Contents

1 Basic

1.1 Default Code

```cpp
#include <iostream>
#include <iomanip>
#include <string>
#include <algorithm>
#include <vector>
#include <queue>
#include <bitset>
#include <map>
#include <set>
#include <unordered_map>
#include <unordered_set>
#include <cstdio>
#include <cstdlib>
#include <cstring>
#include <ctime>
#include <random>
#include <utility>
#include <stack>
#include <sstream>
#include <functional>
#include <deque>
#include <cassert>
using namespace std;
/* include everything for Kotori~ <3 */

typedef long long lld;
typedef unsigned long long llu;
typedef long double llf;
typedef pair<int,int> PII;
typedef pair<int,lld> PIL;
typedef pair<lld,int> PLI;
typedef pair<lld,lld> PLL;
template<typename T>
using maxHeap = priority_queue<T,vector<T>,less<T>>;
template<typename T>
using minHeap = priority_queue<T,vector<T>,greater<T>>;
/* define some types for Ruby! */

#define FF first
#define SS second
#define SZ(x) (int)(x.size())
#define ALL(x) begin(x), end(x)
#define PB push_back
#define WC(x) while(x--)
/* make code shorter for Di~a~ */

template<typename Iter>
ostream& _out(ostream &s, Iter b, Iter e) {
  s<<"[";
  for ( auto it=b; it!=e; it++ ) s<<(it==b?"":" ")<<*it
      ;
  s<<"]";
  return s;
}
template<typename A, typename B>
ostream& operator <<( ostream &s, const pair<A,B> &p )
    { return s<<"("<<p.FF<<","<<p.SS<<")"; }
template<typename T>
ostream& operator <<( ostream &s, const vector<T> &c )
    { return _out(s,ALL(c)); }
/* make output easier for Ainyan~n~ */

bool debug = 0;
#define DUMP(x) if(debug) cerr<<__PRETTY_FUNCTION__<<":
    "<<__LINE__<<" - "<<#x<<"="<<x<<'\n'
template<typename T>
void DEBUG(const T& x){if(debug) cerr<<x;}
template<typename T, typename... Args>
void DEBUG(const T& head,const Args& ...tail){
  if(debug){cerr<<head; DEBUG(tail...);}
}
/* Let's debug with Nico~Nico~Ni */

int main(int argc, char* argv[]){
  if(argc>1 and string(argv[1])=="-D") debug=1;
  if(!debug){ios_base::sync_with_stdio(0);cin.tie(0);}
  return 0;
}
```

1.2 IncreaseStackSize

```
//stack resize
asm( "mov %0,%%esp\n" ::"g"(mem+10000000) );
//change esp to rsp if 64-bit system

//stack resize (linux)
#include <sys/resource.h>
void increase_stack_size() {
  const rlim_t ks = 64*1024*1024;
  struct rlimit rl;
  int res=getrlimit(RLIMIT_STACK, &rl);
  if(res==0){
    if(rl.rlim_cur<ks){
      rl.rlim_cur=ks;
      res=setrlimit(RLIMIT_STACK, &rl);
    }
  }
}
```

1.3 Pragma optimization

```
#pragma GCC optimize("Ofast,no-stack-protector,no-math-
    errno")
#pragma GCC target("sse,sse2,sse3,ssse3,sse4,popcnt,abm
    ,mmx,avx,tune=native")
```

1.4 IO Optimization

```
// I/O optimization start {{{
static inline int_fast32_t fastAtoi(const char *p,
    uint_fast32_t len) {
  uint_fast32_t res = 0;
  uint_fast8_t neg = *p == '-';
  if (neg) p++, len--;
  switch (len) {
    case 10: res += (*p++ & 15) * 1000000000;
    case 9: res += (*p++ & 15) * 100000000;
    case 8: res += (*p++ & 15) * 10000000;
    case 7: res += (*p++ & 15) * 1000000;
    case 6: res += (*p++ & 15) * 100000;
    case 5: res += (*p++ & 15) * 10000;
    case 4: res += (*p++ & 15) * 1000;
    case 3: res += (*p++ & 15) * 100;
    case 2: res += (*p++ & 15) * 10;
    case 1: res += (*p & 15);
  }
  return res * (neg ? -1 : 1);
}

static inline bool getRawChar(char *c) {
  static char buf[1 << 20], *p = buf, *end = buf;
  if (p == end) {
    if ((end = buf + fread(buf, 1, 1 << 20, stdin)) ==
        buf) return false;
    p = buf;
  }
  *c = *p++;
  return true;
}

static inline bool getInt(int32_t *x) {
  static char buf[12];
  uint_fast32_t i = 0;
  while (getRawChar(buf + i)) {
    if ((unsigned)(buf[i] - '0') > 10U && buf[i] != '-'
        ) {
      if (i) break;
      else continue;
    }
    i++;
  }
  if (!i) return false;
  *x = fastAtoi(buf, i);
  return true;
}
// I/O optimization end }}}
```

