Contents

1	Basi	•																							1
-																									1
		Shell s																							
		Default																							1
		vimrc .																							1
	1.4	readcha	r																						1
	1.5	Black M	agic .																						1
	1.6	Texas h	old'em																						2
			010 0		•	•	٠	•	•	•	٠	٠	•	٠	•	•	•	•	•	•	٠	٠	٠	•	_
2	Grap	sh.																							2
_			+*																						2
		BCC Ver																							
		Bridge*																							2
		2SAT (S																							2
	2.4	Minimum	MeanCyc	:le*																					3
	2.5	Virtual	Tree*																						3
		Maximum																							3
		Minimum																							4
																									-
		Dominat																							4
		Minimum																							4
	2.10	Vizing'	s theor	em																					5
	2.11	LMinimum	Clique	Co	ver	*																			5
	2.12	Numbero	fMaxima	101	iau	*ء																			5
		Theory																							6
	2.1.	, incory			•	•	•	•	•	•	•	•	•	•	•	•	•	•	•	•	•	•	•	•	U
3	Dat:	Struct	uno																						6
2																									
	3.1	Leftist	iree		•		•	٠	٠	٠	٠	٠	٠	٠	•	٠	٠	٠	٠	٠	٠	٠	٠	٠	6
	3.2	Heavy 1	ight De	com	pos	it	io	n	•	•	•	•	•	•	•	•	•	•			•	•	•	•	6
	3.3	Centroi	d Decon	1pos	iti	on	*																		6
		Link cu																							7
		KDTree																							7
					•	•	٠	•	•	•	•	•	•	•	•	-	-	•	•	•	•	•	•	•	,
4	Flor	/Matchi	nσ																						8
-																									
	4.1	Kuhn Mu	nkres		٠	•	٠	٠	٠	•	٠	•	•	•	•	٠	٠	•	•	•	٠	٠	٠	•	8
	4.2	Mincost Maximum	Maxflow	١.	•	•	•	•	•	•	•	•	•	•	•	•	•	•			•	•	•	•	8
	4.3	Maximum	Simple	e Gr	aph	M	at	ch	in	g*															8
	4.4	Minimum	Weight	: Ma	tch	in	g	(C	li	aue	٠ د	ver	rsi	or	1)*										9
	1 5	SW-minc	+				0	`		-1			-		.,		•	•	•	•	•	•	•	•	9
		Bounded																							9
		Gomory																							10
	4.8	isap .			•	•	•	•	•	•	•	•		•	•	•	•	•			•	•	•	•	10
5	Stri	ing																							11
	5.1	KMP																							11
		Z-value																							11
		Manache																							11
		Suffix																							11
		SAIS* .																							11
	5.6	Aho-Cor	asick A	luto	mat	an																			12
		Smalles																							12
	5 8	De Brui	in coal	ienc	۰*	•	•	•	•	•	•	•	•	•	•	•	•	•	•	•	•	•	•	•	12
		SAM																							12
		PalTree																							13
	5.11	lcyclicL	cs																						13
6	Math	1																							13
	6.1	ax+by=g	cd* .																						13
		floor a																							14
	6 3	floor s	*	•	•	•	•	•	•	•	•	•	•	•	•	•	•	•	•	•	•	•	•	•	14
	0.5							•	•	•	•	•	•	•	•	•	•	•	•	•	•	•	•	•	
		M:11001. 2	um. Dah÷∽*		٠	•							•	•				•	•						14
		Miller	Rabin*																						14
	6.5	Miller Big num	Rabin* ber .	: :	:	:	:	:																	
	6.5	Miller Big num Fractio	Rabin* ber . n			:	:	:	:						:									٠	15
	6.5	Miller Big num Fractio	Rabin* ber . n			:	:	:	:						:									•	15 15
	6.5 6.6 6.7	Miller Big num Fractio Simulta	Rabin* ber . n neous E	 . qua	tio	ns	:	:	:			:	:	:	:		:	:	:	:	:	:	:		15
	6.5 6.6 6.7 6.8	Miller Big num Fractio Simulta Pollard	Rabin* ber . n neous E Rho .	· · ·	tio	ns	:		:				:	:	:			:	:	:	:	:	:	:	
	6.5 6.6 6.7 6.8 6.9	Miller Big num Fractio Simulta Pollard Simplex	Rabin* ber . n neous E Rho . Algori	qua	tio	ns	:	•	:													:	:		15 15 15
	6.5 6.6 6.7 6.8 6.9	Miller Big num Fractio Simulta Pollard Simplex	Rabin* ber . n neous E Rho . Algori	qua	tio	ns	:	•	:													:	:		15 15 15 16
	6.5 6.6 6.7 6.8 6.9 6.10 6.11	Miller Big num Fractio Simulta Pollard Simplex Ochinese	Rabin* ber . n neous E Rho . Algori Remaind icResid	qua qua thm ler	: : : tio : :	ns																			15 15 15 16 16
	6.5 6.6 6.7 6.8 6.9 6.10 6.11 6.12	Miller Big num Fractio Simulta Pollard Simplex Ochinese Quadrat	Rabin* ber . n neous E Rho . Algori Remaind icResid	qua qua thm ler lue	tio : :	ns																			15 15 15 16 16 16
	6.5 6.6 6.7 6.8 6.9 6.10 6.11 6.12	Miller Big num Fractio Simulta Pollard Simplex Ochinese	Rabin* ber . n neous E Rho . Algori Remaind icResid	qua qua thm ler lue	tio : :	ns																			15 15 15 16 16
	6.5 6.6 6.7 6.8 6.9 6.10 6.11 6.12	Miller Big num Fractio Simulta Pollard Simplex Chinese Quadrat PriCount	Rabin* ber . n neous E Rho . Algori Remaind icResid	qua qua thm ler lue	tio : :	ns																			15 15 15 16 16 16
7	6.5 6.6 6.7 6.8 6.9 6.10 6.11 6.12	Miller Big num Fractio Simulta Pollard Simplex Chinese Quadrat Pricount Brrimes	Rabin* ber . n neous E Rho . Algori Remaind icResid	equant thm der lue	tio																				15 15 15 16 16 16
7	6.5 6.6 6.7 6.8 6.9 6.10 6.11 6.12	Miller Big num Fractio Simulta Pollard Simplex Chinese Quadrat Pricount Brrimes	Rabin* ber . n neous E Rho . Algori Remaind icResid	equant thm der lue	tio																				15 15 15 16 16 16
7	6.5 6.6 6.7 6.8 6.9 6.10 6.11 6.12 7.1	Miller Big num Fractio Simulta Pollard Simplex Chinese Quadrat PriCount Brrimes (momial Fast Fo	Rabin* ber . n neous E Rho . Algori Remainc icResic	qua thm ler lue	tio																				15 15 15 16 16 16 16
7	6.5 6.6 6.7 6.8 6.10 6.11 6.12 6.13 Poly 7.1 7.2	Miller Big num Fractio Simulta Pollard Simplex Chinese Quadrat PriCount Brimes Vnomial Fast Fo Number	Rabin* ber n neous E Rho . Algori Remainc icResic urier 1 Theory	ithm ler lue	tio	ns																			15 15 16 16 16 16 16
7	6.5 6.6 6.7 6.8 6.9 6.13 6.13 Poly 7.1 7.2 7.3	Miller Big num Fractio Simulta Pollard Simplex Chinese Quadrat PiCount Brimes vnomial Fast Fo Number Fast Wa	Rabin* ber . n neous E Rho . Algori Remain icResic urier 1 Theory lsh Tra	ithm ler lue	tio sfo																				15 15 16 16 16 16 16 16 17
7	6.5 6.6 6.7 6.8 6.9 6.13 6.13 Poly 7.1 7.2 7.3	Miller Big num Fractio Simulta Pollard Simplex Chinese Quadrat PriCount Brimes Vnomial Fast Fo Number	Rabin* ber . n neous E Rho . Algori Remain icResic urier 1 Theory lsh Tra	ithm ler lue	tio sfo																				15 15 16 16 16 16 16
	6.5 6.6 6.7 6.8 6.9 6.16 6.12 6.13 7.1 7.2 7.3 7.4	Miller Big num Fractio Simulta Pollard Simplex Ochinese Quadrat PriCount Brrimes vnomial Fast Fo Number Fast Wa Polynom	Rabin* ber . n neous E Rho . Algori Remain icResic urier 1 Theory lsh Tra	ithm ler lue	tio sfo																				15 15 16 16 16 16 16 17 17
7	6.5 6.6 6.7 6.8 6.9 6.16 6.12 6.13 7.1 7.2 7.3 7.4 Geom	Miller Big num Fractio Simulta Pollard Simplex Ochinese Quadrat Pricount Primes Vnomial Fast Fo Number Fast Wa Polynom metry	Rabin* ber n n neous E Rho Algori Remaind icResid urier 1 Theory lsh Tra ial Ope	equa thmm der due Tran Tran	tio sfo nsf	ns rm ori																			15 15 16 16 16 16 16 17 17 17
	6.5 6.6 6.7 6.8 6.9 6.11 6.12 6.13 7.1 7.2 7.3 7.4 Geom	Miller Big num Fractio Simulta Pollard Simplex Cchinese Quadrat PriCount Primes Vnomial Fast Fo Number Fast Wa Polynom Metry Default	Rabin* ber n neous E Rho . Algori Remain icResic Urrier T Theory lsh Tra ial Ope	qua ithm der lue Tran Tran annsferat	tio sfo nsf orm																				15 15 16 16 16 16 16 17 17 17 17
	6.5 6.6 6.7 6.8 6.9 6.11 6.12 6.13 7.1 7.2 7.3 7.4 Geom 8.1 8.2	Miller Big num Fractio Simulta Pollard Simplex Ochinese Quadrat PriCount PriCount Primes Momial Fast Fo Number Fast Wa Polynom Default Convex	Rabin* ber n neous E Rho Algori Remain icResic Urrier 1 Theory lsh Tra ial Ope Code hull*	icquarionic in the control of the co	tio sfo nsf		m																		15 15 16 16 16 16 16 17 17 17
	6.5 6.6 6.7 6.8 6.9 6.11 6.12 6.13 7.1 7.2 7.3 7.4 Geom 8.1 8.2	Miller Big num Fractio Simulta Pollard Simplex Cchinese Quadrat PriCount Primes Vnomial Fast Fo Number Fast Wa Polynom Metry Default	Rabin* ber n neous E Rho Algori Remain icResic Urrier 1 Theory lsh Tra ial Ope Code hull*	icquarionic in the control of the co	tio sfo nsf		m																		15 15 16 16 16 16 16 17 17 17 17
	6.5 6.6 6.7 6.8 6.9 6.10 6.13 7.1 7.2 7.3 7.4 Geon 8.1 8.2 8.3 8.4	Miller Big num Fractio Simulta Pollard Simplex Cchinese LQuadrat Pricount Primes Vnomial Fast Fo Number Fast Wa Polynom Metry Default Convex Externa Heart .	Rabin* ber . n neous E Rho . Algori Remaind icResid Urier T Theory lsh Tra ial Ope Code hull* l bised	iqua iqua ithm der due in Tran Tran Tran Tran insferat	tio sfo nsf orm																				15 15 16 16 16 16 16 17 17 17 18 18 18
	6.5 6.6 6.7 6.8 6.9 6.10 6.13 7.1 7.2 7.3 7.4 Geon 8.1 8.2 8.3 8.4	Miller Big num Fractio Simulta Pollard Simplex Cchinese LQuadrat Pricount Primes Vnomial Fast Fo Number Fast Wa Polynom Metry Default Convex Externa Heart .	Rabin* ber . n neous E Rho . Algori Remaind icResid Urier T Theory lsh Tra ial Ope Code hull* l bised	iqua iqua ithm der due in Tran Tran Tran Tran insferat	tio sfo nsf orm																				15 15 15 16 16 16 16 17 17 17 17 18 18 18 18
	6.5 6.6 6.7 6.8 6.9 6.11 6.12 7.1 7.2 7.3 7.4 Geon 8.1 8.3 8.4 8.5	Miller Big num Fractio Simulta Pollard Simplex Cchinese LQuadrat Pricount Bricount Fast Fo Number Fast Wa Polynom Metry Default Convex Extern Minimum	Rabin* ber n neous E Rho . Algori Remaind icResid Urier T Theory lsh Traial Ope Code hull* l bised Circle	in the second se	tio sfoonsform		m																		15 15 16 16 16 16 16 17 17 17 17 18 18 18 18 18 19
	6.5 6.6 6.7 6.8 6.9 6.11 6.12 7.1 7.2 7.3 7.4 Geom 8.1 8.2 8.3 8.4 8.5 8.6	Miller Big num Fractio Simulta Pollard Simplex Ochinese Quadrat PriCount Primes Vnomial Fast Fo Number Fast Wa Polynom Metry Convex Externa Heart . Minimum Mpolar A Minimum Mpolar A Molar Number	Rabin* ber . n neous E Rho . Algori Remainc icResic Urier T Theory lsh Tra ial Ope Code hull* l bisec Circle ngle So	in the contract of the contrac	tio sfoonsform ver																				15 15 16 16 16 16 16 17 17 17 17 18 18 18 18 18 19 19
	6.5 6.6 6.7 6.8 6.9 6.11 6.12 6.13 7.1 7.2 7.3 7.4 Geon 8.1 8.2 8.3 8.4 8.5 8.6 8.7	Miller Big num Fractio Simulta Pollard Simplex Ochinese Quadrat Pricount Brimes Momial Fast Fo Number Fast Wa Polynom Metry Default Convex Externa Heart Minimum Polar A Interse	Rabin* ber . n neous E Rho . Algori Remainc icResic Urier I Theory lsh Tra ial Ope Code hull* l bisec circle ngle Sc ction c	icquaric icq	tio sfo sfo rm ver wo				· · · · · · · · · · · · · · · · · · ·																15 15 16 16 16 16 16 17 17 17 18 18 18 18 19 19
	6.5 6.6 6.7 6.8 6.10 6.11 7.2 7.3 7.4 Geon 8.1 8.2 8.3 8.4 8.5 8.6 8.8	Miller Big num Fractio Simulta Pollard Simplex Ochinese Quadrat Pricount Brimes Vnomial Fast Fo Number Fast Wa Polynom Default Convex Externa Externa Heart Minimum Polar A Interse Interse	Rabin* ber . n neous E Rho . Algori Remaind icResid Urier T Theory lsh Tra ial Ope Code hull* circle ngle Sc ction c ction c	icquarion icquar	tio sfoonsform ver wo oolv		m rc		· · · · · · · · · · · · · · · · · · ·																15 15 16 16 16 16 16 17 17 17 17 18 18 18 18 18 19 19
	6.5 6.6 6.7 6.8 6.10 6.11 7.2 7.3 7.4 Geon 8.1 8.2 8.3 8.4 8.5 8.6 8.8	Miller Big num Fractio Simulta Pollard Simplex Ochinese Quadrat Pricount Brimes Vnomial Fast Fo Number Fast Wa Polynom Default Convex Externa Externa Heart Minimum Polar A Interse Interse	Rabin* ber . n neous E Rho . Algori Remaind icResid Urier T Theory lsh Tra ial Ope Code hull* circle ngle Sc ction c ction c	icquarion icquar	tio sfoonsform ver wo oolv		m rc		· · · · · · · · · · · · · · · · · · ·																15 15 16 16 16 16 16 17 17 17 18 18 18 18 19 19
	6.5 6.6 6.7 6.8 6.10 6.11 6.12 7.1 7.2 7.3 7.4 Geon 8.1 8.2 8.3 8.4 8.5 8.8 8.9	Miller Big num Fractio Simulta Pollard Simplex Ochinese Quadrat Pricount Brimes Vnomial Fast Fo Number Fast Wa Polynom Default Convex Externa Heart Minimum Polar A Interse Interse	Rabin* ber . n neous E Rho . Algori Remainc icResic Urier T Theory lsh Tra ial Ope Code hull* circle ngle Sc ction c ction c ction c		tio sfonsform wo only ine						· · · · · · · · · · · · · · · · · · ·														15 15 16 16 16 16 17 17 17 18 18 18 18 19 19
	6.5 6.6 6.7 6.19 6.11 6.12 7.1 7.2 7.3 7.4 Geon 8.1 8.2 8.3 8.4 8.5 8.6 8.7 8.8	Miller Big num Fractio Simulta Pollard Simplex Cchinese LQuadrat Pricount Bricount Bricount Convex Extern Minimum Polar A Interse Interse Interse Interse	Rabin* ber . n neous E Rho . Algori Remaind icResid Urier T Theory lsh Tra ial Ope Code hull* circle ngle Sc ction c ction c ction c ction c n circle	ithm der due Tran Tran ansferat ttor pf to	tio sfonsform wo oly ine						· · · · · · · · · · · · · · · · · · ·														15 15 16 16 16 16 17 17 17 18 18 18 18 19 19 19 19
	6.5 6.6 6.7 6.8 6.10 6.11 7.1 7.2 7.3 7.4 Geom 8.1 8.2 8.3 8.5 8.6 8.7 8.8 8.9 8.10 8.11	Miller Big num Fractio Simulta Pollard Simplex Ochinese Quadrat Pricount Brimes Vnomial Fast Fo Number Fast Wa Polynom Metry Convex Externa Heart . Minimum Polar A Interse Interse Interse Interse inHalf pl	Rabin* ber . n neous E Rho . Algori Remainc icResic Urier I Theory Ish Tra ial Ope Code hull* I bisec ction c ction c ction c ction c in circla ane int	ran. Tran. T	tio sfoonsformmion ver voly ect		mrc				· · · · · · · · · · · · · · · · · · ·	· · · · · · · · · · · · · · · · · · ·													15 15 16 16 16 16 17 17 17 18 18 18 18 19 19 19 19 19
	6.5 6.6 6.7 6.9 6.11 6.12 6.13 7.1 7.2 7.3 7.4 Geon 8.1 8.2 8.3 8.4 8.5 8.8 8.9 8.18	Miller Big num Fractio Simulta Pollard Simplex Ochinese Quadrat Pricount Brimes Vnomial Fast Fo Number Fast Wa Polynom Default Convex Externa Heart Minimum Polar A Interse	Rabin* ber . n neous E Rho . Algori Remainc icResic Theory lsh Tra ial Ope Code hull* lbisec ction c	thmmler lue	tio sfoonsform ver wo oly ine ect						· · · · · · · · · · · · · · · · · · ·														15 15 16 16 16 16 17 17 17 18 18 18 18 19 19 19 19 19 19 19 19 20
	6.5 6.6 6.7 6.9 6.11 6.12 6.13 7.1 7.2 7.3 7.4 Geon 8.1 8.5 8.6 8.7 8.8 8.9 8.10 8.11 8.12 8.13	Miller Big num Fractio Simulta Pollard Simplex Ochinese Quadrat PriCount Brimes Vnomial Fast Fo Number Fast Wa Polynom Default Convex Externa Heart Minimum Polar A Interse Interse Interse Interse Jopint i Half pl CCircleC 33Dpoint	Rabin* ber . n neous E Rho . Algori Remainc icResic Theory lsh Tra ial Ope Code hull* l bisec ction c	thmmder due	tio sfoorm sfoorm on on on on on on on on on o						· · · · · · · · · · · · · · · · · · ·														15 15 16 16 16 16 17 17 17 18 18 18 18 19 19 19 19 19 19 19 20 20
	6.5 6.6 6.7 6.10 6.11 6.12 7.1 7.2 7.3 7.4 Geom 8.1 8.2 8.3 8.4 8.5 8.7 8.8 8.1 8.1 8.1 8.1 8.1 8.1 8.1 8.1 8.1	Miller Big num Fractio Simulta Pollard Simplex Cchinese LQuadrat Pricount Pricount Pricount Primes Vnomial Fast Fo Number Fast Wa Polynom Metry Default Convex Externa Heart Interse Interse Interse Coint i Half pl CcircleC S3Dpoint S3Dpoint	Rabin* ber . n neous E Rho . Algori Remaind icResid Urier T Theory lsh Traial Ope Code hull* ction c ction c ction c ction c ction c ction c n circl ane int over* . ull3D*	ithmmder due	tio sfonsform ver wo oly ine ect						· · · · · · · · · · · · · · · · · · ·														15 15 16 16 16 16 17 17 17 18 18 18 18 19 19 19 19 19 19 19 19 20
	6.5 6.6 6.7 6.10 6.11 6.12 7.1 7.2 7.3 7.4 Geom 8.1 8.2 8.3 8.4 8.5 8.7 8.8 8.1 8.1 8.1 8.1 8.1 8.1 8.1 8.1 8.1	Miller Big num Fractio Simulta Pollard Simplex Cchinese LQuadrat Pricount Pricount Pricount Primes Vnomial Fast Fo Number Fast Wa Polynom Metry Default Convex Externa Heart Interse Interse Interse Coint i Half pl CcircleC S3Dpoint S3Dpoint	Rabin* ber . n neous E Rho . Algori Remaind icResid Urier T Theory lsh Traial Ope Code hull* ction c ction c ction c ction c ction c ction c n circl ane int over* . ull3D*	ithmmder due	tio sfonsform ver wo oly ine ect						· · · · · · · · · · · · · · · · · · ·														15 15 16 16 16 16 17 17 17 18 18 18 18 19 19 19 19 19 19 19 20 20
	6.5 6.6 6.7 6.10 6.11 6.12 7.1 7.2 7.3 7.4 Geom 8.1 8.2 8.3 8.4 8.5 8.7 8.8 8.1 8.1 8.1 8.1 8.1 8.1 8.1 8.1 8.1	Miller Big num Fractio Simulta Pollard Simplex Cchinese LQuadrat Pricount Pricount Pricount Primes Vnomial Fast Fo Number Fast Wa Polynom Metry Default Convex Externa Heart Interse Interse Interse Coint i Half pl CcircleC S3Dpoint S3Dpoint	Rabin* ber . n neous E Rho . Algori Remaind icResid Urier T Theory lsh Traial Ope Code hull* ction c ction c ction c ction c ction c ction c n circl ane int over* . ull3D*	ithmmder due	tio sfonsform ver wo oly ine ect						· · · · · · · · · · · · · · · · · · ·														15 15 16 16 16 16 17 17 17 18 18 18 18 19 19 19 19 19 19 20 20 21
	6.5 6.6 6.7 6.12 6.12 6.13 7.2 7.3 7.4 Geom 8.1 8.2 8.3 8.4 8.5 8.8 8.9 8.12 8.12 8.14 8.15 8.14 8.15	Miller Big num Fractio Simulta Pollard Simplex Ochinese Quadrat Pricount Primes Nomial Fast Fo Number Fast Wa Polynom Wetry Default Convex Externa Heart Minimum Polar A Interse Inte	Rabin* ber . neous E Rho . Algori Remainc icResic Theory lsh Tra ial Ope Code hull* l bisec ction c c c ction c c c c c c c c c c c c c c c c c c c	inthmoder in the control of profit in the cont	tio sfooth						· · · · · · · · · · · · · · · · · · ·														15 15 16 16 16 16 17 17 17 18 18 18 18 19 19 19 19 19 20 20 20 21 22
	6.5 6.6 6.7 6.8 6.9 6.11 6.11 7.2 7.3 7.4 Geon 8.1 8.2 8.3 8.4 8.5 8.8 8.9 8.14 8.12 8.13 8.14 8.15 8.16 8.17	Miller Big num Fractio Simulta Pollard Simplex Cchinese LQuadrat Pricount Pricount Pricount Primes Vnomial Fast Fo Number Fast Wa Polynom Metry Default Convex Externa Heart Interse Interse Interse Coint i Half pl CcircleC S3Dpoint S3Dpoint	Rabin* ber . n neous E Rho . Algori Remainc icResic Theory lsh Tra ial Ope Code hull* l bisec ction c tion c ction c ction c ction c labeled yTriang lation line c	thmmler lue	tio sfsfform ver wolyeine ect tioo																				15 15 16 16 16 16 17 17 17 18 18 18 18 19 19 19 19 19 19 20 20 21

```
      8.20Minkowski Sum*
      23

      9 Else
      23

      9.1 Mo's Alogrithm(With modification)
      23

      9.2 Mo's Alogrithm On Tree
      23

      9.3 DynamicConvexTrick*
      24

      9.4 DLX*
      24
```

