Contents

	_				7.2 Suffix Array
1	Bas	IC	1		7.3 Suffix Automaton
	1.1	vimrc	1		7.4 KMP _.
	1.2	Debue Macro	1		7.5 Z value
	1.3	Increase Stack	1		7.6 Manacher
	1.4	Pragma Optimization	2		7.7 Lexico Smallest Rotation
	1.5	- •	2		7.8 BWT
	1.5	IO Optimization	2		7.9 Palindromic Tree
_		•	_		7.5 Talliaroniic free
2	Date	a Structure	2	0	Micc
	2.1	Dark Magic	2		Misc 2
		Link-Cut Tree	2		8.1 Theorems
					8.1.1 Kirchhoff's Theorem
		LiChao Segment Tree	2		8.1.2 Tutte's Matrix
	2.4	Treap	3		
	2.5	Sparse Table	3		
		•			8.1.4 Erdős–Gallai theorem
	2.6	Linear Basis	3		8.1.5 Havel-Hakimi algorithm
					8.1.6 Hall's marriage theorem
3	Gra	ph	3		8.1.7 Euler's planar graph formula
	3.1	BCC Edge	3		, , ,
			4		8.1.8 Pick's theorem
		BCC Vertex	4		8.1.9 Lucas's theorem
	3.3	2-SAT (SCC)	4		8.1.10 Matroid Intersection
	3.4	Lowbit Decomposition	4		
			5		8.2 DP-opt Condition
		MaxClique			8.2.1 totally monotone (concave/convex)
	3.6	MaxCliqueDyn	5		8.2.2 monge condition (concave/convex) 2
	3.7	Virtural Tree	6		8.3 Convex 1D/1D DP
	3.8	Centroid Decomposition	6		8.4 ConvexHull Optimization
		· · · · · · · · · · · · · · · · · · ·			·
		Tree Hashing	6		8.5 Josephus Problem
	3.10	Minimum Mean Cycle	7		8.6 Cactus Matching
	3.11	Mo's Algorithm on Tree	7		8.7 DLX
		Minimum Steiner Tree	7		8.8 Tree Knapsack
			,		·
	3.13	Directed Minimum Spanning Tree	8		8.9 N Queens Problem
	3.14	Dominator Tree	8		8.10 Aliens Optimization
			8		
	ر1.ر	Edge Coloring	0	1	Racic
				ı	Basic
4	Mat	ching & Flow	9		
	4.1	Kuhn Munkres	9	1.1	vimrc
		Bipartite Matching	۵		
			,	se	is nu rnu bs=2 ru mouse=a encoding=utf-8
	4.3	General Graph Matching	9		▼
	4.4	Minimum Weight Matching (Clique version)	10	se	cin et sw=4 sts=4 t_Co=256 tgc sc hls ls=2
		Minimum Cost Circulation	10	sy	n on
				200	lorscheme desert
		Flow Models	10		
	4.7	Dinic	11	fi.	letype indent on
	4.8	Minimum Cost Maximum Flow	11	in	oremap { <cr> {<cr>}<esc>0</esc></cr></cr>
	4.9	Global Min-Cut	12	ma	p <f8> <esc>:w<cr>:!g++ "%" -o "%<" -02 -std=c++17 -</cr></esc></f8>
					DKISEKI -Wall -Wextra -Wshadow -Wfatal-errors -
5	Mat	h	12	i	Wconversion -fsanitize=address -fsanitize=undefined
	5.1	Prime Table	12	ļ	
					-g && echo success <cr></cr>
		n Enumeration	12		
		$\lfloor \frac{n}{i} \rfloor$ Enumeration	12	mai	p <f9> <esc>:w<cr>:!a++ "%" -o "%<" -02 -std=c++17 -</cr></esc></f9>
		$\lfloor \frac{n}{i} \rfloor$ Enumeration	12 12	ma	p <f9> <esc>:w<cr>:!g++ "%" -o "%<" -02 -std=c++17 -</cr></esc></f9>
	5.3				DKISEKI && echo success <cr></cr>
	5.3 5.4	ax+by=gcd	12 12		
	5.3 5.4 5.5	ax+by=gcd Pollard Rho Pi Count (Linear Sieve)	12 12 12		DKISEKI && echo success <cr></cr>
	5.3 5.4 5.5	ax+by=gcd Pollard Rho Pi Count (Linear Sieve) Strling Number	12 12 12 13	ma	DKISEKI && echo success <cr> p <f10> <esc>:!./"%<"<cr></cr></esc></f10></cr>
	5.3 5.4 5.5	ax+by=gcd Pollard Rho Pi Count (Linear Sieve)	12 12 12		DKISEKI && echo success <cr> p <f10> <esc>:!./"%<"<cr></cr></esc></f10></cr>
	5.3 5.4 5.5	ax+by=gcd Pollard Rho Pi Count (Linear Sieve) Strling Number	12 12 12 13 13	ma ₁	DKISEKI && echo success <cr> p <f10> <esc>:!./"%<"<cr> Debue Macro</cr></esc></f10></cr>
	5.3 5.4 5.5 5.6	ax+by=gcd Pollard Rho Pi Count (Linear Sieve) Strling Number 5.6.1 First Kind 5.6.2 Second Kind	12 12 12 13 13	ma ₁	DKISEKI && echo success <cr> p <f10> <esc>:!./"%<"<cr></cr></esc></f10></cr>
	5.3 5.4 5.5 5.6	ax+by=gcd Pollard Rho Pi Count (Linear Sieve) Strling Number 5.6.1 First Kind 5.6.2 Second Kind Range Sieve	12 12 12 13 13 13	1.2	DKISEKI && echo success <cr> p <f10> <esc>:!./"%<"<cr> Debue Macro fdef KISEKI</cr></esc></f10></cr>
	5.3 5.4 5.5 5.6	ax+by=gcd Pollard Rho Pi Count (Linear Sieve) Strling Number 5.6.1 First Kind 5.6.2 Second Kind	12 12 12 13 13 13	1.2	DKISEKI && echo success <cr> p <f10> <esc>:!./"%<"<cr> Debue Macro fdef KISEKI efine safe cerr<<pretty_function\< td=""></pretty_function\<></cr></esc></f10></cr>
	5.3 5.4 5.5 5.6 5.7 5.8	ax+by=gcd Pollard Rho Pi Count (Linear Sieve) Strling Number 5.6.1 First Kind 5.6.2 Second Kind Range Sieve	12 12 12 13 13 13	1.2	DKISEKI && echo success <cr> p <f10> <esc>:!./"%<"<cr> Debue Macro fdef KISEKI efine safe cerr<<pretty_function\ "<<line<<"="" <<"="" line="" safe\n"<="" td=""></pretty_function\></cr></esc></f10></cr>
	5.3 5.4 5.5 5.6 5.7 5.8 5.9	ax+by=gcd Pollard Rho Pi Count (Linear Sieve) Strling Number 5.6.1 First Kind 5.6.2 Second Kind Range Sieve Miller Rabin Inverse Element	12 12 12 13 13 13 13 13 13	1.2	DKISEKI && echo success <cr> p <f10> <esc>:!./"%<"<cr> Debue Macro fdef KISEKI efine safe cerr<<pretty_function\ "<<line<<"="" <<"="" line="" safe\n"<="" td=""></pretty_function\></cr></esc></f10></cr>
	5.3 5.4 5.5 5.6 5.7 5.8 5.9 5.10	ax+by=gcd Pollard Rho Pi Count (Linear Sieve) Strling Number 5.6.1 First Kind 5.6.2 Second Kind Range Sieve Miller Rabin Inverse Element Extended Euler	12 12 12 13 13 13 13 13 13 13	1.2 #i #de	DKISEKI && echo success <cr> p <f10> <esc>:!./"%<"<cr> Debue Macro fdef KISEKI efine safe cerr<<pretty_function\ "<<line<<"="" <<"="" a)<="" debug(a)="" efine="" line="" qwerty(#a,="" safe\n"="" td=""></pretty_function\></cr></esc></f10></cr>
	5.3 5.4 5.5 5.6 5.7 5.8 5.9 5.10 5.11	ax+by=gcd Pollard Rho Pi Count (Linear Sieve) Strling Number 5.6.1 First Kind 5.6.2 Second Kind Range Sieve Miller Rabin Inverse Element Extended Euler Gauss Elimination	12 12 12 13 13 13 13 13 13	1.2 #i #de #de	DKISEKI && echo success <cr> p <f10> <esc>:!./"%<"<cr> Debue Macro fdef KISEKI efine safe cerr<<pretty_function\ "<<line<<"="" <<"="" a)="" a)<="" debug(a)="" dvorak(#a,="" efine="" line="" orange(a)="" qwerty(#a,="" safe\n"="" td=""></pretty_function\></cr></esc></f10></cr>
	5.3 5.4 5.5 5.6 5.7 5.8 5.9 5.10 5.11	ax+by=gcd Pollard Rho Pi Count (Linear Sieve) Strling Number 5.6.1 First Kind 5.6.2 Second Kind Range Sieve Miller Rabin Inverse Element Extended Euler	12 12 12 13 13 13 13 13 13 13	1.2 #i #de #de	DKISEKI && echo success <cr> p <f10> <esc>:!./"%<"<cr> Debue Macro fdef KISEKI efine safe cerr<<pretty_function\ "<<line<<"="" <<"="" a)<="" debug(a)="" efine="" line="" qwerty(#a,="" safe\n"="" td=""></pretty_function\></cr></esc></f10></cr>
	5.3 5.4 5.5 5.6 5.7 5.8 5.9 5.10 5.11 5.12	ax+by=gcd Pollard Rho Pi Count (Linear Sieve) Strling Number 5.6.1 First Kind 5.6.2 Second Kind Range Sieve Miller Rabin Inverse Element Extended Euler Gauss Elimination Fast Fourier Transform	12 12 13 13 13 13 13 13 13 13 13	#1.2 #1:#de #de #de us:	DKISEKI && echo success <cr> p <f10> <esc>:!./"%<"<cr> Debue Macro fdef KISEKI efine safe cerr<<pretty_function\ "<<line<<"="" <<"="" a)="" debug(a)="" dvorak(#a,="" efine="" ing="" line="" orange(a)="" qwerty(#a,="" safe\n"="" std::cerr;<="" td=""></pretty_function\></cr></esc></f10></cr>
	5.3 5.4 5.5 5.6 5.7 5.8 5.9 5.10 5.11 5.12 5.13	ax+by=gcd Pollard Rho Pi Count (Linear Sieve) Strling Number 5.6.1 First Kind 5.6.2 Second Kind Range Sieve Miller Rabin Inverse Element Extended Euler Gauss Elimination Fast Fourier Transform Chinese Remainder	12 12 13 13 13 13 13 13 13 13 14	#1.2 #1.2 #de #de us:	DKISEKI && echo success <cr> p <f10> <esc>:!./"%<"<cr> Debue Macro fdef KISEKI efine safe cerr<<pretty_function\ "<<line<<"="" <<"="" <typenamet="" a)="" debug(a)="" dvorak(#a,="" efine="" ing="" line="" mplate="" orange(a)="" qwerty(#a,="" safe\n"="" std::cerr;=""></pretty_function\></cr></esc></f10></cr>
	5.3 5.4 5.5 5.6 5.7 5.8 5.9 5.10 5.11 5.12 5.13 5.14	ax+by=gcd Pollard Rho Pi Count (Linear Sieve) Strling Number 5.6.1 First Kind 5.6.2 Second Kind Range Sieve Miller Rabin Inverse Element Extended Euler Gauss Elimination Fast Fourier Transform Chinese Remainder Berlekamp Massey	12 12 12 13 13 13 13 13 13 13 14 14	#1.2 #1.2 #dd #dd us: ter	DKISEKI && echo success <cr> p <f10> <esc>:!./"%<"<cr> Debue Macro fdef KISEKI efine safe cerr<<pretty_function\ "<<line<<"="" <<"="" <typenamet="" a)="" debug(a)="" dvorak(#a,="" efine="" ing="" line="" mplate="" orange(a)="" qwerty(#a,="" safe\n"="" std::cerr;=""> id qwerty(const char *s, Ta) {</pretty_function\></cr></esc></f10></cr>
	5.3 5.4 5.5 5.6 5.7 5.8 5.9 5.10 5.11 5.12 5.13 5.14	ax+by=gcd Pollard Rho Pi Count (Linear Sieve) Strling Number 5.6.1 First Kind 5.6.2 Second Kind Range Sieve Miller Rabin Inverse Element Extended Euler Gauss Elimination Fast Fourier Transform Chinese Remainder	12 12 13 13 13 13 13 13 13 13 14	#1.2 #1.2 #dd #dd us: ter	DKISEKI && echo success <cr> p <f10> <esc>:!./"%<"<cr> Debue Macro fdef KISEKI efine safe cerr<<pretty_function\ "<<line<<"="" <<"="" <typenamet="" a)="" debug(a)="" dvorak(#a,="" efine="" ing="" line="" mplate="" orange(a)="" qwerty(#a,="" safe\n"="" std::cerr;=""> id qwerty(const char *s, Ta) {</pretty_function\></cr></esc></f10></cr>
	5.3 5.4 5.5 5.6 5.7 5.8 5.9 5.10 5.11 5.12 5.13 5.14 5.15	ax+by=gcd Pollard Rho Pi Count (Linear Sieve) Strling Number 5.6.1 First Kind 5.6.2 Second Kind Range Sieve Miller Rabin Inverse Element Extended Euler Gauss Elimination Fast Fourier Transform Chinese Remainder Berlekamp Massey NTT	12 12 13 13 13 13 13 13 13 14 14 14	#1.2 #1.2 #de #de us: ter	DKISEKI && echo success <cr> p <f10> <esc>:!./"%<"<cr> Debue Macro fdef KISEKI efine safe cerr<<pretty_function\ "<<line<<"="" <<"="" <typenamet="" a)="" debug(a)="" dvorak(#a,="" efine="" ing="" line="" mplate="" orange(a)="" qwerty(#a,="" safe\n"="" std::cerr;=""> id qwerty(const char *s, Ta) { cerr << "\e[1;32m(" << s << ") = (";</pretty_function\></cr></esc></f10></cr>
	5.3 5.4 5.5 5.6 5.7 5.8 5.9 5.10 5.11 5.12 5.13 5.14 5.15 5.16	ax+by=gcd Pollard Rho Pi Count (Linear Sieve) Strling Number 5.6.1 First Kind 5.6.2 Second Kind Range Sieve Miller Rabin Inverse Element Extended Euler Gauss Elimination Fast Fourier Transform Chinese Remainder Berlekamp Massey NTT Polynomial Operations	12 12 13 13 13 13 13 13 13 13 14 14 14	#1.2 #1 #de #de us: tell vo:	DKISEKI && echo success <cr> p <f10> <esc>:!./"%<"<cr> Debue Macro fdef KISEKI efine safe cerr<<pretty_function\ "<<line<<"="" <<"="" <typenamet="" a)="" debug(a)="" dvorak(#a,="" efine="" ing="" line="" mplate="" orange(a)="" qwerty(#a,="" safe\n"="" std::cerr;=""> id qwerty(const char *s, Ta) { cerr << "\e[1;32m(" << s << ") = ("; int cnt = sizeof(T);</pretty_function\></cr></esc></f10></cr>
	5.3 5.4 5.5 5.6 5.7 5.8 5.9 5.10 5.12 5.13 5.14 5.15 5.16 5.17	ax+by=gcd Pollard Rho Pi Count (Linear Sieve) Strling Number 5.6.1 First Kind 5.6.2 Second Kind Range Sieve Miller Rabin Inverse Element Extended Euler Gauss Elimination Fast Fourier Transform Chinese Remainder Berlekamp Massey NTT Polynomial Operations FWT	12 12 13 13 13 13 13 13 13 14 14 14 14 15	#1.2 #1 #de #de us: tell vo:	DKISEKI && echo success <cr> p <f10> <esc>:!./"%<"<cr> Debue Macro fdef KISEKI efine safe cerr<<pretty_function\ "<<line<<"="" <<"="" <typenamet="" a)="" debug(a)="" dvorak(#a,="" efine="" ing="" line="" mplate="" orange(a)="" qwerty(#a,="" safe\n"="" std::cerr;=""> id qwerty(const char *s, Ta) { cerr << "\e[1;32m(" << s << ") = (";</pretty_function\></cr></esc></f10></cr>
	5.3 5.4 5.5 5.6 5.7 5.8 5.9 5.10 5.12 5.13 5.14 5.15 5.16 5.17 5.18	ax+by=gcd Pollard Rho Pi Count (Linear Sieve) Strling Number 5.6.1 First Kind 5.6.2 Second Kind Range Sieve Miller Rabin Inverse Element Extended Euler Gauss Elimination Fast Fourier Transform Chinese Remainder Berlekamp Massey NTT Polynomial Operations FWT DiscreteLog	12 12 13 13 13 13 13 13 13 14 14 14 14 15 16	#1.2 #1 #de #de us: tell vo:	DKISEKI && echo success <cr> p <f10> <esc>:!./"%<"<cr> Debue Macro fdef KISEKI efine safe cerr<<pretty_function\ "<<line<<"="" <<"="" <typenamet="" a)="" debug(a)="" dvorak(#a,="" efine="" ing="" line="" mplate="" orange(a)="" qwerty(#a,="" safe\n"="" std::cerr;=""> id qwerty(const char *s, Ta) { cerr << "\e[1;32m(" << s << ") = ("; int cnt = sizeof(T);</pretty_function\></cr></esc></f10></cr>
	5.3 5.4 5.5 5.6 5.7 5.8 5.9 5.10 5.12 5.13 5.14 5.15 5.16 5.17 5.18	ax+by=gcd Pollard Rho Pi Count (Linear Sieve) Strling Number 5.6.1 First Kind 5.6.2 Second Kind Range Sieve Miller Rabin Inverse Element Extended Euler Gauss Elimination Fast Fourier Transform Chinese Remainder Berlekamp Massey NTT Polynomial Operations FWT	12 12 13 13 13 13 13 13 13 14 14 14 14 15 16	#1.2 #1.2 #d. #d. #d. us tel vo.	DKISEKI && echo success <cr> p <f10> <esc>:!./"%<"<cr> Debue Macro fdef KISEKI efine safe cerr<<pretty_function\ "<<line<<"="" <<"="" <typenamet="" a)="" debug(a)="" dvorak(#a,="" efine="" ing="" line="" mplate="" orange(a)="" qwerty(#a,="" safe\n"="" std::cerr;=""> id qwerty(const char *s, Ta) { cerr << "\e[1;32m(" << s << ") = ("; int cnt = sizeof(T); (, (cerr << a << (cnt ? ", " : ")\e[0m\n")));</pretty_function\></cr></esc></f10></cr>
	5.3 5.4 5.5 5.6 5.7 5.8 5.9 5.10 5.11 5.12 5.13 5.14 5.15 5.16 5.17 5.18 5.19	ax+by=gcd Pollard Rho Pi Count (Linear Sieve) Strling Number 5.6.1 First Kind 5.6.2 Second Kind Range Sieve Miller Rabin Inverse Element Extended Euler Gauss Elimination Fast Fourier Transform Chinese Remainder Berlekamp Massey NTT Polynomial Operations FWT DiscreteLog FloorSum	12 12 13 13 13 13 13 13 13 14 14 14 14 15 16 16	#1.2 #1.2 #1.2 #1.2 #1.2 #1.2 #1.2 #1.2	<pre>DKISEKI && echo success<cr> p <f10> <esc>:!./"%<"<cr> 2 Debue Macro fdef KISEKI efine safe cerr<<pretty_function\ "<<_line<<"="" <<"="" <typenamet="" a)="" debug(a)="" dvorak(#a,="" efine="" ing="" line="" mplate="" orange(a)="" qwerty(#a,="" safe\n"="" std::cerr;=""> id qwerty(const char *s, Ta) { cerr << "\e[1;32m(" << s << ") = ("; int cnt = sizeof(T); (, (cerr << a << (cnt ? ", " : ")\e[0m\n"))); mplate <typename iter=""></typename></pretty_function\></cr></esc></f10></cr></pre>
	5.3 5.4 5.5 5.6 5.7 5.8 5.9 5.10 5.11 5.12 5.13 5.14 5.15 5.16 5.17 5.18 5.19 5.20	ax+by=gcd Pollard Rho Pi Count (Linear Sieve) Strling Number 5.6.1 First Kind 5.6.2 Second Kind Range Sieve Miller Rabin Inverse Element Extended Euler Gauss Elimination Fast Fourier Transform Chinese Remainder Berlekamp Massey NTT Polynomial Operations FWT DiscreteLog FloorSum Quadratic residue	12 12 13 13 13 13 13 13 13 14 14 14 14 15 16 16	#1.2 #1.2 #1.2 #1.2 #1.2 #1.2 #1.2 #1.2	<pre>DKISEKI && echo success<cr> p <f10> <esc>:!./"%<"<cr> 2 Debue Macro fdef KISEKI efine safe cerr<<pretty_function\ "<<_line<<"="" <<"="" <typenamet="" a)="" debug(a)="" dvorak(#a,="" efine="" ing="" line="" mplate="" orange(a)="" qwerty(#a,="" safe\n"="" std::cerr;=""> id qwerty(const char *s, Ta) { cerr << "\e[1;32m(" << s << ") = ("; int cnt = sizeof(T); (, (cerr << a << (cnt ? ", " : ")\e[0m\n"))); mplate <typename iter=""></typename></pretty_function\></cr></esc></f10></cr></pre>
	5.3 5.4 5.5 5.6 5.7 5.8 5.9 5.10 5.12 5.13 5.14 5.15 5.16 5.17 5.18 5.19 5.20 5.21	ax+by=gcd Pollard Rho Pi Count (Linear Sieve) Strling Number 5.6.1 First Kind 5.6.2 Second Kind Range Sieve Miller Rabin Inverse Element Extended Euler Gauss Elimination Fast Fourier Transform Chinese Remainder Berlekamp Massey NTT Polynomial Operations FWT DiscreteLog FloorSum Quadratic residue De-Bruijn	12 12 13 13 13 13 13 13 13 14 14 14 14 15 16 16	#1.2 #1.2 #1.2 #1.2 #1.2 #1.2 #1.2 #1.2	DKISEKI && echo success <cr> p <f10> <esc>:!./"%<"<cr> Debue Macro fdef KISEKI efine safe cerr<<pretty_function\ "<<line<<"="" <<"="" <typenamet="" a)="" debug(a)="" dvorak(#a,="" efine="" ing="" line="" mplate="" orange(a)="" qwerty(#a,="" safe\n"="" std::cerr;=""> id qwerty(const char *s, Ta) { cerr << "\e[1;32m(" << s << ") = ("; int cnt = sizeof(T); (, (cerr << a << (cnt ? ", " : ")\e[0m\n"))); mplate <typename iter=""> id dvorak(const char *s, Iter L, Iter R) {</typename></pretty_function\></cr></esc></f10></cr>
	5.3 5.4 5.5 5.6 5.7 5.8 5.9 5.10 5.12 5.13 5.14 5.15 5.16 5.17 5.18 5.19 5.20 5.21	ax+by=gcd Pollard Rho Pi Count (Linear Sieve) Strling Number 5.6.1 First Kind 5.6.2 Second Kind Range Sieve Miller Rabin Inverse Element Extended Euler Gauss Elimination Fast Fourier Transform Chinese Remainder Berlekamp Massey NTT Polynomial Operations FWT DiscreteLog FloorSum Quadratic residue	12 12 13 13 13 13 13 13 13 14 14 14 14 15 16 16	ma 1.2 #ii #dd #dd us tel vo	DKISEKI && echo success <cr> p <f10> <esc>:!./"%<"<cr> 2 Debue Macro fdef KISEKI efine safe cerr<<pretty_function\ "<<line<<"="" <<"="" <typenamet="" a)="" debug(a)="" dvorak(#a,="" efine="" ing="" line="" mplate="" orange(a)="" qwerty(#a,="" safe\n"="" std::cerr;=""> id qwerty(const char *s, Ta) { cerr << "\e[1;32m(" << s << ") = ("; int cnt = sizeof(T); (, (cerr << a << (cnt ? ", " : ")\e[0m\n"))); mplate <typename iter=""> id dvorak(const char *s, Iter L, Iter R) { cerr << "\e[1;32m[" << s << "] = [";</typename></pretty_function\></cr></esc></f10></cr>
	5.3 5.4 5.5 5.6 5.7 5.8 5.9 5.10 5.12 5.13 5.14 5.15 5.16 5.17 5.18 5.19 5.20 5.21 5.22	ax+by=gcd Pollard Rho Pi Count (Linear Sieve) Strling Number 5.6.1 First Kind 5.6.2 Second Kind Range Sieve Miller Rabin Inverse Element Extended Euler Gauss Elimination Fast Fourier Transform Chinese Remainder Berlekamp Massey NTT Polynomial Operations FWT DiscreteLog FloorSum Quadratic residue De-Bruijn Simplex Construction	12 12 13 13 13 13 13 13 13 14 14 14 15 16 16 16	ma 1.2 #ii #dd #dd us tel vo	DKISEKI && echo success <cr> p <f10> <esc>:!./"%<" <cr> Debue Macro fdef KISEKI efine safe cerr<<pretty_function\ "<<line<<"="" <<"="" <typenamet="" a)="" debug(a)="" dvorak(#a,="" efine="" ing="" line="" mplate="" orange(a)="" qwerty(#a,="" safe\n"="" std::cerr;=""> id qwerty(const char *s, Ta) { cerr << "\e[1;32m(" << s << ") = ("; int cnt = sizeof(T); (, (cerr << a << (cnt ? ", " : ")\e[0m\n"))); mplate <typename iter=""> id dvorak(const char *s, Iter L, Iter R) { cerr << "\e[1;32m[" << s << "] = ["; for (int f = 0 : l = R : ++l)</typename></pretty_function\></cr></esc></f10></cr>
	5.3 5.4 5.5 5.6 5.7 5.8 5.9 5.10 5.12 5.13 5.14 5.15 5.16 5.17 5.18 5.19 5.20 5.21 5.22	ax+by=gcd Pollard Rho Pi Count (Linear Sieve) Strling Number 5.6.1 First Kind 5.6.2 Second Kind Range Sieve Miller Rabin Inverse Element Extended Euler Gauss Elimination Fast Fourier Transform Chinese Remainder Berlekamp Massey NTT Polynomial Operations FWT DiscreteLog FloorSum Quadratic residue De-Bruijn	12 12 13 13 13 13 13 13 13 14 14 14 15 16 16 16 16	ma 1.2 #ii #dd #dd us tel vo	DKISEKI && echo success <cr> p <f10> <esc>:!./"%<" <cr> Debue Macro fdef KISEKI efine safe cerr<<pretty_function\ "<<line<<"="" <<"="" <typenamet="" a)="" debug(a)="" dvorak(#a,="" efine="" ing="" line="" mplate="" orange(a)="" qwerty(#a,="" safe\n"="" std::cerr;=""> id qwerty(const char *s, Ta) { cerr << "\e[1;32m(" << s << ") = ("; int cnt = sizeof(T); (, (cerr << a << (cnt ? ", " : ")\e[0m\n"))); mplate <typename iter=""> id dvorak(const char *s, Iter L, Iter R) { cerr << "\e[1;32m[" << s << "] = ["; for (int f = 0 : l = R : ++l)</typename></pretty_function\></cr></esc></f10></cr>
6	5.3 5.4 5.5 5.6 5.7 5.8 5.10 5.12 5.13 5.14 5.15 5.16 5.17 5.19 5.20 5.21 5.22 5.23	ax+by=gcd Pollard Rho Pi Count (Linear Sieve) Strling Number 5.6.1 First Kind 5.6.2 Second Kind Range Sieve Miller Rabin Inverse Element Extended Euler Gauss Elimination Fast Fourier Transform Chinese Remainder Berlekamp Massey NTT Polynomial Operations FWT DiscreteLog FloorSum Quadratic residue De-Bruijn Simplex Construction	12 12 13 13 13 13 13 13 13 14 14 14 15 16 16 16 16	#1.2 #1.2 #d. #d. #d. us. tel vo. } tel vo.	DKISEKI && echo success <cr> p <f10> <esc>:!./"%<"<cr> Debue Macro fdef KISEKI efine safe cerr<<pretty_function\ "<<line<<"="" <<"="" <typenamet="" a)="" debug(a)="" dvorak(#a,="" efine="" ing="" line="" mplate="" orange(a)="" qwerty(#a,="" safe\n"="" std::cerr;=""> id qwerty(const char *s, Ta) { cerr << "\e[1;32m(" << s << ") = ("; int cnt = sizeof(T); (, (cerr << a << (cnt ? ", " : ")\e[0m\n"))); mplate <typename iter=""> id dvorak(const char *s, Iter L, Iter R) { cerr << "\e[1;32m[" << s << "] = ["; for (int f = 0; L != R; ++L) cerr << (f++ ? ", " : "") << *L;</typename></pretty_function\></cr></esc></f10></cr>
6	5.3 5.4 5.5 5.6 5.7 5.8 5.9 5.10 5.12 5.13 5.14 5.15 5.19 5.20 5.21 5.22 5.23 Geo	ax+by=gcd Pollard Rho Pi Count (Linear Sieve) Strling Number 5.6.1 First Kind 5.6.2 Second Kind Range Sieve Miller Rabin Inverse Element Extended Euler Gauss Elimination Fast Fourier Transform Chinese Remainder Berlekamp Massey NTT Polynomial Operations FWT DiscreteLog FloorSum Quadratic residue De-Bruijn Simplex Description DiscreteLog Simplex Description DiscreteLog Simplex Description	12 12 12 13 13 13 13 13 13 13 14 14 14 15 16 16 16 16 16 16	#1.2 #1.2 #d. #d. #d. us. tel vo. } tel vo.	DKISEKI && echo success <cr> p <f10> <esc>:!./"%<" <cr> Debue Macro fdef KISEKI efine safe cerr<<pretty_function\ "<<line<<"="" <<"="" <typenamet="" a)="" debug(a)="" dvorak(#a,="" efine="" ing="" line="" mplate="" orange(a)="" qwerty(#a,="" safe\n"="" std::cerr;=""> id qwerty(const char *s, Ta) { cerr << "\e[1;32m(" << s << ") = ("; int cnt = sizeof(T); (, (cerr << a << (cnt ? ", " : ")\e[0m\n"))); mplate <typename iter=""> id dvorak(const char *s, Iter L, Iter R) { cerr << "\e[1;32m[" << s << "] = ["; for (int f = 0 : l = R : ++l)</typename></pretty_function\></cr></esc></f10></cr>
6	5.3 5.4 5.5 5.6 5.7 5.8 5.9 5.10 5.12 5.13 5.14 5.15 5.19 5.20 5.21 5.22 5.23 Geo	ax+by=gcd Pollard Rho Pi Count (Linear Sieve) Strling Number 5.6.1 First Kind 5.6.2 Second Kind Range Sieve Miller Rabin Inverse Element Extended Euler Gauss Elimination Fast Fourier Transform Chinese Remainder Berlekamp Massey NTT Polynomial Operations FWT DiscreteLog FloorSum Quadratic residue De-Bruijn Simplex Description DiscreteLog Simplex Description DiscreteLog Simplex Description	12 12 13 13 13 13 13 13 13 14 14 14 15 16 16 16 16	#1.2 #1.2 #d. #d. #d. us. tel vo. } tel vo.	DKISEKI && echo success <cr> p <f10> <esc>:!./"%<"<cr> Debue Macro fdef KISEKI efine safe cerr<<pretty_function\ "<<line<<"="" <<"="" <typenamet="" a)="" debug(a)="" dvorak(#a,="" efine="" ing="" line="" mplate="" orange(a)="" qwerty(#a,="" safe\n"="" std::cerr;=""> id qwerty(const char *s, Ta) { cerr << "\e[1;32m(" << s << ") = ("; int cnt = sizeof(T); (, (cerr << a << (cnt ? ", " : ")\e[0m\n"))); mplate <typename iter=""> id dvorak(const char *s, Iter L, Iter R) { cerr << "\e[1;32m[" << s << "] = ["; for (int f = 0; L != R; ++L) cerr << (f++ ? ", " : "") << *L;</typename></pretty_function\></cr></esc></f10></cr>
6	5.3 5.4 5.5 5.6 5.7 5.8 5.9 5.10 5.12 5.13 5.14 5.15 5.16 5.17 5.18 5.20 5.21 5.23 Geo	ax+by=gcd Pollard Rho Pi Count (Linear Sieve) Strling Number 5.6.1 First Kind 5.6.2 Second Kind Range Sieve Miller Rabin Inverse Element Extended Euler Gauss Elimination Fast Fourier Transform Chinese Remainder Berlekamp Massey NTT Polynomial Operations FWT DiscreteLog FloorSum Quadratic residue De-Bruijn Simplex Description DiscreteLog Simplex Description DiscreteLog Simplex Description	12 12 12 13 13 13 13 13 13 13 14 14 14 15 16 16 16 16 16 16	#1.2 #1 #1 #1 #1 #1 #1 #1 #1 #1 #1 #1 #1 #1	DKISEKI && echo success <cr> p <f10> <esc>:!./"%<"<cr> 2</cr></esc></f10></cr>
