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5 5555 5555555555555555555555555555555	1.1 1/2 Enumeration 1.2 ax+by=gcd 1.3 Pollard Rho 1.4 Pi Count (Linear Sieve) 1.5 Strling Number 1.5 5.1 First Kind 1.5 5.2 Second Kind 1.6 Range Sieve 1.7 Miller Rabin 1.8 Extended Euler 1.9 Gauss Elimination 1.10 Fast Fourier Transform 1.11 Chinese Remainder 1.12 Berlekamp Massey 1.13 NTT 1.14 Polynomial Operations 1.15 FWT 1.16 DiscreteLog 1.17 FloorSum 1.18 Quadratic residue 1.19 De-Bruijn 1.20 Simplex Construction 1.21 Simplex 1.22 Charateristic Polynomial 1.23 Partition Number 1.25 Secometry 1.15 Basic Geometry 1.16 Basic Geometry 1.17 Basic Geometry 1.17 Polynomial 1.20 Polynomial 1.20 Polynomial 1.21 Polynomial 1.22 Polynomial 1.23 Partition Number 1.25 Polynomial 1.25 Polyno	12 m	<pre>Wconversion -fsanitize=address, und success<cr> map <f9> <esc>:w<cr>:!g++ "%" -o "%<" echo success<cr> map <f10> <esc>:!./"%<"<cr> 1.2 Debug Macro #ifdef KISEKI #define safe cerr<<pretty_function "<<_line<<"="" #define="" <<"="" <typenamet="" a)="" debug(a)="" dvorak(#a,="" line="" orange(a)="" qwerty(#a,="" safe\n"="" std::cerr;="" template="" using=""> void qwerty(const char *s, Ta) { cerr << "\e[1;32m(" << s << ") = ("; int cnt = sizeof(T); (, (cerr << a << (cnt ? ", " : } template <typename iter=""> void dvorak(const char *s, Iter L, Ite cerr << "\e[1;32m[" << s << "] = [for (int f = 0; L != R; ++L) cerr << (f++ ? ", " : "") << *L; cerr << "]\e[0m\n"; }</typename></pretty_function></cr></esc></f10></cr></cr></esc></f9></cr></pre>
5 5555 55555555555 G666	1.1 1/2 Enumeration 1.2 ax+by=gcd 1.3 Pollard Rho 1.4 Pi Count (Linear Sieve) 1.5 Strling Number 1.5 5.5 First Kind 1.5 5.2 Second Kind 1.6 Range Sieve 1.7 Miller Rabin 1.8 Extended Euler 1.9 Gauss Elimination 1.10 Fast Fourier Transform 1.11 Chinese Remainder 1.12 Berlekamp Massey 1.13 NTT 1.14 Polynomial Operations 1.15 FWT 1.16 DiscreteLog 1.17 FloorSum 1.18 Quadratic residue 1.19 De-Bruijn 1.20 Simplex 1.21 Simplex 1.22 Charateristic Polynomial 1.23 Partition Number 1.25 Basic Geometry 1.18 Basic Geometry 1.25 Basic Geometry 1.25 Convex Hull 1.25 Tolor Sum 1.26 Tolor Sum 1.27 Tolor Sum 1.28 Tolor Sum 1.29 Tolor Sumplex 1.20	12 m	<pre>Wconversion -fsanitize=address, und success<cr> nap <f9> <esc>:w<cr>:!g++ "%" -o "%<" echo success<cr> map <f10> <esc>:!./"%<"<cr> 1.2 Debug Macro #ifdef KISEKI #define safe cerr<<pretty_function "<<_line<<"="" #define="" <<"="" <typenamet="" a)="" debug(a)="" dvorak(#a,="" line="" orange(a)="" qwerty(#a,="" safe\n"="" std::cerr;="" template="" using=""> void qwerty(const char *s, Ta) { cerr << "\e[1;32m(" << s << ") = ("; int cnt = sizeof(T); (, (cerr << a << (cnt ? ", " : } template <typename iter=""> void dvorak(const char *s, Iter L, Ite cerr << "\e[1;32m[" << s << "] = [for (int f = 0; L != R; ++L) cerr << (f++ ? ", " : "") << *L; cerr << " \e[0m\n";</typename></pretty_function></cr></esc></f10></cr></cr></esc></f9></cr></pre>
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5 555555555555555555555555555555555555	1.1	12 m	Wconversion -fsanitize=address, und success <cr> map <f9> <esc>:w<cr>:!g++ "%" -o "%<" echo success<cr> map <f10> <esc>:!./"%<"<cr> 1.2 Debug Macro #ifdef KISEKI #define safe cerr<<pretty_function "<<_line<"="" #define="" <<"="" <typenamet="" a)="" debug(a)="" dvorak(#a,="" line="" orange(a)="" qwerty(#a,="" safe\n"="" std::cerr;="" template="" using=""> void qwerty(const char *s, Ta) { cerr << "\e[1;32m(" << s << ") = ("; int cnt = sizeof(T); (, (cerr << a << (cnt ? ", " : } template <typename iter=""> void dvorak(const char *s, Iter L, Iter cerr << "\e[1;32m[" << s << "] = [for (int f = 0; L != R; ++L)</typename></pretty_function></cr></esc></f10></cr></cr></esc></f9></cr>
5 555555555555555555555555555555555555	1	12 m	Wconversion -fsanitize=address, und success <cr> map <f9> <esc>:w<cr>:!g++ "%" -o "%<" echo success<cr> map <f10> <esc>:!./"%<"<cr> 1.2 Debug Macro #ifdef KISEKI #define safe cerr<<pretty_function "<<_line<"="" #define="" <<"="" <typenamet="" a)="" debug(a)="" dvorak(#a,="" line="" orange(a)="" qwerty(#a,="" safe\n"="" std::cerr;="" template="" using=""> void qwerty(const char *s, Ta) { cerr << "\e[1;32m(" << s << ") = ("; int cnt = sizeof(T); (, (cerr << a << (cnt ? ", " : } template <typename iter=""> void dvorak(const char *s, Iter L, Iter cerr << "\e[1;32m[" << s << "] = [for (int f = 0; L != R; ++L)</typename></pretty_function></cr></esc></f10></cr></cr></esc></f9></cr>
5 555555555555555555555555555555555555	1	12 m	Wconversion -fsanitize=address, und success <cr> map <f9> <esc>:w<cr>:!g++ "%" -o "%<" echo success<cr> map <f10> <esc>:!./"%<"<cr> 1.2 Debug Macro #ifdef KISEKI #define safe cerr<<pretty_function "<<_line<"="" #define="" <<"="" <typenamet="" a)="" debug(a)="" dvorak(#a,="" line="" orange(a)="" qwerty(#a,="" safe\n"="" std::cerr;="" template="" using=""> void qwerty(const char *s, Ta) { cerr << "\e[1;32m(" << s << ") = ("; int cnt = sizeof(T); (, (cerr << a << (cnt ? ", " : } template <typename iter=""> void dvorak(const char *s, Iter L, Iter cerr << "\e[1;32m[" << s << "] = [for (int f = 0; L != R; ++L)</typename></pretty_function></cr></esc></f10></cr></cr></esc></f9></cr>
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5 555555555555555555555555555555555555	1	12 m	<pre>Wconversion -fsanitize=address, und success<cr> map <f9> <esc>:w<cr>:!g++ "%" -o "%<" echo success<cr> map <f10> <esc>:!./"%<"<cr> 1.2 Debug Macro #ifdef KISEKI #define safe cerr<<pretty_function "<<_line<"="" #define="" #sing="" <<"="" <typenamet="" a)="" debug(a)="" dvorak(#a,="" line="" orange(a)="" qwerty(#a,="" safe\n"="" std::cerr;="" template=""> #void qwerty(const char *s, Ta) { cerr << "\e[1;32m(" << s << ") = ("; int cnt = sizeof(T); (, (cerr << a << (cnt ? ", " : } template <typename iter=""> #void dvorak(const char *s, Iter L, Iter cerr << "\e[1;32m[" << s << "] = [for (int f = 0; L != R; ++L) cerr << (f++ ? ", " : "") << *L; cerr << "]\e[0m\n"; } #else #define safe ((void)0) #define debug() ((void)0) #define orange() ((void)0) #endif 1.3 Increase Stack const int size = 256 << 20; register long rsp asm("rsp"); char *p = (char*)malloc(size)+size, *b</typename></pretty_function></cr></esc></f10></cr></cr></esc></f9></cr></pre>
5 555555555555555555555555555555555555	1.1 L	12 m	Wconversion -fsanitize=address, und success <cr> map <f9> <esc>:w<cr>:!g++ "%" -o "%<" echo success<cr> map <f10> <esc>:!./"%<"<cr> 1.2 Debug Macro #ifdef KISEKI #define safe cerr<<pretty_function< td=""></pretty_function<></cr></esc></f10></cr></cr></esc></f9></cr>
5 555555555555555555555555555555555555	1.1	12 m	<pre>Wconversion -fsanitize=address, und success<cr> map <f9> <esc>:w<cr>:!g++ "%" -o "%<" echo success<cr> map <f10> <esc>:!./"%<"<cr> 1.2 Debug Macro #ifdef KISEKI #define safe cerr<<pretty_function "<<_line<"="" #define="" #sing="" <<"="" <typenamet="" a)="" debug(a)="" dvorak(#a,="" line="" orange(a)="" qwerty(#a,="" safe\n"="" std::cerr;="" template=""> #void qwerty(const char *s, Ta) { cerr << "\e[1;32m(" << s << ") = ("; int cnt = sizeof(T); (, (cerr << a << (cnt ? ", " : } template <typename iter=""> #void dvorak(const char *s, Iter L, Iter cerr << "\e[1;32m[" << s << "] = [for (int f = 0; L != R; ++L) cerr << (f++ ? ", " : "") << *L; cerr << "]\e[0m\n"; } #else #define safe ((void)0) #define debug() ((void)0) #define orange() ((void)0) #endif 1.3 Increase Stack const int size = 256 << 20; register long rsp asm("rsp"); char *p = (char*)malloc(size)+size, *b</typename></pretty_function></cr></esc></f10></cr></cr></esc></f9></cr></pre>

```
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             (concave/convex) . . . . . . . . . . . . . . . . .
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             (concave/convex) . . . . . . . . . . . . . . . . .
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             a encoding=utf-8 ls=2
             4 sts=4 tgc sc hls
             g++ "%" -o "%<" -std=c++17 -
             tra -Wshadow -Wfatal-errors -
```

```
tize=address,undefined -g && echo
g++ "%" -o "%<" -02 -std=c++17 &&
<CR>
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```
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/orak(#a, a)
*s, T ...a) {
<< s << ") = (";
);
 --cnt ? ", " : ")\e[0m\n")));
*s, Iter L, Iter R) { << s << " ] = [ ";
R; ++L)
' : "") << *L;
oid)0)
/oid)0)
```

```
< 20;
"rsp");
c(size)+size, *bak = (char*)rsp;
p\n"::"r"(p));
```

1.4 Pragma Optimization

```
#pragma GCC target("sse,sse2,sse3,ssse3,sse4")
#pragma GCC target("popcnt,abm,mmx,avx,tune=native")
1.5 IO Optimization
static inline int gc() {
  constexpr int B = 1 << 20;
  static char buf[B], *p, *q;
  if(p == a \&\&
    (q=(p=buf)+fread(buf,1,B,stdin)) == buf)
   return EOF;
  return *p++;
template < typename T >
static inline bool gn( T &x ) {
 int c = gc(); T sgn = 1; x = 0;
while(('0'>c||c>'9') && c!=EOF && c!='-') c = gc();
if(c == '-') sgn = -1, c = gc();
 if(c == EOF) return false;
 while('0'<=c&&c<='9') x = x*10 + c - '0', c = gc();
 return x *= sgn, true;
```

#pragma GCC optimize("Ofast,no-stack-protector")

#pragma GCC optimize("no-math-errno,unroll-loops")

2 Data Structure

2.1 Dark Magic

2.2 Link-Cut Tree

p->ch[dir]=c;

```
struct Node{
Node *par, *ch[2];
int xor_sum, v;
bool is_rev;
Node(int _v){
 v=xor_sum=_v;is_rev=false;
 par=ch[0]=ch[1]=nullptr;
inline void set_rev(){is_rev^=1;swap(ch[0],ch[1]);}
inline void down(){
 if(is_rev){
  if(ch[0]!=nullptr) ch[0]->set_rev();
   if(ch[1]!=nullptr) ch[1]->set_rev();
   is_rev=false;
 }
inline void up(){
 xor_sum=v;
  if(ch[0]!=nullptr){
  xor_sum^=ch[0]->xor_sum;
  ch[0]->par=this;
 if(ch[1]!=nullptr){
  xor_sum^=ch[1]->xor_sum;
  ch[1]->par=this;
inline bool is_root(){
 return par==nullptr ||\
   (par->ch[0]!=this && par->ch[1]!=this);
bool is_rch(){return !is_root() && par->ch[1]==this;}
} *node[maxn], *stk[maxn];
int top;
void to_child(Node* p,Node* c,bool dir){
```

```
p->up();
inline void rotate(Node* node){
 Node* par=node->par;
 Node* par_par=par->par;
 bool dir=node->is_rch()
 bool par_dir=par->is_rch()
 to_child(par, node->ch[!dir], dir);
 to_child(node,par,!dir);
 if(par_par!=nullptr && par_par->ch[par_dir]==par)
  to_child(par_par,node,par_dir);
 else node->par=par_par;
inline void splay(Node* node){
 Node* tmp=node;
 stk[top++]=node;
 while(!tmp->is_root()){
  tmp=tmp->par;
  stk[top++]=tmp;
 while(top) stk[--top]->down();
 for(Node *fa=node->par;
  !node->is_root();
  rotate(node), fa=node->par)
  if(!fa->is_root())
   rotate(fa->is_rch()==node->is_rch()?fa:node);
inline void access(Node* node){
 Node* last=nullptr;
 while(node!=nullptr){
  splay(node);
  to_child(node, last, true);
  last=node;
  node=node->par;
inline void change_root(Node* node){
 access(node);splay(node);node->set_rev();
inline void link(Node* x, Node* y){
 change_root(x);splay(x);x->par=y;
inline void split(Node* x,Node* y){
 change_root(x);access(y);splay(x);
 to_child(x,nullptr,true);y->par=nullptr;
inline void change_val(Node* node,int v){
access(node);splay(node);node->v=v;node->up();
inline int query(Node* x,Node* y){
 change_root(x);access(y);splay(y);
 return y->xor_sum;
inline Node* find_root(Node* node){
 access(node);splay(node);
 Node* last=nullptr:
 while(node!=nullptr){
  node->down();last=node;node=node->ch[0];
 return last;
set<pii> dic;
inline void add_edge(int u,int v){
 if(u>v) swap(u,v)
 if(find_root(node[u])==find_root(node[v])) return;
 dic.insert(pii(u,v))
link(node[u],node[v]);
inline void del_edge(int u,int v){
 if(u>v) swap(u,v);
 if(dic.find(pii(u,v))==dic.end()) return;
 dic.erase(pii(u,v))
 split(node[u],node[v]);
2.3 LiChao Segment Tree
struct Line{
 int m, k, id;
 Line() : id( -1 ) {}
Line('int a, int'b,'int c')
: m(a), k(b), id(c) {}
```

int at(int x) { return m * x + k; }

```
private:
class LiChao {
                                                              vector< vector< T > > tbl;
private:
                                                              vector< int > lg;
                                                              T cv(Ta, Tb) {
  int n; vector< Line > nodes;
  inline int lc( int x ) { return 2 * x + 1; }
                                                               return Cmp_()( a, b ) ? a : b;
  inline int rc( int x ) { return 2 * x + 2; }
  void insert( int 1, int r, int id, Line ln ) {
                                                             public:
   int m = (1 + r) >> 1;
                                                              void init( T arr[], int n ) {
   if ( nodes[ id ].id == -1 ) {
                                                               // 0-base
   nodes[ id ] = ln;
                                                               lg.resize(n+1);
                                                               lg[0] = -1;
    return:
                                                               for( int i=1 ; i<=n ; ++i ) lg[i] = lg[i>>1] + 1;
   bool atLeft = nodes[ id ].at( 1 ) < ln.at( 1 );</pre>
                                                               tbl.resize(lg[n] + 1);
   if ( nodes[ id ].at( m ) < ln.at( m ) ) {</pre>
                                                               tbl[ 0 ].resize( n );
                                                               copy( arr, arr + n, tbl[ 0 ].begin() );
   atLeft ^= 1; swap( nodes[ id ], ln );
                                                               for ( int i = 1 ; i <= lg[ n ] ; ++ i ) {
  int len = 1 << ( i - 1 ), sz = 1 << i;</pre>
   if ( r - l == 1 ) return;
                                                                tbl[ i ].resize( n - sz + 1 );
   if ( atLeft ) insert( l, m, lc( id ), ln );
                                                                for (int_j = 0; j \le n - sz; ++ j
   else insert( m, r, rc( id ), ln );
                                                                 tbl[i][j] = cv(tbl[i-1][j], tbl[i-1][j+len]);
  int query( int 1, int r, int id, int x ) {
   int ret = 0;
   if ( nodes[ id ].id != -1 )
                                                              T query( int 1, int r ) {
                                                               // 0-base [1, r)
   ret = nodes[ id ].at( x );
   int m = (1 + r) >> 1;
                                                               int wh = lg[ r - l ], len = 1 << wh;</pre>
                                                               return cv( tbl[ wh ][ 1 ], tbl[ wh ][ r - len ] );
   if ( r - l == 1 ) return ret;
   else if (x < m )
                                                            };
    return max( ret, query( 1, m, lc( id ), x ) );
   else
                                                             2.6
                                                                  Linear Basis
    return max( ret, query( m, r, rc( id ), x ) );
                                                             template <int BITS>
public:
                                                             struct LinearBasis {
 void build( int n_ ) {
                                                              array<uint64_t, BITS> basis;
                                                              Basis() { basis.fill(0); }
  n = n_; nodes.clear();
  nodes.resize( n << 2, Line() );</pre>
                                                              void add(uint64_t x)
                                                               for (int i = 0; i < BITS; ++i) if ((x >> i) & 1) {
 void insert( Line ln ) { insert( 0, n, 0, ln ); }
                                                                if (basis[i] == 0) {
  int query( int x ) { return query( 0, n, 0, x ); }
                                                                 basis[i] = x;
} lichao;
                                                                 return;
2.4 Treap
                                                                x ^= basis[i];
namespace Treap{
                                                               }
#define sz( x ) ( ( x ) ? ( ( x )->size ) : 0 )
                                                              bool ok(uint64_t x) {
struct node{
                                                               for (int i = 0; i < BITS; ++i)</pre>
 int size;
  uint32_t pri;
                                                                if ((x >> i) & 1) x ^= basis[i];
 node *lc, *rc;
node() : size(0), pri(rand()), lc(0), rc(0) {}
                                                               return x == 0;
                                                            }:
  void pull() {
  size = 1;
                                                                   Binary Search On Segment Tree
  if ( lc ) size += lc->size;
   if ( rc ) size += rc->size;
                                                            // find_first = x -> minimal x s.t. check( [a, x) )
                                                             // find_last = x \rightarrow \max x s.t. check([x, b))
  }
                                                             template <typename C>
node* merge( node* L, node* R ) {
  if ( not L or not R ) return L ? L : R;
                                                             int find_first(int 1, const C &check) {
                                                              if (1 >= n)
 if ( L->pri > R->pri ) {
                                                               return n;
  L->rc = merge( L->rc, R ); L->pull();
                                                              1 += sz;
   return L;
                                                              for (int i = height; i > 0; i--)
 } else {
                                                               propagate(1 >> i);
  R->lc = merge( L, R->lc ); R->pull();
                                                              Monoid sum = identity;
                                                              do {
   return R;
                                                               while ((1 \& 1) == 0)
}
                                                                1 >>= 1
void split_by_size( node*rt,int k,node*&L,node*&R ) {
                                                               if (check(f(sum, data[1]))) {
 if ( not rt ) L = R = nullptr;
                                                                while (1 < sz) {</pre>
  else if( sz( rt->lc ) + 1 <= k ) {
                                                                 propagate(1);
  split_by_size( rt->rc,k-sz(rt->lc)-1,L->rc,R );
                                                                 auto nxt = f(sum, data[1]);
  L->pull();
                                                                 if (not check(nxt)) {
 } else {
                                                                  sum = nxt;
  R = rt:
                                                                  1++;
   split_by_size( rt->lc, k, L, R->lc );
   R->pull();
 }
                                                                return 1 + 1 - sz;
#undef sz
                                                               sum = f(sum, data[1++]);
                                                              } while ((1 & -1) != 1);
                                                              return n;
2.5 Sparse Table
template < typename T, typename Cmp_ = less< T > >
class SparseTable {
                                                            template <typename C>
```

