, check the box next to the questions you <u>COULD</u> answer	
	given this dataset:	
	☐ How old is Boo-boo?	
	☐ What color is Snowcone's fur?	
	$\ \square$ What is the average age of all the animals in the shelter?	
	Are there more fixed or unfixed animals at the shelter?	
	Are families with children more likely to adopt kittens?	
4.	Some questions I have about this dataset:	

What Questions Can You Answer?

The following is a dataset of a bicycle rider's training rides.

date	miles	time	weather	average speed	max speed
04/10/2018	10	44	"cloudy"	13	30
05/30/2018	15	66	"sunny"	13.5	22
06/12/2018	12	61	"rainy"	11.2	25
06/22/2018	15	61	"cloudy"	13	28
07/04/2018	24	103	"sunny"	14	26
07/12/2018	24	120	"windy"	12.5	26

For the questions below, check the box next to the questions you <u>COULD</u> answer given this dataset:

What is the cyclist's average speed across all rides?
 How many miles did they ride in June?
 What is the tallest hill this cyclist climbed?
 Does this cyclist ride slower when it is rainy?
 Does this cyclist ride faster when they are late to an appointment?

For the questions below, check the box next to the questions you <u>COULD NOT</u> answer given this dataset:

- □ What tire pressure produces the highest average speed?
- ☐ What is the average time it takes this cyclist to ride one mile?
- □ Does this cyclist ride more in April or July?
- □ What is the average temperature while this cyclist is riding?
- ☐ How many flat tires did this cyclist fix in June?

Threats to Validity

Some volunteers from the animal shelter surveyed a group of pet owners at a local park. They found that almost all of the owners were there with their dogs, and from this survey they concluded that dogs are the most popular pet in the region.

What are some possible threats to the validity of this conclusion?
The animal shelter noticed a large increase in pet adoptions between Thanksgiving and New Year's Eve. They conclude that at this current rate, there will be a huge demand for pets between January and April. What are some possible threats to the validity of this conclusion?

Threats to Validity

The animal shelter wanted to find out what kind of food to buy for their animals. They took a random sample of two animals and the food they eat, and found that spider and rabbit food was by far the most popular cuisine!

What are some possible threats to the validity of this conclusion?
A volunteer opens the shelter in the morning and walks all the dogs. At mid-day, another volunteer feeds all the dogs and walks them again. In the evening, a third volunteer walks the dogs a final time, and closes the shelter. The volunteers report that the dogs are much friendlier and more active at mid-day, so the shelter staff assume the second volunteer must be better with animals then the others. What are some possible threats to the validity of this conclusion?

My Dataset

1.	Мус	lataset is						
2.	 Some of my columns are (Copy six columns from your dataset, and for each column write its datatype, and whether it contains Qualitative or Categorical data in the table below) 							it
		Quantitative or Categorical?						
3.	Som	e questions I ha	ve about thi	s dataset:				
4.	Wha	t are some poss	sible threats t	to validity ya	ou may end	counter in y	our analys	is?

Unit 3

- Programming languages let us **define our own function**.
- We use the **Design Recipe** to help us define functions without making mistakes.
- The first step is to write a Contract and Purpose Statement for the function, which specify the Name, Domain and Range of the function and give a summary of what it does.
- The second step is to **write at least two examples**, which show how the function should work for specific inputs. These examples help us see patterns, and we express those patterns by **circling and labeling** what changes.
- The final step is to **define the function**, which generalizes our examples.



The Design Recipe

Define a function called is-fixed, which tells us whether or not an animal is fixed

	is-fixed	::	(animal :: Row)	\rightarrow	Boolean
	name		domain		range
# <u>Con</u> :	sumes an anima	al, and produc	ces the value in the	fixed column	
examp	ples:				
_	is-fixed	(sash	<u>a</u>) is	sasha["fi	xed"]
_	· · · · · · · · · · · · · · · · · · ·	() is		
end					
fun _		() :		
end					
the ger	nder of that an	imal		`	
	name	::	domain	-	range
#	Hame		domarii		runge
exam	ples:				
_		() is		
		() is		
end					
fun _		() :		
end					

Define a function called is-cat,	which consumes a	Row of the	animals t	table (and
produces true if it's a cat.					

is	s-cat	::	(animal :: Row)	\rightarrow	Boolean
	name nes an animal,	and return	domain true if the species is		range
example	es:				
	is-cat	(sasha) is		
		_() is		
end					
fun		_ () :		
end					
roauces	true If If S On	i animai tha	it is less than two yed		
	name	_::	domain	- -	
			domain		range
#			domarii		range
	es:		domarii		range
	es:	_() is		
) is		
example					
#example		_() is		