2 Data Structure

2.1 Bigint

```
struct Bigint{
  static const int LEN = 60;
  static const int BIGMOD = 10000;

  int s;
  int vl, v[LEN];
  //  vector<int> v;
  Bigint() : s(1) { vl = 0; }
  Bigint(long long a) {
    s = 1; vl = 0;
    if (a < 0) { s = -1; a = -a; }
    while (a) {
      push_back(a % BIGMOD);
      a /= BIGMOD;
    }
  }
  Bigint(string str) {
    s = 1; vl = 0;
    int stPos = 0, num = 0;
    if (!str.empty() && str[0] == '-') {
      stPos = 1;
      s = -1;
    }
    for (int i=SZ(str)-1, q=1; i>=stPos; i--) {
      num += (str[i] - '0') * q;
      if ((q *= 10) >= BIGMOD) {
        push_back(num);
        num = 0; q = 1;
      }
    }
    if (num) push_back(num);
    n();
  }

  int len() const {
    return vl;
    //    return SZ(v);
  }
  bool empty() const { return len() == 0; }
  void push_back(int x) {
    v[vl++] = x;
    //    v.PB(x);
  }
  void pop_back() {
    vl--;
    //    v.pop_back();
  }
  int back() const {
    return v[vl-1];
    //    return v.back();
  }
  void n() {
    while (!empty() && !back()) pop_back();
  }
  void resize(int nl) {
    vl = nl;
    fill(v, v+vl, 0);
    //    v.resize(nl);
    //    fill(ALL(v), 0);
  }

  void print() const {
    if (empty()) { putchar('0'); return; }
    if (s == -1) putchar('-');
    printf("%d", back());
    for (int i=len()-2; i>=0; i--) printf("%.4d",v[i]);
  }
  friend std::ostream& operator << (std::ostream& out,
      const Bigint &a) {
    if (a.empty()) { out << "0"; return out; }
    if (a.s == -1) out << "-";
    out << a.back();
    for (int i=a.len()-2; i>=0; i--) {
      char str[10];
      snprintf(str, 5, "%.4d", a.v[i]);
      out << str;
    }
    return out;
  }
```

```
int cp3(const Bigint &b)const {
  if (s != b.s) return s - b.s;
  if (s == -1) return -(-*this).cp3(-b);
  if (len() != b.len()) return len()-b.len();//int
  for (int i=len()-1; i>=0; i--)
    if (v[i]!=b.v[i]) return v[i]-b.v[i];
  return 0;
}

bool operator < (const Bigint &b)const{ return cp3(b)
    <0; }
bool operator <= (const Bigint &b)const{ return cp3(b
    )<=0; }
bool operator == (const Bigint &b)const{ return cp3(b
    )==0; }
bool operator != (const Bigint &b)const{ return cp3(b
    )!=0; }
bool operator > (const Bigint &b)const{ return cp3(b)
    >0; }
bool operator >= (const Bigint &b)const{ return cp3(b
    )>=0; }

Bigint operator - () const {
  Bigint r = (*this);
  r.s = -r.s;
  return r;
}
Bigint operator + (const Bigint &b) const {
  if (s == -1) return -(-(*this)+(-b));
  if (b.s == -1) return (*this)-(-b);
  Bigint r;
  int nl = max(len(), b.len());
  r.resize(nl + 1);
  for (int i=0; i<nl; i++) {
    if (i < len()) r.v[i] += v[i];
    if (i < b.len()) r.v[i] += b.v[i];
    if(r.v[i] >= BIGMOD) {
      r.v[i+1] += r.v[i] / BIGMOD;
      r.v[i] %= BIGMOD;
    }
  }
  r.n();
  return r;
}
Bigint operator - (const Bigint &b) const {
  if (s == -1) return -(-(*this)-(-b));
  if (b.s == -1) return (*this)+(-b);
  if ((*this) < b) return -(b-(*this));
  Bigint r;
  r.resize(len());
  for (int i=0; i<len(); i++) {
    r.v[i] += v[i];
    if (i < b.len()) r.v[i] -= b.v[i];
    if (r.v[i] < 0) {
      r.v[i] += BIGMOD;
      r.v[i+1]--;
    }
  }
  r.n();
  return r;
}
Bigint operator * (const Bigint &b) {
  Bigint r;
  r.resize(len() + b.len() + 1);
  r.s = s * b.s;
  for (int i=0; i<len(); i++) {
    for (int j=0; j<b.len(); j++) {
      r.v[i+j] += v[i] * b.v[j];
      if(r.v[i+j] >= BIGMOD) {
        r.v[i+j+1] += r.v[i+j] / BIGMOD;
        r.v[i+j] %= BIGMOD;
      }
    }
  }
  r.n();
  return r;
}
Bigint operator / (const Bigint &b) {
  Bigint r;
  r.resize(max(1, len()-b.len()+1));
  int oriS = s;
  Bigint b2 = b; // b2 = abs(b)
  s = b2.s = r.s = 1;
  for (int i=r.len()-1; i>=0; i--) {
    int d=0, u=BIGMOD-1;
    while(d<u) {
      int m = (d+u+1)>>1;
      r.v[i] = m;
      if((r*b2) > (*this)) u = m-1;
      else d = m;
    }
    r.v[i] = d;
  }
  s = oriS;
  r.s = s * b.s;
  r.n();
  return r;
}
Bigint operator % (const Bigint &b) {
  return (*this)-(*this)/b*b;
}
};
```

2.2 Fraction

```
/************************
 n為分子，d為分母
 若分數為0則n=0,d=1
 若為負數則負號加在分子
 必定約到最簡分數
************************/
#ifndef SUNMOON_FRACTION
#define SUNMOON_FRACTION
#include<algorithm>
template<typename T>
struct fraction{
  T n,d;
  fraction(const T &_n=0,const T &_d=1):n(_n),d(_d){
    T t=std::__gcd(n,d);
    n/=t,d/=t;
    if(d<0)n=-n,d=-d;
  }
  fraction operator-()const{
    return fraction(-n,d);
  }
  fraction operator+(const fraction &b)const{
    return fraction(n*b.d+b.n*d,d*b.d);
  }
  fraction operator-(const fraction &b)const{
    return fraction(n*b.d-b.n*d,d*b.d);
  }
  fraction operator*(const fraction &b)const{
    return fraction(n*b.n,d*b.d);
  }
  fraction operator/(const fraction &b)const{
    return fraction(n*b.d,d*b.n);
  }
  fraction operator+=(const fraction &b){
    return *this=fraction(n*b.d+b.n*d,d*b.d);
  }
  fraction operator-=(const fraction &b){
    return *this=fraction(n*b.d-b.n*d,d*b.d);
  }
  fraction operator*=(const fraction &b){
    return *this=fraction(n*b.n,d*b.d);
  }
  fraction operator/=(const fraction &b){
    return *this=fraction(n*b.d,d*b.n);
  }
  bool operator <(const fraction &b)const{
    return n*b.d<b.n*d;
  }
  bool operator >(const fraction &b)const{
    return n*b.d>b.n*d;
  }
  bool operator ==(const fraction &b)const{
    return n*b.d==b.n*d;
  }
  bool operator <=(const fraction &b)const{
    return n*b.d<=b.n*d;
  }
  bool operator >=(const fraction &b)const{
    return n*b.d>=b.n*d;
  }
};
#endif
```

2.3 ScientificNotation

```
#include <cmath>
#include <cstdio>
#include <iostream>
#include <algorithm>

struct SciFi{
    typedef double base_t;
  base_t x; int p;
  SciFi(){x=0;p=0;}
  SciFi(base_t k){
    p = floor(log10(k));
    x = k / pow((base_t)10, p);
  }
  SciFi(base_t a, int b){
    x=a;p=b;
  }
  SciFi operator=(base_t k){
    p = floor(log10(k));
    x = k / pow((base_t)10, p);
    return *this;
  }
  SciFi operator*(SciFi k)const{
    int nP = p+k.p;
    base_t nX = x*k.x;
    int tp = floor(log10(nX));
    return SciFi(nX/pow((base_t)10, tp), nP+tp);
  }
  SciFi operator*=(SciFi k){
    p+=k.p;
    x*=k.x;
    int tp = floor(log10(x));
    p+=tp;
    x/=pow((base_t)10, tp);
    return *this;
  }
  SciFi operator+(SciFi k)const{
    int newP = std::min(k.p, p);
    base_t x1 = x*pow((base_t)10, p-newP);
    base_t x2 = k.x*pow((base_t)10, k.p-newP);
    x1+=x2;
    int tp = floor(log10(x1));
    newP+=tp;
    x1 /= pow((base_t)10, tp);
    return SciFi(x1, newP);
  }
  SciFi operator+=(SciFi k){
    int newP = std::min(k.p, p);
    base_t x1 = x*pow((base_t)10, p-newP);
    base_t x2 = k.x*pow((base_t)10, k.p-newP);
    x1+=x2;
    int tp = floor(log10(x1));
    newP+=tp;
    x1 /= pow((base_t)10, tp);
    x=x1;p=newP;
    return *this;
  }
  bool operator<(SciFi a)const{
    if(p == a.p) return x<a.x;
    return p<a.p;
  }
  bool operator>(SciFi a)const{
    if(p == a.p) return x>a.x;
    return p>a.p;
  }
  bool operator==(SciFi a)const{
    return p==a.p and x==a.x;
  }
};

int main(){
  double a; scanf("%lf",&a);
  SciFi aa=a, x;
  x = aa*SciFi(2);
  printf("%.2lfe%c%03d\n", x.x, "+-"[x.p<0], abs(x.p));
  return 0;
}
```

