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## 1 Basic

#### 1.1 Default Code

```
#include <iostream>
#include <iomanip>
#include <string>
#include <algorithm>
#include <vector>
#include <queue>
#include <bitset>
#include <map>
#include <set>
#include <unordered map>
#include <unordered set>
#include <cstdio>
#include <cstdlib>
#include <cstring>
#include <ctime>
#include <random>
#include <utility>
#include <stack>
#include <sstream>
#include <functional>
#include <deque>
#include <cassert>
using namespace std;
/* include everything for Kotori~ <3 */
typedef long long lld;
typedef unsigned long long llu;
typedef long double llf;
typedef pair<int, int> PII;
typedef pair<int, lld> PIL;
typedef pair<lld,int> PLI;
typedef pair<lld, lld> PLL;
template<typename T>
using maxHeap = priority_queue<T, vector<T>, less<T>>;
template<typename T>
using minHeap = priority_queue<T,vector<T>,greater<T>>;
/* define some types for Ruby! */
#define FF first
#define SS second
#define SZ(x) (int)(x.size())
#define ALL(x) begin(x), end(x)
#define PB push back
#define WC(x) while(x--)
/* make code shorter for Di~a~ */
template<typename Iter>
ostream& _out(ostream &s, Iter b, Iter e) {
  s<<"/":
  for ( auto it=b; it!=e; it++ ) s<<(it==b?"":" ")<<*it</pre>
  s<<"]";
  return s;
template<typename A, typename B>
ostream& operator <<( ostream &s, const pair<A,B> &p )
    { return s<<"("<<p.FF<<","<<p.SS<<")"; }
template<typename T>
ostream& operator <<( ostream &s, const vector<T> &c )
    { return _out(s,ALL(c)); }
/* make output easier for Ainyan~n~ */
bool debug = 0;
#define DUMP(x) if(debug) cerr<< PRETTY FUNCTION <<":</pre>
    "<<__LINE__<<" - "<<#x<<"="<<x<<'\n'
{\tt template}{<}{\tt typename}\  \, \mathbb{T}{>}
void DEBUG(const T& x) {if(debug) cerr<<x;}</pre>
template<typename T, typename... Args>
void DEBUG(const T& head, const Args& ...tail) {
 if(debug) {cerr<<head; DEBUG(tail...);}</pre>
/* Let's debug with Nico~Nico~Ni */
int main(int argc, char* argv[]){
 if(argc>1 and string(argv[1]) == "-D") debug=1;
  if(!debug) {ios_base::sync_with_stdio(0);cin.tie(0);}
  return 0;
```

#### 1.2 IncreaseStackSize

```
//stack resize
asm( "mov %0,%%esp\n" ::"g"(mem+10000000) );
//change esp to rsp if 64-bit system

//stack resize (linux)
#include <sys/resource.h>
void increase_stack_size() {
   const rlim_t ks = 64*1024*1024;
   struct rlimit rl;
   int res=getrlimit(RLIMIT_STACK, &rl);
   if(res==0) {
      if(rl.rlim_cur<ks) {
        rl.rlim_cur=ks;
        res=setrlimit(RLIMIT_STACK, &rl);
   }
   }
}</pre>
```

## 1.3 Pragma optimization

```
#pragma GCC optimize("Ofast,no-stack-protector,no-math-
errno")
#pragma GCC optimize("unroll-loops")
#pragma GCC target("sse,sse2,sse3,sse4,popent,abm
,mmx,avx,tune=native")
```

#### 1.4 Quick Random

```
// PRNG {{{
template < class T, T x1, T x2, T x3, int y1, int y2, int
     у3>
struct PRNG {
    using S = typename std::make signed<T>::type;
    PRNG(T _s = 0) : s(_s) {}
    T next() {
        T z = (s += x1);
        z = (z ^ (z >> y1)) * x2;

z = (z ^ (z >> y2)) * x3;
        return z ^ (z >> y3);
    T next(T n) { return next() % n; }
    S next(S 1, S r) { return 1 + next(r - 1 + 1); }
    T operator()() { return next(); }
    T operator()(T n) { return next(n); }
    S operator()(S 1, S r) { return next(1, r); }
    static T gen(T s) { return PRNG(s)(); }
    template<class U>
    void shuffle(U first, U last) {
        size t n = last - first;
        for (\text{size t i = 0; i < n; i++}) \text{ swap(first[i],}
             first[next(i + 1)]);
using R32 = PRNG<uint32 t, 0x9E3779B1, 0x85EBCA6B, 0
   xC2B2AE35, 16, 13, 16>;
R32 r32;
using R64 = PRNG<uint64_t, 0x9E3779B97F4A7C15, 0
xBF58476D1CE4E5B9, 0x94D049BB133111EB, 30, 27, 31>;
R64 r64;
// }}}
```

## 1.5 IO Optimization

```
case 7: res += (*p++ & 15) * 1000000;
     case 6: res += (*p++ & 15) * 100000;
     case 5: res += (*p++ & 15) * 10000;
     case 4: res += (*p++ & 15) * 1000;
     case 3: res += (*p++ & 15) * 100;
     case 2: res += (*p++ & 15) * 10;
     case 1: res += (*p & 15);
   return res * (neg ? -1 : 1);
static inline bool getRawChar(char *c) {
   static char buf[1 << 20], *p = buf, *end = buf;</pre>
   if (p == end) {
     if ((end = buf + fread(buf, 1, 1 << 20, stdin)) ==</pre>
        buf) return false;
    p = buf;
   *c = *p++;
   return true;
 static inline bool getInt(int32_t *x) {
   static char buf[12];
   uint fast32 t i = 0;
   while (getRawChar(buf + i)) {
     if ((unsigned)(buf[i] - '0') > 10U && buf[i] != '-'
         ) {
       if (i) break;
       else continue;
     i++;
   if (!i) return false;
   *x = fastAtoi(buf, i);
   return true;
// I/O optimization end }}}
```