1 Basic

1.1 Shell script

```
g++ -O2 -std=c++17 -Dbbq -Wall -Wextra -Wshadow -o $1
    $1.cpp
chmod +x compile.sh
```

1.2 Default code

```
#include<bits/stdc++.h>
using namespace std;
typedef long long ll;
typedef pair<int, int> pii;
typedef pair<ll, ll> pll;
#define X first
#define Y second
#define SZ(a) ((int)a.size())
#define ALL(v) v.begin(), v.end()
#define pb push_back
```

1.3 vimrc

```
"This file should be placed at ~/.vimrc"
se nu ai hls et ru ic is sc cul
se re=1 ts=4 sts=4 sw=4 ls=2 mouse=a
syntax on
hi cursorline cterm=none ctermbg=89
set bg=dark
inoremap {<ENTER> {}<LEFT><ENTER><ENTER><UP><TAB>
```

1.4 readchar

```
inline char readchar() {
   static const size_t bufsize = 65536;
   static char buf[bufsize];
   static char *p = buf, *end = buf;
   if (p == end) end = buf + fread_unlocked(buf, 1,
       bufsize, stdin), p = buf;
   return *p++;
}
```

1.5 Black Magic

```
#include <ext/pb_ds/priority_queue.hpp>
 #include <ext/pb_ds/assoc_container.hpp> //rb_tree
 using namespace __gnu_pbds;
typedef __gnu_pbds::priority_queue<int> heap;
 int main() {
   heap h1, h2;
   h1.push(1), h1.push(3);
   h2.push(2), h2.push(4);
   h1.join(h2);
   cout << h1.size() << h2.size() << h1.top() << endl;</pre>
      //404
   tree<11, null_type, less<11>, rb_tree_tag,
      tree_order_statistics_node_update> st;
   tree<11, 11, less<11>, rb_tree_tag,
       tree_order_statistics_node_update> mp;
   for (int x : {0, 2, 3, 4}) st.insert(x);
   cout << *st.find_by_order(2) << st.order_of_key(1) <<</pre>
        endl; //31
//__int128_t,__float128_t
```

1.6 Texas hold'em

```
char suit[4]={'C','D','H','Y'},ranks[13]={'2','3','4','
   5','6','7','8','9','T','J','Q','K','A'};
int rk[256];
   for(int i=0;i<13;++i)</pre>
   rk[ranks[i]]=i;
   for(int i=0;i<4;++i)
   rk[suit[i]]=i;
struct cards{
  vector<pii> v;
  int suit_count[4],hands;
  void reset(){v.clear(),FILL(suit_count,0),hands=-1;}
  void insert(char a, char b){//suit, rank
    ++suit_count[rk[a]];
    int flag=0;
    for(auto &i:v)
      if(i.Y==rk[b])
        ++i.X,flag=1;
        break;
    if(!flag) v.pb(pii(1,rk[b]));
  void insert(string s){insert(s[0],s[1]);}
  void readv(){
    int Straight=0,Flush=(*max_element(suit_count,
        suit_count+4)==5);
    sort(ALL(v),[](ii a,ii b){return a>b;});
    if(SZ(v)==5&&v[0].Y==v[1].Y+1&&v[1].Y==v[2].Y+1&&v
        [2].Y==v[3].Y+1&&v[3].Y==v[4].Y+1)
      Straight=1;
    else if(SZ(v)==5&&v[0].Y==12&&v[1].Y==3&&v[2].Y
        ==2\&v[3].Y==1\&v[4].Y==0)
      v[0].Y=3,v[1].Y=2,v[2].Y=1,v[1].Y=0,v[0].Y=-1,
          Straight=1;
    if(Straight&&Flush) hands=1;
    else if(v[0].X==4) hands=2;
    else if(v[0].X==3&&v[1].X==2) hands=3;
    else if(Flush) hands=4;
    else if(Straight) hands=5;
    else if(v[0].X==3) hands=6;
    else if(v[0].X==2&&v[1].X==2) hands=7;
    else if(v[0].X==2) hands=8;
    else hands=9;
  bool operator>(const cards &a)const{
    if(hands==a.hands) return v>a.v;
    return hands<a.hands;</pre>
};
```