2.4 unordered_map

```
#include <ext/pb_ds/assoc_container.hpp>
using __gnu_pbds::cc_hash_table;
using __gnu_pbds::gp_hash_table;
template<typename A, typename B> using hTable1 =
    cc_hash_table<A,B>;
template<typename A, typename B> using hTable2 =
    gp_hash_table<A,B>;
```

2.5 extc_balance_tree

```
#include <functional>
#include <ext/pb_ds/assoc_container.hpp>
using std::less;
using std::greater;
using __gnu_pbds::tree;
using __gnu_pbds::rb_tree_tag;
using __gnu_pbds::ov_tree_tag;
using __gnu_pbds::splay_tree_tag;
using __gnu_pbds::null_type;
using __gnu_pbds::tree_order_statistics_node_update;

template<typename T>
using ordered_set = tree<T, null_type, less<T>,
    rb_tree_tag, tree_order_statistics_node_update>;

template<typename A, B>
using ordered_map = tree<A, B, less<A>, rb_tree_tag,
    tree_order_statistics_node_update>;

int main(){
  ordered_set<int> ss;
  ordered_map<int,int> mm;
  ss.insert(1);
  ss.insert(5);
  assert(*ss.find_by_order(0)==1);
  assert(ss.order_of_key(-1)==0);
  assert(ss.order_of_key(87)==2);
  return 0;
}
```

2.6 extc_heap

```
#include <functional>
#include <ext/pb_ds/assoc_container.hpp>
#include <ext/pb_ds/priority_queue.hpp>
using std::less;
using std::greater;
using __gnu_pbds::priority_queue;
using __gnu_pbds::pairing_heap_tag;
using __gnu_pbds::binary_heap_tag;
using __gnu_pbds::binomial_heap_tag;
using __gnu_pbds::rc_binomial_heap_tag;
using __gnu_pbds::thin_heap_tag;

int main(){
  priority_queue<int,less<int>,pairing_heap_tag> pq1,
      pq2;
  pq1.push(1);
  pq2.push(2);
  pq1.join(pq2);
  assert(pq2.size()==0);
  auto it = pq1.push(87);
  pq1.modify(it, 19);
  while(!pq1.empty()){
    pq1.top();
    pq1.pop();
  }
  return 0;
}
```

2.7 PairingHeap

```
#include <vector>
using std::vector;

template<class __type, class __cmp=less<__type>>
class pairingHeap{
  private:
      struct pairingNode{
          __type val;
            vector<pairingNode*> child;
```

```
            pairingNode(){
                val = 0;
                child.clear();
            }
            pairingNode(int x): val(x){
                child.clear();
            }
    };
    pairingNode* root;
    int count;
    __cmp _cp;
    void remove(pairingNode* cur){
        if(cur==nullptr) return;
        for(auto i: cur->child) remove(i);
        delete cur;
    }
  public:
    pairingHeap(){root=nullptr;count=0;}
    inline bool empty(){return count==0;}
    inline __type top(){return root->val;}
    inline int size(){return count;}
    inline void clear(){remove(root);root=nullptr;count
        =0;}
    inline void push(__type a){
      count++;
      auto mynode = new pairingNode(a);
      if(root==nullptr) root = mynode;
      else{
        if(_cp(root->val, mynode->val)) swap(root,
            mynode);
        root->child.push_back(mynode);
      }
    }
    inline void pop(){
      count--;
      queue<pairingNode*> que;
      for(auto i:root->child) que.push(i);
      delete root;
      while(que.size() > 1){
        auto tp1=que.front();que.pop();
        auto tp2=que.front();que.pop();
        if(_cp(tp1->val, tp2->val)) swap(tp1, tp2);
        tp1->child.push_back(tp2);
        que.push(tp1);
      }
      if(que.empty()) root=nullptr;
      else root = que.front();
    }
    inline void join(pairingHeap<__type, __cmp>& pq2){
        if(_cp(root->val, pq2.root->val)) swap(root,
            pq2.root);
        root->child.push_back(pq2.root);
      count += pq2.count;
        pq2.root = nullptr;
        pq2.count = 0;
    }
};

int main(){
  pairingHeap<int> pq1, pq2;
  for(int i=0;i<1e5;i++) pq1.push(i);
  for(int i=1e5;i<2e5;i++) pq2.push(i);
  pq1.join(pq2);
  while(!pq1.empty()){
    // cout<<pq1.top()<<" ";
    pq1.pop();
  }
  return 0;
}
```

2.8 Disjoint Set

```
class DJS{
  private:
    vector<int> fa, sz, sv;
    vector<pair<int*, int>> opt;
    inline void assign(int *k, int v){
      opt.PB({k, *k});
      *k = v;
    }
  public:
    inline void init(int n){
      fa.resize(n);
      sz.resize(n);
      for(int i=0;i<n;i++){
        fa[i] = i;
        sz[i] = 1;
      }
      opt.clear();
    }
    int query(int x){
      if(fa[x] == x) return x;
      return query(fa[x]);
    }
    inline void merge(int a, int b){
      int af = query(a), bf = query(b);
      if(af == bf) return;
      if(sz[af] < sz[bf]) swap(af, bf);
      assign(&fa[bf], fa[af]);
      assign(&sz[af], sz[af]+sz[bf]);
    }
    inline void save(){sv.PB(SZ(opt));}
    inline void undo(){
      int ls = sv.back(); sv.pop_back();
      while(SZ(opt) > ls){
        pair<int*, int> cur=opt.back();
        *cur.FF = cur.SS;
        opt.pop_back();
      }
    }
};
```

2.9 Treap

```
#include <cstdlib>

class Treap{
  private:
    const int MEM = 500000 + 5;
    unsigned seed;
    inline unsigned myrand(){
      static unsigned seed = time(NULL);
      seed = seed*seed*127 + seed*227 + 2147483587;
      seed ^= seed*97;
      seed /= 7123;
      return seed;
    }
    struct node{
      node *lc, *rc;
      int pri, size, val;
      node(){}
      node(int x):
        lc(nullptr),
        rc(nullptr),
        pri(myrand()),
        size(1),
        val(x)
        {}
      inline void pull(){
        size = 1;
        if(lc) size += lc->size;
        if(rc) size += rc->size;
      }
    } *root, pool[MEM];
    int mem_;
    inline node* new_node(int x){
      static int mem_ = 0;
      assert(mem_ < MEM);
      pool[mem_]=node(x);
      return &pool[mem_++];
    }
    inline int sz(node* x){return x?x->size:0;}
    node* merge(node *a, node *b){
      if(!a or !b) return a?a:b;
      if(a->pri > b->pri){
        a->rc = merge(a->rc, b);
        a->pull();
        return a;
      }else{
        b->lc = merge(a, b->lc);
        b->pull();
        return b;
      }
    }
    void split(Treap* t, int k, Treap*& a, Treap*& b){
      if(!t) a=b=nullptr;
      else if(sz(t->lc) < k){
        a = t;
```

```
        split(t->rc, k - sz(t->lc) - 1 , a->rc, b);
        a->pull();
      }else{
        b = t;
        split(t->lc, k, a, b->lc);
        b->pull();
      }
    }
    int oOk(node* rr, int x){
      if(rr==NULL)return 0;
      if((rr->val) < x)return gSize(rr->l)+oOk(rr->r, x
          )+1;
      else return oOk(rr->l, x);
    }
  public:
    Treap(){root=nullptr;seed=time(NULL);mem_=0;}
    void do_something_at(int l, int r){
      // 1-base [l, r]
      split(root, l-1, tl, root);
      split(root, r-l+1, root, tr);
      root = merge(tl, merge(root, tr));
    }
    void insert(int x){
      node *a, *b;
      split(root, x, a, b);
      root = merge(merge(a, new node(x)), b);
      root->size = gSize(root->l)+gSize(root->r)+1;
    }
    void remove(int x){
      //need debug may contain bugs
      node *a, *b, *c, *d;
      split(root, x, a, b);
      a->size = gSize(a->l)+gSize(a->r);
      split(a, x-1, c, d);
      root = merge(b, c);
      root->size = gSize(root->l)+gSize(root->r);
      delete d;
    }
    int order_of_key(int x){return oOk(root,x);}
};

int main(){

  return 0;
}
```

