

Contents

1 Basic	
1.1 Default Code	1
1.2 IncreaseStackSize	1
1.3 Pragma optimization	1
1.4 Debugger	2
1.5 Quick Random	2
1.6 IO Optimization	2
2 Data Structure	
2.1 Bigint	2
2.2 ScientificNotation	2
2.3 unordered_map	3
2.4 extc_balance_tree	3
2.5 extc_heap	4
2.6 SkewHeap	4
2.7 Disjoint Set	4
2.8 Treap	5
2.9 SparseTable	5
2.10 FenwickTree	5
3 Graph	
3.1 BCC Edge	6
3.2 BCC Vertex	6
3.3 Strongly Connected Components	6
3.4 Bipartite Matching	7
3.5 MinimumCostMaximumFlow	7
3.6 MaximumFlow	7
3.7 Kuhn Munkres	7
4 Math	
4.1 Prime Table	8
4.2 ax+by=gcd	8
4.3 Pollard Rho	8
4.4 Linear Sieve	9
4.5 NloglogN Sieve	9
4.6 Range Sieve	9
4.7 Miller Rabin	9
4.8 Inverse Element	10
4.9 Euler Phi Function	10
4.10 Gauss Elimination	10
4.11 Fast Fourier Transform	10
4.12 Chinese Remainder	11
4.13 NTT	11
5 Geometry	
5.1 Point Class	11
5.2 Circle Class	11
5.3 Line Class	12
5.4 Segment Class	12
5.5 Triangle Circumcentre	13
5.6 2D Convex Hull	13
5.7 2D Farthest Pair	13
5.8 SimulateAnnealing	13
5.9 Minimum Covering Circle	14
5.10 KDTree (Nearest Point)	14
6 Stringology	
6.1 Hash	14
6.2 Suffix Array	15
6.3 KMP	15
6.4 Z value	15
6.5 Lexicographically Smallest Rotation	15

1 Basic

1.1 Default Code

```

1 #include <bits/stdc++.h>
1 using namespace std;
2 typedef int64_t lld;
2 typedef uint64_t llu;
2 typedef long double llf;
2 typedef pair<int,int> PII;
3 typedef pair<int,lld> PIL;
4 typedef pair<lld,int> PLI;
4 typedef pair<lld,lll> PLL;
4 template<typename T>
4 using maxHeap = priority_queue<T,vector<T>,less<T>>;
4 template<typename T>
5 using minHeap = priority_queue<T,vector<T>,greater<T>>;
5 #define FF first
5 #define SS second
6 #define SZ(x) ((int)((x).size()))
6 #define ALL(x) begin(x), end(x)
6 #define PB push_back
7 #define WC(x) while((x)-->0)
7 template<typename Iter>
7 ostream& _out(ostream& s, Iter b, Iter e) {
8     s<<"[";
8     for ( auto it=b; it!=e; it++ ) s<<(it==b?" ":" ")<<*
8         it;
8     s<<"]";
9     return s;
9 }
9 template<typename A, typename B>
9 ostream& operator <<( ostream& s, const pair<A,B> &p )
9 { return s<<"("<<p.FF<<" "<<p.SS<<")"; }
10 template<typename T>
10 ostream& operator <<( ostream& s, const vector<T> &c )
10 { return _out(s,ALL(c)); }
10 bool debug = 0;
11 #define DUMP(x) if(debug) cerr<<__PRETTY_FUNCTION__<<":
11     "<<__LINE__<<" - "<<(#x)<<"="<<(x)<<'\n'
11 template<typename T>
11 void DEBUG(const T& x){if(debug) cerr<<x;}
12 template<typename T, typename... Args>
12 void DEBUG(const T& head,const Args& ...tail){
13     if(debug){cerr<<head; DEBUG(tail...);}
13 }
13 int main(int argc, char* argv[]){
14     if(argc>1 and string(argv[1])=="-D") debug=1;
14     if(!debug){ios_base::sync_with_stdio(0);cin.tie(0)}
14     ;}
14     return 0;
14 }

```

1.2 IncreaseStackSize

```

//stack resize
asm( "mov %0,%esp\n" ::"g"(mem+10000000) );
//change esp to rsp if 64-bit system

//stack resize (linux)
#include <sys/resource.h>
void increase_stack_size() {
    const rlim_t ks = 64*1024*1024;
    struct rlimit rl;
    int res=getrlimit(RLIMIT_STACK, &rl);
    if(res==0){
        if(rl.rlim_cur<ks){
            rl.rlim_cur=ks;
            res=setrlimit(RLIMIT_STACK, &rl);
        }
    }
}

```

1.3 Pragma optimization

```

#pragma GCC optimize("Ofast,no-stack-protector,no-math-
errno,unroll-loops")
#pragma GCC target("sse,sse2,sse3,ssse3,sse4,popcnt,abm
,mmx,avx,tune=native")

```

1.4 Debugger

```
#!/usr/bin/env python3
import subprocess, platform

os_name = platform.system()
cmd = []
prefix = ""

if os_name == 'Windows':
    cmd = ["cmd", "/C"]
else:
    cmd = ["bash", "-c"]
    prefix = "./"

def GetTestData(exe):
    myout = subprocess.check_output(cmd + ["%s%s"%(
        prefix, exe)])
    return myout.decode("utf8")

def Judge(a,b,testdata):
    f = open("test.in", "w+")
    f.write(testdata)
    f.close()
    myout = subprocess.check_output(cmd + ["%s%s < test.
        in"%(prefix, a)])
    ansout = subprocess.check_output(cmd + ["%s%s < test
        .in"%(prefix, b)])
    if not myout == ansout:
        print("answer: %s"%ansout.decode("utf8"),end="")
        print("output: %s"%myout.decode("utf8"),end="")
        print("WA!")
        return False
    return True

if __name__ == '__main__':
    cnt = 0
    isOK = True
    while isOK:
        cnt += 1
        print(cnt)
        isOK = Judge("1397.exe", "test.exe", GetTestData(
            "gen.exe"))
```

1.5 Quick Random

```
// PRNG {{{
template<class T, T x1, T x2, T x3, int y1, int y2, int
    y3>
struct PRNG {
    using S = typename std::make_signed<T>::type;
    T s;
    PRNG(T _s = 0) : s(_s) {}
    T next() {
        T z = (s += x1);
        z = (z ^ (z >> y1)) * x2;
        z = (z ^ (z >> y2)) * x3;
        return z ^ (z >> y3);
    }
    T next(T n) { return next() % n; }
    S next(S l, S r) { return l + next(r - l + 1); }
    T operator()() { return next(); }
    T operator()(T n) { return next(n); }
    S operator()(S l, S r) { return next(l, r); }
    static T gen(T s) { return PRNG(s)(); }
template<class U>
    void shuffle(U first, U last) {
        size_t n = last - first;
        for (size_t i = 0; i < n; i++) swap(first[i],
            first[next(i + 1)]);
    }
};

using R32 = PRNG<uint32_t, 0x9E3779B1, 0x85EBCA6B, 0
    xC2B2AE35, 16, 13, 16>;
R32 r32;

using R64 = PRNG<uint64_t, 0x9E3779B97F4A7C15, 0
    xBF58476D1CE4E5B9, 0x94D049BB133111EB, 30, 27, 31>;
R64 r64;
// }}}

```

1.6 IO Optimization

```
static inline int gc() {
    static char buf[1 << 20], *p = buf, *end = buf;
    if (p == end) {
        if ((end = buf + fread(buf, 1, 1 << 20, stdin))
            == buf) return EOF;
        p = buf;
    }
    return *p++;
}

template<typename T>
static inline bool gn(T &_) {
    register int c = gc(); register T __ = 1; _ = 0;
    while(!isdigit(c) and c!=EOF and c!='-') c = gc();
    if(c == '-') { __ = -1; c = gc(); }
    if(c == EOF) return false;
    while(isdigit(c)) _ = _ * 10 + c - '0', c = gc();
    _ *= __;
    return true;
}

template <typename T, typename ...Args>
static inline bool gn(T &x, Args& ...args){return gn(x)
    and gn(args...);}
```