## 2 Data Structure

## 2.1 Bigint

```
struct Bigint{
  static const int LEN = 60;
  static const int BIGMOD = 10000;
  int s;
  int vl, v[LEN];
  // vector<int> v;
  Bigint() : s(1) \{ vl = 0; \}
  Bigint(long long a) {
    s = 1; v1 = 0;
    if (a < 0) \{ s = -1; a = -a; \}
    while (a) {
     push_back(a % BIGMOD);
      a /= BIGMOD;
    }
  Bigint(string str) {
    s = 1; vl = 0;
int stPos = 0, num = 0;
    if (!str.empty() && str[0] == '-') {
     stPos = 1;
      s = -1;
    for (int i=SZ(str)-1, q=1; i>=stPos; i--) {
      num += (str[i] - '0') * q;
      if ((q *= 10) >= BIGMOD) {
       push back(num);
        num = 0; q = 1;
    if (num) push back(num);
    n();
  int len() const {
   return vl;
        return SZ(v);
 bool empty() const { return len() == 0; }
```

```
void push back(int x) {
 v[v]++1 = x:
       v. PB (x);
void pop_back() {
  // v.pop_back();
int back() const {
  return v[v1-1];
  // return v.back();
void n() {
  while (!empty() && !back()) pop back();
void resize(int nl) {
 vl = nl;
  fill(v, v+vl, 0);
       v.resize(nl);
  //
        fill(ALL(v), 0);
void print() const {
  if (empty()) { putchar('0'); return; }
  if (s == -1) putchar('-');
  printf("%d", back());
  for (int i=len()-2; i>=0; i--) printf("%.4d",v[i]);
friend std::ostream& operator << (std::ostream& out,</pre>
    const Bigint &a) {
  if (a.empty()) { out << "0"; return out; }</pre>
  if (a.s == -1) out << "-";</pre>
  out << a.back();
  for (int i=a.len()-2; i>=0; i--) {
    char str[10];
    snprintf(str, 5, "%.4d", a.v[i]);
    out << str;
  return out;
int cp3(const Bigint &b)const {
  if (s != b.s) return s - b.s;
  if (s == -1) return - (-*this).cp3(-b);
  if (len() != b.len()) return len()-b.len();//int
  for (int i=len()-1; i>=0; i--)
    if (v[i]!=b.v[i]) return v[i]-b.v[i];
  return 0;
bool operator < (const Bigint &b) const{ return cp3(b)</pre>
    <0; }
bool operator <= (const Bigint &b) const{ return cp3(b</pre>
    ) <= 0;
bool operator == (const Bigint &b) const{ return cp3(b
    ) == 0;
bool operator != (const Bigint &b) const{ return cp3(b
    ) !=0: 
bool operator > (const Bigint &b) const{ return cp3(b)
    >0; }
bool operator >= (const Bigint &b) const{ return cp3(b
    ) >= 0;
Bigint operator - () const {
  Bigint r = (*this);
  r.s = -r.s;
  return r;
Bigint operator + (const Bigint &b) const {
  if (s == -1) return -(-(*this)+(-b));
  if (b.s == -1) return (*this)-(-b);
  Bigint r;
  int nl = max(len(), b.len());
  r.resize(nl + 1);
  for (int i=0; i<nl; i++) {</pre>
    if (i < len()) r.v[i] += v[i];</pre>
    if (i < b.len()) r.v[i] += b.v[i];</pre>
    if(r.v[i] >= BIGMOD) {
      r.v[i+1] += r.v[i] / BIGMOD;
      r.v[i] %= BIGMOD;
    }
  }
  r.n();
  return r;
Bigint operator - (const Bigint &b) const {
```

```
if (s == -1) return -(-(*this)-(-b));
  if (b.s == -1) return (*this)+(-b);
  if ((*this) < b) return -(b-(*this));</pre>
  Bigint r;
  r.resize(len());
  for (int i=0; i<len(); i++) {</pre>
   r.v[i] += v[i];
    if (i < b.len()) r.v[i] -= b.v[i];</pre>
    if (r.v[i] < 0) {
     r.v[i] += BIGMOD;
     r.v[i+1]--;
  r.n();
  return r;
Bigint operator * (const Bigint &b) {
  Bigint r;
  r.resize(len() + b.len() + 1);
  r.s = s * b.s;
  for (int i=0; i<len(); i++) {</pre>
   for (int j=0; j<b.len(); j++) {</pre>
      r.v[i+j] += v[i] * b.v[j];
      if(r.v[i+j]) >= BIGMOD)
       r.v[i+j+1] += r.v[i+j] / BIGMOD;
        r.v[i+j] %= BIGMOD;
    }
  r.n();
  return r;
Bigint operator / (const Bigint &b) {
  Bigint r;
  r.resize(max(1, len()-b.len()+1));
  int oriS = s;
  Bigint b2 = b; // b2 = abs(b)
  s = b2.s = r.s = 1;
  for (int i=r.len()-1; i>=0; i--) {
    int d=0, u=BIGMOD-1;
    while(d<u) {</pre>
     int m = (d+u+1) >> 1;
      r.v[i] = m;
      if((r*b2) > (*this)) u = m-1;
      else d = m;
    r.v[i] = d;
  s = oriS;
  r.s = s * b.s;
  r.n();
 return r;
Bigint operator % (const Bigint &b) {
  return (*this)-(*this)/b*b;
```

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## 2.2 Fraction

```
/*************
 n為分子,d為分母
 若分數為0則n=0,d=1
 若為負數則負號加在分子
 必定約到最簡分數
#ifndef SUNMOON_FRACTION
 #define SUNMOON FRACTION
 #include < algorithm >
template<typename T>
struct fraction{
  T n,d;
  fraction(const T &_n=0,const T &_d=1):n(_n),d(_d){
    T_t = std:: \underline{gcd(n,d)};
    n/=t,d/=t;
    if (d<0) n=-n, d=-d;
  fraction operator-()const{
    return fraction(-n,d);
  fraction operator+(const fraction &b)const{
    return fraction(n*b.d+b.n*d,d*b.d);
```

```
fraction operator-(const fraction &b)const{
   return fraction(n*b.d-b.n*d,d*b.d);
  fraction operator*(const fraction &b)const{
   return fraction(n*b.n,d*b.d);
 fraction operator/(const fraction &b)const{
   return fraction(n*b.d,d*b.n);
 fraction operator+=(const fraction &b) {
   return *this=fraction(n*b.d+b.n*d,d*b.d);
  fraction operator-=(const fraction &b) {
    return *this=fraction(n*b.d-b.n*d,d*b.d);
 fraction operator*=(const fraction &b) {
   return *this=fraction(n*b.n,d*b.d);
  fraction operator/=(const fraction &b) {
   return *this=fraction(n*b.d,d*b.n);
 bool operator <(const fraction &b) const{</pre>
   return n*b.d<b.n*d;
 bool operator >(const fraction &b)const{
   return n*b.d>b.n*d;
 bool operator == (const fraction &b) const{
   return n*b.d==b.n*d;
 bool operator <= (const fraction &b) const{</pre>
   return n*b.d<=b.n*d;</pre>
 bool operator >= (const fraction &b) const{
   return n*b.d>=b.n*d;
 }
};
#endif
```

#### 2.3 ScientificNotation

```
#include <cmath>
#include <cstdio>
#include <iostream>
#include <algorithm>
struct SciFi{
    typedef double base_t;
 base t x; int p;
  SciFi() \{x=0; p=0; \}
 SciFi(base t k) {
    p = floor(log10(k));
    x = k / pow((base t)10, p);
 SciFi(base_t a, int b) {
   x=a; p=b;
 SciFi operator=(base_t k) {
    p = floor(log10(k));
    x = k / pow((base_t)10, p);
    return *this;
  SciFi operator* (SciFi k) const{
    int nP = p+k.p;
    base t nX = x*k.x;
    \overline{\text{int}} \ \overline{\text{tp}} = \text{floor}(\log 10 (\text{nX}));
    return SciFi(nX/pow((base t)10, tp), nP+tp);
  SciFi operator*=(SciFi k) {
    p+=k.p;
    x*=k.x;
    int tp = floor(log10(x));
    p+=tp;
    x/=pow((base_t)10, tp);
    return *this;
  SciFi operator+(SciFi k)const{
    int newP = std::min(k.p, p);
    base_t x1 = x*pow((base_t)10, p-newP);
    base t x2 = k.x*pow((base t)10, k.p-newP);
    x1+=x2;
    int tp = floor(log10(x1));
    newP+=tp;
    x1 /= pow((base_t)10, tp);
```

```
return SciFi(x1, newP);
  SciFi operator+=(SciFi k) {
    int newP = std::min(k.p, p);
    base t x1 = x*pow((base t)10, p-newP);
    base_t x2 = k.x*pow((base_t)10, k.p-newP);
    x1+=x2:
    int tp = floor(log10(x1));
    newP+=tp;
    x1 /= pow((base t)10, tp);
    x=x1; p=newP;
    return *this;
  bool operator<(SciFi a)const{</pre>
    if(p == a.p) return x<a.x;</pre>
    return p<a.p;</pre>
  bool operator>(SciFi a)const{
    if(p == a.p) return x>a.x;
    return p>a.p;
  bool operator==(SciFi a)const{
    return p==a.p and x==a.x;
};
int main(){
  double a; scanf("%lf",&a);
  SciFi aa=a, x;
  x = aa*SciFi(2);
  printf("%.21fe%c%03d\n", x.x, "+-"[x.p<0], abs(x.p));
  return 0;
```

## 2.4 unordered\_map

```
#include <ext/pb_ds/assoc_container.hpp>
using __gnu_pbds::cc_hash_table;
using __gnu_pbds::gp_hash_table;
template<typename A, typename B> using hTable1 =
    cc_hash_table<A,B>;
template<typename A, typename B> using hTable2 =
    gp_hash_table<A,B>;
```