2.10 SparseTable

```
#include <algorithm>
using std::min;

const int N = 1<<20;
const int LOG_N = 21;

class SparseTable{
  private:
    int table[N][LOG_N];
  public:
    void build(int n, int arr[]){
      // [1, n]
      for(int i=1;i<=n;i++) table[i][0] = arr[i];
      for(int j=1;(1<<j)<=n;j++){
        for(int i=1;i+(1<<j)-1<=n;i++){
          table[i][j] = min(table[i][j-1], table[i
              +(1<<(j-1))][j-1]);
        }
      }
    }
    int query(int l, int r){
      // 1-base [l, r]
      int k = 31-__builtin_clz(r-l+1);
      return min(table[l][k], table[r-(1<<k)+1][k]);
    }
};
```

2.11 FenwickTree

```
#include <vector>
using std::vector;

template<typename T>
class BIT{
    #define ALL(x) begin(x), end(x)
  private:
    vector<T> arr;
    int n;
    inline int lowbit(int x){return x & (-x);}
    T query(int x){
      T ret = 0;
      while(x > 0){
        ret += arr[x];
        x -= lowbit(x);
      }
      return ret;
    }
  public:
    void init(int n_){
      n = n_;
      arr.resize(n);
      fill(ALL(arr), 0);
    }
    void modify(int pos, T v){
      while(pos < n){
        arr[pos] += v;
        pos += lowbit(pos);
      }
    }
    T query(int l, int r){
      // 1-base (l, r]
      return query(r) - query(l);
        }
    #undef ALL
};

template<typename T>
class BIT{
    #define ALL(x) begin(x), end(x)
  private:
        vector<T> arr;
        int n;
        inline int lowbit(int x){return x & (-x);}
        void add(int s, int v){
      while(s){
        arr[s]+=v;
        s-=lowbit(s);
      }
    }
  public:
    void init(int n_){
            n = n_;
            arr.resize(n);
            fill(ALL(arr), 0);
    }
    void add(int l, int r, T v){
            //1-base (l, r]
      add(l, -v);
      add(r, v);
    }
    T query(int x){
      T r=0;
      while(x<size){
        r+=arr[x];
        x+=lowbit(x);
      }
      return r;
        }
    #undef ALL
};
```

3 Graph

3.1 BCC Edge

```
class BCC{
  private:
    int low[N], dfn[N], cnt;
    bool bcc[N];
    vector<PII> G[N];
    void dfs(int w, int f){
      dfn[w] = cnt++;
      low[w] = dfn[w];
      for(auto i: G[w]){
        int u = i.FF, t = i.SS;
        if(u == f) continue;
```

```
      if(dfn[u]!=0){
        low[w] = min(low[w], dfn[u]);
      }else{
        dfs(u, w);
        low[w] = min(low[w], low[u]);
        if(low[u] > dfn[w]) bcc[t] = true;
      }
    }
  }
public:
  void init(int n, int m){
    for(int i=0;i<n;i++) G[i].clear();
    fill(bcc, bcc+m, false);
    cnt = 0;
  }
  void add_edge(int u, int v){
    G[u].PB({v, cnt});
    G[v].PB({u, cnt});
    cnt++;
  }
  void solve(){cnt = 1;dfs(0, 0);}
  // the id will be same as insert order, 0-base
  bool is_bcc(int x){return bcc[x];}
} bcc;
```

3.2 BCC Vertex

```
struct BccVertex {
  int n,nBcc,step,root,dfn[MXN],low[MXN];
  vector<int> E[MXN], ap;
  vector<pii> bcc[MXN];
  int top;
  pii stk[MXN];
  void init(int _n) {
    n = _n;
    nBcc = step = 0;
    for (int i=0; i<n; i++) E[i].clear();
  }
  void add_edge(int u, int v) {
    E[u].PB(v);
    E[v].PB(u);
  }
  void DFS(int u, int f) {
    dfn[u] = low[u] = step++;
    int son = 0;
    for (auto v:E[u]) {
      if (v == f) continue;
      if (dfn[v] == -1) {
        son++;
        stk[top++] = {u,v};
        DFS(v,u);
        if (low[v] >= dfn[u]) {
          if(v != root) ap.PB(v);
          do {
            assert(top > 0);
            bcc[nBcc].PB(stk[--top]);
          } while (stk[top] != pii(u,v));
          nBcc++;
        }
        low[u] = min(low[u], low[v]);
      } else {
        if (dfn[v] < dfn[u]) stk[top++] = pii(u,v);
        low[u] = min(low[u],dfn[v]);
      }
    }
    if (u == root && son > 1) ap.PB(u);
  }
  // return the edges of each bcc;
  vector<vector<pii>> solve() {
    vector<vector<pii>> res;
    for (int i=0; i<n; i++) {
      dfn[i] = low[i] = -1;
    }
    ap.clear();
    for (int i=0; i<n; i++) {
      if (dfn[i] == -1) {
        top = 0;
        root = i;
        DFS(i,i);
      }
    }
    REP(i,nBcc) res.PB(bcc[i]);
    return res;
  }
}
```

3.3 Strongly Connected Components

```
class SCC{
  private:
    int n, num_;
    vector<int> G[N], rG[N], ord, num;
    bool vis[N];
    void dfs(int u){
      if(vis[u]) return;
      vis[u]=1;
      for(auto v: G[u]) dfs(v);
      ord.PB(u);
    }
    void rdfs(int u){
      if(vis[u]) return;
      num[u] = num_;
      vis[u] = 1;
      for(auto v: rG[u]) rdfs(v);
    }
  public:
    inline void init(int n_){
      n=n_, num_=0;
      num.resize(n);
      for(int i=0;i<n;i++) G[i].clear();
      for(int i=0;i<n;i++) rG[i].clear();
    }
    inline void add_edge(int st, int ed){
      G[st].PB(ed);
      rG[ed].PB(st);
    }
    void solve(){
      memset(vis, 0, sizeof(vis));
      for(int i=0;i<n;i++){
        if(!vis[i]) dfs(i);
      }
      reverse(ALL(ord));
      memset(vis, 0, sizeof(vis));
      for(auto i: ord){
        if(!vis[i]){
          rdfs(i);
          num_++;
        }
      }
    }
    inline int get_id(int x){return num[x];}
    inline int count(){return num_;}
} scc;
```