2 Data Structure

2.1 BigInt

```
class BigInt{
public:
    typedef int_fast64_t lld;
    #define PRINTF_ARG PRIdFAST64
    #define LOG_BASE_STR "9"
    static constexpr lld BASE = 1000000000;
    static constexpr int LOG_BASE = 9;
    vector<lld> dig;
    bool neg;

    inline int len() const{return (int)dig.size();}
    inline int cmp_minus(const BigInt& a) const {
        if(len() == 0 and a.len() == 0) return 0;
        if(neg ^ a.neg) return (int)a.neg*2 - 1;
        if(len() != a.len()) return neg?a.len()-len():len
            ()-a.len();
        for(int i=len()-1;i>=0;i--) if(dig[i] != a.dig[i]
            ) {
            return neg?a.dig[i]-dig[i]:dig[i]-a.dig[i];
        }
        return 0;
    }

    inline void trim(){
        while(!dig.empty() and dig.back()==0) dig.
            pop_back();
        if(dig.empty()) neg = false;
    }

public:
    BigInt(): dig(vector<lld>()), neg(false){}
    BigInt(lld a): dig(vector<lld>()){
        neg = a<0; dig.push_back(abs(a));
        trim();
    }
    BigInt(const string& a): dig(vector<lld>()){
        assert(!a.empty()); neg = (a[0]=='-');
        for(int i=((int)(a.size()))-1;i>=neg;i-=LOG_BASE)
            {
                lld cur = 0;
                for(int j=min(LOG_BASE-1, i-neg);j>=0;j--) cur
                    = cur*10+a[i-j]-'0';
                dig.push_back(cur);
            }
        trim();
    }

    inline bool operator<(const BigInt& a) const{return
        cmp_minus(a)<0;}
    inline bool operator<=(const BigInt& a) const{return
        cmp_minus(a)<=0;}
    inline bool operator==(const BigInt& a) const{return
        cmp_minus(a)==0;}
    inline bool operator!=(const BigInt& a) const{return
        cmp_minus(a)!=0;}
    inline bool operator>(const BigInt& a) const{return
        cmp_minus(a)>0;}
    inline bool operator>=(const BigInt& a) const{return
        cmp_minus(a)>=0;}
```

```

BigInt operator-() const {
    BigInt ret = *this;
    ret.neg ^= 1;
    return ret;
}
BigInt operator+(const BigInt& a) const {
    if(neg) return -(*this)+(-a);
    if(a.neg) return (*this)-(-a);
    int n = max(a.len(), len());
    BigInt ret; ret.dig.resize(n);
    lld pro = 0;
    for(int i=0;i<n;i++) {
        ret.dig[i] = pro;
        if(i < a.len()) ret.dig[i] += a.dig[i];
        if(i < len()) ret.dig[i] += dig[i];
        pro = 0;
        if(ret.dig[i] >= BASE) pro = ret.dig[i]/BASE;
        ret.dig[i] -= BASE*pro;
    }
    if(pro != 0) ret.dig.push_back(pro);
    return ret;
}
BigInt operator-(const BigInt& a) const {
    if(neg) return -(-(*this) - (-a));
    if(a.neg) return (*this) + (-a);
    int diff = cmp_minus(a);
    if(diff < 0) return -(a - (*this));
    if(diff == 0) return 0;
    BigInt ret; ret.dig.resize(len(), 0);
    for(int i=0;i<len();i++) {
        ret.dig[i] += dig[i];
        if(i < a.len()) ret.dig[i] -= a.dig[i];
        if(ret.dig[i] < 0){
            ret.dig[i] += BASE;
            ret.dig[i+1]--;
        }
    }
    ret.trim();
    return ret;
}
BigInt operator*(const BigInt& a) const {
    if(len()==0 or a.len()==0) return 0;
    BigInt ret; ret.dig.resize(len()+a.len()+1);
    ret.neg = neg ^ a.neg;
    for(int i=0;i<len();i++) for(int j=0;j<a.len();j++) {
        ret.dig[i+j] += dig[i] * a.dig[j];
        if(ret.dig[i+j] >= BASE) {
            lld x = ret.dig[i+j] / BASE;
            ret.dig[i+j+1] += x;
            ret.dig[i+j] -= x * BASE;
        }
    }
    ret.trim();
    return ret;
}
BigInt operator/(const BigInt& a) const {
    assert(a.len());
    if(len() < a.len()) return 0;
    BigInt ret; ret.dig.resize(len()-a.len()+1);
    ret.neg = a.neg;
    for(int i=len()-a.len();i>=0;i--){
        lld l = 0, r = BASE;
        while(r-l > 1){
            lld mid = (l+r)>>1;
            ret.dig[i] = mid;
            if(ret*a <= (neg?-(*this):(*this))) l = mid;
            else r = mid;
        }
        ret.dig[i] = l;
    }
    ret.neg ^= neg; ret.trim();
    return ret;
}
BigInt operator%(const BigInt& a) const {
    return (*this) - (*this) / a * a;
}
friend BigInt abs(BigInt a){
    a.neg ^= 1; return a;
}
friend void swap(BigInt& a, BigInt& b){
    swap(a.dig, b.dig); swap(a.neg, b.neg);
}
friend ostream& operator>>(ostream& ss, BigInt& a){
    string s; ss >> s;
    a = s;

```

```

        return ss;
    }
    friend ostream& operator<<(ostream& ss, const
        BigInt& a){
        if(a.len() == 0) return ss << '0';
        if(a.neg) ss << '-';
        ss << a.dig.back();
        for(int i=a.len()-2;i>=0;i--) ss << setw(LOG_BASE
            ) << setfill('0') << a.dig[i];
        return ss;
    }
    inline void print() const {
        if(len() == 0){putchar('0');return;}
        if(neg) putchar('-');
        printf("%" PRINTF_ARG, dig.back());
        for(int i=len()-2;i>=0;i--) printf("%0"
            LOG_BASE_STR PRINTF_ARG, dig[i]);
    }
    #undef PRINTF_ARG
    #undef LOG_BASE_STR
};

```

2.2 ScientificNotation

```

#include <cmath>
#include <cstdio>
#include <iostream>
#include <algorithm>

struct SciFi{
    typedef double base_t;
    base_t x; int p;
    SciFi(){x=0;p=0;}
    SciFi(base_t k){
        p = floor(log10(k));
        x = k / pow((base_t)10, p);
    }
    SciFi(base_t a, int b){
        x=a;p=b;
    }
    SciFi operator=(base_t k){
        p = floor(log10(k));
        x = k / pow((base_t)10, p);
        return *this;
    }
    SciFi operator*(SciFi k)const{
        int nP = p+k.p;
        base_t nX = x*k.x;
        int tp = floor(log10(nX));
        return SciFi(nX/pow((base_t)10, tp), nP+tp);
    }
    SciFi operator*=(SciFi k){
        p+=k.p;
        x*=k.x;
        int tp = floor(log10(x));
        p+=tp;
        x/=pow((base_t)10, tp);
        return *this;
    }
    SciFi operator+(SciFi k)const{
        int newP = std::min(k.p, p);
        base_t x1 = x*pow((base_t)10, p-newP);
        base_t x2 = k.x*pow((base_t)10, k.p-newP);
        x1+=x2;
        int tp = floor(log10(x1));
        newP+=tp;
        x1 /= pow((base_t)10, tp);
        return SciFi(x1, newP);
    }
    SciFi operator+=(SciFi k){
        int newP = std::min(k.p, p);
        base_t x1 = x*pow((base_t)10, p-newP);
        base_t x2 = k.x*pow((base_t)10, k.p-newP);
        x1+=x2;
        int tp = floor(log10(x1));
        newP+=tp;
        x1 /= pow((base_t)10, tp);
        x=x1;p=newP;
        return *this;
    }
    bool operator<(SciFi a)const{
        if(p == a.p) return x<a.x;
        return p<a.p;
    }
}

```

```

    bool operator>(SciFi a) const{
        if(p == a.p) return x>a.x;
        return p>a.p;
    }
    bool operator==(SciFi a) const{
        return p==a.p and x==a.x;
    }
};

int main(){
    double a; scanf("%lf",&a);
    SciFi aa=a, x;
    x = aa*SciFi(2);
    printf("%.21fe%c%03d\n", x.x, "+-"[x.p<0], abs(x.p)
    );
    return 0;
}

```

2.3 unordered_map

```

#include <ext/pb_ds/assoc_container.hpp>
using __gnu_pbds::cc_hash_table;
using __gnu_pbds::gp_hash_table;
template<typename A, typename B> using hTable1 =
    cc_hash_table<A,B>;
template<typename A, typename B> using hTable2 =
    gp_hash_table<A,B>;

```

2.4 extc_balance_tree

```

#include <functional>
#include <ext/pb_ds/assoc_container.hpp>
using std::less;
using std::greater;
using __gnu_pbds::tree;
using __gnu_pbds::rb_tree_tag;
using __gnu_pbds::ov_tree_tag;
using __gnu_pbds::splay_tree_tag;
using __gnu_pbds::null_type;
using __gnu_pbds::tree_order_statistics_node_update;

template<typename T>
using ordered_set = tree<T, null_type, less<T>,
    rb_tree_tag, tree_order_statistics_node_update>;

template<typename A, B>
using ordered_map = tree<A, B, less<A>, rb_tree_tag,
    tree_order_statistics_node_update>;

int main(){
    ordered_set<int> ss;
    ordered_map<int,int> mm;
    ss.insert(1);
    ss.insert(5);
    assert(*ss.find_by_order(0)==1);
    assert(ss.order_of_key(-1)==0);
    assert(ss.order_of_key(87)==2);
    return 0;
}

```

2.5 extc_heap

```

#include <functional>
#include <ext/pb_ds/assoc_container.hpp>
#include <ext/pb_ds/priority_queue.hpp>
using std::less;
using std::greater;
using __gnu_pbds::priority_queue;
using __gnu_pbds::pairing_heap_tag;
using __gnu_pbds::binary_heap_tag;
using __gnu_pbds::binomial_heap_tag;
using __gnu_pbds::rc_binomial_heap_tag;
using __gnu_pbds::thin_heap_tag;

int main(){
    priority_queue<int,less<int>,pairing_heap_tag> pq1,
    pq2;
    pq1.push(1);
    pq2.push(2);
}

```

```

pq1.join(pq2);
assert(pq2.size()==0);
auto it = pq1.push(87);
pq1.modify(it, 19);
while(!pq1.empty()){
    pq1.top();
    pq1.pop();
}
return 0;
}