Define	e a function call	ed nameta	g, prints out each anin	nal's name in l	oig red letters.
	nametag	::	(animal :: Row)	\rightarrow	Image
	name		domain		range
# Co.	nsumes an anima	l, and produ	ices an image of their n	name in big, red	l letters
exan	mples:				
	nametag	(sas	<u>ha</u>) is		
		() is		
end		· · · · · · · · · · · · · · · · · ·			· · · · · · · · · · · · · · · · · · ·
fun		() :		
end					
			ten, which consumes er than two years old.	a Row of the c	ınimals table and
				\rightarrow	
	name	* * *	domain	/	range
#					_
exan	mples:				
		() is		
		() is		
end					
fun		() :		
end					

Unit 4

- **Methods** are special functions that are attached to pieces of data. We use them to manipulate Tables.
- They are different from functions in several ways:
 - 1. Their names can't be used alone: they can only be used as part of data, separated by a dot. (For example, animals.order-by)
 - 2. Their contracts are different: they include the type of the data as part of their names. (eg, .order-by :: (column :: String) > Table)
 - 3. They have a "secret" argument, which is the data they are attached to
- We will use three **Table Methods** to manipulate our datasets:
 - <Table>.order-by order the rows of a table based on a column
 - <Table>.filter create a **subset** of the data, with only certain rows
 - <Table>.build-column use the columns of a table to compute a new one



Reviewing Functions

1.	Definitions Area.	imple in the
2.	How many values are defined in this file?	
3.	How many functions are defined in this file?	
4.	What is the name of the last function?	
5.	What is the Domain of the last function?	
6.	What is the Range of the last function?	
7.	What is the variable name that the last function uses?	
8.	Which function will tell us if an animal is a kitten?	
9.	Which function will print out " <name> the <species>"?</species></name>	
10	.Which function will tell us if an animal is a dog older than 10?	
11	.Which function will tell us if an animal has been fixed?	
12	.Which function will draw a nametag for an animal?	

Plans for the Animals Dataset

What are two ways you might want to order the animals dataset?
1)
2)
What are two subsets into which you might filter the animals dataset?
<u>1)</u>
2)
What are two new columns you might want to build from the animals dataset?
1)
2)

Methods

Methods are a lot like functions, but they differ in three important ways:

- They can only be called as **part of a value**, using the **dot-accessor**. For example: **animals.**row-n(2)
- Their Contracts are different, because they contain a **Type** as part of their name. For example: <**Table>.**row-n :: (index :: Number) -> Row
- They have a "secret argument", which is the value they are attached to. In the examples above, the row-n method consumes only a Number as part of its Domain, but it also consumes the Table to which it is attached.

Here is the Contract for a method, which consumes the name of a food and produces True if the person likes that food:

	<pre><person>.likes :: (food :: String) → Boolean</person></pre>	
1.	What Type of data is the method attached to?	
2.	What is the name of this method?	
3.	How many things are in its Domain?	
4.	What is the name of the argument in its Domain?	
5.	What is the Type of the argument in its Domain?	
6.	What Type of data will this method will produce?	
7.	Below are 3 expressions. Based on the contract above, circle the correct	one.
	emma.likes("pizza") likes("pizza") likes(emma, pizza)

8. On the line below, write your own expression that uses this method, replacing emma and "pizza" with your own name and a food you like.

Playing with Methods

You have the following functions defined below (read them carefully!):

```
fun is-fixed(animal): animal["fixed"] end
fun is-young(animal): animal["age"] < 4 end
fun nametag(animal): text(animal["name"], 20, "red") end</pre>
```

The table **t** below represents four animals at the shelter:

name	gender	age	fixed	weight
"Toggle"	"female"	3	true	48
"Fritz"	"male"	4	true	92
"Nori"	"female"	6	true	35.3
"Maple"	"female"	3	true	51.6

Match each Pyret expression (left) to the description of what it does (right).

Produces a table containing only Toggle and Maple
Produces a table, sorted oldest-to- youngest.
Produces a table, sorted youngest-to- oldest
Produces a table with an extra column, named "sticker"
Produces a table containing Maple and Toggle, in that order.
Produces a table containing the same four animals.
Produces a table with an extra "sticker" column, sorted youngest-to-oldest

Unit 5

- Functions can contain value definitions
- We use **Table Plans** to help us use table methods correctly, without making mistakes



Review

- In the Interactions Area, use table methods to sort your table by one column. Try
 sorting your table in both ascending and descending order.
- If a researcher is looking at a dataset of students, they might want to divide the data into separate populations of boys and girls. A veterinarian might want to look at only the cats at a shelter. Copy one of your "filtering" answers from Page 18 below, to define the filtering criteria you want to use.
- In the space below, use the Design Recipe to write a function that checks if a row in your dataset fits that criteria. Whatever criteria you choose, it should be true for some rows and false for others. Type this function into the Definitions Area.

		_::		_ -	
	name		domain		range
#				 	
examp	oles:				
		(~ ~ ~ · · · · · · · · · · · · · · · ·	.		
_		_(sample1)	1S		
		(sample2)	is		
end					
fun _		()	:		
end					

- Use the function to filter your dataset.
- Instead of using the function you wrote to filter your dataset, use another table method to build a new column that shows whether or not each row meets the criteria.