2 Graph

2.1 BCC Vertex*

```
vector<int> G[N]; //1-base
vector<int> nG[N], bcc[N];
int low[N], dfn[N], Time;
int bcc_id[N], bcc_cnt; //1-base
bool is_cut[N]; //whether is av
bool cir[N];
int st[N], top;
void dfs(int u, int pa = -1) {
 int child = 0;
 low[u] = dfn[u] = ++Time;
  st[top++] = u;
  for(int v : G[u])
    if(!dfn[v]) {
      dfs(v,u), ++child;
      low[u] = min(low[u], low[v]);
      if(dfn[u] <= low[v]) {
        is_cut[u]=1;
        bcc[++bcc_cnt].clear();
        int t;
```

```
do {
          bcc_id[t = st[--top]] = bcc_cnt;
          bcc[bcc_cnt].push_back(t);
        }while(t != v);
        bcc_id[u]=bcc_cnt;
        bcc[bcc_cnt].pb(u);
      }
    }
    else if(dfn[v] < dfn[u] && v!=pa)</pre>
      low[u] = min(low[u], dfn[v]);
  if(pa == -1 && child < 2)
    is_cut[u] = 0;
}
void bcc_init(int n) {
  Time = bcc_cnt = top = 0;
  for(int i = 1; i <= n; ++i)</pre>
    G[i].clear(), dfn[i] = bcc_id[i] = is_cut[i] = 0;
}
void bcc_solve(int n) {
  for (int i = 1; i <= n; ++i)</pre>
    if (!dfn[i])
      dfs(i);
  // circle-square tree
  for(int i = 1; i <= n; ++i)</pre>
    if(is_cut[i])
      bcc_id[i] = ++bcc_cnt, cir[bcc_cnt] = 1;
  for(int i = 1; i <= bcc_cnt && !cir[i]; ++i)</pre>
    for(int j : bcc[i])
      if(is_cut[j])
        nG[i].pb(bcc_id[j]), nG[bcc_id[j]].pb(i);
```

2.2 Bridge*

```
int low[N], dfn[N], Time;// 1-base
vector<pii> G[N], edge;
vector<bool> is_bridge;
void init(int n) {
  Time = 0;
   for (int i = 1; i <= n; ++i)</pre>
     G[i].clear(), low[i] = dfn[i] = 0;
void add_edge(int a, int b) {
  G[a].pb(pii(b, SZ(edge))), G[b].pb(pii(a, SZ(edge)));
   edge.pb(pii(a, b));
}
void dfs(int u, int f) {
  dfn[u] = low[u] = ++Time;
   for (auto i : G[u])
     if (!dfn[i.X])
       dfs(i.X, i.Y), low[u] = min(low[u], low[i.X]);
     else if (i.Y != f)
       low[u] = min(low[u], dfn[i.X]);
   if (low[u] == dfn[u] && f != -1)
     is_bridge[f] = 1;
void solve(int n) {
  is_bridge.resize(SZ(edge));
   for (int i = 1; i <= n; ++i)</pre>
     if (!dfn[i])
       dfs(i, -1);
| }
```

2.3 2SAT (SCC)*

```
struct SAT { // 0-base
  int low[N], dfn[N], bln[N], n, Time, nScc;
bool instack[N], istrue[N];
  stack<int> st;
  vector<int> G[N], SCC[N];
  void init(int _n) {
    n = _n; // assert(n * 2 <= N);</pre>
```

```
for (int i = 0; i < n + n; ++i)</pre>
       G[i].clear();
   void add_edge(int a, int b) {
     G[a].pb(b);
  void dfs(int u) {
     dfn[u] = low[u] = ++Time;
     instack[u] = 1, st.push(u);
     for (int i : G[u])
       if (!dfn[i]) dfs(i), low[u]=min(low[i], low[u]);
else if (instack[i] && dfn[i] < dfn[u])</pre>
          low[u] = min(low[u], dfn[i]);
     if (low[u] == dfn[u]) {
       int tmp;
       do {
          tmp = st.top(), st.pop();
instack[tmp] = 0, bln[tmp] = nScc;
       } while(tmp != u);
       ++nScc;
     }
  }
  bool solve() {
     Time = nScc = 0;
     for (int i = 0; i < n + n; ++i)</pre>
       SCC[i].clear(), low[i] = dfn[i] = bln[i] = 0;
     for (int i = 0; i < n + n; ++i)</pre>
       if (!dfn[i]) dfs(i);
     for (int i = 0; i < n + n; ++i)</pre>
       SCC[bln[i]].pb(i);
     for (int i = 0; i < n; ++i) {</pre>
       if (bln[i] == bln[i + n]) return false;
       istrue[i] = bln[i] < bln[i + n];</pre>
       istrue[i + n] = !istrue[i];
     return true;
|};
```

2.4 MinimumMeanCycle*

```
11 road[N][N];//input here
struct MinimumMeanCycle{
  11 dp[N + 5][N], n;
  pll solve() {
    11 a = -1, b = -1, L = n+1;
     for(int i = 2; i <= L; ++i)</pre>
       for(int k = 0; k < n; ++k)
         for(int j = 0; j < n; ++j)</pre>
           dp[i][j] = min(dp[i - 1][k] + road[k][j], dp[
                i][j]);
    for(int i = 0; i < n; ++i) {</pre>
       if(dp[L][i] >= INF) continue;
       11 ta = 0, tb = 1;
       for(int j = 1; j < n; ++j)
  if(dp[j][i] < INF && ta * (L - j) < (dp[L][i] -</pre>
               dp[j][i]) * tb)
           ta = dp[L][i] - dp[j][i], tb = L - j;
       if(ta == 0) continue;
       if(a == -1 || a * tb > ta * b)
         a = ta, b = tb;
    if(a != -1) {
       ll g = \_gcd(a, b);
       return pll(a / g, b / g);
    return pll(-1LL, -1LL);
  void init(int _n){
    n = _n;
     for(int i = 0; i < n; ++i)</pre>
       for(int j = 0; j < n; ++j)</pre>
         dp[i + 2][j] = INF;
  }
};
```

2.5 Virtual Tree*

```
vector<int> vG[N];
int top, st[N];
void insert(int u) {
  if(top == -1)
    return st[++top] = u, void();
  int p = LCA(st[top], u);
  if(p == st[top])
    return st[++top] = u, void();
  while(top >= 1 && dep[st[top - 1]] >= dep[p])
    vG[st[top - 1]].pb(st[top]), --top;
  if(st[top] != p)
    vG[p].pb(st[top]), --top, st[++top] = p;
  st[++top] = u;
}
void reset(int u) {
  for(int i : vG[u])
    reset(i);
  vG[u].clear();
void solve(vector<int> &v) {
  sort(ALL(v), [&](int a, int b){return dfn[a] < dfn[b</pre>
      ];});
  for (int i : v)
   insert(i);
  while (top > 0)
    vG[st[top - 1]].pb(st[top]), --top;
  //do something
  reset(v[0]);
```

2.6 Maximum Clique Dyn*

```
const int N = 150;
struct MaxClique {
                    // Maximum Clique
  bitset<N> a[N], cs[N];
  int ans, sol[N], q, cur[N], d[N], n;
  void init(int _n) {
    n = _n;
    for (int i = 0; i < n; i++) a[i].reset();</pre>
  void addEdge(int u, int v) { a[u][v] = a[v][u] = 1; }
  void csort(vector<int> &r, vector<int> &c) {
    int mx = 1, km = max(ans - q + 1, 1), t = 0, m = r.
        size();
    cs[1].reset(), cs[2].reset();
    for (int i = 0; i < m; i++) {</pre>
      int p = r[i], k = 1;
      while ((cs[k] & a[p]).count()) k++;
      if (k > mx) mx++, cs[mx + 1].reset();
      cs[k][p] = 1;
      if (k < km) r[t++] = p;
    c.resize(m);
    if (t) c[t - 1] = 0;
    for (int k = km; k \leftarrow mx; k++)
      for (int p = cs[k]._Find_first(); p < N; p = cs[k]
          ]._Find_next(p))
        r[t] = p, c[t] = k, t++;
  void dfs(vector<int> &r, vector<int> &c, int 1,
      bitset<N> mask) {
    while (!r.empty()) {
      int p = r.back();
      r.pop_back(), mask[p] = 0;
      if (q + c.back() <= ans) return;</pre>
      cur[q++] = p;
      vector<int> nr, nc;
      bitset<N> nmask = mask & a[p];
      for (int i : r)
        if (a[p][i]) nr.push_back(i);
      if (!nr.empty()) {
        if (1 < 4) {
          for (int i : nr) d[i] = (a[i] & nmask).count
               ();
          sort(nr.begin(), nr.end(), [&](int x, int y)
               { return d[x] > d[y]; });
```

```
csort(nr, nc), dfs(nr, nc, l + 1, nmask);
      } else if (q > ans)
        ans = q, copy_n(cur, q, sol);
      c.pop_back(), q--;
    }
  int solve(bitset<N> mask = bitset<N>(string(N, '1')))
       { // vertex mask
    vector<int> r, c;
    ans = q = 0;
    for (int i = 0; i < n; i++)</pre>
      if (mask[i]) r.push_back(i);
    for (int i = 0; i < n; i++) d[i] = (a[i] & mask).
        count();
    sort(r.begin(), r.end(), [&](int i, int j) { return
         d[i] > d[j]; });
    csort(r, c), dfs(r, c, 1, mask);
    return ans; // sol[0 ~ ans-1]
  }
} graph;
```

2.7 Minimum Steiner Tree*

```
// Minimum Steiner Tree
// O(V 3^T + V^2 2^T)
struct SteinerTree{// 0-base
  static const int T = 10, N = 105, INF = 1e9;
  int n, dst[N][N], dp[1 << T][N], tdst[N];</pre>
  int vcost[N]; // the cost of vertexs
  void init(int _n){
    n = _n;
    for(int i = 0; i < n; ++i) {</pre>
      for(int j = 0; j < n; ++j)</pre>
        dst[i][j] = INF;
      dst[i][i] = vcost[i] = 0;
    }
  void add_edge(int ui, int vi, int wi) {
    dst[ui][vi]=min(dst[ui][vi], wi);
  void shortest_path() {
    for(int k = 0; k < n; ++k)
      for(int i = 0; i < n; ++i)</pre>
        for(int j = 0; j < n; ++j)
           dst[i][j] = min(dst[i][j], dst[i][k] + dst[k]
               1[i]);
  int solve(const vector<int>& ter) {
    shortest_path();
    int t = SZ(ter);
    for(int i = 0; i < (1 << t); ++i)</pre>
      for(int j = 0; j < n; ++j)</pre>
         dp[i][j] = INF;
    for(int i = 0; i < n; ++i)</pre>
      dp[0][i] = vcost[i];
    for(int msk = 1; msk < (1 << t); ++msk){</pre>
      if(!(msk & (msk - 1))){
        int who = __lg(msk);
for(int i = 0; i < n; ++i)
  dp[msk][i] = vcost[ter[who]] + dst[ter[who]][</pre>
               i];
      for(int i = 0; i < n; ++i)</pre>
        for(int submsk = (msk - 1) & msk; submsk;
             submsk = (submsk - 1) \& msk)
           dp[msk][i] = min(dp[msk][i], dp[submsk][i] +
               dp[msk ^ submsk][i] - vcost[i]);
      for(int i = 0; i < n; ++i) {</pre>
        tdst[i] = INF;
         for(int j = 0; j < n; ++j)</pre>
           tdst[i] = min(tdst[i], dp[msk][j] + dst[j][i
      for(int i = 0; i < n; ++i)</pre>
        dp[msk][i] = tdst[i];
    int ans = INF;
    for(int i = 0; i < n; ++i)</pre>
      ans = min(ans, dp[(1 << t) - 1][i]);
```

```
return ans;
}
};
```

2.8 Dominator Tree*

```
struct dominator tree{//1-base
  vector<int> G[N],rG[N];
  int n, pa[N], dfn[N], id[N], Time;
int semi[N], idom[N], best[N];
  vector<int> tree[N];//dominator_tree
  void init(int _n) {
    n = _n;
    for(int i = 1; i <= n; ++i)</pre>
      G[i].clear(), rG[i].clear();
  void add_edge(int u, int v) {
    G[u].pb(v), rG[v].pb(u);
  void dfs(int u) {
    id[dfn[u] = ++Time] = u;
    for(auto v : G[u])
      if(!dfn[v])
        dfs(v), pa[dfn[v]] = dfn[u];
  int find(int y, int x) {
    if(y \ll x)
      return y;
    int tmp = find(pa[y], x);
    if(semi[best[y]] > semi[best[pa[y]]])
      best[y] = best[pa[y]];
    return pa[y] = tmp;
  void tarjan(int root) {
    Time = 0;
    for(int i = 1; i <= n; ++i){</pre>
      dfn[i] = idom[i] = 0;
      tree[i].clear();
      best[i] = semi[i] = i;
    dfs(root);
    for(int i = Time; i > 1; --i) {
      int u = id[i];
      for(auto v : rG[u])
        if(v = dfn[v]) {
           find(v, i);
           semi[i] = min(semi[i], semi[best[v]]);
      tree[semi[i]].pb(i);
      for(auto v : tree[pa[i]]) {
        find(v, pa[i]);
        idom[v] = semi[best[v]] == pa[i] ? pa[i] : best
             [v];
      tree[pa[i]].clear();
    for(int i = 2; i <= Time; ++i) {</pre>
      if(idom[i] != semi[i])
        idom[i] = idom[idom[i]];
      tree[id[idom[i]]].pb(id[i]);
};
```

2.9 Minimum Arborescence*

```
struct zhu_liu{//O(VE)
    struct edge{
        int u,v;
        ll w;
    };
    vector<edge> E; //O-base
    int pe[N], id[N], vis[N];
    ll in[N];
    void init() {E.clear();}
    void add_edge(int u, int v, ll w) {
        if (u != v) E.pb(edge{u, v, w});
    }
}
```

```
11 build(int root, int n) {
    11 \text{ ans} = 0;
    for(;;) {
      fill_n(in, n, INF);
       for (int i = 0; i < SZ(E); ++i)</pre>
        if (E[i].u != E[i].v && E[i].w < in[E[i].v])</pre>
           pe[E[i].v] = i, in[E[i].v] = E[i].w;
      for (int u = 0; u < n; ++u)//no solution
        if (u != root && in[u] == INF) return -INF;
       int cntnode = 0;
      fill_n(id, n, -1), fill_n(vis, n, -1);
      for (int u = 0; u < n; ++u) {
        if (u != root) ans += in[u];
        int v = u;
        while (vis[v] != u && !~id[v] && v != root)
           vis[v] = u, v = E[pe[v]].u;
        if (v != root && !~id[v]) {
           for (int x = E[pe[v]].u; x != v; x = E[pe[x
               ]].u)
             id[x] = cntnode;
          id[v] = cntnode++;
        }
      if (!cntnode) break;//no cycle
      for (int u = 0; u < n; ++u)</pre>
        if (!~id[u]) id[u] = cntnode++;
       for (int i = 0; i < SZ(E); ++i) {</pre>
        int v = E[i].v;
        E[i].u = id[E[i].u], E[i].v = id[E[i].v];
        if (E[i].u != E[i].v) E[i].w -= in[v];
      n = cntnode, root = id[root];
    return ans;
};
```