if (not ins[t]) {

st.push_back(t);

```
int find_last(int r, const C &check) {
                                                                  ins[t] = true;
if (r <= 0)
                                                                 if (dfn[v]) {
 return -1;
                                                                  low[u] = min(low[u], dfn[v]);
 r += sz;
for (int i = height; i > 0; i--)
                                                                  continue
 propagate((r - 1) >> i);
                                                                 } ++ch; dfs(v, u)
Monoid sum = identity;
                                                                 low[u] = min(low[u], low[v]);
                                                                 if (low[v] >= dfn[u]) {
do {
                                                                  ap[u] = true;
 while (r > 1 \text{ and } (r \& 1))
                                                                  while (true) {
                                                                   int eid = st.back(); st.pop_back();
  r >>= 1
  if (check(f(data[r], sum))) {
                                                                   bcc[eid] = ecnt;
                                                                   if (eid == t) break;
  while (r < sz) {</pre>
   propagate(r);
    r = (r << 1) + 1;
                                                                  ecnt++;
   auto nxt = f(data[r], sum);
    if (not check(nxt)) {
    sum = nxt;
                                                                if (ch == 1 and u == f) ap[u] = false;
                                                               }
     r--;
   }
                                                              public:
                                                               void init(int n_) {
   return r - sz;
                                                                G.clear(); G.resize(n = n_);
                                                                ecnt = 0; ap.assign(n, false);
 sum = f(data[r], sum);
                                                                low.assign(n, 0); dfn.assign(n, 0);
} while ((r & -r) != r);
return -1;
                                                               void add_edge(int u, int v) {
                                                               G[u].emplace_back(v, ecnt);
                                                                G[v].emplace_back(u, ecnt++);
3
    Graph
                                                               void solve() {
                                                                ins.assign(ecnt, false);
   BCC Edge
                                                                bcc.resize(ecnt); ecnt = 0;
class BCC_Bridge {
                                                                for (int i = 0; i < n; ++i)</pre>
private:
                                                                 if (not dfn[i]) dfs(i, i);
 int n. ecnt:
 vector<vector<pair<int,int>>> G;
                                                               int get_id(int x) { return bcc[x]; }
  vector<int> dfn, low;
                                                               int count() { return ecnt; }
 vector<bool> bridge;
                                                               bool is_ap(int x) { return ap[x]; }
  void dfs(int u, int f)
                                                            } bcc_ap;
  dfn[u] = low[u] = dfn[f] + 1;
  for (auto [v, t]: G[u]) {
                                                             3.3 2-SAT (SCC)
    if (v == f) continue;
                                                            class TwoSat{
    if (dfn[v]) {
                                                              private:
    low[u] = min(low[u], dfn[v]);
                                                               int n:
     continue;
                                                               vector<vector<int>> rG,G,sccs;
                                                               vector<int> ord,idx;
   dfs(v, u);
                                                               vector<bool> vis,result;
   low[u] = min(low[u], low[v]);
                                                               void dfs(int u){
    if (low[v] > dfn[u]) bridge[t] = true;
                                                                vis[u]=true
                                                                for(int v:G[u])
                                                                 if(!vis[v]) dfs(v);
public:
                                                                ord.push_back(u);
  void init(int n_) {
  G.clear(); G.resize(n = n_);
                                                               void rdfs(int u){
  low.assign(n, ecnt = 0);
                                                                vis[u]=false;idx[u]=sccs.size()-1;
  dfn.assign(n, 0);
                                                                sccs.back().push_back(u);
                                                                for(int v:rG[u])
  void add_edge(int u, int v) {
                                                                 if(vis[v])rdfs(v);
  G[u].emplace_back(v, ecnt);
G[v].emplace_back(u, ecnt++);
                                                              public:
                                                               void init(int n_){
 void solve() {
                                                                n=n_;G.clear();G.resize(n);
  bridge.assign(ecnt, false);
                                                                rG.clear();rG.resize(n);
  for (int i = 0; i < n; ++i)</pre>
                                                                sccs.clear();ord.clear();
   if (not dfn[i]) dfs(i, i);
                                                                idx.resize(n);result.resize(n);
 bool is_bridge(int x) { return bridge[x]; }
                                                               void add_edge(int u,int v){
} bcc_bridge;
                                                                G[u].push_back(v);rG[v].push_back(u);
3.2 BCC Vertex
                                                               void orr(int x,int y){
class BCC_AP {
                                                                if ((x^y)==1) return
                                                                add_edge(x^1,y); add_edge(y^1,x);
private:
 int n, ecnt;
                                                               bool solve(){
 vector<vector<pair<int,int>>> G;
 vector<int> bcc, dfn, low, st;
                                                                vis.clear();vis.resize(n);
 vector<bool> ap, ins;
                                                                for(int i=0;i<n;++i)</pre>
 void dfs(int u, int f) {
  dfn[u] = low[u] = dfn[f] + 1;
                                                                 if(not vis[i])dfs(i);
                                                                reverse(ord.begin(),ord.end());
  int ch = 0;
                                                                for (int u:ord){
   for (auto [v, t]: G[u]) if (v != f) {
                                                                 if(!vis[u])continue;
```

sccs.push_back(vector<int>());

rdfs(u);

time_ = 0; dfschain(1, 1);

```
for(int i=0;i<n;i+=2)</pre>
                                                                PII get_subtree(int u) { return {tl[ u ],tr[ u ] }; }
    if(idx[i]==idx[i+1])
                                                                vector< PII > get_path( int u , int v ){
                                                                 vector< PII > res;
     return false
                                                                 int g = lca( u, v );
   vector<bool> c(sccs.size());
   for(size_t i=0;i<sccs.size();++i){</pre>
                                                                 while ( chain[ u ] != chain[ g ] ) {
                                                                  int s = chain_st[ chain[ u ] ];
res.emplace_back( tl[ s ], tl[ u ] + 1 );
    for(size_t j=0;j<sccs[i].size();++j){</pre>
     result[sccs[i][j]]=c[i];
     c[idx[sccs[i][j]^1]]=!c[i];
                                                                  u = fa[ s ][ 0 ];
                                                                 res.emplace\_back( tl[ g ], tl[ u ] + 1 );
                                                                 while ( chain[ v ] != chain[ g ] ) {
   return true;
                                                                  int s = chain_st[ chain[ v ] ]
 bool get(int x){return result[x];}
                                                                  res.emplace_back( tl[ s ], tl[ v ] + 1 );
  inline int get_id(int x){return idx[x];}
                                                                  v = fa[ s ][ 0 ];
  inline int count(){return sccs.size();}
                                                                 res.emplace_back( tl[ g ] + 1, tl[ v ] + 1 );
                                                                 return res:
3.4 Lowbit Decomposition
                                                                 /* res : list of intervals from u to v
class LowbitDecomp{
                                                                  * ( note only nodes work, not edge )
                                                                  * usage :
private:
                                                                  * vector< PII >& path = tree.get_path( u , v )
int time_, chain_, LOG_N;
                                                                  * for( auto [ 1, r ] : path ) {
vector< vector< int > > G, fa;
vector< int > tl, tr, chain, chain_st;
                                                                  * 0-base [ 1, r )
                                                                  * }
// chain_ : number of chain
                                                                  */
// tl, tr[ u ] : subtree interval in the seq. of u
                                                                }
 // chain_st[ u ] : head of the chain contains u
// chian[ u ] : chain id of the chain u is on
                                                              } tree;
void predfs( int u, int f ) {
                                                               3.5
                                                                     MaxClique
  chain[u] = 0;
  for ( int v : G[ u ] ) {
                                                               // contain a self loop u to u, than u won't in clique
  if ( v == f ) continue;
                                                               template < size_t MAXN >
   predfs( v, u );
                                                               class MaxClique{
   if( lowbit( chain[ u ] ) < lowbit( chain[ v ] ) )</pre>
                                                               private:
    chain[ u ] = chain[ v ];
                                                                using bits = bitset< MAXN >;
                                                                bits popped, G[ MAXN ], ans;
size_t deg[ MAXN ], deo[ MAXN ], n;
 if ( not chain[ u ] )
   chain[ u ] = chain_ ++;
                                                                void sort_by_degree() {
                                                                 popped.reset();
 void dfschain( int u, int f ) {
                                                                 for ( size_t i = 0 ; i < n ; ++ i )</pre>
 fa[ u ][ 0 ] = f;
for ( int i = 1 ; i < LOG_N ; ++ i )
                                                                   deg[ i ] = G[ i ].count();
                                                                 for ( size_t i = 0 ; i < n ; ++ i ) {
  fa[u][i] = fa[fa[u][i-1]][i-1];
                                                                   size_t mi = MAXN, id = 0;
                                                                   for ( size_t j = 0 ; j < n ; ++ j )
  if ( not popped[ j ] and deg[ j ] < mi )
    mi = deg[ id = j ];</pre>
  tl[ u ] = time_++;
  if ( not chain_st[ chain[ u ] ] )
   chain_st[ chain[ u ] ] = u;
  for ( int v : G[ u ] )
                                                                   popped[ deo[ i ] = id ] = 1;
  if ( v != f and chain[ v ] == chain[ u ] )
                                                                   for( size_t u = G[ i ]._Find_first() ;
                                                                    u < n ; u = G[ i ]._Find_next( u ) )</pre>
    dfschain( v, u );
  for ( int v : G[ u ] )
                                                                     -- deg[ u ];
   if ( v != f and chain[ v ] != chain[ u ] )
    dfschain( v, u );
                                                                void BK( bits R, bits P, bits X ) {
  tr[ u ] = time_;
                                                                 if (R.count()+P.count() <= ans.count()) return;</pre>
bool anc( int u, int v ) {
  return tl[ u ] <= tl[ v ] and tr[ v ] <= tr[ u ];</pre>
                                                                 if ( not P.count() and not X.count() ) {
                                                                  if ( R.count() > ans.count() ) ans = R;
                                                                  return;
public:
                                                                 }
int lca( int u, int v ) {
                                                                 /* greedily chosse max degree as pivot
  if ( anc( u, v ) ) return u;
                                                                 bits cur = P | X; size_t pivot = 0, sz = 0;
 for ( int i = LOG_N - 1 ; i >= 0 ; -- i )
if ( not anc( fa[ u ][ i ], v ) )
                                                                 for ( size_t u = cur._Find_first() ;
                                                                  u < n ; u = cur._Find_next( u )</pre>
   u = fa[ u ][ i ];
                                                                   if ( deg[ u ] > sz ) sz = deg[ pivot = u ];
                                                                 cur = P & ( ~G[ pivot ] );
  return fa[ u ][ 0 ];
                                                                 */ // or simply choose first
void init( int n ) {
                                                                 bits cur = P & (~G[ ( P | X )._Find_first() ]);
 fa.assign( ++n, vector< int >( LOG_N ) );
                                                                 for ( size_t u = cur._Find_first()
                                                                  u < n ; u = cur._Find_next( u ) ) {
if ( R[ u ] ) continue;</pre>
  for ( LOG_N = 0 ; ( 1 << LOG_N ) < n ; ++ LOG_N );
 G.clear(); G.resize( n );
 tl.assign( n, 0 ); tr.assign( n, 0 );
                                                                  R[u] = 1;
 chain.assig( n, 0 ); chain_st.assign( n, 0 );
                                                                  BK( R, P & G[ u ], X & G[ u ] );
                                                                  R[u] = P[u] = 0, X[u] = 1;
 void add_edge( int u , int v ) {
  // 1-base
 G[ u ].push_back( v );
                                                               public:
 G[ v ].push_back( u );
                                                                void init( size_t n_ ) {
                                                                 n = n_{-};
void decompose(){
                                                                 for ( size_t i = 0 ; i < n ; ++ i )
 chain_ = 1;
                                                                  G[ i ].reset();
 predfs( 1, 1 );
                                                                 ans.reset();
```

void add_edges(int u, bits S) { G[u] = S; }

```
void add_edge( int u, int v ) {
                                                                sort(r.begin(), r.end(),
                                                                 [&](int i, int j) { return d[i] > d[j]; });
  G[u][v] = G[v][u] = 1;
                                                                csort(r, c);
                                                                dfs(r, c, 1, mask);
return ans; // sol[0 ~ ans-1]
 int solve() {
  sort_by_degree(); // or simply iota( deo... )
  for ( size_t i = 0 ; i < n ; ++ i )</pre>
                                                               }
   deg[ i ] = G[ i ].count();
                                                              } graph;
  bits pob, nob = 0; pob.set();
                                                              3.7 Virtural Tree
  for (size_t i=n; i<MAXN; ++i) pob[i] = 0;</pre>
  for ( size_t i = 0 ; i < n ; ++ i ) {
    size_t v = deo[ i ];</pre>
                                                              inline bool cmp(const int &i, const int &j) {
                                                               return dfn[i] < dfn[j];</pre>
   bits tmp; tmp[ v ] = 1;
   BK( tmp, pob & G[ v ], nob & G[ v ] );
pob[ v ] = 0, nob[ v ] = 1;
                                                              void build(int vectrices[], int k) {
                                                               static int stk[MAX_N];
                                                               sort(vectrices, vectrices + k, cmp);
  return static_cast< int >( ans.count() );
                                                               stk[sz++] = 0;
                                                               for (int i = 0; i < k; ++i) {
  int u = vectrices[i], lca = LCA(u, stk[sz - 1]);</pre>
};
                                                                if (lca == stk[sz - 1]) stk[sz++] = u;
3.6 MaxCliqueDyn
                                                                else {
constexpr int kN = 150;
                                                                 while (sz \ge 2 \&\& dep[stk[sz - 2]] \ge dep[lca]) {
struct MaxClique { // Maximum Clique
                                                                  addEdge(stk[sz - 2], stk[sz - 1]);
sz--:
                                                                 if (stk[sz - 1] != lca) {
 void init(int _n) {
 n = n, ans q = 0;
                                                                  addEdge(lca, stk[--sz]);
  for (int i = 0; i < n; i++) a[i].reset();</pre>
                                                                  stk[sz++] = lca, vectrices[cnt++] = lca;
 void addEdge(int u, int v) { a[u][v] = a[v][u] = 1; }
void csort(vector<int> &r, vector<int> &c) {
                                                                 stk[sz++] = u;
 int mx = 1, km = max(ans - q + 1, 1), t = 0,
                                                               for (int i = 0; i < sz - 1; ++i)
    m = int(r.size())
  cs[1].reset(); cs[2].reset()
                                                                addEdge(stk[i], stk[i + 1]);
  for (int i = 0; i < m; i++) {
   int p = r[i], k = 1
                                                              3.8 Centroid Decomposition
   while ((cs[k] & a[p]).count()) k++;
   if (k > mx) cs[++mx + 1].reset();
                                                              struct Centroid {
   cs[k][p] = 1;
                                                               vector<vector<int64_t>> Dist;
                                                               vector<int> Parent, Depth;
   if (k < km) r[t++] = p;
                                                               vector<int64_t> Sub, Sub2;
  c.resize(m);
                                                               vector<int> Sz, Sz2;
  if(t) c[t-1] = 0;
                                                               Centroid(vector<vector<pair<int, int>>> g) {
  for (int k = km; k <= mx; k++) {</pre>
                                                                int N = g.size()
  for (int p = int(cs[k]._Find_first());
                                                                vector<bool> Vis(N);
      p < kN; p = int(cs[k]._Find_next(p))) {
                                                                vector<int> sz(N), mx(N);
    r[t] = p; c[t++] = k;
                                                                vector<int> Path;
                                                                Dist.resize(N)
  }
                                                                Parent.resize(N);
                                                                Depth.resize(N)
 void dfs(vector<int> &r, vector<int> &c, int 1,
                                                                auto DfsSz = [\&](auto dfs, int x) -> void {
  bitset<kN> mask) {
                                                                 Vis[x] = true; sz[x] = 1; mx[x] = 0;
                                                                 for (auto [u, w] : g[x]) {
  while (!r.empty()) {
                                                                  if (Vis[u]) continue;
   int p = r.back(); r.pop_back();
                                                                  dfs(dfs, u)
   mask[p] = 0;
   if (q + c.back() <= ans) return;</pre>
                                                                  sz[x] += sz[u];
                                                                  mx[x] = max(mx[x], sz[u]);
   cur[q++] = p;
   vector<int> nr, nc;
   bitset<kN> nmask = mask & a[p];
                                                                 Path.push_back(x);
   for (int i : r)
                                                                };
    if (a[p][i]) nr.push_back(i);
                                                                auto DfsDist = [&](auto dfs, int x, int64_t D = 0)
                                                                 -> void {
   if (!nr.empty()) {
    if (1 < 4) {
                                                                 Dist[x].push_back(D); Vis[x] = true;
     for (int i : nr)
                                                                 for (auto [u, w] : g[x]) {
      d[i] = int((a[i] & nmask).count());
                                                                  if (Vis[u]) continue;
     sort(nr.begin(), nr.end(),
                                                                  dfs(dfs, u, D + w);
      [&](int x, int y)
                                                                 }
       return d[x] > d[y];
                                                                };
                                                                auto Dfs = [&]
      });
                                                                 (auto dfs, int x, int D = 0, int p = -1)->void {
   csort(nr, nc); dfs(nr, nc, 1 + 1, nmask);
} else if (q > ans) {
                                                                 Path.clear(); DfsSz(DfsSz, x);
                                                                 int M = Path.size();
                                                                 int C = -1;
    ans = q; copy(cur, cur + q, sol);
                                                                 for (int u : Path) {
   c.pop_back(); q--;
                                                                  if (max(M - sz[u], mx[u]) * 2 <= M) C = u;
  }
                                                                  Vis[u] = false;
 int solve(bitset<kN> mask) { // vertex mask
                                                                 DfsDist(DfsDist, C);
                                                                 for (int u : Path) Vis[u] = false;
  vector<int> r, c;
  for (int i = 0; i < n; i++)
                                                                 Parent[C] = p; Vis[C] = true;
  if (mask[i]) r.push_back(i);
for (int i = 0; i < n; i++)</pre>
                                                                 Depth[C] = D;
                                                                 for (auto [u, w] : g[C]) {
                                                                  if (Vis[u]) continue;
   d[i] = int((a[i] & mask).count());
```

```
dfs(dfs, u, D + 1, C);
                                                                  FZ(vst);edgeID.clear();cycle.clear();rho.clear();
   }
                                                                  for (int i=n; !vst[st]; st=prv[i--][st]) {
  Dfs(Dfs, 0); Sub.resize(N); Sub2.resize(N);
                                                                   vst[st]++
                                                                   edgeID.PB(prve[i][st]);
  Sz.resize(N); Sz2.resize(N);
                                                                   rho.PB(st);
 void Mark(int v) {
  int x = v, z = -1;
                                                                  while (vst[st] != 2) {
  for (int i = Depth[v]; i >= 0; --i) {
                                                                   int v = rho.back(); rho.pop_back();
                                                                   cycle.PB(v);
   Sub[x] += Dist[v][i]; Sz[x]++;
   if (z != -1) {
                                                                   vst[v]++;
    Sub2[z] += Dist[v][i];
    Sz2[z]++;
                                                                  reverse(ALL(edgeID));
                                                                  edgeID.resize(SZ(cycle));
   z = x; x = Parent[x];
                                                                  return mmc;
  }
                                                               } mmc;
 int64_t Query(int v) {
                                                                3.11 Mo's Algorithm on Tree
 int64_t res = 0;
  int x = v, z = -1
                                                                int q; vector< int > G[N];
 for (int i = Depth[v]; i >= 0; --i) {
  res += Sub[x] + 1LL * Sz[x] * Dist[v][i];
                                                                struct Que{
                                                                int u, v, id;
} que[ N ];
   if (z != -1) res-=Sub2[z]+1LL*Sz2[z]*Dist[v][i];
                                                                int dfn[N], dfn_, block_id[N], block_, stk[N], stk_;
   z = x; x = Parent[x];
                                                                void_dfs( int u, int f ) {
                                                                 dfn[ u ] = dfn_++; int saved_rbp = stk_;
for ( int v : G[ u ] ) {
  return res;
                                                                  if ( v == f ) continue;
};
                                                                  dfs( v, u );
3.9
     Tree Hashing
                                                                  if ( stk_ - saved_rbp < SQRT_N ) continue;</pre>
                                                                  for ( ++ block_ ; stk_ != saved_rbp ; )
  block_id[ stk[ -- stk_ ] ] = block_;
uint64_t hsah(int u, int f) {
 uint64_t r = 127;
 for (int v : G[ u ]) if (v != f) {
 uint64_t hh = hsah(v, u);
                                                                stk[ stk_ ++ ] = u;
  r=(r+(hh*hh)%1010101333)%1011820613;
                                                                bool inPath[ N ];
                                                                void Diff( int u ) {
return r;
                                                                if ( inPath[ u ] ^= 1 ) { /*remove this edge*/ }
                                                                 else { /*add this edge*/ }
3.10 Minimum Mean Cycle
/* minimum mean cycle O(VE) */
                                                                void traverse( int& origin_u, int u ) {
                                                                for ( int g = lca( origin_u, u )
struct MMC{
                                                                  origin_u != g ; origin_u = parent_of[ origin_u ] )
#define FZ(n) memset((n),0,sizeof(n))
#define E 101010
                                                                   Diff( origin_u );
#define V 1021
                                                                 for (int v = u; v != origin_u; v = parent_of[v])
#define inf 1e9
                                                                  Diff( v );
 struct Edge { int v,u; double c; };
                                                                 origin_u = u;
 int n, m, prv[V][V], prve[V][V], vst[V];
                                                                }
 Edge e[E];
                                                                void solve() {
 vector<int> edgeID, cycle, rho;
                                                                 dfs( 1, 1 );
 double d[V][V];
                                                                 while ( stk_ ) block_id[ stk[ -- stk_ ] ] = block_;
 void init( int _n ) { n = _n; m = 0; }
// WARNING: TYPE matters
                                                                 sort( que, que + q, [](const Que& x, const Que& y) {
                                                                  return tie( block_id[ x.u ], dfn[ x.v ] )
 void add_edge( int vi , int ui , double ci )
                                                                      < tie( block_id[ y.u ], dfn[ y.v ] );
 { e[ m ++ ] = { vi , ui , ci }; }
void bellman_ford() {
                                                                 } );
                                                                 int U = 1, V = 1;
                                                                 for ( int i = 0 ; i < q ; ++ i ) {
  for(int i=0; i<n; i++) d[0][i]=0;
  for(int i=0; i<n; i++) {
  fill(d[i+1], d[i+1]+n, inf);</pre>
                                                                  pass( U, que[ i ].u );
pass( V, que[ i ].v );
   for(int j=0; j<m; j++) {</pre>
                                                                  // we could get our answer of que[ i ].id
    int v = e[j].v, u = e[j].u;
if(d[i][v]<inf && d[i+1][u]>d[i][v]+e[j].c) {
                                                               }
                                                                /*
     d[i+1][u] = d[i][v]+e[j].c;
     prv[i+1][u] = v;
                                                                Method 2:
     prve[i+1][u] = j;
                                                               dfs u:
                                                                push u
                                                                 iterate subtree
                                                                Let P = LCA(u, v), and St(u) \le St(v)
                                                               if (P == u) query[St(u), St(v)]
 double solve(){
  // returns inf if no cycle, mmc otherwise
                                                                else query[Ed(u), St(v)], query[St(P), St(P)]
  double mmc=inf;
  int st = -1
                                                                3.12 Minimum Steiner Tree
  bellman_ford();
  for(int i=0; i<n; i++) {</pre>
                                                               // Minimum Steiner Tree
   double avg=-inf;
                                                               // 0(V 3^T + V^2 2^T)
                                                               struct SteinerTree{
   for(int k=0; k<n; k++) {</pre>
    if(d[n][i]<inf-eps)</pre>
                                                               #define V 33
     avg=max(avg,(d[n][i]-d[k][i])/(n-k));
                                                                #define T 8
                                                               #define INF 1023456789
    else avg=max(avg,inf);
                                                                 int n , dst[V][V] , dp[1 << T][V] , tdst[V];</pre>
                                                                void init( int _n ){
   if (avg < mmc) tie(mmc, st) = tie(avg, i);</pre>
```