On Kitten Day, the shelter prints up a list of all the cats in their database that are less than 2 years old, and makes nametags for them. They need a function that will help them out! Define a function called get-kittens-tags, which takes in the dataset and produces the correct table.

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	Tables Start Tab		nd a r	esult	based	on the
	s-tab					
name	species	age	fixed	legs	weight	adopt
Sasha Toggle	cat dog	3	FALSE TRUE	4	6.5 48	3
Buddy	lizard	2	FALSE	4	0.3	12
Wade	cat	1	FALSE	4	3.2	4
Mittens	cat	2	TRUE	4	7.4	5
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	nimals uild-col					_ (_
bu						_ (_
bi	ıild-col	lumn				_ (_

The first weekend of every month, the shelter holds a "meet the dogs" picnic, to encourage families to adopt their dogs. Write a function called get-dogs-by-age, that takes their database and produces a table of all the dogs in the shelter, sorted from youngest to oldest.

Consume a table of animals, and produce a table containing only the dogs, sorted by age **Examples Make a Start Table and a result based on that table. **Inimals-table** **Toggle dog 3 TRUE 4 48 3 **Toggle dog 3 TRUE 4 48 3		-dogs-b	y-ag	<i>де</i>	:: _		(anima	als :: Tabl	'e)	>	·		Tai	ble	
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ercules cat 3 FALSE 4 13.4 7 Toggle dog 3 TRUE 4 48 3					_				name	species	age	fixed	legs	weight	adop
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									Fritz	dog	4	TRUE	4	92	6
Fritz dog 4 TRUE 4 92 6	Fritz	dog	4	_	4	92	6								
		aog	_	ткод	_	52									
		a funal	ion												
	ofin a H														
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				ods (circ	le yc	our help	er fund	ctions!), the	en produ	ce a re	sult w	vith th	e ne	w table	Э.
Define the function se the relevant methods (circle your helper functions!), then produce a result with the new table.	se the re	levant m	netho	•	·	·		,	en produ	ce a re	sult w	vith th	e ne	w table	Э.
se the relevant methods (circle your helper functions!), then produce a result with the new table. un	se the re	levant m	netho	•		():	en produ	ce a re:	sult w				
se the relevant methods (circle your helper functions!), then produce a result with the new table. un ():	se the re un <u>† =</u>	levant m	netho			():	en produ	ce a re:	sult w	<u></u>	efin	ne the	tab
se the relevant methods (circle your helper functions!), then produce a result with the new table. un	un	levant m	netho			():	en produ	ce a re:	sult w	<u>D</u>	<u>)efir</u> there	ne the	<u>tab</u>
se the relevant methods (circle your helper functions!), then produce a result with the new table. un	un	levant m	netho			():	en produ	ce a re	sult w	Are:)efir there	ne the more core fewe	<u>tab</u> olumr
se the relevant methods (circle your helper functions!), then produce a result with the new table. un	un	ilevant n	mn(():	en produ	ce a re	sult w	Are:)efir there	ne the more core fewe	<u>tab</u> olumr

It's important for animals to stay healthy, especially when they get older. The veterinarians at the shelter want to put some of the dogs on a diet! They need a regular report of all the older dogs, sorted from heaviest-to-lightest. Define a function old-dogs-diet, which does just that!

Contract	and Purpo	se							_	_				
			::						~	_				
xample														
ıake a St	art Table a	nd a	result b	asec	on the	at tab	•							
nimals	-table						>	old-	-dogs-	-die	et(ani	mal	s-tal	ble
name	species	age	fixed	legs	weight	adopt		namo	species	age	fixed	logs	weight	adı
nowcone	cat	2	TRUE	4	6.1	5		name Mr. PB	dog	10	FALSE	4	161	duc
Lucky	dog	3	TRUE	3	45.4	9		Boo-boo	dog	11	TRUE	4	123	2
Mr. PB	dog	10	FALSE	4	161	6			aog		INOL	_	123	_
Boo-boo	dog	11	TRUE	4	123	24								
nuggles	tarantula	2	FALSE	8	0.1	1								
Snuggles ———	tarantula	2	FALSE	8	0.1	1								
efine th	e function													
	levant met	hods	(circle	your	helper	funct	ns!),	then produ	uce a re	sult v	with the	new	table.	
un					()	:						
					· <u> </u>						De	etine	the i	tab
	ild-column										Are th	nere n	nore col	umn
											Are	there	e fewer	rou
	ter(/ \	Are	the r	ows ord	dere
ord	der-by(,	the r	

The shelter is tracking birth-years for all the animals who've been fixed. They need a function that takes in their database and returns a table that contains the birth-year for each one. Define get-fixed-birth that will do this for them.

