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I Basic

1.1 Default Code

```
#include <bits/stdc++.h>
using namespace std;
using lld = int64_t;
using llu = uint64_t;
using llf = long double;
using PII = pair<int,int>;
using PIL = pair<int, lld>;
using PLI = pair<lld,int>;
using PLL = pair<lld, lld>;
template<typename T>
using maxHeap = priority_queue<T, vector<T>, less<T>>;
template<typename T>
using minHeap = priority_queue<T, vector<T>, greater<T>>;
#define FF first
#define SS second
#define SZ(x) (int)((x).size())
#define ALL(x) begin(x), end(x)
#define PB push_back
#define WC(x) while((x)--)
template<typename Iter>
ostream& out(ostream &s, Iter b, Iter e) {
    s<<"[";
    for ( auto it=b; it!=e; it++ ) s<<(it==b?"":" ")<<*</pre>
        it;
    s<<"]";
    return s;
template<typename A, typename B>
ostream& operator <<( ostream &s, const pair<A,B> &p )
    { return s<<"("<<p.FF<<","<<p.SS<<")"; }
template<typename T>
ostream& operator <<( ostream &s, const vector<T> &c )
    { return _out(s,ALL(c)); }
bool debug = \overline{0};
template<typename T>
void DEBUG(const T& x) {if(debug) cerr<<x;}</pre>
 template<typename T, typename... Args>
void DEBUG(const T& head, const Args& ...tail) {
    if(debug) {cerr<<head; DEBUG(tail...);}</pre>
int main(int argc, char* argv[]){
    if(argc>1 and string(argv[1])=="-D") debug=1;
    if(!debug) {ios_base::sync_with_stdio(0);cin.tie(0)
        ;}
    return 0;
```

1.2 IncreaseStackSize

```
//stack resize
asm( "mov %0,%%esp\n" ::"g"(mem+10000000) );
//change esp to rsp if 64-bit system
//stack resize (linux)
#include <sys/resource.h>
void increase_stack_size() {
    const rlim t ks = 64*1024*1024;
    struct rlimit rl;
    int res=getrlimit(RLIMIT_STACK, &rl);
    if(res==0){
        if(rl.rlim cur<ks){</pre>
            rl.rlim cur=ks;
            res=setrlimit(RLIMIT STACK, &rl);
        }
    }
// craziest way
static void run_with_stack_size(void (*func)(), size t
    stsize) {
    char *stack, *send;
    stack=(char *)malloc(stsize);
    send=stack+stsize-16;
    send=(char *)((uintptr t)send/16*16);
    asm volatile(
      "mov %%rsp, (%0)\n"
```

```
"mov %0, %%rsp\n"
:
    : "r" (send));
func();
asm volatile(
    "mov (%0), %%rsp\n"
:
    : "r" (send));
free(stack);
}
```

1.3 Pragma optimization

```
#pragma GCC optimize("Ofast,no-stack-protector,no-math-
errno,unroll-loops")
#pragma GCC target("sse,sse2,sse3,sse4,popcnt,abm
,mmx,avx,tune=native")
```

1.4 Debugger

```
#! /usr/bin/env python3
import subprocess, platform
os_name = platform.system()
cmd = []
prefix = ""
if os_name == 'Windows':
   cmd = ["cmd", "/C"]
   cmd = ["bash", "-c"]
  prefix = "./"
def GetTestData(exe):
   myout = subprocess.check output(cmd + ["%s%s"%(
       prefix, exe)])
   return myout.decode("utf8")
def Judge(a,b,testdata):
    f = open("test.in", "w+")
   f.write(testdata)
   f.close()
  \verb|myout = subprocess.check_output(cmd + ["%s%s < test.]|
       in"%(prefix, a)])
   ansout = subprocess.check output(cmd + ["%s%s < test
       .in"%(prefix, b)])
   if not myout == ansout:
      print("answer: %s"%ansout.decode("utf8"), end="")
      print("output: %s"%myout.decode("utf8"),end="")
     print("WA!")
      return False
 return True
if __name_
           == ' main ':
   cnt = 0
   isOK = True
   while isOK:
      cnt += 1
      print(cnt)
      isOK = Judge("1397.exe", "test.exe", GetTestData(
          "gen.exe"))
```

1.5 Quick Random

```
// PRNG {{{
    template < class T, T x1, T x2, T x3, int y1, int y2, int
        y3 >
    struct PRNG {
        using S = typename std::make_signed < T > :: type;
        T s;
        PRNG (T _s = 0) : s(_s) {}
        T next() {
            T z = (s += x1);
            z = (z ^ (z >> y1)) * x2;
            z = (z ^ (z >> y2)) * x3;
            return z ^ (z >> y3);
        }
        T next(T n) { return next() % n; }
        S next(S 1, S r) { return 1 + next(r - 1 + 1); }
        T operator()() { return next(n); }
        T operator()(T n) { return next(n); }
```

1.6 IO Optimization

```
static inline int gc() {
    static char buf[1 << 20], *p = buf, *end = buf;</pre>
    if (p == end) {
        if ((end = buf + fread(buf, 1, 1 << 20, stdin))</pre>
             == buf) return EOF;
        p = buf;
    return *p++;
template<typename T>
static inline bool gn(T &_){
    register int c = gc(); register T
                                           = 1;
    while(!isdigit(c) and c!=EOF and c!='-') c = gc();
    if(c == '-') { __ = -1; c = if(c == EOF) return false;
                      = -1; c = gc(); 
    while(isdigit(c)) _ = _ * 10 + c - '0', c = gc();
     return true;
template <typename T, typename ...Args>
static inline bool gn(T &x, Args& ...args) {return gn(x)
     and gn(args...);}
```

2 Data Structure

2.1 Bigint

```
class BigInt{
  private:
    using lld = int fast64 t;
    #define PRINTF ARG PRIdFAST64
    #define LOG_BASE_STR "9"
    static constexpr lld BASE = 1000000000;
    static constexpr int LOG BASE = 9;
    vector<lld> dig;
    bool neg;
    inline int len()const{return (int)dig.size();}
    inline int cmp minus(const BigInt& a) const {
      if(len() == \overline{0} \text{ and } a.len() == 0) \text{ return } 0;
      if(neg ^ a.neg) return (int)a.neg*2 - 1;
      if(len() != a.len()) return neg?a.len()-len():len
           ()-a.len();
      for(int i=len()-1;i>=0;i--) if(dig[i] != a.dig[i
          ]) {
        return neg?a.dig[i]-dig[i]:dig[i]-a.dig[i];
      }
      return 0;
    inline void trim(){
      while(!dig.empty() and dig.back()==0) dig.
          pop back();
      if(dig.empty()) neg = false;
  public:
    BigInt(): dig(vector<lld>()), neg(false){}
    BigInt(lld a): dig(vector<lld>()) {
      neg = a<0; dig.push_back(abs(a));
      trim();
```

```
BigInt(const string& a): dig(vector<lld>()){
  assert(!a.empty()); neg = (a[0] == '-');
  for(int i=((int)(a.size()))-1;i>=neg;i-=LOG BASE)
    11d cur = 0;
    for(int j=min(LOG_BASE-1, i-neg);j>=0;j--) cur
        = cur*10+a[i-j]-'0';
    dig.push back(cur);
  } trim();
inline bool operator<(const BigInt& a)const{return</pre>
    cmp minus(a)<0;}
inline bool operator<=(const BigInt& a)const{return</pre>
     cmp minus(a) <=0;}</pre>
inline bool operator==(const BigInt& a)const{return
     cmp minus(a) == 0;}
inline bool operator!=(const BigInt& a)const{return
     cmp minus(a)!=0;}
inline bool operator>(const BigInt& a)const{return
    cmp minus(a)>0;}
inline bool operator>=(const BigInt@ a)const{return
     cmp_minus(a) >= 0;
BigInt operator-() const {
  BigInt ret = *this;
  ret.neg ^= 1;
  return ret;
BigInt operator+(const BigInt& a) const {
  if(neg) return -(-(*this)+(-a));
  if(a.neg) return (*this)-(-a);
  int n = max(a.len(), len());
  BigInt ret; ret.dig.resize(n);
  11d pro = 0;
  for (int i=0;i<n;i++) {</pre>
    ret.dig[i] = pro;
    if(i < a.len()) ret.dig[i] += a.dig[i];</pre>
    if(i < len()) ret.dig[i] += dig[i];</pre>
    if(ret.dig[i] >= BASE) pro = ret.dig[i]/BASE;
    ret.dig[i] -= BASE*pro;
  if(pro != 0) ret.dig.push_back(pro);
  return ret;
BigInt operator-(const BigInt& a) const {
  if (neg) return - (-(*this) - (-a));
  if(a.neg) return (*this) + (-a);
int diff = cmp_minus(a);
  if(diff < 0) return -(a - (*this));</pre>
  if(diff == 0) return 0;
  BigInt ret; ret.dig.resize(len(), 0);
  for(int i=0;i<len();i++) {</pre>
    ret.dig[i] += dig[i];
    if(i < a.len()) ret.dig[i] -= a.dig[i];</pre>
    if(ret.dig[i] < 0){
      ret.dig[i] += BASE;
      ret.dig[i+1]--;
    }
  ret.trim();
  return ret;
BigInt operator*(const BigInt& a) const {
  if(len()==0 or a.len()==0) return 0;
  BigInt ret; ret.dig.resize(len()+a.len()+1);
  ret.neg = neg ^ a.neg;
  for (int i=0;i<len();i++) for (int j=0;j<a.len();j</pre>
      ++) {
    ret.dig[i+j] += dig[i] * a.dig[j];
    if (ret.dig[i+j] >= BASE) {
     lld x = ret.dig[i+j] / BASE;
      ret.dig[i+j+1] += x;
ret.dig[i+j] -= x * BASE;
   }
  ret.trim();
  return ret;
BigInt operator/(const BigInt& a) const {
  assert(a.len());
  if(len() < a.len()) return 0;</pre>
  BigInt ret; ret.dig.resize(len()-a.len()+1);
  ret.neg = a.neg;
  for(int i=len()-a.len();i>=0;i--){
    lld l = 0, r = BASE;
```

```
while (r-1 > 1) {
      11d \ mid = (1+r) >> 1;
      ret.dig[i] = mid;
      if (ret*a <= (neg?-(*this):(*this))) l = mid;</pre>
      else r = mid;
    ret.dig[i] = 1;
  ret.neg ^= neg; ret.trim();
  return ret;
BigInt operator%(const BigInt& a) const {
  return (*this) - (*this) / a * a;
friend BigInt abs(BigInt a) {
  a.neg = 1; return a;
friend void swap(BigInt& a, BigInt& b){
  swap(a.dig, b.dig); swap(a.neg, b.neg);
friend istream& operator>>(istream& ss, BigInt& a) {
 string s; ss >> s;
  a = s;
  return ss;
friend ostream& operator<<(ostream& ss, const</pre>
   BigInt& a) {
  if(a.len() == 0) return ss << '0';
if(a.neg) ss << '-';</pre>
  ss << a.dig.back();
  for(int i=a.len()-2;i>=0;i--) ss << setw(LOG BASE</pre>
     ) << setfill('0') << a.dig[i];
  return ss;
inline void print() const {
  if(len() == 0) {putchar('0'); return;}
  if(neg) putchar('-');
  printf("%" PRINTF_ARG, dig.back());
  for(int i=len()-2;i>=0;i--) printf("%0"
      LOG BASE STR PRINTF ARG, dig[i]);
#undef PRINTF ARG
#undef LOG BASE STR
```