return -inf;

// find cycle

```
int tot = 0;
  for( int i = 0 ; i < n ; i ++ ){</pre>
                                                                   vector<int> id(n, -1), vis(n, -1);
   for( int j = 0 ; j < n ; j ++ )</pre>
                                                                    for (int i = 0; i < n; i++) {
   dst[ i ][ j ] = INF;
dst[ i ][ i ] = 0;
                                                                     ans += in[i];
                                                                     for (int x = i; x != -1 && id[x] == -1; x = prv[x])
  }
                                                                      if (vis[x] == i) {
                                                                      for (int y = prv[x]; y != x; y = prv[y])
 void add_edge( int ui , int vi , int wi ){
  dst[ ui ][ vi ] = min( dst[ ui ][ vi ] , wi );
                                                                        id[y] = tot;
  dst[ vi ][ ui ] = min( dst[ vi ][ ui ] , wi );
                                                                       id[x] = tot++;
                                                                       break:
 void shortest_path(){
  for( int k = 0 ; k < n ; k ++ )</pre>
                                                                      vis[x] = i;
   for( int i = 0 ; i < n ; i ++ )</pre>
                                                                    }
    for( int j = 0 ; j < n ; j ++ )
dst[ i ][ j ] = min( dst[ i ][ j ],
    dst[ i ][ k ] + dst[ k ][ j ] );</pre>
                                                                   if (!tot)
                                                                     return ans;
                                                                    for (int i = 0; i < n; i++)
                                                                    if (id[i] == -1)
 int solve( const vector<int>& ter ){
  int t = (int)ter.size();
                                                                      id[i] = tot++;
  for( int i = 0 ; i < ( 1 << t ) ; i ++ )</pre>
                                                                    // shrink
   for( int j = 0; j < n; j ++ )
dp[ i ][ j ] = INF;
                                                                   for (auto &e : E) {
  if (id[e.u] != id[e.v])
  for( int i = 0 ; i < n ; i ++ )
                                                                     e.w -= in[e.v];
   dp[0][i] = 0;
                                                                    e.u = id[e.u], e.v = id[e.v];
  for( int msk = 1 ; msk < ( 1 << t ) ; msk ++ ){
  if( msk == ( msk & (-msk) ) ){</pre>
                                                                   n = tot:
    int who = __lg( msk );
                                                                   root = id[root];
    for( int i = 0 ; i < n ; i ++ )
dp[ msk ][ i ] = dst[ ter[ who ] ][ i ];
                                                                  assert(false);
    continue:
                                                                } DMST:
   for( int i = 0 ; i < n ; i ++ )</pre>
                                                                3.14
                                                                      Manhattan Minimum Spanning Tree
    for( int submsk = ( msk - 1 ) & msk ; submsk ;
          submsk = ( submsk - 1 ) & msk )
                                                                typedef Point<int> P;
      dp[ msk ][ i ] = min( dp[ msk ][ i ],
                                                                vector<array<int, 3>> manhattanMST(vector<P> ps) {
               dp[ submsk ][ i ] +
                                                                 vi id(sz(ps));
               dp[ msk ^ submsk ][ i ] );
                                                                 iota(all(id), 0);
   for( int i = 0 ; i < n ; i ++ ){</pre>
                                                                 vector<array<int, 3>> edges;
    tdst[ i ] = INF;
                                                                 rep(k, 0, 4) {
    sort(all(id), [&](int i, int j) {
                                                                   return (ps[i] - ps[j]).x < (ps[j] - ps[i]).y;</pre>
                                                                  });
                                                                  map<int, int> sweep;
   for( int i = 0 ; i < n ; i ++ )</pre>
                                                                  for (int i : id) {
    dp[ msk ][ i ] = tdst[ i ];
                                                                   for (auto it = sweep.lower_bound(-ps[i].y);
                                                                       it != sweep.end(); sweep.erase(it++)) {
                                                                     int j = it->second;
  int ans = INF:
  for( int i = 0 ; i < n ; i ++ )</pre>
                                                                     Pd = ps[i] - ps[j];
   ans = min( ans , dp[ (1 << t) - 1 ][ i ] );
                                                                    if (d.y > d.x) break;
                                                                    edges.push_back({d.y + d.x, i, j});
  return ans;
} solver;
                                                                   sweep[-ps[i].y] = i;
      Directed Minimum Spanning Tree
                                                                  for (P &p : ps)
if (k & 1) p.x = -p.x;
struct DirectedMST { // find maximum
 struct Edge {
                                                                    else swap(p.x, p.y);
  int u, v;
  int w:
                                                                 return edges; // [{w, i, j}, ...]
  Edge(int u, int v, int w) : u(u), v(v), w(w) {}
                                                                3.15
                                                                      Dominator Tree
 vector<Edge> Edges;
 void clear() { Edges.clear(); }
                                                                namespace dominator {
 void addEdge(int a, int b, int w) { Edges.emplace_back
                                                                vector<int> g[maxn], r[maxn], rdom[maxn];
                                                                int dfn[maxn], rev[maxn], fa[maxn], sdom[maxn];
int dom[maxn], val[maxn], rp[maxn], tk;
    (a, b, w); }
 int solve(int root, int n) {
  vector<Edge> E = Edges;
                                                                void init(int n) {
                                                                 // vertices are numbered from 0 to n - 1
  int ans = 0;
                                                                 fill(dfn, dfn + n, -1); fill(rev, rev + n, -1); fill(fa, fa + n, -1); fill(val, val + n, -1);
  while (true) {
   // find best in edge
   vector<int> in(n, -inf), prv(n, -1);
                                                                 fill(sdom, sdom + n, -1); fill(rp, rp + n, -1);
                                                                 fill(dom, dom + n, -1); tk = 0;
   for (auto e : E)
    if (e.u != e.v && e.w > in[e.v]) {
                                                                 for (int i = 0; i < n; ++i) {
     in[e.v] = e.w;
                                                                  g[i].clear(); r[i].clear(); rdom[i].clear();
     prv[e.v] = e.u;
   in[root] = 0;
                                                                void add_edge(int x, int y) { g[x].push_back(y); }
   prv[root] = -1;
                                                                void dfs(int x) {
   for (int i = 0; i < n; i++)
                                                                 rev[dfn[x] = tk] = x;
    if (in[i] == -inf)
                                                                 fa[tk] = sdom[tk] = val[tk] = tk; tk ++;
```

for (int u : g[x]) {

if (dfn[u] == -1) dfs(u), rp[dfn[u]] = dfn[x];

```
r[dfn[u]].push_back(dfn[x]);
                                                                      } else t--;
void merge(int x, int y) { fa[x] = y; }
int find(int x, int c = 0) {
                                                                  }
 if (fa[x] == x) return c ? -1 : x;
                                                                        Matching & Flow
 int p = find(fa[x], 1);
 if (p == -1) return c ? fa[x] : val[x];
                                                                        Kuhn Munkres
 if (sdom[val[x]]>sdom[val[fa[x]]]) val[x]=val[fa[x]];
                                                                  class KM {
 fa[x] = p;
                                                                  private:
 return c ? p : val[x];
                                                                    static constexpr lld INF = 1LL << 60;</pre>
                                                                    vector<lld> hl,hr,slk;
vector<int> build(int s, int n) {
// return the father of each node in the dominator tree
                                                                    vector<int> fl,fr,pre,qu;
                                                                    vector<vector<lld>> w;
// p[i] = -2 if i is unreachable from s
                                                                    vector<bool> v1, vr;
 dfs(s);
                                                                    int n, ql, qr;
 for (int i = tk - 1; i >= 0; --i) {
  for (int u:r[i]) sdom[i]=min(sdom[i],sdom[find(u)]);
                                                                    bool check(int x) {
                                                                     if (v1[x] = true, f1[x] != -1)
  if (i) rdom[sdom[i]].push_back(i);
                                                                      return vr[qu[qr++] = f1[x]] = true;
  for (int &u : rdom[i]) {
                                                                     while (x != -1) swap(x, fr[fl[x] = pre[x]]);
   int p = find(u);
                                                                     return false:
   if (sdom[p] == i) dom[u] = i;
   else dom[u] = p;
                                                                    void bfs(int s) {
                                                                     fill(slk.begin(), slk.end(), INF);
  if (i) merge(i, rp[i]);
                                                                     fill(vl.begin(), vl.end(), false);
                                                                     fill(vr.begin(), vr.end(), false);
 vector<int> p(n, -2); p[s] = -1;
                                                                     ql = qr = 0;
 for (int i = 1; i < tk; ++i)
                                                                     qu[qr++] = s;
  if (sdom[i] != dom[i]) dom[i] = dom[dom[i]];
                                                                     vr[s] = true;
 for (int i = 1; i < tk; ++i) p[rev[i]] = rev[dom[i]];</pre>
                                                                     while (true) {
 return p;
                                                                      11d d;
                                                                      while (ql < qr) {</pre>
                                                                       for (int x = 0, y = qu[ql++]; x < n; ++x) {
  if(!vl[x]&&slk[x]>=(d=hl[x]+hr[y]-w[x][y])){
3.16 Edge Coloring
// max(d_u) + 1 edge coloring, time: O(NM)
                                                                         if (pre[x] = y, d) slk[x] = d;
int C[kN][kN], G[kN][kN]; // 1-based, G: ans
                                                                         else if (!check(x)) return;
void clear(int N) {
 for (int i = 0; i <= N; i++)
                                                                       }
 for (int j = 0; j <= N; j++)
C[i][j] = G[i][j] = 0;</pre>
                                                                      d = INF;
                                                                      for (int x = 0; x < n; ++x)
if (!v1[x] && d > s1k[x]) d = s1k[x];
for (int x = 0; x < n; ++x) {
void solve(vector<pair<int, int>> &E, int N) {
int X[kN] = {}, a;
auto update = [&](int u)
                                                                       if (v1[x]) h1[x] += d;
  for (X[u] = 1; C[u][X[u]]; X[u]++);
                                                                       else slk[x] -= d;
                                                                       if (vr[x]) hr[x] -= d;
 auto color = [&](int u, int v, int c) {
  int p = G[u][v];
G[u][v] = G[v][u] = c;
                                                                      for (int x = 0; x < n; ++x)
                                                                       if (!v1[x] && !slk[x] && !check(x)) return;
  C[u][c] = v, C[v][c] = u;
  C[u][p] = C[v][p] = 0;
  if(p) X[u] = X[v] = p
                                                                  public:
  else update(u), update(v);
                                                                    void init( int n_ ) {
  return p;
                                                                     n = n_; qu.resize(n);
 }:
                                                                    fl.clear(); fl.resize(n, -1);
fr.clear(); fr.resize(n, -1);
 auto flip = [&](int u, int c1, int c2) {
 int p = C[u][c1];
                                                                    hr.clear(); hr.resize(n); hl.resize(n);
  swap(C[u][c1], C[u][c2]);
                                                                    w.clear(); w.resize(n, vector<lld>(n));
slk.resize(n); pre.resize(n);
  if (p) G[u][p] = G[p][u] = c2;
  if (!C[u][c1]) X[u] = c1;
                                                                     vl.resize(n); vr.resize(n);
  if (!C[u][c2]) X[u] = c2;
  return p;
                                                                    void set_edge( int u, int v, lld x ) {w[u][v] = x;}
                                                                    1ld solve() {
 for (int i = 1; i <= N; i++) X[i] = 1;
for (int t = 0; t < E.size(); t++) {
                                                                    for (int i = 0; i < n; ++i)</pre>
                                                                     hl[i] = *max_element(w[i].begin(), w[i].end());
 auto [u, v] = E[t];
                                                                     for (int i = 0; i < n; ++i) bfs(i);
  int v0 = v, c = X[u], c0 = c, d;
                                                                     11d res = 0;
  vector<pair<int, int>> L; int vst[kN] = {};
                                                                     for (int i = 0; i < n; ++i) res += w[i][f1[i]];</pre>
  while (!G[u][v0]) {
                                                                     return res;
   L.emplace_back(v, d = X[v]);
                                                                    }
   if (!C[v][c]) for(a=L.size()-1;a>=0;a--)
  c = color(u, L[a].first, c);
                                                                  } km;
   else if(!C[u][d])for(a=L.size()-1;a>=0;a--)
                                                                  4.2 Bipartite Matching
     color(u, L[a].first, L[a].second);
   else if (vst[d]) break
                                                                  class BipartiteMatching{
   else vst[d] = 1, v = C[u][d];
                                                                  private:
                                                                   vector<int> X[N], Y[N];
int fX[N], fY[N], n;
  if (!G[u][v0]) {
   for (; v; v = flip(v, c, d), swap(c, d));
                                                                   bitset<N> walked;
   if (C[u][c0]) { a = int(L.size()) - 1;
                                                                   bool dfs(int x)
    while (--a >= 0 && L[a].second != c)
                                                                     for(auto i:X[x]){
    for(;a>=0;a--)color(u,L[a].first,L[a].second);
                                                                      if(walked[i])continue;
```

```
walked[i]=1;
                                                                   q.push(match[u]);
   if(fY[i]==-1||dfs(fY[i])){
                                                                   s[match[u]] = 0;
    fY[i]=x;fX[x]=i;
                                                                  } else if (!s[u] && Find(u) != Find(x)) {
                                                                   int 1 = LCA(u, x, n);
Blossom(x, u, 1);
    return 1;
                                                                   Blossom(u, x, 1);
  return 0;
public:
 void init(int _n){
                                                                return false;
  n=_n; walked.reset();
  for(int i=0;i<n;i++){</pre>
                                                               int Solve(int n) {
   X[i].clear();Y[i].clear();
                                                                int res = 0;
   fX[i]=fY[i]=-1;
                                                                for (int x = 0; x < n; ++x) {
                                                                 if (match[x] == n) res += Bfs(x, n);
 void add_edge(int x, int y){
                                                                return res;
 X[x].push_back(y); Y[y].push_back(y);
                                                              }}
                                                                     Minimum Weight Matching (Clique version)
 int solve(){
  int cnt = 0:
                                                              struct Graph {
                                                                // 0-base (Perfect Match)
  for(int i=0;i<n;i++){</pre>
                                                                int n, edge[MXN][MXN];
   walked.reset();
   if(dfs(i)) cnt++;
                                                                int match[MXN], dis[MXN], onstk[MXN];
                                                                vector<int> stk;
  // return how many pair matched
                                                                void init(int _n) {
  return cnt;
                                                                 n =
                                                                     _n;
                                                                 for (int i=0; i<n; i++)</pre>
}:
                                                                  for (int j=0; j<n; j++)</pre>
                                                                   edge[i][j] = 0;
4.3 General Graph Matching
namespace matching {
                                                                void set_edge(int u, int v, int w) {
int fa[kN], pre[kN], match[kN], s[kN], v[kN];
                                                                 edge[u][v] = edge[v][u] = w;
vector<int> g[kN];
queue<int> q;
                                                                bool SPFA(int u){
void Init(int n) {
                                                                 if (onstk[u]) return true;
for (int i = 0; i <= n; ++i) match[i] = pre[i] = n;</pre>
                                                                 stk.PB(u);
 for (int i = 0; i < n; ++i) g[i].clear();</pre>
                                                                 onstk[u] = 1;
                                                                 for (int v=0; v<n; v++){
                                                                  if (u != v && match[u] != v && !onstk[v]){
void AddEdge(int u, int v) {
g[u].push_back(v);
                                                                   int m = match[v]
 g[v].push_back(u);
                                                                   if (dis[m] > dis[u] - edge[v][m] + edge[u][v]){
                                                                    dis[m] = dis[u] - edge[v][m] + edge[u][v];
int Find(int u) {
                                                                    onstk[v] = 1;
return u == fa[u] ? u : fa[u] = Find(fa[u]);
                                                                    stk.PB(v)
                                                                    if (SPFA(m)) return true;
int LCA(int x, int y, int n) {
                                                                    stk.pop_back();
 static int tk = 0; tk++;
                                                                    onstk[v] = 0;
 x = Find(x), y = Find(y);
 for (; ; swap(x, y)) {
  if (x != n) {
                                                                 }
   if (v[x] == tk) return x;
                                                                 onstk[u] = 0;
   v[x] = tk;
                                                                 stk.pop_back();
   x = Find(pre[match[x]]);
                                                                 return false;
                                                                int solve() {
void Blossom(int x, int y, int 1) {
                                                                 // find a match
 while (Find(x) != 1) {
                                                                 for (int i=0; i<n; i+=2){</pre>
 pre[x] = y, y = match[x];
if (s[y] == 1) q.push(y), s[y] = 0;
if (fa[x] == x) fa[x] = 1;
                                                                  match[i] = i+1;
                                                                  match[i+1] = i;
  if (fa[y] == y) fa[y] = 1;
                                                                 while (true){
                                                                  int found = 0;
  x = pre[y];
                                                                  for (int i=0; i<n; i++)</pre>
                                                                   dis[i] = onstk[i] = 0;
bool Bfs(int r, int n) {
  for (int i = 0; i <= n; ++i) fa[i] = i, s[i] = -1;</pre>
                                                                  for (int i=0; i<n; i++){
                                                                   stk.clear()
                                                                   if (!onstk[i] && SPFA(i)){
 while (!q.empty()) q.pop();
 q.push(r);
                                                                    found = 1
 s[r] = 0;
                                                                    while (SZ(stk)>=2){
                                                                     int u = stk.back(); stk.pop_back();
 while (!q.empty()) {
  int x = q.front(); q.pop();
                                                                     int v = stk.back(); stk.pop_back();
  for (int u : g[x]) {
  if (s[u] == -1) {
                                                                     match[u] = v;
                                                                     match[v] = u;
    pre[u] = x, s[u] = 1;
    if (match[u] == n) {
                                                                   }
     for (int a = u, b = x, last; b != n; a = last, b =
     pre[a])
                                                                  if (!found) break;
      last = match[b], match[b] = a, match[a] = b;
     return true;
                                                                 int ret = 0;
                                                                 for (int i=0; i<n; i++)</pre>
```