# 2.5 extc\_balance\_tree

```
#include <functional>
#include <ext/pb_ds/assoc_container.hpp>
using std::less;
using std::greater;
using __gnu_pbds::tree;
using __gnu_pbds::rb_tree_tag;
using __gnu_pbds::ov_tree_tag;
using __gnu_pbds::splay_tree_tag;
using __gnu_pbds::null_type;
using
       _gnu_pbds::tree_order_statistics_node_update;
template<typename T>
using ordered set = tree<T, null type, less<T>,
    rb_tree_tag, tree_order_statistics_node_update>;
template<typename A, B>
using ordered map = tree<A, B, less<A>, rb tree tag,
    tree order statistics node update>;
int main(){
  ordered_set<int> ss;
  ordered map<int, int> mm;
  ss.insert(1);
  ss.insert(5);
  assert(*ss.find_by_order(0)==1);
  assert(ss.order_of_key(-1) == 0);
  assert(ss.order_of_key(87) == 2);
  return 0;
```

## 2.6 extc\_heap

```
if(que.empty()) root=nullptr;
#include <functional>
#include <ext/pb_ds/assoc_container.hpp>
                                                                   else root = que.front();
#include <ext/pb_ds/priority_queue.hpp>
using std::less;
                                                                 inline void join(pairingHeap< type,</pre>
                                                                                                         cmp>& pq2) {
                                                                    if( cp(root->val, pq2.root->val)) swap(root,
using std::greater;
using __gnu_pbds::priority_queue;
                                                                         pq2.root);
using __gnu_pbds::pairing_heap_tag;
                                                                    root->child.push back(pq2.root);
                                                                   count += pq2.count;
using __gnu_pbds::binary_heap_tag;
using __gnu_pbds::binomial_heap_tag;
                                                                     pq2.root = nullptr;
using __gnu_pbds::rc_binomial_heap tag;
                                                                     pq2.count = 0;
using __gnu_pbds::thin heap tag;
                                                            };
int main(){
 priority queue<int, less<int>, pairing heap tag> pq1,
                                                            int main(){
                                                              pairingHeap<int> pq1, pq2;
      pq2;
 pq1.push(1);
                                                               for (int i=0;i<1e5;i++) pq1.push(i);</pre>
                                                               for (int i=1e5;i<2e5;i++) pq2.push(i);</pre>
 pq2.push(2);
 pq1.join(pq2);
                                                               pq1.join(pq2);
 assert(pq2.size() == 0);
                                                               while(!pq1.empty()){
 auto it = pq1.push(87);
                                                                // cout<<pq1.top()<<" ";
 pq1.modify(it, 19);
                                                                pq1.pop();
 while(!pq1.empty()){
   pq1.top();
                                                               return 0;
   pq1.pop();
 return 0;
```

## 2.7 PairingHeap

```
#include <vector>
using std::vector;
template<class __type, class __cmp=less<__type>>
class pairingHeap{
 private:
      struct pairingNode{
          __type val;
            vector<pairingNode*> child;
            pairingNode(){
                val = 0;
                child.clear():
            pairingNode(int x): val(x){
                child.clear();
     } ;
    pairingNode* root;
    int count;
     cmp cp;
    void remove(pairingNode* cur) {
        if(cur==nullptr) return;
        for(auto i: cur->child) remove(i);
        delete cur;
 public:
   pairingHeap() {root=nullptr;count=0;}
    inline bool empty() {return count==0;}
    inline _
            type top() {return root->val;}
    inline int size() {return count;}
    inline void clear() {remove(root);root=nullptr;count
        =0;
    inline void push(__type a){
      count++;
      auto mynode = new pairingNode(a);
      if(root==nullptr) root = mynode;
      else{
        if(_cp(root->val, mynode->val)) swap(root,
            mynode);
        root->child.push back(mynode);
      }
    inline void pop(){
      count--;
      queue<pairingNode*> que;
      for(auto i:root->child) que.push(i);
      delete root;
      while (que.size() > 1) {
        auto tp1=que.front();que.pop();
        auto tp2=que.front();que.pop();
        if( cp(tp1->val, tp2->val)) swap(tp1, tp2);
        tp1->child.push back(tp2);
        que.push(tp1);
```

## 2.8 Disjoint Set

```
class DJS{
  private:
    vector<int> fa, sz, sv;
    vector<pair<int*, int>> opt;
    inline void assign(int *k, int v) {
      opt.PB({k, *k});
       *k = v;
  public:
    inline void init(int n) {
      fa.resize(n);
      sz.resize(n);
      for (int i=0;i<n;i++) {</pre>
        fa[i] = i:
         sz[i] = 1;
      opt.clear();
    int querv(int x){
      if(fa[x] == x) return x;
      return query(fa[x]);
    inline void merge(int a, int b) {
      int af = query(a), bf = query(b);
      if(af == bf) return;
      if(sz[af] < sz[bf]) swap(af, bf);</pre>
      assign(&fa[bf], fa[af]);
assign(&sz[af], sz[af]+sz[bf]);
    inline void save() {sv.PB(SZ(opt));}
    inline void undo() {
      int ls = sv.back(); sv.pop_back();
      while(SZ(opt) > ls){
        pair<int*, int> cur=opt.back();
*cur.FF = cur.SS;
         opt.pop back();
```

### 2.9 Treap

```
#include <cstdlib>
class Treap{
  private:
    const int MEM = 500000 + 5;
    unsigned seed;
  inline unsigned myrand() {
    static unsigned seed = time(NULL);
    seed = seed*seed*127 + seed*227 + 2147483587;
    seed ^= seed*97;
    seed /= 7123;
    return seed;
```

```
struct node{
      node *lc, *rc;
      int pri, size, val;
      node(){}
      node(int x):
        lc(nullptr),
        rc(nullptr),
       pri(myrand()),
        size(1),
        val(x)
        { }
      inline void pull(){
        size = 1;
        if(lc) size += lc->size;
        if(rc) size += rc->size;
    } *root, pool[MEM];
    int mem_;
    inline node* new_node(int x) {
      static int mem = 0;
      assert (mem < \overline{MEM});
      pool[mem ]=node(x);
      return &pool[mem_++];
    inline int sz(node* x) {return x?x->size:0;}
   node* merge(node *a, node *b) {
     if(!a or !b) return a?a:b;
      if(a->pri > b->pri) {
        a->rc = merge(a->rc, b);
        a->pull();
        return a;
      }else{
        b->lc = merge(a, b->lc);
        b->pull();
        return b;
     }
   void split(Treap* t, int k, Treap*& a, Treap*& b) {
      if(!t) a=b=nullptr;
      else if (sz(t->lc) < k) {
        a = t;
        split(t->rc, k - sz(t->lc) - 1, a->rc, b);
        a->pull();
      }else{
       b = t;
        split(t->lc, k, a, b->lc);
        b->pull();
      }
    int oOk(node* rr, int x) {
      if(rr==NULL)return 0;
      if((rr->val) < x)return gSize(rr->l)+oOk(rr->r, x
          )+1:
      else return oOk(rr->1, x);
 public:
   Treap() {root=nullptr; seed=time(NULL); mem =0;}
    void do_something_at(int 1, int r){
      // 1-base [1, r]
      split(root, 1-1, tl, root);
      split(root, r-l+1, root, tr);
      root = merge(tl, merge(root, tr));
   void insert(int x) {
      node *a, *b;
      split(root, x, a, b);
      root = merge(merge(a, new node(x)), b);
      root->size = qSize(root->l)+qSize(root->r)+1;
   void remove(int x) {
      //need debug may contain bugs
      node *a, *b, *c, *d;
      split(root, x, a, b);
      a->size = gSize(a->1)+gSize(a->r);
      split(a, x-1, c, d);
      root = merge(b, c);
      root->size = gSize(root->1)+gSize(root->r);
      delete d;
    int order of key(int x) {return oOk(root,x);}
int main() {
  return 0;
```

## 2.10 SparseTable

```
template<typename T, typename Cmp =std::less<T>>
class SparseTable{
  private:
    vector<vector<T>> table;
    vector<int> lg;
    T cmp (T a, T b) {
        return Cmp_()(a, b)?a:b;
  public:
    void init(T arr[], int n){
      // 0-base
      lg.resize(n+1);
      lg[0] = -1, lg[1] = 0;
      for(int i=2;i<=n;i++) lg[i] = lg[i>>1]+1;
      table.resize(lg[n]+1);
      table[0].resize(n);
      for(int i=0;i<n;i++) table[0][i] = arr[i];</pre>
      for(int i=1;i<=lg[n];i++) {</pre>
        int len = 1 << (i-1), sz = 1 << i;
        table[i].resize(n-sz+1);
        for (int j=0; j<=n-sz; j++) {</pre>
          table[i][j] = cmp (table[i-1][j], table[i-1][
               j+len]);
    T query(int 1, int r) {
      // 0-base [1, r)
      int wh = lg[r-1], len=1 << wh;
      return cmp (table[wh][1], table[wh][r-len]);
} ;
```