```

2.6 SkewHeap

```

#include <functional>
using std::less;

template<typename T, typename cmp=less<T> >
class SkewHeap{
private:
    struct SkewNode{
        T x;
        SkewNode *lc, *rc;
        SkewNode(T a=0):x(a), lc(nullptr), rc(nullptr)
        {}
    } *root;
    cmp CMP_;
    size_t count;
    SkewNode* Merge(SkewNode* a, SkewNode* b){
        if(!a or !b) return a?a:b;
        if(CMP_(a->x, b->x)) swap(a, b);
        a->rc = Merge(a->rc, b);
        swap(a->lc, a->rc);
        return a;
    }
    void clear(SkewNode*& a){
        if(!a) return;
        clear(a->lc); clear(a->rc);
        delete a; a = nullptr;
    }
public:
    SkewHeap(): root(nullptr), count(0){}
    bool empty(){return count==0;}
    size_t size(){return count;}
    T top(){return root->x;}
    void clear(){clear(root);count = 0;}
    void push(const T& x){
        SkewNode* a = new SkewNode(x);
        count += 1;
        root = Merge(root, a);
    }
    void join(SkewHeap& a){
        count += a.count; a.count = 0;
        root = Merge(root, a.root);
    }
    void pop(){
        count -= 1;
        SkewNode* rt = Merge(root->lc, root->rc);
        delete root; root = rt;
    }
    friend void swap(SkewHeap& a, SkewHeap& b){
        swap(a.root, b.root);
    }
};

```

2.7 Disjoint Set

```

class DJS{
private:
    vector<int> fa, sz, sv;
    vector<pair<int*, int>> opt;
    inline void assign(int *k, int v){
        opt.emplace_back(k, *k);
        *k = v;
    }
public:
    inline void init(int n){
        fa.resize(n); iota(fa.begin(), fa.end(), 0);
        sz.resize(n); fill(sz.begin(), sz.end(), 1);
        opt.clear();
    }
    int query(int x){
        if(fa[x] == x) return x;
    }
};

```

```

    return query(fa[x]);
}
inline void merge(int a, int b){
    int af = query(a), bf = query(b);
    if(af == bf) return;
    if(sz[af] < sz[bf]) swap(af, bf);
    assign(&fa[bf], fa[af]);
    assign(&sz[af], sz[af]+sz[bf]);
}
inline void save(){sv.push_back((int)opt.size());}
inline void undo(){
    int ls = sv.back(); sv.pop_back();
    while((int)opt.size() > ls){
        pair<int*, int> cur=opt.back();
        *cur.first = cur.second;
        opt.pop_back();
    }
};

```

2.8 Treap

```

class Treap{
private:
    const int MEM = 500000 + 5;
    unsigned seed;
    inline unsigned myrand(){
        static unsigned seed = time(NULL);
        seed = seed*seed*127 + seed*227 + 2147483587;
        seed ^= seed*97;
        seed /= 7123;
        return seed;
    }
    struct node{
        node *lc, *rc;
        int pri, size, val;
        node(){}
        node(int x):
            lc(nullptr),
            rc(nullptr),
            pri(myrand()),
            size(1),
            val(x)
        {}
        inline void pull(){
            size = 1;
            if(lc) size += lc->size;
            if(rc) size += rc->size;
        }
    } *root, pool[MEM];
    int mem_;
    inline node* new_node(int x){
        static int mem_ = 0;
        assert(mem_ < MEM);
        pool[mem_] = node(x);
        return &pool[mem_++];
    }
    inline int sz(node* x){return x?x->size:0;}
    node* merge(node* a, node* b){
        if(!a or !b) return a?a:b;
        if(a->pri > b->pri){
            a->rc = merge(a->rc, b);
            a->pull();
            return a;
        }else{
            b->lc = merge(a, b->lc);
            b->pull();
            return b;
        }
    }
    void split(Treap* t, int k, Treap*& a, Treap*& b){
        if(!t) a=b=nullptr;
        else if(sz(t->lc) < k){
            a = t;
            split(t->rc, k - sz(t->lc) - 1, a->rc, b);
            a->pull();
        }else{
            b = t;
            split(t->lc, k, a, b->lc);
            b->pull();
        }
    }
    int oOk(node* rr, int x){
        if(rr==NULL) return 0;

```

```

        if((rr->val) < x) return gSize(rr->l)+oOk(rr->r,
            x)+1;
        else return oOk(rr->l, x);
    }
public:
    Treap(){root=nullptr;seed=time(NULL);mem_=0;}
    void do_something_at(int l, int r){
        // 1-base [l, r]
        split(root, l-1, tl, root);
        split(root, r-l+1, root, tr);
        root = merge(tl, merge(root, tr));
    }
    void insert(int x){
        node *a, *b;
        split(root, x, a, b);
        root = merge(merge(a, new node(x)), b);
        root->size = gSize(root->l)+gSize(root->r)+1;
    }
    void remove(int x){
        //need debug may contain bugs
        node *a, *b, *c, *d;
        split(root, x, a, b);
        a->size = gSize(a->l)+gSize(a->r);
        split(a, x-1, c, d);
        root = merge(b, c);
        root->size = gSize(root->l)+gSize(root->r);
        delete d;
    }
    int order_of_key(int x){return oOk(root,x);}
};

```

2.9 SparseTable

```

template<typename T, typename Cmp_ = std::less<T>>
class SparseTable{
private:
    vector<vector<T>> table;
    vector<int> lg;
    T cmp_(T a, T b){
        return Cmp_()(a, b)?a:b;
    }
public:
    void init(T arr[], int n){
        // 0-base
        lg.resize(n+1);
        lg[0] = -1, lg[1] = 0;
        for(int i=2;i<=n;i++) lg[i] = lg[i>>1]+1;
        table.resize(lg[n]+1);
        table[0].resize(n);
        for(int i=0;i<n;i++) table[0][i] = arr[i];
        for(int i=1;i<=lg[n];i++){
            int len = 1<<(i-1), sz = 1<<i;
            table[i].resize(n-sz+1);
            for(int j=0;j<=n-sz;j++){
                table[i][j] = cmp_(table[i-1][j], table
                    [i-1][j+len]);
            }
        }
    }
    T query(int l, int r){
        // 0-base [l, r]
        int wh = lg[r-l], len=1<<wh;
        return cmp_(table[wh][l], table[wh][r-len]);
    }
};

```

2.10 FenwickTree

```

#include <vector>
using std::vector;

template<typename T>
class BIT{
#define ALL(x) begin(x), end(x)
private:
    vector<T> arr;
    int n;
    inline int lowbit(int x){return x & (-x);}
    T query(int x){
        T ret = 0;
        while(x > 0){
            ret += arr[x];

```

```

        x -= lowbit(x);
    }
    return ret;
}
public:
    void init(int n_){
        n = n_;
        arr.resize(n);
        fill(arr.begin(), arr.end(), 0);
    }
    void modify(int pos, T v){
        while(pos < n){
            arr[pos] += v;
            pos += lowbit(pos);
        }
    }
    T query(int l, int r){
        // 1-base (l, r]
        return query(r) - query(l);
    }
}
#undef ALL
};

template<typename T>
class BIT{
#define ALL(x) begin(x), end(x)
private:
    vector<T> arr;
    int n;
    inline int lowbit(int x){return x & (-x);}
    void add(int s, int v){
        while(s){
            arr[s] += v;
            s -= lowbit(s);
        }
    }
public:
    void init(int n_){
        n = n_;
        arr.resize(n);
        fill(ALL(arr), 0);
    }
    void add(int l, int r, T v){
        // 1-base (l, r]
        add(l, -v);
        add(r, v);
    }
    T query(int x){
        T r = 0;
        while(x < size()){
            r += arr[x];
            x += lowbit(x);
        }
        return r;
    }
}
#undef ALL
};

```

3 Graph

3.1 BCC Edge

```

class BCC{
private:
    int low[N], dfn[N], cnt;
    bool bcc[N];
    vector<PII> G[N];
    void dfs(int w, int f){
        dfn[w] = cnt++;
        low[w] = dfn[w];
        for(auto i: G[w]){
            int u = i.FF, t = i.SS;
            if(u == f) continue;
            if(dfn[u] != 0){
                low[w] = min(low[w], dfn[u]);
            } else {
                dfs(u, w);
                low[w] = min(low[w], low[u]);
                if(low[u] > dfn[w]) bcc[t] = true;
            }
        }
    }
}

```

```

public:
    void init(int n, int m){
        for(int i=0; i<n; i++) G[i].clear();
        fill(bcc, bcc+m, false);
        cnt = 0;
    }
    void add_edge(int u, int v){
        G[u].PB({v, cnt});
        G[v].PB({u, cnt});
        cnt++;
    }
    void solve(){cnt = 1; dfs(0, 0);}
    // the id will be same as insert order, 0-base
    bool is_bcc(int x){return bcc[x];}
} bcc;