6	5.3 5.4 5.5 5.6 5.7 5.8 5.9 5.10 5.11 5.12 5.13 5.14 5.15 5.16 5.17 5.20 5.21 5.22 5.23 Geo 6.1 6.2	ax+by=gcd Pollard Rho Pi Count (Linear Sieve) Strling Number 5.6.1 First Kind 5.6.2 Second Kind Range Sieve Miller Rabin Inverse Element Extended Euler Gauss Elimination Fast Fourier Transform Chinese Remainder Berlekamp Massey NTT Polynomial Operations FWT DiscreteLog FloorSum Quadratic residue De-Bruijn Simplex Desconders Discrety Basic Geometry Circle Class	12 12 12 13 13 13 13 13 13 13 14 14 14 15 16 16 16 16 16 17 17	#1.2 #1 #1 #1 #1 #1 #1 #1 #1 #1 #1 #1 #1 #1	DKISEKI && echo success <cr> p <f10> <esc>:!./"%<" <cr> 2</cr></esc></f10></cr>
6	5.3 5.4 5.5 5.6 5.7 5.8 5.9 5.10 5.12 5.13 5.14 5.15 5.16 5.17 5.20 5.21 5.22 5.23 Geo 6.1 6.2 6.3	ax+by=gcd Pollard Rho Pi Count (Linear Sieve) Strling Number 5.6.1 First Kind 5.6.2 Second Kind Range Sieve Miller Rabin Inverse Element Extended Euler Gauss Elimination Fast Fourier Transform Chinese Remainder Berlekamp Massey NTT Polynomial Operations FWT DiscreteLog FloorSum Quadratic residue De-Bruijn Simplex Desarrage Basic Geometry Circle Class 2D Convex Hull	12 12 12 13 13 13 13 13 13 13 14 14 14 15 16 16 16 16 16 17 17 17	#1.2 #1 #1 #1 #1 #1 #1 #1 #1 #1 #1 #1 #1 #1	DKISEKI && echo success <cr> p <f10> <esc>:!./"%<"<cr> 2</cr></esc></f10></cr>
6	5.3 5.4 5.5 5.6 5.7 5.8 5.9 5.10 5.12 5.13 5.14 5.15 5.19 5.20 5.21 5.22 5.23 Geo 6.1 6.2 6.3 6.4	ax+by=gcd Pollard Rho Pi Count (Linear Sieve) Strling Number 5.6.1 First Kind 5.6.2 Second Kind Range Sieve Miller Rabin Inverse Element Extended Euler Gauss Elimination Fast Fourier Transform Chinese Remainder Berlekamp Massey NTT Polynomial Operations FWT DiscreteLog FloorSum Quadratic residue De-Bruijn Simplex Desconders Discretery Basic Geometry Circle Class 2D Convex Hull 3D Convex Hull	12 12 12 13 13 13 13 13 13 13 14 14 14 15 16 16 16 16 16 16 17 17 17	#1.2 #1 #dd #dd us tell vo	DKISEKI && echo success <cr> p <f10> <esc>:!./"%<"<cr> Debue Macro fdef KISEKI efine safe cerr<<pretty_function\ "<<line<<"="" <<"="" <typenamet="" a)="" debug(a)="" dvorak(#a,="" efine="" ing="" line="" mplate="" orange(a)="" qwerty(#a,="" safe\n"="" std::cerr;=""> id qwerty(const char *s, Ta) { cerr << "\e[1;32m(" << s << ") = ("; int cnt = sizeof(T); (, (cerr << a << (cnt ? ", " : ")\e[0m\n"))); mplate <typename iter=""> id dvorak(const char *s, Iter L, Iter R) { cerr << "\e[1;32m[" << s << "] = ["; for (int f = 0; L != R; ++L)</typename></pretty_function\></cr></esc></f10></cr>
6	5.3 5.4 5.5 5.6 5.7 5.8 5.9 5.10 5.12 5.13 5.14 5.15 5.19 5.20 5.21 5.22 5.23 Geo 6.1 6.2 6.3 6.4	ax+by=gcd Pollard Rho Pi Count (Linear Sieve) Strling Number 5.6.1 First Kind 5.6.2 Second Kind Range Sieve Miller Rabin Inverse Element Extended Euler Gauss Elimination Fast Fourier Transform Chinese Remainder Berlekamp Massey NTT Polynomial Operations FWT DiscreteLog FloorSum Quadratic residue De-Bruijn Simplex Desarrage Basic Geometry Circle Class 2D Convex Hull	12 12 12 13 13 13 13 13 13 13 14 14 14 15 16 16 16 16 16 16 17 17 17	#1.2 #1.2 #1.2 #1.2 #1.2 #1.2 #1.2 #1.2	DKISEKI && echo success <cr> p <f10> <esc>:!./"%<"<cr> Debue Macro fdef KISEKI efine safe cerr<<pretty_function\ "<<line<<"="" <<"="" <typenamet="" a)="" debug(a)="" dvorak(#a,="" efine="" ing="" line="" mplate="" orange(a)="" qwerty(#a,="" safe\n"="" std::cerr;=""> id qwerty(const char *s, Ta) { cerr << "\e[1;32m(" << s << ") = ("; int cnt = sizeof(T); (, (cerr << a << (cnt ? ", " : ")\e[0m\n"))); mplate <typename iter=""> id dvorak(const char *s, Iter L, Iter R) { cerr << "\e[1;32m[" << s << "] = ["; for (int f = 0; L != R; ++L) cerr << (f++ ? ", " : "") << *L; cerr << "]\e[0m\n"; lse efine safe ((void)0) efine debug() ((void)0)</typename></pretty_function\></cr></esc></f10></cr>
6	5.3 5.4 5.5 5.6 5.7 5.8 5.9 5.10 5.12 5.13 5.14 5.15 5.16 5.20 5.21 5.22 5.23 Geo 6.1 6.2 6.3 6.4 6.5	ax+by=gcd Pollard Rho Pi Count (Linear Sieve) Strling Number 5.6.1 First Kind 5.6.2 Second Kind Range Sieve Miller Rabin Inverse Element Extended Euler Gauss Elimination Fast Fourier Transform Chinese Remainder Berlekamp Massey NTT Polynomial Operations FWT DiscreteLog FloorSum Quadratic residue De-Bruijn Simplex Convex Hull 3D Convex Hull 2D Farthest Pair	12 12 12 13 13 13 13 13 13 13 13 14 14 14 14 15 16 16 16 16 16 16 17 17 17 17 17 18	#1.2 #1.2 #1.2 #1.2 #1.2 #1.2 #1.2 #1.2	DKISEKI && echo success <cr> p <f10> <esc>:!./"%<"<cr> Debue Macro fdef KISEKI efine safe cerr<<pretty_function\ "<<line<<"="" <<"="" <typenamet="" a)="" debug(a)="" dvorak(#a,="" efine="" ing="" line="" mplate="" orange(a)="" qwerty(#a,="" safe\n"="" std::cerr;=""> id qwerty(const char *s, Ta) { cerr << "\e[1;32m(" << s << ") = ("; int cnt = sizeof(T); (, (cerr << a << (cnt ? ", " : ")\e[0m\n"))); mplate <typename iter=""> id dvorak(const char *s, Iter L, Iter R) { cerr << "\e[1;32m[" << s << "] = ["; for (int f = 0; L != R; ++L)</typename></pretty_function\></cr></esc></f10></cr>
6	5.3 5.4 5.5 5.6 5.7 5.8 5.9 5.10 5.12 5.13 5.14 5.15 5.16 5.20 5.21 5.22 5.23 Geo 6.1 6.2 6.3 6.4 6.5 6.6	ax+by=gcd Pollard Rho Pi Count (Linear Sieve) Strling Number 5.6.1 First Kind 5.6.2 Second Kind Range Sieve Miller Rabin Inverse Element Extended Euler Gauss Elimination Fast Fourier Transform Chinese Remainder Berlekamp Massey NTT Polynomial Operations FWT DiscreteLog FloorSum Quadratic residue De-Bruijn Simplex Dessi Geometry Circle Class 2D Convex Hull 3D Convex Hull 2D Farthest Pair 2D Closest Pair	12 12 12 13 13 13 13 13 13 13 14 14 14 15 16 16 16 16 16 17 17 17 17 17 18 18	#1.2 #1 #1 #1 #1 #1 #1 #1 #1 #1 #1 #1 #1 #1	DKISEKI && echo success <cr> p <f10> <esc>:!./"%<"<cr> Debue Macro fdef KISEKI efine safe cerr<<pretty_function\ "<<_line<<"="" <<"="" <typenamet="" a)="" debug(a)="" dvorak(#a,="" efine="" ing="" line="" mplate="" orange(a)="" qwerty(#a,="" safe\n"="" std::cerr;=""> id qwerty(const char *s, Ta) { cerr << "\e[1;32m(" << s << ") = ("; int cnt = sizeof(T); (, (cerr << a << (cnt ? ", " : ")\e[0m\n"))); mplate <typename iter=""> id dvorak(const char *s, Iter L, Iter R) { cerr << "\e[1;32m[" << s << "] = ["; for (int f = 0; L != R; ++L)</typename></pretty_function\></cr></esc></f10></cr>
6	5.3 5.4 5.5 5.6 5.7 5.8 5.9 5.10 5.12 5.13 5.14 5.15 5.16 5.20 5.21 5.22 5.23 Geo 6.1 6.2 6.3 6.4 6.5 6.6	ax+by=gcd Pollard Rho Pi Count (Linear Sieve) Strling Number 5.6.1 First Kind 5.6.2 Second Kind Range Sieve Miller Rabin Inverse Element Extended Euler Gauss Elimination Fast Fourier Transform Chinese Remainder Berlekamp Massey NTT Polynomial Operations FWT DiscreteLog FloorSum Quadratic residue De-Bruijn Simplex Convex Hull 3D Convex Hull 2D Farthest Pair	12 12 12 13 13 13 13 13 13 13 14 14 14 15 16 16 16 16 16 17 17 17 17 17 18 18	#1.2 #1 #1 #1 #1 #1 #1 #1 #1 #1 #1 #1 #1 #1	DKISEKI && echo success <cr> p <f10> <esc>:!./"%<"<cr> Debue Macro fdef KISEKI efine safe cerr<<pretty_function\ "<<line<<"="" <<"="" <typenamet="" a)="" debug(a)="" dvorak(#a,="" efine="" ing="" line="" mplate="" orange(a)="" qwerty(#a,="" safe\n"="" std::cerr;=""> id qwerty(const char *s, Ta) { cerr << "\e[1;32m(" << s << ") = ("; int cnt = sizeof(T); (, (cerr << a << (cnt ? ", " : ")\e[0m\n"))); mplate <typename iter=""> id dvorak(const char *s, Iter L, Iter R) { cerr << "\e[1;32m[" << s << "] = ["; for (int f = 0; L != R; ++L) cerr << (f++ ? ", " : "") << *L; cerr << "]\e[0m\n"; lse efine safe ((void)0) efine debug() ((void)0)</typename></pretty_function\></cr></esc></f10></cr>
6	5.3 5.4 5.5 5.6 5.7 5.8 5.9 5.10 5.12 5.13 5.14 5.15 5.16 5.17 5.20 5.21 5.22 5.23 Geo 6.1 6.2 6.3 6.4 6.5 6.6 6.6 6.6 6.7	ax+by=gcd Pollard Rho Pi Count (Linear Sieve) Strling Number 5.6.1 First Kind 5.6.2 Second Kind Range Sieve Miller Rabin Inverse Element Extended Euler Gauss Elimination Fast Fourier Transform Chinese Remainder Berlekamp Massey NTT Polynomial Operations FWT DiscreteLog FloorSum Quadratic residue De-Bruijn Simplex Dessi Geometry Circle Class 2D Convex Hull 3D Convex Hull 2D Farthest Pair 2D Closest Pair	12 12 12 13 13 13 13 13 13 13 13 14 14 14 15 16 16 16 16 16 17 17 17 17 17 17 18 18 18 18 18 18 18 18 18 18 18 18 18	#1.2 #1 #dd #dd #dd uss tell vo vo vo when the vo vo when the vo vo when the v	DKISEKI && echo success <cr> p <f10> <esc>:!./"%<"<cr> Debue Macro fdef KISEKI efine safe cerr<<pretty_function\ "<<_line<<"="" <<"="" <typenamet="" a)="" debug(a)="" dvorak(#a,="" efine="" ing="" line="" mplate="" orange(a)="" qwerty(#a,="" safe\n"="" std::cerr;=""> id qwerty(const char *s, Ta) { cerr << "\e[1;32m(" << s << ") = ("; int cnt = sizeof(T); (, (cerr << a << (cnt ? ", " : ")\e[0m\n"))); mplate <typename iter=""> id dvorak(const char *s, Iter L, Iter R) { cerr << "\e[1;32m[" << s << "] = ["; for (int f = 0; L != R; ++L) cerr << (f++ ? ", " : "") << *L; cerr << "]\e[0m\n"; lse efine safe ((void)0) efine debug() ((void)0) efine orange() ((void)0) ndif</typename></pretty_function\></cr></esc></f10></cr>
6	5.3 5.4 5.5 5.6 5.7 5.8 5.9 5.10 5.11 5.15 5.16 5.17 5.18 5.19 5.20 5.21 5.22 6.3 6.4 6.5 6.6 6.6 6.7 6.8	ax+by=gcd Pollard Rho Pi Count (Linear Sieve) Strling Number 5.6.1 First Kind 5.6.2 Second Kind Range Sieve Miller Rabin Inverse Element Extended Euler Gauss Elimination Fast Fourier Transform Chinese Remainder Berlekamp Massey NTT Polynomial Operations FWT DiscreteLog FloorSum Quadratic residue De-Bruijn Simplex Construction Simplex Demetry Basic Geometry Circle Class 2D Convex Hull 3D Convex Hull 3D Farthest Pair 2D Closest Pair kD Closest Pair (3D ver.) Simulated Annealing	12 12 12 13 13 13 13 13 13 13 14 14 14 15 16 16 16 16 17 17 17 17 17 18 18 18 18 18	#1.2 #1 #dd #dd #dd uss tell vo vo vo when the vo vo when the vo vo when the v	DKISEKI && echo success <cr> p <f10> <esc>:!./"%<"<cr> Debue Macro fdef KISEKI efine safe cerr<<pretty_function\ "<<_line<<"="" <<"="" <typenamet="" a)="" debug(a)="" dvorak(#a,="" efine="" ing="" line="" mplate="" orange(a)="" qwerty(#a,="" safe\n"="" std::cerr;=""> id qwerty(const char *s, Ta) { cerr << "\e[1;32m(" << s << ") = ("; int cnt = sizeof(T); (, (cerr << a << (cnt ? ", " : ")\e[0m\n"))); mplate <typename iter=""> id dvorak(const char *s, Iter L, Iter R) { cerr << "\e[1;32m[" << s << "] = ["; for (int f = 0; L != R; ++L) cerr << (f++ ? ", " : "") << *L; cerr << "]\e[0m\n"; lse efine safe ((void)0) efine debug() ((void)0) efine orange() ((void)0) ndif</typename></pretty_function\></cr></esc></f10></cr>
6	5.3 5.4 5.5 5.6 5.7 5.8 5.9 5.10 5.11 5.12 5.13 5.14 5.15 5.16 5.17 5.20 5.21 5.22 5.23 6.4 6.5 6.6 6.7 6.8 6.9	ax+by=gcd Pollard Rho Pi Count (Linear Sieve) Strling Number 5.6.1 First Kind 5.6.2 Second Kind Range Sieve Miller Rabin Inverse Element Extended Euler Gauss Elimination Fast Fourier Transform Chinese Remainder Berlekamp Massey NTT Polynomial Operations FWT DiscreteLog FloorSum Quadratic residue De-Bruijn Simplex Construction Simplex Discrete Class 2D Convex Hull 3D Convex Hull 2D Farthest Pair 2D Closest Pair KD Closest Pair KD Closest Pair (3D ver.) Simulated Annealing Half Plane Intersection	12 12 12 13 13 13 13 13 13 13 14 14 14 14 15 16 16 16 16 17 17 17 17 17 18 18 18 18 18 18 18 18 18 18 18 18 18	#1.2 #1 #1 #1 #1 #1 #1 #1 #1 #1 #1 #1 #1 #1	DKISEKI && echo success <cr> p <f10> <esc>:!./"%<"<cr> Debue Macro fdef KISEKI efine safe cerr<<pretty_function\ "<<line<<"="" <<"="" <typenamet="" a)="" debug(a)="" dvorak(#a,="" efine="" ing="" line="" mplate="" orange(a)="" qwerty(#a,="" safe\n"="" std::cerr;=""> id qwerty(const char *s, Ta) { cerr << "\e[1;32m(" << s << ") = ("; int cnt = sizeof(T); (, (cerr << a << (cnt ? ", " : ")\e[0m\n"))); mplate <typename iter=""> id dvorak(const char *s, Iter L, Iter R) { cerr << "\e[1;32m[" << s << "] = ["; for (int f = 0; L != R; ++L) cerr << (f++ ? ", " : "") << *L; cerr << "]\e[0m\n"; lse efine safe ((void)0) efine debug() ((void)0) ndif</typename></pretty_function\></cr></esc></f10></cr>
6	5.3 5.4 5.5 5.6 5.7 5.8 5.9 5.10 5.12 5.13 5.14 5.15 5.16 5.17 5.18 5.19 5.20 5.21 5.22 5.23 6.4 6.5 6.6 6.7 6.8 6.9 6.10	ax+by=gcd Pollard Rho Pi Count (Linear Sieve) Strling Number 5.6.1 First Kind 5.6.2 Second Kind Range Sieve Miller Rabin Inverse Element Extended Euler Gauss Elimination Fast Fourier Transform Chinese Remainder Berlekamp Massey NTT Polynomial Operations FWT DiscreteLog FloorSum Quadratic residue De-Bruijn Simplex De-Bruijn Simplex De-Bruid Donest Construction Simplex Deconder Hull Donest Pair Donest Pair Closest Pair Closest Pair Closest Pair Closest Pair (3D ver.) Simulated Anneoling Half Plane Intersection Minkowski sum	12 12 12 13 13 13 13 13 13 13 14 14 14 14 15 16 16 16 16 16 17 17 17 17 18 18 18 18 18 18 18 18 18 18 18 18 18	#1.2 #1 #d	DKISEKI && echo success <cr> p <f10> <esc>:!./"%<"<cr> 2 Debue Macro fdef KISEKI efine safe cerr<<pretty_function\ "<<line<<"="" <<"="" <typenamet="" a)="" debug(a)="" dvorak(#a,="" efine="" ing="" line="" mplate="" orange(a)="" qwerty(#a,="" safe\n"="" std::cerr;=""> id qwerty(const char *s, Ta) { cerr << "\e[1;32m(" << s << ") = ("; int cnt = sizeof(T); (, (cerr << a << (cnt ? ", " : ")\e[0m\n"))); mplate <typename iter=""> id dvorak(const char *s, Iter L, Iter R) { cerr << "\e[1;32m[" << s << "] = ["; for (int f = 0; L!= R; ++L)</typename></pretty_function\></cr></esc></f10></cr>
6	5.3 5.4 5.5 5.6 5.7 5.8 5.9 5.10 5.12 5.13 5.14 5.15 5.16 5.17 5.18 5.19 5.20 5.21 5.22 5.23 6.4 6.5 6.6 6.7 6.8 6.9 6.10	ax+by=gcd Pollard Rho Pi Count (Linear Sieve) Strling Number 5.6.1 First Kind 5.6.2 Second Kind Range Sieve Miller Rabin Inverse Element Extended Euler Gauss Elimination Fast Fourier Transform Chinese Remainder Berlekamp Massey NTT Polynomial Operations FWT DiscreteLog FloorSum Quadratic residue De-Bruijn Simplex Construction Simplex Discrete Class 2D Convex Hull 3D Convex Hull 2D Farthest Pair 2D Closest Pair KD Closest Pair KD Closest Pair (3D ver.) Simulated Annealing Half Plane Intersection	12 12 12 13 13 13 13 13 13 13 14 14 14 14 15 16 16 16 16 16 17 17 17 17 18 18 18 18 18 18 18 18 18 18 18 18 18	#1.2 #1 #1 #1 #1 #1 #1 #1 #1 #1 #1 #1 #1 #1	DKISEKI && echo success <cr> p <f10> <esc>:!./"%<"<cr> 2 Debue Macro fdef KISEKI efine safe cerr<<pretty_function\ "<<line<<"="" <<"="" <typenamet="" a)="" debug(a)="" dvorak(#a,="" efine="" ing="" line="" mplate="" orange(a)="" qwerty(#a,="" safe\n"="" std::cerr;=""> id qwerty(const char *s, Ta) { cerr << "\e[1;32m(" << s << ") = ("; int cnt = sizeof(T); (, (cerr << a << (cnt ? ", " : ")\e[0m\n"))); mplate <typename iter=""> id dvorak(const char *s, Iter L, Iter R) { cerr << "\e[1;32m[" << s << "] = ["; for (int f = 0; L != R; ++L)</typename></pretty_function\></cr></esc></f10></cr>
6	5.3 5.4 5.5 5.6 5.7 5.8 5.9 5.10 5.12 5.13 5.14 5.15 5.16 5.20 5.21 5.22 5.23 Geo 6.1 6.2 6.3 6.4 6.5 6.6 6.9 6.10 6.11	ax+by=gcd Pollard Rho Pi Count (Linear Sieve) Strling Number 5.6.1 First Kind 5.6.2 Second Kind Range Sieve Miller Rabin Inverse Element Extended Euler Gauss Elimination Fast Fourier Transform Chinese Remainder Berlekamp Massey NTT Polynomial Operations FWT DiscreteLog FloorSum Quadratic residue De-Bruijn Simplex Construction Simplex Description Simplex Descript	12 12 12 13 13 13 13 13 13 13 13 14 14 14 14 15 16 16 16 16 16 17 17 17 17 17 18 18 18 18 18 18 19 19 19 19 19 19 19 19 19 19 19 19 19	#1.2 #1 #1 #1 #1 #1 #1 #1 #1 #1 #1 #1 #1 #1	DKISEKI && echo success <cr> p <f10> <esc>:!./"%<"<cr> Debue Macro fdef KISEKI efine safe cerr<<pretty_function\ "<<line<<"="" <<"="" <typenamet="" a)="" debug(a)="" dvorak(#a,="" efine="" ing="" line="" mplate="" orange(a)="" qwerty(#a,="" safe\n"="" std::cerr;=""> id qwerty(const char *s, Ta) { cerr << "\e[1;32m(" << s << ") = ("; int cnt = sizeof(T); (, (cerr << a << (cnt ? ", " : ")\e[0m\n"))); mplate <typename iter=""> id dvorak(const char *s, Iter L, Iter R) { cerr << "\e[1;32m[" << s << "] = ["; for (int f = 0; L != R; ++L) cerr << (f++ ? ", " : "") << *L; cerr << "]\e[0m\n"; lse efine safe ((void)0) efine debug() ((void)0) efine orange() ((void)0) ndif S Increase Stack nst int size = 256 << 20; gister long rsp asm("rsp");</typename></pretty_function\></cr></esc></f10></cr>
6	5.3 5.4 5.5 5.6 5.7 5.8 5.10 5.11 5.12 5.13 5.14 5.15 5.16 5.17 5.20 5.21 5.22 5.23 Geo 6.1 6.2 6.3 6.4 6.5 6.6 6.1 6.1 6.1 6.1 6.1 6.1 6.1 6.1 6.1	ax+by=gcd Pollard Rho Pi Count (Linear Sieve) Strling Number 5.6.1 First Kind 5.6.2 Second Kind Range Sieve Miller Rabin Inverse Element Extended Euler Gauss Elimination Fast Fourier Transform Chinese Remainder Berlekamp Massey NTT Polynomial Operations FWT DiscreteLog FloorSum Quadratic residue De-Bruijn Simplex Despruijn Simplex Despruijn Simplex Despruijn Despr	12 12 12 13 13 13 13 13 13 13 13 14 14 14 15 16 16 16 16 17 17 17 17 17 17 18 18 18 18 18 19 19 19 19 19 19 19 19 19 19 19 19 19	#1.2 #1 #1 #1 #1 #1 #1 #1 #1 #1 #1 #1 #1 #1	DKISEKI && echo success <cr> p <f10> <esc>:!./"%<"<cr> 2 Debue Macro fdef KISEKI efine safe cerr<<pretty_function\ "<<line<<"="" <<"="" <typenamet="" a)="" debug(a)="" dvorak(#a,="" efine="" ing="" line="" mplate="" orange(a)="" qwerty(#a,="" safe\n"="" std::cerr;=""> id qwerty(const char *s, Ta) { cerr << "\e[1;32m(" << s << ") = ("; int cnt = sizeof(T); (, (cerr << a << (cnt ? ", " : ")\e[0m\n"))); mplate <typename iter=""> id dvorak(const char *s, Iter L, Iter R) { cerr << "\e[1;32m[" << s << "] = ["; for (int f = 0; L != R; ++L)</typename></pretty_function\></cr></esc></f10></cr>
6	5.3 5.4 5.5 5.6 5.7 5.8 5.9 5.10 5.12 5.13 5.14 5.15 5.16 5.17 5.20 5.21 5.22 5.23 Geo 6.1 6.2 6.3 6.4 6.5 6.6 6.6 6.1 6.1 6.1 6.1 6.1 6.1 6.1 6.1	ax+by=gcd Pollard Rho Pi Count (Linear Sieve) Strling Number 5.6.1 First Kind 5.6.2 Second Kind Range Sieve Miller Rabin Inverse Element Extended Euler Gauss Elimination Fast Fourier Transform Chinese Remainder Berlekamp Massey NTT Polynomial Operations FWT DiscreteLog FloorSum Quadratic residue De-Bruijn Simplex Onestry Basic Geometry Circle Class 2D Convex Hull 3D Convex Hull 3D Convex Hull 3D Convex Hull 2D Farthest Pair 2D Closest Pair kD Closest Pair (3D ver.) Simulated Annealing Half Plane Intersection Minkowski sum intersection of polygon and circle intersection of two circle	12 12 12 13 13 13 13 13 13 13 13 14 14 14 15 16 16 16 16 17 17 17 17 17 17 17 17 17 17 17 18 18 18 18 18 18 19 19 19 19 19 19 19 19 19 19 19 19 19	#1.2 #1 #dd #dd #dd #dd #dd #dd #dd #dd #dd	DKISEKI && echo success <cr> p <f10> <esc>:!./"%<"<cr> 2 Debue Macro fdef KISEKI efine safe cerr<<pretty_function\ "<<line<<"="" <<"="" <typenamet="" a)="" debug(a)="" dvorak(#a,="" efine="" ing="" line="" mplate="" orange(a)="" qwerty(#a,="" safe\n"="" std::cerr;=""> id qwerty(const char *s, Ta) { cerr << "\e[1;32m(" << s << ") = ("; int cnt = sizeof(T); (, (cerr << a << (cnt ? ", " : ")\e[0m\n"))); mplate <typename iter=""> id dvorak(const char *s, Iter L, Iter R) { cerr << "\e[1;32m[" << s << "] = ["; for (int f = 0; L != R; ++L) cerr << (f++ ? ", " : "") << *L; cerr << "]\e[0m\n"; lse efine safe ((void)0) efine debug() ((void)0) efine debug() ((void)0) ndif 3 Increase Stack nst int size = 256 << 20; gister long rsp asm("rsp"); ar *p = (char*)malloc(size)+size, *bak = (char*)rsp; ar *p = (char*)malloc(size)+size, *bak = (char*)rsp;</typename></pretty_function\></cr></esc></f10></cr>
6	5.3 5.4 5.5 5.6 5.7 5.8 5.9 5.10 5.12 5.13 5.14 5.15 5.16 5.17 5.20 5.21 5.22 5.23 Geo 6.1 6.2 6.3 6.4 6.5 6.6 6.6 6.1 6.1 6.1 6.1 6.1 6.1 6.1 6.1	ax+by=gcd Pollard Rho Pi Count (Linear Sieve) Strling Number 5.6.1 First Kind 5.6.2 Second Kind Range Sieve Miller Rabin Inverse Element Extended Euler Gauss Elimination Fast Fourier Transform Chinese Remainder Berlekamp Massey NTT Polynomial Operations FWT DiscreteLog FloorSum Quadratic residue De-Bruijn Simplex Despruijn Simplex Despruijn Simplex Despruijn Despr	12 12 12 13 13 13 13 13 13 13 13 14 14 14 15 16 16 16 16 17 17 17 17 17 17 17 17 17 17 17 18 18 18 18 18 18 19 19 19 19 19 19 19 19 19 19 19 19 19	#1.2 #1 #dd #dd #dd #dd #dd #dd #dd #dd #dd	DKISEKI && echo success <cr> p <f10> <esc>:!./"%<"<cr> Debue Macro fdef KISEKI efine safe cerr<pretty_function\ "<line<\"="" <\"="" <typenamet="" a)="" debug(a)="" dvorak(#a,="" efine="" ing="" line="" mplate="" orange(a)="" qwerty(#a,="" safe\n"="" std::cerr;=""> id qwerty(const char *s, Ta) { cerr << "\e[1;32m(" << s << ") = ("; int cnt = sizeof(T); (, (cerr << a << (cnt ? ", " : ")\e[0m\n"))); mplate <typename iter=""> id dvorak(const char *s, Iter L, Iter R) { cerr << "\e[1;32m[" << s << "] = ["; for (int f = 0; L != R; ++L)</typename></pretty_function\></cr></esc></f10></cr>
6	5.3 5.4 5.5 5.6 5.7 5.8 5.9 5.10 5.11 5.15 5.16 5.17 5.18 5.19 5.20 5.21 5.22 5.23 6.4 6.5 6.6 6.7 6.8 6.9 6.10 6.11 6.12 6.13 6.14 6.14 6.15 6.15 6.16 6.16 6.16 6.16 6.16 6.16	ax+by=gcd Pollard Rho Pi Count (Linear Sieve) Strling Number 5.6.1 First Kind 5.6.2 Second Kind Range Sieve Miller Rabin Inverse Element Extended Euler Gauss Elimination Fast Fourier Transform Chinese Remainder Berlekamp Massey NTT Polynomial Operations FWT DiscreteLog FloorSum Quadratic residue De-Bruijn Simplex Onestry Basic Geometry Circle Class 2D Convex Hull 3D Convex Hull 3D Convex Hull 3D Convex Hull 2D Farthest Pair 2D Closest Pair kD Closest Pair (3D ver.) Simulated Annealing Half Plane Intersection Minkowski sum intersection of polygon and circle intersection of two circle	12 12 12 13 13 13 13 13 13 13 14 14 14 15 16 16 16 16 17 17 17 17 17 17 18 18 18 18 19 19 19 19 19 19 19 19 19 19 19 19 19	#1.2 #1 #dd #dd us tel vo	DKISEKI && echo success <cr> p <f10> <esc>:!./"%<"<cr> 2 Debue Macro fdef KISEKI efine safe cerr<<pretty_function\ "<<line<<"="" <<"="" <typenamet="" a)="" debug(a)="" dvorak(#a,="" efine="" ing="" line="" mplate="" orange(a)="" qwerty(#a,="" safe\n"="" std::cerr;=""> id qwerty(const char *s, Ta) { cerr << "\e[1;32m(" << s << ") = ("; int cnt = sizeof(T); (, (cerr << a << (cnt ? ", " : ")\e[0m\n"))); mplate <typename iter=""> id dvorak(const char *s, Iter L, Iter R) { cerr << "\e[1;32m[" << s << "] = ["; for (int f = 0; L != R; ++L) cerr << (f++ ? ", " : "") << *L; cerr << "]\e[0m\n"; lse efine safe ((void)0) efine debug() ((void)0) efine debug() ((void)0) ndif 3 Increase Stack nst int size = 256 << 20; gister long rsp asm("rsp"); ar *p = (char*)malloc(size)+size, *bak = (char*)rsp; ar *p = (char*)malloc(size)+size, *bak = (char*)rsp;</typename></pretty_function\></cr></esc></f10></cr>