#### 2.11 FenwickTree

```
#include <vector>
using std::vector;
template<typename T>
class BIT{
    \#define ALL(x) begin(x), end(x)
  private:
    vector<T> arr;
    int n:
    inline int lowbit(int x) {return x & (-x);}
    T query(int x) {
      T ret = 0;
      while (x > 0) {
        ret. += arr[x]:
        x -= lowbit(x);
      return ret;
  public:
    void init(int n ) {
      n = n_;
      arr.resize(n);
      fill(ALL(arr), 0);
    void modify(int pos, T v) {
      while(pos < n) {</pre>
        arr[pos] += v;
        pos += lowbit(pos);
    T query(int 1, int r) {
      // 1-base (1, r]
      return query(r) - query(l);
    #undef ALL
template<typename T>
class BIT{
    \#define ALL(x) begin(x), end(x)
  private:
        vector<T> arr;
        inline int lowbit(int x) {return x & (-x);}
        void add(int s, int v) {
      while(s){
```

```
arr[s]+=v;
        s-=lowbit(s);
      }
 public:
    void init(int n_) {
            n = n_;
             arr.resize(n);
             fill(ALL(arr), 0);
    void add(int 1, int r, T v) {
            //1-base (1, r]
      add(1, -v);
      add(r, v);
    T query(int x) {
      T r=0:
      while (x<size) {</pre>
        r+=arr[x];
        x += lowbit(x);
      return r;
    #undef ALL
};
```

# 3 Graph

## 3.1 BCC Edge

```
class BCC {
  private:
    int low[N], dfn[N], cnt;
    bool bcc[N];
    vector<PII> G[N];
    void dfs(int w, int f){
      dfn[w] = cnt++;
      low[w] = dfn[w];
      for(auto i: G[w]){
        int u = i.FF, t = i.SS;
if(u == f) continue;
         if(dfn[u]!=0){
           low[w] = min(low[w], dfn[u]);
         }else{
           dfs(u, w);
           low[w] = min(low[w], low[u]);
           if(low[u] > dfn[w]) bcc[t] = true;
      }
  public:
    void init(int n, int m) {
      for(int i=0;i<n;i++) G[i].clear();</pre>
      fill(bcc, bcc+m, false);
      cnt = 0;
    void add edge(int u, int v) {
      G[u].P\overline{B}(\{v, cnt\});
      G[v].PB({u, cnt});
      cnt++;
    void solve() {cnt = 1;dfs(0, 0);}
    // the id will be same as insert order, 0-base
    bool is_bcc(int x) {return bcc[x];}
} bcc;
```

#### 3.2 BCC Vertex

```
class BCC{
  private:
    int n, m, cnt, bcnt, curoot;
    vector<vector<PII>> G;
    vector<int> low, dfn, ids, sz;
    vector<bod> ap;
    stack<int> stk;
    void dfs(int w, int f) {
        dfn[w] = cnt++;
        low[w] = dfn[w];
        int son = 0;
        for(auto i: G[w]) {
```

```
int u = i.FF, t = i.SS;
        if(u == f) continue;
        if(dfn[u] == -1){
          stk.push(t);
          dfs(u, w);
          if(low[u] >= dfn[w]){
             if(u != curoot) ap[u] = true;
             while(stk.top() != t){
               assert(!stk.empty());
               ids[stk.top()] = bcnt;
               sz[bcnt]++;
               stk.pop();
             ids[stk.top()] = bcnt;
             sz[bcnt]++;
             stk.pop();
            bcnt++;
          low[w] = min(low[w], low[u]);
           if(dfn[u] < dfn[w]) stk.push(t);</pre>
          low[w] = min(low[w], dfn[u]);
      if (w == curoot && son > 1) ap[w] = true;
  public:
    void init(int n_, int m_) {
      n = n_{,} m = m_{,} cnt = 0;
      G.resize(n); fill(ALL(G), vector<PII>());
      low.resize(n);
      dfn.resize(n); fill(ALL(dfn), -1);
      ids.resize(m); sz.resize(m);
      ap.resize(n); fill(ALL(ap), false);
    void add edge(int u, int v) {
      assert(0 \le u \text{ and } u \le n);
      assert(0 \le v and v \le n);
      G[u].PB({v, cnt});
      G[v].PB({u, cnt});
      cnt++;
    void solve() {
      assert(cnt == m);
      cnt = 1, bcnt = 0;
      for (int i=0;i<n;i++) {</pre>
        if(dfn[i] != -1) continue;
        while(!stk.empty()) stk.pop();
        curoot = i;
        dfs(i, i);
    int count() {return bcnt;}
    // get bcc id of edges, same as inserting order (0-
        base)
    int get_id(int t){return ids[t];}
    int get size(int x) {return sz[x];}
    bool isAP(int x) {return ap[x];}
} bcc:
```

## 3.3 Strongly Connected Components

```
class SCC{
  private:
    int n, num_;
vector<int> G[N], rG[N], ord, num;
    bool vis[N];
    void dfs(int u) {
      if(vis[u]) return;
      vis[u]=1;
      for(auto v: G[u]) dfs(v);
      ord.PB(u);
    void rdfs(int u) {
      if(vis[u]) return;
      num[u] = num;
      vis[u] = 1;
      for(auto v: rG[u]) rdfs(v);
  public:
    inline void init(int n ) {
      n=n_, num_=0;
      num.resize(n);
      for(int i=0;i<n;i++) G[i].clear();</pre>
```

```
for (int i=0; i < n; i++) rG[i].clear();</pre>
    inline void add edge(int st, int ed) {
      G[st].PB(ed);
      rG[ed].PB(st);
    void solve(){
      memset(vis, 0, sizeof(vis));
      for (int i=0;i<n;i++) {</pre>
         if(!vis[i]) dfs(i);
      reverse (ALL (ord));
      memset(vis, 0, sizeof(vis));
for(auto i: ord){
        if(!vis[i]){
          rdfs(i);
           num_++;
        }
    inline int get id(int x) {return num[x];}
    inline int count() {return num ;}
} scc;
```

## 3.4 Bipartie Matching

```
#include <bits/stdc++.h>
using namespace std;
#define N 500
class BipartieMatching{
  private:
    vector<int> X[N], Y[N];
    int fX[N], fY[N], n;
    bitset<N> walked;
    bool dfs(int x) {
      for(auto i:X[x]){
        if (walked[i]) continue;
        walked[i]=1;
        if (fY[i] ==-1||dfs(fY[i])) {
          fY[i]=x; fX[x]=i;
          return 1;
        }
      return 0;
  public:
    void init(int n) {
      n=n;
      for (int i=0;i<n;i++) {</pre>
        X[i].clear();
        Y[i].clear());
        fX[i] = fY[i] = -1;
      walked.reset();
    void AddEdge(int x, int y) {
      X[x].push back(y);
      Y[y].push back(y);
    int solve(){
      int cnt = 0;
      for (int i=0;i<n;i++) {</pre>
        walked.reset();
        if(dfs(i)) cnt++;
      // return how many pair matched
      return cnt;
};
```

