Contents

1	Basic 1			
	1.1 1.2 1.3 1.4 1.5 1.6	Default Code IncreaseStackSize Pragma optimization Debugger Quick Random O Optimization	1 1 2 2 2 2	
2	Data 2.1 2.2 2.3 2.4 2.5 2.6 2.7 2.8 2.9	Structure Bigintnordered_mapextc_balance_treeextc_heap SkewHeap Disjoint Set Treap SparseTable Linear Basis	2 2 3 3 4 4 4 5 5	
3	Grap 3.1 3.2 3.3 3.4 3.5 3.6 3.7 3.8 3.9 3.10	h BCC Edge BCC Vertex Strongly Connected Components Bipartite Matching MinimumCostMaximumFlow MaximumFlow Kuhn Munkres 2-SAT HeavyLightDecomp MaxClique	5 5 5 6 6 7 7 8 8 9	
4	4.11 4.12 4.13 4.14	Prime Table	9 9 9 9 9 9 10 10 10 11 11 11 11 12	
5	5.1 5.2 5.3 5.4 5.5 5.6 5.7 5.8 5.9 5.10	netry Point Class Circle Class Line Class Triangle Circumcentre 2D Convex Hull 2D Farthest Pair 2D Cosest Pair SimulateAnnealing Ternary Search on Integer Minimum Covering Circle KDTree (Nearest Point)	12 12 13 13 13 14 14 14 14 14	
6	Strir 6.1 6.2 6.3 6.4 6.5	gology Hash Suffix Array KMP Z value Lexicographically Smallest Rotation	15 15 15 15 15 15	
7	Misc 7.1 7.2	MaximumEmptyRect DP-opt Condition 7.2.1 totally monotone (concave/convex) 7.2.2 monge condition (concave/convex)	16 16 16 16 16	

1 Basic

1.1 Default Code

```
#include <bits/stdc++.h>
using namespace std;
using lld = int64_t;
using llu = uint64_t;
using llf = long double;
using PII = pair<int,int>;
using PIL = pair<int, lld>;
using PLI = pair<lld,int>;
using PLL = pair<lld, lld>;
template<typename T>
using maxHeap = priority_queue<T, vector<T>, less<T>>;
template<typename T>
using minHeap = priority_queue<T, vector<T>, greater<T>>;
#define FF first
 #define SS second
#define SZ(x) (int)((x).size())
#define ALL(x) begin(x), end(x)
#define PB push_back
#define WC(x) while((x)--)
template<typename Iter>
ostream& _out(ostream &s, Iter b, Iter e) {
  s<<"[";
  for ( auto it=b; it!=e; it++ ) s<<(it==b?"":" ")<<*it</pre>
  s<<"]";
  return s;
template<typename A, typename B>
ostream& operator <<( ostream &s, const pair<A,B> &p )
    { return s<<"("<<p.FF<<","<<p.SS<<")"; }
template<typename T>
ostream& operator << ( ostream &s, const vector<T> &c )
    { return _out(s,ALL(c)); }
bool debug = \overline{0};
template<typename T>
void DEBUG(const T& x) {if(debug) cerr<<x;}</pre>
template<typename T, typename... Args>
 void DEBUG(const T& head,const Args& ...tail) {
  if(debug) {cerr<<head; DEBUG(tail...);}</pre>
int main(int argc, char* argv[]){
  if(argc>1 and string(argv[1]) == "-D") debug=1;
   if(!debug) {ios_base::sync_with_stdio(0);cin.tie(0);}
  return 0;
```

1.2 IncreaseStackSize

```
//stack resize
asm("mov %0, %%esp\n" :: "g"(mem+10000000));
//change esp to rsp if 64-bit system
//stack resize (linux)
#include <sys/resource.h>
void increase_stack_size() {
  const rlim_t ks = 64*1024*1024;
  struct rlimit rl;
  int res=getrlimit(RLIMIT STACK, &rl);
  if(res==0){
    if(rl.rlim_cur<ks){</pre>
      rl.rlim cur=ks;
      res=setrlimit(RLIMIT STACK, &rl);
    }
  }
}
// craziest way
static void run with stack size(void (*func)(), size t
   stsize) {
  char *stack, *send;
stack=(char *)malloc(stsize);
  send=stack+stsize-16;
  send=(char *)((uintptr_t)send/16*16);
  asm volatile(
    "mov %%rsp, (%0)\n"
    "mov %0, %%rsp\n"
```

```
:
    : "r" (send));
func();
asm volatile(
    "mov (%0), %%rsp\n"
:
    : "r" (send));
free(stack);
}
```

1.3 Pragma optimization

```
#pragma GCC optimize("Ofast,no-stack-protector,no-math-
errno,unroll-loops")
#pragma GCC target("sse,sse2,sse3,sse4,popcnt,abm
,mmx,avx,tune=native")
```

1.4 Debugger

```
#! /usr/bin/env python3
import subprocess, platform
os_name = platform.system()
cmd = []
prefix = ""
if os name == 'Windows':
 cmd=["cmd", "/C"]
 cmd = ["bash", "-c"]
 prefix = "./"
def GetTestData(exe):
 myout=subprocess.check output(cmd+["%s%s"%(prefix,
     exe)])
 return myout.decode("utf8")
def Judge(a,b,testdata):
 f = open("test.in", "w+")
 f.write(testdata)
 f.close()
 c=subprocess.check_output(cmd+["%s%s < test.in"%(
      prefix, a)])
 d=subprocess.check_output(cmd+["%s%s < test.in"%(
      prefix, b)])
 if not c == d:
   print("answer: %s"%c.decode("utf8"),end="")
   print("output: %s"%d.decode("utf8"), end="")
    print("WA!")
    return False
 return True
if __name__ == '__main__
 cnt = 0
 isOK = True
 while isOK:
   cnt += 1
   print(cnt)
    isOK = Judge("1234.exe", "test.exe", GetTestData("
        gen.exe"))
```

1.5 Quick Random

```
template<class T,T x1,T x2,T x3,int y1,int y2,int y3>
struct PRNG {
  using S = typename std::make signed<T>::type;
  PRNG (T
          s = 0) : s(s) {}
 T next() {
   T z = (s += x1);

z = (z ^ (z >> y1)) * x2;
    z = (z ^ (z >> y2)) * x3;
    return z ^ (z >> y3);
 T next(T n) { return next() % n; }
 S \text{ next}(S 1, S r) \{ \text{ return } 1 + \text{ next}(r - 1 + 1); \}
 T operator()() { return next(); }
  T operator()(T n) { return next(n); }
 S operator()(S 1, S r) { return next(1, r); }
  static T gen(T s) { return PRNG(s)(); }
  template<class U>
```

1.6 IO Optimization

```
static inline int gc() {
  static char buf[1 << 20], *p = buf, *end = buf;</pre>
  if (p == end) {
    if ((end = buf + fread(buf, 1, 1 << 20, stdin)) ==</pre>
         buf) return EOF;
    p = buf;
  return *p++;
template<typename T>
static inline bool gn(T &_){
  register int c = gc(); register T
                                              = 1;
  while(!isdigit(c) and c!=EOF and c!='-') c = gc();
if(c == '-') { __ = -1; c = gc(); }
  if(c == '-') { __ = -1; c
if(c == EOF) return false;
  while(isdigit(c)) _ = _ * 10 + c - '0', c = gc();
  *= __;
return true;
template <typename T, typename ...Args>
static inline bool gn(T &x, Args& ...args)(return gn(x)
      and gn(args...);}
```