```

3.2 BCC Vertex

```

class BCC{
private:
    vector<vector<pair<int, int>>> G;
    vector<int> dfn, low, id, sz;
    vector<bool> vis, ap;
    int n, ecnt, bcnt;
    void tarjan(int u, int f, int d){
        vis[u] = true;
        dfn[u] = low[u] = d;
        int child = 0;
        for(auto e: G[u]) if(e.first != f){
            int v = e.first;
            if(vis[v]){
                low[u] = min(low[u], dfn[v]);
            } else {
                tarjan(v, u, d+1);
                if(low[v] >= dfn[u]) ap[u] = true;
                low[u] = min(low[u], low[v]);
                child++;
            }
        }
        if(dfn[u] == 0 and child <= 1) ap[u] = false;
    }
    void bfs_bcc(int x){
        // not sure
        queue<int> bfs;
        bfs.push(x); vis[x] = true;
        while(!bfs.empty()){
            int u = bfs.front(); bfs.pop();
            for(auto e: G[u]){
                id[e.second] = bcnt;
                if(ap[e.first] or vis[e.first]) continue;
                bfs.push(e.first); vis[e.first] = true;
                sz[bcnt] += 1;
            }
        }
    }
public:
    void init(int n_){
        n = n_; G.clear(); G.resize(n);
        dfn.resize(n); low.resize(n);
        vis.clear(); vis.resize(n);
        ap.clear(); ap.resize(n);
        ecnt = 0, bcnt = 0;
    }
    void add_edge(int u, int v){
        assert(0 <= u and u < n);
        assert(0 <= v and v < n);
        G[u].emplace_back(v, ecnt);
        G[v].emplace_back(u, ecnt);
        ecnt++;
    }
    void solve(){
        for(int i=0; i<n; i++) if(!vis[i]) {
            tarjan(i, i, 0);
        }
        id.resize(ecnt);
        vis.clear(); vis.resize(n);
        sz.clear(); sz.resize(n);
        for(int i=0; i<n; i++) if(ap[i]){
            bfs_bcc(i); bcnt++;
        }
    }
    bool isAP(int x){return ap[x];}
    int count(){return bcnt;}
}

```

```

// bcc_id of edges by insert order (0-base)
int get_id(int x){return id[x];}
// bcc size by bcc_id
int get_size(int x){return sz[x];}
} bcc;

```

3.3 Strongly Connected Components

```

class SCC{
private:
    int n, num_;
    vector<int> G[N], rG[N], ord, num;
    bool vis[N];
    void dfs(int u){
        if(vis[u]) return;
        vis[u]=1;
        for(auto v: G[u]) dfs(v);
        ord.PB(u);
    }
    void rdfs(int u){
        if(vis[u]) return;
        num[u] = num_;
        vis[u] = 1;
        for(auto v: rG[u]) rdfs(v);
    }
public:
    inline void init(int n_){
        n=n_, num_=0;
        num.resize(n);
        for(int i=0;i<n;i++) G[i].clear();
        for(int i=0;i<n;i++) rG[i].clear();
    }
    inline void add_edge(int st, int ed){
        G[st].PB(ed);
        rG[ed].PB(st);
    }
    void solve(){
        memset(vis, 0, sizeof(vis));
        for(int i=0;i<n;i++){
            if(!vis[i]) dfs(i);
        }
        reverse(ALL(ord));
        memset(vis, 0, sizeof(vis));
        for(auto i: ord){
            if(!vis[i]){
                rdfs(i);
                num_++;
            }
        }
        inline int get_id(int x){return num[x];}
        inline int count(){return num_;}
    } scc;
}

```

3.4 Bipartite Matching

```

#include <bits/stdc++.h>
using namespace std;
#define N 500

class BipartiteMatching{
private:
    vector<int> X[N], Y[N];
    int fX[N], fY[N], n;
    bitset<N> walked;
    bool dfs(int x){
        for(auto i:X[x]){
            if(walked[i]) continue;
            walked[i]=1;
            if(fY[i]==-1||dfs(fY[i])){
                fY[i]=x;fX[x]=i;
                return 1;
            }
        }
        return 0;
    }
public:
    void init(int _n){
        n=_n;
        for(int i=0;i<n;i++){
            X[i].clear();
            Y[i].clear();
        }
    }
}

```

```

        fX[i]=fY[i]=-1;
    }
    walked.reset();
}
void AddEdge(int x, int y){
    X[x].push_back(y);
    Y[y].push_back(x);
}
int solve(){
    int cnt = 0;
    for(int i=0;i<n;i++){
        walked.reset();
        if(dfs(i)) cnt++;
    }
    // return how many pair matched
    return cnt;
}
};

```

3.5 Minimum Cost Maximum Flow

```

class MiniCostMaxiFlow{
    typedef int CapT;
    typedef lld WeiT;
    typedef pair<CapT, WeiT> PCW;
    const CapT INF_CAP = 1<<30;
    const WeiT INF_WEI = 1LL<<60;
    const int MAXV = N;
private:
    struct Edge{
        int to, back;
        WeiT wei;
        CapT cap;
        Edge(){}
        Edge(int a, int b, WeiT c, CapT d): to(a), back(b), wei(c), cap(d) {}
    };
    int ori, edd, V;
    vector<Edge> G[MAXV];
    int fa[MAXV], wh[MAXV];
    bool inq[MAXV];
    WeiT dis[MAXV];
    PCW SPFA(){
        for(int i=0;i<V;i++) inq[i]=0;
        for(int i=0;i<V;i++) dis[i]=INF_WEI;
        queue<int> qq;
        qq.push(ori);
        dis[ori]=0;
        while(!qq.empty()){
            int u = qq.front(); qq.pop();
            inq[u]=0;
            for(int i=0;i<SZ(G[u]);i++){
                Edge e = G[u][i];
                int v = e.to;
                WeiT d = e.wei;
                if(e.cap > 0 and dis[v] > dis[u]+d){
                    dis[v]=dis[u]+d;
                    fa[v]=u;
                    wh[v] = i;
                    if(inq[v]) continue;
                    qq.push(v);
                    inq[v]=1;
                }
            }
        }
        if(dis[edd]==INF_WEI) return {-1, -1};
        CapT mw=INF_CAP;
        for(int i=edd;i!=ori;i=fa[i]){
            mw = min(mw, G[fa[i]][wh[i]].cap);
        }
        for(int i=edd;i!=ori;i=fa[i]){
            auto &eg = G[fa[i]][wh[i]];
            eg.cap -= mw;
            G[eg.to][eg.back].cap += mw;
        }
        return {mw, dis[edd]};
    }
public:
    void init(int a, int b, int n=MAXV){
        V=n;
        ori = a;
        edd = b;
        for(int i=0;i<n;i++) G[i].clear();
    }
}

```



```

void addEdge(int st, int ed, WeiT w, CapT c){
    G[st].PB(Edge(ed, SZ(G[ed]), w, c));
    G[ed].PB(Edge(st, SZ(G[st])-1, -w, 0));
}
PCW solve(){
    CapT cc=0; WeiT ww=0;
    while(true){
        PCW ret = SPFA();
        if(ret.FF== -1) break;
        cc += ret.FF;
        ww += ret.SS;
    }
    return {cc, ww};
}
} mcmf;

```

3.6 MaximumFlow

```

class Dinic{
private:
    using CapT = int64_t;
    struct Edge{
        int to, rev;
        CapT cap;
    };
    int n, st, ed;
    vector<vector<Edge>> G;
    vector<int> lv;
    bool BFS(){
        fill(lv.begin(), lv.end(), -1);
        queue<int> bfs;
        bfs.push(st);
        lv[st] = 0;
        while(!bfs.empty()){
            int u = bfs.front(); bfs.pop();
            for(auto e: G[u]){
                if(e.cap <= 0 or lv[e.to] != -1) continue;
                lv[e.to] = lv[u] + 1;
                bfs.push(e.to);
            }
        }
        return (lv[ed] != -1);
    }
    CapT DFS(int u, CapT f){
        if(u == ed) return f;
        CapT ret = 0;
        for(auto& e: G[u]){
            if(e.cap <= 0 or lv[e.to] != lv[u]+1) continue;
            CapT nf = DFS(e.to, min(f, e.cap));
            ret += nf; e.cap -= nf; f -= nf;
            G[e.to][e.rev].cap += nf;
            if(f == 0) return ret;
        }
        if(ret == 0) lv[u] = -1;
        return ret;
    }
public:
    void init(int n_, int st_, int ed_){
        n = n_, st = st_, ed = ed_;
        G.resize(n); lv.resize(n);
        fill(G.begin(), G.end(), vector<Edge>());
    }
    void add_edge(int u, int v, CapT c){
        G[u].push_back({v, (int) (G[v].size()), c});
        G[v].push_back({u, (int) (G[u].size())-1, 0});
    }
    CapT max_flow(){
        CapT ret = 0;
        while(BFS()){
            CapT f = DFS(st, numeric_limits<CapT>::max());
            ret += f;
            if(f == 0) break;
        }
        return ret;
    }
} flow;

```

3.7 Kuhn Munkres

```

struct KM{
    // Maximum Bipartite Weighted Matching (Perfect Match)
    static const int MXN = 650;
    static const int INF = 2147483647; // LL
    int n, match[MXN], vx[MXN], vy[MXN];
    int edge[MXN][MXN], lx[MXN], ly[MXN], slack[MXN];
    // ^^^^ LL
    void init(int _n){
        n = _n;
        for(int i=0; i<n; i++) for(int j=0; j<n; j++)
            edge[i][j] = 0;
    }
    void addEdge(int x, int y, int w) // LL
    { edge[x][y] = w; }
    bool DFS(int x){
        vx[x] = 1;
        for (int y=0; y<n; y++){
            if (vy[y]) continue;
            if (lx[x]+ly[y] > edge[x][y]){
                slack[y]=min(slack[y], lx[x]+ly[y]-edge[x][y]);
            } else {
                vy[y] = 1;
                if (match[y] == -1 || DFS(match[y]))
                    { match[y] = x; return true; }
            }
        }
        return false;
    }
    int solve(){
        fill(match, match+n, -1);
        fill(lx, lx+n, -INF); fill(ly, ly+n, 0);
        for (int i=0; i<n; i++){
            for (int j=0; j<n; j++)
                lx[i] = max(lx[i], edge[i][j]);
            for (int i=0; i<n; i++){
                fill(slack, slack+n, INF);
                while (true){
                    fill(vx, vx+n, 0); fill(vy, vy+n, 0);
                    if ( DFS(i) ) break;
                    int d = INF; // long long
                    for (int j=0; j<n; j++)
                        if (!vy[j]) d = min(d, slack[j]);
                    for (int j=0; j<n; j++){
                        if (vx[j]) lx[j] -= d;
                        if (vy[j]) ly[j] += d;
                        else slack[j] -= d;
                    }
                }
            }
        }
        int res=0;
        for (int i=0; i<n; i++)
            res += edge[match[i]][i];
        return res;
    }
} graph;

