CS143 Spring 2022 – Written Assignment 2 Monday, April 25, 2022 11:59 PM PDT

This assignment covers context free grammars and parsing. You may discuss this assignment with other students and work on the problems together. However, your write-up should be your own / u

Assignment review the policies	nts can be submitte e the course polici /. A LATEX templa	ed electronica es for more in ate for writing	lly through Gradeson formation: https: gyour solutions is a	n who you worked with, cope as a PDF by 11:59 PM //web.stanford.edu/callable on the course wet package: https://ct	A PDT. Please class/cs143/rebsite. If you
acce		ambiguous g	•	ollowing languages. Any as it has the correct la	
(a)		sion evaluates	to some even value	epresenting valid produce.	ets of integers
		112	2*121	221*1*1122	
	Strings not in the Language:				
		arepsilon	11*121	12**22*112	
(b)	The set of all strings over the alphabet $\{x, (,), ;\}$ representing nested tuples of x 's where each tuple has an even length. Example Strings in the Language:				
		()	(x;())	(();x;(();x);x)	
	Strings not in the	e Language:			
	arepsilon	x	(();x;x)	(x;();(x;();x);	x)
(c)	The set of all strings over the alphabet $\{0,1\}$ where the number of 1's is exactly one more than the number of 0's. Example Strings in the Language:				
		1	101	001110101	
	Strings not in the Language:				
		arepsilon	001	01100101	
(d)	The set of all strings over the alphabet $\{0,1\}$ in the language $L:\{0^i1^j0^k\mid j\neq i+k\}$. Example Strings in the Language:				
		00	110000	000111110	
	Strings not in the	e Language:			
		arepsilon	0011	01111000	

2. Consider the following grammar for if-then-else expressions that involve a variable x:

$$E \to \text{if } x \text{ then } E \mid M$$

 $M \to \text{if } x \text{ then } M \text{ else } E \mid x$

Is this grammar ambiguous or not? If yes, give an example of an expression with two different parse trees and draw the two parse trees. If not, explain why that is the case.

3. (a) Eliminate left recursion from the following grammar:

$$S \to S(T) \mid Sa \mid [T] \mid Tb$$
$$T \to T(S) \mid Tc \mid d$$

(b) Left factor the following grammar:

$$S \rightarrow (T+T) \mid (T)$$

$$T \rightarrow U * T \mid U * ? \mid [U]$$

$$U \rightarrow U0 \mid U1 \mid \varepsilon$$

4. Consider the following CFG, where the set of terminals is $\{a, b, c, d, \#, ?\}$:

$$S \to \#UT \mid T?$$

$$T \to aS \mid bUc \mid \varepsilon$$

$$U \to aSc \mid bTd$$

- (a) Construct the FIRST sets for each of the nonterminals.
- (b) Construct the FOLLOW sets for each of the nonterminals.
- (c) Construct the LL(1) parsing table for the grammar.
- (d) Show the sequence of stack, input and action configurations that occur during an LL(1) parse of the string "#a?ca?". At the beginning of the parse, the stack should contain a single S.
- 5. Consider the following grammar G over the alphabet $\{a, b, c\}$:

$$S' \rightarrow S$$

$$S \rightarrow Aa$$

$$S \rightarrow Bb$$

$$A \rightarrow Ac$$

$$A \rightarrow \varepsilon$$

$$B \rightarrow Bc$$

$$B \rightarrow \varepsilon$$

You want to implement G using an SLR(1) parser. Note that we have already added the $S' \to S$ production for you.

- (a) Construct the first state of the LR(0) machine, compute the FOLLOW sets of A and B, and point out the conflicts that prevent the grammar from being SLR(1).
- (b) Show modifications to production $4 (A \to Ac)$ and production $6 (B \to Bc)$ to make the grammar SLR(1) while having the same language as the original grammar G. Explain the intuition behind this result.