3.4 Articulation Point

```
#include <bits/stdc++.h>
using namespace std;
#define N 1000000+5

class AP{
  private:
    vector<int> graph[N];
    bitset<N> visited, result;
    int low[N], lv[N];
    void dfs(int x, int f, int cnt){
      low[x]=cnt;
      lv[x]=cnt;
      visited[x]=1;
      int child=0;
      for(auto i:graph[x]){
        if(i!=f){
          if(visited[i]){
            low[x] = min(low[x], low[i]);
          }else{
            child++;
            dfs(i,x,cnt+1);
            low[x] = min(low[x], low[i]);
            if(low[i] >= lv[x]) result[x]=1;
          }
        }
      }
      if(lv[x]==1 && child <= 1)
        result[x]=0;
    }
  public:
```

```
    void init(int sz){
      for(int i=0;i<sz;i++) graph[i].clear();
      visited.reset(); result.reset();
    }
    void AddEdge(int u, int v){
      graph[u].push_back(v);
      graph[v].push_back(u);
    }
    void solve(){
      dfs(1, 1, 1);
    }
    bool isAP(int x){
      return result[x];
    }
} ap;

int main(){
  int n,m;cin>>n>>m;
  ap.init(n+2);
  for(int i=0;i<m;i++){
    int st,ed;cin>>st>>ed;
    ap.AddEdge(st, ed);
  }
  ap.solve();
  for(int i=1;i<=n;i++) if(ap.isAP(i)) cout<<i<<'\n';
  return 0;
}
```

3.5 Bipartie Matching

```
#include <bits/stdc++.h>
using namespace std;
#define N 500

class BipartieMatching{
  private:
    vector<int> X[N], Y[N];
    int fX[N], fY[N], n;
    bitset<N> walked;
    bool dfs(int x){
      for(auto i:X[x]){
        if(walked[i])continue;
        walked[i]=1;
        if(fY[i]==-1||dfs(fY[i])){
          fY[i]=x;fX[x]=i;
          return 1;
        }
      }
      return 0;
    }
  public:
    void init(int _n){
      n=_n;
      for(int i=0;i<n;i++){
        X[i].clear();
        Y[i].clear());
        fX[i]=fY[i]=-1;
      }
      walked.reset();
    }
    void AddEdge(int x, int y){
      X[x].push_back(y);
      Y[y].push_back(y);
    }
    int solve(){
      int cnt = 0;
      for(int i=0;i<n;i++){
        walked.reset();
        if(dfs(i)) cnt++;
      }
      // return how many pair matched
      return cnt;
    }
};
```

3.6 MinimumCostMaximumFlow

```
class MiniCostMaxiFlow{
  typedef int CapT;
  typedef lld WeiT;
  typedef pair<CapT, WeiT> PCW;
  const CapT INF_CAP = 1<<30;
  const WeiT INF_WEI = 1LL<<60;
  const int MAXV = N;
  private:
    struct Edge{
      int to, back;
      WeiT wei;
      CapT cap;
      Edge(){}
      Edge(int a, int b, WeiT c, CapT d): to(a), back(b
          ), wei(c), cap(d) {}
    };
    int ori, edd, V;
    vector<Edge> G[MAXV];
    int fa[MAXV], wh[MAXV];
    bool inq[MAXV];
    WeiT dis[MAXV];
    PCW SPFA(){
      for(int i=0;i<V;i++) inq[i]=0;
      for(int i=0;i<V;i++) dis[i]=INF_WEI;
      queue<int> qq;
      qq.push(ori);
      dis[ori]=0;
      while(!qq.empty()){
        int u = qq.front(); qq.pop();
        inq[u]=0;
        for(int i=0;i<SZ(G[u]);i++){
          Edge e = G[u][i];
          int v = e.to;
          WeiT d = e.wei;
          if(e.cap > 0 and dis[v] > dis[u]+d){
            dis[v]=dis[u]+d;
            fa[v]=u;
            wh[v] = i;
            if(inq[v]) continue;
            qq.push(v);
            inq[v]=1;
          }
        }
      }
      if(dis[edd]==INF_WEI) return {-1, -1};
      CapT mw=INF_CAP;
      for(int i=edd;i!=ori;i=fa[i]){
        mw = min(mw, G[fa[i]][wh[i]].cap);
      }
      for(int i=edd;i!=ori;i=fa[i]){
        auto &eg = G[fa[i]][wh[i]];
        eg.cap -= mw;
        G[eg.to][eg.back].cap += mw;
      }
      return {mw, dis[edd]};
    }
  public:
    void init(int a, int b, int n=MAXV){
      V=n;
      ori = a;
      edd = b;
      for(int i=0;i<n;i++) G[i].clear();
    }
    void addEdge(int st, int ed, WeiT w, CapT c){
      G[st].PB(Edge(ed, SZ(G[ed]), w, c));
      G[ed].PB(Edge(st, SZ(G[st])-1, -w, 0));
    }
    PCW solve(){
      CapT cc=0; WeiT ww=0;
      while(true){
        PCW ret = SPFA();
        if(ret.FF==-1) break;
        cc += ret.FF;
        ww += ret.SS;
      }
      return {cc, ww};
    }
} mcmf;
```

4 Math

4.1 ax+by=gcd

```
// By Adrien1018 (not knowing how to use.
// ax+ny = 1, ax+ny == ax == 1 (mod n)
tuple<int, int, int> extended_gcd(int a, int b) {
  if (!b) return make_tuple(a, 1, 0);
```

```
  int d, x, y;
  tie(d, x, y) = extended_gcd(b, a % b);
  return make_tuple(d, y, x - (a / b) * y);
}
// ax+by = gcd (by Eddy1021
PII gcd(int a, int b){
  if(b == 0) return {1, 0};
  PII q = gcd(b, a % b);
  return {q.second, q.first - q.second * (a / b)};
}
```

4.2 Pollard Rho

```
// coded by hanhanW
// does not work when n is prime
long long modit(long long x,long long mod) {
  if(x>=mod) x-=mod;
  //if(x<0) x+=mod;
  return x;
}
long long mult(long long x,long long y,long long mod) {
  long long s=0,m=x%mod;
  while(y) {
    if(y&1) s=modit(s+m,mod);
    y>>=1;
    m=modit(m+m,mod);
  }
  return s;
}
long long f(long long x,long long mod) {
  return modit(mult(x,x,mod)+1,mod);
}
long long pollard_rho(long long n) {
  if(!(n&1)) return 2;
  while (true) {
    long long y=2, x=rand()%(n-1)+1, res=1;
    for (int sz=2; res==1; sz*=2) {
      for (int i=0; i<sz && res<=1; i++) {
        x = f(x, n);
        res = __gcd(abs(x-y), n);
      }
      y = x;
    }
    if (res!=0 && res!=n) return res;
  }
}
```