```

4 Math

4.1 Prime Table

```

// 1000000000 < primes < 2147483647
1002939109, 1020288887, 1028798297, 1038684299,
1041211027, 1051762951, 1058585963, 1063020809,
1094763083, 1106384353, 1120154459, 1140593173,
1147930723, 1172520109, 1183835981, 1187659051,
1241251303, 1247184097, 1255940849, 1272759031,
1287027493, 1288511629, 1294632499, 1312650799,
1314753281, 1320080669, 1321970357, 1333133947,
1337684419, 1353508067, 1358715989, 1364961029,
1366046831, 1376536367, 1381705499, 1410637769,
1411311571, 1422795043, 1437499801, 1495803851,
1511764363, 1526710979, 1538018089, 1542373769,
1545326953, 1549429633, 1556212739, 1575971759,
1586465261, 1608336427, 1609783001, 1620728569,
1643267081, 1652401603, 1656717203, 1660920671,
1666858577, 1669260361, 1670240317, 1678791131,
1685583143, 1725964619, 1734856421, 1743134179,
1761537223, 1774260193, 1778872889, 1781930609,
1803000149, 1814256623, 1834876331, 1839154463,
1840044389, 1843241713, 1856039431, 1868564531,
1868732623, 1884198443, 1884616807, 1885059541,
1909942399, 1914471137, 1923951707, 1925453197,

```



```
1937719153, 1954649041, 1958915237, 1970709803,
1979612177, 1980446837, 1989761941, 2007826547,
2008033571, 2011186739, 2039465081, 2039728567,
2093735719, 2116097521, 2123852629, 2140170259
```

```
// 2147483647 < primes < 4000000000
```

```
3148478261, 3153064147, 3176351071, 3187523093,
3196772239, 3201312913, 3203063977, 3204840059,
3210224309, 3213032591, 3217689851, 3218469083,
3219857533, 3231880427, 3235951699, 3273767923,
3276188869, 3277183181, 3282463507, 3285553889,
3319309027, 3327005333, 3327574903, 3341387953,
3373293941, 3380077549, 3380892997, 3381118801,
3384716479, 3386991323
```

倒數枚舉

```
T_0 = 1, T_{i+1} = n // (n // (T_i + 1))
```

4.2 ax+by=gcd

```
// By Adrien1018 (not knowing how to use.
// ax+ny = 1, ax+ny == ax == 1 (mod n)
tuple<int, int, int> extended_gcd(int a, int b) {
    if (!b) return make_tuple(a, 1, 0);
    int d, x, y;
    tie(d, x, y) = extended_gcd(b, a % b);
    return make_tuple(d, y, x - (a / b) * y);
}
// ax+by = gcd (by Eddy1021
PII gcd(int a, int b) {
    if (b == 0) return {1, 0};
    PII q = gcd(b, a % b);
    return {q.second, q.first - q.second * (a / b)};
}
```

4.3 Pollard Rho

```
// coded by hanhanW
// does not work when n is prime
long long modit(long long x, long long mod) {
    if (x >= mod) x -= mod;
    // if (x < 0) x += mod;
    return x;
}
long long mult(long long x, long long y, long long mod) {
    long long s = 0, m = x % mod;
    while (y) {
        if (y & 1) s = modit(s + m, mod);
        y >>= 1;
        m = modit(m + m, mod);
    }
    return s;
}
long long f(long long x, long long mod) {
    return modit(mult(x, x, mod) + 1, mod);
}
long long pollard_rho(long long n) {
    if (!(n & 1)) return 2;
    while (true) {
        long long y = 2, x = rand() % (n - 1) + 1, res = 1;
        for (int sz = 2; res == 1; sz *= 2) {
            for (int i = 0; i < sz && res == 1; i++) {
                x = f(x, n);
                res = __gcd(abs(x - y), n);
            }
            y = x;
        }
        if (res != 0 && res != n) return res;
    }
}
```

4.4 Linear Sieve

```
const int N = 20000000;
bool sieve[N];

void linear_sieve() {
    vector<int> prime;
    for (int i = 2; i < N; i++) {
```

```
        if (!sieve[i]) prime.push_back(i);
        for (int j = 0; i * prime[j] < N; j++) {
            sieve[i * prime[j]] = true;
            if (i % prime[j] == 0) break;
        }
    }
}
```

4.5 NloglogN Sieve

```
void Sieve(int n) {
    for (int i = 2; i <= n; i++) {
        if (!notprime[i]) primes.push_back(i);
        for (int j = i * i; j <= n; j += i) notprime[j] = true;
    }
}
```

4.6 Range Sieve

```
#include <algorithm>
typedef long long lld;
const int MAX_SQRT_B = 50000;
const int MAX_L = 200000 + 5;

bool is_prime_small[MAX_SQRT_B];
bool is_prime[MAX_L];
void sieve(lld, lld);

void sieve(lld l, lld r) {
    // [l, r)
    for (lld i = 2; i * i < r; i++) is_prime_small[i] = true;
    for (lld i = l; i < r; i++) is_prime[i - l] = true;
    if (l == 1) is_prime[0] = false;
    for (lld i = 2; i * i < r; i++) {
        if (!is_prime_small[i]) continue;
        for (lld j = i * i; j < r; j += i) is_prime_small[j] = false;
        for (lld j = std::max(2LL, (l + i - 1) / i) * i; j < r; j += i)
            is_prime[j - l] = false;
    }
}
```

4.7 Miller Rabin

```
lld modu(lld a, lld m) {
    while (a >= m) a -= m;
    return a;
}
lld mul(lld a, lld b, lld m) {
    if (a < b) swap(a, b);
    lld ret = 0;
    while (b) {
        if (b & 1) ret = modu(ret + a, m);
        a = modu(a + a, m);
        b >>= 1;
    }
    return ret;
}
lld qPow(lld a, lld k, lld m) {
    lld ret = 1;
    a %= m;
    while (k) {
        if (k & 1) ret = mul(ret, a, m);
        a = mul(a, a, m);
        k >>= 1;
    }
    return modu(ret, m);
}
bool witness(lld a, lld s, int t, lld n) {
    lld b = qPow(a, s, n);
    if (b == 0) return false;
    while (t--) {
        lld bb = mul(b, b, n);
        if (bb == 1 && b != 1 && b != n - 1) return true;
        b = bb;
    }
}
```

```

    return b != 1;
}
bool miller_rabin(lld n){
    if(n < 2) return false;
    if(!(n & 1)) return (n==2);
    lld x = n-1; int t = 0;
    while(!(x&1)) x >>= 1, t++;
    lld sprp[] = {2,325,9375,28178,450775,9780504,1795265022};
    for(int i=0;i<t;i++){
        if(witness(sprp[i]%n, x, t, n)) return false;
    }
    return true;
}

```

4.8 Inverse Element

```

// x's inverse mod k
// if k is prime
long long GetInv(long long x, long long k){
    return qPow(x, k-2);
}

// x's inverse mod k
// if k is not prime
long long GetInv(long long x, long long k){
    return qPow(x, Euler(k)-1);
}

// or extended_gcd(x, k).second
// if you need [1, x] (most use: [1, k-1])
void solve(int x, long long k){
    inv[1] = 1;
    for(int i=2;i<k;i++){
        inv[i] = ((long long)(k - k/i) * inv[k % i]) % k;
    }
}

```

4.9 Euler Phi Function

```

/*
    extended euler:
    a^b mod p
    if gcd(a, p)==1: a^(b%phi(p))
    elif b < phi(p): a^b mod p
    else a^(b%phi(p) + phi(p))
*/
inline int64_t Euler(int x){
    int64_t r=1;
    for(int i=2;i<=x;i++){
        if(x%i==0){
            x/=i;
            r*=(i-1);
            while(x%i==0){
                x/=i;
                r*=i;
            }
        }
    }
    if(x>1) r*=x-1;
    return r;
}

vector<int> primes;
bool notprime[N];
int64_t phi[N];
inline void euler_sieve(int n){
    for(int i=2;i<n;i++){
        if(!notprime[i]){
            primes.push_back(i);
            phi[i] = i-1;
        }
        for(auto j: primes){
            if(i*j >= n) break;
            notprime[i*j] = true;
            phi[i*j] = phi[i] * phi[j];
            if(i % j == 0){
                phi[i*j] = phi[i] * j;
                break;
            }
        }
    }
}