Contract	and Purpo	ose														
			::							_ =	—					
	· · · · · · · · · · · · · · · · · · ·															
Example:	art Table a	nd a	rogult b	asoc	l on th	at tabl	lo									
Make a si	an rable al	na a	resuii D	asec	i Ori irio		ie.									
animals	-table						\rightarrow	get-i	fixed-	-bv-	leas	(ani	mals	-tab	ole)	
name	species	age	fixed	leas	weight	adopt	_	<u> </u>		~		(
Snowcone	cat	2	TRUE	4	6.1	5		name	species	age	fixed	legs	weight	adopt	year	
Lucky	dog	3	TRUE	3	45.4	9		nowcone	cat	2	TRUE	4	6.1	5	2015	
Hercules	cat	3	FALSE	4	13.4	7		Lucky	dog	3	TRUE	3	45.4	9	2014	
Toggle	dog	3	TRUE	4	48	3		Toggle	dog	3	TRUE	4	48	3	2014	
Snuggles	tarantula	2	FALSE	8	0.1	1										
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	e function levant met		(circle	vour	helper	functi	ions!), then r	produce	e a re	sult wi	th the	new t	able.		
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build-column(Are there fewer rows?					
	ter()					
ord	der-by(Are	the rov	vs orde	red?	
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end																

My Dataset

What are two ways you might want to order this dataset?
1)
2)
What are two subsets into which you might filter this dataset?
1)
2)
What are two new columns you might want to build from this dataset?
1)
2)

Unit 6

- **Bar charts** show the *absolute* quantity of each row in a dataset. The larger the quantity, the longer the bar. Bar charts provide a visual representation of values in a dataset.
- **Pie charts** show the *relative* quantity of each row in a dataset. The greater the percentage, the larger the pie slice. Pie charts provide a visual representation of proportions in a dataset.
- **Choosing a Sample Table** is important when coming up with small examples for Table Plans. A good sample table has:
 - At least all the relevant columns
 - Enough rows to accurately represent the dataset
 - Rows that are randomly-ordered

Statements about Columns

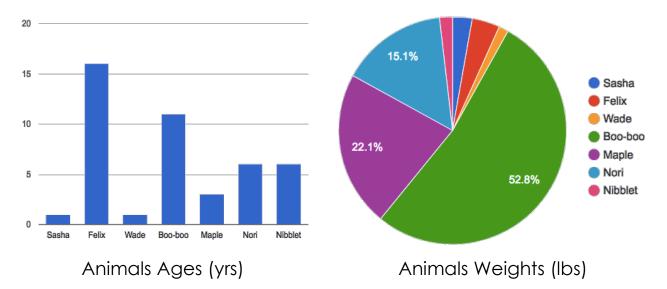
Use the Table below to help you answer the questions.

name	species	age	pounds
Sasha	cat	1	6.5
Felix	cat	16	9.2
Wade	cat	1	3.2
Boo-boo	dog	11	123
Maple	dog	3	51.6
Nori	dog	6	35.3
Nibblet	rabbit	6	4.3

Which animal(s) is/are the heaviest?
 Which animal(s) is/are the youngest?
 How much of the total weight comes from Maple?
 How much of the combined age comes from Nori?
 Would these questions be harder to answer if the table had 100 rows? If so, why?

Visualizing Quantity

In the table below, there are two observations drawn from the following charts. Add two more.



Based on a chart of	I notice that
Based on a bar chart of 7 animals' ages	Felix is by far the oldest
Based on a pie chart of 7 animals' weights	Boo-boo weighs more than the other six animals combined!
Based on a bar chart of 7 animals' ages	
Based on a pie chart of 7 animals' weights	

Dogs are generally a lot bigger heavier than cats, so the shelter wants to look at a chart of *only* the dogs to determine who needs more exercise time. Define a function pie-dog-weight, which will make a pie chart showing the relative weights of all the dogs in the shelter.

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<u>animals-table</u>	\rightarrow	<pre>pie-dog-weight(animals-table)</pre>
name weight		
Snowcone 6.1		
Lucky 45.4		
Hercules 13.4		
Toggle 48 Snuggles 0.1		
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		Are the rows ordered?
		Produce the result
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Bad Sample Tables!

For each word problem, a Sample Table must have (1) all the columns that matter, (2) a representative sample of the rows, and be in (3) random order. For each problem below, check the boxes to determine if the Sample Table meets those criteria.

name	species	age	fixed	legs	pounds	weeks	Relevant columns
Sasha	cat	1	FALSE	4	6.5	3	Representative sample of rows
Mittens	cat	2	TRUE	4	7.4	5	Random order
Sunfower	cat	5	TRUE	4	8.1	10	

2. The shelter wants a pie chart showing all the dogs' weight

name	species	age
Fritz	dog	4
Wade	cat	2
Nibblet	rabbit	6
Daisy	dog	5

3. Sort all the animals alphabetically by name

name	species	age	fixed	legs	pounds	weeks	Delevient edimen
Ada	dog	2	TRUE	4	32	3	Relevant columnsRepresentative sample of rows
Во	dog	4	TRUE	4	76.1	10	□ Representative sample of rows
Boo-boo	dog	11	TRUE	4	123	10	Random order

4. Make a bar chart for all the fixed animals

name	species	age	fixed	legs	pounds	weeks	Relevant columns
Sasha							Representative sample of rows
							Random order

Define a function bar-kitten-adoption, which takes in a Table of animals and creates a bar chart showing how many weeks it took for each kitten to be adopted

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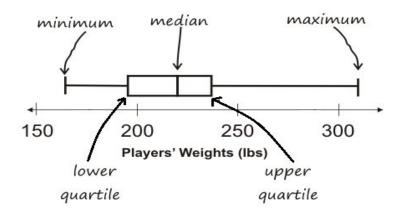
Visualizing My Dataset

What quantity charts did you make, and what do you notice? Fill in the table below.