2 Data Structure

2.1 Bigint

```
class BigInt{
    using lld = int fast64 t;
    #define PRINTF ARG PRIdFAST64
    #define LOG_BASE_STR "9"
    static constexpr lld BASE = 1000000000;
    static constexpr int LOG BASE = 9;
    vector<lld> dig;
    bool neg;
    inline int len()const{return (int)dig.size();}
    inline int cmp_minus(const BigInt& a) const {
      if(len() == 0 and a.len() == 0) return 0;
      if (neg ^ a.neg) return (int)a.neg*2 - 1;
      if(len() != a.len()) return neg?a.len()-len():len
          ()-a.len();
      for (int i=len()-1;i>=0;i--) if (dig[i] != a.dig[i
          ]) {
        return neg?a.dig[i]-dig[i]:dig[i]-a.dig[i];
      return 0;
    inline void trim(){
      while(!dig.empty() and dig.back()==0) dig.
          pop back();
      if(dig.empty()) neg = false;
  public:
    BigInt(): dig(vector<lld>()), neg(false){}
    BigInt(lld a): dig(vector<lld>()) {
      neg = a<0; dig.push back(abs(a));</pre>
      trim();
    BigInt(const string& a): dig(vector<lld>()){
      assert(!a.empty()); neg = (a[0] == '-');
      for (int i=((int)(a.size()))-1;i>=neq;i-=LOG BASE)
        lld cur = 0:
```

```
for(int j=min(LOG BASE-1, i-neg);j>=0;j--) cur
        = cur*10+a[i-j]-'0';
    dig.push back(cur);
  } trim();
inline bool operator<(const BigInt& a)const{return</pre>
    cmp minus(a)<0;}
inline bool operator<=(const BigInt& a)const{return</pre>
     cmp_minus(a) <=0;}</pre>
inline bool operator==(const BigInt& a)const{return
     cmp minus(a) == 0; }
inline bool operator!=(const BigInt& a)const{return
     cmp minus(a)!=0;}
inline bool operator>(const BigInt& a)const{return
    cmp minus(a)>0;}
inline bool operator>=(const BigInt& a)const{return
    cmp minus(a)>=0;}
BigInt operator-() const {
  BigInt ret = *this;
  ret.neg ^= 1;
  return ret;
BigInt operator+(const BigInt& a) const {
  if (neg) return -(-(*this)+(-a));
  if(a.neg) return (*this)-(-a);
  int n = max(a.len(), len());
  BigInt ret; ret.dig.resize(n);
  11d pro = 0;
  for (int i=0;i<n;i++) {</pre>
    ret.dig[i] = pro;
    if(i < a.len()) ret.dig[i] += a.dig[i];</pre>
    if(i < len()) ret.dig[i] += dig[i];</pre>
    pro = 0;
    if(ret.dig[i] >= BASE) pro = ret.dig[i]/BASE;
    ret.dig[i] -= BASE*pro;
  if(pro != 0) ret.dig.push_back(pro);
  return ret;
BigInt operator-(const BigInt& a) const {
  if (neg) return -(-(*this) - (-a));
  if(a.neg) return (*this) + (-a);
  int diff = cmp_minus(a);
  if(diff < 0) return -(a - (*this));</pre>
  if(diff == 0) return 0;
  BigInt ret; ret.dig.resize(len(), 0);
  for(int i=0;i<len();i++) {</pre>
    ret.dig[i] += dig[i];
    if(i < a.len()) ret.dig[i] -= a.dig[i];</pre>
    if(ret.dig[i] < 0){
      ret.dig[i] += BASE;
      ret.dig[i+1]--;
    }
  ret.trim();
  return ret;
BigInt operator*(const BigInt& a) const {
  if(len()==0 or a.len()==0) return 0;
  BigInt ret; ret.dig.resize(len()+a.len()+1);
  ret.neg = neg ^ a.neg;
  for (int i=0; i < len(); i++) for (int j=0; j < a.len(); j</pre>
      ++) {
    ret.dig[i+j] += dig[i] * a.dig[j];
    if (ret.dig[i+j] >= BASE) {
      lld x = ret.dig[i+j] / BASE;
      ret.dig[i+j+1] += x;
      ret.dig[i+j] -= x * BASE;
    }
  ret.trim();
  return ret;
BigInt operator/(const BigInt& a) const {
  assert(a.len());
  if(len() < a.len()) return 0;</pre>
  BigInt ret; ret.dig.resize(len()-a.len()+1);
  ret.neg = a.neg;
  for(int i=len()-a.len();i>=0;i--){
    lld l = 0, r = BASE;
    while (r-1 > 1) {
      11d \ mid = (1+r) >> 1;
      ret.dig[i] = mid;
      if(ret*a <= (neg?-(*this):(*this))) 1 = mid;</pre>
      else r = mid;
```

```
ret.dig[i] = 1;
      ret.neg ^= neg; ret.trim();
    BigInt operator%(const BigInt& a) const {
      return (*this) - (*this) / a * a;
    friend BigInt abs(BigInt a) {
      a.neg = 1; return a;
    friend void swap(BigInt& a, BigInt& b) {
      swap(a.dig, b.dig); swap(a.neg, b.neg);
    friend istream& operator>>(istream& ss, BigInt& a){
      string s; ss >> s;
      a = s;
      return ss;
    friend ostream& operator<<(ostream& ss. const
        BigInt& a) {
      if(a.len() == 0) return ss << '0';</pre>
      if(a.neg) ss << '-';
      ss << a.dig.back();
      for(int i=a.len()-2;i>=0;i--) ss << setw(LOG BASE</pre>
          ) << setfill('0') << a.dig[i];
      return ss;
    inline void print() const {
      if(len() == 0) {putchar('0'); return;}
      if(neg) putchar('-');
      printf("%" PRINTF ARG, dig.back());
      for(int i=len()-2;i>=0;i--) printf("%0"
          LOG BASE STR PRINTF ARG, dig[i]);
    #undef PRINTF ARG
    #undef LOG_BASE_STR
}:
```

2.2 unordered_map

2.3 extc balance tree

```
#include <ext/pb ds/assoc_container.hpp>
using __gnu_pbds::tree;
using __gnu_pbds::rb_tree_tag;
using __gnu_pbds::ov_tree_tag;
using __gnu_pbds::splay_tree_tag;
using __gnu_pbds::null_type;
using
       __gnu_pbds::tree_order_statistics_node_update;
template<typename T>
using ordered set = tree<T, null type, less<T>,
    rb tree tag, tree order statistics node update>;
template<typename A, B>
using ordered_map = tree<A, B, less<A>, rb_tree_tag,
    tree order statistics node update>;
int main(){
  ordered set<int> ss;
  ordered map<int, int> mm;
  ss.insert(1);
  ss.insert(5);
  assert(*ss.find_by_order(0)==1);
assert(ss.order_of_key(-1)==0);
  assert(ss.order of key(87) == 2);
  return 0;
```

2.4 extc_heap

```
#include <ext/pb_ds/assoc_container.hpp>
#include <ext/pb_ds/priority_queue.hpp>
```

```
using __gnu_pbds::priority queue;
using __gnu_pbds::pairing_heap_tag;
using __gnu_pbds::binary_heap_tag;
using _
        gnu pbds::binomial heap tag;
using __gnu_pbds::rc_binomial_heap_tag;
using __gnu_pbds::thin_heap_tag;
int main(){
 priority queue<int,less<int>,pairing heap tag> pq1,
      pq2;
 pq1.push(1);
 pq2.push(2);
 pq1.join(pq2);
  assert (pq2.size() == 0);
 auto it = pq1.push(87);
 pq1.modify(it, 19);
 while(!pq1.empty()){
   pq1.top();
   pq1.pop();
 return 0;
```

2.5 SkewHeap

```
template<typename T, typename cmp=less<T> >
class SkewHeap{
private:
 struct SkewNode {
   T x;
   SkewNode *lc, *rc;
   SkewNode(T a=0):x(a), lc(nullptr), rc(nullptr){}
 } *root;
 cmp CMP ;
 size t count;
 SkewNode* Merge (SkewNode* a, SkewNode* b) {
   if(!a or !b) return a?a:b;
    if (CMP (a->x, b->x)) swap(a, b);
   a->rc = Merge(a->rc, b);
   swap(a->lc, a->rc);
   return a:
  void clear(SkewNode*& a) {
   if(!a) return;
    clear(a->lc); clear(a->rc);
   delete a; a = nullptr;
public:
 SkewHeap(): root(nullptr), count(0){}
 bool empty() {return count==0;}
 size t size() {return count;}
 T top() {return root->x;}
 void clear() {clear(root);count = 0;}
 void push(const T& x) {
   SkewNode* a = new SkewNode(x);
   count += 1;
   root = Merge(root, a);
 void join(SkewHeap& a){
   count += a.count; a.count = 0;
   root = Merge(root, a.root);
 void pop() {
    count -= 1;
    SkewNode* rt = Merge(root->lc, root->rc);
   delete root; root = rt;
 friend void swap(SkewHeap& a, SkewHeap& b){
    swap(a.root, b.root);
```

2.6 Disjoint Set

```
class DJS{
private:
   vector<int> fa, sz, sv;
   vector<pair<int*, int>> opt;
   inline void assign(int *k, int v) {
      opt.emplace_back(k, *k);
      *k = v;
   }
```

```
public:
  inline void init(int n){
    fa.resize(n); iota(fa.begin(), fa.end(), 0);
    sz.resize(n); fill(sz.begin(), sz.end(), 1);
    opt.clear();
  int query(int x) {
    if(fa[x] == x) return x;
    return query(fa[x]);
  inline void merge(int a, int b) {
    int af = query(a), bf = query(b);
    if(af == bf) return;
    if(sz[af] < sz[bf]) swap(af, bf);</pre>
    assign(&fa[bf], fa[af]);
    assign(&sz[af], sz[af]+sz[bf]);
  inline void save() {sv.push_back((int)opt.size());}
  inline void undo() {
    int ls = sv.back(); sv.pop_back();
    while((int)opt.size() > ls) {
      pair<int*, int> cur=opt.back();
       *cur.first = cur.second;
      opt.pop back();
};
```

2.7 Treap

```
namespace Treap{
  \#define sz(x) ((x)? ((x)->size):0)
  \#define sm(x) ((x)? ((x)->sum):0)
  struct node{
    int size, cnt, sum;
    uint32_t pri;
    node *\overline{l}c, *rc;
    node(): size( 0 ), cnt( 0 ), sum( 0 ), pri( rand()
        ),
    lc( nullptr ), rc( nullptr ) {}
node( int x ): size( 1 ), cnt( x ), sum( x ), pri(
        rand()),
             lc( nullptr ), rc( nullptr ) {}
    void pull() {
      sum = cnt;
       if ( lc ) sum += lc->sum;
      if ( rc ) sum += rc->sum;
      size = 1;
      if ( lc ) size += lc->size;
       if ( rc ) size += rc->size;
  }:
  node* merge( node* L, node* R ) {
    if ( not L or not R ) return L ? L : R;
    if ( L->pri > R->pri ) {
      L->rc = merge( L->rc, R );
      L->pull();
      return L:
    } else {
      R->lc = merge(L, R->lc);
      R->pull();
      return R;
  void split by size( node* rt, int k, node*& L, node*&
       R ) {
    if ( not rt ) L = R = nullptr;
     else if( sz( rt->lc ) + 1 <= k ) {
       L = rt;
       split by size( rt->rc, k - sz( rt->lc ) - 1, L->
          rc, R);
      L->pull();
     } else {
       R = rt;
       split by size( rt->lc, k, L, R->lc );
       R->pull();
    }
  void split_by_sum( node* rt, int k, node*& L, node*&
       R ) {
     if ( not rt ) L = R = nullptr;
    else if ( sm( rt->lc ) + rt->cnt <= k ) {
      L = rt;
```

