Peter Smith, Introduction to Formal Logic (CUP, 2nd edition)

Exercises 30: More QL translations

In QL_2 , the proper names with their interpretations are

- m: Maldwyn,
- n: Nerys,
- o: Owen;

and the predicates are

- F: ① is a man,
- G: ① is a woman,
- L: 1 loves 2.
- M: ① is married to ②,
- R: ① is a child of ② and ③.

The domain of quantification: people (living people, for definiteness).

- (a) Translate the following into QL_2 :
 - (1) Maldwyn loves anyone who loves Owen.
 - (2) Everyone loves whoever they are married to.
 - (3) Some man is a child of Owen and someone or other.
 - (4) Whoever is a child of Maldwyn and Nerys loves them both.
 - (5) Owen is a child of Nerys and someone who loves Nerys.
 - (6) Some men do not love those who they are married to.
 - (7) Every man who loves Nerys loves someone who is married to Owen.
 - (8) No woman is loved by every married man.
 - (9) Everyone who loves Maldwyn loves no one who loves Owen.
 - (10) Whoever loves Maldwyn loves a man only if the latter loves Maldwyn too.
- (11) Only if Maldwyn loves every woman does he love whoever is married to Owen.
- (12) No one loves anyone who has no children.
- (b) Now consider the language QL_3 whose quantifiers range over the positive integers, with the following glossary:
 - n: one,
 - F: ① is odd,
 - G : ① is even,
 - H: ① is prime,
 - L: ① is less than ②,
 - R: ① is the sum of ② and ③.

Then translate the following into natural English (they are not all true!):

- (1) $\forall x \forall y \exists z Rzxy$
- (2) $\exists y \forall x Lxy$
- (3) $\forall x \exists y (Lxy \land Hy)$
- (4) $\forall x(Hx \rightarrow \exists y(Lxy \land Hy))$
- (5) $\forall x \forall y ((Fx \land Ryxn) \rightarrow \neg Fy)$
- (6) $\forall x \exists y ((Gx \land Fy) \land Rxyy)$
- (7) $\forall x \forall y (\exists z (Rzxn \land Ryzn) \rightarrow (Gx \rightarrow Gy))$
- (8) $\forall x \forall y \forall z (((Fx \land Fy) \land Rzxy) \rightarrow Gz)$
- (9) $\forall x((Gx \land \neg Rxnn) \rightarrow \exists y \exists z((Hy \land Hz) \land Rxyz))$
- (10) $\forall x \exists y ((Hy \land Lxy) \land \exists w \exists z ((Rwyn \land Rzwn) \land Hz))$