7 Stringology

1.4 Pragma Optimization

```
#pragma GCC target("sse,sse2,sse3,ssse3,sse4")
#pragma GCC target("popcnt,abm,mmx,avx,tune=native")
1.5 IO Optimization
static inline int gc() {
  constexpr int B = 1 << 20;
  static char buf[B], *p, *q;
  if(p == a \&\&
    (q=(p=buf)+fread(buf,1,B,stdin)) == buf)
   return EOF;
  return *p++;
template < typename T >
static inline bool gn( T &x ) {
 int c = gc(); T sgn = 1; x = 0;
while(('0'>c||c>'9') && c!=EOF && c!='-') c = gc();
if(c == '-') sgn = -1, c = gc();
 if(c == EOF) return false;
 while('0'<=c&&c<='9') x = x*10 + c - '0', c = gc();
 return x *= sgn, true;
```

#pragma GCC optimize("Ofast,no-stack-protector")

#pragma GCC optimize("no-math-errno,unroll-loops")

2 Data Structure

2.1 Dark Magic

2.2 Link-Cut Tree

p->ch[dir]=c;

```
struct Node{
Node *par, *ch[2];
int xor_sum, v;
bool is_rev;
Node(int _v){
 v=xor_sum=_v;is_rev=false;
 par=ch[0]=ch[1]=nullptr;
inline void set_rev(){is_rev^=1;swap(ch[0],ch[1]);}
inline void down(){
 if(is_rev){
  if(ch[0]!=nullptr) ch[0]->set_rev();
   if(ch[1]!=nullptr) ch[1]->set_rev();
   is_rev=false;
 }
inline void up(){
 xor_sum=v;
  if(ch[0]!=nullptr){
  xor_sum^=ch[0]->xor_sum;
  ch[0]->par=this;
 if(ch[1]!=nullptr){
  xor_sum^=ch[1]->xor_sum;
  ch[1]->par=this;
inline bool is_root(){
 return par==nullptr ||\
   (par->ch[0]!=this && par->ch[1]!=this);
bool is_rch(){return !is_root() && par->ch[1]==this;}
} *node[maxn], *stk[maxn];
int top;
void to_child(Node* p,Node* c,bool dir){
```

```
p->up();
inline void rotate(Node* node){
 Node* par=node->par;
 Node* par_par=par->par;
 bool dir=node->is_rch()
 bool par_dir=par->is_rch()
 to_child(par, node->ch[!dir], dir);
 to_child(node,par,!dir);
 if(par_par!=nullptr && par_par->ch[par_dir]==par)
  to_child(par_par,node,par_dir);
 else node->par=par_par;
inline void splay(Node* node){
 Node* tmp=node;
 stk[top++]=node;
 while(!tmp->is_root()){
  tmp=tmp->par;
  stk[top++]=tmp;
 while(top) stk[--top]->down();
 for(Node *fa=node->par;
  !node->is_root();
  rotate(node), fa=node->par)
  if(!fa->is_root())
   rotate(fa->is_rch()==node->is_rch()?fa:node);
inline void access(Node* node){
 Node* last=nullptr;
 while(node!=nullptr){
  splay(node);
  to_child(node, last, true);
  last=node;
  node=node->par;
inline void change_root(Node* node){
 access(node);splay(node);node->set_rev();
inline void link(Node* x, Node* y){
 change_root(x);splay(x);x->par=y;
inline void split(Node* x,Node* y){
 change_root(x);access(y);splay(x);
 to_child(x,nullptr,true);y->par=nullptr;
inline void change_val(Node* node,int v){
access(node);splay(node);node->v=v;node->up();
inline int query(Node* x,Node* y){
 change_root(x);access(y);splay(y);
 return y->xor_sum;
inline Node* find_root(Node* node){
 access(node);splay(node);
 Node* last=nullptr:
 while(node!=nullptr){
  node->down();last=node;node=node->ch[0];
 return last;
set<pii> dic;
inline void add_edge(int u,int v){
 if(u>v) swap(u,v)
 if(find_root(node[u])==find_root(node[v])) return;
 dic.insert(pii(u,v))
link(node[u],node[v]);
inline void del_edge(int u,int v){
 if(u>v) swap(u,v);
 if(dic.find(pii(u,v))==dic.end()) return;
 dic.erase(pii(u,v))
 split(node[u],node[v]);
2.3 LiChao Segment Tree
struct Line{
 int m, k, id;
 Line() : id( -1 ) {}
Line('int a, int'b,'int c')
: m(a), k(b), id(c) {}
```