2.8 SparseTable

```
template<typename T, typename Cmp_=less<T>>
class SparseTable{
  vector<vector<T>> table;
  vector<int> lg;
  T cmp_(T a, T b) {
    return Cmp_()(a, b)?a:b;
public:
  void init(T arr[], int n){
    // 0-base
    lq.resize(n+1);
    lg[0] = -1, lg[1] = 0;
    for (int i=2;i<=n;i++) lg[i] = lg[i>>1]+1;
    table.resize(lg[n]+1);
    table[0].resize(n);
    for(int i=0;i<n;i++) table[0][i] = arr[i];</pre>
    for (int i=1;i<=lg[n];i++) {</pre>
      int len = 1 << (i-1), sz = 1 << i;
      table[i].resize(n-sz+1);
      for (int j=0; j<=n-sz; j++) {</pre>
        table[i][j] = cmp (table[i-1][j], table[i-1][j+
             len]);
    }
  T query(int 1, int r) {
     // 0-base [1, r)
    int wh = lg[r-1], len=1 << wh;
    return cmp_(table[wh][1], table[wh][r-len]);
};
```

2.9 Linear Basis

```
struct LinearBasis{
private:
  int n, sz;
  vector<llu> B;
  inline llu two(int x) {return ((llu)1) <<x;}</pre>
public:
  void init(int n ) {
    n = n ; B.clear();
    B.resize(n); sz = 0;
  void insert(llu x){
    // add x into B
    for (int i=n-1;i>=0;i--) if (two(i) & x) {
      if(B[i]) x ^= B[i];
      else{
        B[i] = x; sz++;
        for (int j=i-1; j>=0; j--)
          if(B[j] and two(j) & B[i])
            B[i] ^= B[j];
        for (int j=i+1; j<n; j++)</pre>
          if(two(i) & B[j])
            B[j] ^= B[i];
        break;
    }
  inline int size() {return sz;}
  bool check(llu x) {
     // is x in span(B) ?
    for (int i=n-1;i>=0;i--) if (two(i) & x) {
      if(B[i]) x ^= B[i];
      else return false;
```

```
return true;
}
llu kth_small(llu k) {
    /** 1-base would always > 0 **/
    /** should check it **/
    /* if we choose at least one element
        but size(B) (vectors in B) ==N(original elements)
        then we can't get 0 */
    llu ret = 0;
    for(int i=0;i<n;i++) if(B[i]) {
        if(k & 1) ret ^= B[i];
        k >>= 1;
    }
    return ret;
}
base;
```

3 Graph

3.1 BCC Edge

```
class BCC{
private:
  vector<int> low, dfn;
  int cnt;
  vector<bool> bcc;
  vector<vector<PII>> G:
  void dfs(int w, int f) {
    dfn[w] = cnt++;
    low[w] = dfn[w];
    for(auto i: G[w]){
      int u = i.FF, t = i.SS;
      if(u == f) continue;
      if(dfn[u]!=0){
       low[w] = min(low[w], dfn[u]);
      }else{
        dfs(u, w);
        low[w] = min(low[w], low[u]);
        if(low[u] > dfn[w]) bcc[t] = true;
    }
public:
  void init(int n, int m) {
    G.resize(n);
    fill(G.begin(), G.end(), vector<PII>());
    bcc.clear(); bcc.resize(m);
    low.clear(); low.resize(n);
    dfn.clear(); dfn.resize(n);
   cnt = 0;
  void add edge(int u, int v) {
    // should check for multiple edge
    G[u].PB({v, cnt});
    G[v].PB({u, cnt});
    cnt++;
  void solve() {cnt = 1;dfs(0, 0);}
  // the id will be same as insert order, 0-base
  bool is bcc(int x) {return bcc[x];}
```

3.2 BCC Vertex

```
class BCC{
private:
   vector<vector<pair<int,int>>> G;
   vector<int> dfn, low, id, sz;
   vector<bool> vis, ap;
   int n, ecnt, bcnt;
   void tarjan(int u, int f, int d) {
      vis[u] = true;
      dfn[u] = low[u] = d;
      int child = 0;
      for(auto e: G[u]) if(e.first != f) {
       int v = e.first;
      if(vis[v]) {
            low[u] = min(low[u], dfn[v]);
            }else{
```

```
tarjan(v, u, d+1);
        if(low[v] >= dfn[u]) ap[u] = true;
        low[u] = min(low[u], low[v]);
        child += 1;
    if(dfn[u] == 0 and child <= 1) ap[u] = false;</pre>
  void bfs bcc(int x) {
    // not sure
    queue<int> bfs;
    bfs.push(x); vis[x] = true;
    while(!bfs.empty()){
      int u = bfs.front(); bfs.pop();
      for(auto e: G[u]){
        id[e.second] = bcnt;
        if(ap[e.first] or vis[e.first]) continue;
        bfs.push(e.first); vis[e.first] = true;
        sz[bcnt] += 1;
   }
public:
 void init(int n ) {
   n = n ; G.clear(); G.resize(n);
    dfn.resize(n); low.resize(n);
    vis.clear(); vis.resize(n);
    ap.clear(); ap.resize(n);
    ecnt = 0, bcnt = 0;
 void add edge(int u, int v) {
   assert(0 \le u \text{ and } u \le n);
    assert(0 \le v and v \le n);
    G[u].emplace back(v, ecnt);
    G[v].emplace back(u, ecnt);
   ecnt += 1;
 void solve() {
    for(int i=0;i<n;i++) if(!vis[i]) {</pre>
      tarjan(i, i, 0);
    id.resize(ecnt);
   vis.clear(); vis.resize(n);
    sz.clear(); sz.resize(n);
    for (int i=0;i<n;i++) if (ap[i]) {</pre>
      bfs bcc(i); bcnt += 1;
 bool isAP(int x) {return ap[x];}
 int count() {return bcnt;}
  // bcc id of edges by insert order (0-base)
 int get id(int x) {return id[x];}
  // bcc size by bcc id
 int get size(int x) {return sz[x];}
} bcc;
```

3.3 Strongly Connected Components

```
class SCC{
private:
 int n, num ;
  vector<vector<int>> G, rG;
  vector<int> ord, num;
 bool vis[N];
  void dfs(int u) {
    if(vis[u]) return;
    vis[u]=1;
    for (auto v: G[u]) dfs(v);
    ord.PB(u);
  void rdfs(int u) {
   if(vis[u]) return;
    num[u] = num_;
    vis[u] = 1;
    for(auto v: rG[u]) rdfs(v);
public:
 inline void init(int n_){
    n=n_, num_=0;
    G.resize(n); rG.resize(n);
    num.resize(n);
    for (int i=0;i<n;i++) G[i].clear();</pre>
    for (int i=0;i<n;i++) rG[i].clear();</pre>
```

```
inline void add_edge(int st, int ed) {
   G[st].PB(ed);
   rG[ed].PB(st);
}
void solve() {
   memset(vis, 0, sizeof(vis));
   for(int i=0;i<n;i++) {
      if(!vis[i]) dfs(i);
   }
   reverse(ALL(ord));
   memset(vis, 0, sizeof(vis));
   for(auto i: ord) {
      if(!vis[i]) {
       rdfs(i);
       num_++;
      }
   }
   inline int get_id(int x) {return num[x];}
   inline int count() {return num_;}
}</pre>
```

3.4 Bipartite Matching

```
class BipartiteMatching{
  private:
     vector<int> X[N], Y[N];
     int fX[N], fY[N], n;
     bitset<N> walked;
    bool dfs(int x) {
      for(auto i:X[x]){
         if (walked[i]) continue;
         walked[i]=1;
         if(fY[i] ==-1||dfs(fY[i])){
           fY[i]=x; fX[x]=i;
           return 1;
         }
       return 0;
  public:
     void init(int n) {
      n=n;
       for (int i=0;i<n;i++) {</pre>
         X[i].clear();
         Y[i].clear();
         fX[i]=fY[i]=-1;
       walked.reset();
     void add edge(int x, int v) {
       X[x].push_back(y);
       Y[y].push back(y);
     int solve(){
      int cnt = 0;
       for (int i=0;i<n;i++) {</pre>
        walked.reset();
         if(dfs(i)) cnt++;
       // return how many pair matched
       return cnt;
};
```