2.10 Vizing's theorem

```
namespace vizing { // returns edge coloring in adjacent
    matrix G. 1 - based
  int C[kN][kN], G[kN][kN];
  void clear(int N) {
   for (int i = 0; i <= N; i++) {</pre>
     for (int j = 0; j <= N; j++) C[i][j] = G[i][j] =</pre>
   }
 }
 void solve(vector<pair<int, int>> &E, int N, int M) {
   int X[kN] = {}, a;
   auto update = [&](int u) {
     for (X[u] = 1; C[u][X[u]]; X[u]++);
   auto color = [&](int u, int v, int c) {
     int p = G[u][v];
     G[u][v] = G[v][u] = c;
     C[u][c] = v, C[v][c] = u;
     C[u][p] = C[v][p] = 0;
     if (p) X[u] = X[v] = p;
     else update(u), update(v);
     return p;
   }:
   auto flip = [&](int u, int c1, int c2) {
     int p = C[u][c1];
     swap(C[u][c1], C[u][c2]);
     if (p) G[u][p] = G[p][u] = c2;
     if (!C[u][c1]) X[u] = c1;
     if (!C[u][c2]) X[u] = c2;
     return p;
   };
   for (int i = 1; i <= N; i++) X[i] = 1;
   for (int t = 0; t < E.size(); t++) {</pre>
     vector<pair<int, int>> L;
     int vst[kN] = {};
     while (!G[u][v0]) {
       L.emplace_back(v, d = X[v]);
       if (!C[v][c]) for (a = (int)L.size() - 1; a >=
           0; a--) c = color(u, L[a].first, c);
```

2.11 Minimum Clique Cover*

```
struct Clique_Cover { // 0-base, O(n2^n)
   int co[1 << N], n, E[N];</pre>
   int dp[1 << N];</pre>
   void init(int _n) {
     n = _n, fill_n(dp, 1 << n, 0);</pre>
     fill_n(E, n, 0), fill_n(co, 1 << n, 0);
   void add_edge(int u, int v) {
     E[u] |= 1 << v, E[v] |= 1 << u;
   int solve() {
     for (int i = 0; i < n; ++i)</pre>
       co[1 << i] = E[i] | (1 << i);
     co[0] = (1 << n) - 1;

dp[0] = (n & 1) * 2 - 1;
     for (int i = 1; i < (1 << n); ++i) {
       int t = i & -i;
dp[i] = -dp[i ^ t];
       co[i] = co[i ^ t] & co[t];
     for (int i = 0; i < (1 << n); ++i)</pre>
       co[i] = (co[i] & i) == i;
     fwt(co, 1 << n);
     for (int ans = 1; ans < n; ++ans) {</pre>
       int sum = 0;
       for (int i = 0; i < (1 << n); ++i)</pre>
         sum += (dp[i] *= co[i]);
       if (sum) return ans;
     return n:
   }
};
```

2.12 NumberofMaximalClique*

```
struct BronKerbosch { // 1-base
  int n, a[N], g[N][N];
  int S, all[N][N], some[N][N], none[N][N];
  void init(int _n) {
    n = _n;
for (int i = 1; i <= n; ++i)</pre>
      for (int j = 1; j <= n; ++j)</pre>
        g[i][j] = 0;
  void add_edge(int u, int v) {
    g[u][v] = g[v][u] = 1;
  void dfs(int d, int an, int sn, int nn) {
    if (S > 1000) return; // pruning
    if (sn == 0 && nn == 0) ++S;
    int u = some[d][0];
    for(int i = 0; i < sn; ++i) {</pre>
      int v = some[d][i];
      if(g[u][v]) continue;
      int tsn = 0, tnn = 0;
      copy_n(all[d], an, all[d + 1]);
      all[d + 1][an] = v;
      for(int j = 0; j < sn; ++j)</pre>
```

```
if(g[v][some[d][j]])
          some[d + 1][tsn++] = some[d][j];
for(int j = 0; j < nn; ++j)
        if(g[v][none[d][j]])
          none[d + 1][tnn++] = none[d][j];
        dfs(d + 1, an + 1, tsn, tnn);
        some[d][i] = 0, none[d][nn ++] = v;
    }
}
int solve() {
    iota(some[0], some[0] + n, 1);
    S = 0, dfs(0, 0, n, 0);
    return S;
}
};</pre>
```

2.13 Theory

```
\begin{aligned} &|\text{Maximum independent edge set}| = |V| - |\text{Minimum edge cover}| \\ &|\text{Maximum independent set}| = |V| - |\text{Minimum vertex cover}| \\ &|\text{A sequence of non-negative integers } d_1 \geq \cdots \geq d_n \text{ can be represented as the degree sequence of a finite simple graph on } n \text{ vertices if and only if } d_1 + \cdots + d_n \text{ is even and } \\ &\sum_{i=1}^k d_i \leq k(k-1) + \sum_{i=k+1}^n \min(d_i,k) \text{ holds for every } k \text{ in } 1 \leq k \leq n. \end{aligned}
```

3 Data Structure

3.1 Leftist Tree

```
struct node{
  11 v,data,sz,sum;
  node *1,*r;
  node(ll \ k): v(0), data(k), sz(1), l(0), r(0), sum(k){}
11 sz(node *p){return p ? p->sz : 0;}
11 V(node *p){return p ? p->v : -1;}
11 sum(node *p){return p ? p->sum : 0;}
node* merge(node *a,node *b){
  if(!a || !b) return a ? a : b;
  if(a->data<b->data) swap(a,b);
  a - r = merge(a - r, b);
  if(V(a->r)>V(a->1)) swap(a->r,a->1);
  a->v=V(a->r)+1,a->sz=sz(a->1)+sz(a->r)+1;
  a -> sum = sum(a -> 1) + sum(a -> r) + a -> data;
  return a;
void pop(node *&o){
  node *tmp=o;
  o=merge(o->1,o->r);
  delete tmp;
```

3.2 Heavy light Decomposition

```
struct Heavy_light_Decomposition{//1-base
  int n,ulink[10005],deep[10005],mxson[10005],w[10005],
      pa[10005];
  int t,pl[10005],data[10005],dt[10005],bln[10005],edge
      [10005],et;
 vector<pii> G[10005];
  void init(int _n){n=_n,t=0,et=1;
    for(int i=1;i<=n;++i) G[i].clear(),mxson[i]=0;</pre>
  void add_edge(int a,int b,int w){
   G[a].pb(pii(b,et)),G[b].pb(pii(a,et)),edge[et++]=w;
  void dfs(int u,int f,int d){
    w[u]=1,pa[u]=f,deep[u]=d++;
    for(auto &i:G[u])
      if(i.X!=f){
        dfs(i.X,u,d),w[u]+=w[i.X];
        if(w[mxson[u]]<w[i.X])</pre>
          mxson[u]=i.X;
      }
```

```
else
        bln[i.Y]=u,dt[u]=edge[i.Y];
  void cut(int u,int link){
    data[pl[u]=t++]=dt[u],ulink[u]=link;
    if(!mxson[u]) return ;
    cut(mxson[u],link);
    for(auto i:G[u])
      if(i.X!=pa[u]&&i.X!=mxson[u])
        cut(i.X,i.X);
  void build(){
    dfs(1,1,1),cut(1,1),/*build*/;
  int query(int a,int b){
    int ta=ulink[a],tb=ulink[b],re=0;
    while(ta!=tb)
      if(deep[ta]<deep[tb])</pre>
        /*query*/,tb=ulink[b=pa[tb]];
      else
        /*query*/,ta=ulink[a=pa[ta]];
    if(a==b) return re;
    if(pl[a]>pl[b]) swap(a,b);
    /*query*/
    return re;
  }
};
```

3.3 Centroid Decomposition*

```
struct Cent_Dec { // 1-base
  vector<pll> G[N];
  pll info[N]; // store info. of itself pll upinfo[N]; // store info. of climbing up
  int n, pa[N], layer[N], sz[N], done[N];
  ll dis[__lg(N) + 1][N];
  void init(int _n) {
    n = _n, layer[0] = -1;
    fill_n(pa + 1, n, 0), fill_n(done + 1, n, 0);
    for (int i = 1; i <= n; ++i) G[i].clear();</pre>
  void add_edge(int a, int b, int w) {
    G[a].pb(pll(b, w)), G[b].pb(pll(a, w));
  void get_cent(int u, int f, int &mx, int &c, int num)
    int mxsz = 0;
    sz[u] = 1;
    for (pll e : G[u])
      if (!done[e.X] && e.X != f) {
        get_cent(e.X, u, mx, c, num);
        sz[u] += sz[e.X], mxsz = max(mxsz, sz[e.X]);
    if (mx > max(mxsz, num - sz[u]))
      mx = max(mxsz, num - sz[u]), c = u;
  void dfs(int u, int f, ll d, int org) {
    // if required, add self info or climbing info
    dis[layer[org]][u] = d;
    for (pll e : G[u])
      if (!done[e.X] && e.X != f)
        dfs(e.X, u, d + e.Y, org);
  int cut(int u, int f, int num) {
    int mx = 1e9, c = 0, lc;
    get_cent(u, f, mx, c, num);
    done[c] = 1, pa[c] = f, layer[c] = layer[f] + 1;
    for (pll e : G[c])
      if (!done[e.X]) {
        if (sz[e.X] > sz[c])
          lc = cut(e.X, c, num - sz[c]);
          lc = cut(e.X, c, sz[e.X]);
        upinfo[lc] = pll(), dfs(e.X, c, e.Y, c);
    return done[c] = 0, c;
  void build(){cut(1, 0, n);}
  void modify(int u) {
```

3.4 Link cut tree*

```
struct Splay { // xor-sum
    static Splay nil;
    Splay *ch[2], *f;
    int val, sum, rev, size;
    Splay (int _val = 0) : val(_val), sum(_val), rev(0)
          size(1)
    {f = ch[0] = ch[1] = &nil; }
    bool isr()
    { return f -> ch[0] != this && f -> ch[1] != this;
    int dir()
    { return f -> ch[0] == this ? 0 : 1; }
    void setCh(Splay *c, int d) {
        ch[d] = c;
        if (c != &nil) c -> f = this;
        pull();
    void push() {
        if(!rev) return;
        swap(ch[0], ch[1]);
        if (ch[0] != &nil) ch[0] -> rev ^= 1;
        if (ch[1] != &nil) ch[1] -> rev ^= 1;
        rev = 0:
    void pull() {
        // take care of the nil!
        size = ch[0] \rightarrow size + ch[1] \rightarrow size + 1;
        sum = ch[0] \rightarrow sum ^ ch[1] \rightarrow sum ^ val;
        if (ch[0] != &nil) ch[0] -> f = this;
        if (ch[1] != &nil) ch[1] -> f = this;
} Splay::nil;
Splay *nil = &Splay::nil;
void rotate(Splay *x) {
    Splay *p = x \rightarrow f;
    int d = x -> dir();
    if (!p -> isr())
        p -> f -> setCh(x, p -> dir());
        x \rightarrow f = p \rightarrow f;
    p -> setCh(x -> ch[!d], d);
    x -> setCh(p, !d);
    p -> pull(), x -> pull();
void splay(Splay *x) {
    vector<Splay*> splayVec;
    for (Splay *q = x;; q = q \rightarrow f) {
        splayVec.pb(q);
        if (q -> isr()) break;
    reverse(ALL(splayVec));
    for (auto it : splayVec) it -> push();
    while (!x -> isr()) {
        if (x \rightarrow f \rightarrow isr()) rotate(x);
        else if (x -> dir() == x -> f -> dir())
             rotate(x -> f), rotate(x);
        else rotate(x), rotate(x);
    }
```

```
Splay* access(Splay *x) {
    Splay *q = nil;
    for (; x != nil; x = x -> f)
         splay(x), x \rightarrow setCh(q, 1), q = x;
    return q;
void root_path(Splay *x) {
    access(x), splay(x);
void chroot(Splay *x){
    root_path(x), x -> rev ^= 1;
    x -> push(), x -> pull();
void split(Splay *x, Splay *y) {
    chroot(x), root_path(y);
void link(Splay *x, Splay *y) {
    root_path(x), chroot(y);
    x->setCh(y, 1);
void cut(Splay *x, Splay *y) {
    split(x, y);
    if (y -> size != 5) return;
    y -> push();
    y \rightarrow ch[0] = y \rightarrow ch[0] \rightarrow f = nil;
Splay* get_root(Splay *x) {
    for(root_path(x); x \rightarrow ch[0] != nil; x = x \rightarrow ch
         [0])
        x -> push();
    splay(x);
    return x:
bool conn(Splay *x, Splay *y) {
    return get_root(x) == get_root(y);
Splay* lca(Splay *x, Splay *y) {
    access(x), root_path(y);
if (y -> f == nil) return y;
    return y -> f;
void change(Splay *x, int val) {
    splay(x), x \rightarrow val = val, x \rightarrow pull();
int query(Splay *x, Splay *y) {
    split(x, y);
    return y -> sum;
```

3.5 KDTree

```
namespace kdt {
int root, lc[maxn], rc[maxn], xl[maxn], xr[maxn], yl[
    maxn], yr[maxn];
point p[maxn];
int build(int 1, int r, int dep = 0) {
    if (1 == r) return -1;
    function<bool(const point &, const point &)> f = [
        dep](const point &a, const point &b) {
        if (dep & 1) return a.x < b.x;</pre>
        else return a.y < b.y;</pre>
    };
    int m = (1 + r) >> 1;
    nth_element(p + 1, p + m, p + r, f);
    x1[m] = xr[m] = p[m].x;
    yl[m] = yr[m] = p[m].y;
    lc[m] = build(1, m, dep + 1);
    if (~lc[m]) {
        xl[m] = min(xl[m], xl[lc[m]]);
        xr[m] = max(xr[m], xr[lc[m]]);
        yl[m] = min(yl[m], yl[lc[m]]);
        yr[m] = max(yr[m], yr[lc[m]]);
    rc[m] = build(m + 1, r, dep + 1);
    if (~rc[m]) {
        xl[m] = min(xl[m], xl[rc[m]]);
        xr[m] = max(xr[m], xr[rc[m]]);
        yl[m] = min(yl[m], yl[rc[m]]);
        yr[m] = max(yr[m], yr[rc[m]]);
```

```
return m;
bool bound(const point &q, int o, long long d) {
    double ds = sqrt(d + 1.0);
    if (q.x < x1[o] - ds || q.x > xr[o] + ds ||
        q.y < yl[o] - ds || q.y > yr[o] + ds) return
    return true:
long long dist(const point &a, const point &b) {
    return (a.x - b.x) * 111 * (a.x - b.x) +
           (a.y - b.y) * 111 * (a.y - b.y);
void dfs(const point &q, long long &d, int o, int dep =
    if (!bound(q, o, d)) return;
    long long cd = dist(p[o], q);
    if (cd != 0) d = min(d, cd);
    if ((dep & 1) && q.x < p[o].x || !(dep & 1) && q.y</pre>
        < p[o].y)
        if (~lc[o]) dfs(q, d, lc[o], dep + 1);
        if (~rc[o]) dfs(q, d, rc[o], dep + 1);
    } else +
        if (~rc[o]) dfs(q, d, rc[o], dep + 1);
        if (~lc[o]) dfs(q, d, lc[o], dep + 1);
void init(const vector<point> &v) {
    for (int i = 0; i < v.size(); ++i) p[i] = v[i];</pre>
    root = build(0, v.size());
long long nearest(const point &q) {
    long long res = 1e18;
    dfs(q, res, root);
    return res;
}}
```