int at(int x) { return m * x + k; }

```
private:
class LiChao {
                                                                 vector< vector< T > > tbl;
 private:
                                                                 vector< int > lg;
                                                                 T cv(Ta, Tb) {
  int n; vector< Line > nodes;
  inline int lc( int x ) { return 2 * x + 1; }
                                                                  return Cmp_()( a, b ) ? a : b;
  inline int rc( int x ) { return 2 * x + 2; }
  void insert( int 1, int r, int id, Line ln ) {
                                                                public:
   int m = (1 + r) >> 1;
                                                                 void init( T arr[], int n ) {
   if ( nodes[ id ].id == -1 ) {
                                                                  // 0-base
    nodes[ id ] = ln;
                                                                  lg.resize(n+1);
                                                                  lg[0] = -1;
    return:
                                                                  for( int i=1 ; i<=n ; ++i ) lg[i] = lg[i>>1] + 1;
   bool atLeft = nodes[ id ].at( 1 ) < ln.at( 1 );</pre>
                                                                  tbl.resize(lg[n] + 1);
   if ( nodes[ id ].at( m ) < ln.at( m ) ) {</pre>
                                                                  tbl[ 0 ].resize( n );
                                                                  copy( arr, arr + n, tbl[ 0 ].begin() );
    atLeft ^= 1; swap( nodes[ id ], ln );
                                                                  for ( int i = 1 ; i <= lg[ n ] ; ++ i ) {
  int len = 1 << ( i - 1 ), sz = 1 << i;</pre>
   if ( r - l == 1 ) return;
if ( atLeft ) insert( 1, m, lc( id ), ln );
                                                                   tbl[ i ].resize( n - sz + 1 );
                                                                   for (int_j = 0; j \le n - sz; ++ j
   else insert( m, r, rc( id ), ln );
                                                                    tbl[i][j] = cv(tbl[i-1][j], tbl[i-1][j+len]);
  int query( int 1, int r, int id, int x ) {
   int ret = 0;
   if ( nodes[ id ].id != -1 )
                                                                 T query( int 1, int r ) {
                                                                  // 0-base [1, r)
    ret = nodes[ id ].at( x );
                                                                  int wh = lg['r - 1 ], len = 1 << wh;
return cv( tbl[ wh ][ 1 ], tbl[ wh ][ r - len ] );</pre>
   int m = (1 + r) >> 1;
   if ( r - l == 1 ) return ret;
   else if ( x < m )
    return max( ret, query( 1, m, lc( id ), x ) );
   else
    return max( ret, query( m, r, rc( id ), x ) );
                                                                2.6 Linear Basis
                                                                struct LinearBasis {
 public:
                                                                private:
  void build( int n_ ) {
                                                                 int n, sz
  n = n_; nodes.clear();
                                                                 vector< llu > B;
   nodes.resize( n << 2, Line() );</pre>
                                                                 inline llu two( int x ){ return ( ( llu ) 1 ) << x; }</pre>
                                                                public:
  void insert( Line ln ) { insert( 0, n, 0, ln ); }
                                                                 void init( int n_ ) {
  int query( int x ) { return query( 0, n, 0, x ); }
                                                                  n = n_{;} B.clear(); B.resize(n); sz = 0;
} lichao:
2.4 Treap
                                                                 void insert( llu x ) {
                                                                  // add x into B
namespace Treap{
                                                                  for ( int i = n-1; i >= 0 ; --i ) if( two(i) & x ){
  if ( B[ i ] ) x ^= B[ i ];
 #define sz( x ) ( ( x ) ? ( ( x )->size ) : 0 )
 struct node{
                                                                   else {
  int size;
                                                                    B[ i ] = x; sz++;
for ( int j = i - 1 ; j >= 0 ; -- j
  uint32_t pri;
 node *lc, *rc;
node() : size(0), pri(rand()), lc(0), rc(0) {}
                                                                     if(`B[ j ] && ( two( j ) & B[ i ] )))
                                                                      B[ i ] ^= B[ j ];
  void pull() {
                                                                     for (int j = i + 1)
                                                                     for (int j = i + 1 ; j < i
if ( two( i ) & B[ j ] )
                                                                                           j < n; ++ j)
  size = 1;
   if ( lc ) size += lc->size;
                                                                      B[ j ] ^= B[ i ];
   if ( rc ) size += rc->size;
                                                                    break;
  }
node* merge( node* L, node* R ) {
  if ( not L or not R ) return L ? L : R;
                                                                 inline int size() { return sz; }
  if ( L->pri > R->pri ) {
                                                                 bool check( llu x ) {
  L->rc = merge( L->rc, R ); L->pull();
                                                                  // is x in span(B) ? for ( int i = n-1 ; i >= 0 ; --i ) if( two(i) & x )
   return L;
  } else {
                                                                   if( B[ i ] ) x ^= B[ i ];
   R->lc = merge( L, R->lc ); R->pull();
                                                                   else return false;
   return R;
                                                                  return true;
 }
                                                                 llu kth_small(llu k) {
 void split_by_size( node*rt,int k,node*&L,node*&R ) {
                                                                  /** 1-base would always > 0 **/
  if ( not rt ) L = R = nullptr;
                                                                  /** should check it **/
  else if( sz( rt->lc ) + 1 <= k ) {
                                                                  /* if we choose at least one element
                                                                    but size(B)(vectors in B)==N(original elements)
   split_by_size( rt->rc,k-sz(rt->lc)-1,L->rc,R );
                                                                    then we can't get 0 \star/
   L->pull();
                                                                  llu ret = 0;
  } else {
                                                                  for ( int i = 0 ; i < n ; ++ i ) if( B[ i ] ) {
  if( k & 1 ) ret ^= B[ i ];</pre>
   R = rt:
   split_by_size( rt->lc, k, L, R->lc );
                                                                   k >>= 1:
   R->pull();
                                                                  }
  }
                                                                  return ret;
                                                                 }
 #undef sz
                                                                } base;
2.5 Sparse Table
                                                                     Graph
template < typename T, typename Cmp_ = less< T > >
                                                                     BCC Edge
class SparseTable {
```

```
class BCC_Bridge {
                                                                  for (int i = 0; i < n; ++i)
                                                                   if (not dfn[i]) dfs(i, i);
private:
 int n, ecnt;
  vector<vector<pair<int,int>>> G;
                                                                 int get_id(int x) { return bcc[x]; }
 vector<int> dfn, low;
                                                                 int count() { return ecnt; }
  vector<bool> bridge;
                                                                 bool is_ap(int x) { return ap[x]; }
 void dfs(int u, int f) {
  dfn[u] = low[u] = dfn[f] + 1;
                                                              } bcc_ap;
                                                               3.3 2-SAT (SCC)
   for (auto [v, t]: G[u]) {
  if (v == f) continue;
                                                              class TwoSat{
    if (dfn[v]) {
                                                                private:
     low[u] = min(low[u], dfn[v]);
                                                                 int n:
     continue;
                                                                 vector<vector<int>> rG,G,sccs;
                                                                 vector<int> ord,idx;
    dfs(v, u);
                                                                 vector<bool> vis,result;
   low[u] = min(low[u], low[v]);
if (low[v] > dfn[u]) bridge[t] = true;
                                                                 void dfs(int u){
                                                                  vis[u]=true
                                                                  for(int v:G[u])
  }
                                                                   if(!vis[v]) dfs(v);
public:
                                                                  ord.push_back(u);
  void init(int n_) {
   G.clear(); G.resize(n = n_);
                                                                 void rdfs(int u){
   low.assign(n, ecnt = 0);
                                                                  vis[u]=false;idx[u]=sccs.size()-1;
                                                                  sccs.back().push_back(u);
   dfn.assign(n, 0);
                                                                  for(int v:rG[u])
  void add_edge(int u, int v) {
                                                                   if(vis[v])rdfs(v);
  G[u].emplace_back(v, ecnt);
   G[v].emplace_back(u, ecnt++);
                                                                public:
                                                                 void init(int n_){
  void solve() {
                                                                  n=n_;G.clear();G.resize(n);
  bridge.assign(ecnt, false);
                                                                  rG.clear();rG.resize(n)
   for (int i = 0; i < n; ++i)
                                                                  sccs.clear();ord.clear();
    if (not dfn[i]) dfs(i, i);
                                                                  idx.resize(n);result.resize(n);
  bool is_bridge(int x) { return bridge[x]; }
                                                                 void add_edge(int u,int v){
} bcc_bridge;
                                                                  G[u].push_back(v);rG[v].push_back(u);
3.2 BCC Vertex
                                                                 void orr(int x,int y){
class BCC_AP {
                                                                  if ((x^y)==1)return
                                                                  add_edge(x^1,y); add_edge(y^1,x);
private:
 int n, ecnt;
 vector<vector<pair<int,int>>> G;
                                                                 bool solve(){
  vector<int> bcc, dfn, low, st;
                                                                  vis.clear();vis.resize(n);
  vector<bool> ap, ins;
                                                                  for(int i=0;i<n;++i)</pre>
 void dfs(int u, int f) {
  dfn[u] = low[u] = dfn[f] + 1;
                                                                   if(not vis[i])dfs(i);
                                                                  reverse(ord.begin(),ord.end());
   int ch = 0;
                                                                  for (int u:ord){
   for (auto [v, t]: G[u]) if (v != f) {
                                                                   if(!vis[u])continue:
    if (not ins[t]) {
                                                                   sccs.push_back(vector<int>());
     st.push_back(t);
                                                                   rdfs(u);
     ins[t] = true;
                                                                  for(int i=0;i<n;i+=2)</pre>
    if (dfn[v]) {
                                                                   if(idx[i]==idx[i+1])
     low[u] = min(low[u], dfn[v]);
                                                                    return false;
                                                                  vector<bool> c(sccs.size());
    } ++ch; dfs(v, u);
                                                                  for(size_t i=0;i<sccs.size();++i){</pre>
    low[u] = min(low[u], low[v]);
                                                                   for(size_t j=0;j<sccs[i].size();++j){</pre>
                                                                    result[sccs[i][j]]=c[i]
    if (low[v] >= dfn[u]) {
     ap[u] = true;
                                                                    c[idx[sccs[i][j]^1]]=!c[i];
     while (true) {
      int eid = st.back(); st.pop_back();
      bcc[eid] = ecnt;
                                                                  return true;
      if (eid == t) break;
     }
                                                                 bool get(int x){return result[x];}
                                                                 inline int get_id(int x){return idx[x];}
     ecnt++;
                                                                 inline int count(){return sccs.size();}
    }
                                                              } sat2;
   if (ch == 1 and u == f) ap[u] = false;
                                                               3.4 Lowbit Decomposition
public:
                                                              class LowbitDecomp{
  void init(int n_) {
                                                               private:
  G.clear(); G.resize(n = n_);
                                                                int time_, chain_, LOG_N;
   ecnt = 0; ap.assign(n, false);
                                                                vector< vector< int > > G, fa;
                                                                vector< int > tl, tr, chain, chain_st;
// chain_ : number of chain
   low.assign(n, 0); dfn.assign(n, 0);
                                                                // tl, tr[ u ] : subtree interval in the seq. of u
  void add_edge(int u, int v) {
                                                                // chain_st[ u ] : head of the chain contains u // chian[ u ] : chain id of the chain u is on
   G[u].emplace_back(v, ecnt);
   G[v].emplace_back(u, ecnt++);
                                                                void predfs( int u, int f ) {
  void solve() {
                                                                 chain[ u ] = 0;
   ins.assign(ecnt, false);
                                                                 for ( int v : G[ u ] ) {
                                                                  if ( v == f ) continue;
   bcc.resize(ecnt); ecnt = 0;
```

```
predfs( v, u );
                                                              class MaxClique{
   if( lowbit( chain[ u ] ) < lowbit( chain[ v ] ) )</pre>
                                                              private:
    chain[ u ] = chain[ v ];
                                                               using bits = bitset< MAXN >;
                                                               bits popped, G[ MAXN ], ans;
size_t deg[ MAXN ], deo[ MAXN ], n;
  if ( not chain[ u ] )
   chain[ u ] = chain_ ++;
                                                               void sort_by_degree() {
                                                                popped.reset();
                                                                for ( size_t i = 0 ; i < n ; ++ i )</pre>
 void dfschain( int u, int f ) {
  fa[ u ][ 0 ] = f;
for ( int i = 1 ; i < LOG_N ; ++ i )
                                                                  deg[ i ] = G[ i ].count();
                                                                for ( size_t i = 0 ; i < n ; ++ i ) {
    size_t mi = MAXN, id = 0;</pre>
   fa[u][i] = fa[fa[u][i-1]][i-1];
                                                                  for ( size_t j = 0 ; j < n ; ++ j )
  if ( not popped[ j ] and deg[ j ] < mi )
    mi = deg[ id = j ];</pre>
  tl[ u ] = time_++;
  if ( not chain_st[ chain[ u ] ] )
   chain_st[ chain[ u ] ] = u;
                                                                  popped[ deo[ i ] = id ] = 1;
  for ( int v : G[ u ] )
   if ( v != f and chain[ v ] == chain[ u ] )
                                                                  for( size_t u = G[ i ]._Find_first() ;
  dfschain( v, u );
for ( int v : G[ u ] )
                                                                   u < n ; u = G[ i ]._Find_next( u ) )</pre>
                                                                    -- deg[ u ];
   if ( v != f and chain[ v ] != chain[ u ] )
                                                                }
    dfschain( v, u );
                                                               void BK( bits R, bits P, bits X ) {
  tr[ u ] = time_;
                                                                if (R.count()+P.count() <= ans.count()) return;</pre>
                                                                if ( not P.count() and not X.count() ) {
 bool anc( int u, int v )
 return tl[ u ] <= tl[ v ] and tr[ v ] <= tr[ u ];
                                                                 if ( R.count() > ans.count() ) ans = R;
                                                                 return:
public:
                                                                }
                                                                /* greedily chosse max degree as pivot
 int lca( int u, int v ) {
  if ( anc( u, v ) ) return u;
                                                                bits cur = P | X; size_t pivot = 0, sz = 0;
  for ( int i = LOG_N - 1 ; i >= 0 ; -- i )
                                                                for ( size_t u = cur._Find_first() ;
   if ( not anc( fa[ u ][ i ], v ) )
                                                                 u < n ; u = cur._Find_next( u )
    u = fa[ u ][ i ];
                                                                  if ( deg[ u ] > sz ) sz = deg[ pivot = u ];
                                                                cur = P & ( ~G[ pivot ] );
  return fa[ u ][ 0 ];
                                                                */ // or simply choose first
                                                                bits cur = P & (~G[ ( P | X )._Find_first() ]);
 void init( int n ) {
  fa.assign( ++n, vector< int >( LOG_N ) );
                                                                for ( size_t u = cur._Find_first()
  for (LOG_N = 0 ; (1 << LOG_N ) < n ; ++ LOG_N );
                                                                 u < n ; u = cur._Find_next( u ) ) {
                                                                 if ( R[ u ] ) continue;
  G.clear(); G.resize( n );
  tl.assign( n, 0 ); tr.assign( n, 0 )
                                                                 R[u] = 1;
  chain.assig( n, 0 ); chain_st.assign( n, 0 );
                                                                 BK( R, P & G[ u ], X & G[ u ] );
                                                                 R[u] = P[u] = 0, X[u] = 1;
 void add_edge( int u , int v ) {
  // 1-base
  G[ u ].push_back( v );
                                                              public:
  G[ v ].push_back( u );
                                                               void init( size_t n_ ) {
                                                                n = n_{-};
 }
 void decompose(){
                                                                for ( size_t i = 0 ; i < n ; ++ i )
                                                                 G[ i ].reset();
 chain_ = 1;
 predfs( 1, 1 );
                                                                ans.reset();
  time_{-} = 0;
 dfschain( 1, 1 );
                                                               void add_edges( int u, bits S ) { G[ u ] = S; }
                                                               void add_edge( int u, int v ) {
 PII get_subtree(int u) { return {tl[ u ],tr[ u ] }; }
                                                                G[u][v] = G[v][u] = 1;
 vector< PII > get_path( int u , int v ){
  vector< PII > res;
                                                               int solve() {
  int g = lca( u, v );
                                                                sort_by_degree(); // or simply iota( deo... )
  while ( chain[ u ] != chain[ g ] ) {
                                                                for ( size_t i = 0 ; i < n ; ++ i )</pre>
   int s = chain_st[ chain[ u ] ];
                                                                 deg[ i ] = G[ i ].count();
   res.emplace_back( tl[ s ], tl[ u ] + 1 );
                                                                bits pob, nob = 0; pob.set();
   u = fa[ s ][ 0 ];
                                                                for (size_t i=n; i<MAXN; ++i) pob[i] = 0;</pre>
                                                                for ( size_t i = 0 ; i < n ; ++ i ) {</pre>
  res.emplace_back( tl[ g ], tl[ u ] + 1 );
while ( chain[ v ] != chain[ g ] ) {
                                                                 size_t v = deo[ i ];
                                                                 bits tmp; tmp[ v ] = 1;
                                                                 BK( tmp, pob & G[ v ], nob & G[ v ] );
  int s = chain_st[ chain[ v ] ];
   res.emplace_back( tl[ s ], tl[ v ] + 1 );
                                                                 pob[v] = 0, nob[v] = 1;
   v = fa[ s ][ 0 ];
                                                                return static_cast< int >( ans.count() );
  res.emplace_back( tl[ g ] + 1, tl[ v ] + 1 );
                                                               }
  return res;
                                                              };
  /* res : list of intervals from u to v
                                                                   MaxCliqueDyn
   \star ( note only nodes work, not edge )
                                                              constexpr int kN = 150;
   * vector< PII >& path = tree.get_path( u , v )
                                                              struct MaxClique { // Maximum Clique
   * for( auto [ 1, r ] : path ) {
                                                               bitset<kN> a[kN], cs[kN];
   * 0-base [ 1, r )
                                                               int ans, sol[kN], q, cur[kN], d[kN], n;
   * }
                                                               void init(int _n) {
   */
                                                                n = _n; for (int i = 0; i < n; i++) a[i].reset();</pre>
} tree;
                                                               void addEdge(int u, int v) { a[u][v] = a[v][u] = 1; }
                                                               void csort(vector<int> &r, vector<int> &c)
3.5 MaxClique
                                                                int mx = 1, km = max(ans - q + 1, 1), t = 0,
// contain a self loop u to u, than u won't in clique
                                                                  m = int(r.size())
template < size_t MAXN >
                                                                cs[1].reset(); cs[2].reset();
```

addEdge(stk[i], stk[i + 1]);

```
for (int i = 0; i < m; i++) {</pre>
                                                             }
   int p = r[i], k = 1;
                                                               3.8 Centroid Decomposition
   while ((cs[k] & a[p]).count()) k++;
   if (k > mx) cs[++mx + 1].reset();
                                                               struct Centroid {
   cs[k][p] = 1;
                                                                vector<vector<int64_t>> Dist;
   if (k < km) r[t++] = p;
                                                                vector<int> Parent, Depth;
                                                                vector<int64_t> Sub, Sub2;
                                                                vector<int> Sz, Sz2;
  c.resize(m);
  if(t) c[t-1] = 0;
                                                                Centroid(vector<vector<pair<int, int>>> g) {
  for (int k = km; k <= mx; k++) {
  for (int p = int(cs[k]._Find_first());</pre>
                                                                 int N = g.size();
                                                                 vector<bool> Vis(N);
      p < kN; p = int(cs[k]._Find_next(p))) {</pre>
                                                                 vector<int> sz(N), mx(N);
    r[t] = p; c[t++] = k;
                                                                 vector<int> Path;
                                                                 Dist.resize(N)
  }
                                                                 Parent.resize(N);
                                                                 Depth.resize(N)
                                                                 auto DfsSz = [&](auto dfs, int x) -> void {
    Vis[x] = true; sz[x] = 1; mx[x] = 0;
 void dfs(vector<int> &r, vector<int> &c, int 1,
  bitset<kN> mask) {
                                                                  for (auto [u, w] : g[x]) {
  if (Vis[u]) continue;
  while (!r.empty()) {
   int p = r.back(); r.pop_back();
   mask[p] = 0;
                                                                   dfs(dfs, u)
   if (q + c.back() <= ans) return;</pre>
                                                                   sz[x] += sz[u];
   cur[q++] = p;
                                                                   mx[x] = max(mx[x], sz[u]);
   vector<int> nr, nc;
   bitset<kN> nmask = mask & a[p];
                                                                  Path.push_back(x);
   for (int i : r)
                                                                 }:
    if (a[p][i]) nr.push_back(i);
                                                                 auto DfsDist = [&](auto dfs, int x, int64_t D = 0)
   if (!nr.empty()) {
    if (1 < 4) {
                                                                  Dist[x].push_back(D);Vis[x] = true;
     for (int i : nr)
                                                                  for (auto [u, w] : g[x]) {
  if (Vis[u]) continue;
      d[i] = int((a[i] \& nmask).count());
                                                                   dfs(dfs, u, D + w);
     sort(nr.begin(), nr.end(),
      [&](int x, int y)
       return d[x] > d[y];
                                                                 }:
      });
                                                                 auto Dfs = [&]
                                                                  (auto dfs, int x, int D = 0, int p = -1)->void {
    csort(nr, nc); dfs(nr, nc, 1 + 1, nmask);
                                                                  Path.clear(); DfsSz(DfsSz, x);
   } else if (q > ans) {
                                                                  int M = Path.size();
    ans = q; copy(cur, cur + q, sol);
                                                                  int C = -1;
                                                                  for (int u : Path) {
   c.pop_back(); q--;
                                                                   if (max(M - sz[u], mx[u]) * 2 <= M) C = u;
                                                                   Vis[u] = false;
                                                                  DfsDist(DfsDist, C);
 int solve(bitset<kN> mask) { // vertex mask
  vector<int> r, c;
for (int i = 0; i < n; i++)</pre>
                                                                  for (int u : Path) Vis[u] = false;
                                                                  Parent[C] = p; Vis[C] = true;
   if (mask[i]) r.push_back(i);
                                                                  Depth[C] = D;
  for (int i = 0; i < n; i++)
                                                                  for (auto [u, w] : g[C]) {
   d[i] = int((a[i] & mask).count());
                                                                   if (Vis[u]) continue;
  sort(r.begin(), r.end(),
                                                                   dfs(dfs, u, D + 1, C);
   [&](int i, int j) { return d[i] > d[j]; });
                                                                  }
  csort(r, c);
  dfs(r, c, 1, mask);
                                                                 Dfs(Dfs, 0); Sub.resize(N); Sub2.resize(N);
  return ans; // sol[0 ~ ans-1]
                                                                 Sz.resize(N); Sz2.resize(N);
 }
} graph;
                                                                void Mark(int v) {
                                                                 int x = v, z = -1
3.7 Virtural Tree
                                                                 for (int i = Depth[v]; i >= 0; --i) {
  Sub[x] += Dist[v][i]; Sz[x]++;
inline bool cmp(const int &i, const int &j) {
return dfn[i] < dfn[j];</pre>
                                                                  if (z != -1) {
                                                                   Sub2[z] += Dist[v][i];
void build(int vectrices[], int k) {
                                                                   Sz2[z]++;
 static int stk[MAX_N];
                                                                  z = x; x = Parent[x];
 sort(vectrices, vectrices + k, cmp);
 stk[sz++] = 0;
 for (int i = 0; i < k; ++i) {
  int u = vectrices[i], lca = LCA(u, stk[sz - 1]);
                                                                int64_t Query(int v) {
  if (lca == stk[sz - 1]) stk[sz++] = u;
                                                                 int64_t res = 0;
                                                                 int x = v, z = -1
  else {
                                                                 for (int i = Depth[v]; i >= 0; --i) {
   while (sz \ge 2 \&\& dep[stk[sz - 2]] \ge dep[lca]) {
                                                                  res += Sub[x] + 1LL * Sz[x] * Dist[v][i];
    addEdge(stk[sz - 2], stk[sz - 1]);
                                                                  if (z != -1) res-=Sub2[z]+1LL*Sz2[z]*Dist[v][i];
    sz--;
                                                                  z = x; x = Parent[x];
   if (stk[sz - 1] != lca) {
                                                                 }
    addEdge(lca, stk[--sz]);
                                                                 return res;
    stk[sz++] = lca, vectrices[cnt++] = lca;
                                                              };
   stk[sz++] = u;
                                                               3.9 Tree Hashing
  }
                                                              uint64_t hsah(int u, int f) {
 for (int i = 0; i < sz - 1; ++i)
                                                               uint64_t r = 127;
```

for (int v : G[u]) if (v != f) {

```
uint64_t hh = hsah(v, u);
                                                                  stk[ stk_ ++ ] = u;
  r=(r+(hh*hh)%1010101333)%1011820613;
                                                                 bool inPath[ N ];
                                                                 void Diff( int u )
 return r;
                                                                  if ( inPath[ u ] ^= 1 ) { /*remove this edge*/ }
                                                                  else { /*add this edge*/ }
3.10 Minimum Mean Cycle
/* minimum mean cycle O(VE) */
                                                                 void traverse( int& origin_u, int u ) {
struct MMC{
                                                                  for ( int g = lca( origin_u, u )
#define FZ(n) memset((n),0,sizeof(n))
                                                                   origin_u != g ; origin_u = parent_of[ origin_u ] )
#define E 101010
                                                                    Diff( origin_u );
#define V 1021
                                                                  for (int v = u; v != origin_u; v = parent_of[v])
                                                                   Diff( v );
#define inf 1e9
 struct Edge { int v,u; double c; };
                                                                  origin_u = u;
 int n, m, prv[V][V], prve[V][V], vst[V];
                                                                 void solve() {
 Edge e[E];
                                                                  dfs(1,1);
 vector<int> edgeID, cycle, rho;
 double d[V][V];
                                                                  while ( stk_ ) block_id[ stk[ -- stk_ ] ] = block_;
                                                                  sort( que, que + q, [](const Que& x, const Que& y) {
 void init( int _n ) { n = _n; m = 0; }
                                                                   // WARNING: TYPE matters
 void add_edge( int vi , int ui , double ci )
 { e[ m ++ ] = { vi , ui , ci }; }
                                                                  } );
 void bellman_ford() {
                                                                  int U = 1, V = 1;
for ( int i = 0 ; i < q ; ++ i ) {
  for(int i=0; i<n; i++) d[0][i]=0;
                                                                   pass( U, que[ i ].u );
pass( V, que[ i ].v );
  for(int i=0; i<n; i++) {</pre>
   fill(d[i+1], d[i+1]+n, inf);
for(int j=0; j<m; j++) {
                                                                   // we could get our answer of que[ i ].id
    int v = e[j].v, u = e[j].u;
    if(d[i][v]<inf && d[i+1][u]>d[i][v]+e[j].c) {
                                                                 }
     d[i+1][u] = d[i][v]+e[j].c;
     prv[i+1][u] = v;
                                                                 Method 2:
     prve[i+1][u] = j;
                                                                 dfs u:
                                                                  push u
                                                                  iterate subtree
                                                                  push u
                                                                 Let P = LCA(u, v), and St(u) <= St(v)
                                                                 if (P == u) query[St(u), St(v)]
 double solve(){
                                                                 else query[Ed(u), St(v)], query[St(P), St(P)]
  // returns inf if no cycle, mmc otherwise
  double mmc=inf;
  int st = -1
                                                                 3.12 Minimum Steiner Tree
  bellman_ford();
                                                                 // Minimum Steiner Tree
  for(int i=0; i<n; i++) {</pre>
   double avg=-inf;
                                                                 // 0(V 3^T + V^2 2^T)
   for(int k=0; k<n; k++) {</pre>
                                                                 struct SteinerTree{
    if(d[n][i]<inf-eps)</pre>
                                                                 #define V 33
     avg=max(avg,(d[n][i]-d[k][i])/(n-k));
                                                                 #define T 8
                                                                 #define INF 1023456789
    else avg=max(avg,inf);
                                                                  int n , dst[V][V] , dp[1 << T][V] , tdst[V];</pre>
   if (avg < mmc) tie(mmc, st) = tie(avg, i);</pre>
                                                                  void init( int _n ){
                                                                   n = _n:
  FZ(vst);edgeID.clear();cycle.clear();rho.clear();
                                                                   for( int i = 0 ; i < n ; i ++ ){</pre>
                                                                    for( int j = 0 ; j < n ; j ++ )
dst[ i ][ j ] = INF;</pre>
  for (int i=n; !vst[st]; st=prv[i--][st]) {
   vst[st]++:
   edgeID.PB(prve[i][st]);
                                                                     dst[ i ][ i ] = 0;
   rho.PB(st);
                                                                   }
                                                                  void add_edge( int ui , int vi , int wi ){
  dst[ ui ][ vi ] = min( dst[ ui ][ vi ] , wi );
  dst[ vi ][ ui ] = min( dst[ vi ][ ui ] , wi );
  while (vst[st] != 2) {
   int v = rho.back(); rho.pop_back();
   cycle.PB(v);
   vst[v]++;
                                                                  void shortest_path(){
                                                                   for( int k = 0 ; k < n ; k ++ )</pre>
  reverse(ALL(edgeID));
                                                                    for( int i = 0 ; i < n ; i ++ )</pre>
  edgeID.resize(SZ(cycle));
                                                                      for( int j = 0 ; j < n ; j ++ )
dst[ i ][ j ] = min( dst[ i ][ j</pre>
  return mmc;
                                                                          dst[ i ][ k ] + dst[ k ][ j ] );
} mmc;
3.11 Mo's Algorithm on Tree
                                                                  int solve( const vector<int>& ter ){
int q; vector< int > G[N];
                                                                   int t = (int)ter.size();
struct Que{
                                                                   for( int i = 0 ; i < ( 1 << t ) ; i ++ )
                                                                    for( int j = 0 ; j < n ; j ++ )
dp[ i ][ j ] = INF;
int u, v,
} que[ N ];
           id:
int dfn[N], dfn_, block_id[N], block_, stk[N], stk_;
void dfs( int u, int f ) {
                                                                   for( int i = 0 ; i < n ; i ++ )</pre>
                                                                    dp[0][i] = 0;
                                                                    for( int msk = 1 ; msk < ( 1 << t ) ; msk ++ ){</pre>
 dfn[ u ] = dfn_++; int saved_rbp = stk_;
 for ( int v : G[ u ] ) {
                                                                    if( msk == ( msk & (-msk) ) ){
  if ( v == f ) continue;
                                                                      int who = __lg( msk );
for( int i = 0 ; i < n ; i ++ )</pre>
  dfs( v, u );
  if ( stk_ - saved_rbp < SQRT_N ) continue;</pre>
                                                                       dp[ msk ][ i ] = dst[ ter[ who ] ][ i ];
  for ( ++ block_ ; stk_ != saved_rbp ; )
  block_id[ stk[ -- stk_ ] ] = block_;
                                                                      continue;
                                                                     for( int i = 0 ; i < n ; i ++ )</pre>
```

```
for( int submsk = ( msk - 1 ) & msk ; submsk ;
         submsk = ( submsk - 1 ) & msk )
      dp[ msk ][ i ] = min( dp[ msk ][ i ],
              dp[ submsk ][ i ] +
              dp[ msk ^ submsk ][ i ] );
  for( int i = 0 ; i < n ; i ++ ){</pre>
   tdst[ i ] = INF;
   for( int j = 0 ; j < n ; j ++ )
     tdst[ i ] = min( tdst[ i ]
           dp[ msk ][ j ] + dst[ j ][ i ] );
  for( int i = 0 ; i < n ; i ++ )</pre>
   dp[ msk ][ i ] = tdst[ i ];
 int ans = INF;
 for( int i = 0 ; i < n ; i ++ )</pre>
  ans = min( ans , dp[ ( 1 << t ) - 1 ][ i ] );
 return ans:
} solver;
3.13
```