ret += edge[i][match[i]];

return ret>>1;

```
} graph;
4.5 Minimum Cost Circulation
struct Edge { int to, cap, rev, cost; };
vector<Edge> g[kN];
int dist[kN], pv[kN], ed[kN];
bool mark[kN];
int NegativeCycle(int n) {
memset(mark, false, sizeof(mark));
memset(dist, 0, sizeof(dist));
int upd = -1;
for (int i = 0; i <= n; ++i) {
 for (int j = 0; j < n; ++j) {
   int idx = 0;
   for (auto &e : g[j]) {
    if(e.cap > 0 && dist[e.to] > dist[j] + e.cost){
     dist[e.to] = dist[j] + e.cost;
     pv[e.to] = j, ed[e.to] = idx;
     if (i == n) {
      upd = j;
      while(!mark[upd])mark[upd]=1,upd=pv[upd];
      return upd:
     }
    idx++:
  }
 }
return -1;
int Solve(int n) {
int rt = -1, ans = 0;
while ((rt = NegativeCycle(n)) >= 0) {
 memset(mark, false, sizeof(mark));
 vector<pair<int, int>> cyc;
 while (!mark[rt]) {
  cyc.emplace_back(pv[rt], ed[rt]);
  mark[rt] = true;
  rt = pv[rt];
 reverse(cyc.begin(), cyc.end());
  int cap = kInf;
 for (auto &i : cyc) {
  auto &e = g[i.first][i.second];
  cap = min(cap, e.cap);
 for (auto &i : cyc) {
  auto &e = g[i.first][i.second];
  e.cap -= cap;
   g[e.to][e.rev].cap += cap;
  ans += e.cost * cap;
return ans;
4.6
```

Flow Models

- Maximum/Minimum flow with lower bound / Circulation problem
 - 1. Construct super source ${\cal S}$ and sink ${\cal T}$.

 - 2. For each edge (x,y,l,u), connect $x\to y$ with capacity u-l. 3. For each vertex v, denote by in(v) the difference between the sum
 - of incoming lower bounds and the sum of outgoing lower bounds. 4. If in(v)>0, connect $S\to v$ with capacity in(v), otherwise, connect $v \to T$ with capacity -in(v).
 - To maximize, connect t o s with capacity ∞ (skip this in circulation problem), and let f be the maximum flow from S to T. If $f
 eq \sum_{v \in V, in(v) > 0} in(v)$, there's no solution. Otherwise, the
 - maximum flow from s to t is the answer. To minimize, let f be the maximum flow from S to T. Connect t o s with capacity ∞ and let the flow from S to T be f'. If $f+f' \neq \sum_{v\in V, in(v)>0} in(v)$, there's no solution. Otherwise, f' is the answer.
 - 5. The solution of each edge e is $l_e + f_e$, where f_e corresponds to the flow of edge e on the graph.
- ullet Construct minimum vertex cover from maximum matching M on bipartite graph(X, Y)
 - 1. Redirect every edge: $y \to x$ if $(x, y) \in M$, $x \to y$ otherwise.
 - 2. DFS from unmatched vertices in X
 - 3. $x \in X$ is chosen iff x is unvisited. 4. $y \in Y$ is chosen iff y is visited.
- · Minimum cost cyclic flow

- Consruct super source S and sink T
- 2. For each edge (x, y, c), connect $x \to y$ with (cost, cap) = (c, 1) if c>0 , otherwise connect $y\to x$ with (cost,cap)=(-c,1) 3. For each edge with c<0 , sum these cost as K , then increase d(y)
- by 1, decrease d(x) by 1 4. For each vertex v with d(v) > 0, connect $S \to v$ with (cost, cap) =
- 5. For each vertex v with d(v) < 0, connect $v \to T$ with (cost, cap) =(0, -d(v))
- 6. Flow from S to T, the answer is the cost of the flow C+K
- · Maximum density induced subgraph
 - 1. Binary search on answer, suppose we're checking answer ${\cal T}$
 - 2. Construct a max flow model, let ${\cal K}$ be the sum of all weights
 - 3. Connect source $s \to v, v \in G$ with capacitu K
 - 4. For each edge (u,v,w) in G, connect $u \to v$ and $v \to u$ with capacity
 - 5. For $v~\in~G$, connect it with sink $v~\rightarrow~t$ with capacity K~+~2T~- $\left(\sum_{e \in E(v)} w(e)\right) - 2w(v)$
 - 6. T is a valid answer if the maximum flow f < K |V|
- · Minimum weight edge cover
 - 1. For each $v \in V$ create a copy v', and connect $u' \to v'$ with weight
 - 2. Connect v
 ightarrow v' with weight $2\mu(v)$, where $\mu(v)$ is the cost of the cheapest edge incident to v
 - 3. Find the minimum weight perfect matching on G'.
- · Project selection problem
 - 1. If $p_v > 0$, create edge (s, v) with capacity p_v ; otherwise, create edge (v,t) with capacity $-p_v$
 - 2. Create edge $(\boldsymbol{u},\boldsymbol{v})$ with capacity \boldsymbol{w} with \boldsymbol{w} being the cost of choosing u without choosing v.
 - 3. The mincut is equivalent to the maximum profit of a subset of projects.
- 0/1 quadratic programming

$$\sum_{x} c_{x}x + \sum_{y} c_{y}\bar{y} + \sum_{xy} c_{xy}x\bar{y} + \sum_{xyx'y'} c_{xyx'y'}(x\bar{y} + x'\bar{y'})$$

can be minimized by the mincut of the following graph:

- 1. Create edge (x, t) with capacity c_x and create edge (s, y) with capacity c
- 2. Create edge (x,y) with capacity c_{xy} . 3. Create edge (x,y) and edge (x',y') with capacity $c_{xyx'y'}$.

4.7 Dinic template <typename Cap = int64_t>

```
class Dinic{
private:
  struct E{
    int to, rev;
    Cap cap;
  int n, st, ed;
  vector<vector<E>> G;
  vector<int> lv, idx;
  bool BFS(){
    lv.assign(n, -1);
    queue<int> bfs;
    bfs.push(st); lv[st] = 0;
    while (not bfs.empty()){
      int u = bfs.front(); bfs.pop();
      for (auto e: G[u]) {
         if (e.cap <= 0 or lv[e.to]!=-1) continue;</pre>
         bfs.push(e.to); lv[e.to] = lv[u] + 1;
      }
    return lv[ed] != -1;
  Cap DFS(int u, Cap f){
    if (u == ed) return f;
    Cap ret = 0;
    for(int &i = idx[u]; i < int(G[u].size()); ++i) {</pre>
      auto &e = G[u][i];
      if (e.cap <= 0 or lv[e.to]!=lv[u]+1) continue;</pre>
      Cap nf = DFS(e.to, min(f, e.cap));
ret += nf; e.cap -= nf; f -= nf;
      G[e.to][e.rev].cap += nf;
      if (f == 0) return ret;
    if (ret == 0) lv[u] = -1;
    return ret;
public:
  void init(int n_) { G.assign(n = n_, vector<E>()); }
  void add_edge(int u, int v, Cap c){
    G[u].push_back({v, int(G[v].size()), c});
```

```
G[v].push_back({u, int(G[u].size())-1, 0});
                                                                   ww+=ret.first * ret.second;
  Cap max_flow(int st_, int ed_){
                                                                  return {cc,ww};
    st = st_, ed = ed_; Cap ret = 0;
    while (BFS()) {
                                                               } mcmf;
      idx.assign(n, 0);
                                                                4.9 GomoryHu Tree
      Cap f = DFS(st, numeric_limits<Cap>::max());
      ret += f;
                                                               int g[maxn];
      if (f == 0) break;
                                                               vector<edge> GomoryHu(int n){
                                                                 vector<edge> rt;
    return ret;
                                                                 for(int i=1;i<=n;++i)g[i]=1;</pre>
                                                                 for(int i=2;i<=n;++i){</pre>
};
                                                                  int t=g[i];
                                                                  flow.reset(); // clear flows on all edge
      Minimum Cost Maximum Flow
4.8
                                                                  rt.push_back({i,t,flow(i,t)});
class MiniCostMaxiFlow{
                                                                  flow.walk(i); // bfs points that connected to i (use
 using Cap = int; using Wei = int64_t;
                                                                    edges not fully flow)
 using PCW = pair<Cap,Wei>;
                                                                  for(int j=i+1;j<=n;++j){
  if(g[j]==t && flow.connect(j))g[j]=i; // check if i</pre>
 static constexpr Cap INF_CAP = 1 << 30;</pre>
 static constexpr Wei INF_WEI = 1LL<<60;</pre>
                                                                    can reach j
private:
                                                                  }
 struct Edge{
                                                                 }
  int to, back;
                                                                 return rt;
  Cap cap; Wei wei;
  Edge() {}
  Edge(int a,int b, Cap c, Wei d):
                                                                4.10 Global Min-Cut
   to(a),back(b),cap(c),wei(d)
                                                               const int maxn = 500 + 5;
  {}
                                                               int w[maxn][maxn], g[maxn];
 };
                                                               bool v[maxn], del[maxn];
 int ori, edd;
                                                               void add_edge(int x, int y, int c) {
 vector<vector<Edge>> G;
                                                                w[x][y] += c; w[y][x] += c;
 vector<int> fa, wh;
 vector<bool> inq;
                                                               pair<int, int> phase(int n) {
 vector<Wei> dis:
                                                                memset(v, false, sizeof(v));
 PCW SPFA(){
                                                                memset(g, 0, sizeof(g));
int s = -1, t = -1;
  fill(inq.begin(),inq.end(),false);
  fill(dis.begin(), dis.end(), INF_WEI);
                                                                 while (true) {
  queue<int> qq; qq.push(ori);
                                                                  int c = -1;
  dis[ori] = 0;
                                                                  for (int i = 0; i < n; ++i) {
  while(not qq.empty()){
                                                                   if (del[i] || v[i]) continue;
   int u=qq.front();qq.pop();
                                                                   if (c == -1 \mid | g[i] > g[c]) c = i;
   inq[u] = false
   for(int i=0;i<SZ(G[u]);++i){</pre>
                                                                  if (c == -1) break;
    Edge e=G[u][i];
                                                                  v[s = t, t = c] = true;
    int v=e.to; Wei d=e.wei;
                                                                  for (int i = 0; i < n; ++i) {
  if (del[i] || v[i]) continue;</pre>
    if(e.cap <= 0 | |dis[v] <= dis[u] + d)
     continue
                                                                   g[i] += w[c][i];
    dis[v] = dis[u] + d;
                                                                  }
    fa[v] = u, wh[v] = i;
if (inq[v]) continue;
                                                                 return make_pair(s, t);
    qq.push(v);
    inq[v] = true;
                                                               int mincut(int n) {
                                                                int cut = 1e9;
                                                                memset(del, false, sizeof(del));
  if(dis[edd]==INF_WEI) return {-1, -1};
                                                                 for (int i = 0; i < n - 1; ++i) {
  Cap mw=INF_CAP;
                                                                  int s, t; tie(s, t) = phase(n);
  for(int i=edd;i!=ori;i=fa[i])
                                                                  del[t] = true; cut = min(cut, g[t]);
for (int j = 0; j < n; ++j) {</pre>
   mw=min(mw,G[fa[i]][wh[i]].cap);
  for (int i=edd;i!=ori;i=fa[i]){
                                                                   w[s][j] += w[t][j]; w[j][s] += w[j][t];
   auto &eg=G[fa[i]][wh[i]];
                                                                  }
   eg.cap -= mw;
   G[eg.to][eg.back].cap+=mw;
                                                                 return cut;
  return {mw, dis[edd]};
                                                                5
                                                                     Math
public:
 void init(int a,int b,int n){
                                                               5.1 \left| \frac{n}{i} \right| Enumeration
  ori=a,edd=b;
                                                               T_0 = 1, T_{i+1} = \lfloor \frac{n}{\lfloor \frac{n}{T_i + 1} \rfloor} \rfloor
  G.clear();G.resize(n);
  fa.resize(n);wh.resize(n);
                                                                5.2 ax+by=gcd
  inq.resize(n); dis.resize(n);
                                                               // ax+ny = 1, ax+ny == ax == 1 \pmod{n}
                                                               void exgcd(lld x,lld y,lld &g,lld &a,lld &b) {
 void add_edge(int st, int ed, Cap c, Wei w){
                                                                if (y == 0) g=x, a=1, b=0;
  G[st].emplace_back(ed,SZ(G[ed]),c,w);
                                                                else exgcd(y,x%y,g,b,a),b=(x/y)*a;
  G[ed].emplace_back(st,SZ(G[st])-1,0,-w);
 PCW solve(){
                                                               5.3 Pollard Rho
  Cap cc=0; Wei ww=0;
  while(true){
                                                               // does not work when n is prime
   PCW ret=SPFA();
                                                               // return any non-trivial factor
   if(ret.first==-1) break;
                                                               llu pollard_rho(llu n){
   cc+=ret.first;
                                                                static auto f=[](llu x,llu k,llu m){
```

```
return add(k,mul(x,x,m),m);
};
if (!(n&1)) return 2;
mt19937 rnd(120821011);
while(true){
    llu y=2,yy=y,x=rnd()%n,t=1;
    for(llu sz=2;t==1;sz<<=1) {
        for(llu i=0;i<sz;++i){
            if(t!=1)break;
            yy=f(yy,x,n);
            t=gcd(yy>y?yy-y:y-yy,n);
        }
        y=yy;
    }
    if(t!=1&&t!=n) return t;
}
```

5.4 Pi Count (Linear Sieve)

```
static constexpr int N = 1000000 + 5;
11d pi[N];
vector<int> primes;
bool sieved[N];
11d cube_root(11d x){
lld s=cbrt(x-static_cast<long double>(0.1));
while(s*s*s <= x) ++s;
return s-1:
11d square_root(11d x){
1ld s=sqrt(x-static_cast<long double>(0.1));
while(s*s <= x) ++s;</pre>
return s-1;
void init(){
primes.reserve(N);
primes.push_back(1);
 for(int i=2;i<N;i++) {</pre>
 if(!sieved[i]) primes.push_back(i);
  pi[i] = !sieved[i] + pi[i-1];
  for(int p: primes) if(p > 1) {
  if(p * i >= N) break;
   sieved[p * i] = true;
  if(p % i == 0) break;
  }
11d phi(11d m, 11d n) {
static constexpr int MM = 80000, NN = 500;
static lld val[MM][NN];
if(m<MM&&n<NN&&val[m][n])return val[m][n]-1;</pre>
if(n == 0) return m;
 if(primes[n] >= m) return 1;
lld ret = phi(m,n-1)-phi(m/primes[n],n-1);
if(m<MM&&n<NN) val[m][n] = ret+1;</pre>
 return ret;
11d pi_count(11d);
11d P2(11d m, 11d n) {
1ld sm = square_root(m), ret = 0;
for(lld i = n+1;primes[i]<=sm;i++)</pre>
 ret+=pi_count(m/primes[i])-pi_count(primes[i])+1;
return ret;
11d pi_count(11d m) {
if(m < N) return pi[m];</pre>
11d n = pi_count(cube_root(m));
return phi(m, n) + n - 1 - P2(m, n);
```

5.5 Strling Number

5.5.1 First Kind

 $S_1(n,k)$ counts the number of permutations of n elements with k disjoint cycles.