4 Flow/Matching

4.1 Kuhn Munkres

```
struct KM{// 0-base
 int w[MAXN][MAXN],hl[MAXN],hr[MAXN],slk[MAXN],n;
  int fl[MAXN],fr[MAXN],pre[MAXN],qu[MAXN],ql,qr;
  bool v1[MAXN], vr[MAXN];
  void init(int _n){n=_n;
    for(int i=0;i<n;++i)</pre>
      for(int j=0;j<n;++j)</pre>
        w[i][j]=-INF;
  void add_edge(int a,int b,int wei){
   w[a][b]=wei;
  bool Check(int x){
    if(vl[x]=1,~fl[x]) return vr[qu[qr++]=fl[x]]=1;
    while(~x) swap(x,fr[fl[x]=pre[x]]);
    return 0;
  void Bfs(int s){
    fill(slk,slk+n,INF);
    fill(vl,vl+n,0),fill(vr,vr+n,0);
    ql=qr=0,qu[qr++]=s,vr[s]=1;
    while(1){
      int d;
      while(ql<qr)
        for(int x=0,y=qu[ql++];x<n;++x)</pre>
          if(!vl[x]\&\&slk[x]>=(d=hl[x]+hr[y]-w[x][y]))
            if(pre[x]=y,d) slk[x]=d;
            else if(!Check(x)) return;
      d=INF;
      for (int x=0;x<n;++x)
        if (!v1[x]&&d>s1k[x]) d=s1k[x];
      for (int x=0;x<n;++x){
        if(vl[x]) hl[x]+=d;
        else slk[x]-=d;
        if(vr[x]) hr[x]-=d;
```

4.2 MincostMaxflow

```
struct MCMF{//0-base
  struct edge{
    11 from,to,cap,flow,cost,rev;
  }*past[MAXN];
  vector<edge> G[MAXN];
  bitset<MAXN> inq;
  11 dis[MAXN],up[MAXN],s,t,mx,n;
  bool BellmanFord(ll &flow,ll &cost){
    fill(dis,dis+n,INF);
    queue<11> q;
    q.push(s),inq.reset(),inq[s]=1;
    up[s]=mx-flow,past[s]=0,dis[s]=0;
    while(!q.empty()){
      11 u=q.front();
      q.pop(),inq[u]=0;
      if(!up[u]) continue;
      for(auto &e:G[u])
        if(e.flow!=e.cap&&dis[e.to]>dis[u]+e.cost){
          dis[e.to]=dis[u]+e.cost,past[e.to]=&e;
          up[e.to]=min(up[u],e.cap-e.flow);
          if(!inq[e.to]) inq[e.to]=1,q.push(e.to);
        }
    if(dis[t]==INF) return 0;
    flow+=up[t],cost+=up[t]*dis[t];
    for(ll i=t;past[i];i=past[i]->from){
      auto &e=*past[i];
      e.flow+=up[t],G[e.to][e.rev].flow-=up[t];
    return 1:
  11 MinCostMaxFlow(11 _s,11 _t,11 &cost){
    s=_s,t=_t,cost=0;11 flow=0;
    while(BellmanFord(flow,cost));
    return flow;
  void init(ll _n,ll _mx){n=_n,mx=_mx;
    for(int i=0;i<n;++i) G[i].clear();</pre>
  void add_edge(ll a,ll b,ll cap,ll cost){
    G[a].pb(edge{a,b,cap,0,cost,G[b].size()});
    G[b].pb(edge{b,a,0,0,-cost,G[a].size()-1});
};
```

4.3 Maximum Simple Graph Matching*

```
struct GenMatch { // 1-base
  int V, pr[N];
  bool el[N][N], inq[N], inp[N], inb[N];
  int st, ed, nb, bk[N], djs[N], ans;
  void init(int _V) {
    V=_V;
    for(int i = 0; i <= V; ++i) {
        for(int j = 0; j <= V; ++j)
            el[i][j] = 0;
        pr[i] = bk[i] = djs[i] = 0;
        inq[i] = inp[i] = inb[i] = 0;
    }
}
void add_edge(int u, int v){</pre>
```

```
el[u][v] = el[v][u] = 1;
int lca(int u, int v) {
  fill_n(inp, V + 1, 0);
  while(1)
    if(u = djs[u], inp[u] = true, u == st) break;
    else u = bk[pr[u]];
  while(1)
    if(v = djs[v], inp[v]) return v;
    else v = bk[pr[v]];
}
void upd(int u){
  for(int v; djs[u] != nb;) {
    v = pr[u], inb[djs[u]] = inb[djs[v]] = true;
    u = bk[v];
    if(djs[u] != nb) bk[u] = v;
void blo(int u, int v, queue<int> &qe) {
  nb = lca(u, v), fill_n(inb, V + 1, 0);
  upd(u), upd(v);
  if(djs[u] != nb) bk[u] = v;
  if(djs[v] != nb) bk[v] = u;
  for(int tu = 1; tu <= V; ++tu)</pre>
    if(inb[djs[tu]])
      if(djs[tu] = nb, !inq[tu])
        qe.push(tu), inq[tu]=1;
void flow() {
  fill_n(inq + 1, V, 0), fill_n(bk + 1, V, 0);
  iota(djs + 1, djs + V + 1, 1);
  queue<int> qe;
  qe.push(st), inq[st] = 1, ed = 0;
  while(!qe.empty()) {
    int u = qe.front();
    qe.pop();
    for(int v = 1; v <= V; ++v)</pre>
      if(el[u][v] && djs[u] != djs[v] && pr[u] != v)
        if((v == st) || (pr[v] > 0 \&\& bk[pr[v]] > 0))
          blo(u, v, qe);
        else if(!bk[v]) {
          if(bk[v] = u, pr[v] > 0) {
            if(!inq[pr[v]])
              qe.push(pr[v]);
          }
          else
            return ed = v, void();
      }
 }
void aug(){
  for(int u = ed, v, w; u > 0;)
    v = bk[u], w = pr[v], pr[v] = u, pr[u] = v, u = w
int solve() {
 fill_n(pr, V + 1, 0), ans = 0;
  for(int u = 1; u <= V; ++u)</pre>
    if(!pr[u])
      if(st = u, flow(), ed > 0)
        aug(), ++ans;
  return ans;
}
```

4.4 Minimum Weight Matching (Clique version)*

```
void add_edge(int u, int v, ll w) { edge[u][v] = edge
       [v][u] = w; }
  bool SPFA(int u) {
    stk[tp++] = u, onstk[u] = 1;
    for (int v = 0; v < n; ++v)
      if (!onstk[v] && match[u] != v) {
         int m = match[v];
         if (dis[m] > dis[u] - edge[v][m] + edge[u][v])
           dis[m] = dis[u] - edge[v][m] + edge[u][v];
           onstk[v] = 1, stk[tp++] = v;
if (onstk[m] || SPFA(m)) return 1;
           --tp, onstk[v] = 0;
      }
    onstk[u] = 0, --tp;
    return 0;
  11 solve() { // find a match
    for (int i = 0; i < n; ++i) match[i] = i ^ 1;</pre>
    while (1) {
      int found = 0;
      fill_n(dis, n, 0); fill_n(onstk, n, 0);
       for (int i = 0; i < n; ++i)</pre>
        if (tp = 0, !onstk[i] && SPFA(i))
           for (found = 1; tp >= 2;) {
             int u = stk[--tp];
             int v = stk[--tp];
             match[u] = v, match[v] = u;
      if (!found) break;
    11 \text{ ret} = 0;
    for (int i = 0; i < n; ++i) ret += edge[i][match[i</pre>
         ]];
    return ret >> 1;
};
```

4.5 SW-mincut

```
// global min cut
struct SW{ // 0(V^3)
   static const int MXN = 514;
   int n, vst[MXN], del[MXN];
   int edge[MXN][MXN], wei[MXN];
   void init(int _n){
     n=_n,MEM(edge,0),MEM(del,0);
   void addEdge(int u,int v,int w){
     edge[u][v]+=w,edge[v][u]+=w;
   void search(int &s,int &t){
     MEM(vst,0), MEM(wei,0), s=t=-1;
     while(1){
       int mx=-1,cur=0;
       for(int i=0;i<n;++i)</pre>
         if(!del[i]&&!vst[i]&&mx<wei[i])</pre>
           cur=i,mx=wei[i];
       if(mx==-1) break;
       vst[cur]=1,s=t,t=cur;
       for(int i=0;i<n;++i)</pre>
         if(!vst[i]&&!del[i]) wei[i]+=edge[cur][i];
    }
  }
   int solve(){
     int res=INF;
     for(int i=0,x,y;i<n-1;++i){</pre>
       search(x,y),res=min(res,wei[y]),del[y]=1;
       for(int j=0;j<n;++j)</pre>
         edge[x][j]=(edge[j][x]+=edge[y][j]);
     }
     return res;
   }
};
```

4.6 BoundedFlow(Dinic*)

struct BoundedFlow {//0-base struct edge { int to, cap, flow, rev; }: vector<edge> G[N]; int n, s, t, dis[N], cur[N], cnt[N]; void init(int _n) { n = _n; for (int i = 0; i < n + 2; ++i)</pre> G[i].clear(), cnt[i] = 0;void add_edge(int u, int v, int lcap, int rcap) { cnt[u] -= lcap, cnt[v] += lcap; G[u].pb(edge{v, rcap, lcap, SZ(G[v])}); G[v].pb(edge{u, 0, 0, SZ(G[u]) - 1}); void add_edge(int u, int v, int cap){ G[u].pb(edge{v, cap, 0, SZ(G[v])}); G[v].pb(edge{u, 0, 0, SZ(G[u]) - 1}); int dfs(int u, int cap) { if (u == t || !cap) return cap; for (int &i = cur[u]; i < SZ(G[u]); ++i) {</pre> edge &e = G[u][i]; if (dis[e.to] == dis[u]+1 && e.cap != e.flow) { int df = dfs(e.to, min(e.cap - e.flow, cap)); e.flow += df, G[e.to][e.rev].flow -= df; return df; } } dis[u] = -1;return 0; bool bfs() { $fill_n(dis, n + 3, -1);$ queue<int> q; q.push(s), dis[s] = 0; while (!q.empty()) { int u = q.front(); q.pop(); for (edge &e : G[u]) if (!~dis[e.to] && e.flow != e.cap) q.push(e.to), dis[e.to] = dis[u] + 1; return dis[t] != -1; int maxflow(int _s, int _t) { s = _s, t = _t; int flow = 0, df; while(bfs()) { fill_n(cur, n + 3, 0); while ((df = dfs(s, INF))) flow += df; return flow; bool solve() { int sum = 0;for(int i = 0; i < n; ++i) if(cnt[i] > 0) add_edge(n + 1, i, cnt[i]), sum += cnt[i]; else if(cnt[i] < 0) add_edge(i, n + 2, -cnt[i]);</pre> if(sum != maxflow(n + 1, n + 2)) sum = -1;for(int i = 0; i < n; ++i)</pre> $if(cnt[i] > 0) G[n + 1].pop_back(), G[i].pop_back$ (); else if(cnt[i] < 0) G[i].pop_back(), G[n + 2].</pre> pop_back(); return sum != -1; int solve(int _s, int add_edge(_t, _s, INF); if(!solve()) return -1; //invalid flow int x = G[_t].back().flow; return G[_t].pop_back(), G[_s].pop_back(), x; } };

4.7 Gomory Hu tree

```
struct Gomory_Hu_tree{//0-base
  MaxFlow Dinic;
  int n;
  vector<pii> G[MAXN];
  void init(int _n){n=_n;
    for(int i=0;i<n;++i) G[i].clear();</pre>
  void solve(vector<int> &v){
    if(v.size()<=1) return;</pre>
    int s=rand()%SZ(v);
    swap(v.back(),v[s]),s=v.back();
    int t=v[rand()%(SZ(v)-1)];
    vector<int> L,R;
    int x=(Dinic.reset(),Dinic.maxflow(s,t));
    G[s].pb(pii(t,x)),G[t].pb(pii(s,x));
    for(int i:v)
      if(~Dinic.dis[i]) L.pb(i);
      else R.pb(i);
    solve(L), solve(R);
  void build(){
    vector<int> v(n);
    for(int i=0;i<n;++i) v[i]=i;</pre>
    solve(v);
}ght;//test by BZOJ 4519
MaxFlow &Dinic=ght.Dinic;
```

4.8 isap

```
struct Maxflow {
  static const int MAXV = 20010;
  static const int INF = 1000000;
  struct Edge {
    int v, c, r;
Edge(int _v, int _c, int _r):
      v(_v), c(_c), r(_r) {}
  };
  int s, t;
  vector<Edge> G[MAXV*2];
  int iter[MAXV*2], d[MAXV*2], gap[MAXV*2], tot;
  void init(int x) {
    tot = x+2;
    s = x+1, t = x+2;
    for(int i = 0; i <= tot; i++) {</pre>
      G[i].clear();
      iter[i] = d[i] = gap[i] = 0;
  void addEdge(int u, int v, int c) {
    G[u].push_back(Edge(v, c, SZ(G[v]) ));
G[v].push_back(Edge(u, 0, SZ(G[u]) - 1));
  int dfs(int p, int flow) {
    if(p == t) return flow;
    for(int &i = iter[p]; i < SZ(G[p]); i++) {</pre>
       Edge &e = G[p][i];
      if(e.c > 0 \&\& d[p] == d[e.v]+1) {
         int f = dfs(e.v, min(flow, e.c));
         if(f) {
           e.c -= f;
           G[e.v][e.r].c += f;
           return f;
      }
    if( (--gap[d[p]]) == 0) d[s] = tot;
    else {
      d[p]++;
      iter[p] = 0;
      ++gap[d[p]];
    return 0;
  int solve() {
    int res = 0;
    gap[0] = tot;
```

```
for(res = 0; d[s] < tot; res += dfs(s, INF));</pre>
    return res;
} flow;
```