Directed Minimum Spanning Tree

```
template <typename T> struct DMST {
 T g[maxn][maxn], fw[maxn];
 int n, fr[maxn];
 bool vis[maxn], inc[maxn];
 void clear() {
  for(int i = 0; i < maxn; ++i) {</pre>
   for(int j = 0; j < maxn; ++j) g[i][j] = inf;</pre>
   vis[i] = inc[i] = false;
 void addEdge(int u,int v,T w){g[u][v]=min(g[u][v],w);}
 T operator()(int root, int _n) {
  n = n; T ans = 0;
  if (dfs(root) != n) return -1;
  while (true) {
   for(int i = 1;i <= n;++i) fw[i] = inf, fr[i] = i;</pre>
   for (int i = 1; i <= n; ++i) if (!inc[i]) {
    for (int j = 1; j <= n; ++j) {
  if (!inc[j] && i != j && g[j][i] < fw[i]) {</pre>
      fw[i] = g[j][i]; fr[i] = j;
   int x = -1;
   for(int i = 1;i <= n;++i)if(i != root && !inc[i]){</pre>
    int j = i, c = 0;
    while(j!=root && fr[j]!=i && c<=n) ++c, j=fr[j];</pre>
    if (j == root || c > n) continue;
    else { x = i; break; }
   if (!~x) {
    for (int i = 1; i <= n; ++i)</pre>
     if (i != root && !inc[i]) ans += fw[i];
    return ans:
   int y = x;
   for (int i = 1; i <= n; ++i) vis[i] = false;</pre>
    ans += fw[y]; y = fr[y]; vis[y] = inc[y] = true;
   } while (y != x);
   inc[x] = false;
   for (int k = 1; k <= n; ++k) if (vis[k]) {</pre>
    for (int j = 1; j <= n; ++j) if (!vis[j]) {
     if (g[x][j] > g[k][j]) g[x][j] = g[k][j];
if (g[j][k] < inf && g[j][k]-fw[k] < g[j][x])</pre>
      g[j][x] = g[j][k] - fw[k];
  return ans:
 int dfs(int now) {
  int r = 1; vis[now] = true;
  for (int i = 1; i <= n; ++i)
   if (g[now][i] < inf && !vis[i]) r += dfs(i);</pre>
  return r:
}:
```

```
namespace dominator {
vector<int> g[maxn], r[maxn], rdom[maxn];
int dfn[maxn], rev[maxn], fa[maxn], sdom[maxn];
int dom[maxn], val[maxn], rp[maxn], tk;
void init(int n) {
 // vertices are numbered from 0 to n-1
 fill(dfn, dfn + n, -1); fill(rev, rev + n, -1);
 fill(fa, fa + n, -1); fill(val, val + n, -1);
 fill(sdom, sdom + n, -1); fill(rp, rp + n, -1);
 fill(dom, dom + n, -1); tk = 0;
for (int i = 0; i < n; ++i) {
  g[i].clear(); r[i].clear(); rdom[i].clear();
 }
void add_edge(int x, int y) { g[x].push_back(y); }
void dfs(int x) {
 rev[dfn[x] = tk] = x;
 fa[tk] = sdom[tk] = val[tk] = tk; tk ++;
 for (int u : g[x]) {
  if (dfn[u] == -1) dfs(u), rp[dfn[u]] = dfn[x];
  r[dfn[u]].push_back(dfn[x]);
void merge(int x, int y) { fa[x] = y; }
int find(int x, int c = 0) {
 if (fa[x] == x) return c ? -1 : x;
 int p = find(fa[x], 1);
 if (p == -1) return c ? fa[x] : val[x];
 if (sdom[val[x]]>sdom[val[fa[x]]]) val[x]=val[fa[x]];
 fa[x] = p;
 return c ? p : val[x];
vector<int> build(int s, int n) {
// return the father of each node in the dominator tree
// p[i] = -2 if i is unreachable from s
 dfs(s);
 for (int i = tk - 1; i >= 0; --i)
  for (int u:r[i]) sdom[i]=min(sdom[i],sdom[find(u)]);
  if (i) rdom[sdom[i]].push_back(i);
  for (int &u : rdom[i]) {
   int p = find(u);
   if (sdom[p] == i) dom[u] = i;
else dom[u] = p;
  if (i) merge(i, rp[i]);
 vector<int> p(n, -2); p[s] = -1;
 for (int i = 1; i < tk; ++i)
if (sdom[i] != dom[i]) dom[i] = dom[dom[i]];</pre>
 for (int i = 1; i < tk; ++i) p[rev[i]] = rev[dom[i]];</pre>
 return p;
3.15 Edge Coloring
// max(d_u) + 1 edge coloring, time: O(NM)
int C[kN][kN], G[kN][kN]; // 1-based, G: ans
void clear(int N) {
 for (int i = 0; i <= N; i++)</pre>
       (int j = 0; j \le N; j++)
    C[i][j] = G[i][j] = 0;
void solve(vector<pair<int, int>> &E, int N) {
 int X[kN] = {}, a;
auto update = [&](int u) {
  for (X[u] = 1; C[u][X[u]]; X[u]++);
 auto color = [&](int u, int v, int c) {
  int p = G[u][v];
  G[u][v] = G[v][u] = c;
  C[u][c] = v, C[v][c] = u;
  C[u][p] = C[v][p] = 0;
  if(p) X[u] = X[v] = p
  else update(u), update(v);
  return p;
 auto flip = [&](int u, int c1, int c2) {
  int p = C[u][c1];
  swap(C[u][c1], C[u][c2]);
  if (p) G[u][p] = G[p][u] = c2;
if (!C[u][c1]) X[u] = c1;
if (!C[u][c2]) X[u] = c2;
  return p;
```

3.14 Dominator Tree

```
for (int i = 1; i <= N; i++) X[i] = 1;
 for (int t = 0; t < E.size(); t++) {</pre>
  auto [u, v] = E[t];
  int v0 = v, c = X[u], c0 = c, d;
  vector<pair<int, int>> L; int vst[kN] = {};
  while (!G[u][v0]) {
   L.emplace_back(v, d = X[v]);
   if (!C[v][c]) for(a=L.size()-1;a>=0;a--)
   c = color(u, L[a].first, c);
else if(!C[u][d])for(a=L.size()-1;a>=0;a--)
     color(u, L[a].first, L[a].second);
   else if (vst[d]) break
   else vst[d] = 1, v = C[u][d];
  if (!G[u][v0]) {
  for (; v; v = flip(v, c, d), swap(c, d));
   if (C[u][c0]) { a = int(L.size()) - 1;
    while (--a >= 0 && L[a].second != c);
    for(;a>=0;a--)color(u,L[a].first,L[a].second);
   } else t--;
}
```

4 Matching & Flow

4.1 Kuhn Munkres

```
class KM {
private:
 static constexpr 1ld INF = 1LL << 60;</pre>
 vector<lld> h1,hr,slk;
 vector<int> fl,fr,pre,qu;
 vector<vector<lld>> w;
 vector<bool> v1,vr;
 int n, ql, qr;
 bool check(int x) {
  if (v1[x] = true, f1[x] != -1)
   return vr[qu[qr++] = f1[x]] = true;
  while (x != -1) swap(x, fr[fl[x] = pre[x]]);
  return false;
 void bfs(int s) {
  fill(slk.begin(), slk.end(), INF);
  fill(v1.begin(), v1.end(), false);
fill(vr.begin(), vr.end(), false);
  ql = qr = 0;
  qu[qr++] = s;
  vr[s] = true;
  while (true) {
   11d d;
   while (ql < qr) {</pre>
    for (int x = 0, y = qu[ql++]; x < n; ++x) {
     if(!v1[x]&&slk[x]>=(d=h1[x]+hr[y]-w[x][y])){
      if (pre[x] = y, d) slk[x] = d;
else if (!check(x)) return;
     }
    }
   d = INF;
   for (int x = 0; x < n; ++x)
if (!v1[x] && d > s1k[x]) d = s1k[x];
   for (int x = 0; x < n; ++x) {
    if (v1[x]) h1[x] += d;
    else slk[x] -= d;
    if (vr[x]) hr[x] -= d;
   for (int x = 0; x < n; ++x)
    if (!v1[x] && !slk[x] && !check(x)) return;
  }
public:
 void init( int n_ ) {
 n = n_; qu.resize(n);
  fl.clear(); fl.resize(n, -1)
  fr.clear(); fr.resize(n, -1);
 hr.clear(); hr.resize(n); hl.resize(n);
 w.clear(); w.resize(n, vector<lld>(n));
  slk.resize(n); pre.resize(n);
  vl.resize(n); vr.resize(n);
 void set_edge( int u, int v, lld x ) {w[u][v] = x;}
```

```
11d solve() {
  for (int i = 0; i < n; ++i)
   hl[i] = *max_element(w[i].begin(), w[i].end());
  for (int i = 0; i < n; ++i) bfs(i);</pre>
  11d res = 0;
  for (int i = 0; i < n; ++i) res += w[i][f1[i]];</pre>
  return res;
} km;
4.2 Bipartite Matching
class BipartiteMatching{
private:
 vector<int> X[N], Y[N];
 int fX[N], fY[N], n;
 bitset<N> walked;
 bool dfs(int x)
  for(auto i:X[x]){
   if(walked[i])continue;
   walked[i]=1;
   if(fY[i]==-1||dfs(fY[i])){
    fY[i]=x;fX[x]=i;
    return 1;
  return 0;
public:
 void init(int _n){
  n=_n; walked.reset();
  for(int i=0;i<n;i++){</pre>
   X[i].clear();Y[i].clear();
   fX[i]=fY[i]=-1;
  }
 void add_edge(int x, int y){
  X[x].push_back(y); Y[y].push_back(y);
 int solve(){
  int cnt = 0:
  for(int i=0;i<n;i++){</pre>
   walked.reset();
   if(dfs(i)) cnt++;
  // return how many pair matched
  return cnt;
};
4.3 General Graph Matching
namespace matching {
int fa[kN], pre[kN], match[kN], s[kN], v[kN];
vector<int> g[kN];
queue<int> q;
for (int i = 0; i < n; ++i) g[i].clear();</pre>
void AddEdge(int u, int v) {
 g[u].push_back(v);
 g[v].push_back(u);
int Find(int u) {
return u == fa[u] ? u : fa[u] = Find(fa[u]);
int LCA(int x, int y, int n) {
 static int tk = 0; tk++;
 x = Find(x), y = Find(y);
 for (; ; swap(x, y)) {
  if (x != n) {
   if (v[x] == tk) return x;
   v[x] = tk;
   x = Find(pre[match[x]]);
  }
void Blossom(int x, int y, int l) {
  while (Find(x) != 1) {
  pre[x] = y, y = match[x];
if (s[y] == 1) q.push(y), s[y] = 0;
if (fa[x] == x) fa[x] = 1;
```

if (fa[y] == y) fa[y] = 1;

while (true){

```
int found = 0;
  x = pre[y];
                                                                for (int i=0; i<n; i++)</pre>
                                                                 dis[i] = onstk[i] = 0;
bool Bfs(int r, int n) {
                                                                for (int i=0; i<n; i++){</pre>
for (int i = 0; i \le n; ++i) fa[i] = i, s[i] = -1;
                                                                 stk.clear()
while (!q.empty()) q.pop();
                                                                 if (!onstk[i] && SPFA(i)){
q.push(r);
                                                                  found = 1;
                                                                  while (SZ(stk)>=2){
s[r] = 0;
while (!q.empty()) {
                                                                   int u = stk.back(); stk.pop_back();
 int x = q.front(); q.pop();
for (int u : g[x]) {
                                                                   int v = stk.back(); stk.pop_back();
                                                                   match[u] = v;
  if (s[u] == -1) {
                                                                   match[v] = u;
    pre[u] = x, s[u] = 1;
    if (match[u] == n) {
                                                                 }
     for (int a = u, b = x, last; b != n; a = last, b =
                                                                if (!found) break;
     pre[a])
      last = match[b], match[b] = a, match[a] = b;
     return true;
                                                               int ret = 0;
                                                               for (int i=0; i<n; i++)
    q.push(match[u]);
                                                                ret += edge[i][match[i]];
    s[match[u]] = 0;
                                                               return ret>>1;
   } else if (!s[u] && Find(u) != Find(x)) {
   int 1 = LCA(u, x, n);
Blossom(x, u, 1);
                                                             } graph;
                                                                   Minimum Cost Circulation
    Blossom(u, x, 1);
                                                             struct Edge { int to, cap, rev, cost; };
  }
                                                             vector<Edge> g[kN];
int dist[kN], pv[kN], ed[kN];
return false;
                                                             bool mark[kN];
                                                             int NegativeCycle(int n) {
int Solve(int n) {
                                                              memset(mark, false, sizeof(mark));
                                                              memset(dist, 0, sizeof(dist));
int res = 0;
 for (int x = 0; x < n; ++x) {
                                                              int upd = -1:
 if (match[x] == n) res += Bfs(x, n);
                                                              for (int i = 0; i <= n; ++i)
                                                               for (int j = 0; j < n; ++j) {
return res;
                                                                int idx = 0;
}}
                                                                for (auto &e : g[j]) {
                                                                 if(e.cap > 0 && dist[e.to] > dist[j] + e.cost){
      Minimum Weight Matching (Clique version)
                                                                  dist[e.to] = dist[j] + e.cost;
struct Graph {
                                                                  pv[e.to] = j, ed[e.to] = idx;
// 0-base (Perfect Match)
                                                                  if (i == n) {
int n, edge[MXN][MXN];
                                                                   upd = j;
int match[MXN], dis[MXN], onstk[MXN];
                                                                   while(!mark[upd])mark[upd]=1,upd=pv[upd];
vector<int> stk;
                                                                   return upd;
void init(int _n) {
                                                                  }
 n = _n;
 for (int i=0; i<n; i++)</pre>
                                                                 idx++;
   for (int j=0; j<n; j++)</pre>
    edge[i][j] = 0;
                                                               }
void set_edge(int u, int v, int w) {
                                                              return -1;
 edge[u][v] = edge[v][u] = w;
                                                             int Solve(int n) {
bool SPFA(int u){
                                                              int rt = -1, ans = 0;
 if (onstk[u]) return true;
                                                              while ((rt = NegativeCycle(n)) >= 0) {
  stk.PB(u);
                                                               memset(mark, false, sizeof(mark));
  onstk[u] = 1;
                                                               vector<pair<int, int>> cyc;
  for (int v=0; v<n; v++){</pre>
                                                               while (!mark[rt]) {
   if (u != v && match[u] != v && !onstk[v]){
                                                                cyc.emplace_back(pv[rt], ed[rt]);
    int m = match[v];
                                                                mark[rt] = true;
    if (dis[m] > dis[u] - edge[v][m] + edge[u][v]){
                                                                rt = pv[rt];
     dis[m] = dis[u] - edge[v][m] + edge[u][v];
     onstk[v] = 1;
                                                               reverse(cyc.begin(), cyc.end());
     stk.PB(v)
                                                               int cap = kInf;
     if (SPFA(m)) return true;
                                                               for (auto &i : cyc)
     stk.pop_back();
                                                                auto &e = g[i.first][i.second];
     onstk[v] = 0;
                                                                cap = min(cap, e.cap);
                                                               for (auto &i : cyc)
                                                                auto &e = g[i.first][i.second];
 onstk[u] = 0
                                                                e.cap -= cap;
  stk.pop_back();
                                                                g[e.to][e.rev].cap += cap;
  return false;
                                                                ans += e.cost * cap;
                                                               }
int solve() {
                                                              return ans;
  // find a match
  for (int i=0; i<n; i+=2){
  match[i] = i+1;
                                                             4.6 Flow Models
  match[i+1] = i;

    Maximum/Minimum flow with lower bound / Circulation problem
```

1. Construct super source S and sink T.

2. For each edge (x,y,l,u), connect $x \to y$ with capacity u-l.

- 3. For each vertex \emph{v} , denote by $in(\emph{v})$ the difference between the sum of incoming lower bounds and the sum of outgoing lower bounds.
- 4. If in(v)>0, connect $S\to v$ with capacity in(v), otherwise, connect v o T with capacity -in(v).
 - To maximize, connect $t \to s$ with capacity ∞ (skip this in circulation problem), and let f be the maximum flow from S to T. If $f
 eq \sum_{v \in V, in(v) > 0} in(v)$, there's no solution. Otherwise, the
 - maximum flow from s to t is the answer. To minimize, let f be the maximum flow from S to T. Connect t o s with capacity ∞ and let the flow from S to T be f'. If $f+f'\neq \sum_{v\in V, in(v)>0}in(v)$, there's no solution. Otherwise, f' is the answer.
- 5. The solution of each edge e is l_e+f_e , where f_e corresponds to the flow of edge e on the graph.
- ullet Construct minimum vertex cover from maximum matching M on bipartite $\operatorname{graph}\left(X,Y\right)$
 - 1. Redirect every edge: $y \to x$ if $(x,y) \in M, x \to y$ otherwise. 2. DFS from unmatched vertices in X.

 - 3. $x \in X$ is chosen iff x is unvisited.
 - 4. $y \in Y$ is chosen iff y is visited.
- · Minimum cost cyclic flow
 - 1. Consruct super source ${\cal S}$ and sink ${\cal T}$
 - 2. For each edge (x,y,c), connect $x \to y$ with (cost,cap)=(c,1) if c>0, otherwise connect $y \to x$ with (cost,cap)=(-c,1)
 - 3. For each edge with c < 0, sum these cost as K, then increase d(y)by 1, decrease d(x) by 1
 - 4. For each vertex v with d(v)>0, connect $S\to v$ with (cost, cap)=(0, d(v))
 - 5. For each vertex v with d(v) < 0, connect $v \to T$ with (cost, cap) =(0, -d(v))
 - 6. Flow from S to T, the answer is the cost of the flow C+K
- · Maximum density induced subgraph
 - 1. Binary search on answer, suppose we're checking answer ${\cal T}$
 - 2. Construct a max flow model, let ${\cal K}$ be the sum of all weights
 - 3. Connect source $s \to v, v \in G$ with capacity K
 - 4. For each edge (u, v, w) in G, connect $u \to v$ and $v \to u$ with capacity
 - 5. For $v \in \mathit{G}$, connect it with sink $v \rightarrow t$ with capacity K + 2T - $\left(\sum_{e \in E(v)} w(e)\right) - 2w(v)$
 - 6. T is a valid answer if the maximum flow f < K|V|
- · Minimum weight edge cover
 - 1. For each $v \in V$ create a copy v', and connect $u' \to v'$ with weight
 - 2. Connect v
 ightarrow v' with weight $2\mu(v)$, where $\mu(v)$ is the cost of the cheapest edge incident to v.
 - 3. Find the minimum weight perfect matching on G'.
- · Project selection problem
 - 1. If $p_v>0$, create edge (s,v) with capacity p_v ; otherwise, create edge in $p_v > 0$, refer eagle (s,v) with capacity p_v , other wise, a rate eagle (v,t) with capacity $-p_v$. 2. Create edge (u,v) with capacity w with w being the cost of choosing
 - u without choosing \overline{v}
 - 3. The mincut is equivalent to the maximum profit of a subset of projects.
- 0/1 quadratic programming

$$\sum_{x} c_{x} x + \sum_{y} c_{y} \bar{y} + \sum_{xy} c_{xy} x \bar{y} + \sum_{xyx'y'} c_{xyx'y'} (x \bar{y} + x' \bar{y'})$$

can be minimized by the mincut of the following graph:

- 1. Create edge (x,t) with capacity c_x and create edge (s,y) with ca-
- pacity c_y .

 2. Create edge (x,y) with capacity c_{xy} .

 3. Create edge (x,y) and edge (x',y') with capacity $c_{xyx'y'}$.

Dinic

```
template <typename Cap = int64_t>
class Dinic{
private:
struct Edge{
 int to, rev;
 Cap cap;
int n, st, ed;
vector<vector<Edge>> G;
vector<int> lv, idx;
bool BFS(){
 fill(lv.begin(), lv.end(), -1);
 queue<int> bfs;
 bfs.push(st); lv[st] = 0;
 while(!bfs.empty()){
   int u = bfs.front(); bfs.pop();
   for(auto e: G[u]){
    if(e.cap <= 0 or lv[e.to]!=-1) continue;</pre>
    bfs.push(e.to); lv[e.to] = lv[u] + 1;
```

```
return (lv[ed]!=-1);
 Cap DFS(int u, Cap f){
  if(u == ed) return f;
  Cap ret = 0;
  for(int &i = idx[u]; i < (int)G[u].size(); ++i){</pre>
   auto &e = G[u][i];
   if(e.cap <= 0 or lv[e.to]!=lv[u]+1) continue;</pre>
   Cap nf = DFS(e.to, min(f, e.cap));
ret += nf; e.cap -= nf; f -= nf;
   G[e.to][e.rev].cap += nf;
   if(f == 0) return ret;
  if(ret == 0) lv[u] = -1;
  return ret;
public:
 void init(int n_, int st_, int ed_){
  n = n_{,} st = st_{,} ed = ed_{,}
  G.resize(n); lv.resize(n);
  fill(G.begin(), G.end(), vector<Edge>());
 void add_edge(int u, int v, Cap c){
  G[u].push_back({v, (int)G[v].size(), c});
  G[v].push_back({u, ((int)G[u].size())-1, 0});
 Cap max_flow(){
  Cap ret = 0;
  while(BFS()){
   idx.assign(n, 0);
   Cap f = DFS(st, numeric_limits<Cap>::max());
   ret += f;
   if(f == 0) break;
  return ret;
};
```

```
Minimum Cost Maximum Flow
class MiniCostMaxiFlow{
using Cap = int; using Wei = int64_t;
using PCW = pair<Cap,Wei>;
static constexpr Cap INF_CAP = 1 << 30;</pre>
static constexpr Wei INF_WEI = 1LL<<60;</pre>
private:
struct Edge{
 int to, back;
 Cap cap; Wei wei;
 Edge() {}
 Edge(int a,int b, Cap c, Wei d):
  to(a),back(b),cap(c),wei(d)
 {}
int ori, edd;
vector<vector<Edge>> G;
vector<int> fa, wh;
vector<bool> inq;
vector<Wei> dis;
PCW SPFA(){
 fill(inq.begin(),inq.end(),false);
 fill(dis.begin(), dis.end(), INF_WEI);
 queue<int> qq; qq.push(ori);
 dis[ori] = 0;
 while(not qq.empty()){
   int u=qq.front();qq.pop();
   inq[u] = false
   for(int i=0;i<SZ(G[u]);++i){</pre>
   Edge e=G[u][i];
    int v=e.to; Wei d=e.wei;
    if(e.cap<=0||dis[v]<=dis[u]+d)</pre>
    continue;
    dis[v] = dis[u] + d:
    fa[v] = u, wh[v] = i;
    if (inq[v]) continue;
    qq.push(v);
   inq[v] = true;
  }
 if(dis[edd]==INF_WEI) return {-1, -1};
 Cap mw=INF_CAP;
 for(int i=edd;i!=ori;i=fa[i])
  mw=min(mw,G[fa[i]][wh[i]].cap);
```

2008033571, 2011186739, 2039465081, 2039728567

2093735719, 2116097521, 2123852629, 2140170259, 3148478261, 3153064147, 3176351071, 3187523093,

```
for (int i=edd;i!=ori;i=fa[i]){
                                                                      3196772239, 3201312913, 3203063977, 3204840059,\\
                                                                     \begin{matrix} 3210224309, 3213032591, 3217689851, 3218469083, \\ 3219857533, 3231880427, 3235951699, 3273767923, \end{matrix}
   auto &eg=G[fa[i]][wh[i]];
   eg.cap -= mw;
                                                                     3276188869, 3277183181, 3282463507, 3285553889, \\ 3319309027, 3327005333, 3327574903, 3341387953, \\
   G[eg.to][eg.back].cap+=mw;
                                                                      3373293941, 3380077549, 3380892997, 3381118801
  return {mw, dis[edd]};
                                                                           \lfloor \frac{n}{i} \rfloor Enumeration
                                                                      T_0 = 1, T_{i+1} = \lfloor \frac{n}{\lfloor \frac{n}{T_i + 1} \rfloor} \rfloor
public:
 void init(int a,int b,int n){
                                                                      5.3 ax+by=gcd
  ori=a,edd=b;
                                                                      // ax+ny = 1, ax+ny == ax == 1 \pmod{n}
  G.clear();G.resize(n);
                                                                      void exgcd(lld x,lld y,lld &g,lld &a,lld &b) {
  fa.resize(n);wh.resize(n);
                                                                       if (y == 0) g=x, a=1, b=0;
  inq.resize(n); dis.resize(n);
                                                                       else exgcd(y, x\%y, g, b, a), b=(x/y)*a;
 void add_edge(int st, int ed, Cap c, Wei w){
  G[st].emplace\_back(ed,SZ(G[ed]),c,w);
                                                                      5.4 Pollard Rho
  G[ed].emplace_back(st,SZ(G[st])-1,0,-w);
                                                                     // does not work when n is prime
 PCW solve(){
                                                                      // return any non-trivial factor
                                                                     llu pollard_rho(llu n){
  Cap cc=0; Wei ww=0;
                                                                       static auto f=[](llu x,llu k,llu m){
  while(true){
                                                                        return add(k,mul(x,x,m),m);
   PCW ret=SPFA();
   if(ret.first==-1) break;
                                                                       if (!(n&1)) return 2;
   cc+=ret.first;
                                                                       mt19937 rnd(120821011);
   ww+=ret.first * ret.second;
                                                                       while(true){
                                                                        llu y=2,yy=y,x=rnd()%n,t=1;
  return {cc,ww};
                                                                        for(llu sz=2;t==1;sz<<=1) {</pre>
                                                                         for(llu i=0;i<sz;++i){</pre>
} mcmf;
                                                                          if(t!=1)break;
                                                                          yy=f(yy,x,n);
4.9
       Global Min-Cut
                                                                          t=gcd(yy>y?yy-y:y-yy,n);
const int maxn = 500 + 5;
int w[maxn][maxn], g[maxn];
                                                                         y=yy;
bool v[maxn], del[maxn];
void add_edge(int x, int y, int c) {
                                                                        if(t!=1&&t!=n) return t;
w[x][y] += c; w[y][x] += c;
pair<int, int> phase(int n) {
memset(v, false, sizeof(v));
                                                                      5.5 Pi Count (Linear Sieve)
 memset(g, 0, sizeof(g));
                                                                      static constexpr int N = 1000000 + 5;
 int s = -1, t = -1;
                                                                      11d pi[N];
 while (true) {
                                                                     vector<int> primes;
  int c = -1;
                                                                      bool sieved[N];
  for (int i = 0; i < n; ++i) {
                                                                     11d cube_root(11d x){
   if (del[i] || v[i]) continue;
                                                                       lld s=cbrt(x-static_cast<long double>(0.1));
   if (c == -1 \mid | g[i] > g[c]) c = i;
                                                                       while(s*s*s <= x) ++s;</pre>
  if (c == -1) break;
                                                                       return s-1;
  v[s = t, t = c] = true;
for (int i = 0; i < n; ++i) {
                                                                      11d square_root(11d x){
                                                                       lld s=sqrt(x-static_cast<long double>(0.1));
   if (del[i] || v[i]) continue;
                                                                       while(s*s <= x) ++s;
   g[i] += w[c][i];
                                                                       return s-1;
  }
                                                                      void init(){
 return make_pair(s, t);
                                                                       primes.reserve(N);
                                                                       primes.push_back(1);
int mincut(int n) {
                                                                       for(int i=2;i<N;i++) {</pre>
int cut = 1e9;
                                                                        if(!sieved[i]) primes.push_back(i);
 memset(del, false, sizeof(del));
                                                                        pi[i] = !sieved[i] + pi[i-1];
 for (int i = 0; i < n - 1; ++i) {
                                                                        for(int p: primes) if(p > 1) {
  if(p * i >= N) break;
  int s, t; tie(s, t) = phase(n);
  del[t] = true; cut = min(cut, g[t]);
                                                                         sieved[p * i] = true;
  for (int j = 0; j < n; ++j) {
  w[s][j] += w[t][j]; w[j][s] += w[j][t];</pre>
                                                                         if(p % i == 0) break;
  }
 }
 return cut;
                                                                      11d phi(11d m, 11d n) {
                                                                       static constexpr int MM = 80000, NN = 500;
                                                                       static lld val[MM][NN];
5
     Math
                                                                       if(m<MM&&n<NN&&val[m][n])return val[m][n]-1;</pre>
                                                                       if(n == 0) return m;
      Prime Table
                                                                       if(primes[n] >= m) return 1;
1002939109, 1020288887, 1028798297, 1038684299,\\
                                                                       11d ret = phi(m,n-1)-phi(m/primes[n],n-1);
1041211027, 1051762951, 1058585963, 1063020809,
                                                                       if(m < MM\&n < NN) val[m][n] = ret+1;
\begin{array}{c} 1147930723, 1172520109, 1183835981, 1187659051, \\ 1241251303, 1247184097, 1255940849, 1272759031, \\ 1287027493, 1288511629, 1294632499, 1312650799, \end{array}
                                                                       return ret;
1868732623, 1884198443, 1884616807, 1885059541,
                                                                     11d pi_count(11d);
1909942399, 1914471137, 1923951707, 1925453197,\\
                                                                     11d P2(11d m, 11d n) {
1979612177, 1980446837, 1989761941, 2007826547, \\
                                                                       lld sm = square_root(m), ret = 0;
```

for(lld i = n+1;primes[i]<=sm;i++)</pre>

ret+=pi_count(m/primes[i])-pi_count(primes[i])+1;

```
return ret;
}
lld pi_count(lld m) {
  if(m < N) return pi[m];
  lld n = pi_count(cube_root(m));
  return phi(m, n) + n - 1 - P2(m, n);
}</pre>
```