$$S_1(n,k) = (n-1) \cdot S_1(n-1,k) + S_1(n-1,k-1)$$
$$x(x+1) \dots (x+n-1) = \sum_{k=0}^{n} S_1(n,k) x^k$$

$$g(x) = x(x+1)\dots(x+n-1) = \sum_{k=0}^{n} a_k x^k$$

$$\Rightarrow g(x+n) = \sum_{k=0}^{n} \frac{b_k}{(n-k)!} x^{n-k},$$

$$b_k = \sum_{i=0}^{k} ((n-i)! a_{n-i}) \cdot (\frac{n^{k-i}}{(k-i)!})$$

5.5.2 Second Kind

 $S_2(n,k)$ counts the number of ways to partition a set of n elements into k nonempty sets.

$$S_2(n,k) = S_2(n-1,k-1) + k \cdot S_2(n-1,k)$$

$$S_2(n,k) = \sum_{i=0}^k \binom{k}{i} i^n (-1)^{k-i} = \sum_{i=0}^k \frac{(-1)^i}{i!} \cdot \frac{(k-i)^n}{(k-i)!}$$

5.6 Range Sieve

5.7 Miller Rabin

```
bool isprime(llu x){
 static llu magic[]={2,325,9375,28178,\
          450775,9780504,1795265022};
 static auto witn=[](llu a,llu u,llu n,int t)
 ->bool{
  if (!(a = mpow(a%n,u,n)))return 0;
  while(t--){
   1lu a2=mul(a,a,n);
   if(a2==1 && a!=1 && a!=n-1)
    return 1;
   a = a2;
 }
  return a!=1;
 if(x<2)return 0;</pre>
 if(!(x&1))return x==2;
 llu x1=x-1;int t=0;
 while(!(x1&1))x1>>=1,t++;
 for(llu m:magic)if(witn(m,x1,x,t))return 0;
 return 1:
```

5.8 Extended Euler

$$a^b \equiv \begin{cases} a^b \mod \varphi(m) + \varphi(m) & \text{if } (a,m) \neq 1 \land b \geq \varphi(m) \\ a^b \mod \varphi(m) & \text{otherwise} \end{cases} \pmod m$$

5.9 Gauss Elimination

```
void gauss(vector<vector<double>> &d) {
  int n = d.size(), m = d[0].size();
  for (int i = 0; i < m; ++i) {
    int p = -1;
    for (int j = i; j < n; ++j) {
      if (fabs(d[j][i]) < eps) continue;
      if (p == -1 || fabs(d[j][i])>fabs(d[p][i])) p=j;
    }
  if (p == -1) continue;
  for (int j = 0; j < m; ++j) swap(d[p][j], d[i][j]);
  for (int j = 0; j < n; ++j) {
    if (i == j) continue;
    double z = d[j][i] / d[i][i];
}</pre>
```

```
for (int k = 0; k < m; ++k) d[j][k] -= z*d[i][k];
                                                                int sz = 1;
                                                                while (sz + 1 < a.size() + b.size()) sz <<= 1;</pre>
                                                                vector<cplx> fa(sz), fb(sz);
 }
                                                                for (int i = 0; i < (int)a.size(); ++i)</pre>
                                                                 fa[i] = cplx(a[i] & ((1 << 15) - 1), a[i] >> 15);
      Fast Fourier Transform
5.10
                                                                for (int i = 0; i < (int)b.size(); ++i)</pre>
const int mod = 1000000007;
                                                                  fb[i] = cplx(b[i] & ((1 << 15) - 1), b[i] >> 15);
                                                                fft(fa, sz), fft(fb, sz);
const int M1 = 985661441; // G = 3
                                                                double r = 0.25 / sz;
                                                                cplx r2(0, -1), r3(r, 0), r4(0, -r), r5(0, 1);
for (int i = 0; i <= (sz >> 1); ++i) {
const int M2 = 998244353;
const int M3 = 1004535809;
                                                                  int j = (sz - i) & (sz - 1);
                                                                  cplx a1 = (fa[i] + fa[j].conj());
int superBigCRT(int64_t A, int64_t B, int64_t C) {
                                                                  cplx a2 = (fa[i] - fa[j].conj()) * r2;
 static_assert (M1 <= M2 && M2 <= M3);
                                                                  cplx b1 = (fb[i] + fb[j].conj()) * r3;
  constexpr int64_t r12 = modpow(M1, M2-2, M2);
                                                                  cplx b2 = (fb[i] - fb[j].conj()) * r4;
  constexpr int64_t r13 = modpow(M1, M3-2, M3);
 constexpr int64_t r23 = modpow(M2, M3-2, M3);
constexpr int64_t M1M2 = 1LL * M1 * M2 % mod;
                                                                  if (i != j)
                                                                  cplx c1 = (fa[j] + fa[i].conj());
cplx c2 = (fa[j] - fa[i].conj()) * r2;
 B = (B - A + M2) * r12 % M2;
 C = (C - A + M3) * r13 % M3;
                                                                   cplx d1 = (fb[j] + fb[i].conj()) * r3;
 C = (C - B + M3) * r23 % M3;
                                                                   cplx d2 = (fb[j] - fb[i].conj()) * r4;
  return (A + B * M1 + C * M1M2) % mod;
                                                                   fa[i] = c1 * d1 + c2 * d2 * r5;
                                                                   fb[i] = c1 * d2 + c2 * d1;
                                                                  fa[j] = a1 * b1 + a2 * b2 * r5;
namespace fft {
using VI = vector<int>;
                                                                 fb[j] = a1 * b2 + a2 * b1;
using VL = vector<long long>;
const double pi = acos(-1);
                                                                fft(fa, sz), fft(fb, sz);
                                                                vector<int> res(sz);
cplx omega[maxn + 1];
                                                                for (int i = 0; i < sz; ++i) {</pre>
void prefft()
                                                                  long long a = round(fa[i].re), b = round(fb[i].re),
for (int i = 0; i <= maxn; i++)</pre>
  omega[i] = cplx(cos(2 * pi * j / maxn),
                                                                       c = round(fa[i].im);
     sin(2 * pi * j / maxn));
                                                                  res[i] = (a+((b \% p) << 15)+((c \% p) << 30)) \% p;
                                                                }
void fft(vector<cplx> &v, int n) {
                                                                return res;
 int z = __builtin_ctz(n) - 1;
for (int i = 0; i < n; ++i) {
                                                               }}
                                                               5.11 Chinese Remainder
  int x = 0, j = 0;
  for (;(1 << j) < n;++j) x^{=(i >> j & 1)<<(z - j);
                                                               1ld crt(lld ans[], lld pri[], int n){
  if (x > i) swap(v[x], v[i]);
                                                                lld M = 1, ret = 0;
                                                                for(int i=0;i<n;i++) M *= pri[i];</pre>
 for (int s = 2; s <= n; s <<= 1) {
                                                                for(int i=0;i<n;i++){</pre>
  int z = s >> 1;
                                                                 lld iv = (gcd(M/pri[i],pri[i]).FF+pri[i])%pri[i];
  for (int i = 0; i < n; i += s) {
                                                                  ret += (ans[i]*(M/pri[i])%M * iv)%M;
   for (int k = 0; k < z; ++k) {
  cplx x = v[i + z + k] * omega[maxn / s * k];
                                                                  ret %= M;
    v[i + z + k] = v[i + k] - x;
                                                                return ret;
    v[i + k] = v[i + k] + x;
                                                               }
                                                               Another:
                                                               x = a1 \% m1
                                                               x = a2 \% m2
void ifft(vector<cplx> &v, int n) {
                                                               g = gcd(m1, m2)
 fft(v, n);
                                                               assert((a1-a2)%g==0)
 reverse(v.begin() + 1, v.end());
                                                               [p, q] = exgcd(m2/g, m1/g)
 for (int i=0;i<n;++i) v[i] = v[i] * cplx(1. / n, 0);
                                                               return a2+m2*(p*(a1-a2)/g)
                                                               0 <= x < lcm(m1, m2)
VL convolution(const VI &a, const VI &b) {
 // Should be able to handle N <= 10^5, C <= 10^4
 int sz = 1;
                                                               5.12 Berlekamp Massey
 while (sz < a.size() + b.size() - 1) sz <<= 1;</pre>
 vector<cplx> v(sz);
                                                               // x: 1-base, p[]: 0-base
 for (int i = 0; i < sz; ++i) {
                                                               template<size_t N>
  double re = i < a.size() ? a[i] : 0;
double im = i < b.size() ? b[i] : 0;</pre>
                                                               vector<llf> BM(llf x[N], size_t n){
                                                                size_t f[N]={0},t=0;11f d[N];
  v[i] = cplx(re, im);
                                                                vector<llf> p[N];
                                                                for(size_t i=1,b=0;i<=n;++i) {</pre>
                                                                  for(size_t j=0;j<p[t].size();++j)</pre>
 fft(v, sz);
                                                                   d[i]+=x[i-j-1]*p[t][j];
 for (int i = 0; i \le sz / 2; ++i) {
  int j = (sz - i) & (sz - 1);
                                                                  if(abs(d[i]-=x[i])<=EPS)continue;</pre>
                                                                  f[t]=i;if(!t){p[++t].resize(i);continue;}
  cplx x = (v[i] + v[j].conj()) * (v[i] - v[j].conj())
                                                                  vector<llf> cur(i-f[b]-1);
    * cplx(0, -0.25);
                                                                  llf k=-d[i]/d[f[b]]; cur.PB(-k);
  if (j != i) v[j] = (v[j] + v[i].conj()) * (v[j] - v[i
                                                                  for(size_t j=0;j<p[b].size();j++)</pre>
    ].conj()) * cplx(0, -0.25);
                                                                   cur.PB(p[b][j]*k);
  v[i] = x;
                                                                  if(cur.size()<p[t].size())cur.resize(p[t].size());</pre>
 ifft(v, sz);
                                                                  for(size_t j=0;j<p[t].size();j++)cur[j]+=p[t][j];</pre>
                                                                  if(i-f[b]+p[b].size()>=p[t].size()) b=t;
 VL c(sz);
 for (int i = 0; i < sz; ++i) c[i] = round(v[i].re);</pre>
                                                                 p[++t]=cur;
 return c;
                                                                return p[t];
VI convolution_mod(const VI &a, const VI &b, int p) {
```

5.13 NTT

using VL = vector<LL>

```
template <int mod, int G, int maxn>
struct NTT {
static_assert (maxn == (maxn & -maxn));
 int roots[maxn];
NTT () {
 int r = modpow(G, (mod - 1) / maxn);
  for (int i = maxn >> 1; i; i >>= 1) {
  roots[i] = 1;
   for (int j = 1; j < i; j++)
    roots[i + j] = modmul(roots[i + j - 1], r);
   r = modmul(r, r);
// n must be 2^k, and 0 <= F[i] < mod
void inplace_ntt(int n, int F[], bool inv = false) {</pre>
 for (int i = 0, j = 0; i < n; i++) {
  if (i < j) swap(F[i], F[j]);</pre>
   for (int k = n > 1; (j^k < k; k > = 1);
  for (int s = 1; s < n; s *= 2) {
   for (int i = 0; i < n; i += s * 2) {
   for (int j = 0; j < s; j++) {
     int a = F[i+j];
     int b = modmul(F[i+j+s], roots[s+j]);
     F[i+j] = modadd(a, b); // a + b
     F[i+j+s] = modsub(a, b); // a - b
   }
  if (inv) {
   int invn = modinv(n);
   for (int i = 0; i < n; i++)</pre>
   F[i] = modmul(F[i], invn);
   reverse(F + 1, F + n);
};
const int P=2013265921, root=31;
const int MAXN=1<<20;</pre>
NTT<P, root, MAXN> ntt;
5.14 Polynomial Operations
```

```
#define fi(s, n) for (int i=int(s); i<int(n); ++i)</pre>
#define Fi(s, n) for (int i=int(n); i>int(s); --i)
int n2k(int n) -
int sz = 1; while (sz < n) sz <<= 1;</pre>
return sz;
template<int MAXN, LL P, LL RT> // MAXN = 2^k
struct Poly { // coefficients in [0, P)
static NTT<MAXN, P, RT> ntt;
VL coef;
int n() const { return coef.size(); } // n()>=1
LL *data() { return coef.data(); }
const LL *data() const { return coef.data(); }
LL &operator[](size_t i) { return coef[i]; }
const LL &operator[](size_t i)const{return coef[i];}
Poly(initializer_list<LL> a) : coef(a) { }
explicit Poly(int _n = 1) : coef(_n) { }
Poly(const LL *arr, int _n) : coef(arr, arr + _n) {}
Poly(const Poly &p, int _n) : coef(_n) {
 copy_n(p.data(), min(p.n(), _n), data());
Poly& irev(){return reverse(data(),data()+n()),*this;}
Poly& isz(int _n) { return coef.resize(_n), *this; }
Poly& iadd(const Poly &rhs) { // n() == rhs.n()
 fi(0, n()) if ((coef[i]+=rhs[i]) >= P)coef[i]-=P;
  return *this;
Poly& imul(LL k) {
 fi(0, n()) coef[i] = coef[i] * k % P;
  return *this;
Poly Mul(const Poly &rhs) const {
 const int _n = n2k(n() + rhs.n() - 1);
  Poly X(*this, _n), Y(rhs, _n);
 ntt(X.data(), _n), ntt(Y.data(), _n);
fi(0, _n) X[i] = X[i] * Y[i] % P;
 ntt(X.data(), _n, true);
```

```
return X.isz(n() + rhs.n() - 1);
Poly Inv() const { // coef[0] != 0
 if (n() == 1) return {ntt.minv(coef[0])};
 const int _n = n2k(n() * 2);
 Poly Xi = Poly(*this, (n() + 1)/2).Inv().isz(_n);
Poly Y(*this, _n);
ntt(Xi.data(), _n), ntt(Y.data(), _n);
 fi(0, _n) {
Xi[i] *= (2 - Xi[i] * Y[i]) % P
  if ((Xi[i] %= P) < 0) Xi[i] += P;</pre>
ntt(Xi.data(), _n, true);
 return Xi.isz(n());
Poly Sqrt() const { // Jacobi(coef[0], P) = 1
if (n()==1) return {QuadraticResidue(coef[0], P)};
 Poly X = Poly(*this, (n()+1) / 2).Sqrt().isz(n());
 return X.iadd(Mul(X.Inv()).isz(n())).imul(P/2+1);
pair<Poly, Poly> DivMod(const Poly &rhs) const {
 // (rhs.)back() != 0
 if (n() < rhs.n()) return {{0}, *this};</pre>
 const int _n = n() - rhs.n() + 1;
 Poly X(rhs); X.irev().isz(_n);
Poly Y(*this); Y.irev().isz(_n);
Poly Q = Y.Mul(X.Inv()).isz(_n).irev();
 X = rhs.Mul(Q), Y = *this
fi(0, n()) if ((Y[i] -= X[i]) < 0) Y[i] += P;
return {0, Y.isz(max(1, rhs.n() - 1))};
Poly Dx() const {
Poly ret(n() - 1);
fi(0, ret.n()) ret[i] = (i + 1) * coef[i + 1] % P;
 return ret.isz(max(1, ret.n()));
Poly Sx() const {
Poly ret(n() + 1);
 fi(0, n()) ret[i + 1]=ntt.minv(i + 1)*coef[i] % P;
 return ret:
Poly _tmul(int nn, const Poly &rhs) const {
  Poly Y = Mul(rhs).isz(n() + nn - 1);
 return Poly(Y.data() + n() - 1, nn);
VL _eval(const VL &x, const auto up)const{
const int _n = (int)x.size();
 if (!_n) return {};
 vector<Poly> down(_n * 2);
 down[1] = DivMod(up[1]).second;
 \label{eq:fi-down}  \mbox{fi}(2,\_n^{\star}2) \mbox{ down[i]=down[i/2].DivMod(up[i]).second;} 
 /* down[1] = Poly(up[1]).irev().isz(n()).Inv().irev()
    _tmul(_n, *this)
 fi(2, _n * 2) down[i] = up[i ^ 1]._tmul(up[i].n() -
   1, down[i / 2]); */
 VL y(_n);
 fi(0, _n) y[i] = down[_n + i][0];
 return y;
static vector<Poly> _tree1(const VL &x) {
const int _n = (int)x.size();
 vector<Poly> up(_n * 2);
 fi(0, _n) up[_n + i] = \{(x[i] ? P - x[i] : 0), 1\};
 Fi(0, _n-1) up[i] = up[i * 2].Mul(up[i * 2 + 1]);
 return up;
VL Eval(const VL&x)const{return _eval(x,_tree1(x));}
static Poly Interpolate(const VL &x, const VL &y) {
const int _n = (int)x.size();
vector<Poly> up = _tree1(x), down(_n * 2);
VL z = up[1].Dx()._eval(x, up);
 fi(0, _n) z[i] = y[i] * ntt.minv(z[i]) % P;
 fi(0, _n) down[_n + i] = \{z[i]\};
 Fi(0, _n-1) down[i]=down[i * 2].Mul(up[i * 2 + 1])
  .iadd(down[i * 2 + 1].Mul(up[i * 2]));
 return down[1];
Poly Ln() const { // coef[0] == 1
return Dx().Mul(Inv()).Sx().isz(n());
Poly Exp() const \{ // coef[0] == 0 \}
if (n() == 1) return {1};
```

```
Poly X = Poly(*this, (n() + 1)/2).Exp().isz(n());
                                                                x[i] %= MOD;
  Poly Y = X.Ln(); Y[0] = P - 1;
                                                               }
                                                             }
 fi(0, n()) if((Y[i] = coef[i] - Y[i]) < 0)Y[i]+=P;
  return X.Mul(Y).isz(n());
                                                                    DiscreteLog
Poly Pow(const string &K) const {
                                                             template<typename Int>
 int nz = 0;
                                                             Int BSGS(Int x, Int y, Int M) {
  while (nz < n() && !coef[nz]) ++nz;</pre>
                                                               // x^? \equiv y (mod M)
 LL nk = 0, nk2 = 0;
                                                               Int t = 1, c = 0, g = 1;
  for (char c : K) {
                                                               for (Int M_ = M; M_ > 0; M_ >>= 1)
  nk = (nk * 10 + c - '0') % P;
                                                                 g = g * x % M;
   nk2 = nk2 * 10 + c - '0';
                                                               for (g = gcd(g, M); t % g != 0; ++c) {
  if (nk2 * nz >= n()) return Poly(n());
                                                                 if (t == y) return c;
   nk2 %= P - 1;
                                                                 t = t * x % M;
  if (!nk && !nk2) return Poly({1}, n());
                                                               if (y % g != 0) return -1;
 Poly X(data() + nz, n() - nz * nk2);
                                                               t /= g, y /= g, M /= g;
 LL \times 0 = X[0];
                                                               Int h = 0, gs = 1;
for (; h * h < M; ++h) gs = gs * x % M;
  return X.imul(ntt.minv(x0)).Ln().imul(nk).Exp()
   .imul(ntt.mpow(x0, nk2)).irev().isz(n()).irev();
                                                               unordered_map<Int, Int> bs;
                                                               for (Int s = 0; s < h; bs[y] = ++s)
Poly InvMod(int L) { // (to evaluate linear recursion)
                                                                 y = y * x % M;
 Poly R{1, 0}; // *this * R mod x^L = 1 (*this[0] ==
                                                               for (Int s = 0; s < M; s += h) {
   1)
                                                                 t = t * gs % M;
  for (int level = 0; (1 << level) < L; ++level) {</pre>
                                                                 if (bs.count(t)) return c + s + h - bs[t];
  Poly 0 = R.Mul(Poly(data(), min(2 << level, n())));
   Poly Q(2 << level); Q[0] = 1;
                                                               return -1:
   for (int j = (1 << level); j < (2 << level); ++j)</pre>
   Q[j] = (P - O[j]) \% P;
   R = R.Mul(Q).isz(4 << level);
                                                             5.17 FloorSum
                                                             // @param n `n < 2^32`
 return R.isz(L);
                                                             // @param m `1 <= m < 2^32`
                                                             // @return sum_{i=0}^{n-1} floor((ai + b)/m) mod 2^64
static LL LinearRecursion(const VL&a,const VL&c,LL n){
                                                             1lu floor_sum_unsigned(llu n, llu m, llu a, llu b) {
 // a_n = \sum_{j=0}^{n-j} a_{n-j}
                                                              llu ans = 0;
  const int k = (int)a.size();
                                                              while (true)
 assert((int)c.size() == k + 1);
 Poly C(k + 1), W(\{1\}, k), M = \{0, 1\}; fi(1, k + 1) C(k - i) = c[i] ? P - c[i] : 0;
                                                               if (a >= m)
                                                                ans += n * (n - 1) / 2 * (a / m); a %= m;
 C[k] = 1:
                                                               if (b >= m) {
  while (n) {
                                                                ans += n * (b / m); b %= m;
  if (n % 2) W = W.Mul(M).DivMod(C).second;
  n /= 2, M = M.Mul(M).DivMod(C).second;
                                                               llu y_max = a * n + b;
                                                               if (y_max < m) break;</pre>
 LL ret = 0:
                                                               // y_max < m * (n + 1)
 fi(0, k) ret = (ret + W[i] * a[i]) % P;
                                                               // floor(y_max / m) <= n
  return ret:
                                                               n = (llu)(y_max / m), b = (llu)(y_max % m);
                                                               swap(m, a);
#undef fi
                                                              return ans;
#undef Fi
using Poly_t = Poly<131072 * 2, 998244353, 3>;
                                                             11d floor_sum(lld n, lld m, lld a, lld b) {
template<> decltype(Poly_t::ntt) Poly_t::ntt = {};
                                                              11u ans = 0:
5.15 FWT
                                                              if (a < 0) {
                                                               11u \ a2 = (a \% m + m) \% m;
/* xor convolution:
                                                               ans -= 1ULL * n * (n - 1) / 2 * ((a2 - a) / m);
* x = (x0, x1) , y = (y0, y1)
                                                               a = a2;
*z = (x0y0 + x1y1 , x0y1 + x1y0 )
                                                              if (b < 0) {
* x' = (x0+x1, x0-x1), y' = (y0+y1, y0-y1)
                                                               11u b2 = (b \% m + m) \% m;
* z' = ((x\theta + x1)(y\theta + y1)), (x\theta - x1)(y\theta - y1))
* z = (1/2) * z''
                                                               ans -= 1ULL * n * ((b2 - b) / m);
                                                               b = b2:
 * or convolution:
* x = (x0, x0+x1), inv = (x0, x1-x0) w/o final div
                                                              return ans + floor_sum_unsigned(n, m, a, b);
* and convolution:
 * x = (x0+x1, x1), inv = (x0-x1, x1) w/o final div */
const LL MOD = 1e9+7;
                                                             5.18 Quadratic residue
inline void fwt( LL x[ MAXN ] , int N , bool inv=0 ) {
for( int d = 1 ; d < N ; d <<= 1 ) {</pre>
                                                             struct S {
  int d2 = d << 1;
                                                              int MOD, w;
                                                              int64_t x, y;
  for( int s = 0 ; s < N ; s += d2 )
   for( int i = s , j = s+d ; i < s+d ; i++, j++ ){</pre>
                                                              S(int m, int w_=-1, int64_t x_=1, int64_t y_=0)
   LL ta = x[ i ] , tb = x[ j ];
                                                               : MOD(m), w(w_{-}), x(x_{-}), y(y_{-}) {}
   x[ i ] = ta+tb;
                                                              S operator*(const S &rhs) const {
   x[ j ] = ta-tb;
                                                               int w_{-} = w
    if( x[ i ] >= MOD ) x[ i ] -= MOD;
                                                               if (w_{-} == -1) w_{-} = rhs.w;
                                                               assert(w_ != -1 and w_ == rhs.w);
    if( x[ j ] < 0 ) x[ j ] += MOD;</pre>
                                                               return { MOD, w_,
   }
                                                                (x * rhs.x + y * rhs.y % MOD * w) % MOD,
                                                                 (x * rhs.y + y * rhs.x) % MOD };
if( inv )
  for( int i = 0 ; i < N ; i++ ) {</pre>
                                                            };
  x[ i ] *= inv( N, MOD );
```

```
int get_root(int n, int P) {
  if (P == 2 or n == 0) return n;
if (qpow(n, (P - 1) / 2, P) != 1) return -1;
  auto check = [&](int x) {
  return qpow(x, (P - 1) / 2, P); };
if (check(n) == P-1) return -1;
  int64_t a; int w; mt19937 rnd(7122);
  do { a = rnd() % P;
    w = ((a * a - n) % P + P) % P;
  } while (check(w) != P - 1);
  return qpow(S(P, w, a, 1), (P + 1) / 2).x;
5.19 De-Bruijn
int res[maxn], aux[maxn], sz;
void db(int t, int p, int n, int k) {
 if (t > n) {
  if (n \% p == 0)
   for (int i = 1; i <= p; ++i)
     res[sz++] = aux[i];
 } else {
  aux[t] = aux[t - p];
  db(t + 1, p, n, k);
  for (int i = aux[t - p] + 1; i < k; ++i) {</pre>
   aux[t] = i;
   db(t + 1, t, n, k);
  }
int de_bruijn(int k, int n) {
  // return cyclic string of len k^n s.t. every string
 // of len n using k char appears as a substring.
 if (k == 1) {
  res[0] = 0;
  return 1;
 for (int i = 0; i < k * n; i++) aux[i] = 0;
 sz = 0;
 db(1, 1, n, k);
 return sz;
5.20 Simplex Construction
Standard form: maximize \sum_{1 \le i \le n} c_i x_i such that for all 1 \le j \le m,
\sum_{1 \leq i \leq n} A_{ji} x_i \leq b_j. \text{and } x_i \geq 0 \text{ for all } 1 \leq i \leq n.
  1. In case of minimization, let c'_i = -c_i
  2. \sum_{1 < i < n} A_{ji} x_i \ge b_j \to \sum_{1 < i < n} -A_{ji} x_i \le -b_j
  3. \sum_{1 < i < n} A_{ji} x_i = b_j
         • \sum_{1 \leq i \leq n} A_{ji} x_i \leq b_j
         • \sum_{1 \leq i \leq n} A_{ji} x_i \geq b_j
  4. If x_i has no lower bound, replace x_i with x_i - x_i'
5.21 Simplex
namespace simplex {
// maximize c^Tx under Ax <= B
// return VD(n, -inf) if the solution doesn't exist
                                                                               }
// return VD(n, +inf) if the solution is unbounded
using VD = vector<double>;
using VVD = vector<vector<double>>;
const double eps = 1e-9;
const double inf = 1e+9;
int n, m;
VVD d;
vector<int> p, q;
void pivot(int r, int s) {
  double inv = 1.0 / d[r][s];
 for (int i = 0; i < m + 2; ++i)
  for (int j = 0; j < n + 2; ++j)
if (i != r && j != s)
```