3.5 MinimumCostMaximumFlow

```
{}
  }:
  int ori, edd;
  vector<vector<Edge>> G;
  vector<int> fa, wh;
  vector<bool> inq;
  vector<WeiT> dis;
  PCW SPFA() {
    fill(inq.begin(),inq.end(),false);
    fill(dis.begin(), dis.end(), INF WEI);
    queue<int> qq; qq.push(ori);
    dis[ori]=0;
    while(!qq.empty()){
      int u=qq.front();qq.pop();
      inq[u] = 0;
      for (int i=0;i<SZ(G[u]);++i) {</pre>
        Edge e=G[u][i];
        int v=e.to;
        WeiT d=e.wei;
        if(e.cap<=0||dis[v]<=dis[u]+d)
          continue;
        dis[v]=dis[u]+d;
        fa[v]=u, wh[v]=i;
        if(inq[v]) continue;
        qq.push(v);
        inq[v]=1;
    if (dis[edd] == INF WEI)
      return {-1,-1};
    CapT mw=INF CAP;
    for (int i=edd; i!=ori; i=fa[i])
      mw=min(mw,G[fa[i]][wh[i]].cap);
    for (int i=edd;i!=ori;i=fa[i]) {
      auto &eg=G[fa[i]][wh[i]];
      eg.cap-=mw;
      G[eg.to][eg.back].cap+=mw;
    return {mw,dis[edd]};
public:
  void init(int a, int b, int n) {
    ori=a,edd=b;
    G.clear();G.resize(n);
    fa.resize(n); wh.resize(n);
    inq.resize(n); dis.resize(n);
  void add edge(int st,int ed,WeiT w,CapT c) {
    G[st].emplace_back(ed,SZ(G[ed]),w,c);
    G[ed].emplace\_back(st,SZ(G[st])-1,-w,0);
  PCW solve(){
    CapT cc=0; WeiT ww=0;
    while(true) {
      PCW ret=SPFA();
      if(ret.first==-1) break;
      cc+=ret.first;
      ww+=ret.second;
    return {cc,ww};
} mcmf;
```

3.6 MaximumFlow

```
class Dinic{
private:
 using CapT = int64_t;
  struct Edge{
    int to, rev;
   CapT cap;
 };
 int n, st, ed;
 vector<vector<Edge>> G;
  vector<int> lv;
 bool BFS(){
   fill(lv.begin(), lv.end(), -1);
    queue<int> bfs;
   bfs.push(st);
   lv[st] = 0;
    while(!bfs.empty()){
      int u = bfs.front(); bfs.pop();
      for(auto e: G[u]){
        if(e.cap <= 0 or lv[e.to]!=-1) continue;</pre>
```

```
lv[e.to] = lv[u] + 1;
        bfs.push(e.to);
      }
    return (lv[ed]!=-1);
  CapT DFS(int u, CapT f) {
    if(u == ed) return f;
    CapT ret = 0;
    for(auto& e: G[u]){
      if(e.cap <= 0 or lv[e.to]!=lv[u]+1) continue;</pre>
      CapT nf = DFS(e.to, min(f, e.cap));
      ret += nf; e.cap -= nf; f -= nf;
      G[e.to][e.rev].cap += nf;
      if(f == 0) return ret;
    if (ret == 0) lv[u] = -1;
    return ret;
public:
  void init(int n_, int st_, int ed_){
    n = n_, st = st_, ed = ed_;
    G.resize(n); lv.resize(n);
    fill(G.begin(), G.end(), vector<Edge>());
  void add edge(int u, int v, CapT c) {
    G[u].push_back({v, (int)(G[v].size()), c});
    G[v].push_back({u, (int)(G[u].size())-1, 0});
  CapT max_flow() {
    CapT ret = 0;
    while (BFS()) {
     CapT f = DFS(st, numeric_limits<CapT>::max());
      ret += f;
      if(f == 0) break;
    return ret;
} flow;
```

3.7 Kuhn Munkres

```
struct KM{
// Maximum Bipartite Weighted Matching (Perfect Match)
  static const int MXN = 650;
  static const lld INF = 2147483647;
  int n,match[MXN],vx[MXN],vy[MXN];
  11d edge[MXN][MXN], lx[MXN], ly[MXN], slack[MXN];
  void init(int _n) {
    n = n;
    for(int i=0; i<n; i++) for(int j=0; j<n; j++)</pre>
      edge[i][j] = 0;
  void addEdge(int x, int y, lld w) { edge[x][y] = w; }
  bool DFS(int x) {
    vx[x] = 1;
    for (int y=0; y<n; y++) {</pre>
      if (vy[y]) continue;
      if (lx[x]+ly[y] > edge[x][y]){
        slack[y] = min(slack[y], lx[x] + ly[y] - edge[x][y]);
      } else {
        vy[y] = 1;
        if (match[y] == -1 || DFS(match[y]))
         { match[y] = x; return true; }
    return false;
  int solve(){
    fill (match, match+n, -1);
    fill(lx, lx+n, -INF); fill(ly, ly+n, 0);
    for (int i=0; i<n; i++)</pre>
      for (int j=0; j<n; j++)</pre>
        lx[i] = max(lx[i], edge[i][j]);
    for (int i=0; i<n; i++) {</pre>
      fill(slack, slack+n, INF);
      while (true) {
        fill(vx, vx+n, 0); fill(vy, vy+n, 0);
        if ( DFS(i) ) break;
        11d d = INF; // long long
        for (int j=0; j<n; j++)</pre>
          if (!vy[j]) d = min(d, slack[j]);
        for (int j=0; j<n; j++) {</pre>
          if (vx[j]) lx[j] -= d;
```

```
if (vy[j]) ly[j] += d;
    else slack[j] -= d;

    }
}
lld res=0;
for (int i=0; i<n; i++)
    res += edge[match[i]][i];
return res;
}
}graph;</pre>
```

3.8 2-SAT

```
// 2-SAT solver based on Kosaraju's algorithm.
// Variables are 0-based. Positive variables are stored
     in vertices 2n, corresponding negative variables
// TODO: This is quite slow (3x-4x slower than Gabow's
    algorithm)
struct TwoSat {
  int n;
  vector<vector<int> > adj, radj, scc;
  vector<int> sid, vis, val;
  stack<int> stk;
  int scnt:
   // n: number of variables, including negations
  TwoSat(\textbf{int} \ n): \ n(n) \text{, adj}(n) \text{, radj}(n) \text{, sid}(n) \text{, vis}(n) \text{,}
        val(n, -1) \{ \}
  // adds an implication
  void impl(int x, int y) { adj[x].push back(y); radj[y
      ].push back(x); }
   // adds a disjunction
  void vee(int x, int y) { impl(x^1, y); impl(y^1, x);
       }
  // forces variables to be equal
  void eq(int x, int y) { impl(x, y); impl(y, x); impl(
       x^1, y^1; impl(y^1, x^1); 
   // forces variable to be true
  void tru(int x) { impl(x^1, x); }
  void dfs1(int x) {
    if (vis[x]++) return;
for (int i = 0; i < adj[x].size(); i++) {</pre>
       dfs1(adj[x][i]);
    stk.push(x);
  void dfs2(int x) {
    if (!vis[x]) return; vis[x] = 0;
    sid[x] = scnt; scc.back().push back(x);
    for (int i = 0; i < radj[x].size(); i++) {</pre>
      dfs2(radj[x][i]);
  // returns true if satisfiable, false otherwise
  // on completion, val[x] is the assigned value of
       variable x
   // note, val[x] = 0 implies val[x^1] = 1
  bool two sat() {
    scnt = 0;
    for (int i = 0; i < n; i++) {</pre>
      dfs1(i);
    while (!stk.empty()) {
       int v = stk.top(); stk.pop();
       if (vis[v]) {
        scc.push back(vector<int>());
         dfs2(v);
         scnt++;
      }
    for (int i = 0; i < n; i += 2) {</pre>
      if (sid[i] == sid[i+1]) return false;
    vector<int> must(scnt);
    for (int i = 0; i < scnt; i++) {</pre>
       for (int j = 0; j < scc[i].size(); j++) {</pre>
         val[scc[i][j]] = must[i];
         must[sid[scc[i][j]^1]] = !must[i];
    return true;
};
```

3.9 HeavyLightDecomp

```
#define REP(i, s, e) for(int i = (s); i \le (e); i ++)
#define REPD(i, s, e) for(int i = (s); i \ge (e); i --)
const int MAXN = 100010;
const int LOG = 19;
struct HLD{
  int n;
  vector<int> g[MAXN];
  int sz[MAXN], dep[MAXN];
  int ts, tid[MAXN], tdi[MAXN], tl[MAXN], tr[MAXN];
  // ts : timestamp , useless after yutruli
  // tid[u]: pos. of node u in the seq.
     tdi[i]: node at pos i of the seq.
  // tl , tr[ u ] : subtree interval in the seq. of
  int prt[MAXN][LOG], head[MAXN];
  // head[ u ] : head of the chain contains u
  void dfssz(int u, int p) {
    dep[u] = dep[p] + 1;
    prt[u][0] = p; sz[u] = 1; head[u] = u;
    for(int& v:g[u]) if(v != p){
      dep[v] = dep[u] + 1;
      dfssz(v, u);
      sz[u] += sz[v];
  void dfshl(int u){
    ts++:
    tid[u] = tl[u] = tr[u] = ts;
    tdi[tid[u]] = u;
    sort(ALL(g[u]),
         [&] (int a, int b) {return sz[a] > sz[b];});
    bool flag = 1;
    for(int& v:g[u]) if(v != prt[u][0]){
      if(flag) head[v] = head[u], flag = 0;
      dfshl(v);
      tr[u] = tr[v];
  inline int lca(int a, int b){
    if(dep[a] > dep[b]) swap(a, b);
    int diff = dep[b] - dep[a];
REPD(k, LOG-1, 0) if(diff & (1<<k)){</pre>
     b = prt[b][k];
    if(a == b) return a;
    REPD(k, LOG-1, 0) if(prt[a][k] != prt[b][k]){
      a = prt[a][k]; b = prt[b][k];
    return prt[a][0];
  void init( int _n ) {
   n = _n; REP( i , 1 , n ) g[ i ].clear();
  void addEdge( int u , int v ){
    g[ u ].push_back( v );
    g[ v ].push back( u );
  void vutruli() {
    dfssz(1, 0);
    ts = 0;
    dfshl(1);
    REP(k, 1, LOG-1) REP(i, 1, n)
      prt[i][k] = prt[prt[i][k-1]][k-1];
 vector< PII > getPath( int u , int v ) {
    vector< PII > res;
    while( tid[ u ] < tid[ head[ v ] ] ){</pre>
     res.push_back( PII(tid[ head[ v ] ] , tid[ v ]) )
      v = prt[ head[ v ] ][ 0 ];
   res.push back( PII( tid[ u ] , tid[ v ] ) );
    reverse( ALL( res ) );
    return res;
    /* res : list of intervals from u to v
     * u must be ancestor of v
     * usage :
     * vector< PII >& path = tree.getPath( u , v )
     * for( PII tp : path ) {
        int l, r; tie(l, r) = tp;
         upd(1,r);
         uu = tree.tdi[ 1 ] , vv = tree.tdi[ r ];
         uu ~> vv is a heavy path on tree
```

```
*/
}
tree;
```