Based on a	_ chart of	I notice that
		·
		-
		-

Unit 7

- There are three ways to measure the "center" of a dataset, to talk about a whole column of data using just one number:
 - 1. The **mean** of a dataset is the average of all the numbers
 - 2. The **median** of a dataset is a value that is smaller than half the dataset, and larger than the other half
 - 3. The **modes** of a dataset are the numbers that appear the most often.
- Data Scientists can also measure the "variation" of a dataset using a five number summary:
 - 1. The **minimum** the smallest value in the dataset
 - 2. The **first**, **or "lower" quartile (Q1)** the median value that separates the first quarter of the values in the dataset from the second quarter
 - 3. The **second quartile (Q2)** the median value which separates the entire dataset into "top" and "bottom" halves.
 - 4. The **third**, **or** "**upper**" **quartile (Q3)** the median value that separates the third quarter of the values in the dataset from the fourth quarter
 - 5. The **maximum** the largest value in the dataset
- The five number summary can be used to draw a box-and-whisker plot.



Summarizing Columns in Animals

The column I cho	ose to measure is	s weeks		
		Aeasures of Cent e measures for this c		
Mean (Ave	rage)	Median	N	Mode(s)
Based on the diff	erences betweer	n mean and medic	an, I conclude :	
		easures of Variative-number summo		
Minimum	Q1	Q2 (Median)	Q3	Maximum
A box plot can be	e drawn from this	s summary on the r	number line below	√ :
From this summar	y and box-plot, I	conclude:		

The shelter wants a summary of the variation in ages among the dogs. Write a function called variation-dog-age that will take in a table of animals and produce a boxplot that shows this variation.

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name	species	age	fixed		weight																
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Lucky	dog	3	TRUE	3	45.4	9	_														
Hercules	cat	3	FALSE	4	13.4	7															
Toggle	dog	3	TRUE	4	48	3															
Snuggles	tarantula	2	FALSE	8	0.1	1															
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Interpreting Variation

Consider the following list dataset, representing the annual income of ten people:

\$65k, \$12k, \$14k, \$280k, \$15k, \$22k, \$45k, \$34k, \$45k, \$175k

1. In the space below, rewrite this dataset in **sorted order**.

2. In the table below, compute the **measures of center** for this dataset.

Mean (Average)	Median	Mode(s)

3. In the table below, compute the **five number summary** of this dataset.

Minimum	Q1	Q2 (Median)	Q3	Maximum

4. On the number line below, draw a **box plot** for this dataset.

←

5. The following statements are correct...but misleading. Write down the reason why.

"They're rich! The average person makes more than \$70k dollars!"

"It's a middle-income list: the most common salary is \$45k/yr!"

"This group is really diverse, with people making as little as 12k and as much as \$280k!"

Summarizing a Column in My Dataset

ne column i cho	ose to measure i	S		
		Measures of Cent measures for this o		
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ased on the diff	erences betwee	n mean and medi	an, I conclude :	
		easures of Variat	_	
Minimum	Q1	Q2 (Median)	Q3	Maximum
\ box plot can bo	e drawn from thi	s summary on the r	number line below	/ : ▶
rom this summar	y and box-plot, I	conclude:		

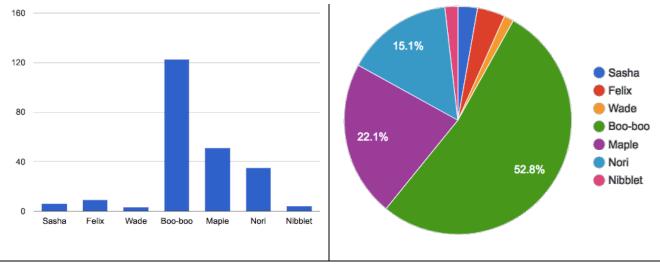
Unit 8

- Frequency Bar charts show the number of rows belonging to a given category. The more rows in each category, the longer the bar. Frequency bar charts provide a visual representation of the frequency of values in a categorical column. Since categorical data cannot be ordered, there is no strict ordering of bars in a frequency bar chart.
- Histograms show the number of rows that fall within certain ranges, or "bins" of a
 dataset. The more rows that that fall within a particular "bin", the longer the bar.
 Histograms provide a visual representation of the frequency of values in a
 quantitative column. Quantitative data can be ordered, so the bars of a
 histogram are always sorted.
- When dealing with histograms, it's important to select a good **bin size**. If the bins are too small or too large, it is difficult to see the distribution in the dataset.