2.2 Linear Basis

};

```
struct LinearBasis{
private:
    int n, sz;
    vector<llu> B;
    public:
    void init(int n ) {
        n = n_{;} B.clear();
        B.resize(n); sz = 0;
    void insert(llu x) {
        // add x into B
        for (int i=n-1;i>=0;i--) if (two(i) & x) {
            if(B[i]) x ^= B[i];
            else{
                B[i] = x; sz++;
                for (int j=i-1; j>=0; j--)
                    if(B[j] and two(j) & B[i])
                        B[i] ^= B[j];
                for (int j=i+1; j < n; j++)</pre>
                    if(two(i) & B[j])
    B[j] ^= B[i];
                break;
            }
        }
    inline int size() {return sz;}
    bool check(llu x) {
        // is x in span(B) ?
        for (int i=n-1;i>=0;i--) if (two(i) & x) {
            if(B[i]) x ^= B[i];
            else return false;
        return true;
    llu kth_small(llu k) {
        /** 1-base would always > 0 **/
```

2.3 unordered_map

```
#include <ext/pb_ds/assoc_container.hpp>
using __gnu_pbds::cc_hash_table;
using __gnu_pbds::gp_hash_table;
template<typename A, typename B> using hTable1 =
    cc_hash_table<A,B>;
template<typename A, typename B> using hTable2 =
    gp_hash_table<A,B>;
```

2.4 extc_balance_tree

```
#include <functional>
#include <ext/pb_ds/assoc_container.hpp>
using std::less;
using std::greater;
using __gnu_pbds::tree;
using __gnu_pbds::rb_tree_tag;
using __gnu_pbds::ov_tree_tag;
using __gnu_pbds::splay_tree_tag;
using __gnu_pbds::null_type;
using __gnu_pbds::tree_order_statistics_node_update;
template<typename T>
using ordered_set = tree<T, null_type, less<T>,
    rb tree tag, tree order statistics node update>;
template<typename A, B>
using ordered map = tree<A, B, less<A>, rb tree tag,
    tree order statistics node update>;
int main() {
   ordered set<int> ss;
    ordered map<int,int> mm;
    ss.insert(1);
    ss.insert(5);
    assert(*ss.find_by_order(0)==1);
assert(ss.order_of_key(-1)==0);
    assert(ss.order_of_key(87) == 2);
    return 0;
```

2.5 extc_heap

```
#include <functional>
#include <ext/pb ds/assoc container.hpp>
#include <ext/pb ds/priority queue.hpp>
using std::less;
using std::greater;
using __gnu_pbds::priority_queue;
using __gnu_pbds::pairing_heap_tag;
using __gnu_pbds::binary_heap_tag;
using __gnu_pbds::binomial_heap_tag;
using __gnu_pbds::rc_binomial_heap_tag;
using __gnu_pbds::thin_heap_tag;
int main(){
   priority queue<int,less<int>,pairing heap tag> pq1,
         pq2;
    pq1.push(1);
    pq2.push(2);
    pq1.join(pq2);
    assert(pq2.size() == 0);
    auto it = pq1.push(87);
    pq1.modify(it, 19);
```

```
while(!pq1.empty()) {
        pq1.top();
        pq1.pop();
    }
    return 0;
}
```

2.6 SkewHeap

```
#include <functional>
using std::less;
template<typename T, typename cmp=less<T> >
class SkewHeap{
private:
    struct SkewNode {
        T x;
         SkewNode *lc, *rc;
        SkewNode(T a=0):x(a), lc(nullptr), rc(nullptr)
    } *root;
    cmp CMP_;
    size t count;
    SkewNode* Merge(SkewNode* a, SkewNode* b) {
        if(!a or !b) return a?a:b;
        if(CMP_(a->x, b->x)) swap(a, b);
        a->rc = Merge(a->rc, b);
        swap(a->lc, a->rc);
        return a;
    void clear(SkewNode*& a) {
        if(!a) return;
         clear(a->lc); clear(a->rc);
        delete a; a = nullptr;
public:
    SkewHeap(): root(nullptr), count(0){}
    bool empty() {return count==0;}
    size t size() {return count;}
    T top() {return root->x;}
    void clear() {clear(root); count = 0; }
    void push(const T& x) {
        SkewNode* a = new SkewNode(x);
        count += 1;
        root = Merge(root, a);
    void join(SkewHeap& a) {
        count += a.count; a.count = 0;
         root = Merge(root, a.root);
    }() gog biov
         count -= 1:
         SkewNode* rt = Merge(root->lc, root->rc);
        delete root; root = rt;
    friend void swap (SkewHeap& a, SkewHeap& b) {
        swap(a.root, b.root);
};
```

2.7 Disjoint Set

```
class DJS{
private:
    vector<int> fa, sz, sv;
    vector<pair<int*, int>> opt;
    inline void assign(int *k, int v) {
        opt.emplace back(k, *k);
        *k = v;
public:
    inline void init(int n) {
        fa.resize(n); iota(fa.begin(), fa.end(), 0);
        sz.resize(n); fill(sz.begin(), sz.end(), 1);
        opt.clear();
    int query(int x){
        if(fa[x] == x) return x;
        return query(fa[x]);
    inline void merge(int a, int b) {
        int af = query(a), bf = query(b);
```

```
if(af == bf) return;
if(sz[af] < sz[bf]) swap(af, bf);
assign(&fa[bf], fa[af]);
assign(&sz[af], sz[af]+sz[bf]);
}
inline void save(){sv.push_back((int)opt.size());}
inline void undo(){
   int ls = sv.back(); sv.pop_back();
   while((int)opt.size() > ls){
      pair<int*, int> cur=opt.back();
      *cur.first = cur.second;
      opt.pop_back();
   }
};
```

2.8 Treap

```
class Treap{
private:
    const int MEM = 500000 + 5;
    unsigned seed;
    inline unsigned myrand() {
        static unsigned seed = time(NULL);
        seed = seed*seed*127 + seed*227 + 2147483587;
        seed ^= seed*97;
        seed /= 7123;
        return seed;
    struct node{
        node *lc, *rc;
        int pri, size, val;
        node(){}
        node(int x):
            lc(nullptr),
            rc(nullptr),
            pri(myrand()),
            size(1),
            val(x)
        inline void pull(){
            size = 1:
            if(lc) size += lc->size;
            if(rc) size += rc->size;
        }
    } *root, pool[MEM];
    int mem ;
    inline node* new_node(int x) {
        static int mem = 0;
        assert (mem < \overline{MEM});
        pool[mem_] = node(x);
        return &pool[mem ++];
    inline int sz(node* x) {return x?x->size:0;}
    node* merge(node *a, node *b) {
        if(!a or !b) return a?a:b;
        if(a->pri > b->pri){
            a->rc = merge(a->rc, b);
            a->pull();
            return a;
        }else{
            b->lc = merge(a, b->lc);
            b->pull();
            return b;
    void split(Treap* t, int k, Treap*& a, Treap*& b) {
        if(!t) a=b=nullptr;
        else if (sz(t->lc) < k) {
            a = t;
            split(t->rc, k-sz(t->lc)-1, a->rc, b);
            a->pull();
        }else{
            b = t;
            split(t->lc, k, a, b->lc);
            b->pull();
        }
    int oOk(node* rr, int x){
        if(rr==NULL)return 0;
        if((rr->val) < x)return gSize(rr->l)+oOk(rr->r,
             x) + 1;
        else return oOk(rr->1, x);
    }
```

```
public:
    Treap() {root=nullptr; seed=time(NULL); mem =0;}
    void do_something_at(int 1, int r){
        // \overline{1}-base [1, r]
        split(root, 1-1, tl, root);
        split(root, r-l+1, root, tr);
        root = merge(tl, merge(root, tr));
    void insert(int x) {
        node *a, *b;
        split(root, x, a, b);
        root = merge(merge(a, new node(x)), b);
        root->size = gSize(root->1)+gSize(root->r)+1;
    void remove(int x) {
        //need debug may contain bugs
        node *a, *b, *c, *d;
        split(root, x, a, b);
        a->size = gSize(a->1)+gSize(a->r);
        split(a, x-1, c, d);
        root = merge(b, c);
        root->size = gSize(root->1)+gSize(root->r);
        delete d;
    int order of key(int x) {return oOk(root,x);}
};
```