3.10 MaxClique

```
struct MaxClique {
     int n, deg[maxn], ans;
    bitset<maxn> adj[maxn];
     vector<pair<int, int>> edge;
     void init(int _n) {
         n = _n;
         for (int i = 0; i < n; ++i) adj[i].reset();
for (int i = 0; i < n; ++i) deg[i] = 0;</pre>
         edge.clear();
     void add edge(int a, int b) {
         edge.emplace_back(a, b);
         ++deg[a]; ++deg[b];
     int solve() {
         vector<int> ord;
         for (int i = 0; i < n; ++i) ord.push_back(i);</pre>
         sort(ord.begin(), ord.end(), [&](const int &a,
              const int &b) { return deg[a] < deg[b]; });</pre>
         vector<int> id(n);
         for (int i = 0; i < n; ++i) id[ord[i]] = i;</pre>
         for (auto e : edge) {
              int u = id[e.first], v = id[e.second];
              adj[u][v] = adj[v][u] = true;
         bitset<maxn> r, p;
for (int i = 0; i < n; ++i) p[i] = true;</pre>
         ans = 0:
         dfs(r, p);
         return ans;
     void dfs(bitset<maxn> r, bitset<maxn> p) {
         if (p.count() == 0) return ans = max(ans, (int)
             r.count()), void();
         if ((r | p).count() <= ans) return;</pre>
         int now = p._Find_first();
         bitset<maxn> cur = p & ~adj[now];
         for (now = cur._Find_first(); now < n; now =</pre>
              cur. Find next(now)) {
              r[now] = \overline{true};
             dfs(r, p & adj[now]);
             r[now] = false;
              p[now] = false;
};
```

4 Math

4.1 Prime Table

```
\begin{array}{c} 1002939109, 1020288887, 1028798297, 1038684299, \\ 1041211027, 1051762951, 1058585963, 1063020809, \\ 1147930723, 1172520109, 1183835981, 1187659051, \\ 1241251303, 1247184097, 1255940849, 1272759031, \\ 1287027493, 1288511629, 1294632499, 1312650799, \\ 1868732623, 1884198443, 1884616807, 1885059541, \\ 1909942399, 1914471137, 1923951707, 1925453197, \\ 1979612177, 1980446837, 1989761941, 2007826547, \\ 2008033571, 2011186739, 2039465081, 2039728567, \\ 2093735719, 2116097521, 2123852629, 2140170259, \\ 3148478261, 3153064147, 3176351071, 3187523093, \\ 3196772239, 3201312913, 3203063977, 3204840059, \\ 3210224309, 3213032591, 3217689851, 3218469083, \\ 3219857533, 3231880427, 3235951699, 3273767923, \\ 3276188869, 3277183181, 3282463507, 3285553889, \\ 3319309027, 3327005333, 3327574903, 3341387953, \\ 3373293941, 3380077549, 3380892997, 3381118801 \\ \end{array}
```

4.2 $\lfloor \frac{n}{i} \rfloor$ Enumeration

```
T_0 = 1, T_{i+1} = \lfloor \frac{n}{\lfloor \frac{n}{T_i + 1} \rfloor} \rfloor
```

4.3 ax+by=gcd

```
// By Adrien1018 (not knowing how to use.
// ax+ny = 1, ax+ny == ax == 1 (mod n)
tuple<int, int, int> extended_gcd(int a, int b) {
   if (!b) return make_tuple(a, 1, 0);
   int d, x, y;
   tie(d, x, y) = extended_gcd(b, a % b);
   return make_tuple(d, y, x - (a / b) * y);
}
```

4.4 Pollard Rho

```
// does not work when n is prime
lld modit(lld x,lld mod) {
  if(x \ge mod) x = mod;
  //if(x<0) x+=mod;
  return x;
lld mult(lld x,lld y,lld mod) {
  11d s=0, m=x%mod;
  while(y) {
    if(y&1) s=modit(s+m, mod);
    v >> = 1:
   m=modit(m+m, mod);
  return s;
lld f(lld x,lld mod) {
  return modit(mult(x,x,mod)+1,mod);
lld pollard rho(lld n) {
  if(!(n&1)) return 2;
  while (true) {
    11d y=2, x=rand()%(n-1)+1, res=1;
    for (int sz=2; res==1; sz*=2) {
      for (int i=0; i<sz && res<=1; i++) {</pre>
        x = f(x, n);
        res = \_gcd(abs(x-y), n);
      }
      y = x;
    if (res!=0 && res!=n) return res;
```

4.5 Pi Count (Linear Sieve)

```
static constexpr int N = 1000000 + 5;
lld pi[N];
vector<int> primes;
bool sieved[N];
lld cube_root(lld x) {
  11d s = static_cast<11d>(cbrt(x - static_cast<long</pre>
      double>(0.1)));
  while (s*s*s <= x) ++s;
  return s-1;
lld square_root(lld x){
  11d s = static cast<11d>(sqrt(x - static cast<long</pre>
      double > (0.1));
  while (s*s \le x) ++s;
  return s-1;
void init(){
  primes.reserve(N);
  primes.push back(1);
  for (int i=2;i<N;i++) {</pre>
    if(!sieved[i]) primes.push_back(i);
    pi[i] = !sieved[i] + pi[i-1];
    for(int p: primes) if(p > 1) {
      if(p * i >= N) break;
      sieved[p * i] = true;
      if(p % i == 0) break;
 }
lld phi(lld m, lld n) {
  static constexpr int MM = 80000, NN = 500;
  static lld val[MM][NN];
```

```
if(m < MM and n < NN and val[m][n]) return val[m][n]</pre>
      - 1;
  if(n == 0) return m;
  if(primes[n] >= m) return 1;
 lld ret = phi(m, n - 1) - phi(m / primes[n], n - 1);
 if (m < MM and n < NN) val[m][n] = ret + 1;</pre>
 return ret;
lld pi count(lld);
11d P2(11d m, 11d n) {
 11d sm = square root(m), ret = 0;
  for(lld i = n+1;primes[i] <=sm;i++)</pre>
    ret += pi_count(m / primes[i]) - pi_count(primes[i
        ]) + \overline{1};
  return ret;
lld pi_count(lld m) {
 if(m < N) return pi[m];</pre>
 lld n = pi_count(cube_root(m));
  return phi(m, n) + n - 1 - P2(m, n);
```

4.6 NloglogN Sieve

```
void Sieve(int n) {
  for(int i=2;i<=n;i++) {
    if(notprime[i]) continue;
    primes.push_back(i);
  for(int j=i*i;j<=n;j+=i) notprime[i]=true;
  }
}</pre>
```

4.7 Range Sieve

4.8 Miller Rabin

```
lld modu(lld a, lld m) {
 while (a >= m) a -= m;
 return a;
lld mul(lld a, lld b, lld m) {
 if(a < b) swap(a, b);
 11d ret = 0;
 while(b) {
   if(b & 1) ret = modu(ret+a, m);
    a = modu(a+a, m);
   b >>= 1;
 return ret;
lld qPow(lld a, lld k, lld m) {
 11d ret = 1;
 a %= m;
 while(k) {
   if(k & 1) ret = mul(ret, a, m);
    a = mul(a, a, m);
   k >>= 1;
 return modu(ret, m);
```

```
bool witness(lld a, lld s, int t, lld n) {
   lld b = qPow(a, s, n);
   if(b == 0) return false;
   while(t--){
     lld bb = mul(b, b, n);
     if(bb == 1 and b != 1 and b != n-1) return true;
     b = bb:
   return b != 1;
bool miller_rabin(lld n) {
  if(n < 2) return false;</pre>
   if(!(n & 1)) return (n==2);
lld x = n-1; int t = 0;
   while(!(x&1)) x >>= 1, t++;
   lld sprp[] =
       {2,325,9375,28178,450775,9780504,1795265022};
   for(int i=0;i<7;i++){
     if(witness(sprp[i]%n, x, t, n)) return false;
   return true;
```

4.9 Inverse Element

```
// x's inverse mod k
long long GetInv(long long x, long long k) {
    // k is prime: euler_(k)=k-1
    return qPow(x, euler_phi(k)-1);
}
// if you need [1, x] (most use: [1, k-1]
void solve(int x, long long k) {
    inv[1] = 1;
    for(int i=2;i<x;i++)
        inv[i] = ((long long)(k - k/i) * inv[k % i]) % k;
}</pre>
```