Visualizing Quantity (Review)

Use the charts below to help you answer the questions.



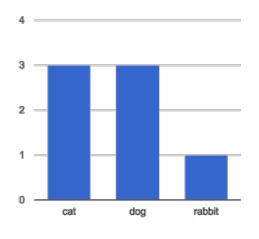
Animals Weights (lbs)

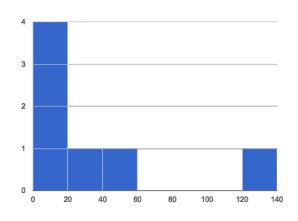
- 1. Which animal is the heaviest?
- 2. Which animal is the lightest?
- 3. How much of the total weight comes from Maple?
- 4. How much of the total weight comes from Nori?
- 5. Which chart did you use for questions 1 and 2?
- 6. Which chart did you use for questions 3 and 4?
- 7. Why are some questions easier to answer with one kind of chart or another?

Visualizing Frequency

name	species	age	pounds
"Sasha"	"cat"	1	6.5
"Boo-boo"	"dog"	11	123
"Felix"	"cat"	16	9.2
"Nori"	"dog"	6	35.3
"Wade"	"cat"	1	3.2
"Nibblet"	"rabbit"	6	4.3
"Maple"	"dog"	3	51.6

- 1. How many cats are there?
- 2. How many dogs are there?
- 3. How many animals are between 3-6 years old?
- 4. How many weigh between 0-5 pounds?
- 5. Are there more animals weighing 0-5 than 6-10 pounds?
- 6. The charts below are based on the Sample Table above. What is each one measuring? Write down your guess underneath each one.





Define a function freq-bar-gender, which takes in a Table of animals and creates a frequency bar chart showing how many animals are male v. female.

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Define a function histogram-adoption, which takes in a Table of animals and creates a histogram showing how long it took for animals to get adopted

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Visualizing My Dataset

What frequency charts did you make, and what do you notice? Fill in the table below.

Based on a chart of	I notice that

Matching Charts to Questions

For each of the questions below, draw a line to the chart that will best answer it. (You may find that more than one question is best answered by the same chart!)

	Are there more of the animals at the shelter fixed or unfixed?	1.
Pie Chart	How many weeks did each cat wait to be adopted?	2.
Bar Chart	How many male v. female dogs are there?	3.
Bui Chun	How many animals have 4 legs? 8? 3?	4.
Frequency Bar Chart	What percent of the total weight at the shelter is made up by Boo-boo?	5.
	What is the distribution of weights across all the animals older than 3?	6.
Histogram	How many animals are there of each species?	7.
	Who waited the longest to be adopted?	8.

Unit 9

- **Scatter Plots** show the relationship between two quantitative columns. Each row in the dataset is represented by a point, with one column providing the x-value and the other providing the y-value. The resulting "point cloud" makes it possible to look for a relationship between those two columns.
- If the points in a scatter plot appear to follow a pattern, it is possible that a relationship or **correlation** exists between those two columns.
- If there is a pattern to the points in a scatter plot, points that are far away from the pattern are called **outliers**.
- We can express this correlation by drawing line through the data cloud, so that
 the distance between the line and each of the points is as small as possible. This
 line is called the line of best fit or predictor function and allows us to make
 predictions based on the dataset.

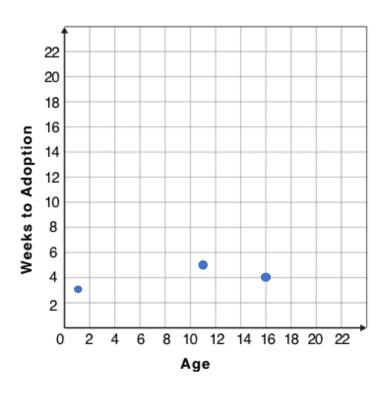
(Dis)Proving a Claim

"Younger animals are cuter, so they get adopted faster."

Do you agree? If so, why?
I hypothesize
What would you look for in the dataset to see if you are right?

Creating a Scatter Plot

name	species	age	weeks
"Sasha"	"cat"	1	3
"Boo-boo"	"dog"	11	5
"Felix"	"cat"	16	4
"Buddy"	"lizard"	2	24
"Nori"	"dog"	6	9
"Wade"	"cat"	1	2
"Nibblet"	"rabbit"	6	12
"Maple"	"dog"	3	2