String

5.1 KMP

```
int F[MAXN];
vector<int> match(string A, string B){
  vector<int> ans;
  F[0]=-1,F[1]=0;
  for(int i=1,j=0;i<B.size();F[++i]=++j){</pre>
    if(B[i]==B[j]) F[i]=F[j];//optimize
    while(j!=-1&&B[i]!=B[j]) j=F[j];
  for(int i=0,j=0;i-j+B.size()<=A.size();++i,++j){</pre>
    while(j!=-1&&A[i]!=B[j]) j=F[j];
    if(j==B.size()-1) ans.pb(i-j);
  }
  return ans;
```

5.2 Z-value

```
const int MAXn = 1e5 + 5;
int z[MAXn];
void make_z(string s){
  int 1 = 0, r = 0;
  for(int i = 1;i < s.size();i++){</pre>
    for(z[i] = max(0, min(r - i + 1, z[i - 1]));
        i + z[i] < s.size() && s[i + z[i]] == s[z[i]];z
             [i]++);
    if(i + z[i] - 1 > r)l = i, r = i + z[i] - 1;
  }
| }
```

5.3 Manacher*

```
int z[MAXN];
int Manacher(string tmp){
  string s="&";
  int l=0,r=0,x,ans;
  for(char c:tmp) s.pb(c),s.pb('%');
  ans=0, x=0;
  for(int i=1;i<SZ(s);++i){</pre>
    z[i]=r > i ? min(z[2*1-i],r-i) : 1;
    while(s[i+z[i]]==s[i-z[i]])++z[i];
    if(z[i]+i>r)r=z[i]+i,l=i;
  for(int i=1;i<SZ(s);++i)</pre>
    if(s[i]=='%')
      x=max(x,z[i]);
  ans=x/2*2,x=0;
  for(int i=1;i<SZ(s);++i)</pre>
    if(s[i]!='%')
      x=max(x,z[i]);
  return \max(ans,(x-1)/2*2+1);
```

Suffix Array

```
struct suffix_array{
  int box[MAXN],tp[MAXN],m;
  bool not_equ(int a,int b,int k,int n){
    return ra[a]!=ra[b]||a+k>=n||b+k>=n||ra[a+k]!=ra[b+
        k];
  void radix(int *key,int *it,int *ot,int n){
    fill n(box, m, 0);
    for(int i=0;i<n;++i) ++box[key[i]];</pre>
```

```
partial_sum(box,box+m,box);
     for(int i=n-1;i>=0;--i) ot[--box[key[it[i]]]]=it[i
   void make_sa(string s,int n){
     int k=1;
     for(int i=0;i<n;++i) ra[i]=s[i];</pre>
     do{
       iota(tp,tp+k,n-k),iota(sa+k,sa+n,0);
       radix(ra+k,sa+k,tp+k,n-k);
       radix(ra,tp,sa,n);
       tp[sa[0]]=0,m=1;
       for(int i=1;i<n;++i){</pre>
         m+=not_equ(sa[i],sa[i-1],k,n);
         tp[sa[i]]=m-1;
       copy_n(tp,n,ra);
       k*=2;
     }while(k<n&&m!=n);</pre>
   void make_he(string s,int n){
     for(int j=0,k=0;j<n;++j){</pre>
       if(ra[j])
         for(;s[j+k]==s[sa[ra[j]-1]+k];++k);
       he[ra[j]]=k,k=max(0,k-1);
     }
   int sa[MAXN],ra[MAXN],he[MAXN];
   void build(string s){
     FILL(sa,0),FILL(ra,0),FILL(he,0);
     FILL(box,0),FILL(tp,0),m=256;
     make_sa(s,s.size());
     make_he(s,s.size());
};
 5.5
```

SAIS*

```
class SAIS {
  public:
    int *SA, *H;
    // zero based, string content MUST > 0
    // result height H[i] is LCP(SA[i - 1], SA[i])
    // string, length, |sigma|
    void build(int *s, int n, int m = 128){
      copy_n(s, n, _s);
       h[0] = s[n++] = 0;
      sais(_s, _sa, _p, _q, _t, _c, n, m);
      mkhei(n);
      SA = _sa + 1; H = _h + 1;
  private:
    bool _t[N * 2];
int _s[N * 2], _c[N * 2], x
     [N], _sa[N * 2], _h[N];
                     _c[N * 2], x[N], _p[N], _q[N * 2], r
    void mkhei(int n){
      for (int i = 0; i < n; i++) r[_sa[i]] = i;</pre>
      for (int i = 0; i < n; i++) if(r[i]) {</pre>
        int ans = i > 0 ? max([h[r[i - 1]] - 1, 0) : 0;
        while(\_s[i + ans] == \_s[\_sa[r[i] - 1] + ans])
             ans++;
         _h[r[i]] = ans;
      }
    }
    void sais(int *s, int *sa, int *p, int *q, bool *t,
          int *c, int n, int z){
      bool uniq = t[n - 1] = 1, neq;
      int nn = 0, nmxz = -1, *nsa = sa + n, *ns = s + n
           , lst = -1;
#define MAGIC(XD) \
      fill_n(sa, n, 0); \
      copy_n(c, z, x); \
      XD; \
      copy_n(c, z - 1, x + 1); \
      for (int i = 0; i < n; i++) if(sa[i] && !t[sa[i]</pre>
            1]) \
```

 $sa[x[s[sa[i]-1]]++] = sa[i] - 1; \$

 $copy_n(c, z, x); \$

```
for(int i = n - 1; i >= 0; i--) if(sa[i] && t[sa[
          i]-1]) \
      sa[--x[s[sa[i]-1]]] = sa[i] - 1;
      fill_n(c, z, 0);
      for (int i = 0; i < n; i++) uniq &= ++c[s[i]] <</pre>
          2;
      partial_sum(c, c + z, c);
      if (uniq) {
        for (int i = 0; i < n; i++) sa[--c[s[i]]] = i;</pre>
      for(int i = n - 2; i >= 0; i--)
        t[i] = (s[i] == s[i + 1] ? t[i + 1] : s[i] < s[
            i + 1]);
      MAGIC(
          for (int i = 1; i <= n - 1; i++) if (t[i] &&
               !t[i - 1])
          sa[--x[s[i]]] = p[q[i] = nn++] = i
          );
      for (int i = 0; i < n; i++) if (sa[i] && t[sa[i]]</pre>
           && !t[sa[i] - 1]) {
        neq = (lst < 0) || !equal(s + lst, s + lst + p[
            q[sa[i]] + 1] - sa[i], s + sa[i]);
        ns[q[1st = sa[i]]] = nmxz += neq;
      sais(ns, nsa, p + nn, q + n, t + n, c + z, nn,
          nmxz + 1);
      MAGIC(
          for(int i = nn - 1; i >= 0; i--)
          sa[--x[s[p[nsa[i]]]]] = p[nsa[i]]
} sa;
```

5.6 Aho-Corasick Automatan

```
const int len=400000,sigma=26;
struct AC Automatan{
  int nx[len][sigma],fl[len],cnt[len],pri[len],top;
  int newnode(){
    fill(nx[top],nx[top]+sigma,-1);
    return top++;
  void init(){top=1,newnode();}
  int input(string &s){//return the end_node of string
   int X=1:
    for(char c:s){
      if(!~nx[X][c-'a'])nx[X][c-'a']=newnode();
      X=nx[X][c-'a'];
    return X:
  void make_fl(){
    queue<int> q;
    q.push(1),fl[1]=0;
    for(int t=0;!q.empty();){
      int R=q.front();
      q.pop(),pri[t++]=R;
      for(int i=0;i<sigma;++i)</pre>
        if(~nx[R][i]){
          int X=nx[R][i],Z=fl[R];
          for(;Z&&!~nx[Z][i];)Z=f1[Z];
          fl[X]=Z?nx[Z][i]:1,q.push(X);
    }
  void get_v(string &s){
    int X=1;
    fill(cnt,cnt+top,0);
    for(char c:s){
      while(X&&!~nx[X][c-'a'])X=f1[X];
      X=X?nx[X][c-'a']:1,++cnt[X];
    for(int i=top-2;i>0;--i) cnt[fl[pri[i]]]+=cnt[pri[i
        11;
  }
};
```

5.7 Smallest Rotation

```
string mcp(string s){
  int n=SZ(s),i=0,j=1;
  s+=s;
  while(i<n&&j<n){
    int k=0;
    while(k<n&&s[i+k]==s[j+k]) ++k;
    if(s[i+k]<=s[j+k]) j+=k+1;
    else i+=k+1;
    if(i==j) ++j;
  }
  int ans=i<n?i:j;
  return s.substr(ans,n);
}</pre>
```

5.8 De Bruijn sequence*

```
constexpr int MAXC = 10, MAXN = 1e5 + 10;
 struct DBSeq {
   int C, N, K, L, buf[MAXC * MAXN]; //K \leftarrow C^N
   void dfs(int *out, int t, int p, int &ptr) {
     if (ptr >= L) return;
     if (t > N) {
        if (N % p) return;
        for (int i = 1; i <= p && ptr < L; ++i)</pre>
          out[ptr++] = buf[i];
     } else {
        buf[t] = buf[t - p], dfs(out, t + 1, p, ptr);
for (int j = buf[t - p] + 1; j < C; ++j)</pre>
          buf[t] = j, dfs(out, t +1 , t, ptr);
   void solve(int _c, int _n, int _k, int *out) {
     int p = 0;
     C = _{c}, N = _{n}, K = _{k}, L = N + K - 1;
dfs(out, 1, 1, p);
     if (p < L) fill(out + p, out + L, 0);</pre>
} dbs;
```

5.9 SAM

```
const int MAXM = 1000010;
struct SAM{
 int tot, root, lst, mom[MAXM], mx[MAXM];
 int acc[MAXM], nxt[MAXM][33];
 int newNode(){
   int res = ++tot;
    fill(nxt[res], nxt[res]+33, 0);
    mom[res] = mx[res] = acc[res] = 0;
   return res;
 void init(){
   tot = 0;
    root = newNode();
    mom[root] = 0, mx[root] = 0;
   lst = root:
 void push(int c){
   int p = lst;
    int np = newNode();
    mx[np] = mx[p]+1;
    for(; p && nxt[p][c] == 0; p = mom[p])
      nxt[p][c] = np;
    if(p == 0) mom[np] = root;
    else{
      int q = nxt[p][c];
      if(mx[p]+1 == mx[q]) mom[np] = q;
      else{
        int nq = newNode();
        mx[nq] = mx[p]+1;
        for(int i = 0; i < 33; i++)</pre>
         nxt[nq][i] = nxt[q][i];
        mom[nq] = mom[q];
        mom[q] = nq;
        mom[np] = nq;
```

5.10 PalTree

```
struct palindromic_tree{// Check by APIO 2014
    palindrome
  struct node{
    int next[26],fail,len;
    int cnt,num;//cnt: appear times, num: number of pal
          suf.
    node(int 1=0):fail(0),len(1),cnt(0),num(0){
      for(int i=0;i<26;++i)next[i]=0;</pre>
    }
  };
  vector<node>St;
  vector<char>s;
  int last,n;
  palindromic_tree():St(2),last(1),n(0){
    St[0].fail=1, St[1].len=-1, s.pb(-1);
  inline void clear(){
    St.clear(), s.clear(), last=1, n=0;
    St.pb(0), St.pb(-1);
    St[0].fail=1, s.pb(-1);
  inline int get_fail(int x){
    while(s[n-St[x].len-1]!=s[n])x=St[x].fail;
    return x;
  inline void add(int c){
    s.push_back(c-='a'), ++n;
    int cur=get_fail(last);
    if(!St[cur].next[c]){
      int now=SZ(St);
      St.pb(St[cur].len+2);
      St[now].fail=St[get_fail(St[cur].fail)].next[c];
      St[cur].next[c]=now;
      St[now].num=St[St[now].fail].num+1;
    last=St[cur].next[c], ++St[last].cnt;
  inline void count(){// counting cnt
    auto i=St.rbegin();
    for(;i!=St.rend();++i){
      St[i->fail].cnt+=i->cnt;
    }
  inline int size(){// The number of diff. pal.
    return SZ(St)-2;
};
```

5.11 cyclicLCS

```
#define L 0
#define LU 1
#define U 2
const int mov[3][2]={0,-1, -1,-1, -1,0};
int al,bl;
char a[MAXL*2],b[MAXL*2]; // 0-indexed
int dp[MAXL*2][MAXL];
char pred[MAXL*2][MAXL];
inline int lcs_length(int r) {
   int i=r+al,j=bl,l=0;
   while(i>r) {
      char dir=pred[i][j];
      if(dir==LU) l++;
      i+=mov[dir][0];
```

6 Math

}

}

}

6.1 ax+by=gcd*

j+=mov[dir][1];

inline void reroot(int r) { // r = new base row

} else if(j<bl&&pred[i+1][j+1]==LU) {</pre>

// a, b, al, bl should be properly filled

-- concatenated after itself

if(a[i-1]==b[j-1]) dp[i][j]=dp[i-1][j-1]+1;

else dp[i][j]=max(dp[i-1][j],dp[i][j-1]);
if(dp[i][j-1]==dp[i][j]) pred[i][j]=L;

else if(a[i-1]==b[j-1]) pred[i][j]=LU;

// note: a WILL be altered in process

while(j<=bl&&pred[i][j]!=LU) j++;</pre>

return 1:

int i=r,j=1;

pred[i][j]=L;

i++:

i++;

} else {

j++;

int cyclic_lcs() {

char tmp[MAXL];
if(al>bl) {

swap(al,bl);

strcpy(a,b);
strcpy(b,tmp);

strcpy(tmp,a);

strcat(a,tmp);

dp[i][0]=0;

dp[0][j]=0;

pred[0][j]=L;

// do cyclic lcs

reroot(i+1);

int clcs=0;

// recover a

a[al]='\0'; return clcs;

pred[i][0]=U;

for(int i=0;i<=2*al;i++) {</pre>

for(int j=0;j<=bl;j++) {</pre>

for(int i=1;i<=2*al;i++) {</pre>

else pred[i][j]=U;

for(int i=0;i<al;i++) {</pre>

clcs=max(clcs,lcs_length(i));

for(int j=1;j<=bl;j++) {</pre>

// basic lcs

strcpy(tmp,a);

}

}

if(j>bl) return;

while(i<2*al&&j<=bl) {</pre>

pred[i][j]=L;

pred[i][j]=L;

if(pred[i+1][j]==U) {

```
pll exgcd(ll a, ll b) {
   if(b == 0) return pll(1, 0);
   else {
      ll p = a / b;
      pll q = exgcd(b, a % b);
      return pll(q.Y, q.X - q.Y * p);
   }
}
```

