

Ars Digita University

Theory of Computation

Recitation 5 , 05/09/01

Topics

- Decision Problems
- Context free grammars.

Problems to work on

Decision Problems

1. Finish the decision problems from the last recitation handout.

CFG warmup

2. Give a context free grammar that generates the language of palindromes $\{w(0+1+\epsilon)w^R \mid w \text{ is in } (0+1)^*\}$
3. Give a context free grammar that generates every possible string over $\{0,1\}$
4. Give a context free grammar that generates the language $0^n 1 0^n 111 0^m 1^r$ where $n, m, r \geq 0$
5. Give a context free grammar that generates the language of all strings that contain 101.
6. Give a context free grammar that generates the language of all strings with an equal number of zeros and ones.

And/Or

7. Give a context free grammar that generates the language that has equal numbers of 0's and 1's or contains 101.
8. Give a context free grammar that generates the language that has equal numbers of 0's and 1's and contains 101.

Complements

9. Give a context free grammar that generates the language of all strings of the form $0^m 1^n$ where $n \geq m \geq 0$.
10. Give a context free grammar that generates the language of all strings of the form $0^m 1^n$ where $n > m \geq 0$.
11. Give a context free grammar that generates the complement of the language $0^* 1^*$.
12. Give a context free grammar that generates the language $\{w \mid w \text{ is not equal to } 0^n 1^n\}$

for any choice of n }

13. Challenging problem: Give a context free grammar that generates the language $\{ w \mid w \text{ is not a palindrome} \}$

Dimitri Kountourogiannis, dimitrik@alum.mit.edu