4.3 Linear Sieve

```
const int N = 20000000;
bool sieve[N];

void linear_sieve(){
  vector<int> prime;
  for (int i=2; i<N; i++){
    if (!sieve[i]) prime.push_back(i);
    for (int j=0; i*prime[j]<N; j++)
    {
      sieve[i*prime[j]] = true;
      if (i % prime[j] == 0) break;
    }
  }
}
```

4.4 NloglogN Sieve

```
bool notprime[N];
vector<int> primes;

void Sieve(int n){
  // reverse true false for quicker
  for(int i=2;i<=n;i++){
    if(!notprime[i]){
      primes.push_back(i);
      for(int j=i*i;j<=n;j+=i) notprime[i]=true;
    }
  }
}
```

4.5 Miller Rabin

```
template<typename T>
inline T pow(T a,T b,T mod){// a^b mod mod
  T ret=1;
  while(b){
    if(b&1) ret=(ret*a)%mod;
    b>>=1;
    a = (a*a)%mod;
  }
  return ret%mod;
}
int sprp[3]={2,7,61};// for int range
int llsprp
    [7]={2,325,9375,28178,450775,9780504,1795265022};//
     at least unsigned long long

template<typename T>
inline bool isprime(T n,int *sprp,int num){
  if(n==2)return 1;
  if(n<2||n%2==0)return 0;
  int t=0;
  T u=n-1;
  for(;u%2==0;++t)u>>=1;
  for(int i=0;i<num;++i){
    T a=sprp[i]%n;
    if(a==0 or a==1 or a==n-1)continue;
    T x=pow(a,u,n);
    if(x==1 or x==n-1)continue;
    for(int j=0;j<t;++j){
      x=(x*x)%n;
      if(x==1)return 0;
      if(x==n-1)break;
    }
    if(x==n-1)continue;
    return 0;
  }
  return 1;
}
```

4.6 Inverse Element

```
// x's inverse mod k
// if k is prime
long long GetInv(long long x, long long k){
  return qPow(x, k-2);
}

inline long long Euler(long long x){
  long long r=1;
  for(long long i=2;i*i<=x;++i){
    if(x%i==0){
      x/=i;
      r*=(i-1);
      while(x%i==0){
        x/=i;
        r*=i;
      }
    }
  }
  if(x>1) r*=x-1;
  return r;
}
// x's inverse mod k
// if k is not prime
long long GetInv(long long x, long long k){
  return qPow(x, Euler(k)-1);
}
// or extended_gcd(x, k).second
// if you need [1, x] (most use: [1, k-1]
void solve(int x, long long k){
  inv[1] = 1;
  for(int i=2;i<x;i++)
    inv[i] = ((long long)(k - k/i) * inv[k % i]) % k;
}
```

4.7 Fast Fourier Transform

```
// const int MAXN = 262144;
// (must be 2^k)
// before any usage, run pre_fft() first
```

```
//
// To implement poly. multiply:
//
// fft( n , a );
// fft( n , b );
// for( int i = 0 ; i < n ; i++ )
//   c[ i ] = a[ i ] * b[ i ];
// fft( n , c , 1 );
//
// then you have the result in c :: [cplx]
typedef long double ld;
typedef complex<ld> cplx;
const ld PI = acosl(-1);
const cplx I(0, 1);
cplx omega[MAXN+1];
void pre_fft(){
  for(int i=0; i<=MAXN; i++)
    omega[i] = exp(i * 2 * PI / MAXN * I);
}
// n must be 2^k
void fft(int n, cplx a[], bool inv=false){
  int basic = MAXN / n;
  int theta = basic;
  for (int m = n; m >= 2; m >>= 1) {
    int mh = m >> 1;
    for (int i = 0; i < mh; i++) {
      cplx w = omega[inv ? MAXN-(i*theta%MAXN)
                         : i*theta%MAXN];
      for (int j = i; j < n; j += m) {
        int k = j + mh;
        cplx x = a[j] - a[k];
        a[j] += a[k];
        a[k] = w * x;
      }
    }
    theta = (theta * 2) % MAXN;
  }
  int i = 0;
  for (int j = 1; j < n - 1; j++) {
    for (int k = n >> 1; k > (i ^= k); k >>= 1);
    if (j < i) swap(a[i], a[j]);
  }
  if (inv)
    for (i = 0; i < n; i++)
      a[i] /= n;
}
```

4.8 NTT

```
typedef long long LL;
// Remember coefficient are mod P
/* p=a*2^n+1
   n    2^n          p           a     root
   5    32           97          3     5
   6    64           193         3     5
   7    128          257         2     3
   8    256          257         1     3
   9    512          7681        15    17
   10   1024         12289       12    11
   11   2048         12289       6     11
   12   4096         12289       3     11
   13   8192         40961       5     3
   14   16384        65537       4     3
   15   32768        65537       2     3
   16   65536        65537       1     3
   17   131072       786433      6     10
   18   262144       786433      3     10 (605028353,
       2308, 3)
   19   524288       5767169     11    3
   20   1048576      7340033     7     3
   21   2097152      23068673    11    3
   22   4194304      104857601   25    3
   23   8388608      167772161   20    3
   24   16777216     167772161   10    3
   25   33554432     167772161   5     3 (1107296257, 33,
       10)
   26   67108864     469762049   7     3
   27   134217728    2013265921  15    31 */
// (must be 2^k)
// To implement poly. multiply:
// NTT<P, root, MAXN> ntt;
// ntt( n , a ); // or ntt.tran( n , a );
// ntt( n , b );
// for( int i = 0 ; i < n ; i++ )
//   c[ i ] = a[ i ] * b[ i ];
// ntt( n , c , 1 );
//
// then you have the result in c :: [LL]

template<LL P, LL root, int MAXN>
struct NTT{
  static LL bigmod(LL a, LL b) {
    LL res = 1;
    for (LL bs = a; b; b >>= 1, bs = (bs * bs) % P) {
      if(b&1) res=(res*bs)%P;
    }
    return res;
  }
  static LL inv(LL a, LL b) {
    if(a==1)return 1;
    return (((LL)(a-inv(b%a,a))*b+1)/a)%b;
  }
  LL omega[MAXN+1];
  NTT() {
    omega[0] = 1;
    LL r = bigmod(root, (P-1)/MAXN);
    for (int i=1; i<=MAXN; i++)
      omega[i] = (omega[i-1]*r)%P;
  }
  // n must be 2^k
  void tran(int n, LL a[], bool inv_ntt=false){
    int basic = MAXN / n;
    int theta = basic;
    for (int m = n; m >= 2; m >>= 1) {
      int mh = m >> 1;
      for (int i = 0; i < mh; i++) {
        LL w = omega[i*theta%MAXN];
        for (int j = i; j < n; j += m) {
          int k = j + mh;
          LL x = a[j] - a[k];
          if (x < 0) x += P;
          a[j] += a[k];
          if (a[j] > P) a[j] -= P;
          a[k] = (w * x) % P;
        }
      }
      theta = (theta * 2) % MAXN;
    }
    int i = 0;
    for (int j = 1; j < n - 1; j++) {
      for (int k = n >> 1; k > (i ^= k); k >>= 1);
      if (j < i) swap(a[i], a[j]);
    }
    if (inv_ntt) {
      LL ni = inv(n,P);
      reverse( a+1 , a+n );
      for (i = 0; i < n; i++)
        a[i] = (a[i] * ni) % P;
    }
  }
  void operator()(int n, LL a[], bool inv_ntt=false) {
    tran(n, a, inv_ntt);
  }
};

const LL P=2013265921,root=31;
const int MAXN=4194304;
NTT<P, root, MAXN> ntt;
```