4.10 Euler Phi Function

```
extended euler:
   a^b mod p
   if gcd(a, p) == 1: a^(b%phi(p))
   elif b < phi(p): a^b mod p
   else a^(b%phi(p) + phi(p))
lld euler_phi(int x) {
  11d r=1;
  for (int i=2;i*i<=x;++i) {</pre>
    if (x%i==0) {
      x/=i;
      r*=(i-1):
      while (x%i==0) {
        x/=i;
        r*=i;
      }
    }
  if (x>1) r*=x-1;
  return r;
vector<int> primes;
bool notprime[N];
lld phi[N];
void euler sieve(int n) {
  for(int =2;i<n;i++){
    if(!notprime[i]){
      primes.push back(i);
      phi[i] = i-\overline{1};
    for(auto j: primes) {
      if(i*j >= n) break;
      notprime[i*j] = true;
      phi[i*j] = phi[i] * phi[j];
      if(i % j == 0) {
  phi[i*j] = phi[i] * j;
        break;
      }
    }
  }
```

4.11 Gauss Elimination

```
typedef long double llf;
const int N = 300;
const llf EPS = 1e-8;
// make m[i][i] = x, m[i][j] = 0
// v is for solving equation:
// for(int i=0;i < n;i++) ans[pos[i]] = val[i]/mtx[i][pos
    [i]];
// for(int i=0;i<n;i++) cout << ans[i] << '\n';
bool Gauss(llf m[N][N], llf v[N], int n, int pos[N]) {
 for (int i=0;i<n;i++) {</pre>
    int x=-1, y=-1; llf e = 0;
    for (int j=i;j<n;j++) for (int k=i;k<n;k++) {</pre>
      if(fabs(m[j][pos[k]])>e){
        e = fabs(m[j][pos[k]]);
        x = j, y = k;
      }
    if(x==-1 or y==-1) return false;
    swap(m[x], m[i]);
    swap(v[x], v[i]);
    swap(pos[y], pos[i]);
    for (int j=i+1; j<n; j++) {</pre>
      llf xi = m[j][pos[i]]/m[i][pos[i]];
      for(int k=0; k<n; k++) m[j][pos[k]] -= xi*m[i][pos[</pre>
          k]];
      v[j] -= xi*v[i];
   }
  for (int i=n-1;i>=0;i--) {
    for (int j=i-1; j>=0; j--) {
      llf xi = m[j][pos[i]]/m[i][pos[i]];
      for (int k=0; k<n; k++) m[j][pos[k]] -= xi*m[i][pos[</pre>
          k]];
      v[j] = xi*v[i];
  return true:
```

4.12 Fast Fourier Transform

```
polynomial multiply:
   FFT(a, N, true);
   FFT(b, N, true);
  for(int i=0;i<MAXN;i++) c[i] = a[i]*b[i];
  FFT(c, N, false);
  yeah~ go result in c
(N must be 2^k and >= len(a)+len(b))
typedef long double llf;
typedef complex<llf> cplx;
const int MAXN = 262144;
const llf PI = acos((llf)-1);
cplx A[MAXN], B[MAXN], C[MAXN], omega[MAXN+1];
void init omega() {
 const cplx I = {0, 1};
  for(int i=0;i<=MAXN;i++) omega[i] = exp(i*2*PI/MAXN*I</pre>
     );
void FFT(cplx arr[], int n, bool ori){
  // n must be 2^k
  int theta = MAXN / n;
 for(int len=n;len>=2;len>>=1) {
   int tot = len>>1;
    for (int i=0;i<tot;i++) {</pre>
      cplx omg = omega[ori?i*theta%MAXN:MAXN-(i*theta%
          MAXN)];
      for(int j=i;j<n;j+=len){</pre>
       int k = j+tot;
        cplx x = arr[j] - arr[k];
        arr[j] += arr[k];
        arr[k] = omg * x;
    theta = (theta * 2) % MAXN;
```

```
int i = 0;
for(int j=1;j<n-1;j++) {
   for(int k=n>>1;k>(i^=k);k>>=1);
   if(j < i) swap(arr[j], arr[i]);
}
if(ori) return;
for(int i=0;i<n;i++) arr[i] /= n;
}</pre>
```

4.13 Chinese Remainder

```
lld crt(lld ans[], lld pri[], int n) {
   11d M = 1;
   for (int i=0;i<n;i++) M *= pri[i];</pre>
   11d ret = 0;
   for (int i=0;i<n;i++) {</pre>
    lld inv = (gcd(M/pri[i], pri[i]).first + pri[i])%
     ret += (ans[i] * (M/pri[i]) %M * inv) %M;
    ret %= M;
  return ret;
Another:
x = a1 % m1
x = a2 \% m2
g = gcd(m1, m2)
assert((a1-a2)%g==0)
 [p, q] = exgcd(m2/g, m1/g)
return a2+m2*(p*(a1-a2)/g)
0 <= x < 1cm(m1, m2)
```

4.14 NTT

```
// Remember coefficient are mod P
/* p=a*2^n+1
        2^n
  n
                                       root
                                 а
   16
       65536
                     65537
                                 7
                     7340033
   20
       1048576
// (must be 2^k)
template<LL P, LL root, int MAXN>
struct NTT{
  static LL bigmod(LL a, LL b) {
    LL res = 1;
    for (LL bs = a; b; b >>= 1, bs = (bs * bs) % P)
     if(b&1) res=(res*bs)%P;
   return res;
  static LL inv(LL a, LL b) {
    if (a==1) return 1;
    return (((LL) (a-inv(b%a,a))*b+1)/a)%b;
  LL omega[MAXN+1];
  NTT() {
    omega[0] = 1;
    LL r = bigmod(root, (P-1)/MAXN);
    for (int i=1; i<=MAXN; i++)</pre>
      omega[i] = (omega[i-1]*r)%P;
  // n must be 2^k
  void tran(int n, LL a[], bool inv_ntt=false) {
    int basic = MAXN / n , theta = basic;
for (int m = n; m >= 2; m >>= 1) {
      int mh = m >> 1;
      for (int i = 0; i < mh; i++) {</pre>
        LL w = omega[i*theta%MAXN];
        for (int j = i; j < n; j += m) {</pre>
          int k = j + mh;
          LL x = a[j] - a[k];
          if (x < 0) x += P;
          a[j] += a[k];
          if (a[j] > P) a[j] -= P;
          a[k] = (w * x) % P;
        }
      theta = (theta * 2) % MAXN;
    int i = 0;
    for (int j = 1; j < n - 1; j++) {</pre>
      for (int k = n >> 1; k > (i ^= k); k >>= 1);
```

```
if (j < i) swap(a[i], a[j]);
}
if (inv_ntt) {
    LL ni = inv(n,P);
    reverse( a+1 , a+n );
    for (i = 0; i < n; i++)
        a[i] = (a[i] * ni) % P;
}
};
const LL P=2013265921, root=31;
const int MAXN=4194304;
NTT<P, root, MAXN> ntt;
```

4.15 DiscreteLog

```
// Baby-step Giant-step Algorithm
// a x + by = g
void exgcd(long long x, long long y, long long &g,
   long long &a, long long &b) {
 if (y == 0)
   g = x, a = 1, b = 0;
 else
   exgcd(y, x%y, g, b, a), b = (x/y) * a;
long long inverse(long long x, long long p) {
 long long g, b, r;
 exgcd(x, p, g, r, b);
 if (g < 0) r = -r;
 return (r%p + p)%p;
long long BSGS(long long P, long long B, long long N) {
 // find B^L = N \mod P
 unordered map<long long, int> R;
 long long sq = (long long) sqrt(P);
 long long t = 1, f;
 for (int i = 0; i < sq; i++) {</pre>
   if (t == N)
     return i;
   if (!R.count(t))
     R[t] = i;
    t = (t * B) % P;
 f = inverse(t, P);
 for (int i = 0; i <= sq+1; i++) {</pre>
   if (R.count(N))
     return i * sq + R[N];
   N = (N * f) % P;
 return -1;
```

5 Geometry

5.1 Point Class

```
template<typename T>
struct Point{
  typedef long double llf;
  static constexpr llf EPS = 1e-8;
  Тх, у;
  Point(T _=0, T __=0): x(_), y(__){}
  \textbf{template} \small < \textbf{typename} \quad \mathbb{T} 2 \small >
    Point(const Point<T2>& a): x(a.x), y(a.y){}
  inline llf theta() const {
    return atan2((llf)y, (llf)x);
  inline llf dis() const {
    return hypot((llf)x, (llf)y);
  inline llf dis(const Point& o) const {
    return hypot((llf)(x-o.x), (llf)(y-o.y));
  Point operator-(const Point& o) const {
    return Point(x-o.x, y-o.y);
  Point operator = (const Point& o) {
   x-=o.x, y-=o.y;
return *this;
```

```
Point operator+(const Point& o) const {
    return Point(x+o.x, y+o.y);
  Point operator+=(const Point& o) {
    x+=o.x, y+=o.y;
return *this;
  Point operator* (const T& k) const {
    return Point(x*k, y*k);
  Point operator*=(const T& k) {
    x*=k, y*=k;
    return *this;
  Point operator/(const T& k) const {
    return Point(x/k, y/k);
  Point operator/=(const T& k) {
    x/=k, y/=k;
    return *this;
  Point operator-() const {
    return Point(-x, -y);
  Point rot90() const {
    return Point(-y, x);
  template<typename T2>
  bool in(const Circle<T2>& a) const {
     /* Add struct Circle at top */
    return a.o.dis(*this) +EPS <= a.r;</pre>
  bool equal(const Point& o, true_type) const {
    return fabs (x-o.x) < EPS and \overline{f}abs (y-o.y) < EPS;
  bool equal(const Point& o, false type) const {
    return tie(x, y) == tie(o.x, o.y);
  bool operator==(const Point& o) const {
    return equal(o, is floating point<T>());
  bool operator!=(const Point& o) const {
    return ! (*this == 0);
  bool operator<(const Point& o) const {</pre>
    return theta() < o.theta();</pre>
     // sort like what pairs did
     // if(is_floating_point<T>()) return fabs(x-o.x)<
         EPS?y<o.y:x<o.x;
    // else return tie(x, y) < tie(o.x, o.y);
  friend inline T cross(const Point& a, const Point& b)
    return a.x*b.y - b.x*a.y;
  friend inline T dot(const Point& a, const Point &b) {
    return a.x*b.x + a.y*b.y;
  friend ostream& operator<<(ostream& ss, const Point&</pre>
    ss<<"("<<o.x<<", "<<o.y<<")";
    return ss;
};
```