2.9 SparseTable

```
template<typename T, typename Cmp_=std::less<T>>
class SparseTable{
private:
    vector<vector<T>> table;
    vector<int> lg;
    T cmp_(T a, T b) {
         return Cmp_()(a, b)?a:b;
public:
    void init(T arr[], int n){
         // 0-base
         lg.resize(n+1);
         lg[0] = -1, lg[1] = 0;
         for(int i=2;i<=n;i++) lg[i] = lg[i>>1]+1;
         table.resize(lg[n]+1);
         table[0].resize(n);
         for(int i=0;i<n;i++) table[0][i] = arr[i];</pre>
         for (int i=1;i<=lg[n];i++) {</pre>
             int len = 1 << (i-1), sz = 1 << i;
              table[i].resize(n-sz+1);
             for (int j=0; j<=n-sz; j++) {</pre>
                  table[i][j] = cmp_(table[i-1][j], table
                      [i-1][j+len]);
              }
         }
    T query(int 1, int r){
         // 0-base [1, r)
int wh = lg[r-l], len=1<<wh;</pre>
         return cmp (table[wh][1], table[wh][r-len]);
    }
};
```

2.10 FenwickTree

```
#include <vector>
using std::vector;

template<typename T>
class BIT{
    #define ALL(x) begin(x), end(x)
private:
    vector<T> arr;
    int n;
    inline int lowbit(int x){return x & (-x);}
    T query(int x){
        T ret = 0;
        while(x > 0) {
            ret += arr[x];
            x -= lowbit(x);
        }
        return ret;
}
```

```
public:
    void init(int n ) {
        n = n ;
        arr.resize(n);
        fill(arr.begin(), arr.end(), 0);
    void modify(int pos, T v) {
        while (pos < n) {</pre>
             arr[pos] += v;
             pos += lowbit(pos);
    T query(int 1, int r) {
    // 1-base (1, r]
        return query(r) - query(l);
#undef ALL
};
template<typename T>
class BIT{
#define ALL(x) begin(x), end(x)
private:
    vector<T> arr;
    inline int lowbit(int x) {return x & (-x);}
    void add(int s, int v) {
        while(s){
            arr[s]+=v;
             s-=lowbit(s);
public:
    void init(int n ) {
        n = n ;
        arr.resize(n);
        fill(ALL(arr), 0);
    void add(int 1, int r, T v) {
        //1-base (1, r]
        add(l, -v);
        add(r, v);
    T query(int x) {
        T r=0;
        while (x<size) {
            r+=arr[x];
             x+=lowbit(x);
        return r;
#undef ALL
} :
```

3 Graph

3.1 BCC Edge

```
class BCC{
private:
    vector<int> low, dfn;
    int cnt;
    vector<bool> bcc;
    vector<vector<PII>> G;
    void dfs(int w, int f){
        dfn[w] = cnt++;
        low[w] = dfn[w];
        for(auto i: G[w]){
            int u = i.FF, t = i.SS;
            if(u == f) continue;
            if (dfn[u]!=0) {
                low[w] = min(low[w], dfn[u]);
            }else{
                dfs(u, w);
                low[w] = min(low[w], low[u]);
                if(low[u] > dfn[w]) bcc[t] = true;
public:
    void init(int n, int m) {
        G.resize(n);
```

```
fill(G.begin(), G.end(), vector<PII>());
   bcc.clear(); bcc.resize(m);
   low.clear(); low.resize(n);
   dfn.clear(); dfn.resize(n);
   cnt = 0;
}

void add_edge(int u, int v){
   // should check for multiple edge
   G[u].PB({v, cnt});
   G[v].PB({u, cnt});
   cnt++;
}

void solve(){cnt = 1;dfs(0, 0);}
   // the id will be same as insert order, 0-base
bool is_bcc(int x){return bcc[x];}
} bcc;
```

3.2 BCC Vertex

```
class BCC{
private:
   vector<vector<pair<int,int>>> G;
    vector<int> dfn, low, id, sz;
    vector<bool> vis, ap;
    int n, ecnt, bcnt;
    void tarjan(int u, int f, int d) {
        vis[u] = true;
        dfn[u] = low[u] = d;
        int child = 0;
        for(auto e: G[u]) if(e.first != f){
            int v = e.first;
            if(vis[v]){
                low[u] = min(low[u], dfn[v]);
                 tarjan(v, u, d+1);
                 if(low[v] >= dfn[u]) ap[u] = true;
                low[u] = min(low[u], low[v]);
                child += 1;
        if(dfn[u] == 0 and child <= 1) ap[u] = false;</pre>
    void bfs bcc(int x) {
        // not sure
        queue<int> bfs;
        bfs.push(x); vis[x] = true;
        while(!bfs.empty()){
            int u = bfs.front(); bfs.pop();
            for(auto e: G[u]){
                id[e.second] = bcnt;
                if(ap[e.first] or vis[e.first])
                     continue;
                bfs.push(e.first); vis[e.first] = true;
                sz[bcnt] += 1;
        }
public:
    void init(int n ) {
        n = n ; G.clear(); G.resize(n);
        dfn.resize(n); low.resize(n);
        vis.clear(); vis.resize(n);
        ap.clear(); ap.resize(n);
        ecnt = 0, bcnt = 0;
    void add edge(int u, int v) {
        assert (0 \le u \text{ and } u \le n);
        assert(0 \leq v and v \leq n);
        G[u].emplace back(v, ecnt);
        G[v].emplace back(u, ecnt);
        ecnt += 1;
    void solve(){
        for(int i=0;i<n;i++) if(!vis[i]) {</pre>
            tarjan(i, i, 0);
        id.resize(ecnt);
        vis.clear(); vis.resize(n);
        sz.clear(); sz.resize(n);
        for(int i=0;i<n;i++) if(ap[i]){</pre>
            bfs bcc(i); bcnt += 1;
    bool isAP(int x){return ap[x];}
```

```
int count() {return bcnt;}
// bcc_id of edges by insert order (0-base)
int get_id(int x) {return id[x];}
// bcc size by bcc_id
int get_size(int x) {return sz[x];}
} bcc;
```

3.3 Strongly Connected Components

```
class SCC{
private:
    int n, num ;
    vector<vector<int>> G, rG;
    vector<int> ord, num;
    bool vis[N];
    void dfs(int u){
        if(vis[u]) return;
        vis[u]=1;
        for(auto v: G[u]) dfs(v);
        ord.PB(u);
    void rdfs(int u) {
        if(vis[u]) return;
        num[u] = num;
        vis[u] = 1;
        for(auto v: rG[u]) rdfs(v);
public:
    inline void init(int n ) {
        G.resize(n); rG.resize(n);
        n=n_, num_=0;
        num.resize(n);
        for(int i=0;i<n;i++) G[i].clear();</pre>
        for(int i=0;i<n;i++) rG[i].clear();</pre>
    inline void add edge(int st, int ed) {
        G[st].PB(ed);
        rG[ed].PB(st);
    void solve(){
        memset(vis, 0, sizeof(vis));
        for (int i=0;i<n;i++) {</pre>
            if(!vis[i]) dfs(i);
        reverse (ALL (ord));
        memset(vis, 0, sizeof(vis));
        for(auto i: ord) {
            if(!vis[i]){
                 rdfs(i);
                 num ++;
    inline int get_id(int x) {return num[x];}
    inline int count() {return num ;}
} scc;
```

3.4 Bipartie Matching

```
#include <bits/stdc++.h>
using namespace std;
#define N 500
class BipartieMatching{
 private:
    vector < int > X[N], Y[N];
    int fX[N], fY[N], n;
    bitset<N> walked;
    bool dfs(int x) {
      for(auto i:X[x]){
        if (walked[i]) continue;
        walked[i]=1;
        if (fY[i] ==-1||dfs(fY[i])) {
          fY[i]=x; fX[x]=i;
          return 1;
        }
      return 0;
 public:
    void init(int _n) {
      n=_n;
```

```
for (int i=0;i<n;i++) {</pre>
        X[i].clear();
         Y[i].clear());
        fX[i] = fY[i] = -1;
      walked.reset();
    void AddEdge(int x, int y) {
      X[x].push back(y);
      Y[y].push back(y);
    int solve(){
      int cnt = 0;
      for (int i=0;i<n;i++) {</pre>
        walked.reset();
        if(dfs(i)) cnt++;
       // return how many pair matched
      return cnt;
};
```

3.5 MinimumCostMaximumFlow

```
class MiniCostMaxiFlow{
    typedef int CapT;
    typedef lld WeiT;
    typedef pair<CapT, WeiT> PCW;
    const CapT INF CAP = 1<<30;</pre>
    const WeiT INF WEI = 1LL<<60;</pre>
    const int MAXV = N;
private:
    struct Edge{
        int to, back;
        WeiT wei;
        CapT cap;
        Edge () { }
        Edge(int a, int b, WeiT c, CapT d): to(a), back
             (b), wei(c), cap(d) {}
    int ori, edd, V;
    vector<Edge> G[MAXV];
    int fa[MAXV], wh[MAXV];
    bool inq[MAXV];
    WeiT dis[MAXV];
    PCW SPFA(){
        for (int i=0;i<V;i++) inq[i]=0;</pre>
         for(int i=0;i<V;i++) dis[i]=INF WEI;</pre>
        queue<int> qq;
        qq.push(ori);
        dis[ori]=0;
        while(!qq.empty()){
             int u = qq.front(); qq.pop();
             inq[u]=0;
             for (int i=0;i<SZ(G[u]);i++) {</pre>
                 Edge e = G[u][i];
                 int v = e.to;
                 WeiT d = e.wei;
                 if(e.cap > 0 \text{ and } dis[v] > dis[u]+d){
                     dis[v]=dis[u]+d;
                     fa[v]=u;
                     wh[v] = i;
                     if(inq[v]) continue;
                     qq.push(v);
                     inq[v]=1;
                 }
             }
        if(dis[edd] == INF WEI) return {-1, -1};
        CapT mw=INF CAP;
         for(int i=edd;i!=ori;i=fa[i]){
             mw = min(mw, G[fa[i]][wh[i]].cap);
         for(int i=edd;i!=ori;i=fa[i]){
             auto &eg = G[fa[i]][wh[i]];
             eg.cap -= mw;
             G[eg.to][eg.back].cap += mw;
        return {mw, dis[edd]};
public:
    void init(int a, int b, int n=MAXV) {
        V=n;
        ori = a:
```

```
edd = b;
    for(int i=0;i<n;i++) G[i].clear();
}
void addEdge(int st, int ed, WeiT w, CapT c) {
    G[st].PB(Edge(ed, SZ(G[ed]), w, c));
    G[ed].PB(Edge(st, SZ(G[st])-1, -w, 0));
}
PCW solve() {
    CapT cc=0; WeiT ww=0;
    while(true) {
        PCW ret = SPFA();
        if(ret.FF==-1) break;
        cc += ret.FF;
        ww += ret.SS;
    }
    return {cc, ww};
}
mcmf;</pre>
```