d[i][j] -= d[r][j] * d[i][s] * inv;

d[r][s] = inv; swap(p[r], q[s]);

bool phase(int z) {

int x = m + z;

for(int i=0;i<m+2;++i) if (i != r) d[i][s] *= -inv;
for(int j=0;j<n+2;++j) if (j != s) d[r][j] *= +inv;</pre>

```
while (true) {
  int s = -1;
  for (int i = 0; i <= n; ++i) {
  if (!z && q[i] == -1) continue
   if (s == -1 \mid | d[x][i] < d[x][s]) s = i;
  if (d[x][s] > -eps) return true;
  int r = -1;
  for (int i = 0; i < m; ++i) {
  if (d[i][s] < eps) continue;
  if (r == -1 || \</pre>
    d[i][n+1]/d[i][s] < d[r][n+1]/d[r][s]) r = i;
  if (r == -1) return false;
  pivot(r, s);
VD solve(const VVD &a, const VD &b, const VD &c) {
m = b.size(), n = c.size();
 d = VVD(m + 2, VD(n + 2));
 for (int i = 0; i < m; ++i)
  for (int j = 0; j < n; ++j) d[i][j] = a[i][j];
 p.resize(m), q.resize(n + 1);
for (int i = 0; i < m; ++i)</pre>
  p[i] = n + i, d[i][n] = -1, d[i][n + 1] = b[i];
 for (int i = 0; i < n; ++i) q[i] = i,d[m][i] = -c[i];
q[n] = -1, d[m + 1][n] = 1;
 int r = 0;
 for (int i = 1; i < m; ++i)
if (d[i][n + 1] < d[r][n + 1]) r = i;</pre>
 if (d[r][n + 1] < -eps) {</pre>
  pivot(r, n);
  if (!phase(1) || d[m + 1][n + 1] < -eps)</pre>
   return VD(n, -inf);
  for (int i = 0; i < m; ++i) if (p[i] == -1) {
   int s = min_element(d[i].begin(), d[i].end() - 1)
        - d[i].begin();
   pivot(i, s);
 if (!phase(0)) return VD(n, inf);
 VD x(n);
 for (int i = 0; i < m; ++i)
  if (p[i] < n) \times [p[i]] = d[i][n + 1];
 return x:
5.22 Charateristic Polynomial
```

```
vector<vector<int>> Hessenberg(const vector<vector<int
    >> &A) {
 int N = A.size();
 vector<vector<int>> H = A;
 for (int i = 0; i < N - 2; ++i) {</pre>
  if (!H[i + 1][i]) {
   for (int j = i + 2; j < N; ++j) {
  if (H[j][i]) {
      for (int k = i; k < N; ++k) swap(H[i + 1][k], H[j
    ][k]);
      for (int k = 0; k < N; ++k) swap(H[k][i + 1], H[k]
    ][j]);
     break:
  if (!H[i + 1][i]) continue;
  int val = fpow(H[i + 1][i], kP - 2);
  for (int j = i + 2; j < N; ++j) {
  int coef = 1LL * val * H[j][i] % kP;</pre>
   for (int k = i; k < N; ++k) H[j][k] = (H[j][k] + 1LL + H[i + 1][k] * (kP - coef)) % kP;
   for (int k = 0; k < N; ++k) H[k][i + 1] = (H[k][i +
    1] + 1LL * H[k][j] * coef) % kP;
 return H;
vector<int> CharacteristicPoly(const vector<vector<int
    >> &A) {
 int N = A.size();
 auto H = Hessenberg(A);
 for (int i = 0; i < N; ++i) {
```

for (int j = 0; j < N; ++j) H[i][j] = kP - H[i][j];

5.23 Partition Number

```
int b = sqrt(n);
ans[0] = tmp[0] = 1;
for (int i = 1; i <= b; i++) {
  for (int rep = 0; rep < 2; rep++)
    for (int j = i; j <= n - i * i; j++)
      modadd(tmp[j], tmp[j-i]);
  for (int j = i * i; j <= n; j++)
    modadd(ans[j], tmp[j - i * i]);
}</pre>
```

6 Geometry

6.1 Basic Geometry

```
using coord_t = int;
using Real = double;
using Point = std::complex<coord_t>;
int sgn(coord_t x) {
return (x > 0) - (x < 0);
coord_t dot(Point a, Point b) {
return real(conj(a) * b);
coord_t cross(Point a, Point b) {
return imag(conj(a) * b);
int ori(Point a, Point b, Point c) {
return sgn(cross(b - a, c - a));
bool operator<(const Point &a, const Point &b) {</pre>
return real(a) != real(b)
  ? real(a) < real(b) : imag(a) < imag(b);
int argCmp(Point a, Point b) {
// -1 / 0 / 1 <-> < / == / > (atan2)
int qa = (imag(a) == 0
   ? (real(a) < 0 ? 3 : 1) : (imag(a) < 0 ? 0 : 2));
int qb = (imag(b) == 0
   ? (real(b) < 0 ? 3 : 1) : (imag(b) < 0 ? 0 : 2));
if (qa != qb)
 return sgn(qa - qb);
 return sgn(cross(b, a));
template <typename V> Real area(const V & pt) {
coord_t ret = 0;
for (int i = 1; i + 1 < (int)pt.size(); i++)</pre>
 ret += cross(pt[i] - pt[0], pt[i+1] - pt[0]);
 return ret / 2.0;
```

6.2 2D Convex Hull

```
template<typename PT>
vector<PT> buildConvexHull(vector<PT> d) {
  sort(ALL(d), [](const PT& a, const PT& b){
    return tie(a.x, a.y) < tie(b.x, b.y);});
  vector<PT> s(SZ(d)<<1);
  int o = 0;
  for(auto p: d) {
    while(o>=2 && cross(p-s[o-2],s[o-1]-s[o-2])<=0)
    o--;</pre>
```

```
s[o++] = p;
 for(int i=SZ(d)-2, t = o+1; i>=0; i--){
  while(o = t\&cross(d[i] - s[o-2], s[o-1] - s[o-2]) <= 0)
   0--:
  s[o++] = d[i];
 s.resize(o-1);
 return s;
6.3
     3D Convex Hull
// return the faces with pt indexes
int flag[MXN][MXN];
struct Point{
 ld x,y,z;
 Point operator * (const 1d &b) const {
 return (Point){x*b,y*b,z*b};}
Point operator * (const Point &b) const {
  return(Point) {y*b.z-b.y*z,z*b.x-b.z*x,x*b.y-b.x*y};
 }
Point ver(Point a, Point b, Point c) {
return (b - a) * (c - a);}
vector<Face> convex_hull_3D(const vector<Point> pt) {
 int n = SZ(pt), ftop = 0;
 REP(i,n) REP(j,n) flag[i][j] = 0;
 vector<Face> now;
 now.emplace_back(0,1,2);
 now.emplace_back(2,1,0);
 for (int i=3; i<n; i++){
  ftop++; vector<Face> next;
  REP(j, SZ(now)) {
   Face& f=now[j]; int ff = 0;
ld d=(pt[i]-pt[f.a]).dot(
     ver(pt[f.a], pt[f.b], pt[f.c]));
   if (d <= 0) next.push_back(f);</pre>
   if (d > 0) ff=ftop;
   else if (d < 0) ff=-ftop;</pre>
   flag[f.a][f.b]=flag[f.b][f.c]=flag[f.c][f.a]=ff;
  REP(j, SZ(now)) {
Face& f=now[j];
   if (flag[f.a][f.b] > 0 &&
     flag[f.a][f.b] != flag[f.b][f.a])
    next.emplace_back(f.a,f.b,i);
   if (flag[f.b][f.c] > 0 &&
   flag[f.b][f.c] != flag[f.c][f.b])
    next.emplace_back(f.b,f.c,i);
   if (flag[f.c][f.a] > 0 &&
  flag[f.c][f.a] != flag[f.a][f.c])
    next.emplace_back(f.c,f.a,i);
  now=next;
 return now:
     2D Farthest Pair
// stk is from convex hull
n = (int)(stk.size());
int pos = 1, ans = 0; stk.push_back(stk[0]);
for(int i=0;i<n;i++) {</pre>
 while(abs(cross(stk[i+1]-stk[i],
   stk[(pos+1)%n]-stk[i])) >
   abs(cross(stk[i+1]-stk[i],
   stk[pos]-stk[i]))) pos = (pos+1)%n;
 ans = max({ans, dis(stk[i], stk[pos])},
  dis(stk[i+1], stk[pos])});
6.5 2D Closest Pair
struct cmp_y {
 bool operator()(const P& p, const P& q) const {
  return p.y < q.y;</pre>
 }
```

multiset<P, cmp_y> s;

void solve(P a[], int n) {

sort(a, a + n, [](const P& p, const P& q) {
 return tie(p.x, p.y) < tie(q.x, q.y);</pre>

Line (Point _s, Point _e)

```
: st(_s), ed(_e), dir(_e - _s) {}
11f d = INF; int pt = 0;
for (int i = 0; i < n; ++i) {
 while (pt < i and a[i].x - a[pt].x >= d)
                                                              bool operator<(const Line &lhs, const Line &rhs) {</pre>
  s.erase(s.find(a[pt++]));
                                                                if (int cmp = argCmp(lhs.dir, rhs.dir))
  auto it = s.lower_bound(P(a[i].x, a[i].y - d));
                                                                  return cmp == -1;
  while (it != s.end() and it->y - a[i].y < d)
                                                                return ori(lhs.st, lhs.ed, rhs.st) < 0;</pre>
  d = min(d, dis(*(it++), a[i]));
  s.insert(a[i]);
                                                              Point intersect(const Line &A, const Line &B) {
                                                                Real t = cross(B.st - A.st, B.dir) /
                                                                 cross(A.dir, B.dir);
                                                                return A.st + t * A.dir;
     kD Closest Pair (3D ver.)
                                                              }
11f solve(vector<P> v) {
                                                              Real HPI(vector<Line> &lines) {
shuffle(v.begin(), v.end(), mt19937());
unordered_map<lld, unordered_map<lld,</pre>
                                                                sort(lines.begin(), lines.end());
                                                                deque<Line> que;
  unordered_map<lld, int>>> m;
 11f d = dis(v[0], v[1]);
                                                                deque<Point> pt;
                                                                que.push_back(lines[0]);
auto Idx = [&d] (11f x) -> 11d {
                                                                for (int i = 1; i < (int)lines.size(); i++) {</pre>
 return round(x * 2 / d) + 0.1; };
                                                                  if (argCmp(lines[i].dir, lines[i-1].dir) == 0)
 auto rebuild_m = [&m, &v, &Idx](int k) {
                                                                   continue;
  m.clear();
                                                              #define POP(L, R) \
  for (int i = 0; i < k; ++i)
                                                                  while (pt.size() > 0 \
  m[Idx(v[i].x)][Idx(v[i].y)]
                                                                    && ori(L.st, L.ed, pt.back()) < 0) \
    [Idx(v[i].z)] = i;
                                                                  pt.pop_back(), que.pop_back(); \
while (pt.size() > 0 \
 }; rebuild_m(2);
 for (size_t i = 2; i < v.size(); ++i) {</pre>
                                                                    && ori(R.st, R.ed, pt.front()) < 0) \
 const lld kx = Idx(v[i].x), ky = Idx(v[i].y),
                                                                     pt.pop_front(), que.pop_front();
     kz = Idx(v[i].z); bool found = false;
                                                                  POP(lines[i], lines[i])
  for (int dx = -2; dx <= 2; ++dx) {
                                                                  pt.push_back(intersect(que.back(), lines[i]));
   const 11d nx = dx + kx
                                                                  que.push_back(lines[i]);
   if (m.find(nx) == m.end()) continue;
   auto& mm = m[nx];
                                                                POP(que.front(), que.back())
   for (int dy = -2; dy <= 2; ++dy) {
  const lld ny = dy + ky;</pre>
                                                                if (que.size() <= 1 ||</pre>
                                                                  argCmp(que.front().dir, que.back().dir) == 0)
    if (mm.find(ny) == mm.end()) continue;
                                                                  return 0:
    auto& mmm = mm[ny];
                                                                pt.push_back(intersect(que.front(), que.back()));
    for (int dz = -2; dz <= 2; ++dz) {
                                                                return area(pt);
     const 11d nz = dz + kz;
     if (mmm.find(nz) == mmm.end()) continue;
     const int p = mmm[nz];
                                                              6.9 Minkowski Sum
     if (dis(v[p], v[i]) < d) {</pre>
      d = dis(v[p], v[i]);
                                                              vector<pll> Minkowski(vector<pll> A, vector<pll> B) {
      found = true;
                                                               hull(A), hull(B);
                                                               vector<pll> C(1, A[0] + B[0]), s1, s2;
                                                               for(int i = 0; i < SZ(A); ++i)
                                                                s1.pb(A[(i + 1) % SZ(A)] - A[i]);
  }
                                                               for(int i = 0; i < SZ(B); i++)</pre>
  if (found) rebuild_m(i + 1);
                                                                s2.pb(B[(i + 1) % SZ(B)] - B[i]);
 else m[kx][ky][kz] = i;
                                                               for(int p1 = 0, p2 = 0; p1 < SZ(A) \mid \mid p2 < SZ(B);)
                                                                if (p2 >= SZ(B)
                                                                  || (p1 < SZ(A) \&\& cross(s1[p1], s2[p2]) >= 0))
return d;
                                                                 C.pb(C.back() + s1[p1++]);
6.7
      Simulated Annealing
                                                                 C.pb(C.back() + s2[p2++]);
                                                               return hull(C), C;
11f anneal() {
mt19937 rnd_engine( seed );
uniform_real_distribution< llf > rnd( 0, 1 );
                                                              6.10 Intersection of line and Circle
const llf dT = 0.001;
                                                              vector<pdd> line_interCircle(const pdd &p1,
 // Argument p
llf S_{cur} = calc(p), S_{best} = S_{cur};
for ( llf T = 2000 ; T > EPS ; T -= dT ) {
                                                                  const pdd &p2,const pdd &c,const double r){
                                                               pdd ft=foot(p1,p2,c),vec=p2-p1;
 // Modify p to p_prime
                                                               double dis=abs(c-ft);
 const llf S_prime = calc( p_prime );
                                                               if(fabs(dis-r)<eps) return vector<pdd>{ft};
 const llf delta_c = S_prime - S_cur;
llf prob = min( ( llf ) 1, exp( -delta_c / T ) );
                                                               if(dis>r) return {};
                                                               vec=vec*sqrt(r*r-dis*dis)/abs(vec);
  if ( rnd( rnd_engine ) <= prob )</pre>
                                                               return vector<pdd>{ft+vec,ft-vec};
   S_{cur} = S_{prime}, p = p_{prime};
 if ( S_prime < S_best ) // find min</pre>
                                                              6.11 Intersection of Polygon and Circle
   S_best = S_prime, p_best = p_prime;
                                                              // Divides into multiple triangle, and sum up
 return S_best;
                                                              // test by HDU2892
                                                              const double PI=acos(-1);
                                                              double _area(pdd pa, pdd pb, double r){
6.8 Half Plane Intersection
                                                               if(abs(pa)<abs(pb)) swap(pa, pb);</pre>
// NOTE: Point is complex<Real>
                                                               if(abs(pb)<eps) return 0;</pre>
// cross(pt-line.st, line.dir)<=0 <-> pt in half plane
                                                               double S, h, theta;
struct Line {
                                                               double a=abs(pb), b=abs(pa), c=abs(pb-pa);
 Point st, ed;
                                                               double cosB = dot(pb,pb-pa) / a / c, B = acos(cosB);
  Point dir
                                                               double cosC = dot(pa,pb) / a / b, C = acos(cosC);
```