5.6 Strling Number

5.6.1 First Kind

 $S_1(n,k)$ counts the number of permutations of n elements with k disjoint cycles.

$$S_1(n,k) = (n-1) \cdot S_1(n-1,k) + S_1(n-1,k-1)$$

$$x(x+1) \dots (x+n-1) = \sum_{k=0}^n S_1(n,k) x^k$$

$$g(x) = x(x+1) \dots (x+n-1) = \sum_{k=0}^n a_k x^k$$

$$\Rightarrow g(x+n) = \sum_{k=0}^n \frac{b_k}{(n-k)!} x^{n-k},$$

$$b_k = \sum_{i=0}^k ((n-i)! a_{n-i}) \cdot (\frac{n^{k-i}}{(k-i)!})$$

5.6.2 Second Kind

 $S_2(n,k)$ counts the number of ways to partition a set of n elements into k nonempty sets.

$$S_2(n,k) = S_2(n-1,k-1) + k \cdot S_2(n-1,k)$$

$$S_2(n,k) = \sum_{i=0}^k {k \choose i} i^n (-1)^{k-i} = \sum_{i=0}^k \frac{(-1)^i}{i!} \cdot \frac{(k-i)^n}{(k-i)!}$$

5.7 Range Sieve

5.8 Miller Rabin

```
bool isprime(llu x){
static llu magic[j={2,325,9375,28178,\
          450775,9780504,1795265022};
static auto witn=[](llu a,llu u,llu n,int t)
->bool{
 if (!(a = mpow(a%n,u,n)))return 0;
 while(t--){
  1lu a2=mul(a,a,n);
  if(a2==1 && a!=1 && a!=n-1)
    return 1;
  a = a2;
 }
 return a!=1;
if(x<2)return 0;</pre>
if(!(x&1))return x==2;
1lu x1=x-1;int t=0;
while(!(x1&1))x1>>=1,t++;
for(llu m:magic)if(witn(m,x1,x,t))return 0;
return 1;
```

5.9 Inverse Element

```
// x's inverse mod k
long long GetInv(long long x, long long k){
  // k is prime: euler_(k)=k-1
  return qPow(x, euler_phi(k)-1);
}
// if you need [1, x] (most use: [1, k-1]
  void solve(int x, long long k){
  inv[1] = 1;
  for(int i=2;i<x;i++)
   inv[i] = ((long long)(k - k/i) * inv[k % i]) % k;
}</pre>
```

5.10 Extended Euler

```
a^b \equiv \begin{cases} a^b \mod \varphi(m) + \varphi(m) & \text{if } (a,m) \neq 1 \land b \geq \varphi(m) \\ a^b \mod \varphi(m) & \text{otherwise} \end{cases} \pmod m
```

5.11 Gauss Elimination

```
void gauss(vector<vector<double>> &d) {
  int n = d.size(), m = d[0].size();
  for (int i = 0; i < m; ++i) {
    int p = -1;
    for (int j = i; j < n; ++j) {
        if (fabs(d[j][i]) < eps) continue;
        if (p == -1 || fabs(d[j][i])>fabs(d[p][i])) p=j;
    }
    if (p == -1) continue;
    for (int j = 0; j < m; ++j) swap(d[p][j], d[i][j]);
    for (int j = 0; j < n; ++j) {
        if (i == j) continue;
        double z = d[j][i] / d[i][i];
        for (int k = 0; k < m; ++k) d[j][k] -= z*d[i][k];
    }
}</pre>
```

5.12 Fast Fourier Transform

```
namespace fft {
using VI = vector<int>;
using VL = vector<long long>;
const double pi = acos(-1);
cplx omega[maxn + 1];
void prefft() {
 generate_n(omega, maxn + 1, [i=0]()mutable{
  auto j = i++;
  return cplx(cos(2*pi*j/maxn), sin(2*pi*j/maxn));
 });
void fft(vector<cplx> &v, int n) {
 int z = __builtin_ctz(n) - 1;
 for (int i = 0; i < n; ++i) {
  int x = 0, j = 0;
  for (;(1 << j) < n;++j) x^{=(i >> j & 1)<<(z - j);
  if (x > i) swap(v[x], v[i]);
 for (int s = 2; s <= n; s <<= 1) {
  int z = s >> 1;
  for (int i = 0; i < n; i += s) {
   for (int k = 0; k < z; ++k) {
  cplx x = v[i + z + k] * omega[maxn / s * k];
  v[i + z + k] = v[i + k] - x;</pre>
    v[i+k] = v[i+k] + x;
void ifft(vector<cplx> &v, int n) {
 fft(v, n);
 reverse(v.begin() + 1, v.end());
 for (int i=0;i<n;++i) v[i] = v[i] * cplx(1. / n, 0);
VL convolution(const VI &a, const VI &b) {
 // Should be able to handle N <= 10^5, C <= 10^4
 int sz = 1;
 while (sz < a.size() + b.size() - 1) sz <<= 1;</pre>
 vector<cplx> v(sz);
 for (int i = 0; i < sz; ++i) {
  double re = i < a.size() ? a[i] : 0;</pre>
  double im = i < b.size() ? b[i] : 0;</pre>
  v[i] = cplx(re, im);
```

for(size_t j=0;j<p[t].size();++j)</pre>

```
fft(v, sz);
                                                                  d[i]+=x[i-j-1]*p[t][j];
                                                                 if(abs(d[i]-=x[i])<=EPS)continue;</pre>
 for (int i = 0; i \le sz / 2; ++i) {
  int j = (sz - i) & (sz - 1);
                                                                 f[t]=i;if(!t){p[++t].resize(i);continue;}
  cplx x = (v[i] + v[j].conj()) * (v[i] - v[j].conj())
                                                                 vector<llf> cur(i-f[b]-1);
    * cplx(0, -0.25);
                                                                 11f k=-d[i]/d[f[b]];cur.PB(-k);
  if (j != i) v[j] = (v[j] + v[i].conj()) * (v[j] - v[i
                                                                 for(size_t j=0;j<p[b].size();j++)</pre>
    ].conj()) * cplx(0, -0.25);
                                                                  cur.PB(p[b][j]*k);
  v[i] = x;
                                                                 if(cur.size()<p[t].size())cur.resize(p[t].size());</pre>
                                                                 for(size_t j=0;j<p[t].size();j++)cur[j]+=p[t][j];</pre>
 ifft(v, sz);
                                                                 if(i-f[b]+p[b].size()>=p[t].size()) b=t;
 VL c(sz);
                                                                 p[++t]=cur;
 for (int i = 0; i < sz; ++i) c[i] = round(v[i].re);</pre>
                                                                return p[t];
 return c;
VI convolution_mod(const VI &a, const VI &b, int p) {
                                                               5.15 NTT
 int sz = 1;
 while (sz + 1 < a.size() + b.size()) sz <<= 1;</pre>
                                                               template <int mod, int G, int maxn>
 vector<cplx> fa(sz), fb(sz);
                                                               struct NTT {
 for (int i = 0; i < (int)a.size(); ++i)</pre>
                                                                static_assert (maxn == (maxn & -maxn));
  fa[i] = cplx(a[i] & ((1 << 15) - 1), a[i] >> 15);
                                                                int roots[maxn];
 for (int i = 0; i < (int)b.size(); ++i)</pre>
                                                                NTT () {
  fb[i] = cplx(b[i] & ((1 << 15) - 1), b[i] >> 15);
                                                                 int r = modpow(G, (mod - 1) / maxn);
 fft(fa, sz), fft(fb, sz);
                                                                 for (int i = maxn >> 1; i; i >>= 1) {
 double r = 0.25 / sz;
                                                                  roots[i] = 1;
 cplx r2(0, -1), r3(r, 0), r4(0, -r), r5(0, 1);
for (int i = 0; i <= (sz >> 1); ++i) {
  int j = (sz - i) & (sz - 1);
                                                                  for (int j = 1; j < i; j++)
                                                                   roots[i + j] = modmul(roots[i + j - 1], r);
                                                                  r = modmul(r, r);
  cplx a1 = (fa[i] + fa[j].conj());
  cplx a2 = (fa[i] - fa[j].conj()) * r2;
cplx b1 = (fb[i] + fb[j].conj()) * r3;
                                                                // n must be 2^k, and 0 \le F[i] < mod
                                                                void inplace_ntt(int n, int F[], bool inv = false) {
for (int i = 0, j = 0; i < n; i++) {</pre>
  cplx b2 = (fb[i] - fb[j].conj()) * r4;
  if (i != j) {
   cplx c1 = (fa[j] + fa[i].conj());
                                                                  if (i < j) swap(F[i], F[j]);</pre>
   cplx c2 = (fa[j] - fa[i].conj()) * r2;
                                                                  for (int k = n>1; (j^*=k) < k; k>=1);
   cplx d1 = (fb[j] + fb[i].conj()) * r3;
   cplx d2 = (fb[j] - fb[i].conj()) * r4;
                                                                 for (int s = 1; s < n; s *= 2) {
   fa[i] = c1 * d1 + c2 * d2 * r5;
                                                                  for (int i = 0; i < n; i += s * 2) {
   fb[i] = c1 * d2 + c2 * d1;
                                                                   for (int j = 0; j < s; j++) {
                                                                    int a = F[i+j];
  fa[j] = a1 * b1 + a2 * b2 * r5:
                                                                    int b = modmul(F[i+j+s], roots[s+j]);
  fb[j] = a1 * b2 + a2 * b1;
                                                                    F[i+j] = modadd(a, b); // a + b
                                                                    F[i+j+s] = modsub(a, b); // a - b
 fft(fa, sz), fft(fb, sz);
 vector<int> res(sz);
 for (int i = 0; i < sz; ++i) {
  long long a = round(fa[i].re), b = round(fb[i].re),
                                                                 if (inv) {
       c = round(fa[i].im);
                                                                  int invn = modinv(n);
  res[i] = (a+((b \% p) << 15)+((c \% p) << 30)) \% p;
                                                                  for (int i = 0; i < n; i++)
                                                                   F[i] = modmul(F[i], invn);
 return res;
                                                                  reverse(F + 1, F + n);
}}
5.13 Chinese Remainder
                                                              };
lld crt(lld ans[], lld pri[], int n){
                                                               const int P=2013265921, root=31;
                                                               const int MAXN=1<<20;</pre>
 11d M = 1, ret = 0;
 for(int i=0;i<n;i++) M *= pri[i];</pre>
                                                              NTT<P, root, MAXN> ntt;
 for(int i=0;i<n;i++){</pre>
                                                               5.16 Polynomial Operations
  lld iv = (gcd(M/pri[i],pri[i]).FF+pri[i])%pri[i];
  ret += (ans[i]*(M/pri[i])%M * iv)%M;
                                                              using VL = vector<LL>;
  ret %= M;
                                                               #define fi(s, n) for (int i=int(s); i<int(n); ++i)</pre>
                                                               #define Fi(s, n) for (int i=int(n); i>int(s); --i)
 return ret;
                                                              int n2k(int n) {
                                                               int sz = 1; while (sz < n) sz <<= 1;</pre>
                                                                return sz;
Another:
x = a1 \% m1
                                                               template<int MAXN, LL P, LL RT> // MAXN = 2^k
x = a2 \% m2
                                                               struct Poly { // coefficients in [0, P)
g = gcd(m1, m2)
                                                                static NTT<MAXN, P, RT> ntt;
assert((a1-a2)%g==0)
                                                                VL coef;
[p, q] = exgcd(m2/g, m1/g)
                                                                int n() const { return coef.size(); } // n()>=1
return a2+m2*(p*(a1-a2)/g)
                                                                LL *data() { return coef.data(); }
0 <= x < lcm(m1, m2)
                                                                const LL *data() const { return coef.data(); }
                                                                LL &operator[](size_t i) { return coef[i]; }
                                                                const LL &operator[](size_t i)const{return coef[i];}
5.14
      Berlekamp Massey
                                                                Poly(initializer_list<LL> a) : coef(a) { }
                                                                explicit Poly(int _n = 1) : coef(_n) { }
// x: 1-base, p[]: 0-base
                                                                Poly(const LL *arr, int _n) : coef(arr, arr + _n) {}
Poly(const Poly &p, int _n) : coef(_n) {
template<size t N>
vector<llf> BM(llf x[N], size_t n){
 size_t f[N]={0},t=0;11f d[N];
                                                                copy_n(p.data(), min(p.n(), _n), data());
 vector<llf> p[N];
 for(size_t i=1,b=0;i<=n;++i) {</pre>
                                                                Poly& irev(){return reverse(data(),data()+n()),*this;}
```

Poly& isz(int _n) { return coef.resize(_n), *this; }

```
Poly& iadd(const Poly &rhs) { // n() == rhs.n()
                                                                const int _n = (int)x.size();
 fi(0, n()) if ((coef[i]+=rhs[i]) >= P)coef[i]-=P;
                                                                vector<Poly> up = _{tree1(x)}, down(_n * 2);
                                                                VL z = up[1].Dx().\_eval(x, up);
 return *this:
                                                                fi(0, _n) z[i] = y[i] * ntt.minv(z[i]) % P;
                                                                fi(0, n) down[n + i] = {z[i]};
Poly& imul(LL k) {
 fi(0, n()) coef[i] = coef[i] * k % P;
                                                                Fi(0, _n-1) down[i]=down[i * 2].Mul(up[i * 2 + 1])
                                                                  .iadd(down[i * 2 + 1].Mul(up[i * 2]));
 return *this;
                                                                 return down[1];
Poly Mul(const Poly &rhs) const {
                                                               Poly Ln() const { // coef[0] == 1
  return Dx().Mul(Inv()).Sx().isz(n());
 const int _n = n2k(n() + rhs.n() - 1);
 Poly X(*this, _n), Y(rhs, _n);
 ntt(X.data(), _n), ntt(Y.data(),
fi(0, _n) X[i] = X[i] * Y[i] % P;
                                                               Poly Exp() const { // coef[0] == 0
 ntt(X.data(), _n, true);
return X.isz(n() + rhs.n() - 1);
                                                                if (n() == 1) return {1};
                                                                Poly X = Poly(*this, (n() + 1)/2).Exp().isz(n());
                                                                Poly Y = X.Ln(); Y[0] = P - 1;
                                                                fi(0, n()) if((Y[i] = coef[i] - Y[i]) < 0)Y[i]+=P;
Poly Inv() const { // coef[0] != 0
 if (n() == 1) return {ntt.minv(coef[0])};
                                                                return X.Mul(Y).isz(n());
 const int _n = n2k(n() * 2);
 Poly Xi = Poly(*this, (n() + 1)/2).Inv().isz(_n);
                                                               Poly Pow(const string &K) const {
 Poly Y(*this, _n);
                                                                int nz = 0;
                                                                while (nz < n() && !coef[nz]) ++nz;</pre>
 ntt(Xi.data(), _n), ntt(Y.data(), _n);
 fi(0, _n) {
Xi[i] *= (2 - Xi[i] * Y[i]) % P;
                                                                LL nk = 0, nk2 = 0;
                                                                for (char c : K) {
  if ((Xi[i] %= P) < 0) Xi[i] += P;</pre>
                                                                 nk = (nk * 10 + c - '0') % P;
                                                                 nk2 = nk2 * 10 + c - '0';
                                                                 if (nk2 * nz >= n()) return Poly(n());
 ntt(Xi.data(), _n, true);
 return Xi.isz(n());
                                                                 nk2 %= P - 1;
Poly Sqrt() const { // Jacobi(coef[0], P) = 1
                                                                if (!nk && !nk2) return Poly({1}, n());
 if (n()==1) return {QuadraticResidue(coef[0], P)};
                                                                Poly X(data() + nz, n() - nz * nk2);
 Poly X = Poly(*this, (n()+1) / 2).Sqrt().isz(n());
                                                                LL x0 = X[0]
 return X.iadd(Mul(X.Inv()).isz(n())).imul(P/2+1);
                                                                 return X.imul(ntt.minv(x0)).Ln().imul(nk).Exp()
                                                                 .imul(ntt.mpow(x0, nk2)).irev().isz(n()).irev();
pair<Poly, Poly> DivMod(const Poly &rhs) const {
 // (rhs.)back() != 0
                                                               Poly InvMod(int L) { // (to evaluate linear recursion)
                                                                Poly R{1, 0}; // *this * R mod x^L = 1 (*this[0] ==
 if (n() < rhs.n()) return {{0}, *this};</pre>
                                                                   1)
 const int _n = n() - rhs.n() + 1;
 Poly X(rhs); X.irev().isz(_n);
                                                                for (int level = 0; (1 << level) < L; ++level) {</pre>
 Poly Y(*this); Y.irev().isz(_n);
                                                                 Poly 0 = R.Mul(Poly(data(), min(2 << level, n())));
 Poly Q = Y.Mul(X.Inv()).isz(_n).irev();
                                                                 Poly Q(2 << level); Q[0] = 1;
 X = rhs.Mul(Q), Y = *this;
fi(0, n()) if ((Y[i] -= X[i]) < 0) Y[i] += P;</pre>
                                                                 for (int j = (1 << level); j < (2 << level); ++j)
Q[j] = (P - O[j]) % P;</pre>
 return {Q, Y.isz(max(1, rhs.n() - 1))};
                                                                 R = R.Mul(Q).isz(4 << level);
Poly Dx() const {
                                                                return R.isz(L);
 Poly ret(n() - 1);
 fi(0, ret.n()) ret[i] = (i + 1) * coef[i + 1] % P;
                                                               static LL LinearRecursion(const VL&a,const VL&c,LL n){
 return ret.isz(max(1, ret.n()));
                                                                // a_n = \sum_{j=0}^{n-j} a_{j}
                                                                const int k = (int)a.size();
Poly Sx() const {
                                                                assert((int)c.size() == k + 1);
 Poly ret(n() + 1);
                                                                Poly C(k + 1), W(\{1\}, k), M = \{0, 1\};
                                                                fi(1, k + 1) C[k - i] = c[i] ? P - c[i] : 0;
 fi(0, n()) ret[i + 1]=ntt.minv(i + 1)*coef[i] % P;
 return ret;
                                                                C[k] = 1
                                                                while (n)
Poly _tmul(int nn, const Poly &rhs) const {
  Poly Y = Mul(rhs).isz(n() + nn - 1);
                                                                 if (n % 2) W = W.Mul(M).DivMod(C).second;
                                                                 n /= 2, M = M.Mul(M).DivMod(C).second;
 return Poly(Y.data() + n() - 1, nn);
                                                                LL ret = 0;
VL _eval(const VL &x, const auto up)const{
                                                                fi(0, k) ret = (ret + W[i] * a[i]) % P;
 const int _n = (int)x.size();
                                                                return ret:
 if (!_n) return {};
 vector<Poly> down(_n * 2);
 down[1] = DivMod(up[1]).second;
                                                              #undef fi
 fi(2, _n*2) down[i]=down[i/2].DivMod(up[i]).second;
                                                              #undef Fi
 /* down[1] = Poly(up[1]).irev().isz(n()).Inv().irev()
                                                              using Poly_t = Poly<131072 * 2, 998244353, 3>;
     _tmul(_n, *this)
                                                              template<> decltype(Poly_t::ntt) Poly_t::ntt = {};
 fi(2, _n * 2) down[i] = up[i ^ 1]._tmul(up[i].n() -
                                                              5.17
                                                                     FWT
   1, down[i / 2]); */
 VL y(_n);
                                                              /* xor convolution:
 fi(0, _n) y[i] = down[_n + i][0];
                                                               * x = (x0, x1) , y = (y0, y1)
 return y;
                                                               *z = (x0y0 + x1y1 , x0y1 + x1y0 )
                                                               * x' = (x0+x1, x0-x1), y' = (y0+y1, y0-y1)
* z' = ((x0+x1)(y0+y1), (x0-x1)(y0-y1)
* z = (1/2) * z''
static vector<Poly> _tree1(const VL &x) {
 const int _n = (int)x.size();
 vector<Poly> up(_n * 2);
 fi(0, _n) up[_n + i] = \{(x[i] ? P - x[i] : 0), 1\};

Fi(0, _n-1) up[i] = up[i * 2].Mul(up[i * 2 + 1]);
                                                               * or convolution:
                                                               * x = (x0, x0+x1), inv = (x0, x1-x0) w/o final div
                                                               * and convolution:
                                                               * x = (x0+x1, x1), inv = (x0-x1, x1) w/o final div */
VL Eval(const VL&x)const{return _eval(x,_tree1(x));}
                                                              const LL MOD = 1e9+7;
static Poly Interpolate(const VL &x, const VL &y) {
                                                              inline void fwt( LL x[ MAXN ] , int N , bool inv=0 ) {
```

```
for( int d = 1 ; d < N ; d <<= 1 ) {</pre>
                                                                    S(int m, int w_=-1, int64_t x_=1, int64_t y_=0)
  int d2 = d << 1;
                                                                     : MOD(m), w(w_{-}), x(x_{-}), y(y_{-}) {}
                                                                    S operator*(const S &rhs) const {
  for( int s = 0; s < N; s += d2)
   for( int i = s , j = s+d ; i < s+d ; i++, j++ ){
  LL ta = x[ i ] , tb = x[ j ];</pre>
                                                                     int w_{-} = w;
                                                                     if (w_{-} = -1) w_{-} = rhs.w;
                                                                     assert(w_ != -1 and w_ == rhs.w);
    x[i] = ta+tb;
                                                                     return { MOD, w_,
(x * rhs.x + y * rhs.y % MOD * w) % MOD,
    x[ j ] = ta-tb;
if( x[ i ] >= MOD ) x[ i ] -= MOD;
                                                                       (x * rhs.y + y * rhs.x) % MOD };
    if( x[ j ] < 0 ) x[ j ] += MOD;</pre>
 if( inv )
                                                                   int64_t get_root(int64_t n, int P) {
  for( int i = 0 ; i < N ; i++ ) {
    x[ i ] *= inv( N, MOD );
                                                                    if (P == 2) return 1
                                                                    auto check = [\&](int64_t x) {
                                                                    return qpow(x, (P - 1) / 2, P); };
if (check(n) == P-1) return -1;
   x[ i ] %= MOD;
                                                                    int64_t a; int w; mt19937 rnd(7122);
                                                                    do { a = rnd() % P;
5.18
                                                                     w = ((a * a - n) % P + P) % P;
       DiscreteLog
                                                                    } while (check(w) != P-1);
11d BSGS(11d P, 11d B, 11d N) {
                                                                    return qpow(S(P, w, a, 1), (P + 1) / 2).x;
 // find B^L = N mod P
 unordered_map<lld, int> R;
 11d sq = (11d)sqrt(P);
                                                                   5.21 De-Bruijn
 11d t = 1;
                                                                   int res[maxn], aux[maxn], sz;
 for (int i = 0; i < sq; i++) {
  if (t == N) return i;
                                                                   void db(int t, int p, int n, int k) {
                                                                    if (t > n) {
  if (!R.count(t)) R[t] = i;
  t = (t * B) % P;
                                                                     if (n % p == 0)
                                                                      for (int i = 1; i <= p; ++i)
 11d f = inverse(t, P);
                                                                       res[sz++] = aux[i];
                                                                    } else {
 for(int i=0;i<=sq+1;i++) {</pre>
                                                                     aux[t] = aux[t - p];
 if (R.count(N))
                                                                     db(t + 1, p, n, k);
   return i * sq + R[N];
  N = (N * f) % P;
                                                                     for (int i = aux[t - p] + 1; i < k; ++i) {
                                                                      aux[t] = i;
                                                                      db(t + 1, t, n, k);
 return -1;
                                                                     }
5.19 FloorSum
                                                                   int de_bruijn(int k, int n) {
// @param n `n < 2^32`
// @param m `1 <= m < 2^32`
                                                                    // return cyclic string of len k^n s.t. every string
                                                                    // of len n using k char appears as a substring.
// @return sum_{i=0}^{n-1} floor((ai + b)/m) mod 2^64
                                                                    if (k == 1) {
1lu floor_sum_unsigned(llu n, llu m, llu a, llu b) {
                                                                     res[0] = 0;
llu ans = 0;
                                                                     return 1;
 while (true)
  if (a >= m) {
                                                                    for (int i = 0; i < k * n; i++) aux[i] = 0;
   ans += n * (n - 1) / 2 * (a / m); a %= m;
                                                                    sz = 0;
                                                                    db(1, 1, n, k);
  if (b >= m) {
                                                                    return sz;
   ans += n * (b / m); b %= m;
  llu y_max = a * n + b;
                                                                          Simplex Construction
                                                                   5.22
  if (y_max < m) break;</pre>
                                                                   Standard form: maximize \sum_{1 < i < n} c_i x_i such that for all 1 \le j \le m,
  // y_max < m * (n + 1)
                                                                   \sum_{1 \leq i \leq n} A_{ji} x_i \leq b_j. \text{and } x_i \geq 0 \text{ for all } 1 \leq i \leq n.
  // floor(y_max / m) <= n
  n = (1lu)(y_max / m), b = (1lu)(y_max % m);
                                                                     1. In case of minimization, let c_i^\prime = -c_i
  swap(m, a);
                                                                     2. \sum_{1 \leq i \leq n} A_{ji} x_i \geq b_j \rightarrow \sum_{1 \leq i \leq n} -A_{ji} x_i \leq -b_j
 return ans;
                                                                     3. \sum_{1 < i < n} A_{ji} x_i = b_j
11d floor_sum(11d n, 11d m, 11d a, 11d b) {
 assert(0 <= n && n < (1LL << 32));
                                                                           • \sum_{1 \leq i \leq n} A_{ji} x_i \leq b_j
 assert(1 <= m && m < (1LL << 32));
                                                                           • \sum_{1 \le i \le n} A_{ji} x_i \ge b_j
 llu\ ans = 0;
 if (a < 0) {
                                                                     4. If x_i has no lower bound, replace x_i with x_i - x_i'
 llu a2 = (a % m + m) % m;
  ans -= 1ULL * n * (n - 1) / 2 * ((a2 - a) / m);
                                                                   5.23 Simplex
  a = a2;
                                                                   namespace simplex {
 if (b < 0) {
                                                                   // maximize c^Tx under Ax <= B
  11u b2 = (b \% m + m) \% m;
                                                                   // return VD(n, -inf) if the solution doesn't exist
  ans -= 1ULL * n * ((b2 - b) / m);
                                                                   // return VD(n, +inf) if the solution is unbounded
  b = b2;
                                                                   using VD = vector<double>;
                                                                   using VVD = vector<vector<double>>;
 return ans + floor_sum_unsigned(n, m, a, b);
                                                                   const double eps = 1e-9;
                                                                   const double inf = 1e+9;
                                                                   int n, m;
5.20 Quadratic residue
                                                                   VVD d;
struct S {
                                                                   vector<int> p, q;
 int MOD, w;
                                                                   void pivot(int r, int s) {
int64_t x, y;
                                                                   double inv = 1.0 / d[r][s];
```