3.6 MaximumFlow

```
class Dinic{
private:
    using CapT = int64 t;
    struct Edge{
        int to, rev;
         CapT cap;
    int n, st, ed;
    vector<vector<Edge>> G;
    vector<int> lv;
    bool BFS() {
         fill(lv.begin(), lv.end(), -1);
         queue<int> bfs;
         bfs.push(st);
         lv[st] = 0;
         while(!bfs.empty()){
              int u = bfs.front(); bfs.pop();
              for(auto e: G[u]) {
                  if(e.cap <= 0 or lv[e.to]!=-1) continue</pre>
                   lv[e.to] = lv[u] + 1;
                  bfs.push(e.to);
         return (lv[ed]!=-1);
    CapT DFS(int u, CapT f) {
         if(u == ed) return f;
         CapT ret = 0;
         for(auto& e: G[u]){
             if(e.cap <= 0 or lv[e.to]!=lv[u]+1)
                 continue;
              CapT nf = DFS(e.to, min(f, e.cap));
              ret += nf; e.cap -= nf; f -= nf;
              G[e.to][e.rev].cap += nf;
              if(f == 0) return ret;
         if(ret == 0) lv[u] = -1;
         return ret;
public:
    void init(int n_, int st_, int ed_) {
    n = n_, st = st_, ed = ed_;
    G.resize(n); lv.resize(n);
         fill(G.begin(), G.end(), vector<Edge>());
    void add_edge(int u, int v, CapT c){
    G[u].push_back({v, (int)(G[v].size()), c});
    G[v].push_back({u, (int)(G[u].size())-1, 0});
    CapT max flow(){
         CapT ret = 0;
         while (BFS()) {
             CapT f = DFS(st, numeric limits<CapT>::max
                  ());
              ret += f;
             if(f == 0) break;
         return ret;
} flow;
```

3.7 Kuhn Munkres

```
struct KM{
 // Maximum Bipartite Weighted Matching (Perfect Match)
   static const int MXN = 650;
   static const int INF = 2147483647; // LL
   int n, match[MXN], vx[MXN], vy[MXN];
   int edge[MXN][MXN], lx[MXN], ly[MXN], slack[MXN];
      ^^^^ LL
  void init(int _n) {
    n = _n;
     for(int i=0; i<n; i++) for(int j=0; j<n; j++)</pre>
       edge[i][j] = 0;
  \{ edge[x][y] = w; \}
  bool DFS(int x) {
     vx[x] = 1;
     for (int y=0; y<n; y++) {</pre>
       if (vy[y]) continue;
       if (lx[x]+ly[y] > edge[x][y]){
         slack[y]=min(slack[y], lx[x]+ly[y]-edge[x][y]);
         vy[y] = 1;
         if (match[y] == -1 || DFS(match[y]))
         { match[y] = x; return true; }
    return false;
  int solve(){
     fill(match, match+n, -1);
     fill(lx, lx+n, -INF); fill(ly, ly+n, 0);
     for (int i=0; i<n; i++)</pre>
       for (int j=0; j<n; j++)</pre>
         lx[i] = max(lx[i], edge[i][j]);
     for (int i=0; i<n; i++) {</pre>
       fill(slack, slack+n, INF);
       while (true) {
         fill(vx, vx+n, 0); fill(vy, vy+n, 0);
         if ( DFS(i) ) break;
int d = INF; // long long
         for (int j=0; j<n; j++)</pre>
           if (!vy[j]) d = min(d, slack[j]);
         for (int j=0; j<n; j++) {</pre>
           if (vx[j]) lx[j] -= d;
if (vy[j]) ly[j] += d;
           else slack[j] -= d;
       }
     int res=0;
     for (int i=0; i<n; i++)</pre>
      res += edge[match[i]][i];
     return res;
}graph;
```

3.8 2-SAT

```
// 2-SAT solver based on Kosaraju's algorithm.
// Variables are 0-based. Positive variables are stored
     in vertices 2n, corresponding negative variables
    in 2n+1
// TODO: This is quite slow (3x-4x slower than Gabow's
   algorithm)
struct TwoSat {
  int n;
  vector<vector<int> > adj, radj, scc;
  vector<int> sid, vis, val;
  stack<int> stk;
  int scnt;
  // n: number of variables, including negations
  TwoSat(int n): n(n), adj(n), radj(n), sid(n), vis(n),
       val(n, -1) \{ \}
  // adds an implication
  void impl(int x, int y) { adj[x].push_back(y); radj[y
      ].push back(x); }
     adds a disjunction
  void vee(int x, int y) { impl(x^1, y); impl(y^1, x);
      }
```

```
// forces variables to be equal
  void eq(int x, int y) { impl(x, y); impl(y, x); impl(
      x^1, y^1; impl(y^1, x^1); }
   // forces variable to be true
  void tru(int x) { impl(x^1, x); }
  void dfs1(int x) {
    if (vis[x]++) return;
    for (int i = 0; i < adj[x].size(); i++) {</pre>
      dfs1(adj[x][i]);
    stk.push(x);
  void dfs2(int x) {
    if (!vis[x]) return; vis[x] = 0;
    sid[x] = scnt; scc.back().push back(x);
    for (int i = 0; i < radj[x].size(); i++) {</pre>
      dfs2(radj[x][i]);
  // returns true if satisfiable, false otherwise
  // on completion, val[x] is the assigned value of
       variable x
     note, val[x] = 0 implies val[x^1] = 1
  bool two sat() {
    scnt = 0;
    for (int i = 0; i < n; i++) {</pre>
      dfs1(i);
    while (!stk.empty()) {
      int v = stk.top(); stk.pop();
      if (vis[v]) {
        scc.push back(vector<int>());
        dfs2(v);
        scnt++;
      }
     for (int i = 0; i < n; i += 2) {</pre>
      if (sid[i] == sid[i+1]) return false;
    vector<int> must(scnt);
    for (int i = 0; i < scnt; i++) {</pre>
      for (int j = 0; j < scc[i].size(); j++) {</pre>
         val[scc[i][j]] = must[i];
        must[sid[scc[i][j]^1]] = !must[i];
      }
    return true;
};
```

3.9 HeavyLightDecomp

```
#define REP(i, s, e) for(int i = (s); i <= (e); i++)
#define REPD(i, s, e) for(int i = (s); i \ge (e); i - -)
const int MAXN = 100010;
const int LOG = 19;
struct HLD{
 int n;
  vector<int> g[MAXN];
 int sz[MAXN], dep[MAXN];
  int ts, tid[MAXN], tdi[MAXN], tl[MAXN], tr[MAXN];
    ts : timestamp , useless after yutruli
tid[ u ] : pos. of node u in the seq.
     tdi[i]: node at pos i of the seq.
      tl , tr[ u ] : subtree interval in the seq. of
      node u
  int prt[MAXN][LOG], head[MAXN];
  // head[ u ] : head of the chain contains u
  void dfssz(int u, int p) {
    dep[u] = dep[p] + 1;
    prt[u][0] = p; sz[u] = 1; head[u] = u;
    for (int& v:g[u]) if (v != p) {
      dep[v] = dep[u] + 1;
      dfssz(v, u);
      sz[u] += sz[v];
  void dfshl(int u){
    tid[u] = tl[u] = tr[u] = ts;
    tdi[tid[u]] = u;
```

```
sort (ALL (a[u]),
         [&] (int a, int b) {return sz[a] > sz[b];});
    bool flag = 1;
    for(int& v:g[u]) if(v != prt[u][0]){
     if(flag) head[v] = head[u], flag = 0;
      dfshl(v);
      tr[u] = tr[v];
    }
  inline int lca(int a, int b) {
    if(dep[a] > dep[b]) swap(a, b);
    int diff = dep[b] - dep[a];
    REPD(k, LOG-1, 0) if(diff & (1 << k)) {
      b = prt[b][k];
    if(a == b) return a;
    REPD(k, LOG-1, 0) if(prt[a][k] != prt[b][k]){
     a = prt[a][k]; b = prt[b][k];
    return prt[a][0];
  void init( int _n ){
    n = _n; REP( i , 1 , n ) g[ i ].clear();
  void addEdge( int u , int v ) {
    g[ u ].push back( v );
    g[v].push_back(u);
  void yutruli(){
    dfssz(1, 0);
    t.s = 0:
    dfshl(1);
    REP(k, 1, LOG-1) REP(i, 1, n)
      prt[i][k] = prt[prt[i][k-1]][k-1];
  vector< PII > getPath( int u , int v ) {
    vector< PII > res;
    while( tid[ u ] < tid[ head[ v ] ] ){</pre>
      res.push_back( PII(tid[ head[ v ] ] , tid[ v ]) )
      v = prt[ head[ v ] ][ 0 ];
    res.push back( PII( tid[ u ] , tid[ v ] ) );
    reverse ( ALL ( res ) );
    return res;
    /* res : list of intervals from u to v
     * u must be ancestor of v
     * usage :
     * vector< PII >& path = tree.getPath( u , v )
     * for( PII tp : path ) {
         int 1 , r; tie(1 , r) = tp;
         upd(1,r);
         uu = tree.tdi[ 1 ] , vv = tree.tdi[ r ];
         uu ~> vv is a heavy path on tree
} tree;
```