```

4.10 Gauss Elimination

```

typedef long double llf;
const int N = 300;
const llf EPS = 1e-8;

// make m[i][i] = x, m[i][j] = 0
// v is for solving equation:
// for(int i=0;i<n;i++) ans[pos[i]] = val[i]/mtx[i][pos[i]];
// for(int i=0;i<n;i++) cout << ans[i] << '\n';
bool Gauss(llf m[N][N], llf v[N], int n, int pos[N]){
    for(int i=0;i<n;i++){
        int x=-1, y=-1; llf m = 0;
        for(int j=i;j<n;j++){
            for(int k=i;k<n;k++){
                if(fabs(m[j][pos[k]])>m){
                    m = fabs(m[j][pos[k]]);
                    x = j, y = k;
                }
            }
        }
        if(x==-1 || y==-1) return false;
        swap(m[x], m[i]);
        swap(v[x], v[i]);
        swap(pos[y], pos[i]);
        for(int j=i+1;j<n;j++){
            llf xi = m[j][pos[i]]/m[i][pos[i]];
            for(int k=0;k<n;k++){
                m[j][pos[k]] -= xi*m[i][pos[k]];
                v[j] -= xi*v[i];
            }
        }
    }
    for(int i=n-1;i>=0;i--){
        for(int j=i-1;j>=0;j--){
            llf xi = m[j][pos[i]]/m[i][pos[i]];
            for(int k=0;k<n;k++){
                m[j][pos[k]] -= xi*m[i][pos[k]];
                v[j] -= xi*v[i];
            }
        }
    }
    return true;
}

```

4.11 Fast Fourier Transform

```

/*
    polynomial multiply:
    FFT(a, N, true);
    FFT(b, N, true);
    for(int i=0;i<MAXN;i++) c[i] = a[i]*b[i];
    FFT(c, N, false);
    yeah~ go result in c
    (N must be 2^k and >= len(a)+len(b))
*/
typedef long double llf;
typedef complex<llf> cplx;
const int MAXN = 262144;
const llf PI = acos((llf)-1);

cplx A[MAXN], B[MAXN], C[MAXN], omega[MAXN+1];

void init_omega(){
    const cplx I = {0, 1};
    for(int i=0;i<MAXN;i++) omega[i] = exp(i*2*PI/MAXN * I);
}

void FFT(cplx arr[], int n, bool ori){
    // n must be 2^k
    int theta = MAXN / n;
    for(int len=n;len>=2;len>>=1){
        int tot = len>>1;
        for(int i=0;i<tot;i++){
            cplx omg = omega[ori*i*theta*MAXN:MAXN-(i*theta*MAXN)];
            for(int j=i;j<n;j+=len){
                int k = j+tot;
                cplx x = arr[j] - arr[k];
                arr[j] += arr[k];
                arr[k] = omg * x;
            }
        }
        theta = (theta * 2) % MAXN;
    }
}

```

```

int i = 0;
for(int j=1;j<n-1;j++){
    for(int k=n>>1;k>(i^=k);k>>=1);
    if(j < i) swap(arr[j], arr[i]);
}
if(ori) return;
for(int i=0;i<n;i++) arr[i] /= n;
}

```

4.12 Chinese Remainder

```

// ax+ny = 1, ax+ny == ax == 1 (mod n)
pair<lld,lld> gcd(lld a, lld b){
    if(b == 0) return {1, 0};
    pair<lld,lld> q = gcd(b, a % b);
    return {q.second, q.first - q.second * (a / b)};
}

lld crt(lld ans[], lld pri[], int n){
    lld M = 1;
    for(int i=0;i<n;i++) M *= pri[i];
    lld ret = 0;
    for(int i=0;i<n;i++){
        lld inv = (gcd(M/pri[i], pri[i]).first + pri[i]
        )%pri[i];
        ret += (ans[i]*(M/pri[i])%M * inv)%M;
        ret %= M;
    }
    return ret;
}

```

4.13 NTT

```

typedef long long LL;
// Remember coefficient are mod P
/* p=a*2^n+1
n    2^n    p    a    root
5    32     97    3    5
6    64    193    3    5
7    128    257    2    3
8    256    257    1    3
9    512    7681   15   17
10   1024   12289   12   11
11   2048   12289    6   11
12   4096   12289    3   11
13   8192   40961    5    3
14   16384  65537    4    3
15   32768  65537    2    3
16   65536  65537    1    3
17   131072 786433    6   10
18   262144 786433    3   10 (605028353,
    2308, 3)
19   524288 5767169   11    3
20   1048576 7340033    7    3
21   2097152 23068673   11    3
22   4194304 104857601  25    3
23   8388608 167772161  20    3
24   16777216 167772161 10    3
25   33554432 167772161  5    3 (1107296257, 33,
    10)
26   67108864 469762049  7    3
27   134217728 2013265921 15   31 */
// (must be 2^k)
// To implement poly. multiply:
// NTT<P, root, MAXN> ntt;
// ntt( n , a ); // or ntt.tran( n , a );
// ntt( n , b );
// for( int i = 0 ; i < n ; i++ )
//   c[ i ] = a[ i ] * b[ i ];
// ntt( n , c , 1 );
//
// then you have the result in c :: [LL]

template<LL P, LL root, int MAXN>
struct NTT{
    static LL bigmod(LL a, LL b) {
        LL res = 1;
        for (LL bs = a; b; b >>= 1, bs = (bs * bs) % P)
            if(b&1) res=(res*bs)%P;
        return res;
    }
}

```

```

}
static LL inv(LL a, LL b) {
    if(a==1) return 1;
    return ((LL) (a-inv(b*a,a))*b+1)/a%b;
}
LL omega[MAXN+1];
NTT() {
    omega[0] = 1;
    LL r = bigmod(root, (P-1)/MAXN);
    for (int i=1; i<=MAXN; i++)
        omega[i] = (omega[i-1]*r)%P;
}
// n must be 2^k
void tran(int n, LL a[], bool inv_ntt=false){
    int basic = MAXN / n;
    int theta = basic;
    for (int m = n; m >= 2; m >>= 1) {
        int mh = m >> 1;
        for (int i = 0; i < mh; i++) {
            LL w = omega[i*theta%MAXN];
            for (int j = i; j < n; j += m) {
                int k = j + mh;
                LL x = a[j] - a[k];
                if (x < 0) x += P;
                a[j] += a[k];
                if (a[j] > P) a[j] -= P;
                a[k] = (w * x) % P;
            }
        }
        theta = (theta * 2) % MAXN;
    }
    int i = 0;
    for (int j = 1; j < n - 1; j++) {
        for (int k = n >> 1; k > (i ^= k); k >>= 1)
            ;
        if (j < i) swap(a[i], a[j]);
    }
    if (inv_ntt) {
        LL ni = inv(n,P);
        reverse( a+1 , a+n );
        for (i = 0; i < n; i++)
            a[i] = (a[i] * ni) % P;
    }
}
void operator()(int n, LL a[], bool inv_ntt=false)
{
    tran(n, a, inv_ntt);
}
};

const LL P=2013265921,root=31;
const int MAXN=4194304;
NTT<P, root, MAXN> ntt;

```

5 Geometry

5.1 Point Class

```

template<typename T>
struct Point{
    typedef long double llf;
    static constexpr llf EPS = 1e-8;
    T x, y;
    Point(T __=0, T __=0): x(__), y(__){}
    template<typename T2>
    Point(const Point<T2>& a): x(a.x), y(a.y){}
    inline llf theta() const {
        return atan2((llf)y, (llf)x);
    }
    inline llf dis() const {
        return hypot((llf)x, (llf)y);
    }
    inline llf dis(const Point& o) const {
        return hypot((llf)(x-o.x), (llf)(y-o.y));
    }
    Point operator-(const Point& o) const {
        return Point(x-o.x, y-o.y);
    }
    Point operator+=(const Point& o){
        x+=o.x, y+=o.y;
        return *this;
    }
}

```

```

Point operator+(const Point& o) const {
    return Point(x+o.x, y+o.y);
}
Point operator+=(const Point& o){
    x+=o.x, y+=o.y;
    return *this;
}
Point operator*(const T& k) const {
    return Point(x*k, y*k);
}
Point operator*=(const T& k){
    x*=k, y*=k;
    return *this;
}
Point operator/(const T& k) const {
    return Point(x/k, y/k);
}
Point operator/=(const T& k){
    x/=k, y/=k;
    return *this;
}
Point operator-() const {
    return Point(-x, -y);
}
Point rot90() const {
    return Point(-y, x);
}
template<typename T2>
bool in(const Circle<T2>& a) const {
    /* Add struct Circle at top */
    return a.o.dis(*this)+EPS <= a.r;
}
bool equal(const Point& o, true_type) const {
    return fabs(x-o.x) < EPS and fabs(y-o.y) < EPS;
}
bool equal(const Point& o, false_type) const {
    return tie(x, y) == tie(o.x, o.y);
}
bool operator==(const Point& o) const {
    return equal(o, is_floating_point<T>());
}
bool operator!=(const Point& o) const {
    return !(*this == o);
}
bool operator<(const Point& o) const {
    return theta() < o.theta();
    // sort like what pairs did
    // if(is_floating_point<T>()) return fabs(x-o.x)
    <EPS?y<o.y:x<o.x;
    // else return tie(x, y) < tie(o.x, o.y);
}
friend inline T cross(const Point& a, const Point&
    b){
    return a.x*b.y - b.x*a.y;
}
friend inline T dot(const Point& a, const Point& b){
    return a.x*b.x + a.y*b.y;
}
friend ostream& operator<<(ostream& ss, const Point
    & o){
    ss<<"("<<o.x<<"", "<<o.y<<"")";
    return ss;
}
};