if(a > r){

6.12 Intersection of Two Circle

6.13 Tangent line of Two Circle

```
vector<Line> go(const Cir& c1,
 const Cir& c2, int sign1){
 // sign1 = 1 for outer tang, -1 for inter tang
 vector<Line> ret;
double d_{sq} = norm2(c1.0 - c2.0);
if( d_sq < eps ) return ret;</pre>
double d = sqrt( d_sq );
Pt v = ( c2.0 - c1.0 ) / d;
for( int sign2 = 1 ; sign2 >= -1 ; sign2 -= 2 ){
  Pt n = { v.X * c - sign2 * h * v.Y ,
  v.Y * c + sign2 * h * v.X };
 Pt p1 = c1.0 + n * c1.R;
 Pt p2 = c2.0 + n * (c2.R * sign1);
 if( fabs( p1.X - p2.X ) < eps and</pre>
    fabs( p1.Y - p2.Y ) < eps )
  p2 = p1 + perp(c2.0 - c1.0);
  ret.push_back( { p1 , p2 } );
return ret;
```

6.14 Minimum Covering Circle

```
template<typename P>
Circle getCircum(const P &a, const P &b, const P &c){
  Real a1 = a.x-b.x, b1 = a.y-b.y;
  Real c1 = (a.x+b.x)/2 * a1 + (a.y+b.y)/2 * b1;
  Real a2 = a.x-c.x, b2 = a.y-c.y;
  Real c2 = (a.x+c.x)/2 * a2 + (a.y+c.y)/2 * b2;
  Circle cc;
  cc.o.x = (c1*b2-b1*c2)/(a1*b2-b1*a2);
  cc.o.y = (a1*c2-c1*a2)/(a1*b2-b1*a2);
  cc.r = hypot(cc.o.x-a.x, cc.o.y-a.y);
  return cc;
}

template<typename P>
Circle MinCircleCover(const vector<P>& pts){
  random_shuffle(pts.begin(), pts.end());
  Circle c = { pts[0], 0 };
}
```

```
for(int i=0;i<(int)pts.size();i++){</pre>
  if (dist(pts[i], c.o) <= c.r) continue;</pre>
  c = \{ pts[i], 0 \};
  for (int j = 0; j < i; j++) {
  if(dist(pts[j], c.o) <= c.r) continue;</pre>
   c.o = (pts[i] + pts[j]) / 2;
   c.r = dist(pts[i], c.o);
   for (int k = 0; k < j; k++) {
    if (dist(pts[k], c.o) <= c.r) continue;</pre>
    c = getCircum(pts[i], pts[j], pts[k]);
 return c;
      KDTree (Nearest Point)
6.15
const int MXN = 100005;
struct KDTree {
 struct Node {
  int x,y,x1,y1,x2,y2;
  int id,f;
  Node *L, *R;
 } tree[MXN], *root;
 LL dis2(int x1, int y1, int x2, int y2) {
LL dx = x1-x2, dy = y1-y2;
  return dx*dx+dy*dy;
 static bool cmpx(Node& a, Node& b){return a.x<b.x;}</pre>
 static bool cmpy(Node& a, Node& b){return a.y<b.y;}</pre>
 void init(vector<pair<int,int>> ip) {
  n = ip.size();
  for (int i=0; i<n; i++) {
   tree[i].id = i;
   tree[i].x = ip[i].first;
   tree[i].y = ip[i].second;
  root = build_tree(0, n-1, 0);
 Node* build_tree(int L, int R, int d) {
  if (L>R) return nullptr;
  int M = (L+R)/2; tree[M].f = d%2;
  nth_element(tree+L, tree+M, tree+R+1, d%2?cmpy:cmpx);
  tree[M].x1 = tree[M].x2 = tree[M].x;
  tree[M].y1 = tree[M].y2 = tree[M].y;
  tree[M].L = build_tree(L, M-1, d+1);
  if (tree[M].L) {
   tree[M].x1 = min(tree[M].x1, tree[M].L->x1);
   tree[M].x2 = max(tree[M].x2, tree[M].L->x2);
   tree[M].y1 = min(tree[M].y1, tree[M].L->y1);
tree[M].y2 = max(tree[M].y2, tree[M].L->y2);
  tree[M].R = build_tree(M+1, R, d+1);
  if (tree[M].R) {
   tree[M].x1 = min(tree[M].x1, tree[M].R->x1);
   tree[M].x2 = max(tree[M].x2, tree[M].R->x2);
   tree[M].y1 = min(tree[M].y1, tree[M].R->y1);
tree[M].y2 = max(tree[M].y2, tree[M].R->y2);
  return tree+M;
 int touch(Node* r, int x, int y, LL d2){
  LL dis = sqrt(d2)+1;
  if (x<r->x1-dis || x>r->x2+dis ||
    y<r->y1-dis || y>r->y2+dis)
   return 0;
  return 1;
 void nearest(Node* r,int x,int y,int &mID,LL &md2) {
  if (!r || !touch(r, x, y, md2)) return;
  LL d2 = dis2(r\rightarrow x, r\rightarrow y, x, y)
  if (d2 < md2 \mid | (d2 == md2 \&\& mID < r->id)) {
   mID = r -> id;
   md2 = d2:
  // search order depends on split dim
  if ((r->f == 0 && x < r->x) ||
    (r->f == 1 && y < r->y)) {
   nearest(r\rightarrow L, x, y, mID, md2);
   nearest(r->R, x, y, mID, md2);
  } else {
```

if (sa[i] && t[sa[i] - 1])

```
nearest(r->R, x, y, mID, md2);
                                                                      sa[--x[s[sa[i] - 1]]] = sa[i] - 1;
   nearest(r->L, x, y, mID, md2);
                                                                  void sais(int *s, int *sa, int *p, int *q,
  }
                                                                   bool *t, int *c, int n, int z) {
bool uniq = t[n - 1] = true;
 int query(int x, int y) {
  int id = 1029384756;
                                                                    int nn=0, nmxz=-1, *nsa = sa+n, *ns=s+n, last=-1;
  LL d2 = 102938475612345678LL;
                                                                    memset(c, 0, sizeof(int) * z);
                                                                    for (int i = 0; i < n; ++i) uniq &= ++c[s[i]] < 2;
  nearest(root, x, y, id, d2);
                                                                    for (int i = 0; i < z - 1; ++i) c[i + 1] += c[i];
  return id;
 }
                                                                    if (uniq) -
} tree;
                                                                    for (int i = 0; i < n; ++i) sa[--c[s[i]]] = i;
                                                                     return:
6.16 Rotating Sweep Line
                                                                    for (int i = n - 2; i \ge 0; --i)
void rotatingSweepLine(pair<int, int> a[], int n) {
                                                                    t[i] = (s[i] = s[i + 1] ? t[i + 1] : s[i] < s[i + 1]);
 vector<pair<int, int>> 1;
1.reserve(n * (n - 1) / 2);
                                                                    pre(sa, c, n, z);
                                                                    for (int i = 1; i <= n - 1; ++i)
  for (int i = 0; i < n; ++i)

for (int j = i + 1; j < n; ++j)
                                                                     if (t[i] && !t[i - 1])
                                                                      sa[--x[s[i]]] = p[q[i] = nn++] = i;
  \label{lemplace_back} $1.$ emplace_back(i, j); $$ sort(1.begin(), 1.end(), [\&a](auto \&u, auto \&v){} $$
                                                                    induce(sa, c, s, t, n, z);
for (int i = 0; i < n; ++i) {
    1ld udx = a[u.first].first - a[u.second].first;
                                                                     if (sa[i] && t[sa[i]] && !t[sa[i] - 1]) {
    11d udy = a[u.first].second - a[u.second].second;
                                                                     bool neq = last < 0 ||</pre>
    1ld vdx = a[v.first].first - a[v.second].first;
                                                                      memcmp(s + sa[i], s + last
    11d vdy = a[v.first].second - a[v.second].second;
                                                                      (p[q[sa[i]] + 1] - sa[i]) * sizeof(int));
    if (udx == 0 or vdx == 0) return not udx == 0;
                                                                     ns[q[last = sa[i]]] = nmxz += neq;
    int s = sgn(udx * vdx);
                                                                    }}
    return udy * vdx * s < vdy * udx * s;
                                                                    sais(ns, nsa, p+nn, q+n, t+n, c+z, nn, nmxz+1);
                                                                    pre(sa, c, n, z);
for (int i = nn - 1; i >= 0; --i)
  vector<int> idx(n), p(n);
 iota(idx.begin(), idx.end(), 0);
sort(idx.begin(), idx.end(), [&a](int i, int j){
  return a[i] < a[j]; });</pre>
                                                                     sa[--x[s[p[nsa[i]]]]] = p[nsa[i]];
                                                                    induce(sa, c, s, t, n, z);
  for (int i = 0; i < n; ++i) p[idx[i]] = i;</pre>
                                                                  void build(const string &s) {
  for (auto [i, j]: 1) {
                                                                   for (int i = 0; i < (int)s.size(); ++i) _s[i] = s[i];
    // do here
                                                                    _s[(int)s.size()] = 0; // s shouldn't contain 0
    swap(p[i], p[j]);
                                                                   sais(_s, sa, p, q, t, c, (int)s.size() + 1, 256);
for(int i = 0; i < (int)s.size(); ++i) sa[i]=sa[i+1];
for(int i = 0; i < (int)s.size(); ++i) rev[sa[i]]=i;</pre>
    idx[p[i]] = i, idx[p[j]] = j;
                                                                    int ind = 0; hi[0] = 0;
                                                                    for (int i = 0; i < (int)s.size(); ++i) {
  if (!rev[i]) {</pre>
7
     Stringology
                                                                      ind = 0;
7.1 Hash
                                                                      continue:
class Hash {
 private:
                                                                     while (i + ind < (int)s.size() && \</pre>
  static constexpr int P = 127, Q = 1051762951;
                                                                      s[i + ind] == s[sa[rev[i] - 1] + ind]) ++ind;
  vector<int> h, p;
                                                                     hi[rev[i]] = ind ? ind-- : 0;
  void init(const string &s){
                                                                  }}
   h.assign(s.size()+1, 0); p.resize(s.size()+1);
                                                                   7.3 Suffix Automaton
   for (size_t i = 0; i < s.size(); ++i)</pre>
    h[i + 1] = add(mul(h[i], P), s[i]);
                                                                  struct Node{
   generate(p.begin(), p.end(),[x=1,y=1,this]()
                                                                    Node *green, *edge[26];
     mutable{y=x;x=mul(x,P);return y;});
                                                                    int max_len;
                                                                    Node(const int _max_len)
  int query(int 1, int r){ // 1-base (1, r]
                                                                     : green(NULL), max_len(_max_len){
   return sub(h[r], mul(h[1], p[r-1]));}
                                                                     memset(edge,0,sizeof(edge));
                                                                   } *ROOT, *LAST;
7.2 Suffix Array
                                                                   void Extend(const int c) {
                                                                    Node *cursor = LAST;
namespace sfxarray {
                                                                    LAST = new Node((LAST->max_len) + 1);
bool t[maxn * 2];
int hi[maxn], rev[maxn];
int _s[maxn * 2], sa[maxn * 2], c[maxn * 2];
                                                                    for(;cursor&&!cursor->edge[c]; cursor=cursor->green)
                                                                     cursor->edge[c] = LAST;
int x[maxn], p[maxn], q[maxn * 2];
                                                                    if (!cursor)
// sa[i]: sa[i]-th suffix is the \
                                                                    LAST->green = ROOT;
// i-th lexigraphically smallest suffix.
// hi[i]: longest common prefix \
                                                                     Node *potential_green = cursor->edge[c];
// of suffix sa[i] and suffix sa[i - 1].
                                                                     if((potential_green->max_len)==(cursor->max_len+1))
void pre(int *sa, int *c, int n, int z) {
  memset(sa, 0, sizeof(int) * n);
                                                                      LAST->green = potential_green;
                                                                     else {
 memcpy(x, c, sizeof(int) * z);
                                                                   //assert(potential_green->max_len>(cursor->max_len+1));
                                                                      Node *wish = new Node((cursor->max_len) + 1);
void induce(int *sa,int *c,int *s,bool *t,int n,int z){
                                                                      for(;cursor && cursor->edge[c]==potential_green;
memcpy(x + 1, c, sizeof(int) * (z - 1));
for (int i = 0; i < n; ++i)
if (sa[i] && !t[sa[i] - 1])
                                                                         cursor = cursor->green)
                                                                       cursor->edge[c] = wish;
                                                                      for (int i = 0; i < 26; i++)
   sa[x[s[sa[i] - 1]]++] = sa[i] - 1;
                                                                       wish->edge[i] = potential_green->edge[i];
 memcpy(x, c, sizeof(int) * z);
for (int i = n - 1; i >= 0; --i)
                                                                      wish->green = potential_green->green;
                                                                      potential_green->green = wish;
```

LAST->green = wish;

```
for(int i=1;i<t.length();++i) ans = max(ans, z[i]-1);</pre>
}
                                                                 return ans:
char S[10000001], A[10000001];
                                                               7.7 Lexico Smallest Rotation
int N:
int main(){
                                                               string mcp(string s){
scanf("%d%s", &N, S);
ROOT = LAST = new Node(0);
                                                                int n = s.length();
                                                                 s += s:
for (int i = 0; S[i]; i++)
Extend(S[i] - 'a');
                                                                 int i=0, j=1;
                                                                while (i<n && j<n){</pre>
while (N--){
                                                                  int k = 0;
  scanf("%s", A);
                                                                  while (k < n \&\& s[i+k] == s[j+k]) k++;
 Node *cursor = ROOT;
                                                                 if (s[i+k] <= s[j+k]) j += k+1;</pre>
  bool ans = true;
                                                                 else i += k+1;
 for (int i = 0; A[i]; i++){
                                                                 if (i == j) j++;
   cursor = cursor->edge[A[i] - 'a'];
   if (!cursor) {
                                                                 int ans = i < n ? i : j;</pre>
   ans = false;
                                                                 return s.substr(ans, n);
   break;
   }
                                                               7.8 BWT
 puts(ans ? "Yes" : "No");
                                                               struct BurrowsWheeler{
                                                               #define SIGMA 26
return 0:
                                                               #define BASE 'a'
                                                                vector<int> v[ SIGMA ];
                                                                 void BWT(char* ori, char* res){
7.4 KMP
                                                                  // make ori -> ori + ori
vector<int> kmp(const string &s) {
                                                                  // then build suffix array
vector<int> f(s.size(), 0);
 /* f[i] = length of the longest prefix
                                                                 void iBWT(char* ori, char* res){
   (excluding s[0:i]) such that it coincides with the suffix of s[0:i] of the same length */
                                                                 for( int i = 0 ; i < SIGMA ; i ++ )</pre>
                                                                   v[ i ].clear();
 /* i + 1 - f[i] is the length of the
                                                                  int len = strlen( ori );
   smallest recurring period of s[0:i] */
                                                                  for( int i = 0 ; i < len ; i ++ )</pre>
 int k = 0:
                                                                   v[ ori[i] - BASE ].push_back( i );
for (int i = 1; i < (int)s.size(); ++i) {</pre>
                                                                  vector<int> a:
 while (k > 0 \&\& s[i] != s[k]) k = f[k - 1];
                                                                  for( int i = 0 , ptr = 0 ; i < SIGMA ; i ++ )</pre>
  if (s[i] == s[k]) ++k;
                                                                   for( auto j : v[ i ] ){
 f[i] = k;
                                                                    a.push_back( j );
ori[ ptr ++ ] = BASE + i;
return f;
                                                                 for( int i = 0 , ptr = 0 ; i < len ; i ++ ){
  res[ i ] = ori[ a[ ptr ] ];</pre>
vector<int> search(const string &s, const string &t) {
 // return 0-indexed occurrence of t in s
                                                                   ptr = a[ ptr ];
vector<int> f = kmp(t), r
                                                                  }
for (int i = 0, k = 0; i < (int)s.size(); ++i) {</pre>
                                                                  res[ len ] = 0;
 while(k > 0 && (k==(int)t.size() \mid \mid s[i]!=t[k]))
  k = f[k - 1];
                                                               } bwt;
  if (s[i] == t[k]) ++k;
 if (k == (int)t.size()) r.push_back(i-t.size()+1);
                                                                7.9
                                                                     Palindromic Tree
                                                               struct palindromic_tree{
return res;
                                                                 struct node{
                                                                  int next[26],f,len;
                                                                  int cnt, num, st, ed;
7.5 Z value
                                                                 node(int l=0):f(0),len(1),cnt(0),num(0) {
char s[MAXN];
                                                                   memset(next, 0, sizeof(next)); }
int len,z[MAXN];
void Z_value() {
                                                                 vector<node> st;
int i,j,left,right;
                                                                 vector<char> s;
z[left=right=0]=len;
                                                                 int last n
for(i=1;i<len;i++)</pre>
                                                                 void init(){
  j=max(min(z[i-left], right-i),0);
                                                                 st.clear();s.clear();last=1; n=0;
  for(;i+j<len&&s[i+j]==s[j];j++);
                                                                  st.push_back(0);st.push_back(-1);
  if(i+(z[i]=j)>right)right=i+z[left=i];
                                                                  st[0].f=1;s.push_back(-1); }
                                                                 int getFail(int x){
                                                                  while(s[n-st[x].len-1]!=s[n])x=st[x].f;
                                                                  return x;}
7.6 Manacher
                                                                 void add(int c){
                                                                  s.push_back(c-='a'); ++n;
int z[maxn]:
int manacher(const string& s) {
  string t = ".";
                                                                  int cur=getFail(last);
                                                                  if(!st[cur].next[c]){
 for(char c: s) t += c, t += '.';
                                                                   int now=st.size();
 int 1 = 0, r = 0, ans = 0;
                                                                   st.push_back(st[cur].len+2);
for (int i = 1; i < t.length(); ++i) {
z[i] = (r > i ? min(z[2 * 1 - i], r - i) : 1);
                                                                   st[now].f=st[getFail(st[cur].f)].next[c];
                                                                   st[cur].next[c]=now;
 while (i - z[i] \ge 0 \&\& i + z[i] < t.length()) {
                                                                   st[now].num=st[st[now].f].num+1;
  if(t[i - z[i]] == t[i + z[i]]) ++z[i];
   else break;
                                                                  last=st[cur].next[c];
                                                                 ++st[last].cnt;}
  if (i + z[i] > r) r = i + z[i], l = i;
                                                                 void dpcnt() {
                                                                 for (int i=st.size()-1; i >= 0; i--)
```

```
st[st[i].f].cnt += st[i].cnt;
}
int size(){ return st.size()-2;}
} pt;
int main() {
    string s; cin >> s; pt.init();
    for (int i=0; i<SZ(s); i++) {
        int prvsz = pt.size(); pt.add(s[i]);
        if (prvsz != pt.size()) {
            int r = i, l = r - pt.st[pt.last].len + 1;
        // pal @ [l,r]: s.substr(l, r-l+1)
        }
    return 0;
}</pre>
```

8 Misc

8.1 Theorems

8.1.1 Kirchhoff's Theorem

Denote L be a $n\times n$ matrix as the Laplacian matrix of graph G, where $L_{ii}=d(i)$, $L_{ij}=-c$ where c is the number of edge (i,j) in G.