#### 3.5 MinimumCostMaximumFlow

```
class MiniCostMaxiFlow{
  typedef int CapT;
  typedef lld WeiT;
  typedef pair<CapT, WeiT> PCW;
  const CapT INF_CAP = 1<<30;
  const WeiT INF_WEI = 1LL<<60;
  const int MAXV = N;
  private:
    struct Edge{</pre>
```

```
int to, back;
      WeiT wei:
      CapT cap;
      Edge(){}
      Edge(int a, int b, WeiT c, CapT d): to(a), back(b
           ), wei(c), cap(d) {}
    int ori, edd, V;
    vector<Edge> G[MAXV];
    int fa[MAXV], wh[MAXV];
    bool inq[MAXV];
    WeiT dis[MAXV];
    PCW SPFA() {
      for (int i=0;i<V;i++) inq[i]=0;</pre>
      for(int i=0;i<V;i++) dis[i]=INF WEI;</pre>
      queue<int> qq;
      qq.push(ori);
      dis[ori]=0;
      while(!qq.empty()){
         int u = qq.front(); qq.pop();
         inq[u]=0;
         for (int i=0;i<SZ(G[u]);i++) {</pre>
          Edge e = G[u][i];
int v = e.to;
WeiT d = e.wei;
           if(e.cap > 0 and dis[v] > dis[u]+d){
             dis[v]=dis[u]+d;
             fa[v]=u;
             wh[v] = i;
             if(inq[v]) continue;
             qq.push(v);
             inq[v]=1;
          }
      if (dis[edd] == INF WEI) return {-1, -1};
      CapT mw=INF CAP;
       for(int i=edd;i!=ori;i=fa[i]) {
         mw = min(mw, G[fa[i]][wh[i]].cap);
      for(int i=edd;i!=ori;i=fa[i]) {
        auto &eg = G[fa[i]][wh[i]];
         eq.cap -= mw;
        G[eg.to][eg.back].cap += mw;
      return {mw, dis[edd]};
  public:
    void init(int a, int b, int n=MAXV) {
      ∨=n;
      ori = a;
      edd = b;
      for(int i=0;i<n;i++) G[i].clear();</pre>
    void addEdge(int st, int ed, WeiT w, CapT c){
   G[st].PB(Edge(ed, SZ(G[ed]), w, c));
      G[ed].PB(Edge(st, SZ(G[st])-1, -w, 0));
    PCW solve(){
      CapT cc=0; WeiT ww=0;
      while(true) {
        PCW ret = SPFA();
         if(ret.FF==-1) break;
         cc += ret.FF;
        ww += ret.SS;
      return {cc, ww};
} mcmf;
```

#### 3.6 MaximumFlow

```
class Dinic{
  private:
    using CapT = int64_t;
    struct Edge{
       int to, rev;
       CapT cap;
    };
  int n, st, ed;
    vector<vector<Edge>> G;
    vector<int> lv;
  bool BFS() {
      fill(lv.begin(), lv.end(), -1);
```

```
queue<int> bfs;
      bfs.push(st);
      lv[st] = 0;
      while(!bfs.empty()){
        int u = bfs.front(); bfs.pop();
        for(auto e: G[u]){
          if(e.cap <= 0 or lv[e.to]!=-1) continue;</pre>
          lv[e.to] = lv[u] + 1;
          bfs.push(e.to);
      }
      return (lv[ed]!=-1);
    CapT DFS(int u, CapT f) {
      if(u == ed) return f;
      CapT ret = 0;
      for (auto& e: G[u]) {
        if(e.cap <= 0 or lv[e.to]!=lv[u]+1) continue;</pre>
        CapT nf = DFS(e.to, min(f, e.cap));
        ret += nf; e.cap -= nf; f -= nf;
        G[e.to][e.rev].cap += nf;
        if(f == 0) return ret;
      if (ret == 0) lv[u] = -1;
      return ret;
 public:
   void init(int n_, int st_, int ed_){
      n = n_, st = st_, ed = ed_;
      G.resize(n); lv.resize(n);
      fill(G.begin(), G.end(), vector<Edge>());
    void add_edge(int u, int v, CapT c){
      G[u].push_back({v, (int)(G[v].size()), c});
      G[v].push back({u, (int)(G[u].size())-1, 0});
    CapT max flow() {
     CapT ret = 0;
      while (BFS()) {
        CapT f = DFS(st, numeric limits<CapT>::max());
        ret += f;
        if(f == 0) break;
      return ret;
} flow;
```

## 4 Math

#### 4.1 Prime Table

```
3210224309, 3213032591, 3217689851, 3218469083, 3219857533, 3231880427, 3235951699, 3273767923, 3276188869, 3277183181, 3282463507, 3285553889, 3319309027, 3327005333, 3327574903, 3341387953, 3373293941, 3380077549, 3380892997, 3381118801, 3384716479, 3386991323
```

## 4.2 ax+by=gcd

```
// By Adrien1018 (not knowing how to use.
// ax+ny = 1, ax+ny == ax == 1 (mod n)
tuple<int, int, int> extended_gcd(int a, int b) {
   if (!b) return make_tuple(a, 1, 0);
   int d, x, y;
   tie(d, x, y) = extended_gcd(b, a % b);
   return make_tuple(d, y, x - (a / b) * y);
}
// ax+by = gcd (by Eddy1021
PII gcd(int a, int b) {
   if(b == 0) return {1, 0};
   PII q = gcd(b, a % b);
   return {q.second, q.first - q.second * (a / b)};
}
```

## 4.3 Pollard Rho

```
// coded by hanhanW
// does not work when n is prime
long long modit(long long x,long long mod) {
  if(x \ge mod) x = mod;
  //if(x<0) x+=mod;
  return x;
long long mult(long long x,long long y,long long mod) {
  long long s=0, m=x%mod;
  while(v) {
   if(y&1) s=modit(s+m, mod);
    y >> = 1;
    m=modit(m+m, mod);
  return s;
long long f(long long x,long long mod) {
  return modit(mult(x,x,mod)+1,mod);
long long pollard_rho(long long n) {
  if(!(n&1)) return 2;
  while (true) {
    long long y=2, x=rand()%(n-1)+1, res=1;
    for (int sz=2; res==1; sz*=2) {
      for (int i=0; i<sz && res<=1; i++) {</pre>
        x = f(x, n);
        res = \_gcd(abs(x-y), n);
      y = x;
    if (res!=0 && res!=n) return res;
```

## 4.4 Linear Sieve

```
const int N = 20000000;
bool sieve[N];

void linear_sieve() {
  vector<int> prime;
  for (int i=2; i<N; i++) {
    if (!sieve[i]) prime.push_back(i);
    for (int j=0; i*prime[j]<N; j++)
    {
       sieve[i*prime[j]] = true;
       if (i % prime[j] == 0) break;
    }
  }
}</pre>
```

### 4.5 NloglogN Sieve

```
bool notprime[N];
vector<int> primes;

void Sieve(int n) {
    // reverse true false for quicker
    for(int i=2;i<=n,i++) {
        if(!notprime[i]) {
            primes.push_back(i);
            for(int j=i*i;j<=n;j+=i) notprime[i]=true;
        }
    }
}</pre>
```

## 4.6 Range Sieve

```
#include <algorithm>
typedef long long lld;
const int MAX_SQRT_B = 50000;
const int MAX L = \overline{2000000} + 5;
bool is_prime_small[MAX_SQRT_B];
bool is_prime[MAX_L];
void sieve(lld,lld);
void sieve(lld l, lld r) {
  for(lld i=2;i*i<r;i++) is_prime_small[i] = true;</pre>
  for(lld i=1;i<r;i++) is_prime[i-1] = true;</pre>
  if(l==1) is prime[0] = false;
 for(lld i=2;i*i<r;i++){
    if(!is prime small[i]) continue;
    for(lld j=i*i;j*j<r;j+=i) is_prime_small[j]=false;</pre>
    for (lld j=std::max(2LL, (l+i-1)/i)*i;j<r;j+=i)</pre>
        is_prime[j-l]=false;
```

#### 4.7 Miller Rabin

```
lld modu(lld a, lld m) {
 while(a >= m) a -= m;
  return a;
lld mul(lld a, lld b, lld m) {
 if(a < b) swap(a, b);
 11d ret = 0:
 while(b){
   if(b & 1) ret = modu(ret+a, m);
    a = modu(a+a, m);
   b >>= 1;
 return ret;
lld qPow(lld a, lld k, lld m) {
 11d ret = 1;
 a %= m;
 while(k) {
   if(k & 1) ret = mul(ret, a, m);
    a = mul(a, a, m);
   k >>= 1;
 return modu(ret, m);
bool witness(lld a, lld s, int t, lld n) {
 lld b = qPow(a, s, n);
  if(b == 0) return false;
 while(t--){
   lld bb = mul(b, b, n);
    if(bb == 1 and b != 1 and b != n-1) return true;
   b = bb:
 return b != 1;
bool miller_rabin(lld n) {
  if(n < 2) return false;</pre>
  if(!(n & 1)) return (n==2);
  11d x = n-1; int t = 0;
 while(!(x&1)) x >>= 1, t++;
```