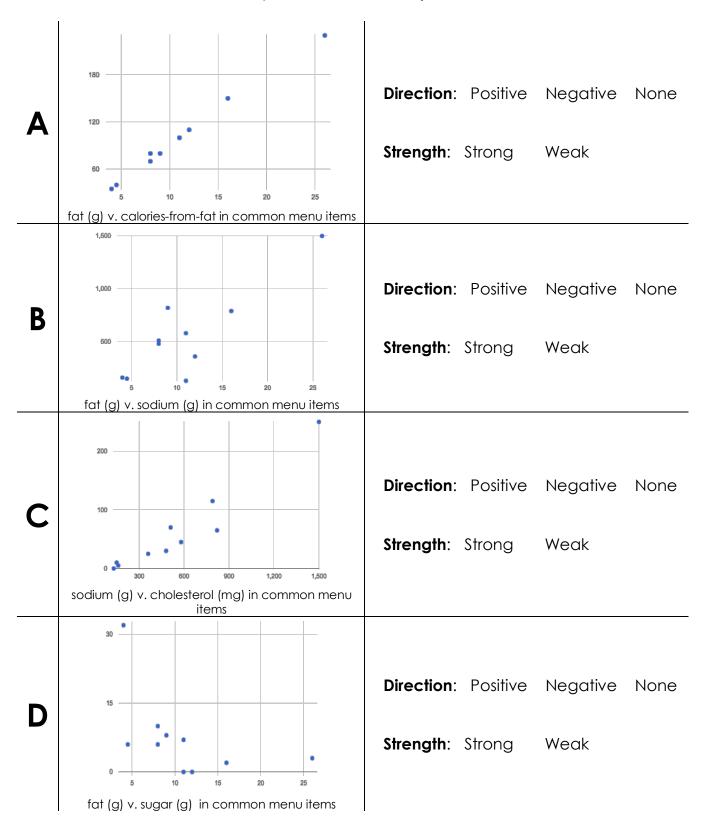
- 1. For each row in the Sample Table on the left, add a point to the scatter plot on the right. The first 3 rows have been completed for you. Use the values from the age column for the x-axis, and values from the weeks column for the y-axis.
- 2. Do you see a pattern? Do the points seem to shift up or down as age increases? **Draw a line on the scatter plot to show this pattern**.
- 3. Does the line slope upwards or downwards?
- 4. Are the points mostly close to the line?

Define a function <code>dogs-age-weeks</code>, which takes in a Table of animals and creates a scatter plot of all the dogs, tracking their <code>age</code> on the x-axis and the number of <code>weeks</code> it took for them to be adopted on the y-axis.

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Drawing Predictors

For each of the scatter plots below, draw a predictor line that fits best.



Correlations in My Dataset

1) There may be a correlation between		and
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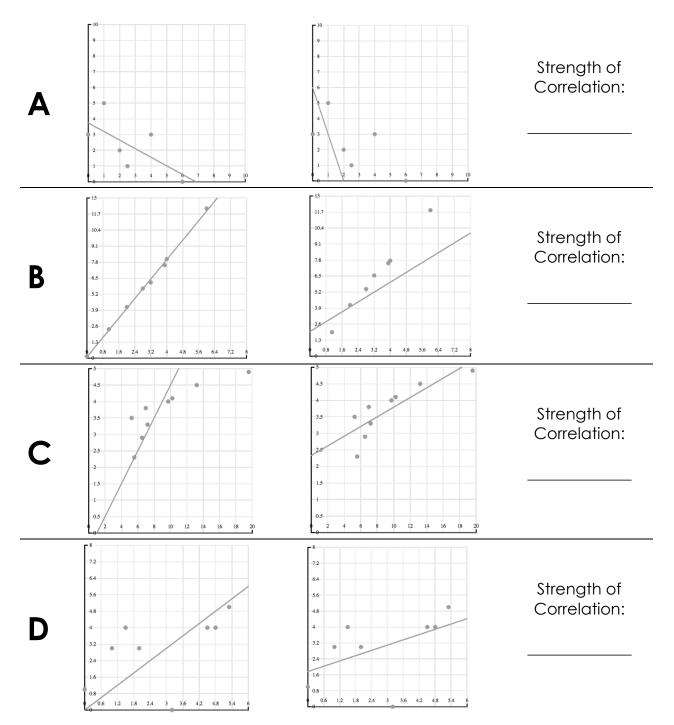
Unit 10

- Given a **predictor function** and a scatter plot, we can compute the error by adding the squares of all the distances between the function and each point in the plot. The error is called the **r**² **statistic**, which tells us how much of the variation in the y-axis can be explained by the x-axis.
- A strong correlation will have a large r^2 . A weak correlation will have a small r^2 .
- A **positive correlation** means the slope of the line of best fit is positive. A **negative correlation** means the slope is negative.
- **Linear Regression** is a way of computing the **line of best fit**, by taking a scatter plot and deriving the slope and y-intercept for a line that has the smallest possible r².
- <u>Correlation is not causation!</u> Correlation only suggests that two measures are related, but does not tell us if one causes the other. For example, hot days are correlated with people running their air conditioners, air conditioners do not cause hot days!