- The number of undirected spanning in G is $|\det(\tilde{L}_{11})|$.
- The number of directed spanning tree rooted at r in G is $|{\rm det}(\tilde{L}_{rr})|.$

8.1.2 Tutte's Matrix

Let D be a $n \times n$ matrix, where $d_{ij}=x_{ij}$ (x_{ij} is chosen uniform randomly) if i < j and $(i,j) \in E$, otherwise $d_{ij}=-d_{ji}.$ $\frac{rank(D)}{2}$ is the maximum matching an C

8.1.3 Cayley's Formula

- Given a degree sequence d_1,d_2,\dots,d_n for each labeled vertices, there're $\frac{(n-2)!}{(d_1-1)!(d_2-1)!\cdots(d_n-1)!}$ spanning trees.
- Let $T_{n,k}$ be the number of labeled forests on n vertices with k components, such that vertex $1,2,\ldots,k$ belong to different components. Then $T_{n,k}=kn^{n-k-1}$.

8.1.4 Erdős-Gallai theorem

A sequence of non-negative integers $d_1 \geq d_2 \geq \ldots \geq d_n$ can be represented as the degree sequence of a finite simple graph on n vertices if and only if $d_1 + d_2 + \ldots + d_n$ is even and

$$\sum_{i=1}^{k} d_i \le k(k-1) + \sum_{i=k+1}^{n} \min(d_i, k)$$

holds for all $1 \le k \le n$.

8.1.5 Havel-Hakimi algorithm

find the vertex who has greatest degree unused, connect it with other greatest vertex.

8.1.6 Hall's marriage theorem

Let G be a finite bipartite graph with bipartite sets X and Y. For a subset W of X, let $N_G(W)$ denote the set of all vertices in Y adjacent to some element of W. Then there is an X-saturating matching iff $\forall W \subseteq X, |W| \leq |N_G(W)|$

8.1.7 Euler's planar graph formula

$$V - E + F = C + 1$$
, $E \le 3V - 6$ (?)

8.1.8 Pick's theorem

For simple polygon, when points are all integer, we have $A=\#\{\text{lattice points in the interior}\}+\frac{\#\{\text{lattice points on the boundary}\}}{2}-1$

8.1.9 Lucas's theorem

 ${m\choose n}\equiv\prod_{i=0}^k{m_i\choose n_i}\pmod{p}, \text{ where } m=m_kp^k+m_{k-1}p^{k-1}+\cdots+m_1p+m_0,$ and $n=n_kp^k+n_{k-1}p^{k-1}+\cdots+n_1p+n_0.$

8.1.10 Matroid Intersection

Given matroids $M_1=(G,I_1),M_2=(G,I_2)$, find maximum $S\in I_1\cap I_2$. For each iteration, build the directed graph and find a shortest path from s to t.

- $s \to x : S \sqcup \{x\} \in I_1$
- $x \to t : S \sqcup \{x\} \in I_2$
- $y \to x: S \setminus \{y\} \sqcup \{x\} \in I_1$ (y is in the unique circuit of $S \sqcup \{x\}$)
- $x \to y : S \setminus \{y\} \sqcup \{x\} \in I_2$ (y is in the unique circuit of $S \sqcup \{x\}$)

Alternate the path, and |S| will increase by 1. Let $R=\min(\mathrm{rank}(I_1),\mathrm{rank}(I_2)),N=|G|.$ In each iteration, |E|=O(RN). For weighted case, assign weight -w(x) and w(x) to $x\in S$ and $x\notin S$, resp. Use Bellman-Ford to find the weighted shortest path. The maximum iteration of Bellman-Ford is 2R+1.

8.2 DP-opt Condition

8.2.1 totally monotone (concave/convex)

```
\begin{array}{l} \forall i < i', j < j', B[i][j] \leq B[i'][j] \implies B[i][j'] \leq B[i'][j'] \\ \forall i < i', j < j', B[i][j] \geq B[i'][j] \implies B[i][j'] \geq B[i'][j'] \end{array}
```

8.2.2 monge condition (concave/convex)

```
\begin{array}{l} \forall i < i', j < j', B[i][j] + B[i'][j'] \geq B[i][j'] + B[i'][j] \\ \forall i < i', j < j', B[i][j] + B[i'][j'] \leq B[i][j'] + B[i'][j] \end{array}
```

8.3 Convex 1D/1D DP

```
struct segment {
int i, 1, r;
 segment() {}
 segment(int a, int b, int c): i(a), l(b), r(c) {}
inline 1ld f(int 1, int r){return dp[1] + w(1+1, r);}
void solve() {
 dp[0] = 0;
 deque<segment> dq; dq.push_back(segment(0, 1, n));
 for (int i = 1; i <= n; ++i) {
  dp[i] = f(dq.front().i, i);
  while(dq.size()&&dq.front().r<i+1) dq.pop_front();</pre>
  dq.front().l = i + 1;
  segment seg = segment(i, i + 1, n);
  while (dq.size() &&
   f(i, dq.back().1) < f(dq.back().i, dq.back().1))
    dq.pop_back();
  if (dq.size())
   int d = 1 << 20, c = dq.back().1;
while (d >>= 1) if (c + d <= dq.back().r)
    if(f(i, c+d) > f(dq.back().i, c+d)) c += d;
   dq.back().r = c; seg.l = c + 1;
  if (seg.1 <= n) dq.push_back(seg);</pre>
}
```

8.4 ConvexHull Optimization

```
struct Line {
 mutable int64_t a, b, p;
 bool operator<(const Line &rhs) const { return a < rhs
    .a; }
 bool operator<(int64_t x) const { return p < x; }</pre>
}:
struct DynamicHull : multiset<Line, less<>> {
 static const int64_t kInf = 1e18;
 bool Isect(iterator x, iterator y)
  auto Div = [](int64_t a, int64_t b) {
    return a / b - ((a ^ b) < 0 && a % b); }
  if (y == end()) { x->p = kInf; return false; }
if (x->a == y->a) x->p = x->b > y->b ? kInf : -kInf;
  else x->p = Div(y->b - x->b, x->a - y->a);
  return x->p >= y->p;
 void Insert(int64_t a, int64_t b) {
  auto z = insert({a, b, 0}), y = z++, x = y;
  while (Isect(y, z)) z = erase(z);
  if (x != begin() \&\& Isect(--x, y)) Isect(x, y = erase)
    (y));
  while ((y = x) != begin() && (--x)->p >= y->p) Isect(
    x, erase(y));
 int64_t Query(int64_t x) {
  auto 1 = *lower_bound(x);
  return 1.a * x + 1.b;
```

3.5 Josephus Problem

```
// n people kill m for each turn
int f(int n, int m) {
  int s = 0;
  for (int i = 2; i <= n; i++)
    s = (s + m) % i;
  return s;
}</pre>
```

```
// died at kth
                                                                  tmp[1][1]=min_dp[1][0]+dp[v][0]+1;
int kth(int n, int m, int k){
                                                                  memcpy(min_dp,tmp,sizeof tmp);
if (m == 1) return n-1;
for (k = k*m+m-1; k >= n; k = k-n+(k-n)/(m-1));
                                                                 dp[u][1]=max(min_dp[0][1],min_dp[1][0]);
                                                                 dp[u][0]=min_dp[0][0];
return k:
8.6 Cactus Matching
                                                               int main(){
                                                                int m,a,b;
vector<int> init_g[maxn],g[maxn*2];
                                                                scanf("%d%d",&n,&m);
for(int i=0;i<m;i++){
int n,dfn[maxn],low[maxn],par[maxn],dfs_idx,bcc_id;
void tarjan(int u)
dfn[u]=low[u]=++dfs_idx;
                                                                 scanf("%d%d",&a,&b);
                                                                 init_g[a].push_back(b);
for(int i=0;i<(int)init_g[u].size();i++){</pre>
  int v=init_g[u][i];
                                                                 init_g[b].push_back(a);
  if(v==par[u]) continue;
  if(!dfn[v]){
                                                                par[1]=-1;
                                                                tarjan(1);
   par[v]=u;
                                                                dfs(1,-1);
   tarjan(v);
                                                                printf("%d\n", max(dp[1][0], dp[1][1]));
   low[u]=min(low[u],low[v]);
   if(dfn[u]<low[v]){</pre>
                                                                return 0:
    g[u].push_back(v);
    g[v].push_back(u);
                                                               8.7 DLX
  }else{
                                                               struct DLX {
   low[u]=min(low[u],dfn[v]);
                                                                const static int maxn=210;
   if(dfn[v]<dfn[u]){</pre>
                                                                const static int maxm=210;
                                                                const static int maxnode=210*210;
    int temp_v=u;
    bcc_id++;
                                                                int n, m, size, row[maxnode], col[maxnode];
                                                                int U[maxnode], D[maxnode], L[maxnode], R[maxnode];
int H[maxn], S[maxm], ansd, ans[maxn];
    while(temp_v!=v){
     g[bcc_id+n].push_back(temp_v);
     g[temp_v].push_back(bcc_id+n);
                                                                void init(int _n, int _m) {
     temp_v=par[temp_v];
                                                                 n = _n, m = _m;
                                                                 for(int i = 0; i <= m; ++i) {</pre>
    g[bcc_id+n].push_back(v);
                                                                  S[i] = 0;
    g[v].push_back(bcc_id+n);
                                                                  U[i] = D[i] = i;
    reverse(g[bcc_id+n].begin(),g[bcc_id+n].end());
                                                                  L[i] = i-1, R[i] = i+1;
                                                                 R[L[0] = size = m] = 0;
                                                                 for(int i = 1; i <= n; ++i) H[i] = -1;
int dp[maxn][2], min_dp[2][2], tmp[2][2], tp[2];
                                                                void Link(int r, int c) {
void dfs(int u,int fa){
                                                                 ++S[col[++size] = c];
                                                                 row[size] = r; D[size] = D[c];
 if(u<=n){
                                                                 U[D[c]] = size; U[size] = c; D[c] = size;
if(H[r] < 0) H[r] = L[size] = R[size] = size;</pre>
  for(int i=0;i<(int)g[u].size();i++){</pre>
   int v=g[u][i];
                                                                 else {
   if(v==fa) continue;
   dfs(v,u);
                                                                  R[size] = R[H[r]];
   memset(tp,0x8f,sizeof tp);
                                                                  L[R[H[r]]] = size;
   if(v<=n){
                                                                  L[size] = H[r];
                                                                  R[H[r]] = size;
    tp[0]=dp[u][0]+max(dp[v][0],dp[v][1]);
    tp[1]=max(
                                                                 }
     dp[u][0]+dp[v][0]+1
     dp[u][1]+max(dp[v][0],dp[v][1])
                                                                void remove(int c) {
                                                                 L[R[c]] = L[c]; R[L[c]] = R[c];
                                                                 for(int i = D[c]; i != c; i = D[i])
for(int j = R[i]; j != i; j = R[j]) {
   }else{
    tp[0]=dp[u][0]+dp[v][0];
                                                                   U[D[j]] = U[j];
    tp[1]=max(dp[u][0]+dp[v][1],dp[u][1]+dp[v][0]);
                                                                   D[U[j]] = D[j];
   dp[u][0]=tp[0],dp[u][1]=tp[1];
                                                                   --S[col[j]];
                                                                  }
 }else{
  for(int i=0;i<(int)g[u].size();i++){</pre>
                                                                void resume(int c) {
                                                                 L[R[c]] = c; R[L[c]] = c;
   int v=g[u][i];
   if(v==fa) continue;
                                                                 for(int i = U[c]; i != c; i = U[i])
   dfs(v,u);
                                                                  for(int j = L[i]; j != i; j = L[j]) {
  }
                                                                   U[D[j]] = j;
  min_dp[0][0]=0;
                                                                   D[U[j]] = j
  min_dp[1][1]=1;
                                                                   ++S[col[j]];
  min_dp[0][1]=min_dp[1][0]=-0x3f3f3f3f;
  for(int i=0;i<(int)g[u].size();i++){</pre>
   int v=g[u][i];
                                                                void dance(int d) {
                                                                 if(d>=ansd) return;
   if(v==fa) continue;
   memset(tmp,0x8f,sizeof tmp);
                                                                 if(R[0] == 0) {
   tmp[0][0]=max(
                                                                  ansd = d;
   min_dp[0][0]+max(dp[v][0],dp[v][1]),
                                                                  return;
    min_dp[0][1]+dp[v][0]
                                                                 int c = R[0];
                                                                 for(int i = R[0]; i; i = R[i])
   tmp[0][1]=min_dp[0][0]+dp[v][0]+1;
   tmp[1][0]=max(
                                                                  if(S[i] < S[c]) c = i;
   min_dp[1][0]+max(dp[v][0],dp[v][1]),
                                                                 remove(c);
    min_dp[1][1]+dp[v][0]
                                                                 for(int i = D[c]; i != c; i = D[i]) {
                                                                  ans[d] = row[i];
```

```
for(int j = R[i]; j != i; j = R[j])
    remove(col[j]);
    dance(d+1);
    for(int j = L[i]; j != i; j = L[j])
     resume(col[j]);
}
    resume(c);
}
sol;
```

8.8 Tree Knapsack

```
int dp[N][K];PII obj[N];
vector<int> G[N];
void dfs(int u, int mx){
for(int s: G[u]) {
  if(mx < obj[s].first) continue;</pre>
  for(int i=0;i<=mx-obj[s].FF;i++)</pre>
  dp[s][i] = dp[u][i];
  dfs(s, mx - obj[s].first);
  for(int i=obj[s].FF;i<=mx;i++)</pre>
  dp[u][i] = max(dp[u][i],
    dp[s][i - obj[s].FF] + obj[s].SS);
int main(){
int n, k; cin >> n >> k:
for(int i=1;i<=n;i++){</pre>
 int p; cin >> p;
 G[p].push_back(i);
 cin >> obj[i].FF >> obj[i].SS;
dfs(0, k); int ans = 0;
for(int i=0;i<=k;i++) ans = max(ans, dp[0][i]);
cout << ans << '\n':
return 0;
```

8.9 N Queens Problem

```
vector< int > solve( int n ) {
 // no solution when n=2, 3
vector< int > ret;
if ( n % 6 == 2 ) {
  for ( int i = 2 ; i <= n ; i += 2 )
    ret.push_back( i );</pre>
  ret.push_back( 3 ); ret.push_back( 1 );
 for ( int i = 7 ; i <= n ; i += 2 )
  ret.push_back( i );</pre>
  ret.push_back( 5 );
 } else if ( n % 6 == 3 ) {
  for ( int i = 4 ; i <= n ; i += 2 )
  ret.push_back( i );
  ret.push_back( 2 );
  for ( int i = 5 ; i <= n ; i += 2 )
  ret.push_back( i );
  ret.push_back( 1 ); ret.push_back( 3 );
 } else {
 for ( int i = 2 ; i <= n ; i += 2 )
  ret.push_back( i );
  for ( int i = 1 ; i <= n ; i += 2 )
  ret.push_back( i );
return ret;
```

8.10 Aliens Optimization

```
long long Alien() {
  long long c = kInf;
  for (int d = 60; d >= 0; --d) {
    // cost can be negative, depending on the problem.
    if (c - (1LL << d) < 0) continue;
    long long ck = c - (1LL << d);
    pair<long long, int> r = check(ck);
    if (r.second == k) return r.first - ck * k;
    if (r.second < k) c = ck;
}
pair<long long, int> r = check(c);
return r.first - c * k;
}
```

8.11 Hilbert Curve

```
long long hilbert(int n, int x, int y) {
  long long res = 0;
  for (int s = n / 2; s; s >>= 1) {
    int rx = (x & s) > 0, ry = (y & s) > 0;
    res += s * 1ll * s * ((3 * rx) ^ ry);
    if (ry == 0) {
        if (rx == 1) x = s - 1 - x, y = s - 1 - y;
        swap(x, y);
    }
  }
  return res;
}
```

8.12 Binary Search On Fraction

```
struct Q {
11 p, q;
 Q go(Q b, 11 d) { return {p + b.p*d, q + b.q*d}; }
bool pred(Q);
// returns smallest p/q in [lo, hi] such that
// pred(p/q) is true, and 0 \le p,q \le N
Q frac_bs(ll N) {
 Q lo{0, 1}, hi{1, 0};
 if (pred(lo)) return lo;
 assert(pred(hi));
 bool dir = 1, L = 1, H = 1;
 for (; L || H; dir = !dir) {
  11 len = 0, step = 1;
  for (int t = 0; t < 2 && (t ? step/=2 : step*=2);)</pre>
   if (Q mid = hi.go(lo, len + step);
     mid.p > N || mid.q > N || dir ^ pred(mid))
    t++:
   else len += step;
  swap(lo, hi = hi.go(lo, len));
  (dir ? L : H) = !!len;
 return dir ? hi : lo;
```