#### 4.8 Inverse Element

```
// x's inverse mod k
// if k is prime
long long GetInv(long long x, long long k) {
    return qPow(x, k-2);
}

// x's inverse mod k
// if k is not prime
long long GetInv(long long x, long long k) {
    return qPow(x, Euler(k)-1);
}

// or extended_gcd(x, k).second
// if you need [1, x] (most use: [1, k-1]
void solve(int x, long long k) {
    inv[1] = 1;
    for(int i=2;i<x;i++)
        inv[i] = ((long long)(k - k/i) * inv[k % i]) % k;
}</pre>
```

#### 4.9 Euler Phi Function

```
inline int64_t Euler(int x) {
  int64_t r=1;
  for (int i=2;i*i<=x;++i) {</pre>
    if (x%i==0) {
      x/=i;
      r*=(i-1):
      while (x%i==0) {
        x/=i;
         r*=i;
      }
    }
  if(x>1) r*=x-1;
  return r;
vector<int> primes;
bool notprime[N];
int64 t phi[N];
inline void euler sieve(int n) {
    for (int i=2; i < n; i++) {</pre>
         if(!notprime[i]){
             primes.push_back(i);
             phi[i] = i-\overline{1};
         for(auto j: primes) {
             if(i*j >= n) break;
             notprime[i*j] = true;
             phi[i*j] = phi[i] * phi[j];
             if(i % j == 0){
                  phi[i*j] = phi[i] * j;
                  break;
         }
    }
}
```

#### 4.10 Gauss Elimination

```
#include <cmath>
#include <algorithm>
typedef long double llf;
const int N = 300;
const llf EPS = 1e-8;

// make m[i][i] = x, m[i][j] = 0
// v is for solving equation:
```

```
// for(int i=0;i<n;i++) ans[pos[i]] = val[i]/mtx[i][pos 4.12 Chinese Remainder
// for(int i=0;i<n;i++) cout << ans[i] << '\n';
bool Gauss(llf m[N][N], llf v[N], int n, int pos[N]){
 for (int i=0;i<n;i++) {</pre>
    int x=-1, y=-1; llf m = 0;
    for (int j=i; j < n; j++) for (int k=i; k < n; k++) {</pre>
      if(fabs(m[j][pos[k]])>m){
        m = fabs(m[j][pos[k]]);
        x = j, y = k;
      }
    if(x==-1 or y==-1) return false;
    swap(m[x], m[i]);
    swap(v[x], v[i]);
    swap(pos[y], pos[i]);
    for (int j=i+1; j<n; j++) {</pre>
      llf xi = m[j][pos[i]]/m[i][pos[i]];
      for(int k=0; k<n; k++) m[j][pos[k]] -= xi*m[i][pos[</pre>
          k]];
      v[j] -= xi*v[i];
  for (int i=n-1;i>=0;i--) {
    for (int j=i-1; j>=0; j--) {
      11f xi = m[j][pos[i]]/m[i][pos[i]];
for(int k=0;k<n;k++) m[j][pos[k]] -= xi*m[i][pos[</pre>
           k]];
      v[j] = xi*v[i];
 return true;
```

#### 4.11 Fast Fourier Transform

```
polynomial multiply:
FFT(a, N, true);
FFT(b, N, true);
for (int i=0; i < MAXN; i++) c[i] = a[i] * b[i];
FFT(c, N, false);
yeah~ go result in c
(N must be 2^k and >= len(a) + len(b))
typedef long double llf;
typedef complex<llf> cplx;
const int MAXN = 262144;
const llf PI = acos((llf)-1);
cplx A[MAXN], B[MAXN], C[MAXN], omega[MAXN+1];
void init omega() {
 const cplx I = {0, 1};
  for(int i=0;i<=MAXN;i++) omega[i] = exp(i*2*PI/MAXN*I</pre>
void FFT(cplx arr[], int n, bool ori){
 // n must be 2^k
  int theta = MAXN / n;
 for (int len=n; len>=2; len>>=1) {
    int tot = len>>1;
    for (int i=0;i<tot;i++) {</pre>
      cplx omg = omega[ori?i*theta%MAXN:MAXN-(i*theta%
         MAXN)];
      for(int j=i;j<n;j+=len){</pre>
        int k = j+tot;
        cplx x = arr[j] - arr[k];
        arr[j] += arr[k];
        arr[k] = omg * x;
    theta = (theta * 2) % MAXN;
  int i = 0:
  for (int j=1; j<n-1; j++) {</pre>
    for (int k=n>>1; k>(i^=k); k>>=1);
    if(j < i) swap(arr[j], arr[i]);</pre>
  if(ori) return;
  for (int i=0; i<n; i++) arr[i] /= n;</pre>
```

```
// ax+ny = 1, ax+ny == ax == 1 \pmod{n}
pair<lld, lld> gcd(lld a, lld b) {
 if(b == 0) return {1, 0};
  pair<lld,lld>q = gcd(b, a % b);
  return {q.second, q.first - q.second * (a / b)};
lld crt(lld ans[], lld pri[], int n) {
    11d M = 1;
    for (int i=0;i<n;i++) M *= pri[i];</pre>
    11d ret = 0;
    for (int i=0; i < n; i++) {</pre>
        lld inv = (gcd(M/pri[i], pri[i]).first + pri[i
            ])%pri[i];
        ret += (ans[i] * (M/pri[i]) %M * inv) %M;
        ret %= M;
    return ret;
```

#### 4.13 NTT

```
typedef long long LL;
// Remember coefficient are mod P
/* p=a*2^n+1
       2^n
   n
                                    root
        32
                   97
   6
        64
                    193
                               3
                    257
       128
                               2
                    257
   8
       256
                               7
   9
        512
                    7681
                               15
                                    17
                    12289
   10
       1024
   11
        2048
                    12289
                               6
                                    11
                    12289
       4096
   12
                                    11
   13
       8192
                    40961
                               5
   14
        16384
                    65537
                               4
                                    3
       32768
   15
                    65537
   16
        65536
                    65537
       131072
                    786433
   17
                                    10
                               6
   18
                                    10 (605028353,
       262144
                    786433
       2308, 3)
   19
       524288
                    5767169
   20
       1048576
                    7340033
                                    .3
                    23068673
   21
       2097152
                               11
                    104857601 25
   22
        4194304
   23
       8388608
                    167772161
                               20
       16777216
                   167772161 10
   24
   25
        33554432
                    167772161
                                    3 (1107296257, 33,
       10)
   26
       67108864
                    469762049
                   2013265921 15
                                    31 */
   27
       134217728
// (must be 2^k)
// To implement poly. multiply:
// NTT<P, root, MAXN> ntt;
// ntt( n , a ); // or ntt.tran( n , a );
// ntt( n , b );
// for( int i = 0 ; i < n ; i++ )
    c[i] = a[i] * b[i];
// ntt(n,c,1);
// then you have the result in c :: [LL]
template<LL P, LL root, int MAXN>
struct NTT{
  static LL bigmod(LL a, LL b) {
   LL res = 1;
    for (LL bs = a; b; b >>= 1, bs = (bs * bs) % P) {
     if(b&1) res=(res*bs)%P;
   return res;
  static LL inv(LL a, LL b) {
    if(a==1)return 1;
    return (((LL)(a-inv(b%a,a))*b+1)/a)%b;
 LL omega[MAXN+1];
 NTT() {
    omega[0] = 1;
    LL r = bigmod(root, (P-1)/MAXN);
    for (int i=1; i<=MAXN; i++)</pre>
      omega[i] = (omega[i-1]*r)%P;
```

```
// n must be 2^k
  void tran(int n, LL a[], bool inv ntt=false) {
    int basic = MAXN / n;
    int theta = basic;
    for (int m = n; m >= 2; m >>= 1) {
      int mh = m >> 1;
      for (int i = 0; i < mh; i++) {</pre>
        LL w = omega[i*theta%MAXN];
        for (int j = i; j < n; j += m) {</pre>
          int k = j + mh;
          LL x = a[j] - a[k];
          if (x < 0) x += P;
          a[j] += a[k];
          if (a[j] > P) a[j] -= P;
          a[k] = (w * x) % P;
      theta = (theta * 2) % MAXN;
    int i = 0;
    for (int j = 1; j < n - 1; j++) {</pre>
      for (int k = n >> 1; k > (i ^= k); k >>= 1);
      if (j < i) swap(a[i], a[j]);</pre>
    if (inv ntt) {
      LL ni = inv(n, P);
      reverse( a+1 , a+n );

for (i = 0; i < n; i++)
        a[i] = (a[i] * ni) % P;
  void operator()(int n, LL a[], bool inv_ntt=false) {
    tran(n, a, inv ntt);
};
const LL P=2013265921, root=31;
const int MAXN=4194304;
NTT<P, root, MAXN> ntt;
```