4 Math

4.1 Prime Table

```
// 10000000000 < primes < 2147483647
1002939109, 1020288887, 1028798297, 1038684299,
1041211027, 1051762951, 1058585963, 1063020809, 1094763083, 1106384353, 1120154459, 1140593173,
1147930723, 1172520109, 1183835981, 1187659051,
1241251303, 1247184097, 1255940849, 1272759031,
1287027493, 1288511629, 1294632499, 1312650799,
1314753281, 1320080669, 1321970357, 1333133947,
1337684419, 1353508067, 1358715989, 1364961029,
1366046831, 1376536367, 1381705499, 1410637769,
1411311571, 1422795043, 1437499801, 1495803851,
1511764363, 1526710979, 1538018089, 1542373769,
1545326953, 1549429633, 1556212739, 1575971759, 1586465261, 1608336427, 1609783001, 1620728569,
1643267081, 1652401603, 1656717203, 1660920671,
1666858577, 1669260361, 1670240317, 1678791131,
1685583143, 1725964619, 1734856421, 1743134179,
1761537223, 1774260193, 1778872889, 1781930609, 1803000149, 1814256623, 1834876331, 1839154463,
```

```
| 1840044389, 1843241713, 1856039431, 1868564531, 1868732623, 1884198443, 1884616807, 1885059541, 1909942399, 1914471137, 1923951707, 1925453197, 1937719153, 1954649041, 1958915237, 1970709803, 1979612177, 1980446837, 1989761941, 2007826547, 2008033571, 2011186739, 2039465081, 2039728567, 2093735719, 2116097521, 2123852629, 2140170259

// 2147483647 < primes < 400000000

3148478261, 3153064147, 3176351071, 3187523093, 3196772239, 3201312913, 3203063977, 3204840059, 3210224309, 3213032591, 3217689851, 3218469083, 3219857533, 3231880427, 3235951699, 3273767923, 3276188869, 3277183181, 3282463507, 3285553889, 3319309027, 3327005333, 3327574903, 3341387953, 3373293941, 3380077549, 3380892997, 3381118801, 3384716479, 3386991323
```

4.2 ax+by=gcd

```
// By Adrien1018 (not knowing how to use.
// ax+ny = 1, ax+ny == ax == 1 (mod n)
tuple<int, int, int> extended_gcd(int a, int b) {
    if (!b) return make_tuple(a, 1, 0);
    int d, x, y;
    tie(d, x, y) = extended_gcd(b, a % b);
    return make_tuple(d, y, x - (a / b) * y);
}
// ax+by = gcd (by Eddy1021
PII gcd(int a, int b) {
    if(b == 0) return {1, 0};
    PII q = gcd(b, a % b);
    return {q.second, q.first - q.second * (a / b)};
}
```

4.3 Pollard Rho

```
// coded by hanhanW
// does not work when n is prime
long long modit(long long x,long long mod) {
    if (x \ge mod) x = mod;
    //if(x<0) x+=mod;
    return x;
long long mult(long long x,long long y,long long mod) {
    long long s=0, m=x%mod;
    while(y) {
        if(v&1) s=modit(s+m, mod);
        v>>=1:
        m=modit(m+m, mod);
   return s;
long long f(long long x,long long mod) {
   return modit(mult(x,x,mod)+1,mod);
long long pollard rho(long long n) {
    if(!(n&1)) return 2;
    while (true) {
        long long y=2, x=rand()%(n-1)+1, res=1;
        for (int sz=2; res==1; sz*=2) {
            for (int i=0; i<sz && res<=1; i++) {</pre>
                x = f(x, n);
                res = \_gcd(abs(x-y), n);
        if (res!=0 && res!=n) return res;
```

4.4 Pi Count (Linear Sieve)

```
static constexpr int N = 1000000 + 5;
lld pi[N];
vector<int> primes;
```

```
bool sieved[N];
lld cube_root(lld x) {
  lld s = static_cast<lld>(cbrt(x - static_cast<long</pre>
      double>(0.1)));
  while(s*s*s <= x) ++s;</pre>
  return s-1;
lld square root(lld x) {
  1ld s = static_cast<lld>(sqrt(x - static_cast<long</pre>
      double > (0.1)));
  while (s*s <= x) ++s;
  return s-1;
void init(){
 primes.reserve(N);
  primes.push back(1);
  for (int i=2;i<N;i++) {</pre>
    if(!sieved[i]) primes.push_back(i);
    pi[i] = !sieved[i] + pi[i-1];
    for(int p: primes) if(p > 1) {
      if(p * i >= N) break;
      sieved[p * i] = true;
      if(p % i == 0) break;
lld phi(lld m, lld n) {
  static constexpr int MM = 80000, NN = 500;
  static lld val[MM][NN];
  if(m < MM and n < NN and val[m][n]) return val[m][n]</pre>
      - 1;
  if(n == 0) return m;
  if(primes[n] >= m) return 1;
  lld ret = phi(m, n - 1) - phi(m / primes[n], n - 1);
  if(m < MM and n < NN) val[m][n] = ret + 1;</pre>
  return ret;
lld pi_count(lld);
11d P2(11d m, 11d n) {
  lld sm = square_root(m), ret = 0;
  for(lld i = n+1;primes[i] <= sm; i++)</pre>
    ret += pi count(m / primes[i]) - pi count(primes[i
        1) + \overline{1};
  return ret;
lld pi count(lld m) {
  if(m < N) return pi[m];</pre>
  lld n = pi_count(cube_root(m));
  return phi(m, n) + n - 1 - P2(m, n);
```

4.5 NloglogN Sieve

```
void Sieve(int n) {
    for(int i=2;i<=n;i++) {
        if(notprime[i]) continue;
        primes.push_back(i);
        for(int j=i*i;j<=n;j+=i) notprime[i]=true;
    }
}</pre>
```

4.6 Range Sieve

4.7 Miller Rabin

```
lld modu(lld a, lld m) {
    while(a >= m) a -= m;
    return a:
lld mul(lld a, lld b, lld m) {
    if(a < b) swap(a, b);</pre>
    11d ret = 0:
    while(b){
        if(b & 1) ret = modu(ret+a, m);
        a = modu(a+a, m);
        b >>= 1;
    return ret;
lld qPow(lld a, lld k, lld m) {
   lld ret = 1;
    a %= m;
    while(k){
        if(k & 1) ret = mul(ret, a, m);
        a = mul(a, a, m);
        k >>= 1;
    return modu(ret, m);
bool witness(lld a, lld s, int t, lld n) {
   lld b = qPow(a, s, n);
    if(b == 0) return false;
    while(t--){
        lld bb = mul(b, b, n);
        if(bb == 1 and b != 1 and b != n-1) return true
        b = bb;
    return b != 1;
bool miller rabin(lld n) {
    if (n < \overline{2}) return false;
    if(!(n & 1)) return (n==2);
    11d x = n-1; int t = 0;
    while(!(x&1)) x >>= 1, t++;
    lld sprp[] =
        {2,325,9375,28178,450775,9780504,1795265022};
    for (int i=0;i<7;i++) {</pre>
        if (witness(sprp[i]%n, x, t, n)) return false;
    return true;
```

4.8 Inverse Element

```
// x's inverse mod k
// if k is prime
long long GetInv(long long x, long long k) {
    return qPow(x, k-2);
}

// x's inverse mod k
// if k is not prime
long long GetInv(long long x, long long k) {
    return qPow(x, Euler(k)-1);
}

// or extended_gcd(x, k).second
// if you need [1, x] (most use: [1, k-1]
void solve(int x, long long k) {
    inv[1] = 1;
    for(int i=2;i<x;i++)
        inv[i] = ((long long)(k - k/i) * inv[k % i]) %
        k;
}</pre>
```

4.9 Euler Phi Function

```
extended euler:
   a^b \mod p
   if gcd(a, p) ==1: a^(b%phi(p))
   elif b < phi(p): a^b mod p
   else a^(b%phi(p) + phi(p))
inline int64_t Euler(int x) {
    int64 t r=1;
    for (int i=2;i*i<=x;++i) {</pre>
        if (x%i==0) {
            x/=i;
             r*=(i-1);
             while (x\%i==0) {
                 x/=i;
                 r*=i;
        }
    if(x>1) r*=x-1;
    return r;
vector<int> primes;
bool notprime[N];
int64 t phi[N];
inline void euler sieve(int n) {
    for (int i=2;i<n;i++) {</pre>
        if(!notprime[i]){
             primes.push back(i);
             phi[i] = i-\overline{1};
         for(auto j: primes) {
             if(i*j >= n) break;
             notprime[i*j] = true;
             phi[i*j] = phi[i] * phi[j];
             if(i % j == 0){
                 phi[i*j] = phi[i] * j;
                 break;
         }
    }
```