5.2 Circle Class

```
template<typename T>
struct Circle{
    static constexpr llf EPS = 1e-8;
    Point<T> o;
    T r;
    vector<Point<llf>> operator&(const Circle& aa)const{
        // https://www.cnblogs.com/wangzming/p/8338142.html
        llf d=o.dis(aa.o);
        if(d > r+aa.r+EPS or d < fabs(r-aa.r)-EPS) return
        {};
        llf dt = (r*r - aa.r*aa.r)/d, dl = (d+dt)/2;
        Point<llf>> dir = (aa.o-o); dir /= d;
        Point<llf>> pcrs = dir*dl + o;
        dt=sqrt(max(0.0L, r*r - dl*dl)), dir=dir.rot90();
        return {pcrs + dir*dt, pcrs - dir*dt};
    }
}
```

5.3 Line Class

};

```
const Point<long double> INF P(-1e20, 1e20);
const Point<long double> NOT EXIST(1e20, 1e-20);
template<typename T>
struct Line{
  static constexpr long double EPS = 1e-8;
  // ax+by+c = 0
 T a, b, c;
 Line(): a(0), b(1), c(0){}
Line(T_, T__, T__): a(
                        _): a(_), b(__), c(___){
    assert(fabs(a)>EPS or fabs(b)>EPS);
 template<typename T2>
    Line(const Line\langle T2 \rangle \& x): a(x.a), b(x.b), c(x.c){}
  typedef Point<long double> Pt;
 bool equal(const Line& o, true_type) const {
    return fabs(a-o.a) < EPS and fabs(b-o.b) < EPS and</pre>
        fabs(c-o.b) < EPS;</pre>
 bool euqal(const Line& o, false_type) const {
    return a==o.a and b==o.b and c==o.c;
 bool operator==(const Line& o) const {
    return eugal(o, is floating point<T>());
 bool operator!=(const Line& 0) const {
    return ! (*this == 0);
 friend inline bool on_line__(const Point<T>& p, const
       Line& l, true_type) {
    return fabs(l.a*p.x + l.b*p.y + l.c) < EPS;</pre>
  friend inline bool on_line__(const Point<T>& p, const
    Line& 1, false_type) {
return l.a*p.x + l.b*p.y + l.c == 0;
  friend inline bool on_line(const Point<T>&p const
      Line& 1) {
    return on line (p, l, is floating point<T>());
  friend inline bool is parallel (const Line& x, const
       Line& y, true_type) {
    return fabs(x.a*y.b - x.b*y.a) < EPS;</pre>
 friend inline bool is_parallel__(const Line& x, const
       Line& y, false_type) {
    return x.a*y.b == x.b*y.a;
 friend inline bool is parallel(const Line& x, const
      Line& v) {
    return is_parallel__(x, y, is_floating_point<T>());
 friend inline Pt get inter(const Line& x, const Line&
      y) {
    typedef long double llf;
    if(x==y) return INF P;
    if(is parallel(x, y)) return NOT EXIST;
    llf delta = x.a*y.b - x.b*y.a;
    lif delta_x = x.b*y.c - x.c*y.b;
lif delta_y = x.c*y.a - x.a*y.c;
return Pt(delta_x / delta, delta_y / delta);
 friend ostream& operator<<(ostream& ss, const Line& o</pre>
    ss<<o.a<<"x+"<<o.b<<"y+"<<o.c<<"=0";
    return ss;
template<typename T>
inline Line<T> get line(const Point<T>& a, const Point<</pre>
    T>& b) {
  return Line<T>(a.y-b.y, b.x-a.x, (b.y-a.y) *a.x-(b.x-a
      .x)*a.y);
```

```
5.4 Triangle Circumcentre
```

5.5 2D Convex Hull

```
template<typename T>
class ConvexHull 2D{
private:
  typedef Point<T> PT;
  vector<PT> dots;
  struct myhash{
    uint64 t operator()(const PT& a) const {
      uint\overline{6}4 t xx=0, yy=0;
      memcpy(&xx, &a.x, sizeof(a.x));
      memcpy(&yy, &a.y, sizeof(a.y));
      uint64_t ret = xx*17+yy*31;
ret = (ret ^ (ret >> 16))*0x9E3779B1;
      ret = (ret ^ (ret >> 13))*0xC2B2AE35;
      ret = ret ^ xx;
      return (ret ^ (ret << 3)) * yy;</pre>
  };
  unordered set<PT, myhash> in hull;
public:
  inline void init() {in_hull.clear();dots.clear();}
  void insert(const PT& x) {dots.PB(x);}
  void solve(){
    sort(ALL(dots), [](const PT& a, const PT& b){
      return tie(a.x, a.y) < tie(b.x, b.y);</pre>
    }):
    vector<PT> stk(SZ(dots)<<1);
    int top = 0;
    for (auto p: dots) {
      while(top >= 2 and cross(p-stk[top-2], stk[top
          -1]-stk[top-2]) <= 0)
        top --:
      stk[top++] = p;
    for (int i=SZ (dots) -2, t = top+1;i>=0;i--) {
      while(top >= t and cross(dots[i]-stk[top-2], stk[
          top-1]-stk[top-2]) <= 0)
        top --;
      stk[top++] = dots[i];
    stk.resize(top-1);
    swap(stk, dots);
    for(auto i: stk) in hull.insert(i);
  vector<PT> get() {return dots;}
  inline bool in it(const PT& x){
    return in_hull.find(x)!=in_hull.end();
```

5.6 2D Farthest Pair

5.7 2D Cosest Pair

```
struct Point{
  llf x, y;
  llf dis;
} arr[N];
inline llf get dis(Point a, Point b){
 return sqrt((a.x-b.x)*(a.x-b.x) + (a.y-b.y)*(a.y-b.y)
llf solve() {
 int cur = rand()%n;
  for(int i=0;i<n;i++) arr[i].dis = get_dis(arr[cur],</pre>
      arr[i]);
  sort(arr, arr+n, [](Point a, Point b){return a.dis <</pre>
      b.dis; });
  llf ans = 1e50;
 for (int i=0;i<n;i++) {</pre>
    for (int j=i+1; j<n; j++) {</pre>
      if(arr[j].dis - arr[i].dis > ans) break;
      ans = min(ans, get dis(arr[i], arr[j]));
 }
  return ans;
```

5.8 SimulateAnnealing

```
double getY(double);
int main(){
 int rr, 11;
 default random engine rEng(time(NULL));
 uniform real distribution < double > Range (-1,1);
 uniform real distribution < double > expR(0,1);
 auto Random=bind(Range, rEng), expRand=bind(expR, rEng)
 int step=0;
 double pace=rr-ll, mini=0.95; // need to search for
      i t
 double x=max(min(Random()*pace+ll, rr), ll), y=getY(x
      );
 while(pace>=1e-7) {
   double newX = max(min(x + Random()*pace, rr), ll);
    double newY = getY(newX);
    if(newY < y || expRand() < exp(-step))</pre>
     x=newX, y=newY;
    step++;
   pace*=mini;
```

5.9 Ternary Search on Integer

```
int TernarySearch(int 1, int r) {
    // (1, r]
    while (r - 1 > 1) {
        int mid = (1 + r) >> 1;
        if (f(mid) > f(mid + 1)) r = mid;
        else 1 = mid;
    }
    return 1+1;
}
```

5.10 Minimum Covering Circle

```
c.o = (pts[i] + pts[j]) / 2;
c.r = pts[i].dis(c.o);
for(int k=0;k<j;k++) {
    if(pts[k].in(c)) continue;
    c = get_circum(pts[i], pts[j], pts[k]);
    }
}
return c;
}</pre>
```