# 5 Geometry

## 5.1 Point Class

```
template<typename T>
struct Point{
    typedef long double llf;
    static constexpr llf EPS = 1e-8;
    Т х, у;
    Point(): x(0), y(0){}
Point(T _, T __): x(_), y(__){}
    template<typename T2>
    Point(const Point<T2>& a): x(a.x), y(a.y){}
    inline llf theta() const {
        return atan2((llf)y, (llf)x);
    inline llf dis() const {
        return hypot((llf)x, (llf)y);
    inline llf dis(const Point& o) const {
        return hypot((llf)(x-o.x), (llf)(y-o.y));
    Point operator-(const Point& o) const {
        return Point(x-o.x, y-o.y);
    Point operator = (const Point @ o) {
       x-=o.x, y-=o.y;
        return *this;
    Point operator+(const Point& o) const {
        return Point(x+o.x, y+o.y);
    Point operator+=(const Point& o) {
       x+=o.x, y+=o.y;
return *this;
    Point operator* (const T& k) const {
        return Point(x*k, y*k);
    Point operator*=(const T& k) {
        x*=k, y*=k;
```

```
return *this;
    Point operator/(const T& k) const {
        return Point(x/k, y/k);
    Point operator/=(const T& k) {
        x/=k, y/=k;
        return *this;
    Point operator-() const {
        return Point(-x, -y);
    Point rot90() const {
        return Point(-y, x);
    bool equal(const Point& o, true type) const {
        return fabs(x-o.x) < EPS and fabs(y-o.y) < EPS;
    bool equal(const Point& o, false type) const {
        return x==0.x and y==0.y;
    bool operator==(const Point& o) const {
        return equal(o, is_floating_point<T>());
    bool operator!=(const Point& o) const {
        return ! (*this == 0);
    bool operator<(const Point& o) const {</pre>
        return theta() < o.theta();</pre>
        // sort like what pairs did
        // return fabs(x-o.x) < EPS?y < o.y:x < o.x;
    friend inline T cross(const Point& a, const Point&
        b) {
        return a.x*b.v - b.x*a.v;
    friend inline T dot(const Point& a, const Point &b)
        return a.x*b.x + a.y*b.y;
    friend ostream& operator<<(ostream& ss, const Point</pre>
        } (o &
        ss<<"("<<o.x<<", "<<o.y<<")";
        return ss;
};
```

#### 5.2 Circle Class

```
template<typename T>
struct Circle{
    Point<T> o:
    Tr;
    vector<Point<llf>> operator&(const Circle& aa)
       const {
        // https://www.cnblogs.com/wangzming/p/8338142.
            h+m1
        llf d=o.dis(aa.o);
        if(d > r+aa.r+EPS or d < fabs(r-aa.r)-EPS)</pre>
            return {};
        llf dt = (r*r - aa.r*aa.r)/d, d1 = (d+dt)/2;
        Point<llf> dir = (aa.o-o); dir /= d;
        Point<llf> pcrs = dir*d1 + o;
        dt=sqrt(max(0.0L, r*r - d1*d1)), dir=dir.rot90
            ();
        return {pcrs + dir*dt, pcrs - dir*dt};
};
```

## 5.3 Line Class

```
const Point<long double> INF_P(-1e20, 1e20);
const Point<long double> NOT_EXIST(1e20, 1e-20);
template<typename T>
struct Line{
    static constexpr long double EPS = 1e-8;
    // ax+by+c = 0
    T a, b, c;
    Line(): a(0), b(1), c(0){}
    Line(T_, T__, T__): a(_), b(_), c(__){
        assert(fabs(a)>EPS or fabs(b)>EPS);
    }
```

```
template<typename T2>
    Line(const Line<T2>& x): a(x.a), b(x.b), c(x.c) {}
    typedef Point<long double> Pt;
    bool equal(const Line& o, true type) const {
        return fabs(a-o.a) < EPS and fabs(b-o.b) < EPS
            and fabs(c-o.b) < EPS;</pre>
    bool euqal(const Line& o, false type) const {
        return a==o.a and b==o.b and c==o.c;
    bool operator==(const Line& o) const {
        return euqal(o, is_floating_point<T>());
    bool operator!=(const Line& o) const {
        return ! (*this == 0);
    friend inline bool on_line__(const Point<T>& p,
        const Line& 1, true_type) {
        return fabs(l.a*p.x + l.b*p.y + l.c) < EPS;</pre>
    friend inline bool on line (const Point<T>& p,
        const Line& 1, false_type) {
        return 1.a*p.x + 1.b*p.y + 1.c == 0;
    friend inline bool on line(const Point<T>&p const
        Line& 1) {
        return on_line__(p, 1, is_floating_point<T>());
    friend inline bool is_parallel__(const Line& x,
        const Line& y, true type) {
        return fabs(x.a*y.b - x.b*y.a) < EPS;</pre>
    friend inline bool is_parallel__(const Line& x,
        const Line& y, false_type) {
        return x.a*y.b == x.\overline{b}*y.a;
    friend inline bool is parallel(const Line& x, const
         Line& y) {
        return is_parallel__(x, y, is_floating_point<T</pre>
    friend inline Pt get inter(const Line& x, const
        Line& y) {
        typedef long double llf;
        if(x==y) return INF P;
        if(is parallel(x, y)) return NOT EXIST;
        llf delta = x.a*y.b - x.b*y.a;
        llf delta_x = x.b*y.c - x.c*y.b;
llf delta_y = x.c*y.a - x.a*y.c;
        return Pt (delta_x / delta, delta_y / delta);
    friend ostream& operator<<(ostream& ss, const Line&</pre>
        0){
        ss<<o.a<<"x+"<<o.b<<"y+"<<o.c<<"=0";
        return ss;
template<typename T>
inline Line<T> get_line(const Point<T>& a, const Point<</pre>
    T>& b) {
    return Line<T>(a.y-b.y, b.x-a.x, (b.y-a.y) *a.x-(b.x
        -a.x) *a.v);
```

