

Peak Index in a Mountain Array

(Divide-and-Conquer)

Problem Statement

- The **Peak Index in a Mountain Array** refers to the index of the maximum element in a *mountain array*.
- A **mountain array** is an array that satisfies the following properties:
 - It contains at least three elements.
 - There exists an index i (the peak index) such that:
 - $\text{arr}[0] < \text{arr}[1] < \dots < \text{arr}[i-1] < \text{arr}[i]$ (strictly increasing sequence up to the peak).
 - $\text{arr}[i] > \text{arr}[i+1] > \dots > \text{arr}[\text{arr.length}-1]$ (strictly decreasing sequence after the peak).
- Thus, a mountain array has one peak element where the array values first increase and then decrease.
- The **peak index** is the position of this maximum element.

Examples

- For the array [1, 3, 5, 4, 2]:
 - The peak element is 5, and its index is 2.
 - So, the peak index is 2.
- Array: [10, 20, 30, 40, 35, 25, 15, 5]
 - Peak Element: 40
 - Peak Index: 3
- Array: [0, 10, 5, 2]
 - Peak Element: 10
 - Peak Index: 1

Brute force approach

Brute force approach

- Initialize a variable to keep track of the maximum value found so far (`max_value`) and its corresponding index (`peak_index`).
- Traverse the array from left to right: Compare each element with `max_value`.
- If the current element is greater than `max_value`, update `max_value` and set `peak_index` to the current index.
- After traversing the entire array, the `peak_index` will hold the index of the peak element
- Time Complexity: $O(n)$

Divide-and-Conquer approach

DAC Approach

- Start with two pointers, $low=0$ and $high=arr.length-1$
- Compute the mid-point: $mid=(low+high)/2$
- If $arr[mid]<arr[mid+1]$, the peak is in the right half ($low=mid+1$)
- Otherwise, the peak is in the left half ($high=mid$).
- Continue until $low==high$, and that index is the peak index.
- Time Complexity: $O(\log n)$

Pseudocode

```
1.  #include <vector>
2.  class Solution {
3.  public:
4.  int peakIndexInMountainArray(vector<int>& arr) {
5.      int left = 1; // Starting from 1 because the peak cannot be the first element
6.      int right = arr.size() - 2; // Ending at size - 2 because the peak cannot be the last element
7.      while (left < right) {
8.          int mid = (left + right) >> 1;
9.          if (arr[mid] > arr[mid + 1]) {
10.             right = mid;
11.          } else {
12.             left = mid + 1;}}
13.     return left;}};
```


Example

Example

- Let's consider a sample mountain array `arr = [1, 3, 5, 4, 2]` to illustrate the solution approach:



- Initialize two pointers, `left = 1` and `right = len(arr) - 2 = 3`, to avoid checking the first and last elements as they cannot be the peak by definition.



- Start the while loop since `left < right` (`1 < 3` is true).
- Calculate the midpoint `mid` using `(left + right) >> 1`. For our example, it's `(1 + 3) >> 1`, which equals 2.



Example

- Compare $\text{arr}[\text{mid}]$ to $\text{arr}[\text{mid} + 1]$. For $\text{mid} = 2$, $\text{arr}[\text{mid}]$ is 5 and $\text{arr}[\text{mid} + 1]$ is 4. Because $5 > 4$, we update right to mid. Now **left** = 1 and **right** = 2.



- The loop continues because $\text{left} < \text{right}$ is still true.
- Recalculate the midpoint with the updated pointers. Now, **mid** is $(1 + 2) \gg 1$, which equals 1.



Example

- Compare $\text{arr}[\text{mid}]$ to $\text{arr}[\text{mid} + 1]$ again. For $\text{mid} = 1$, $\text{arr}[\text{mid}]$ is 3 and $\text{arr}[\text{mid} + 1]$ is 5. Because $3 < 5$, we update left to $\text{mid} + 1$. Now left = 2 and right = 2.

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1	3	5	4	2
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- The loop ends because left equals right, indicating convergence at the peak's index, which is 2 in our example array.
- Return left, which is the peak index. In our array, $\text{arr}[2]$ is indeed the peak with a value of 5.