6.2 floor and ceil

```
int floor(int a,int b){
  return a/b-(a%b&&a<0^b<0);
}
int ceil(int a,int b){
  return a/b+(a%b&&a<0^b>0);
}
```

6.3 floor sum*

```
ll floor_sum(ll n, ll m, ll a, ll b) {
    ll ans = 0;
    if (a >= m)
        ans += (n - 1) * n * (a / m) / 2, a %= m;
    if (b >= m)
        ans += n * (b / m), b %= m;
    ll y_max = (a * n + b) / m, x_max = (y_max * m - b)
    ;
    if (y_max == 0) return ans;
    ans += (n - (x_max + a - 1) / a) * y_max;
    ans += floor_sum(y_max, a, m, (a - x_max % a) % a);
    return ans;
}// sum^{n-1}_0 floor((a * i + b) / m) in log(n + m + a + b)
```

6.4 Miller Rabin*

```
// n < 4,759,123,141
                            3 : 2, 7, 61
// n < 1,122,004,669,633 4 : 2, 13, 23, 1662803
// n < 3,474,749,660,383 6 : pirmes <= 13
// n < 2^64
// 2, 325, 9375, 28178, 450775, 9780504, 1795265022
bool Miller_Rabin(ll a, ll n) {
  if((a = a % n) == 0) return 1;
  if((n & 1) ^ 1) return n == 2;
  11 \text{ tmp} = (n - 1) / ((n - 1) & (1 - n));
  ll t = __lg(((n - 1) & (1 - n))), x = 1;
  for(; tmp; tmp >>= 1, a = mul(a, a, n))
    if(tmp & 1) x = mul(x, a, n);
  if(x == 1 || x == n - 1) return 1;
  while(--t)
    if((x = mul(x, x, n)) == n - 1) return 1;
  return 0;
}
```

6.5 Big number

```
template<typename T>
inline string to_string(const T& x){
  stringstream ss;
  return ss<<x,ss.str();</pre>
struct bigN:vector<ll>{
  const static int base=1000000000, width=log10(base);
  bool negative;
  bigN(const_iterator a,const_iterator b):vector<11>(a,
      b){}
  bigN(string s){
    if(s.empty())return;
if(s[0]=='-')negative=1,s=s.substr(1);
    else negative=0;
    for(int i=int(s.size())-1;i>=0;i-=width){
      ll t=0;
      for(int j=max(0,i-width+1);j<=i;++j)</pre>
        t=t*10+s[j]-'0';
      push_back(t);
    trim();
  template<typename T>
    bigN(const T &x):bigN(to_string(x)){}
  bigN():negative(0){}
  void trim(){
    while(size()&&!back())pop_back();
```

```
if(empty())negative=0;
void carry(int _base=base){
  for(size_t i=0;i<size();++i){</pre>
    if(at(i)>=0&&at(i)<_base)continue;</pre>
    if(i+1u==size())push_back(0);
    int r=at(i)%_base;
    if(r<0)r+=_base;</pre>
    at(i+1)+=(at(i)-r)/_base,at(i)=r;
int abscmp(const bigN &b)const{
  if(size()>b.size())return 1;
  if(size()<b.size())return -1;</pre>
  for(int i=int(size())-1;i>=0;--i){
    if(at(i)>b[i])return 1;
    if(at(i)<b[i])return -1;</pre>
  return 0:
int cmp(const bigN &b)const{
  if(negative!=b.negative)return negative?-1:1;
  return negative?-abscmp(b):abscmp(b);
bool operator<(const bigN&b)const{return cmp(b)<0;}</pre>
bool operator>(const bigN&b)const{return cmp(b)>0;}
bool operator<=(const bigN&b)const{return cmp(b)<=0;}</pre>
bool operator>=(const bigN&b)const{return cmp(b)>=0;}
bool operator==(const bigN&b)const{return !cmp(b);}
bool operator!=(const bigN&b)const{return cmp(b)!=0;}
bigN abs()const{
  bigN res=*this;
  return res.negative=0, res;
bigN operator-()const{
  bigN res=*this;
  return res.negative=!negative,res.trim(),res;
bigN operator+(const bigN &b)const{
  if(negative)return -(-(*this)+(-b));
  if(b.negative)return *this-(-b);
  bigN res=*this;
  if(b.size()>size())res.resize(b.size());
  for(size_t i=0;i<b.size();++i)res[i]+=b[i];</pre>
  return res.carry(),res.trim(),res;
bigN operator-(const bigN &b)const{
  if(negative)return -(-(*this)-(-b));
  if(b.negative)return *this+(-b);
  if(abscmp(b)<0)return -(b-(*this));</pre>
  bigN res=*this;
  if(b.size()>size())res.resize(b.size());
  for(size_t i=0;i<b.size();++i)res[i]-=b[i];</pre>
  return res.carry(),res.trim(),res;
bigN operator*(const bigN &b)const{
  bigN res;
  res.negative=negative!=b.negative;
  res.resize(size()+b.size());
  for(size_t i=0;i<size();++i)</pre>
    for(size_t j=0;j<b.size();++j)</pre>
      if((res[i+j]+=at(i)*b[j])>=base){
        res[i+j+1]+=res[i+j]/base;
        res[i+j]%=base;
      }//%4k¥@carry·|·,¦@
  return res.trim(),res;
bigN operator/(const bigN &b)const{
  int norm=base/(b.back()+1);
  bigN x=abs()*norm;
  bigN y=b.abs()*norm;
  bigN q,r;
  q.resize(x.size());
  for(int i=int(x.size())-1;i>=0;--i){
    r=r*base+x[i];
    int s1=r.size()<=y.size()?0:r[y.size()];</pre>
    int s2=r.size()<y.size()?0:r[y.size()-1];</pre>
    int d=(ll(base)*s1+s2)/y.back();
    r=r-v*d;
    while(r.negative)r=r+y,--d;
    q[i]=d;
```

```
q.negative=negative!=b.negative;
    return q.trim(),q;
  bigN operator%(const bigN &b)const{
    return *this-(*this/b)*b;
  friend istream& operator>>(istream &ss,bigN &b){
    string s;
    return ss>>s, b=s, ss;
  friend ostream& operator<<(ostream &ss,const bigN &b)</pre>
    if(b.negative)ss<<'-';</pre>
    ss<<(b.empty()?0:b.back());</pre>
    for(int i=int(b.size())-2;i>=0;--i)
      ss<<setw(width)<<setfill('0')<<b[i];</pre>
    return ss:
  template<typename T>
    operator T(){
      stringstream ss;
      ss<<*this;</pre>
      T res;
      return ss>>res,res;
};
```

6.6 Fraction

```
struct fraction{
  11 n.d:
  fraction(const 11 &_n=0,const 11 &_d=1):n(_n),d(_d){
    11 t=__gcd(n,d);
    n/=t, \overline{d/=t};
    if(d<0) n=-n,d=-d;
  fraction operator-()const{
    return fraction(-n,d);
  fraction operator+(const fraction &b)const{
    return fraction(n*b.d+b.n*d,d*b.d);
  fraction operator-(const fraction &b)const{
    return fraction(n*b.d-b.n*d,d*b.d);
  fraction operator*(const fraction &b)const{
    return fraction(n*b.n,d*b.d);
  fraction operator/(const fraction &b)const{
    return fraction(n*b.d,d*b.n);
  void print(){
    cout << n;
    if(d!=1) cout << "/" << d;
  }
};
```

6.7 Simultaneous Equations

```
struct matrix { //m variables, n equations
  int n, m;
  fraction M[MAXN][MAXN + 1], sol[MAXN];
  int solve() { //-1: inconsistent, >= 0: rank
    for (int i = 0; i < n; ++i) {</pre>
      int piv = 0;
      while (piv < m && !M[i][piv].n) ++piv;</pre>
      if (piv == m) continue;
      for (int j = 0; j < n; ++j) {</pre>
        if (i == j) continue;
        fraction tmp = -M[j][piv] / M[i][piv];
        for (int k = 0; k <= m; ++k) M[j][k] = tmp * M[</pre>
             i][k] + M[j][k];
      }
    int rank = 0;
    for (int i = 0; i < n; ++i) {</pre>
      int piv = 0;
      while (piv < m && !M[i][piv].n) ++piv;</pre>
```

6.8 Pollard Rho

```
// does not work when n is prime
ll f(ll x,ll mod){ return add(mul(x,x,mod),1,mod); }
ll pollard_rho(ll n){
   if(!(n&1)) return 2;
   while(1){
      ll y=2,x=rand()%(n-1)+1,res=1;
      for(int sz=2;res==1;y=x,sz*=2)
      for(int i=0;i<sz&&res<=1;++i)
            x=f(x,n),res=__gcd(abs(x-y),n);
   if(res!=0&&res!=n) return res;
}
}</pre>
```

6.9 Simplex Algorithm

```
const int MAXN = 111;
const int MAXM = 111;
const double eps = 1E-10;
double a[MAXN][MAXM], b[MAXN], c[MAXM], d[MAXN][MAXM];
double x[MAXM];
int ix[MAXN + MAXM]; // !!! array all indexed from 0
// max{cx} subject to {Ax<=b,x>=0}
// n: constraints, m: vars !!!
// x[] is the optimal solution vector
// usage :
// value = simplex(a, b, c, N, M);
double simplex(double a[MAXN][MAXM], double b[MAXN],
    double c[MAXM], int n, int m){
  ++m;
  int r = n, s = m - 1;
  memset(d, 0, sizeof(d));
  for (int i = 0; i < n + m; ++i) ix[i] = i;</pre>
  for (int i = 0; i < n; ++i) {</pre>
    for (int j = 0; j < m - 1; ++j) d[i][j] = -a[i][j];</pre>
    d[i][m - 1] = 1;
    d[i][m] = b[i];
    if (d[r][m] > d[i][m]) r = i;
  for (int j = 0; j < m - 1; ++j) d[n][j] = c[j];</pre>
  d[n + 1][m - 1] = -1;
  for (double dd;; ) {
    if (r < n) {
      int t = ix[s]; ix[s] = ix[r + m]; ix[r + m] = t;
      d[r][s] = 1.0 / d[r][s];
      for (int j = 0; j <= m; ++j)</pre>
        if (j != s) d[r][j] *= -d[r][s];
      for (int i = 0; i <= n + 1; ++i) if (i != r) {
        for (int j = 0; j <= m; ++j) if (j != s)
  d[i][j] += d[r][j] * d[i][s];</pre>
         d[i][s] *= d[r][s];
      }
    }
    r = -1; s = -1;
    for (int j = 0; j < m; ++j)</pre>
      if (s < 0 || ix[s] > ix[j]) {
        if (d[n + 1][j] > eps ||
             (d[n + 1][j] > -eps && d[n][j] > eps))
    if (s < 0) break;</pre>
    for (int i = 0; i < n; ++i) if (d[i][s] < -eps) {</pre>
      if (r < 0 ||
           (dd = d[r][m] / d[r][s] - d[i][m] / d[i][s])
               < -eps ||
           (dd < eps && ix[r + m] > ix[i + m]))
         r = i;
    if (r < 0) return -1; // not bounded</pre>
```

6.10 chineseRemainder

```
LL solve(LL x1, LL m1, LL x2, LL m2) {
   LL g = __gcd(m1, m2);
   if((x2 - x1) % g) return -1;// no sol
   m1 /= g; m2 /= g;
   pair<LL,LL> p = gcd(m1, m2);
   LL lcm = m1 * m2 * g;
   LL res = p.first * (x2 - x1) * m1 + x1;
   return (res % lcm + lcm) % lcm;
}
```

6.11 QuadraticResidue

```
int Jacobi(int a, int m) {
 int s = 1;
  for (; m > 1; ) {
    a %= m;
    if (a == 0) return 0;
    const int r = __builtin_ctz(a);
    if ((r \& 1) \&\& ((m + 2) \& 4)) s = -s;
    if (a \& m \& 2) s = -s;
    swap(a, m);
  return s;
}
int QuadraticResidue(int a, int p) {
 if (p == 2) return a & 1;
  const int jc = Jacobi(a, p);
  if (jc == 0) return 0;
  if (jc == -1) return -1;
  int b, d;
  for (;;) {
   b = rand() % p;
d = (1LL * b * b + p - a) % p;
    if (Jacobi(d, p) == -1) break;
  int f0 = b, f1 = 1, g0 = 1, g1 = 0, tmp;
  for (int e = (1LL + p) >> 1; e; e >>= 1) {
    if (e & 1) {
      tmp = (1LL * g0 * f0 + 1LL * d * (1LL * g1 * f1 %
           p)) % p;
      g1 = (1LL * g0 * f1 + 1LL * g1 * f0) % p;
      g0 = tmp;
    tmp = (1LL * f0 * f0 + 1LL * d * (1LL * f1 * f1 % p)
       )) % p;
    f1 = (2LL * f0 * f1) % p;
    f0 = tmp;
  return g0;
```

6.12 PiCount

```
int64_t PrimeCount(int64_t n) {
   if (n <= 1) return 0;
   const int v = sqrt(n);
   vector<int> smalls(v + 1);
   for (int i = 2; i <= v; ++i) smalls[i] = (i + 1) / 2;</pre>
```

```
int s = (v + 1) / 2:
  vector<int> roughs(s);
  for (int i = 0; i < s; ++i) roughs[i] = 2 * i + 1;</pre>
  vector<int64_t> larges(s);
  for (int i = 0; i < s; ++i) larges[i] = (n / (2 * i +</pre>
        1) + 1) / 2;
  vector<bool> skip(v + 1);
  int pc = 0;
  for (int p = 3; p <= v; ++p) {</pre>
     if (smalls[p] > smalls[p - 1]) {
       int q = p * p;
       pc++;
       if (1LL * q * q > n) break;
       skip[p] = true;
       for (int i = q; i <= v; i += 2 * p) skip[i] =</pre>
       int ns = 0;
       for (int k = 0; k < s; ++k) {
         int i = roughs[k];
         if (skip[i]) continue;
         int64_t d = 1LL * i * p;
         larges[ns] = larges[k] - (d <= v ? larges[</pre>
             smalls[d] - pc] : smalls[n / d]) + pc;
         roughs[ns++] = i;
      }
       s = ns;
       for (int j = v / p; j >= p; --j) {
        int c = smalls[j] - pc;
         for (int i = j * p, e = min(i + p, v + 1); i <</pre>
             e; ++i) smalls[i] -= c;
      }
    }
  for (int k = 1; k < s; ++k) {
    const int64_t m = n / roughs[k];
     int64_t = larges[k] - (pc + k - 1);
     for (int 1 = 1; 1 < k; ++1) {
       int p = roughs[1];
       if (1LL * p * p > m) break;
       s = smalls[m / p] - (pc + 1 - 1);
     larges[0] -= s;
  return larges[0];
}
```