5 Geometry

5.1 Point Class

```
namespace Geometry{
  const long double EPS = 1e-8;
  const long double PI = acos((long double)-1);
  template<typename T>
  struct Point{
    typedef long double llf;
    T x, y;
    Point(): x(0), y(0){}
    Point(T _, T __): x(_), y(__){}
    template<typename T2>
    Point(const Point<T2>& a): x(a.x), y(a.y){}
    inline llf theta() const {
      return atan2((llf)y, (llf)x);
```

```
    }
    inline llf dis() const {
      return hypot((llf)x, (llf)y);
    }
    inline llf dis(const Point& o) const {
      return hypot((llf)(x-o.x), (llf)(y-o.y));
    }
    Point operator-(const Point& o) const {
      return Point(x-o.x, y-o.y);
    }
    Point operator-=(const Point& o){
      x-=o.x, y-=o.y;
      return *this;
    }
    Point operator+(const Point& o) const {
      return Point(x+o.x, y+o.y);
    }
    Point operator+=(const Point& o){
      x+=o.x, y+=o.y;
      return *this;
    }
    Point operator*(const T& k) const {
      return Point(x*k, y*k);
    }
    Point operator*=(const T& k){
      x*=k, y*=k;
      return *this;
    }
    Point operator/(const T& k) const {
      return Point(x/k, y/k);
    }
    Point operator/=(const T& k){
      x/=k, y/=k;
      return *this;
    }
    Point operator-() const {
      return Point(-x, -y);
    }
    template<class = typename is_floating_point<T>::
        type>
    bool operator==(const Point& o) const {
      return fabs(x-o.x) < EPS and fabs(y-o.y) < EPS;
    }
    bool operator==(const Point& o) const {
      return x==o.x and y==o.y;
    }
    bool operator!=(const Point& o) const {
      return !(*this == o);
    }
    friend inline T cross(const Point& a, const Point&
        b){
      return a.x*b.y - b.x*a.y;
    }
    friend inline T dot(const Point& a, const Point &b)
        {
      return a.x*b.x + a.y*b.y;
    }
    friend ostream& operator<<(ostream& ss, const Point
        & o){
      ss<<"("<<o.x<<", "<<o.y<<")";
      return ss;
    }
};
const Point<long double> INF_P(-1e20, 1e20);
const Point<long double> NOT_EXIST(1e20, 1e-20);
template<typename T>
struct Line{
  // ax+by+c = 0
  T a, b, c;
  Line(): a(0), b(1), c(0){}
  Line(T _, T __, T ___): a(_), b(__), c(___){
    assert(fabs(a)>EPS or fabs(b)>EPS);
  }
  template<typename T2>
  Line(const Line<T2>& x): a(x.a), b(x.b), c(x.c){}
  typedef Point<long double> Pt;
  template<class = typename is_floating_point<T>::
      type>
  bool operator==(const Line& o) const {
    return fabs(a-o.a) < EPS and fabs(b-o.b) < EPS
        and fabs(c-o.b) < EPS;
  }
  bool operator==(const Line& o) const {
    return a==o.a and b==o.b and c==o.c;
  }
  bool operator!=(const Line& o) const {
    return !(*this == o);
  }
  template<class = typename is_floating_point<T>::
      type>
  friend inline bool on_line(const Point<T>& p, const
       Line& l){
    return fabs(l.a*p.x + l.b*p.y + l.c) < EPS;
  }
  friend inline bool on_line(const Point<T>& p, const
       Line& l){
    return l.a*p.x + l.b*p.y + l.c == 0;
  }
  template<class = typename is_floating_point<T>::
      type>
  friend inline bool is_parallel(const Line& x, const
       Line& y){
    return fabs(x.a*y.b - x.b*y.a) < EPS;
  }
  friend inline bool is_parallel(const Line& x, const
       Line& y){
    return x.a*y.b == x.b*y.a;
  }
  friend inline Pt get_inter(const Line& x, const
      Line& y){
    typedef long double llf;
    if(x==y) return INF_P;
    if(is_parallel(x, y)) return NOT_EXIST;
    llf delta = x.a*y.b - x.b*y.a;
    llf delta_x = x.b*y.c - x.c*y.b;
    llf delta_y = x.c*y.a - x.a*y.c;
    return Pt(delta_x / delta, delta_y / delta);
  }
  friend ostream& operator<<(ostream& ss, const Line&
       o){
    ss<<o.a<<"x+"<<o.b<<"y+"<<o.c<<"=0";
    return ss;
  }
};
template<typename T>
inline Line<T> get_line(const Point<T>& a, const
    Point<T>& b){
  return Line<T>(a.y-b.y, b.x-a.x, (b.y-a.y)*a.x-(b.x
      -a.x)*a.y);
}
template<typename T>
struct Segment{
  // p1.x < p2.x
  Line<T> base;
  Point<T> p1, p2;
  Segment(): base(Line<T>()), p1(Point<T>()), p2(
      Point<T>()){
    assert(on_line(p1, base) and on_line(p2, base));
  }
  Segment(Line<T> _, Point<T> __, Point<T> ___): base
      (_), p1(__), p2(___){
    assert(on_line(p1, base) and on_line(p2, base));
  }
  template<typename T2>
  Segment(const Segment<T2>& _): base(_.base), p1(_.
      p1), p2(_.p2) {}
  typedef Point<long double> Pt;
  friend bool on_segment(const Point<T>& p, const
      Segment& l){
    if(on_line(p, l.base))
      return (l.p1.x-p.x)*(p.x-l.p2.x)>=0 and (l.p1.y
          -p.y)*(p.y-l.p2.y)>=0;
    return false;
  }
  friend bool have_inter(const Segment& a, const
      Segment& b){
    if(is_parallel(a.base, b.base)){
      return on_segment(a.p1, b) or on_segment(a.p2,
          b) or on_segment(b.p1, a) or on_segment(b.
          p2, a);
    }
    Pt inter = get_inter(a.base, b.base);
    return on_segment(inter, a) and on_segment(inter,
        b);
  }
  friend inline Pt get_inter(const Segment& a, const
      Segment& b){
    if(!have_inter(a, b)){
      return NOT_EXIST;
    }else if(is_parallel(a.base, b.base)){
      if(a.p1 == b.p1){
```

```
        if(on_segment(a.p2, b) or on_segment(b.p2, a)
            ) return INF_P;
        else return a.p1;
      }else if(a.p1 == b.p2){
        if(on_segment(a.p2, b) or on_segment(b.p1, a)
            ) return INF_P;
        else return a.p1;
      }else if(a.p2 == b.p1){
        if(on_segment(a.p1, b) or on_segment(b.p2, a)
            ) return INF_P;
        else return a.p2;
      }else if(a.p2 == b.p2){
        if(on_segment(a.p1, b) or on_segment(b.p1, a)
            ) return INF_P;
        else return a.p2;
      }
      return INF_P;
    }
    return get_inter(a.base, b.base);
  }
  friend ostream& operator<<(ostream& ss, const
      Segment& o){
    ss<<o.base<<", "<<o.p1<<" ~ "<<o.p2;
    return ss;
  }
};
template<typename T>
inline Segment<T> get_segment(const Point<T>& a,
    const Point<T>& b){
  return Segment<T>(get_line(a, b), a, b);
}
};
```