## 5.4 Segment Class

```
const long double EPS = 1e-8;
template<typename T>
struct Segment{
  // p1.x < p2.x
  Line<T> base;
  Point<T> p1, p2;
 \label{eq:segment} Segment(): base(Line<T>()), p1(Point<T>()), p2(Point<
      T>()){
    assert (on line (p1, base) and on line (p2, base));
 Segment(Line<T>
                     _, Point<T> ___, Point<T> ___): base(_
    ), p1(_), p2(_) {
assert(on_line(p1, base) and on_line(p2, base));
  template<typename T2>
  Segment(const Segment<T2>& ): base( .base), p1( .p1)
      , p2(_.p2) {}
  typedef Point<long double> Pt;
```

```
friend bool on segment(const Point<T>& p, const
      Segment& 1) {
    if(on line(p, l.base))
      return (1.p1.x-p.x) * (p.x-1.p2.x) >= 0 and (1.p1.y-p
         .y) * (p.y-1.p2.y) >=0;
   return false;
  friend bool have_inter(const Segment& a, const
      Segment& b) {
    if(is parallel(a.base, b.base)){
      return on_segment(a.p1, b) or on_segment(a.p2, b)
           or on_segment(b.p1, a) or on_segment(b.p2, a
    Pt inter = get inter(a.base, b.base);
    return on segment (inter, a) and on segment (inter, b
        );
  friend inline Pt get inter(const Segment& a, const
      Segment& b) {
    if(!have inter(a, b)){
      return NOT EXIST;
    }else if(is_parallel(a.base, b.base)){
      if(a.p1 == b.p1) {
       if(on segment(a.p2, b) or on segment(b.p2, a))
            return INF P;
        else return a.p1;
     }else if(a.p1 == b.p2){
       if(on_segment(a.p2, b) or on_segment(b.p1, a))
            return INF P;
        else return a.pl;
      }else if(a.p2 == b.p1) {
       if(on_segment(a.p1, b) or on_segment(b.p2, a))
            return INF P;
        else return a.p2;
      }else if(a.p2 == b.p2) {
       if(on segment(a.pl, b) or on segment(b.pl, a))
            return INF_P;
        else return a.p2;
      return INF P;
    return get inter(a.base, b.base);
  friend ostream& operator<<(ostream& ss, const Segment</pre>
      1(0 3
    ss<<o.base<<", "<<o.p1<<" ~ "<<o.p2;
   return ss;
};
template<typename T>
inline Segment<T> get segment(const Point<T>& a, const
    Point<T>& b) {
  return Segment<T>(get line(a, b), a, b);
```

#### 5.5 Triangle Circumcentre

#### 5.6 2D Convex Hull

```
template<typename T>
class ConvexHull_2D{
  private:
```

```
typedef Point<T> PT;
    vector<PT> dots:
    struct myhash{
      uint64 t operator()(const PT& a) const {
        uint\overline{6}4 t xx=0, yy=0;
        \texttt{memcpy(\&xx, \&a.x, sizeof(a.x));}
        memcpy(&yy, &a.y, sizeof(a.y));
        uint64 t ret = xx*17+yy*31;
        ret = (\text{ret } ^ (\text{ret } >> 16))*0x9E3779B1;
        ret = (ret ^ (ret >> 13)) *0xC2B2AE35;
        ret = ret ^ xx;
        return (ret ^ (ret << 3)) * yy;</pre>
      }
    unordered set<PT, myhash> in hull;
  public:
    inline void init() {in hull.clear(); dots.clear();}
    void insert(const PT& x) {dots.PB(x);}
    void solve(){
      sort(ALL(dots), [](const PT& a, const PT& b){
        return tie(a.x, a.y) < tie(b.x, b.y);</pre>
      });
      vector<PT> stk(SZ(dots)<<1);
      int top = 0;
      for(auto p: dots) {
        while(top >= 2 and cross(p-stk[top-2], stk[top
            -1]-stk[top-2]) <= 0)
          t.op --:
        stk[top++] = p;
      for(int i=SZ(dots)-2, t = top+1;i>=0;i--){
        while(top >= t and cross(dots[i]-stk[top-2],
            stk[top-1]-stk[top-2]) <= 0)
          top --;
        stk[top++] = dots[i];
      stk.resize(top-1);
      swap(stk, dots);
      for(auto i: stk) in hull.insert(i);
    vector<PT> get() {return dots;}
    inline bool in it(const PT& x){
      return in hull.find(x)!=in hull.end();
};
```

## 5.7 SimulateAnnealing

```
#include <random>
#include <functional>
#include <utility>
#include <algorithm>
using namespace std;
double getY(double);
int main(){
    int rr, 11;
    default random engine rEng(time(NULL));
 uniform_real_distribution<double> Range(-1,1);
 uniform real distribution < double > expR(0,1);
 auto Random=bind(Range, rEng);
 auto expRand=bind(expR, rEng);
  int step=0;
  double pace=rr-ll, mini=0.95; // need to search for
      it
 double x=max(min(Random()*pace+ll, rr), ll), y=getY(x
      );
 while (pace>=1e-7) {
    double newX = max(min(x + Random()*pace, rr), 11);
    double newY = getY(newX);
    if(newY < y || expRand() < exp(-step))</pre>
     x=newX, y=newY;
    step++:
    pace*=mini;
double getY(double x) {
    // get y using x
    return x;
```

# 6 Stringology

#### 6.1 Hash

```
#include <string>
typedef long long lld;
const int N = 1000000;
class Hash{
    private:
        const 11d p = 127, q = 1208220623;
         int sz;
        lld prefix[N], power[N];
    public:
        void init(const std::string &x){
             sz = x.size();
             prefix[0]=0;
             for(int i=1;i<=sz;i++) prefix[i]=((prefix[i])</pre>
                 -1]*p)%q+x[i-1])%q;
             power[0]=1;
             for(int i=1;i<=sz;i++) power[i]=(power[i</pre>
                 -1]*p)%q;
         lld query(int 1, int r) {
             // 1-base (1, r)
             return (prefix[r] - (prefix[l]*power[r-l])%
                 q + q) %q;
};
```

## 6.2 Suffix Array

```
//help by http://www.geeksforgeeks.org/suffix-array-set
     -2-a-nlognlogn-algorithm/
#include <bits/stdc++.h>
using namespace std;
#define PB push back
struct sfx{
  int index;
  int r,nr;
};
char str[N + 10];
int len;
vector<sfx> srs[N + 10];
int mapping[N + 10];
sfx sa[N + 10];
bool cmp(sfx a,sfx b) {
  if(a.r==b.r){
    return a.nr<b.nr;</pre>
    return a.r<b.r;</pre>
}
void SA();
void radixSort();
int main(){
  gets(str);
  len = strlen(str);
  SA();
  for (int i=0;i<len;i++) {</pre>
    printf("%d \setminus n", sa[i].index);
  return 0;
void SA() {
  for (int i=0;i<len;i++) {</pre>
    sa[i].index = i;
    sa[i].r=str[i];
    sa[i].nr=(i+1>=len)?0:str[i+1];
  //sort(sa,sa+len,cmp);
  radixSort();
  for (int j=2;j<=len;j*=2) {</pre>
    int cnt=1;
    int rr = sa[0].r;
    sa[0].r=cnt;
```

```
mapping[sa[0].index]=0;
    for (int i=1;i<len;i++) {</pre>
      if(sa[i].r == rr && sa[i].nr == sa[i-1].nr) {
        rr=sa[i].r;
        sa[i].r=cnt;
      }else{
        rr=sa[i].r;
        sa[i].r=++cnt;
      mapping[sa[i].index]=i;
    for (int i=0;i<len;i++) {</pre>
      int nn = sa[i].index+j;
      sa[i].nr = (nn>=len)?0:sa[mapping[nn]].r;
    //sort(sa, sa+len, cmp);
   radixSort();
void radixSort(){
 int m = 0;
  for (int i=0; i<len; i++) {</pre>
   srs[sa[i].nr].PB(sa[i]);
   m=max(m,sa[i].nr);
 int cnt=0;
 for (int i=0;i<=m;i++) {</pre>
    if(srs[i].empty())continue;
    for(auto j:srs[i]){
     sa[cnt++] = j;
   srs[i].clear();
 m = 0;
 for (int i=0; i<len; i++) {</pre>
   srs[sa[i].r].PB(sa[i]);
   m=max(m,sa[i].r);
 cnt=0;
 for (int i=0;i<=m;i++) {</pre>
   if(srs[i].empty())continue;
   for (auto j:srs[i]) {
      sa[cnt++] = j;
   srs[i].clear();
```

## 6.3 KMP

```
int F[N<<1];
void KMP(char s1[], char s2[], int n, int m) {
    // make F[] for s1+'\0'+s2;
    char ss[N<<1];
    int len = n+m+1;
    for(int i=0;i<n;i++) ss[i] = s1[i];
    ss[n] = '\0';
    for(int i=0;i<m;i++) ss[i+1+n] = s2[i];
    F[0] = F[1] = 0;
    for(int i=1;i<len;i++) {
        int j = F[i];
        while(j > 0 and ss[i]!=ss[j]) j = F[j];
        F[i+1] = (ss[i]==ss[j]?j+1:0);
    }
    // just find (F[len2+i] == len2), i from 1 to len+1
        for matching
}
```