```

5.2 Circle Class

```

template<typename T>
struct Circle{
    static constexpr llf EPS = 1e-8;
    Point<T> o;
    T r;
    vector<Point<llf>> operator&(const Circle& aa)
        const {
        // https://www.cnblogs.com/wangzming/p/8338142.html
        llf d=o.dis(aa.o);
        if(d > r+aa.r+EPS or d < fabs(r-aa.r)-EPS)
            return {};
        llf dt = (r*r - aa.r*aa.r)/d, d1 = (d+dt)/2;
        Point<llf> dir = (aa.o-o); dir /= d;
        Point<llf> pcrs = dir*d1 + o;
    }
};

```

```

        dt=sqrt(max(0.0L, r*r - d1*d1)), dir=dir.rot90
            ();
        return {pcrs + dir*dt, pcrs - dir*dt};
    }
};

```

5.3 Line Class

```

const Point<long double> INF_P(-1e20, 1e20);
const Point<long double> NOT_EXIST(1e20, 1e-20);
template<typename T>
struct Line{
    static constexpr long double EPS = 1e-8;
    // ax+by+c = 0
    T a, b, c;
    Line(): a(0), b(1), c(0){}
    Line(T __, T ___, T ___): a(__), b(___), c(___){
        assert(fabs(a)>EPS or fabs(b)>EPS);
    }
    template<typename T2>
    Line(const Line<T2>& x): a(x.a), b(x.b), c(x.c){}
    typedef Point<long double> Pt;
    bool equal(const Line& o, true_type) const {
        return fabs(a-o.a) < EPS and fabs(b-o.b) < EPS
            and fabs(c-o.c) < EPS;
    }
    bool euqal(const Line& o, false_type) const {
        return a==o.a and b==o.b and c==o.c;
    }
    bool operator==(const Line& o) const {
        return euqal(o, is_floating_point<T>());
    }
    bool operator!=(const Line& o) const {
        return !(*this == o);
    }
    friend inline bool on_line__(const Point<T>& p,
        const Line& l, true_type){
        return fabs(l.a*p.x + l.b*p.y + l.c) < EPS;
    }
    friend inline bool on_line__(const Point<T>& p,
        const Line& l, false_type){
        return l.a*p.x + l.b*p.y + l.c == 0;
    }
    friend inline bool on_line(const Point<T>&p const
        Line& l){
        return on_line__(p, l, is_floating_point<T>());
    }
    friend inline bool is_parallel__(const Line& x,
        const Line& y, true_type){
        return fabs(x.a*y.b - x.b*y.a) < EPS;
    }
    friend inline bool is_parallel__(const Line& x,
        const Line& y, false_type){
        return x.a*y.b == x.b*y.a;
    }
    friend inline bool is_parallel(const Line& x, const
        Line& y){
        return is_parallel__(x, y, is_floating_point<T>
            >());
    }
    friend inline Pt get_inter(const Line& x, const
        Line& y){
        typedef long double llf;
        if(x==y) return INF_P;
        if(is_parallel(x, y)) return NOT_EXIST;
        llf delta = x.a*y.b - x.b*y.a;
        llf delta_x = x.b*y.c - x.c*y.b;
        llf delta_y = x.c*y.a - x.a*y.c;
        return Pt(delta_x / delta, delta_y / delta);
    }
    friend ostream& operator<<(ostream& ss, const Line&
        o){
        ss<<o.a<<"x+"<<o.b<<"y+"<<o.c<<"=0";
        return ss;
    }
};
template<typename T>
inline Line<T> get_line(const Point<T>& a, const Point<
    T>& b){
    return Line<T>(a.y-b.y, b.x-a.x, (b.y-a.y)*a.x-(b.x
        -a.x)*a.y);
}

```

5.4 Segment Class

```
const long double EPS = 1e-8;
template<typename T>
struct Segment{
    // p1.x < p2.x
    Line<T> base;
    Point<T> p1, p2;
    Segment(): base(Line<T>()), p1(Point<T>()), p2(
        Point<T>()) {
        assert(on_line(p1, base) and on_line(p2, base))
    }
    Segment(Line<T> _, Point<T> __, Point<T> ___): base
        (_, p1(__), p2(___)) {
        assert(on_line(p1, base) and on_line(p2, base))
    }
}
template<typename T2>
Segment(const Segment<T2>& _): base(_.base), p1(
    _.p1), p2(_.p2) {}
typedef Point<long double> Pt;
friend bool on_segment(const Point<T>& p, const
    Segment& l){
    if(on_line(p, l.base))
        return (l.p1.x-p.x)*(p.x-l.p2.x)>=0 and (l.
            p1.y-p.y)*(p.y-l.p2.y)>=0;
    return false;
}
friend bool have_inter(const Segment& a, const
    Segment& b){
    if(is_parallel(a.base, b.base)){
        return on_segment(a.p1, b) or on_segment(a.
            p2, b) or on_segment(b.p1, a) or
            on_segment(b.p2, a);
    }
    Pt inter = get_inter(a.base, b.base);
    return on_segment(inter, a) and on_segment(
        inter, b);
}
friend inline Pt get_inter(const Segment& a, const
    Segment& b){
    if(!have_inter(a, b)){
        return NOT_EXIST;
    } else if(is_parallel(a.base, b.base)){
        if(a.p1 == b.p1){
            if(on_segment(a.p2, b) or on_segment(b.
                p2, a)) return INF_P;
            else return a.p1;
        } else if(a.p1 == b.p2){
            if(on_segment(a.p2, b) or on_segment(b.
                p1, a)) return INF_P;
            else return a.p1;
        } else if(a.p2 == b.p1){
            if(on_segment(a.p1, b) or on_segment(b.
                p2, a)) return INF_P;
            else return a.p2;
        } else if(a.p2 == b.p2){
            if(on_segment(a.p1, b) or on_segment(b.
                p1, a)) return INF_P;
            else return a.p2;
        }
        return INF_P;
    }
    return get_inter(a.base, b.base);
}
friend ostream& operator<<(ostream& ss, const
    Segment& o){
    ss<<o.base<<"", "<<o.p1<<" ~ "<<o.p2;
    return ss;
}
};
template<typename T>
inline Segment<T> get_segment(const Point<T>& a, const
    Point<T>& b){
    return Segment<T>(get_line(a, b), a, b);
}
}
```

5.5 Triangle Circumcentre

```
template<typename T>
Circle<llf> get_circum(const Point<T>& a, const Point<T>
    & b, const Point<T>& c){
```

```
    llf a1 = a.x-b.x;
    llf b1 = a.y-b.y;
    llf c1 = (a.x+b.x)/2 * a1 + (a.y+b.y)/2 * b1;

    llf a2 = a.x-c.x;
    llf b2 = a.y-c.y;
    llf c2 = (a.x+c.x)/2 * a2 + (a.y+c.y)/2 * b2;

    Circle<llf> cc;
    cc.o.x = (c1*b2-b1*c2)/(a1*b2-b1*a2);
    cc.o.y = (a1*c2-c1*a2)/(a1*b2-b1*a2);
    cc.r = hypot(cc.o.x-a.x, cc.o.y-a.y);
    return cc;
}
```

5.6 2D Convex Hull

```
template<typename T>
class ConvexHull_2D{
private:
    typedef Point<T> PT;
    vector<PT> dots;
    struct myhash{
        uint64_t operator()(const PT& a) const {
            uint64_t xx=0, yy=0;
            memcpy(&xx, &a.x, sizeof(a.x));
            memcpy(&yy, &a.y, sizeof(a.y));
            uint64_t ret = xx*17+yy*31;
            ret = (ret ^ (ret >> 16))*0x9E3779B1;
            ret = (ret ^ (ret >> 13))*0xC2B2AE35;
            ret = ret ^ xx;
            return (ret ^ (ret << 3)) * yy;
        }
    };
    unordered_set<PT, myhash> in_hull;
public:
    inline void init(){in_hull.clear();dots.clear();}
    void insert(const PT& x){dots.pb(x);}
    void solve(){
        sort(ALL(dots), [](const PT& a, const PT& b){
            return tie(a.x, a.y) < tie(b.x, b.y);
        });
        vector<PT> stk(SZ(dots)<<1);
        int top = 0;
        for(auto p: dots){
            while(top >= 2 and cross(p-stk[top-2], stk[
                top-1]-stk[top-2]) <= 0)
                top--;
            stk[top++] = p;
        }
        for(int i=SZ(dots)-2, t = top+1; i>=0; i--){
            while(top >= t and cross(dots[i]-stk[top
                -2], stk[top-1]-stk[top-2]) <= 0)
                top--;
            stk[top++] = dots[i];
        }
        stk.resize(top-1);
        swap(stk, dots);
        for(auto i: stk) in_hull.insert(i);
    }
    vector<PT> get(){return dots;}
    inline bool in_it(const PT& x){
        return in_hull.find(x)!=in_hull.end();
    }
};
```

5.7 2D Farthest Pair

```
// stk is from convex hull
n = (int)(stk.size());
int pos = 1, ans = 0; stk.push_back(arr[0]);
for(int i=0; i<n; i++){
    while(abs(cross(stk[i+1]-stk[i], stk[(pos+1)%n]-stk
        [i]))\
        > abs(cross(stk[i+1]-stk[i], stk[pos]-stk[i]
            ))) pos = (pos+1)%n;
    ans = max({ans, dis(stk[i], stk[pos]), dis(stk[i
        +1], stk[pos])});
}
```