5.11 KDTree (Nearest Point)

```
const int MXN = 100005;
struct KDTree {
  struct Node {
    int x,y,x1,y1,x2,y2;
    int id,f;
    Node *L, *R;
  }tree[MXN];
  int n;
  Node *root:
  LL dis2(int x1, int y1, int x2, int y2) {
    LL dx = x1-x2;
    LL dy = y1-y2;
    return dx*dx+dy*dy;
  static bool cmpx(Node& a, Node& b) { return a.x<b.x; }</pre>
  static bool cmpy(Node& a, Node& b) { return a.y<b.y; }</pre>
  void init(vector<pair<int,int>> ip) {
    n = ip.size();
    for (int i=0; i<n; i++) {</pre>
     tree[i].id = i;
      tree[i].x = ip[i].first;
      tree[i].y = ip[i].second;
    root = build tree(0, n-1, 0);
  Node* build_tree(int L, int R, int dep) {
    if (L>R) return nullptr;
    int M = (L+R)/2;
    tree[M].f = dep%2;
    nth element(tree+L, tree+M, tree+R+1, tree[M].f?
        cmpy : cmpx);
    tree[M].x1 = tree[M].x2 = tree[M].x;
    tree[M].y1 = tree[M].y2 = tree[M].y;
    tree[M].L = build tree(L, M-1, dep+1);
    if (tree[M].L) {
      tree[M].x1 = min(tree[M].x1, tree[M].L->x1);
      tree[M].x2 = max(tree[M].x2, tree[M].L->x2);
      tree[M].y1 = min(tree[M].y1, tree[M].L->y1);
      tree[M].y2 = max(tree[M].y2, tree[M].L->y2);
    tree[M].R = build_tree(M+1, R, dep+1);
    if (tree[M].R) {
     tree[M].x1 = min(tree[M].x1, tree[M].R->x1);
      tree[M].x2 = max(tree[M].x2, tree[M].R->x2);
      tree[M].y1 = min(tree[M].y1, tree[M].R->y1);
      tree[M].y2 = max(tree[M].y2, tree[M].R->y2);
    return tree+M;
  int touch(Node* r, int x, int y, LL d2) {
    LL dis = sqrt(d2)+1;
    if (x<r->x1-dis || x>r->x2+dis ||
       y<r->y1-dis || y>r->y2+dis)
      return 0;
    return 1;
  void nearest(Node* r, int x, int y,
               int &mID, LL &md2) {
    if (!r || !touch(r, x, y, md2)) return;
    LL d2 = dis2(r->x, r->y, x, y);
    if (d2 < md2 || (d2 == md2 && mID < r->id)) {
      mID = r->id;
      md2 = d2;
    // search order depends on split dim
    if ((r->f == 0 \&\& x < r->x) ||
        (r->f == 1 && y < r->y))
      nearest(r->L, x, y, mID, md2);
      nearest(r->R, x, y, mID, md2);
```

} else {

```
nearest(r->R, x, y, mID, md2);
    nearest(r->L, x, y, mID, md2);
}
int query(int x, int y) {
    int id = 1029384756;
    LL d2 = 102938475612345678LL;
    nearest(root, x, y, id, d2);
    return id;
}
}tree;
```

6 Stringology

6.1 Hash

```
class Hash{
private:
  static const int N = 1000000;
  const int p = 127, q = 1208220623;
  int sz, prefix[N], power[N];
  inline int add(int x, int y) {return x+y>=q?x+y-q:x+y
  inline int sub(int x, int y) {return x-y<0?x-y+q:x-y;}</pre>
  inline int mul(int x, int y) {return 1LL*x*y%q;}
  void init(const std::string &x) {
    sz = x.size();
    prefix[0]=0;
    for (int i=1;i<=sz;i++) prefix[i]=add(mul(prefix[i</pre>
        -1], p), x[i-1]);
    power[0]=1;
    for (int i=1;i<=sz;i++) power[i]=mul(power[i-1], p);</pre>
  int query(int 1, int r){
    // 1-base (1, r]
    return sub(prefix[r], mul(prefix[l], power[r-l]));
};
```

6.2 Suffix Array

```
//help by http://www.geeksforgeeks.org/suffix-array-set
    -2-a-nlognlogn-algorithm/
struct sfx{
  int index;
 int r,nr;
char str[N + 10];
int len;
vector<sfx> srs[N + 10];
int mapping[N + 10];
sfx sa[N + 10];
bool cmp(sfx a, sfx b) {
  if(a.r==b.r){
    return a.nr<b.nr;</pre>
  }else{
    return a.r<b.r;</pre>
void SA() {
  len = strlen(str);
  for (int i=0; i<len; i++) {</pre>
    sa[i].index = i;
    sa[i].r=str[i];
    sa[i].nr=(i+1>=len)?0:str[i+1];
  //sort(sa,sa+len,cmp);
  radixSort();
  for (int j=2; j<=len; j*=2) {</pre>
    int cnt=1;
    int rr = sa[0].r;
    sa[0].r=cnt;
    mapping[sa[0].index]=0;
    for (int i=1; i < len; i++) {</pre>
      if(sa[i].r == rr && sa[i].nr == sa[i-1].nr) {
        rr=sa[i].r;
        sa[i].r=cnt;
      }else{
        rr=sa[i].r;
```

```
sa[i].r=++cnt;
      mapping[sa[i].index]=i;
    for(int i=0;i<len;i++) {</pre>
      int nn = sa[i].index+j;
      sa[i].nr = (nn>=len)?0:sa[mapping[nn]].r;
     //sort(sa, sa+len, cmp);
    radixSort();
  }
void radixSort() {
  int m = 0;
  for (int i=0; i<len; i++) {</pre>
    srs[sa[i].nr].PB(sa[i]);
    m=max(m,sa[i].nr);
  int cnt=0;
  for (int i=0;i<=m;i++) {</pre>
    if(srs[i].empty())continue;
    for(auto i:srs[i]){
      sa[cnt++] = j;
    srs[i].clear();
  m = 0;
  for (int i=0; i<len; i++) {</pre>
    srs[sa[i].r].PB(sa[i]);
    m=max(m,sa[i].r);
  cnt=0;
  for (int i=0;i<=m;i++) {</pre>
    if(srs[i].empty())continue;
    for(auto j:srs[i]){
      sa[cnt++] = j;
    srs[i].clear();
```

6.3 KMP

```
int F[N<<1];</pre>
void KMP(char s1[], char s2[], int n, int m) {
  // make F[] for s1+'\0'+s2;
  char ss[N<<1];</pre>
  int len = n+m+1;
  for (int i=0;i<n;i++) ss[i] = s1[i];</pre>
  ss[n] = ' \setminus 0';
  for (int i=0;i<m;i++) ss[i+1+n] = s2[i];</pre>
  F[0] = F[1] = 0;
  for (int i=1;i<len;i++) {</pre>
    int j = F[i];
    while (j > 0 \text{ and } ss[i]!=ss[j]) j = F[j];
    F[i+1] = (ss[i]==ss[j]?j+1:0);
  // just find (F[len2+i] == len2), i from 1 to len+1
      for matching
  [0, i] 是個循環字串,且循環節為i-f[i]:
  if(f[i]>0 and i%(i-f[i])==0) cout << i << " " << i/(i</pre>
       -f[i]) << '\n';
```

6.4 Z value

```
char s[MAXN];
int len,z[MAXN];
void Z_value() {
   int i,j,left,right;
   left=right=0; z[0]=len;
   for(i=1;i<len;i++) {
      j=max(min(z[i-left],right-i),0);
      for(;i+j<len&&s[i+j]==s[j];j++);
      z[i]=j;
      if(i+z[i]>right) {
        right=i+z[i];
      left=i;
    }
}
```

```
| }
|}
```

6.5 Lexicographically Smallest Rotation

```
string mcp(string s) {
  int n = s.length();
  s += s;
  int i=0, j=1;
  while (i<n && j<n) {
    int k = 0;
    while (k < n && s[i+k] == s[j+k]) k++;
    if (s[i+k] <= s[j+k]) j += k+1;
    else i += k+1;
    if (i == j) j++;
  }
  int ans = i < n ? i : j;
  return s.substr(ans, n);
}</pre>
```


7 Misc

7.1 MaximumEmptyRect

```
int largest_empty_rectangle(){
  int max_area = 0;
for (int i=1; i<=n; ++i) {</pre>
    for (int j=1; j<=n; ++j)</pre>
      if (array[i][j]) wl[j] = wl[j-1] + 1;
      else wl[j] = 0;
    for (int j=n; j>=1; --j)
      if (array[i][j]) wr[j] = wr[j+1] + 1;
       else wr[j] = 0;
    for (int j=1; j<=n; ++j)</pre>
      if (array[i][j]) h[j] = h[j] + 1;
      else h[j] = 0;
     for (int j=1; j<=n; ++j)</pre>
      if (1[j] == 0) 1[j] = w1[j];
      else l[j] = min(wl[j], l[j]);
    for (int j=1; j<=n; ++j)</pre>
      if (r[j] == 0) r[j] = wr[j];
      else r[j] = min(wr[j], r[j]);
    for (int j=1; j<=n; ++j)</pre>
      \max \text{ area} = \max(\max \text{ area}, (l[j] + r[j] - 1) * h[j]
           ]);
  return max_area;
```

7.2 DP-opt Condition

7.2.1 totally monotone (concave/convex)

```
\begin{array}{l} \forall i < i', j < j', B[i][j] \leq B[i'][j] \implies B[i][j'] \leq B[i'][j'] \\ \forall i < i', j < j', B[i][j] \geq B[i'][j] \implies B[i][j'] \geq B[i'][j'] \end{array}
```

7.2.2 monge condition (concave/convex)

```
\begin{array}{l} \forall i < i', j < j', B[i][j] + B[i'][j'] \geq B[i][j'] + B[i'][j] \\ \forall i < i', j < j', B[i][j] + B[i'][j'] \leq B[i][j'] + B[i'][j] \end{array}
```

7.3 Convex 1D/1D DP

```
struct segment {
   int i, 1, r;
   segment() {}
   segment(int a, int b, int c): i(a), l(b), r(c) {}
};

inline long long f(int l, int r) {
   return dp[1] + w(1 + 1, r);
}

void solve() {
   dp[0] = 011;
   deque<segment> deq; deq.push_back(segment(0, 1, n));
```