int argCmp(Point a, Point b) {
 // -1 / 0 / 1 <-> < / == / > (atan2)

int qa = (imag(a) == 0

```
for (int i = 0; i < m + 2; ++i)
                                                                  ? (real(a) < 0 ? 3 : 1) : (imag(a) < 0 ? 0 : 2));
  for (int j = 0; j < n + 2; ++j)
                                                               int qb = (imag(b) == 0
   if (i != r && j != s)
                                                                 ? (real(b) < 0 ? 3 : 1) : (imag(b) < 0 ? 0 : 2));
    d[i][j] -= d[r][j] * d[i][s] * inv;
                                                               if (qa != qb)
 for(int i=0;i<m+2;++i) if (i != r) d[i][s] *= -inv;
for(int j=0;j<n+2;++j) if (j != s) d[r][j] *= +inv;</pre>
                                                                return sgn(qa - qb);
                                                               return sgn(cross(b, a));
 d[r][s] = inv; swap(p[r], q[s]);
                                                              template <typename V> Real area(const V & pt) {
                                                               coord_t ret = 0;
bool phase(int z) {
                                                               for (int i = 1; i + 1 < (int)pt.size(); i++)</pre>
 int x = m + z
                                                                ret += cross(pt[i] - pt[0], pt[i+1] - pt[0]);
 while (true) {
  int s = -1;
                                                               return ret / 2.0;
  for (int i = 0; i <= n; ++i) {
  if (!z && q[i] == -1) continue;</pre>
                                                              6.2 Circle Class
   if (s == -1 \mid | d[x][i] < d[x][s]) s = i;
                                                              struct Circle { Point o; Real r; };
  if (d[x][s] > -eps) return true;
  int r = -1;
                                                              vector<Real> intersectAngle(Circle a, Circle b) {
  for (int i = 0; i < m; ++i) {</pre>
                                                               Real d2 = norm(a.o - b.o)
   if (d[i][s] < eps) continue;</pre>
                                                               if (norm(A.r - B.r) >= d2)
   if (r == -1 ||
                                                                if (A.r < B.r)
    d[i][n+1]/d[i][s] < d[r][n+1]/d[r][s]) r = i;
                                                                 return {-PI, PI};
                                                                else
  if (r == -1) return false;
                                                                 return {};
  pivot(r, s);
                                                               if (norm(A.r + B.r) <= d2) return {};</pre>
                                                               Real dis = hypot(A.x - B.x, A.y - B.y);
                                                               Real theta = atan2(B.y - A.y, B.x - A.x);
Real phi = acos((A.r * A.r + d2 - B.r * B.r) /
VD solve(const VVD &a, const VD &b, const VD &c) {
m = b.size(), n = c.size();
                                                                 (2 * A.r * dis));
 d = VVD(m + 2, VD(n + 2))
                                                               Real L = theta - phi, R = theta + phi;
 for (int i = 0; i < m; ++i)
                                                               while (L < -PI) L += PI * 2;
 for (int j = 0; j < n; ++j) d[i][j] = a[i][j];
                                                               while (R > PI) R -= PI * 2;
 p.resize(m), q.resize(n + 1);
                                                               return { L, R };
 for (int i = 0; i < m; ++i)
 p[i] = n + i, d[i][n] = -1, d[i][n + 1] = b[i];
 for (int i = 0; i < n; ++i) q[i] = i,d[m][i] = -c[i];
                                                              vector<Point> intersectPoint(Circle a, Circle b) {
 q[n] = -1, d[m + 1][n] = 1;
                                                               Real d=o.dis(aa.o);
 int r = 0;
                                                               if (d >= r+aa.r || d <= fabs(r-aa.r)) return {};</pre>
 for (int i = 1; i < m; ++i)</pre>
                                                               Real dt = (r*r - aa.r*aa.r)/d, d1 = (d+dt)/2;
  if (d[i][n + 1] < d[r][n + 1]) r = i;
                                                               Point dir = (aa.o-o); dir /= d;
 if (d[r][n + 1] < -eps) {</pre>
                                                               Point pcrs = dir*d1 + o;
 pivot(r, n);
                                                               dt=sqrt(max(0.0L, r*r - d1*d1)), dir=dir.rot90();
  if (!phase(1) || d[m + 1][n + 1] < -eps)</pre>
                                                               return {pcrs + dir*dt, pcrs - dir*dt};
   return VD(n, -inf);
  for (int i = 0; i < m; ++i) if (p[i] == -1)
  int s = min_element(d[i].begin(), d[i].end() - 1)
                                                              6.3 2D Convex Hull
        - d[i].begin();
                                                              template<typename PT>
   pivot(i, s);
                                                              vector<PT> buildConvexHull(vector<PT> d) {
  }
                                                               sort(ALL(d), [](const PT& a, const PT& b){
                                                                 return tie(a.x, a.y) < tie(b.x, b.y);});</pre>
 if (!phase(0)) return VD(n, inf);
                                                               vector<PT> s(SZ(d)<<1);</pre>
 VD x(n);
                                                               int o = 0;
 for (int i = 0; i < m; ++i)
                                                               for(auto p: d) {
 if (p[i] < n) x[p[i]] = d[i][n + 1];
                                                                while(o \ge 2 \& cross(p-s[o-2], s[o-1]-s[o-2]) <= 0)
 return x;
                                                                 0--
}}
                                                                s[o++] = p;
6
    Geometry
                                                               for(int i=SZ(d)-2, t = o+1; i>=0; i--){
                                                                while(o = t\&cross(d[i] - s[o-2], s[o-1] - s[o-2]) <= 0)
6.1
    Basic Geometry
using coord_t = int;
                                                                s[o++] = d[i];
using Real = double;
using Point = std::complex<coord_t>;
                                                               s.resize(o-1):
int sgn(coord_t x) {
                                                               return s;
return (x > 0) - (x < 0);
coord_t dot(Point a, Point b) {
                                                              6.4 3D Convex Hull
return real(conj(a) * b);
                                                              // return the faces with pt indexes
coord_t cross(Point a, Point b) {
                                                              int flag[MXN][MXN];
return imag(conj(a) * b);
                                                              struct Point{
                                                               ld x,y,z;
int ori(Point a, Point b, Point c) {
                                                               Point operator * (const ld &b) const {
return sgn(cross(b - a, c - a));
                                                                return (Point) {x*b,y*b,z*b};}
                                                               Point operator * (const Point &b) const {
bool operator<(const Point &a, const Point &b) {</pre>
                                                                return(Point) {y*b.z-b.y*z,z*b.x-b.z*x,x*b.y-b.x*y};
return real(a) != real(b)
                                                               }
  ? real(a) < real(b) : imag(a) < imag(b);</pre>
```

Point ver(Point a, Point b, Point c) {
 return (b - a) * (c - a);}

int n = SZ(pt), ftop = 0;

vector<Face> convex_hull_3D(const vector<Point> pt) {

}; rebuild_m(2);

```
REP(i,n) REP(j,n) flag[i][j] = 0;
                                                                  for (size_t i = 2; i < v.size(); ++i) {</pre>
                                                                  const 11d kx = Idx(v[i].x), ky = Idx(v[i].y),
 vector<Face> now;
 now.emplace_back(0,1,2);
                                                                      kz = Idx(v[i].z); bool found = false;
 now.emplace_back(2,1,0);
for (int i=3; i<n; i++){
                                                                   for (int dx = -2; dx <= 2; ++dx) {
                                                                    const 11d nx = dx + kx;
  ftop++; vector<Face> next;
REP(j, SZ(now)) {
  Face& f=now[j]; int ff = 0;
                                                                    if (m.find(nx) == m.end()) continue;
                                                                    auto& mm = m[nx];
                                                                    for (int dy = -2; dy <= 2; ++dy) {
   ld d=(pt[i]-pt[f.a]).dot(
                                                                     const 11d ny = dy + ky;
                                                                     if (mm.find(ny) == mm.end()) continue;
     ver(pt[f.a], pt[f.b], pt[f.c]));
   if (d <= 0) next.push_back(f);</pre>
                                                                     auto& mmm = mm[ny];
   if (d > 0) ff=ftop;
                                                                     for (int dz = -2; dz <= 2; ++dz) {
   else if (d < 0) ff=-ftop
                                                                      const 11d nz = dz + kz;
   flag[f.a][f.b]=flag[f.b][f.c]=flag[f.c][f.a]=ff;
                                                                      if (mmm.find(nz) == mmm.end()) continue;
                                                                      const int p = mmm[nz];
  REP(j, SZ(now)) {
  Face& f=now[j];
                                                                      if (dis(v[p], v[i]) < d) {</pre>
                                                                       d = dis(v[p], v[i]);
   if (flag[f.a][f.b] > 0 &&
                                                                       found = true;
     flag[f.a][f.b] != flag[f.b][f.a])
                                                                      }
    next.emplace_back(f.a,f.b,i);
   if (flag[f.b][f.c] > 0 &&
     flag[f.b][f.c] != flag[f.c][f.b])
    next.emplace_back(f.b,f.c,i);
                                                                   if (found) rebuild_m(i + 1);
   if (flag[f.c][f.a] > 0 &&
                                                                  else m[kx][ky][kz] = i;
     flag[f.c][f.a] != flag[f.a][f.c])
    next.emplace_back(f.c,f.a,i);
                                                                  return d;
                                                                }
  now=next;
                                                                       Simulated Annealing
 return now;
                                                                11f anneal() {
                                                                 mt19937 rnd_engine( seed );
                                                                  uniform_real_distribution< llf > rnd( 0, 1 );
6.5 2D Farthest Pair
                                                                  const 11f dT = 0.001;
                                                                  // Argument p
// stk is from convex hull
                                                                  11f S_cur = calc( p ), S_best = S_cur;
n = (int)(stk.size());
                                                                  for ( 11f T = 2000 ; T > EPS ; T -= dT ) {
int pos = 1, ans = 0; stk.push_back(stk[0]);
                                                                   // Modify p to p_prime
for(int i=0;i<n;i++) {
  while(abs(cross(stk[i+1]-stk[i],</pre>
                                                                   const llf S_prime = calc( p_prime );
                                                                  const llf delta_c = S_prime - S_cur;
llf prob = min( ( llf ) 1, exp( -delta_c / T ) );
   stk[(pos+1)%n]-stk[i])) >
   abs(cross(stk[i+1]-stk[i],
                                                                   if ( rnd( rnd_engine ) <= prob )</pre>
stk[pos]-stk[i]))) pos = (pos+1)%n;
ans = max({ans, dis(stk[i], stk[pos]),
                                                                  S_cur = S_prime, p = p_prime;
if ( S_prime < S_best ) // find min</pre>
  dis(stk[i+1], stk[pos])});
                                                                    S_best = S_prime, p_best = p_prime;
6.6 2D Closest Pair
                                                                  return S_best;
struct cmp_y {
 bool operator()(const P& p, const P& q) const {
                                                                6.9 Half Plane Intersection
  return p.y < q.y;</pre>
                                                                // NOTE: Point is complex<Real>
                                                                // cross(pt-line.st, line.dir)<=0 <-> pt in half plane
                                                                struct Line {
multiset<P, cmp_y> s;
void solve(P a[], int n) {
                                                                  Point st, ed;
                                                                   Point dir;
 sort(a, a + n, [](const P& p, const P& q) {
                                                                  Line (Point _s, Point _e)
  return tie(p.x, p.y) < tie(q.x, q.y);</pre>
                                                                    : st(_s), ed(_e), dir(_e - _s) {}
                                                                };
 llf d = INF; int pt = 0;
 for (int i = 0; i < n; ++i) {
                                                                bool operator<(const Line &lhs, const Line &rhs) {</pre>
  while (pt < i \text{ and } a[i].x - a[pt].x >= d)
                                                                  if (int cmp = argCmp(lhs.dir, rhs.dir))
  s.erase(s.find(a[pt++]));
                                                                     return cmp == -1;
  auto it = s.lower_bound(P(a[i].x, a[i].y - d));
                                                                   return ori(lhs.st, lhs.ed, rhs.st) < 0;</pre>
  while (it != s.end() and it->y - a[i].y < d)</pre>
   d = min(d, dis(*(it++), a[i]));
                                                                Point intersect(const Line &A, const Line &B) {
  s.insert(a[i]);
                                                                  Real t = cross(B.st - A.st, B.dir) /
                                                                   cross(A.dir, B.dir);
                                                                   return A.st + t * A.dir;
     kD Closest Pair (3D ver.)
11f solve(vector<P> v) {
                                                                Real HPI(vector<Line> &lines) {
 shuffle(v.begin(), v.end(), mt19937());
unordered_map<lld, unordered_map<lld,</pre>
                                                                  sort(lines.begin(), lines.end());
                                                                   deque<Line> que;
                                                                   deque<Point> pt;
  unordered_map<lld, int>>> m;
                                                                   que.push_back(lines[0]);
 llf d = dis(v[0], v[1]);
                                                                   for (int i = 1; i < (int)lines.size(); i++) {</pre>
 auto Idx = [&d] (11f x) -> 11d {
  return round(x * 2 / d) + 0.1; };
                                                                     if (argCmp(lines[i].dir, lines[i-1].dir) == 0)
 auto rebuild_m = [&m, &v, &Idx](int k) {
                                                                      continue;
                                                                #define POP(L, R) \
  m.clear();
  for (int i = 0; i < k; ++i)
                                                                     while (pt.size() > 0 \
   m[Idx(v[i].x)][Idx(v[i].y)]
                                                                       && ori(L.st, L.ed, pt.back()) < 0) \
    [Idx(v[i].z)] = i;
                                                                       pt.pop_back(), que.pop_back(); \
                                                                     while (pt.size() > 0 \
```

d = sqrt(d2);

 $if(d < max(r1, r2) - min(r1, r2) \mid \mid d > r1 + r2)$

```
&& ori(R.st, R.ed, pt.front()) < 0) \
                                                               return 0;
      pt.pop_front(), que.pop_front();
                                                              pdd u = (o1 + o2) * 0.5
                                                               + (o1 - o2) * ((r2 * r2 - r1 * r1) / (2 * d2));
    POP(lines[i], lines[i]);
   pt.push_back(intersect(que.back(), lines[i]));
                                                              double A = sqrt((r1 + r2 + d) * (r1 - r2 + d)
                                                                  * (r1 + r2 - d) * (-r1 + r2 + d));
    que.push_back(lines[i]);
                                                              pdd v = pdd(o1.Y - o2.Y, -o1.X + o2.X) * A
                                                               / (2 * d2);
 POP(que.front(), que.back())
 if (que.size() <= 1 ||</pre>
                                                              p1 = u + v, p2 = u - v;
    argCmp(que.front().dir, que.back().dir) == 0)
                                                              return 1;
    return 0;
 pt.push_back(intersect(que.front(), que.back()));
                                                             6.14 tangent line of two circle
  return area(pt);
                                                             vector<Line> go(const Cir& c1,
                                                               const Cir& c2, int sign1){
6.10 Minkowski sum
                                                              // sign1 = 1 for outer tang, -1 for inter tang
vector<pll> Minkowski(vector<pll> A, vector<pll> B) {
                                                              vector<Line> ret;
hull(A), hull(B);
                                                              double d_sq = norm2( c1.0 - c2.0 );
vector<pll> C(1, A[0] + B[0]), s1, s2;
for(int i = 0; i < SZ(A); ++i)</pre>
                                                              if( d_sq < eps ) return ret;
double d = sqrt( d_sq );</pre>
 s1.pb(A[(i + 1) % SZ(A)] - A[i]);
                                                              Pt v = (c2.0 - c1.0) / d;
for(int i = 0; i < SZ(B); i++)
s2.pb(B[(i + 1) % SZ(B)] - B[i]);
                                                              double c = (c1.R - sign1 * c2.R) / d;
                                                              if( c * c > 1 ) return ret;
for(int p1 = 0, p2 = 0; p1 < SZ(A) || p2 < SZ(B);)
                                                              double h = sqrt( max( 0.0 , 1.0 - c * c ) );
 if (p2 >= SZ(B)
                                                              for( int sign2 = 1 ; sign2 >= -1 ; sign2 -= 2 ){
    | | (p1 < SZ(A) \& cross(s1[p1], s2[p2]) >= 0))
                                                               Pt n = \{ v.X * c - sign2 * h * v.Y ,
                                                                v.Y * c + sign2 * h * v.X };
  C.pb(C.back() + s1[p1++]);
 else
                                                               Pt p1 = c1.0 + n * c1.R;
  C.pb(C.back() + s2[p2++]);
                                                               Pt p2 = c2.0 + n * (c2.R * sign1);
return hull(C), C;
                                                               if( fabs( p1.X - p2.X ) < eps and
                                                                 fabs( p1.Y - p2.Y ) < eps )
                                                                p2 = p1 + perp(c2.0 - c1.0);
6.11 intersection of line and circle
                                                               ret.push_back( { p1 , p2 } );
vector<pdd> line_interCircle(const pdd &p1,
                                                              return ret;
    const pdd &p2,const pdd &c,const double r){
pdd ft=foot(p1,p2,c),vec=p2-p1;
double dis=abs(c-ft);
                                                             6.15 Minimum Covering Circle
if(fabs(dis-r)<eps) return vector<pdd>{ft};
if(dis>r) return {};
                                                             template<typename P>
vec=vec*sqrt(r*r-dis*dis)/abs(vec);
                                                             Circle getCircum(const P &a, const P &b, const P &c){
return vector<pdd>{ft+vec,ft-vec};
                                                              Real a1 = a.x-b.x, b1 = a.y-b.y;
                                                              Real c1 = (a.x+b.x)/2 * a1 + (a.y+b.y)/2 * b1;
                                                              Real a2 = a.x-c.x, b2 = a.y-c.y;
     intersection of polygon and circle
                                                              Real c2 = (a.x+c.x)/2 * a2 + (a.y+c.y)/2 * b2;
                                                              Circle cc;
// Divides into multiple triangle, and sum up
// test by HDU2892
                                                              cc.o.x = (c1*b2-b1*c2)/(a1*b2-b1*a2);
const double PI=acos(-1);
                                                              cc.o.y = (a1*c2-c1*a2)/(a1*b2-b1*a2)
                                                              cc.r = hypot(cc.o.x-a.x, cc.o.y-a.y);
double _area(pdd pa, pdd pb, double r){
if(abs(pa)<abs(pb)) swap(pa, pb);</pre>
                                                              return cc;
if(abs(pb)<eps) return 0;</pre>
double S, h, theta;
                                                             template<typename P>
double a=abs(pb), b=abs(pa), c=abs(pb-pa);
                                                             Circle MinCircleCover(const vector<P>& pts){
double cosB = dot(pb,pb-pa) / a / c, B = acos(cosB);
                                                              random_shuffle(pts.begin(), pts.end());
double cosC = dot(pa,pb) / a / b, C = acos(cosC);
                                                              Circle c = { pts[0], 0 };
if(a > r){
                                                              for(int i=0;i<(int)pts.size();i++){</pre>
 S = (C/2)*r*r
                                                               if (dist(pts[i], c.o) <= c.r) continue;</pre>
 h = a*b*sin(C)/c;
 if (h < r && B < PI/2)
                                                               c = { pts[i], 0 };
                                                               for (int j = 0; j < i; j++) {
  if(dist(pts[j], c.o) <= c.r) continue;</pre>
  S = (acos(h/r)*r*r - h*sqrt(r*r-h*h));
                                                                c.o = (pts[i] + pts[i]) / 2;
else if(b > r){
                                                                c.r = dist(pts[i], c.o);
 theta = PI - B - asin(sin(B)/r*a);
 S = .5*a*r*sin(theta) + (C-theta)/2*r*r;
                                                                for (int k = 0; k < j; k++) {
                                                                 if (dist(pts[k], c.o) <= c.r) continue;</pre>
                                                                 c = getCircum(pts[i], pts[j], pts[k]);
else S = .5*sin(C)*a*b;
return S;
double area_poly_circle(const vector<pdd> poly,
                                                              return c;
 const pdd &0,const double r){
 double S=0;
for(int i=0;i<SZ(poly);++i)</pre>
                                                                   KDTree (Nearest Point)
                                                             6.16
 S+=_area(poly[i]-0,poly[(i+1)%SZ(poly)]-0,r)
    *ori(0,poly[i],poly[(i+1)%SZ(poly)]);
                                                             const int MXN = 100005;
return fabs(S);
                                                             struct KDTree {
                                                              struct Node {
                                                               int x,y,x1,y1,x2,y2;
     intersection of two circle
                                                               int id,f;
Node *L, *R;
bool CCinter(Cir &a, Cir &b, pdd &p1, pdd &p2) {
pdd o1 = a.0, o2 = b.0;
                                                              } tree[MXN], *root;
double r1 = a.R, r2 = b.R, d2 = abs2(o1 - o2),
                                                              int n;
```