5.2 2D Convex Hull

```
#include <bits/stdc++.h>
using namespace std;
typedef long long lld;
typedef pair<lld, lld> PLL;

template<typename A, typename B>
pair<A, B> operator-(const pair<A, B>& a, const pair<A,
    B>& b){
  return {a.first-b.first, a.second-b.second};
}

class ConvexHull_2D{
  #define x first
  #define y second
  private:
    vector<PLL> dots, down, up;
    inline lld cross(PLL a, PLL b){
      return a.x*b.y-b.x*a.y;
    }
  public:
    void insert(PLL x){dots.push_back(x);}
    void solve(){
      down.clear();up.clear();
      sort(dots.begin(), dots.end());
      for(auto i: dots){
        while(up.size()>1){
          if(cross(i-up[up.size()-2], up.back()-up[up.
              size()-2]) <= 0) up.pop_back();
          else break;
        }
        up.push_back(i);
      }
      reverse(dots.begin(), dots.end());
      for(auto i: dots){
        while(down.size()>1){
          if(cross(i-down[down.size()-2], down.back()-
              down[down.size()-2]) <= 0) down.pop_back
              ();
          else break;
        }
        down.push_back(i);
      }
      dots.clear();
      dots.insert(dots.end(), down.begin(), down.end())
          ;
      dots.insert(dots.end(), up.begin(), up.end());
      sort(dots.begin(), dots.end());
      dots.resize(distance(dots.begin(), unique(dots.
          begin(), dots.end())));
      down.clear();up.clear();
    }
    vector<PLL> get(){
      return dots;
    }
    bool IsThis(PLL x){
      auto ret = lower_bound(dots.begin(), dots.end(),
          x);
      return *ret==x;
    }
    int count(){return dots.size();}
  #undef x
  #undef y
} cv;


int main(){
  ios_base::sync_with_stdio(0);cin.tie(0);
  int n; cin>>n;
  for(int i=0;i<n;i++){
    lld a,b;cin>>a>>b;
    cv.insert({a, b});
  }
  cv.solve();
  cout<<cv.count()<<'\n';
  return 0;
}
```

5.3 SimulateAnnealing

```
#include <random>
#include <functional>
#include <utility>
#include <algorithm>
using namespace std;

double getY(double);

int main(){
    int rr, ll;
    default_random_engine rEng(time(NULL));
  uniform_real_distribution<double> Range(-1,1);
  uniform_real_distribution<double> expR(0,1);
  auto Random=bind(Range,rEng);
  auto expRand=bind(expR,rEng);
  int step=0;
  double pace=rr-ll, mini=0.95; // need to search for
      it
  double x=max(min(Random()*pace+ll, rr), ll), y=getY(x
      );
  while(pace>=1e-7){
    double newX = max(min(x + Random()*pace, rr), ll);
    double newY = getY(newX);
    if(newY < y || expRand() < exp(-step))
      x=newX, y=newY;
    step++;
    pace*=mini;
  }
}

double getY(double x){
    // get y using x
    return x;
}
```

6 Stringology

6.1 Hash

```
#include <string>
typedef long long lld;
const int N = 1000000;
class Hash{
    private:
        const lld p = 127, q = 1208220623;
        int sz;
        lld prefix[N], power[N];
    public:
        void init(const std::string &x){
            sz = x.size();
```

```
            prefix[0]=0;
            for(int i=1;i<=sz;i++) prefix[i]=((prefix[i
                -1]*p)%q+x[i-1])%q;
            power[0]=1;
            for(int i=1;i<=sz;i++) power[i]=(power[i
                -1]*p)%q;
        }
        lld query(int l, int r){
            // 1-base (l, r]
            return (prefix[r] - (prefix[l]*power[r-l])%
                q + q)%q;
        }
};
```

6.2 Suffix Array

```
//help by http://www.geeksforgeeks.org/suffix-array-set
    -2-a-nlognlogn-algorithm/
#include <bits/stdc++.h>
using namespace std;
#define PB push_back

struct sfx{
  int index;
  int r,nr;
};

char str[N + 10];
int len;

vector<sfx> srs[N + 10];
int mapping[N + 10];
sfx sa[N + 10];

bool cmp(sfx a,sfx b){
  if(a.r==b.r){
    return a.nr<b.nr;
  }else{
    return a.r<b.r;
  }
}

void SA();
void radixSort();

int main(){
  gets(str);
  len = strlen(str);
  SA();
  for(int i=0;i<len;i++){
    printf("%d\n",sa[i].index);
  }
  return 0;
}

void SA(){
  for(int i=0;i<len;i++){
    sa[i].index = i;
    sa[i].r=str[i];
    sa[i].nr=(i+1>=len)?0:str[i+1];
  }
  //sort(sa,sa+len,cmp);
  radixSort();
  for(int j=2;j<=len;j*=2){
    int cnt=1;
    int rr = sa[0].r;
    sa[0].r=cnt;
    mapping[sa[0].index]=0;
    for(int i=1;i<len;i++){
      if(sa[i].r == rr && sa[i].nr == sa[i-1].nr){
        rr=sa[i].r;
        sa[i].r=cnt;
      }else{
        rr=sa[i].r;
        sa[i].r=++cnt;
      }
      mapping[sa[i].index]=i;
    }
    for(int i=0;i<len;i++){
      int nn = sa[i].index+j;
      sa[i].nr = (nn>=len)?0:sa[mapping[nn]].r;
    }
    //sort(sa, sa+len, cmp);
    radixSort();
  }
}

void radixSort(){
  int m = 0;
  for(int i=0;i<len;i++){
    srs[sa[i].nr].PB(sa[i]);
    m=max(m,sa[i].nr);
  }
  int cnt=0;
  for(int i=0;i<=m;i++){
    if(srs[i].empty())continue;
    for(auto j:srs[i]){
      sa[cnt++] = j;
    }
    srs[i].clear();
  }
  m = 0;
  for(int i=0;i<len;i++){
    srs[sa[i].r].PB(sa[i]);
    m=max(m,sa[i].r);
  }
  cnt=0;
  for(int i=0;i<=m;i++){
    if(srs[i].empty())continue;
    for(auto j:srs[i]){
      sa[cnt++] = j;
    }
    srs[i].clear();
  }
}
```

6.3 KMP

```
int F[N];
int match(const std::string& A, const std::string& B) {
  F[0] = -1, F[1] = 0;
  for (int i=1, j=0; i < B.size()-1; F[++i] = ++j) { //
      calculate failure function
    if (B[i] == B[j]) F[i] = F[j]; // optimization by
        Knuth, may not need this
    while (j != -1 && B[i] != B[j]) j = F[j];
  }
  for (int i=0, j=0; i-j+B.size() <= A.size(); i++, j
      ++) { // match
    while (j != -1 && A[i] != B[j]) j = F[j];
    if (j == B.size() - 1) return i - j; // match
        successfully at string B's end return result
  }
  return -1;
}
```