Grading Predictors

Below are the scatter plots for data sets A-D, with two different lines predictor lines drawn on top. For plots A-D:

- 1. Circle the plot with the line that fits better
- 2. Give the plot you circled a grade between 0 (no correlation) and 1 (perfect correlation)



Findings in the animals Dataset

I performed a linear regression on		dogs at the shelter		, and
			dataset or subset	
found	a weak (r²=0.	25), positive	correlation bet	ween
age of the do	o gs (in weeks) -axis]	and <u>number of</u>	weeks to be adopted axis]	From this, I
conclude that	25% of the v	ariability in adopt	ion time is explained explained by [x-axis]	
		on in [y-axis] is ϵ	explained by [x-axis]	
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Correlations in My Dataset

I performed a linear regression on	, and
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and	From this, I
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r^2 % of the variation in [<pre>γ-axis] is explained by [x-axis]</pre>

Unit 11

Fake News!

Every claim below is wrong! Your job is to figure out why, by looking at the data.

	Data	Claim	Why it's wrong
1	The average player on a basketball team is 6'1".	"Most of the players on the team are taller than 6'."	
2	After performing linear regression on census data, a positive correlation (r ² =0.18) was found between people's height and salary.	"Taller people get paid more."	
3	y=12.234x + -17.089; r-sq: 0.636	"According to the predictor function indicated here, the value on the x-axis is will predict the value on the y-axis 63.6% of the time."	
4	15 Sasha Felix Wade Boo-boo Maple Nori Bar Chart of Pet Ages	"According to this bar chart, Felix makes up a little more than 15% of the total ages of all the animals in the dataset."	
5	1 0 20 40 60 80 100 120 140 160 180 Weight (pounds)	"According to this histogram, most animals weigh between 40 and 60 pounds."	
6	After performing linear regression, a negative correlation (r ² =0.91) was found between the number of hairs on a person's head and their likelihood of owning a wig.	"Owning wigs causes people to go bald."	

Blank Recipes, Table Plans, and References

Design Recipes

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Design Recipes

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Table Plan

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Table Plan

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Table Plan

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			\rightarrow			
Define the function						
Use the relevant meth	nods (circle your	helper fur	nctions!),	then proc	duce a result	with the new table.
fun		_ ()	:		Define the table
<u>† =</u>						-
						Are there more columns?
						Are there fewer rows?
						Are the rows ordered?
						Produce the result
end						

Contracts

Name	Domain		Range
triangle	:: (side-length :: Number, style :: String, color :: String)	\rightarrow	Image
circle	:: (radius :: Number, style :: String, color :: String)	\rightarrow	Image
star	:: (radius :: Number, style :: String, color :: String)	\rightarrow	Image
rectangle	:: (width :: Num, height :: Num, style :: Str, color :: Str)	\rightarrow	Image
ellipse	:: (width :: Num, height :: Num, style :: Str, color :: Str)	\rightarrow	Image
square	:: (size-length :: Number, style :: String, color :: String)	\rightarrow	Image
text	:: (str :: String, size :: Number, color :: String)	\rightarrow	Image
overlay	:: (img1 :: <i>Image</i> , img2 :: <i>Image</i>)	\rightarrow	Image
rotate	:: (degree :: Number, img :: Image)	\rightarrow	Image
scale	:: (factor :: Number, img :: Image)	\rightarrow	Image
string-repeat	:: (text :: String, repeat :: Number)	\rightarrow	String
string-contains	:: (text :: String, search-for :: String)	\rightarrow	Boolean
num-sqr	:: (n :: Number)	\rightarrow	Number
num-sqrt	:: (n :: Number)	\rightarrow	Number
num-min	:: (a :: Number, b:: Number)	\rightarrow	Number
num-max	:: (a :: Number, b:: Number)	\rightarrow	Number
get-row	:: (t :: Table, index :: Number)	\rightarrow	Row

Contracts

Name	Domain		Range
<table>.row-n</table>	:: (n :: Number)	\rightarrow	Row
<table>.order-by</table>	:: (col :: String, increasing :: Boolean)	\rightarrow	Table
<table>.filter</table>	:: (test :: (Row → Boolean))	\rightarrow	Table
<table>.build-column</table>	:: (col :: String, builder :: (Row → Value))	\rightarrow	Table
mean	$:: (\underline{t} :: Table, col :: String)$	\rightarrow	Number
median	:: (t :: Table, col :: String)	\rightarrow	Number
modes	:: (t :: Table, col :: String)	\rightarrow	List <number></number>
bar-chart	:: (t :: Table, labels :: String, values :: String)	\rightarrow	Image
pie-chart	:: (t :: Table, labels :: String, values :: String)	\rightarrow	Image
box-plot	:: (t :: Table, col:: String)	\rightarrow	Image
freq-bar-chart	:: (t :: Table, values :: String)	\rightarrow	Image
histogram	:: (t :: Table, values :: String, bin-width :: Number)	\rightarrow	Image
scatter-plot	:: (t :: Table, xs :: String, ys :: String)	\rightarrow	Image
labeled-scatter-plot	:: (t :: Table, labels :: String, xs :: String, ys :: String)	\rightarrow	Image
lr-plot	:: (t :: Table, xs :: String, ys :: String)	\rightarrow	Image
labeled-lr-plot	:: (t :: Table, labels :: String, xs :: String, ys :: String)	\rightarrow	Image