4.10 Gauss Elimination

```
typedef long double llf;
const int N = 300;
const llf EPS = 1e-8;
  make m[i][i] = x, m[i][i] = 0
// v is for solving equation:
// for(int i=0;i< n;i++) ans[pos[i]] = val[i]/mtx[i][pos[i]]
// for(int i=0;i<n;i++) cout << ans[i] << '\n';
bool Gauss(llf m[N][N], llf v[N], int n, int pos[N]) {
    for (int i=0; i<n; i++) {</pre>
        int x=-1, y=-1; llf m = 0;
for(int j=i;j<n;j++) for(int k=i;k<n;k++) {</pre>
             if(fabs(m[j][pos[k]])>m){
                m = fabs(m[j][pos[k]]);
x = j, y = k;
             }
        if(x==-1 or y==-1) return false;
        swap(m[x], m[i]);
        swap(v[x], v[i]);
        swap(pos[y], pos[i]);
        for (int j=i+1; j<n; j++) {</pre>
             llf xi = m[j][pos[i]]/m[i][pos[i]];
             for (int k=0; k<n; k++) m[j][pos[k]] -= xi*m[i</pre>
                 ][pos[k]];
             v[j] = xi*v[i];
        }
    for (int i=n-1;i>=0;i--) {
        for (int j=i-1; j>=0; j--) {
             llf xi = m[j][pos[i]]/m[i][pos[i]];
             ][pos[k]];
             v[j] = xi*v[i];
    return true;
```

4.11 Fast Fourier Transform

| }

```
polynomial multiply:
   FFT(a, N, true);
   FFT(b, N, true);
   for(int i=0;i<MAXN;i++) c[i] = a[i]*b[i];
  FFT(c, N, false);
  yeah~ go result in c
   (N must be 2^k and >= len(a) + len(b))
typedef long double llf;
typedef complex<llf> cplx;
const int MAXN = 262144;
const llf PI = acos((llf)-1);
cplx A[MAXN], B[MAXN], C[MAXN], omega[MAXN+1];
void init_omega(){
    const cplx I = {0, 1};
    for(int i=0;i<=MAXN;i++) omega[i] = exp(i*2*PI/MAXN</pre>
        *I);
void FFT(cplx arr[], int n, bool ori){
    // n must be 2^k
    int theta = MAXN / n;
    for(int len=n;len>=2;len>>=1) {
        int tot = len>>1;
        for (int i=0;i<tot;i++) {</pre>
            cplx omg = omega[ori?i*theta%MAXN:MAXN-(i*
                theta%MAXN)];
             for(int j=i;j<n;j+=len) {</pre>
                int k = j+tot;
cplx x = arr[j] - arr[k];
                 arr[j] += arr[k];
                 arr[k] = omg * x;
        theta = (theta * 2) % MAXN;
    int i = 0;
    for (int j=1; j<n-1; j++) {</pre>
        for (int k=n>>1; k> (i^=k); k>>=1);
        if(j < i) swap(arr[j], arr[i]);</pre>
    if(ori) return;
    for (int i=0;i<n;i++) arr[i] /= n;</pre>
```

4.12 Chinese Remainder

```
// ax+ny = 1, ax+ny == ax == 1 \pmod{n}
pair<lld, lld> exgcd(lld a, lld b) {
   if(b == 0) return {1, 0};
    pair<lld,lld> q = gcd(b, a % b);
    return {q.second, q.first - q.second * (a / b)};
lld crt(lld ans[], lld pri[], int n) {
    11d M = 1;
    for (int i=0;i<n;i++) M *= pri[i];</pre>
    11d ret = 0;
    for (int i=0;i<n;i++) {</pre>
       lld inv = (gcd(M/pri[i], pri[i]).first + pri[i
            ])%pri[i];
        ret += (ans[i] * (M/pri[i]) %M * inv) %M;
        ret %= M;
   return ret;
}
Another:
x = a1 % m1
x = a2 % m2
g = gcd(m1, m2)
assert((a1-a2) %g==0)
[p, q] = exgcd(m2/g, m1/g)
return a2+m2*(p*(a1-a2)/g)
```

4.13 NTT

```
\mbox{typedef long long $L$L};
// Remember coefficient are mod P
/* p=a*2^n+1
       2^n
                    Ø
                                    root
        32
                   97
   6
        64
                    193
                               3
                    257
       128
                               2
                    257
       256
                               7
   9
        512
                    7681
                               15
                                    17
  10 1024
                   12289
                               12
                                    11
       2048
                    12289
   11
                               6
                                    11
   12
       4096
                    12289
                               3
                                    11
       8192
   13
                    40961
                               .5
        16384
                    65537
   14
                               4
   15
       32768
                    65537
                               2
   16
       65536
                    65537
                               1
       131072
                    786433
   17
                                    10
                               6
   18
       262144
                    786433
                                    10 (605028353,
       2308, 3)
                   5767169
                               11
   20
       1048576
                    7340033
                                    3
                   23068673
                              11
       2097152
   21
   22
       4194304
                   104857601 25
   23
       8388608
                   167772161
                               20
       16777216
                   167772161 10
   25
        33554432
                    167772161 5
                                    3 (1107296257, 33,
       10)
       67108864
   26
                    469762049 7
                   2013265921 15
   27
       134217728
                                    31 */
// (must be 2^k)
// To implement poly. multiply:
// NTT<P, root, MAXN> ntt;
// ntt( n , a ); // or ntt.tran( n , a );
// ntt( n , b );
// for( int i = 0 ; i < n ; i++ )
   c[i] = a[i] * b[i];
// ntt(n,c,1);
//
// then you have the result in c :: [LL]
template<LL P, LL root, int MAXN>
struct NTT{
   static LL bigmod(LL a, LL b) {
       LL res = 1;
        for (LL bs = a; b; b >>= 1, bs = (bs * bs) % P)
            if(b&1) res=(res*bs)%P;
        1
        return res;
    static LL inv(LL a, LL b) {
       if(a==1)return 1;
        return (((LL) (a-inv(b%a,a))*b+1)/a)%b;
   LL omega[MAXN+1];
   NTT() {
       omega[0] = 1;
        LL r = bigmod(root, (P-1)/MAXN);
        for (int i=1; i<=MAXN; i++)</pre>
           omega[i] = (omega[i-1]*r)%P;
    // n must be 2^k
    void tran(int n, LL a[], bool inv_ntt=false) {
       int basic = MAXN / n;
        int theta = basic;
        for (int m = n; m >= 2; m >>= 1) {
           int mh = m >> 1;
            for (int i = 0; i < mh; i++) {</pre>
                LL w = omega[i*theta%MAXN];
                for (int j = i; j < n; j += m) {</pre>
                    int k = j + mh;
                    LL x = a[j] - a[k];
                    if (x < 0) x += P;
                    a[j] += a[k];
                    if (a[j] > P) a[j] -= P;
                    a[k] = (w * x) % P;
            theta = (theta * 2) % MAXN;
        int i = 0;
        for (int j = 1; j < n - 1; j++) {
            for (int k = n >> 1; k > (i ^= k); k >>= 1)
```

```
if (j < i) swap(a[i], a[j]);

if (inv_ntt) {
    LL ni = inv(n,P);
    reverse( a+1 , a+n );
    for (i = 0; i < n; i++)
        a[i] = (a[i] * ni) % P;

}

void operator() (int n, LL a[], bool inv_ntt=false)
    {
    tran(n, a, inv_ntt);
}

;

const LL P=2013265921, root=31;
const int MAXN=4194304;
NTT<P, root, MAXN> ntt;
```

4.14 DiscreteLog

```
// Baby-step Giant-step Algorithm
// a x + by = g
void exgcd(long long x, long long y, long long &g,
    long long &a, long long &b) {
    if (y == 0)
         g = x, a = 1, b = 0;
    else
         exgcd(y, x%y, g, b, a), b = (x/y) * a;
long long inverse(long long x, long long p) {
   long long g, b, r;
    exgcd(x, p, g, r, b);
if (g < 0) r = -r;
    return (r%p + p)%p;
long long BSGS(long long P, long long B, long long N) {
    // find B^L = N \mod P
    unordered map<long long, int> R;
    long long sq = (long long) sqrt(P);
    long long t = 1, f;
for (int i = 0; i < sq; i++) {</pre>
        if (t == N)
              return i;
         if (!R.count(t))
             R[t] = i;
         t = (t * B) % P;
    f = inverse(t, P);
    for (int i = 0; i <= sq+1; i++) {</pre>
         if (R.count(N))
    return i * sq + R[N];
         N = (N * f) % P;
    return -1;
```

5 Geometry

5.1 Point Class

```
template<typename T>
struct Point{
    typedef long double llf;
    static constexpr llf EPS = 1e-8;
    T x, y;
    Point(T _=0, T _=0): x(_), y(__){}
    template<typename T2>
        Point(const Point<T2>& a): x(a.x), y(a.y){}
    inline llf theta() const {
        return atan2((llf)y, (llf)x);
    }
    inline llf dis() const {
        return hypot((llf)x, (llf)y);
    }
    inline llf dis(const Point& o) const {
        return hypot((llf)(x-o.x), (llf)(y-o.y));
    }
    Point operator-(const Point& o) const {
```

```
return Point(x-o.x, y-o.y);
    Point operator = (const Point& o) {
        x-=o.x, y-=o.y;
        return *this;
    Point operator+(const Point& o) const {
        return Point(x+o.x, y+o.y);
    Point operator+=(const Point& o) {
        x+=o.x, y+=o.y;
return *this;
    Point operator* (const T& k) const {
        return Point(x*k, y*k);
    Point operator*=(const T& k) {
        x*=k, y*=k;
        return *this;
    Point operator/(const T& k) const {
        return Point(x/k, y/k);
    Point operator/=(const T& k) {
       x/=k, y/=k;
        return *this;
    Point operator-() const {
        return Point(-x, -y);
    Point rot90() const {
       return Point(-y, x);
    template<typename T2>
    bool in (const Circle<T2>& a) const {
        /* Add struct Circle at top */
      return a.o.dis(*this)+EPS <= a.r;</pre>
    bool equal(const Point& o, true_type) const {
        return fabs(x-o.x) < EPS and fabs(y-o.y) < EPS;
    bool equal(const Point& o, false_type) const {
        return tie(x, y) == tie(o.x, o.y);
    bool operator==(const Point& o) const {
        return equal(o, is floating point<T>());
    bool operator!=(const Point& o) const {
        return ! (*this == 0);
    bool operator<(const Point& o) const {</pre>
       return theta() < o.theta();</pre>
        // sort like what pairs did
        // if(is floating_point<T>()) return fabs(x-o.x
             ) <EPS?y<o.y:x<o.x;
        // else return tie(x, y) < tie(o.x, o.y);
    friend inline T cross(const Point& a, const Point&
        b) {
        return a.x*b.y - b.x*a.y;
    friend inline T dot(const Point& a, const Point &b)
        return a.x*b.x + a.y*b.y;
    friend ostream& operator<<(ostream& ss, const Point</pre>
        & 0){
        ss<<"("<<o.x<<", "<<o.y<<")";
        return ss;
    }
};
```