5.8 SimulateAnnealing

```
#include <random>
#include <functional>
#include <utility>
#include <algorithm>
using namespace std;

double getY(double);

int main(){
    int rr, ll;
    default_random_engine rEng(time(NULL));
    uniform_real_distribution<double> Range(-1,1);
    uniform_real_distribution<double> expR(0,1);
    auto Random=bind(Range,rEng);
    auto expRand=bind(expR,rEng);
    int step=0;
    double pace=rr-ll, mini=0.95; // need to search for
    it
    double x=max(min(Random()*pace+ll, rr), ll), y=getY
    (x);
    while(pace>=1e-7){
        double newX = max(min(x + Random()*pace, rr),
        ll);
        double newY = getY(newX);
        if(newY < y || expRand() < exp(-step))
            x=newX, y=newY;
        step++;
        pace*=mini;
    }

    double getY(double x){
        // get y using x
        return x;
    }
```

5.9 Minimum Covering Circle

```
template<typename T>
Circle<llf> MinCircleCover(const vector<Point<T>>& pts)
{
    random_shuffle(ALL(pts));
    Circle<llf> c = {pts[0], 0};
    int n = SZ(pts);
    for(int i=0;i<n;i++){
        if(pts[i].in(c)) continue;
        c = {pts[i], 0};
        for(int j=0;j<i;j++){
            if(pts[j].in(c)) continue;
            c.o = (pts[i] + pts[j]) / 2;
            c.r = pts[i].dis(c.o);
            for(int k=0;k<j;k++){
                if(pts[k].in(c)) continue;
                c = get_circum(pts[i], pts[j], pts[k]);
            }
        }
    }
    return c;
}
```

5.10 KDTree (Nearest Point)

```
const int MXN = 100005;
struct KDTree {
    struct Node {
        int x,y,x1,y1,x2,y2;
        int id,f;
        Node *L, *R;
    } tree[MXN];
    int n;
    Node *root;
    LL dis2(int x1, int y1, int x2, int y2) {
        LL dx = x1-x2;
        LL dy = y1-y2;
        return dx*dx+dy*dy;
    }
    static bool cmpx(Node& a, Node& b){ return a.x<b.x; }
    static bool cmpy(Node& a, Node& b){ return a.y<b.y; }
    void init(vector<pair<int,int>> ip) {
```

```
n = ip.size();
    for (int i=0; i<n; i++) {
        tree[i].id = i;
        tree[i].x = ip[i].first;
        tree[i].y = ip[i].second;
    }
    root = build_tree(0, n-1, 0);
}

Node* build_tree(int L, int R, int dep) {
    if (L>R) return nullptr;
    int M = (L+R)/2;
    tree[M].f = dep%2;
    nth_element(tree+L, tree+M, tree+R+1, tree[M].f ?
    cmpy : cmpx);
    tree[M].x1 = tree[M].x2 = tree[M].x;
    tree[M].y1 = tree[M].y2 = tree[M].y;

    tree[M].L = build_tree(L, M-1, dep+1);
    if (tree[M].L) {
        tree[M].x1 = min(tree[M].x1, tree[M].L->x1);
        tree[M].x2 = max(tree[M].x2, tree[M].L->x2);
        tree[M].y1 = min(tree[M].y1, tree[M].L->y1);
        tree[M].y2 = max(tree[M].y2, tree[M].L->y2);
    }
    tree[M].R = build_tree(M+1, R, dep+1);
    if (tree[M].R) {
        tree[M].x1 = min(tree[M].x1, tree[M].R->x1);
        tree[M].x2 = max(tree[M].x2, tree[M].R->x2);
        tree[M].y1 = min(tree[M].y1, tree[M].R->y1);
        tree[M].y2 = max(tree[M].y2, tree[M].R->y2);
    }
    return tree+M;
}

int touch(Node* r, int x, int y, LL d2) {
    LL dis = sqrt(d2)+1;
    if (x<r->x1-dis || x>r->x2+dis ||
        y<r->y1-dis || y>r->y2+dis)
        return 0;
    return 1;
}

void nearest(Node* r, int x, int y,
    int &mID, LL &md2){
    if (!r || !touch(r, x, y, md2)) return;
    LL d2 = dis2(r->x, r->y, x, y);
    if (d2 < md2 || (d2 == md2 && mID < r->id)) {
        mID = r->id;
        md2 = d2;
    }
    // search order depends on split dim
    if ((r->f == 0 && x < r->x) ||
        (r->f == 1 && y < r->y)) {
        nearest(r->L, x, y, mID, md2);
        nearest(r->R, x, y, mID, md2);
    } else {
        nearest(r->R, x, y, mID, md2);
        nearest(r->L, x, y, mID, md2);
    }
}

int query(int x, int y) {
    int id = 1029384756;
    LL d2 = 102938475612345678LL;
    nearest(root, x, y, id, d2);
    return id;
}

}tree;
```

6 Stringology

6.1 Hash

```
#include <string>
typedef long long lld;
const int N = 1000000;
class Hash{
private:
    const lld p = 127, q = 1208220623;
    int sz;
    lld prefix[N], power[N];
public:
    void init(const std::string &x) {
        sz = x.size();
        prefix[0]=0;
```

```

    for(int i=1;i<=sz;i++) prefix[i]=(prefix[i-1]*
        p)%q+x[i-1]%q;
    power[0]=1;
    for(int i=1;i<=sz;i++) power[i]=(power[i-1]*p)%
        q;
}
lld query(int l, int r){
    // 1-base (l, r)
    return (prefix[r] - (prefix[l]*power[r-l])%q +
        q)%q;
}
};

```

6.2 Suffix Array

```

//help by http://www.geeksforgeeks.org/suffix-array-set
-2-a-nlognlogn-algorithm/
#include <bits/stdc++.h>
using namespace std;
#define PB push_back

struct sfx{
    int index;
    int r,nr;
};

char str[N + 10];
int len;

vector<sfx> srs[N + 10];
int mapping[N + 10];
sfx sa[N + 10];

bool cmp(sfx a,sfx b){
    if(a.r==b.r){
        return a.nr<b.nr;
    }else{
        return a.r<b.r;
    }
}

void SA();
void radixSort();

int main(){
    gets(str);
    len = strlen(str);
    SA();
    for(int i=0;i<len;i++){
        printf("%d\n",sa[i].index);
    }
    return 0;
}

void SA(){
    for(int i=0;i<len;i++){
        sa[i].index = i;
        sa[i].r=str[i];
        sa[i].nr=(i+1>len)?0:str[i+1];
    }
    //sort(sa,sa+len,cmp);
    radixSort();
    for(int j=2;j<=len;j*=2){
        int cnt=1;
        int rr = sa[0].r;
        sa[0].r=cnt;
        mapping[sa[0].index]=0;
        for(int i=1;i<len;i++){
            if(sa[i].r == rr && sa[i].nr == sa[i-1].nr)
                {
                    rr=sa[i].r;
                    sa[i].r=cnt;
                }else{
                    rr=sa[i].r;
                    sa[i].r=++cnt;
                }
            mapping[sa[i].index]=i;
        }
        for(int i=0;i<len;i++){
            int nn = sa[i].index+j;
            sa[i].nr = (nn>len)?0:sa[mapping[nn]].r;
        }
        //sort(sa, sa+len, cmp);
        radixSort();
    }
}

```

```

}
}

void radixSort(){
    int m = 0;
    for(int i=0;i<len;i++){
        srs[sa[i].nr].PB(sa[i]);
        m=max(m,sa[i].nr);
    }
    int cnt=0;
    for(int i=0;i<=m;i++){
        if(srs[i].empty()) continue;
        for(auto j:srs[i]){
            sa[cnt++] = j;
        }
        srs[i].clear();
    }
    m = 0;
    for(int i=0;i<len;i++){
        srs[sa[i].r].PB(sa[i]);
        m=max(m,sa[i].r);
    }
    cnt=0;
    for(int i=0;i<=m;i++){
        if(srs[i].empty()) continue;
        for(auto j:srs[i]){
            sa[cnt++] = j;
        }
        srs[i].clear();
    }
}
}

```

6.3 KMP

```

int F[N<<1];
void KMP(char s1[], char s2[], int n, int m){
    // make F[] for s1+'\0'+s2;
    char ss[N<<1];
    int len = n+m+1;
    for(int i=0;i<n;i++) ss[i] = s1[i];
    ss[n] = '\0';
    for(int i=0;i<m;i++) ss[i+n] = s2[i];
    F[0] = F[1] = 0;
    for(int i=1;i<len;i++){
        int j = F[i];
        while(j > 0 and ss[i]!=ss[j]) j = F[j];
        F[i+1] = (ss[i]==ss[j]?j+1:0);
    }
    // just find (F[len2+i] == len2), i from 1 to len+1
    for matching
}

```

6.4 Z value

```

char s[MAXN];
int len,z[MAXN];
void Z_value(){
    int i,j,left,right;
    left=right=0; z[0]=len;
    for(i=1;i<len;i++){
        j=max(min(z[i-left],right-i),0);
        for(;i+j<len&&s[i+j]==s[j];j++);
        z[i]=j;
        if(i+z[i]>right){
            right=i+z[i];
            left=i;
        }
    }
}

```

6.5 Lexicographically Smallest Rotation

```

string mcp(string s){
    int n = s.length();
    s += s;
    int i=0, j=1;
    while (i<n && j<n){
        int k = 0;
        while (k < n && s[i+k] == s[j+k]) k++;
    }
}

```



```
    if (s[i+k] <= s[j+k]) j += k+1;
    else i += k+1;
    if (i == j) j++;
}
int ans = i < n ? i : j;
return s.substr(ans, n);
}
```