LL dis2(int x1, int y1, int x2, int y2) {

LL dx = x1-x2, dy = y1-y2;

mutable{y=x;x=mul(x,P);return y;});

```
return dx*dx+dy*dy;
                                                                  int query(int 1, int r){ // 1-base (1, r]
                                                                   return sub(h[r], mul(h[1], p[r-1]));}
 static bool cmpx(Node& a, Node& b){return a.x<b.x;}</pre>
                                                               };
 static bool cmpy(Node& a, Node& b){return a.y<b.y;}</pre>
                                                                7.2 Suffix Array
 void init(vector<pair<int,int>> ip) {
  n = ip.size();
                                                                namespace sfxarray {
  for (int i=0; i<n; i++) {</pre>
                                                                bool t[maxn * 2];
int hi[maxn], rev[maxn];
   tree[i].id = i;
                                                                int _s[maxn * 2], sa[maxn * 2], c[maxn * 2];
   tree[i].x = ip[i].first;
   tree[i].y = ip[i].second;
                                                                int x[maxn], p[maxn], q[maxn * 2];
                                                                // sa[i]: sa[i]-th suffix is the \
                                                                // i-th lexigraphically smallest suffix.
  root = build_tree(0, n-1, 0);
                                                                // hi[i]: longest common prefix \
 Node* build_tree(int L, int R, int d) {
                                                                // of suffix sa[i] and suffix sa[i - 1].
                                                                void pre(int *sa, int *c, int n, int z) {
  if (L>R) return nullptr;
  int M = (L+R)/2; tree[M].f = d%2;
                                                                 memset(sa, 0, sizeof(int) * n);
  nth_element(tree+L,tree+M,tree+R+1,d%2?cmpy:cmpx);
                                                                 memcpy(x, c, sizeof(int) * z);
  tree[M].x1 = tree[M].x2 = tree[M].x;
  tree[M].y1 = tree[M].y2 = tree[M].y;
                                                                void induce(int *sa,int *c,int *s,bool *t,int n,int z){
  tree[M].L = build_tree(L, M-1, d+1);
                                                                 memcpy(x + 1, c, sizeof(int) * (z - 1));
  if (tree[M].L) {
                                                                 for (int i = 0; i < n; ++i)</pre>
   tree[M].x1 = min(tree[M].x1, tree[M].L->x1);
                                                                  if (sa[i] && !t[sa[i] - 1])
   tree[M].x2 = max(tree[M].x2, tree[M].L->x2);
tree[M].y1 = min(tree[M].y1, tree[M].L->y1);
                                                                   sa[x[s[sa[i] - 1]]++] = sa[i] - 1;
                                                                 memcpy(x, c, sizeof(int) * z);
   tree[M].y2 = max(tree[M].y2, tree[M].L->y2);
                                                                 for (int i = n - 1; i >= 0; --i)
                                                                  if (sa[i] && t[sa[i] - 1])
  tree[M].R = build_tree(M+1, R, d+1);
                                                                   sa[--x[s[sa[i] - 1]]] = sa[i] - 1;
  if (tree[M].R) {
   tree[M].x1 = min(tree[M].x1, tree[M].R->x1);
tree[M].x2 = max(tree[M].x2, tree[M].R->x2);
                                                                void sais(int *s, int *sa, int *p, int *q,
bool *t, int *c, int n, int z) {
                                                                 bool uniq = t[n - 1] = true;
   tree[M].y1 = min(tree[M].y1, tree[M].R->y1);
                                                                 int nn=0, nmxz=-1, *nsa = sa+n, *ns=s+n, last=-1;
   tree[M].y2 = max(tree[M].y2, tree[M].R->y2);
                                                                 memset(c, 0, sizeof(int) * z);
  return tree+M;
                                                                 for (int i = 0; i < n; ++i) uniq &= ++c[s[i]] < 2;
                                                                 for (int i = 0; i < z - 1; ++i) c[i + 1] += c[i];
 int touch(Node* r, int x, int y, LL d2){
                                                                 if (uniq) {
  LL dis = sqrt(d2)+1;
                                                                  for (int i = 0; i < n; ++i) sa[--c[s[i]]] = i;
  if (x<r->x1-dis || x>r->x2+dis ||
                                                                  return;
    y<r->y1-dis || y>r->y2+dis)
                                                                 for (int i = n - 2; i >= 0; --i)
   return 0:
  return 1;
                                                                  t[i] = (s[i] = s[i + 1] ? t[i + 1] : s[i] < s[i + 1]);
                                                                 pre(sa, c, n, z);
for (int i = 1; i <= n - 1; ++i)
 void nearest(Node* r,int x,int y,int &mID,LL &md2) {
  if (!r || !touch(r, x, y, md2)) return;
                                                                  if (t[i] && !t[i - 1])
  LL d2 = dis2(r->x, r->y, x, y);
                                                                   sa[--x[s[i]]] = p[q[i] = nn++] = i;
  if (d2 < md2 \mid | (d2 == md2 && mID < r->id)) {
                                                                 induce(sa, c, s, t, n, z);
for (int i = 0; i < n; ++i)
   mID = r -> id;
   md2 = d2:
                                                                  if (sa[i] && t[sa[i]] && !t[sa[i] - 1]) {
                                                                  bool neq = last < 0 ||</pre>
  // search order depends on split dim
                                                                   memcmp(s + sa[i], s + last,
  if ((r->f == 0 \&\& x < r->x) ||
                                                                    (p[q[sa[i]] + 1] - sa[i]) * sizeof(int));
                                                                  ns[q[last = sa[i]]] = nmxz += neq;
    (r->f == 1 \&\& y < r->y)) {
   nearest(r->L, x, y, mID, md2);
   nearest(r->R, x, y, mID, md2);
                                                                 sais(ns, nsa, p+nn, q+n, t+n, c+z, nn, nmxz+1);
                                                                 pre(sa, c, n, z);
for (int i = nn - 1; i >= 0; --i)
  } else {
   nearest(r->R, x, y, mID, md2);
   nearest(r->L, x, y, mID, md2);
                                                                  sa[--x[s[p[nsa[i]]]]] = p[nsa[i]];
  }
                                                                 induce(sa, c, s, t, n, z);
 }
 int query(int x, int y) {
                                                                void build(const string &s) {
  int id = 1029384756;
                                                                 for (int i = 0; i < (int)s.size(); ++i) _s[i] = s[i];
  LL d2 = 102938475612345678LL;
                                                                 _s[(int)s.size()] = 0; // s shouldn't contain 0
                                                                 sais(_s, sa, p, q, t, c, (int)s.size() + 1, 256);
for(int i = 0; i < (int)s.size(); ++i) sa[i]=sa[i+1];</pre>
  nearest(root, x, y, id, d2);
  return id;
                                                                 for(int i = 0; i < (int)s.size(); ++i) rev[sa[i]]=i;</pre>
                                                                 int ind = 0; hi[0] = 0;
for (int i = 0; i < (int)s.size(); ++i) {
   if (!rev[i]) {</pre>
} tree;
     Stringology
                                                                   ind = 0:
7.1 Hash
                                                                   continue;
class Hash {
                                                                  while (i + ind < (int)s.size() && \</pre>
 private:
  static constexpr int P = 127, Q = 1051762951;
                                                                   s[i + ind] == s[sa[rev[i] - 1] + ind]) ++ind;
  vector<int> h, p;
                                                                  hi[rev[i]] = ind ? ind-- : 0;
                                                                }}
  void init(const string &s){
   h.assign(s.size()+1, 0); p.resize(s.size()+1);
                                                                7.3 Suffix Automaton
   for (size_t i = 0; i < s.size(); ++i)</pre>
    h[i + 1] = add(mul(h[i], P), s[i]);
                                                                struct Node{
                                                                 Node *green, *edge[26];
   generate(p.begin(), p.end(),[x=1,y=1,this]()
```

int max_len;

Node(const int _max_len)

```
: green(NULL), max_len(_max_len){
                                                              char s[MAXN];
                                                              int len,z[MAXN];
  memset(edge, 0, sizeof(edge));
                                                              void Z_value() {
} *ROOT, *LAST;
                                                                int i,j,left,right;
void Extend(const int c) {
                                                                z[left=right=0]=len;
Node *cursor = LAST;
                                                                for(i=1;i<len;i++) </pre>
LAST = new Node((LAST->max_len) + 1);
                                                                 j=max(min(z[i-left], right-i),0);
for(;cursor&&!cursor->edge[c]; cursor=cursor->green)
                                                                 for(;i+j<len&&s[i+j]==s[j];j++);
 cursor->edge[c] = LAST;
                                                                 if(i+(z[i]=j)>right)right=i+z[left=i];
 if (!cursor)
                                                              }
 LAST->green = ROOT;
                                                               7.6
                                                                    Manacher
 Node *potential_green = cursor->edge[c];
  if((potential_green->max_len)==(cursor->max_len+1))
                                                              int z[maxn];
   LAST->green = potential_green;
                                                              int manacher(const string& s) {
  string t = ".";
//assert(potential_green->max_len>(cursor->max_len+1));
                                                                for(char c: s) t += c, t += '.';
   Node *wish = new Node((cursor->max_len) + 1);
                                                                int 1 = 0, r = 0, ans = 0;
   for(;cursor && cursor->edge[c]==potential_green;
                                                                for (int i = 1; i < t.length(); ++i) {
  z[i] = (r > i ? min(z[2 * 1 - i], r - i) : 1);
      cursor = cursor->green)
    cursor->edge[c] = wish;
                                                                 while (i - z[i] >= 0 \&\& i + z[i] < t.length()) {
   for (int i = 0; i < 26; i++)
                                                                  if(t[i - z[i]] == t[i + z[i]]) ++z[i];
   wish->edge[i] = potential_green->edge[i];
                                                                  else break;
   wish->green = potential_green->green;
   potential_green->green = wish;
                                                                 if (i + z[i] > r) r = i + z[i], l = i;
   LAST->green = wish;
                                                                for(int i=1;i<t.length();++i) ans = max(ans, z[i]-1);
                                                                return ans;
char S[10000001], A[10000001];
int N;
                                                               7.7 Lexico Smallest Rotation
int main(){
                                                              string mcp(string s){
scanf("%d%s", &N, S);
                                                               int n = s.length();
ROOT = LAST = new Node(0);
                                                                s += s;
for (int i = 0; S[i]; i++)
Extend(S[i] - 'a');
                                                                int i=0, j=1;
                                                                while (i<n && j<n){</pre>
while (N--){
                                                                int k = 0;
  scanf("%s", A);
                                                                 while (k < n \&\& s[i+k] == s[j+k]) k++;
  Node *cursor = ROOT;
                                                                if (s[i+k] <= s[j+k]) j += k+1;
 bool ans = true;
                                                                else i += k+1;
  for (int i = 0; A[i]; i++){
                                                                if (i == j) j++;
  cursor = cursor->edge[A[i] - 'a'];
  if (!cursor) {
                                                                int ans = i < n ? i : j;</pre>
   ans = false;
                                                                return s.substr(ans, n);
    break:
   }
                                                              7.8 BWT
 puts(ans ? "Yes" : "No");
                                                              struct BurrowsWheeler{
                                                              #define SIGMA 26
return 0;
                                                              #define BASE 'a'
                                                               vector<int> v[ SIGMA ];
                                                                void BWT(char* ori, char* res){
7.4
      KMP
                                                                // make ori -> ori + ori
                                                                 // then build suffix array
vector<int> kmp(const string &s) {
vector<int> f(s.size(), 0);
                                                                void iBWT(char* ori, char* res){
 /* f[i] = length of the longest prefix
   (excluding s[0:i]) such that it coincides
                                                                for( int i = 0 ; i < SIGMA ; i ++ )</pre>
   with the suffix of s[0:i] of the same length */
                                                                  v[ i ].clear();
                                                                 int len = strlen( ori_);
 /* i + 1 - f[i] is the length of the
                                                                 for( int i = 0 ; i < len ; i ++ )</pre>
   smallest recurring period of s[0:i] */
                                                                  v[`ori[i] - BASE ].push_back( i );
int k = 0;
for (int i = 1; i < (int)s.size(); ++i) {
  while (k > 0 && s[i] != s[k]) k = f[k - 1];
                                                                 vector<int> a:
                                                                 for( int i = 0 , ptr = 0 ; i < SIGMA ; i ++ )</pre>
  if (s[i] == s[k]) ++k;
                                                                  for( auto j : v[ i ] ){
                                                                   a.push_back( j );
ori[ ptr ++ ] = BASE + i;
 f[i] = k;
return f:
                                                                for( int i = 0 , ptr = 0 ; i < len ; i ++ ){
  res[ i ] = ori[ a[ ptr ] ];</pre>
vector<int> search(const string &s, const string &t) {
// return 0-indexed occurrence of t in s
                                                                  ptr = a[ ptr ];
vector < int > f = kmp(t), r;
                                                                 }
for (int i = 0, k = 0; i < (int)s.size(); ++i) {</pre>
                                                                 res[ len ] = 0;
 while(k > 0 && (k==(int)t.size() \mid \mid s[i]!=t[k]))
  k = f[k - 1]
                                                              } bwt;
  if (s[i] == t[k]) ++k;
                                                               7.9
                                                                    Palindromic Tree
 if (k == (int)t.size()) r.push_back(i-t.size()+1);
                                                              struct palindromic_tree{
return res;
                                                               struct node{
                                                                 int next[26],f,len;
                                                                 int cnt,num,st,ed;
                                                                 node(int l=0):f(0),len(l),cnt(0),num(0) {
```

7.5 Z value

```
memset(next, 0, sizeof(next)); }
vector<node> st:
 vector<char> s:
int last.n:
void init(){
 st.clear();s.clear();last=1; n=0;
 st.push_back(0);st.push_back(-1);
  st[0].f=1;s.push_back(-1); }
 int getFail(int x){
 while(s[n-st[x].len-1]!=s[n])x=st[x].f;
  return x;}
void add(int c){
s.push_back(c-='a'); ++n;
  int cur=getFail(last);
  if(!st[cur].next[c]){
   int now=st.size();
   st.push_back(st[cur].len+2);
   st[now].f=st[getFail(st[cur].f)].next[c];
   st[cur].next[c]=now;
  st[now].num=st[st[now].f].num+1;
  last=st[cur].next[c];
 ++st[last].cnt;}
int size(){ return st.size()-2;}
} pt:
int main() {
string s; cin >> s; pt.init();
for (int i=0; i<SZ(s); i++) {
  int prvsz = pt.size(); pt.add(s[i]);</pre>
  if (prvsz != pt.size()) {
  int r = i, l = r - pt.st[pt.last].len + 1;
   // pal @ [1,r]: s.substr(1, r-1+1)
return 0;
```

8 Misc

8.1 Theorems

8.1.1 Kirchhoff's Theorem

Denote L be a $n\times n$ matrix as the Laplacian matrix of graph G, where $L_{ii}=d(i)$, $L_{ij}=-c$ where c is the number of edge (i,j) in G.

- The number of undirected spanning in G is $|\det(\tilde{L}_{11})|$.
- The number of directed spanning tree rooted at r in G is $|\det(\tilde{L}_{rr})|$.

8.1.2 Tutte's Matrix

Let D be a $n \times n$ matrix, where $d_{ij} = x_{ij}$ (x_{ij} is chosen uniform randomly) if i < j and $(i,j) \in E$, otherwise $d_{ij} = -d_{ji}$. $\frac{rank(D)}{2}$ is the maximum matching on G.

8.1.3 Cayley's Formula

- Given a degree sequence d_1,d_2,\ldots,d_n for each labeled vertices, there're $\frac{(n-2)!}{(d_1-1)!(d_2-1)!\cdots(d_n-1)!}$ spanning trees.
- Let $T_{n,k}$ be the number of labeled forests on n vertices with k components, such that vertex $1,2,\ldots,k$ belong to different components. Then $T_{n,k}=kn^{n-k-1}$.

8.1.4 Erdős-Gallai theorem

A sequence of non-negative integers $d_1 \geq d_2 \geq \ldots \geq d_n$ can be represented as the degree sequence of a finite simple graph on n vertices if and only if $d_1+d_2+\ldots+d_n$ is even and

$$\sum_{i=1}^k d_i \leq k(k-1) + \sum_{i=k+1}^n \min(d_i, k)$$

holds for all $1 \le k \le n$.

8.1.5 Havel-Hakimi algorithm

find the vertex who has greatest degree unused, connect it with other greatest vertex.

8.1.6 Hall's marriage theorem

Let G be a finite bipartite graph with bipartite sets X and Y. For a subset W of X, let $N_G(W)$ denote the set of all vertices in Y adjacent to some element of W. Then there is an X-saturating matching iff $\forall W\subseteq X, |W|\leq |N_G(W)|$

8.1.7 Euler's planar graph formula

V - E + F = C + 1, $E \le 3V - 6$ (?)

8.1.8 Pick's theorem

For simple polygon, when points are all integer, we have $A=\#\{\text{lattice points in the interior}\}+\frac{\#\{\text{lattice points on the boundary}\}}{2}-1$

8.1.9 Lucas's theorem

```
{m\choose n}\equiv\prod_{i=0}^k{m_i\choose n_i}\pmod{p}, \text{ where } m=m_kp^k+m_{k-1}p^{k-1}+\cdots+m_1p+m_0, and n=n_kp^k+n_{k-1}p^{k-1}+\cdots+n_1p+n_0.
```

8.1.10 Matroid Intersection

Given matroids $M_1=(G,I_1),M_2=(G,I_2)$, find maximum $S\in I_1\cap I_2$. For each iteration, build the directed graph and find a shortest path from s to t.

- $s \rightarrow x : S \sqcup \{x\} \in I_1$
- $x \to t : S \sqcup \{x\} \in I_2$
- $y \to x : S \setminus \{y\} \sqcup \{x\} \in I_1$ (y is in the unique circuit of $S \sqcup \{x\}$)
- $x \to y: S \setminus \{y\} \sqcup \{x\} \in I_2$ (y is in the unique circuit of $S \sqcup \{x\}$)

Alternate the path, and |S| will increase by 1. Let $R=\min(\mathrm{rank}(I_1),\mathrm{rank}(I_2)),N=|G|.$ In each iteration, |E|=O(RN). For weighted case, assign weight -w(x) and w(x) to $x\in S$ and $x\notin S$, resp. Use Bellman-Ford to find the weighted shortest path. The maximum iteration of Bellman-Ford is 2R+1.

8.2 DP-opt Condition

8.2.1 totally monotone (concave/convex)

```
\begin{array}{l} \forall i < i', j < j', B[i][j] \leq B[i'][j] \implies B[i][j'] \leq B[i'][j'] \\ \forall i < i', j < j', B[i][j] \geq B[i'][j] \implies B[i][j'] \geq B[i'][j'] \end{array}
```

8.2.2 monge condition (concave/convex)

```
\begin{array}{l} \forall i < i', j < j', B[i][j] + B[i'][j'] \geq B[i][j'] + B[i'][j] \\ \forall i < i', j < j', B[i][j] + B[i'][j'] \leq B[i][j'] + B[i'][j] \end{array}
```

8.3 Convex 1D/1D DP

```
struct segment {
 int i, 1, r;
 segment() {}
 segment(int a, int b, int c): i(a), l(b), r(c) {}
inline 1ld f(int 1, int r){return dp[1] + w(1+1, r);}
void solve() {
 dp[0] = 0;
 deque<segment> dq; dq.push_back(segment(0, 1, n));
 for (int i = 1; i <= n; ++i) {
  dp[i] = f(dq.front().i, i);
  while(dq.size()&&dq.front().r<i+1) dq.pop_front();</pre>
  dq.front().l = i + 1;
  segment seg = segment(i, i + 1, n);
  while (dq.size() &&
   f(i, dq.back().1) < f(dq.back().i, dq.back().1)
    dq.pop_back()
  if (dq.size())
   int d = 1 << 20, c = dq.back().1;
while (d >>= 1) if (c + d <= dq.back().r)</pre>
    if(f(i, c+d) > f(dq.back().i, c+d)) c += d;
   dq.back().r = c; seg.l = c + 1;
  if (seg.1 <= n) dq.push_back(seg);</pre>
```

8.4 ConvexHull Optimization

```
void Insert(int64_t a, int64_t b) {
                                                               }else{
 auto z = insert({a, b, 0}), y = z++, x = y;
                                                                for(int i=0;i<(int)g[u].size();i++){</pre>
  while (Isect(y, z)) z = erase(z);
                                                                 int v=g[u][i];
  if (x != begin() && Isect(--x, y)) Isect(x, y = erase
                                                                 if(v==fa) continue;
                                                                 dfs(v,u);
 while ((y = x) != begin() && (--x)->p >= y->p) Isect(
    x, erase(y));
                                                                min_dp[0][0]=0;
                                                                min_dp[1][1]=1;
int64_t Query(int64_t x) {
                                                                min_dp[0][1]=min_dp[1][0]=-0x3f3f3f3f;
 auto 1 = *lower_bound(x);
                                                                for(int i=0;i<(int)g[u].size();i++){</pre>
  return 1.a * x + 1.b;
                                                                 int v=g[u][i];
                                                                 if(v==fa) continue;
                                                                 memset(tmp,0x8f,sizeof tmp);
};
                                                                 tmp[0][0]=max(
8.5
      Josephus Problem
                                                                  \min_{dp[0][0]+\max(dp[v][0],dp[v][1])}
                                                                  min_dp[0][1]+dp[v][0]
// n people kill m for each turn
int f(int n, int m) {
int s = 0:
                                                                 tmp[0][1]=min_dp[0][0]+dp[v][0]+1;
                                                                 tmp[1][0]=max(
for (int i = 2; i <= n; i++)
 s = (s + m) \% i;
                                                                  \min_{dp[1][0]+\max(dp[v][0],dp[v][1])}
                                                                  min_dp[1][1]+dp[v][0]
 return s;
// died at kth
                                                                 tmp[1][1]=min_dp[1][0]+dp[v][0]+1;
int kth(int n, int m, int k){
                                                                 memcpy(min_dp,tmp,sizeof tmp);
if (m == 1) return n-1;
for (k = k*m+m-1; k >= n; k = k-n+(k-n)/(m-1));
                                                                dp[u][1]=max(min_dp[0][1],min_dp[1][0]);
                                                                dp[u][0]=min_dp[0][0];
return k;
8.6 Cactus Matching
                                                              int main(){
vector<int> init_g[maxn],g[maxn*2];
                                                               int m,a,b;
                                                               scanf("%d%d",&n,&m);
for(int i=0;i<m;i++){</pre>
int n,dfn[maxn],low[maxn],par[maxn],dfs_idx,bcc_id;
void tarjan(int u){
                                                                scanf("%d%d",&a,&b);
dfn[u]=low[u]=++dfs_idx;
                                                                init_g[a].push_back(b);
for(int i=0;i<(int)init_g[u].size();i++){</pre>
  int v=init_g[u][i];
                                                                init_g[b].push_back(a);
  if(v==par[u]) continue;
  if(!dfn[v]){
                                                               par[1]=-1;
                                                               tarjan(1);
  par[v]=u:
                                                               dfs(1,-1);
   tarjan(v);
                                                               printf("%d\n", max(dp[1][0], dp[1][1]));
   low[u]=min(low[u],low[v]);
   if(dfn[u]<low[v]){</pre>
                                                               return 0;
                                                             }
    g[u].push_back(v);
    g[v].push_back(u);
                                                              8.7 DLX
                                                             struct DLX {
  }else{
   low[u]=min(low[u],dfn[v]);
                                                               const static int maxn=210;
   if(dfn[v]<dfn[u]){</pre>
                                                               const static int maxm=210;
                                                               const static int maxnode=210*210;
    int temp_v=u;
                                                               int n, m, size, row[maxnode], col[maxnode];
    bcc_id++;
                                                               int U[maxnode], D[maxnode], L[maxnode], R[maxnode];
    while(temp_v!=v){
                                                               int H[maxn], S[maxm], ansd, ans[maxn];
     g[bcc_id+n].push_back(temp_v);
                                                               void init(int _n, int _m) {
     g[temp_v].push_back(bcc_id+n);
     temp_v=par[temp_v];
                                                                n = _n, m = _m;
                                                                for(int i = 0; i <= m; ++i) {</pre>
                                                                 S[\hat{i}] = 0
    g[bcc_id+n].push_back(v);
    g[v].push_back(bcc_id+n);
                                                                 U[i] = D[i] = i;
    reverse(g[bcc_id+n].begin(),g[bcc_id+n].end());
                                                                 L[i] = i-1, R[i] = i+1;
                                                                R[L[0] = size = m] = 0;
                                                                for(int i = 1; i <= n; ++i) H[i] = -1;</pre>
                                                               void Link(int r, int c) {
int dp[maxn][2], min_dp[2][2], tmp[2][2], tp[2];
void dfs(int u,int fa){
                                                                ++S[col[++size] = c];
 if(u<=n){</pre>
                                                                row[size] = r; D[size] = D[c];
  for(int i=0;i<(int)g[u].size();i++){</pre>
                                                                U[D[c]] = size; U[size] = c; D[c] = size;
   int v=g[u][i];
                                                                if(H[r] < 0) H[r] = L[size] = R[size] = size;
   if(v==fa) continue;
                                                                else {
                                                                 R[size] = R[H[r]];
   dfs(v,u);
                                                                 L[R[H[r]]] = size;
   memset(tp,0x8f,sizeof tp);
   if(v<=n){
                                                                 L[size] = H[r];
                                                                 R[H[r]] = size;
    tp[0]=dp[u][0]+max(dp[v][0],dp[v][1]);
    tp[1]=max(
     dp[u][0]+dp[v][0]+1
     dp[u][1]+max(dp[v][0],dp[v][1])
                                                               void remove(int c) {
                                                                L[R[c]] = L[c]; R[L[c]] = R[c];
    );
                                                                for(int i = D[c]; i != c; i = D[i])
for(int j = R[i]; j != i; j = R[j]) {
   }else{
    tp[0]=dp[u][0]+dp[v][0];
                                                                  U[D[j]] = U[j];
D[U[j]] = D[j];
    tp[1]=max(dp[u][0]+dp[v][1],dp[u][1]+dp[v][0]);
   dp[u][0]=tp[0],dp[u][1]=tp[1];
                                                                  --S[col[j]];
```

```
void resume(int c) {
 L[R[c]] = c; R[L[c]] = c;
  for(int i = U[c]; i != c; i = U[i])
   for(int j = L[i]; j != i; j = L[j]) {
    U[D[j]] = j;
    D[U[j]] = j;
    ++S[col[j]];
void dance(int d) {
  if(d>=ansd) return;
  if(R[0] == 0) {
   ansd = d;
   return;
  int c = R[0];
  for(int i = R[0]; i; i = R[i])
  if(S[i] < S[c]) c = i;
  remove(c);
  for(int i = D[c]; i != c; i = D[i]) {
   ans[d] = row[i];
   for(int j = R[i]; j != i; j = R[j])
    remove(col[j]);
   dance(d+1);
   for(int j = L[i]; j != i; j = L[j])
    resume(col[j]);
 resume(c);
} sol;
8.8 Tree Knapsack
int dp[N][K];PII obj[N];
vector<int> G[N];
void dfs(int u, int mx){
for(int s: G[u]) {
  if(mx < obj[s].first) continue;</pre>
  for(int i=0;i<=mx-obj[s].FF;i++)</pre>
   dp[s][i] = dp[u][i];
  dfs(s, mx - obj[s].first);
  for(int i=obj[s].FF;i<=mx;i++)</pre>
   dp[u][i] = max(dp[u][i],
    dp[s][i - obj[s].FF] + obj[s].SS);
}
int main(){
int n, k; cin >> n >> k;
for(int i=1;i<=n;i++){</pre>
 int p; cin >> p;
 G[p].push_back(i);
 cin >> obj[i].FF >> obj[i].SS;
dfs(0, k); int ans = 0;
for(int i=0; i<=k; i++) ans = max(ans, dp[0][i]);
cout << ans << '\n';
return 0;
8.9 N Queens Problem
vector< int > solve( int n ) {
 // no solution when n=2, 3
vector< int > ret;
if ( n % 6 == 2 ) {
  for ( int i = 2 ; i <= n ; i += 2 )
    ret.push_back( i );</pre>
 ret.push_back( 3 ); ret.push_back( 1 );
for ( int i = 7 ; i <= n ; i += 2 )
  ret.push_back( i );</pre>
 ret.push_back( 5 );
} else if ( n % 6 == 3 ) {
for ( int i = 4 ; i <= n ; i += 2 )</pre>
   ret.push_back( i );
  ret.push_back( 2 );
 for ( int i = 5 ; i <= n ; i += 2 )
  ret.push_back( i );</pre>
 ret.push_back( 1 ); ret.push_back( 3 );
 } else {
 for ( int i = 2 ; i <= n ; i += 2 )
   ret.push_back( i );
  for ( int i = 1 ; i <= n ; i += 2 )
   ret.push_back( i );
```

```
}
return ret;
}

8.10 Aliens Optimization
long long Alien() {
  long long c = kInf;
  for (int d = 60; d >= 0; --d) {
    // cost can be negative, depending on the problem.
    if (c - (1LL << d) < 0) continue;
    long long ck = c - (1LL << d);
    pair<long long, int> r = check(ck);
    if (r.second == k) return r.first - ck * k;
    if (r.second < k) c = ck;
}

pair<long long, int> r = check(c);
    return r.first - c * k;
}
```