5.2 Circle Class

5.3 Line Class

```
const Point<long double> INF P(-1e20, 1e20);
const Point<long double> NOT EXIST(1e20, 1e-20);
template<typename T>
struct Line{
   static constexpr long double EPS = 1e-8;
    // ax+by+c = 0
    T a, b, c;
    Line(): a(0), b(1), c(0){}
Line(T _, T __, T ___): a(_), b(__), c(___){
        assert(fabs(a)>EPS or fabs(b)>EPS);
    template<typename T2>
      Line(const Line<T2>& x): a(x.a), b(x.b), c(x.c){}
    typedef Point<long double> Pt;
    bool equal(const Line& o, true_type) const {
        return fabs(a-o.a) < EPS and fabs(b-o.b) < EPS
             and fabs(c-o.b) < EPS;</pre>
    bool euqal(const Line& o, false type) const {
        return a==o.a and b==o.b and c==o.c;
    bool operator==(const Line& o) const {
        return euqal(o, is floating point<T>());
    bool operator!=(const Line& o) const {
        return ! (*this == 0);
    friend inline bool on_line__(const Point<T>& p,
        const Line& 1, true_type) {
        return fabs(1.a*p.x + 1.b*p.y + 1.c) < EPS;
    friend inline bool on line (const Point<T>& p,
        const Line& 1, false_type) {
return l.a*p.x + l.b*p.y + l.c == 0;
    friend inline bool on line(const Point<T>&p const
        Line& 1) {
        return on_line__(p, l, is_floating_point<T>());
    friend inline bool is parallel (const Line& x,
        const Line& y, true_type) {
        return fabs(x.a*y.b - x.b*y.a) < EPS;</pre>
    friend inline bool is_parallel__(const Line& x,
        const Line& y, false_type) {
        return x.a*y.b == x.b*y.a;
    friend inline bool is parallel(const Line& x, const
         Line& y) {
        return is_parallel__(x, y, is_floating_point<T</pre>
             >());
    friend inline Pt get inter(const Line& x, const
        Line& y) {
        typedef long double llf;
if(x==y) return INF_P;
        if(is parallel(x, y)) return NOT EXIST;
        llf delta = x.a*y.b - x.b*y.a;
        llf delta x = x.b*y.c - x.c*y.b;
        llf delta_y = x.c*y.a - x.a*y.c;
return Pt(delta_x / delta, delta_y / delta);
    friend ostream& operator<<(ostream& ss, const Line&</pre>
        ss<<o.a<<"x+"<<o.b<<"y+"<<o.c<<"=0";
        return ss;
    }
template<typename T>
inline Line<T> get_line(const Point<T>& a, const Point<</pre>
    T>& b) {
```

```
return Line<T>(a.y-b.y, b.x-a.x, (b.y-a.y)*a.x-(b.x
-a.x)*a.y);
}
```

5.4 Segment Class

```
const long double EPS = 1e-8;
template<typename T>
struct Segment{
    // p1.x < p2.x
   Line<T> base;
    Point<T> p1, p2;
    Segment(): base(LineT>()), p1(PointT>()), p2(
       Point<T>()) {
        assert(on_line(p1, base) and on_line(p2, base))
    {\tt assert} \, ({\tt on\_line} \, ({\tt p\overline{1,\;\; base}}) \,\, {\tt and} \,\, {\tt on\_line} \, ({\tt p2,\;\; base}) \,)
    template<typename T2>
      Segment(const Segment<T2>& _): base(_.base), p1(_
          .p1), p2(_.p2) {}
    typedef Point<long double> Pt;
    friend bool on segment(const Point<T>& p, const
        Segment& 1) {
        if(on line(p, l.base))
            return (1.p1.x-p.x) * (p.x-1.p2.x) >= 0 and (1.
               p1.y-p.y)*(p.y-1.p2.y)>=0;
        return false;
   friend bool have inter(const Segment& a, const
        Seament& b) {
        if(is_parallel(a.base, b.base)){
            return on_segment(a.p1, b) or on_segment(a.
                p2, b) or on segment(b.p1, a) or
                on segment(b.p2, a);
        Pt inter = get_inter(a.base, b.base);
        return on_segment(inter, a) and on_segment(
            inter, b);
    friend inline Pt get inter(const Segment& a, const
        Segment& b) {
        if(!have inter(a, b)){
            return NOT EXIST;
        }else if(is_parallel(a.base, b.base)){
           if(a.p1 == b.p1) {
                if (on segment (a.p2, b) or on segment (b.
                   p2, a)) return INF_P;
                else return a.p1;
            }else if(a.p1 == b.p2) {
                if(on_segment(a.p2, b) or on_segment(b.
                    p1, a)) return INF P;
                else return a.p1;
            }else if(a.p2 == b.p1) {
                if(on segment(a.pl, b) or on segment(b.
                    p2, a)) return INF P;
                else return a.p2;
            }else if(a.p2 == b.p2) {
                if(on_segment(a.pl, b) or on_segment(b.
                    pl, a)) return INF P;
                else return a.p2;
            return INF P;
        return get inter(a.base, b.base);
    friend ostream& operator<<(ostream& ss, const</pre>
        Segment& o) {
        ss<<o.base<<", "<<o.p1<<" ~ "<<o.p2;
        return ss;
template<typename T>
inline Segment<T> get segment(const Point<T>& a, const
    Point<T>& b) {
    return Segment<T>(get_line(a, b), a, b);
```

5.5 Triangle Circumcentre

5.6 2D Convex Hull

```
template<typename T>
class ConvexHull 2D{
private:
    typedef Point<T> PT;
    vector<PT> dots;
    struct myhash{
        uint64 t operator()(const PT& a) const {
            uint64_t xx=0, yy=0;
            memcpy(&xx, &a.x, sizeof(a.x));
            memcpy(&yy, &a.y, sizeof(a.y));
            uint64_t ret = xx*17+yy*31;
            ret = (ret ^ (ret >> 16))*0x9E3779B1;
            ret = (ret ^ (ret >> 13)) *0xC2B2AE35;
            ret = ret ^ xx;
            return (ret ^ (ret << 3)) * yy;</pre>
        }
    };
    unordered set<PT, myhash> in hull;
public:
    inline void init() {in hull.clear(); dots.clear();}
    void insert(const PT& x) {dots.PB(x);}
    void solve() {
        sort(ALL(dots), [](const PT& a, const PT& b){
          return tie(a.x, a.y) < tie(b.x, b.y);</pre>
        });
        vector<PT> stk(SZ(dots)<<1);</pre>
        int top = 0;
        for(auto p: dots) {
            while(top >= 2 and cross(p-stk[top-2], stk[
                top-1]-stk[top-2]) <= 0)
                top --;
            stk[top++] = p;
        for (int i=SZ(dots)-2, t = top+1;i>=0;i--) {
            while(top >= t and cross(dots[i]-stk[top
                 -2], stk[top-1]-stk[top-2]) <= 0)
                top --;
            stk[top++] = dots[i];
        stk.resize(top-1);
        swap(stk, dots);
        for(auto i: stk) in_hull.insert(i);
    vector<PT> get() {return dots;}
    inline bool in it(const PT& x){
        return in hull.find(x)!=in hull.end();
};
```

5.7 2D Farthest Pair

```
ans = max({ans, dis(stk[i], stk[pos]), dis(stk[i
+1], stk[pos])});
```

5.8 SimulateAnnealing

}

```
#include <random>
#include <functional>
#include <utilitv>
#include <algorithm>
using namespace std;
double getY(double);
int main(){
    int rr, 11;
    default random engine rEng(time(NULL));
    uniform_real_distribution<double> Range(-1,1);
    uniform real distribution < double > expR(0,1);
    auto Random=bind(Range, rEng), expRand=bind(expR,
    int step=0;
    double pace=rr-ll, mini=0.95; // need to search for
        it
    double x=max(min(Random()*pace+ll, rr), ll), y=getY
    while(pace>=1e-7){
        double newX = max(min(x + Random()*pace, rr),
            11);
        double newY = getY(newX);
        if(newY < y \mid \mid expRand() < exp(-step))
            x=newX, y=newY;
        step++;
        pace*=mini;
```

5.9 Ternary Search on Interger

```
int TernarySearch(int 1, int r) {
    // (1, r)
    while (r - 1 > 1) {
        int mid = (1 + r)>>1;
        if (f(mid) > f(mid + 1)) r = mid;
        else 1 = mid;
    }
    return 1+1;
```

5.10 Minimum Covering Circle

```
template<typename T>
Circle<llf> MinCircleCover(const vector<Point<T>>& pts)
    random shuffle(ALL(pts));
    Circle < llf > c = \{pts[0], 0\};
    int n = SZ(pts);
    for (int i=0;i<n;i++) {</pre>
        if(pts[i].in(c)) continue;
         c = \{pts[i], 0\};
        for (int j=0; j<i; j++) {</pre>
             if(pts[j].in(c)) continue;
             c.o = (pts[i] + pts[j]) / 2;
             c.r = pts[i].dis(c.o);
             for (int k=0; k<j; k++) {</pre>
                 if(pts[k].in(c)) continue;
                 c = get_circum(pts[i], pts[j], pts[k]);
         }
    return c;
```

5.11 KDTree (Nearest Point)

```
const int MXN = 100005;
struct KDTree {
   struct Node {
     int x,y,x1,y1,x2,y2;
     int id,f;
     Node *L, *R;
   }tree[MXN];
   int n;
   Node *root;
   LL dis2(int x1, int y1, int x2, int y2) {
     LL dx = x1-x2;
     LL dy = y1-y2;
     return dx*dx+dy*dy;
   static bool cmpx(Node& a, Node& b) { return a.x<b.x; }</pre>
   static bool cmpy(Node& a, Node& b) { return a.y<b.y; }</pre>
   void init(vector<pair<int,int>> ip) {
     n = ip.size();
     for (int i=0; i<n; i++) {</pre>
        tree[i].id = i;
        tree[i].x = ip[i].first;
tree[i].y = ip[i].second;
     root = build tree(0, n-1, 0);
   Node* build tree(int L, int R, int dep) {
     if (L>R) return nullptr;
     int M = (L+R)/2;
     tree[M].f = dep%2;
     nth element(tree+L, tree+M, tree+R+1, tree[M].f ?
          cmpy : cmpx);
     tree[M].x1 = tree[M].x2 = tree[M].x;
     tree[M].y1 = tree[M].y2 = tree[M].y;
     tree[M].L = build_tree(L, M-1, dep+1);
     if (tree[M].L) {
        tree[M].x1 = min(tree[M].x1, tree[M].L->x1);
        \label{eq:continuous} \begin{array}{lll} \texttt{tree}\,[\,M\,]\,\,.\,x\,2 &=& \texttt{max}\,(\,\texttt{tree}\,[\,M\,]\,\,.\,x\,2\,, & \texttt{tree}\,[\,M\,]\,\,.\,L\,-\,>\,x\,2\,)\,\,;\\ \texttt{tree}\,[\,M\,]\,\,.\,y\,1 &=& \texttt{min}\,(\,\texttt{tree}\,[\,M\,]\,\,.\,y\,1\,, & \texttt{tree}\,[\,M\,]\,\,.\,L\,-\,>\,y\,1\,)\,\,;\\ \end{array}
        tree[M].y2 = max(tree[M].y2, tree[M].L->y2);
     tree[M].R = build tree(M+1, R, dep+1);
     if (tree[M].R) {
        tree[M].x1 = min(tree[M].x1, tree[M].R->x1);
        tree[M].x2 = max(tree[M].x2, tree[M].R->x2);
tree[M].y1 = min(tree[M].y1, tree[M].R->y1);
tree[M].y2 = max(tree[M].y2, tree[M].R->y2);
     return tree+M;
   int touch(Node* r, int x, int y, LL d2){
     LL dis = sqrt(d2)+1;
     if (x<r->x1-dis || x>r->x2+dis ||
          y < r > y1-dis \mid \mid y>r > y2+dis)
        return 0;
     return 1;
   void nearest(Node* r, int x, int y,
                   int &mID, LL &md2) {
     if (!r || !touch(r, x, y, md2)) return;
     LL d2 = dis2(r->x, r->y, x, y);
     if (d2 < md2 || (d2 == md2 && mID < r->id)) {
       mTD = r -> id:
        md2 = d2:
      // search order depends on split dim
     if ((r->f == 0 \&\& x < r->x) | |
           (r->f == 1 && y < r->y))
        nearest(r->L, x, y, mID, md2);
        nearest(r->R, x, y, mID, md2);
     } else {
        nearest(r->R, x, y, mID, md2);
        nearest(r->L, x, y, mID, md2);
   int query(int x, int y) {
     int id = 1029384756;
     LL d2 = 102938475612345678LL;
     nearest(root, x, y, id, d2);
     return id;
}tree;
```

6 Stringology

6.1 Hash

```
const int N = 1000000;
class Hash{
private:
     const int p = 127, q = 1208220623;
     int sz, prefix[N], power[N];
     inline int add(int x, int y) {return x+y>=q?x+y-q:x+
         y; }
     inline int sub(int x, int y) {return x-y<0?x-y+q:x-y</pre>
     inline int mul(int x, int y) {return 1LL*x*y%q;}
public:
     void init(const std::string &x) {
         sz = x.size();
         prefix[0]=0;
         for(int i=1;i<=sz;i++) prefix[i]=add(mul(prefix</pre>
             [i-1], p), x[i-1]);
         power[0]=1;
         for (int i=1;i<=sz;i++) power[i]=mul(power[i-1],</pre>
     int query(int 1, int r) {
         // 1-base (1, r)
         return sub(prefix[r], mul(prefix[l], power[r-l
             ]));
};
```

6.2 Suffix Array

```
//help by http://www.geeksforgeeks.org/suffix-array-set
    -2-a-nlognlogn-algorithm/
#include <bits/stdc++.h>
using namespace std;
#define PB push back
struct sfx{
    int index;
    int r,nr;
char str[N + 10];
int len;
vector<sfx> srs[N + 10];
int mapping[N + 10];
sfx sa[N + 10];
bool cmp(sfx a,sfx b) {
   if(a.r==b.r){
        return a.nr<b.nr;</pre>
    }else{
        return a.r<b.r;</pre>
void SA();
void radixSort();
int main(){
   gets(str);
    len = strlen(str);
    SA():
    for(int i=0;i<len;i++) {</pre>
        printf("%d\n", sa[i].index);
    return 0;
}
void SA() {
    for (int i=0; i<len; i++) {</pre>
        sa[i].index = i;
         sa[i].r=str[i];
        sa[i].nr=(i+1>=len)?0:str[i+1];
    //sort(sa,sa+len,cmp);
    radixSort();
    for(int j=2;j<=len;j*=2) {</pre>
        int cnt=1;
```

```
int rr = sa[0].r;
        sa[0].r=cnt;
        mapping[sa[0].index]=0;
        for (int i=1;i<len;i++) {</pre>
            if(sa[i].r == rr && sa[i].nr == sa[i-1].nr)
                 rr=sa[i].r;
                 sa[i].r=cnt;
             }else{
                 rr=sa[i].r;
                 sa[i].r=++cnt;
            mapping[sa[i].index]=i;
        for (int i=0; i<len; i++) {</pre>
             int nn = sa[i].index+j;
             sa[i].nr = (nn>=len)?0:sa[mapping[nn]].r;
         //sort(sa, sa+len, cmp);
        radixSort();
void radixSort() {
    int m = 0;
    for (int i=0; i<len; i++) {</pre>
        srs[sa[i].nr].PB(sa[i]);
        m=max(m,sa[i].nr);
    int cnt=0;
    for (int i=0;i<=m;i++) {</pre>
        if(srs[i].empty())continue;
        for(auto j:srs[i]){
             sa[cnt++] = j;
        srs[i].clear();
    }
    m = 0;
    for (int i=0;i<len;i++) {</pre>
        srs[sa[i].r].PB(sa[i]);
        m=max(m,sa[i].r);
    cnt=0;
    for (int i=0;i<=m;i++) {</pre>
        if (srs[i].empty())continue;
        for(auto j:srs[i]){
            sa[cnt++] = i;
        srs[i].clear();
```

6.3 KMP

```
int F[N<<1];
void KMP(char s1[], char s2[], int n, int m) {
    // make F[] for s1+'\0'+s2;
    char ss[N<<1];
    int len = n+m+1;
    for(int i=0;i<n;i++) ss[i] = s1[i];
    ss[n] = '\0';
    for(int i=0;i<m;i++) ss[i+1+n] = s2[i];
    F[0] = F[1] = 0;
    for(int i=1;i<len;i++) {
        int j = F[i];
        while(j > 0 and ss[i]!=ss[j]) j = F[j];
        F[i+1] = (ss[i]==ss[j]?j+1:0);
    }
    // just find (F[len2+i] == len2), i from 1 to len+1
        for matching
}
```

6.4 Z value

```
char s[MAXN];
int len,z[MAXN];
void Z_value() {
  int i,j,left,right;
  left=right=0; z[0]=len;
  for(i=1;i<len;i++) {
    j=max(min(z[i-left],right-i),0);
    for(;i+j<len&&s[i+j]==s[j];j++);</pre>
```

```
z[i]=j;
if(i+z[i]>right) {
    right=i+z[i];
    left=i;
}
}
```

6.5 Lexicographically Smallest Rotation

```
string mcp(string s) {
   int n = s.length();
   s += s;
   int i=0, j=1;
   while (i<n && j<n) {
      int k = 0;
      while (k < n && s[i+k] == s[j+k]) k++;
      if (s[i+k] <= s[j+k]) j += k+1;
      else i += k+1;
      if (i == j) j++;
   }
   int ans = i < n ? i : j;
   return s.substr(ans, n);
}</pre>
```

7 Problems

7.1 MaximumEmptyRect

```
int largest_empty_rectangle(){
    int max_area = 0;
    for (int i=1; i<=n; ++i) {</pre>
         for (int j=1; j<=n; ++j)</pre>
             if (array[i][j]) wl[j] = wl[j-1] + 1;
             else wl[j] = 0;
         for (int j=n; j>=1; --j)
             if (array[i][j]) wr[j] = wr[j+1] + 1;
             else wr[j] = 0;
         for (int j=1; j<=n; ++j)</pre>
             if (array[i][j]) h[j] = h[j] + 1;
             else h[j] = 0;
          for (int j=1; j<=n; ++j)</pre>
             if (1[j] == 0) 1[j] = w1[j];
             else l[j] = min(wl[j], l[j]);
         for (int j=1; j<=n; ++j)</pre>
             if (r[j] == 0) r[j] = wr[j];
             else r[j] = min(wr[j], r[j]);
         for (int j=1; j<=n; ++j)</pre>
             \max \text{ area} = \max(\max \text{ area}, (l[j] + r[j] - 1)
                  * h[j]);
    return max_area;
```