6.13 Primes

```
/*

12721 13331 14341 75577 123457 222557 556679 999983

1097774749 1076767633 100102021 999997771

1001010013 1000512343 987654361 999991231

999888733 98789101 987777733 999991921

1010101333 1010102101 1000000000039

1000000000000037 2305843009213693951

4611686018427387847 9223372036854775783

18446744073709551557

*/
```

7 Polynomial

7.1 Fast Fourier Transform

```
template<int MAXN>
struct FFT {
    using val_t = complex<double>;
    const double PI = acos(-1);
    val_t w[MAXN];
    FFT() {
        for (int i = 0; i < MAXN; ++i) {
            double arg = 2 * PI * i / MAXN;
            w[i] = val_t(cos(arg), sin(arg));
        }
    void bitrev(val_t *a, int n); // see NTT
    void trans(val_t *a, int n, bool inv = false); // see
        NTT;</pre>
```

```
// remember to replace LL with val_t
};
```

7.2 Number Theory Transform

```
//(2^16)+1, 65537, 3
//7*17*(2^23)+1, 998244353, 3
//1255*(2^20)+1, 1315962881, 3
//51*(2^25)+1, 1711276033, 29
template<int MAXN, LL P, LL RT> //MAXN must be 2^k
struct NTT {
  LL w[MAXN];
  LL mpow(LL a, LL n);
  LL minv(LL a) { return mpow(a, P - 2); }
  NTT() {
    LL dw = mpow(RT, (P - 1) / MAXN);
    w[0] = 1;
    for (int i = 1; i < MAXN; ++i) w[i] = w[i - 1] * dw
          % P;
  }
  void bitrev(LL *a, int n) {
    int i = 0;
    for (int j = 1; j < n - 1; ++j) {
  for (int k = n >> 1; (i ^= k) < k; k >>= 1);
      if (j < i) swap(a[i], a[j]);</pre>
    }
  void operator()(LL *a, int n, bool inv = false) { //0
        \langle = a[i] \langle P
    bitrev(a, n);
    for (int L = 2; L <= n; L <<= 1) {</pre>
      int dx = MAXN / L, d1 = L >> 1;
       for (int i = 0; i < n; i += L) {</pre>
        for (int j = i, x = 0; j < i + dl; ++j, x += dx
           LL tmp = a[j + dl] * w[x] % P;
           if ((a[j + dl] = a[j] - tmp) < 0) a[j + dl]
           if ((a[j] += tmp) >= P) a[j] -= P;
        }
      }
    if (inv) {
      reverse(a + 1, a + n);
      LL invn = minv(n);
       for (int i = 0; i < n; ++i) a[i] = a[i] * invn %</pre>
  }
};
```

7.3 Fast Walsh Transform*

```
/* x: a[j], y: a[j + (L >> 1)]
or: (y += x * op), and: (x += y * op)
xor: (x, y = (x + y) * op, (x - y) * op)
invop: or, and, xor = -1, -1, 1/2 */
void fwt(int *a, int n, int op) { //or
    for (int L = 2; L <= n; L <<= 1)</pre>
         for (int i = 0; i < n; i += L)</pre>
             for (int j = i; j < i + (L >> 1); ++j)
                  a[j + (L >> 1)] += a[j] * op;
const int N = 21;
int f[N][1 << N], g[N][1 << N], h[N][1 << N], ct[1 << N</pre>
    ];
void subset_convolution(int *a, int *b, int *c, int L)
    // c_k = \sum_{i | j = k, i & j = 0} a_i * b_j
    int n = 1 << L;
    for (int i = 1; i < n; ++i)</pre>
         ct[i] = ct[i & (i - 1)] + 1;
    for (int i = 0; i < n; ++i)</pre>
         f[ct[i]][i] = a[i], g[ct[i]][i] = b[i];
    for (int i = 0; i <= L; ++i)</pre>
         fwt(f[i], n, 1), fwt(g[i], n, 1);
    for (int i = 0; i <= L; ++i)
         for (int j = 0; j <= i; ++j)</pre>
```

7.4 Polynomial Operation

```
#define fi(s, n) for (int i = (int)(s); i < (int)(n);
    ++i)
#define Fi(s, n) for (int i = (int)(n); i > (int)(s);
    --i)
int n2k(int n) {
  int sz = 1; while (sz < n) sz <<= 1;</pre>
  return sz;
template<int MAXN, LL P, LL RT> // MAXN = 2^k
struct Poly : public vector<LL> { // coefficients in
    [0, P)
  static NTT<MAXN, P, RT> ntt;
  static const LL INV2;
  int n() const { return (int)size(); } // n() >= 1
  explicit Poly(int _n = 1) : vector<LL>(_n) { }
  Poly(initializer_list<LL> a) : vector<LL>(a) { }
  Poly(const Poly &p, int _n) : vector<LL>(_n) {
    copy_n(p.data(), min(p.n(), _n), data());
  Poly& operator=(const Poly &rhs) {
    clear(), insert(begin(), rhs.begin(), rhs.end());
    return *this;
  Poly Mul(const Poly &rhs) const {
    int _n = n2k(n() + rhs.n() - 1);
    Poly X(*this, _n), Y(rhs, _n);
    ntt(X.data(), _n), ntt(Y.data(),
    fi(0, _n) X[i] = X[i] * Y[i] % P;
    ntt(X.data(), _n, true);
    return X.resize(n() + rhs.n() - 1), X;
  Poly Inv() const { // at(0) != 0
    if (n() == 1) return {ntt.minv(at(0))};
    int _n = n2k(n() * 2);
    Poly Xi = Poly(*this, (n() + 1) / 2).Inv();
    Poly Y(*this, _n); Xi.resize(_n);
    ntt(Xi.data(), _n), ntt(Y.data(), _n);
    fi(0, _n) {
    Xi[i] *= (2 - Xi[i] * Y[i]) % P;
      if ((Xi[i] %= P) < 0) Xi[i] += P;</pre>
    ntt(Xi.data(), _n, true);
    return Xi.resize(n()), Xi;
  Poly Sqrt() const { //at(\theta) != \theta && sqrt(at(\theta))
      exists
    if (n() == 1) return {QuadraticResidue(at(0), P)};
    int _n = n2k(n() * 2);
    Poly X = Poly(*this, (n() + 1) / 2).Sqrt();
    Poly Xi = Poly(X, n()).Inv();
    Poly Y(*this, _n); Xi.resize(_n); X.resize(_n);
    ntt(X.data(), _n), ntt(Xi.data(), _n), ntt(Y.data()
    , _n);
fi(0, _n) {
        if ((X[i] += Y[i] * Xi[i] % P) >= P) X[i] -= P;
        X[i] = X[i] * INV2 % P;
    ntt(X.data(), _n, true);
    return X.resize(n()), X;
  Poly& irev() { reverse(data(), data() + n()); return
      *this;}
  pair<Poly, Poly> DivMod(const Poly &rhs) const { // (
      rhs.)back() != 0
    if (n() < rhs.n()) return {{0}, *this};</pre>
    int _n = n() - rhs.n() + 1;
    Poly X(rhs, rhs.n()); X.irev(); X.resize(_n);
    Poly Y(*this, n()); Y.irev(); Y.resize(_n);
    Poly Q = Y.Mul(X.Inv());
    Q.resize(_n); Q.irev();
```

```
Poly XX = rhs.Mul(Q); Y.resize(n());
    fi(0, n()) if ((Y[i] = (*this)[i] - XX[i]) < 0) Y[i]
        1 += P:
    return {Q, (Y.resize(max(1, rhs.n() - 1)), Y)};
 Poly Derivative() const {
   Poly ret(n() - 1);
    fi(0, ret.n()) ret[i] = (i + 1) * (*this)[i + 1] %
    if (ret.empty()) ret.push_back(0);
    return ret;
 Poly Integral() const {
   Poly ret(n() + 1);
    fi(0, n()) ret[i + 1] = ntt.minv(i + 1) * (*this)[i
        ] % P;
    return ret:
  vector<LL> Eval(const vector<LL> &x) const {
    const int _n = x.size();
    vector<Poly> node(_n * 2);
    fi(0, _n) node[_n + i] = {(x[i] % P ? P - x[i] % P}
    : 0), 1};
Fi(0, _n - 1) node[i] = node[i * 2].Mul(node[i * 2
       + 1]);
    node[0] = *this;
    fi(1, _n * 2) node[i] = node[i / 2].DivMod(node[i])
        .second;
    vector<LL> y(_n);
    fi(0, _n) y[i] = node[_n + i][0];
    return y;
 Poly Interpolate(const vector<LL> &x, const vector<LL
      > &y) const {
    const int _n = x.size();
 }
#undef fi
#undef Fi
template<int MAXN, LL P, LL RT> NTT<MAXN, P, RT> Poly<
   MAXN, P, RT>::ntt;
template<int MAXN, LL P, LL RT> const LL Poly<MAXN, P,
    RT>:::INV2 = ntt.minv(2);
using Poly_t = Poly<131072 * 2, 998244353, 3>;
```

8 Geometry

8.1 Default Code

```
typedef pair<double,double> pdd;
typedef pair<pdd,pdd> Line;
struct Cir{pdd O; double R;};
const double eps=1e-8;
pdd operator+(const pdd &a, const pdd &b)
{ return pdd(a.X + b.X, a.Y + b.Y);}
pdd operator-(const pdd &a, const pdd &b)
{ return pdd(a.X - b.X, a.Y - b.Y);}
pdd operator*(const pdd &a, const double &b)
{ return pdd(a.X * b, a.Y * b);}
pdd operator/(const pdd &a, const double &b)
{ return pdd(a.X / b, a.Y / b);}
double dot(const pdd &a,const pdd &b)
{ return a.X * b.X + a.Y * b.Y;}
double cross(const pdd &a,const pdd &b)
{ return a.X * b.Y - a.Y * b.X;}
double abs2(const pdd &a)
{ return dot(a, a);}
double abs(const pdd &a)
{ return sqrt(dot(a, a));}
int sign(const double &a)
{ return fabs(a) < eps ? 0 : a > 0 ? 1 : -1;}
int ori(const pdd &a,const pdd &b,const pdd &c)
{ return sign(cross(b - a, c - a));}
bool collinearity(const pdd &p1, const pdd &p2, const
    pdd &p3)
{ return fabs(cross(p1 - p3, p2 - p3)) < eps;}
bool btw(const pdd &p1,const pdd &p2,const pdd &p3) {
 if(!collinearity(p1, p2, p3)) return 0;
```

```
return dot(p1 - p3, p2 - p3) < eps;
bool seg_intersect(const pdd &p1,const pdd &p2,const
    pdd &p3, const pdd &p4) {
  int a123 = ori(p1, p2, p3);
  int a124 = ori(p1, p2, p4);
  int a341 = ori(p3, p4, p1);
  int a342 = ori(p3, p4, p2);
  if(a123 == 0 && a124 == 0)
    return btw(p1, p2, p3) || btw(p1, p2, p4) ||
btw(p3, p4, p1) || btw(p3, p4, p2);
  return a123 * a124 <= 0 && a341 * a342 <= 0;
pdd intersect(const pdd &p1, const pdd &p2, const pdd &
    p3, const pdd &p4) {
  double a123 = cross(p2 - p1, p3 - p1);
  double a124 = cross(p2 - p1, p4 - p1);
return (p4 * a123 - p3 * a124) / (a123 - a124);
pdd perp(const pdd &p1)
{ return pdd(-p1.Y, p1.X);}
pdd foot(const pdd &p1, const pdd &p2, const pdd &p3)
{ return intersect(p1, p2, p3, p3 + perp(p2 - p1));}
```

8.2 Convex hull*

8.3 External bisector

```
pdd external_bisector(pdd p1,pdd p2,pdd p3){//213
  pdd L1=p2-p1,L2=p3-p1;
  L2=L2*abs(L1)/abs(L2);
  return L1+L2;
}
```

8.4 Heart

```
pdd excenter(pdd p0,pdd p1,pdd p2,double &radius){
  p1=p1-p0,p2=p2-p0;
  double x1=p1.X,y1=p1.Y,x2=p2.X,y2=p2.Y;
  double m=2.*(x1*y2-y1*x2);
  center.X=(x1*x1*y2-x2*x2*y1+y1*y2*(y1-y2))/m;
  center.Y=(x1*x2*(x2-x1)-y1*y1*x2+x1*y2*y2)/m;
  return radius=abs(center),center+p0;
pdd incenter(pdd p1,pdd p2,pdd p3,double &radius){
  double a=abs(p2-p1),b=abs(p3-p1),c=abs(p3-p2);
  double s=(a+b+c)/2, area=sqrt(s*(s-a)*(s-b)*(s-c));
  pdd L1=external_bisector(p1,p2,p3),L2=
      external_bisector(p2,p1,p3);
  return radius=area/s,intersect(p1,p1+L1,p2,p2+L2),
pdd escenter(pdd p1,pdd p2,pdd p3){//213
  pdd L1=external_bisector(p1,p2,p3),L2=
      external_bisector(p2,p2+p2-p1,p3);
  return intersect(p1,p1+L1,p2,p2+L2);
pdd barycenter(pdd p1,pdd p2,pdd p3){
 return (p1+p2+p3)/3;
pdd orthocenter(pdd p1,pdd p2,pdd p3){
```

```
pdd L1=p3-p2,L2=p3-p1;
swap(L1.X,L1.Y),L1.X*=-1;
swap(L2,X,L2.Y),L2.X*=-1;
return intersect(p1,p1+L1,p2,p2+L2);
}
```

8.5 Minimum Circle Cover*

```
pdd Minimum_Circle_Cover(vector<pdd> dots, double &r) {
  pdd cent;
  random_shuffle(ALL(dots));
  cent = dots[0], r = 0;
  for (int i = 1; i < SZ(dots); ++i)</pre>
    if (abs(dots[i] - cent) > r) {
      cent = dots[i], r = 0;
      for (int j = 0; j < i; ++j)</pre>
        if (abs(dots[j] - cent) > r) {
          cent = (dots[i] + dots[j]) / 2;
           r = abs(dots[i] - cent);
          for(int k = 0; k < j; ++k)
  if(abs(dots[k] - cent) > r)
               cent = excenter(dots[i], dots[j], dots[k
                    ], r);
        }
  return cent:
```

8.6 Polar Angle Sort*

```
pdd center;//sort base
int Quadrant(pdd a) {
  if(a.X > 0 && a.Y >= 0) return 1;
  if(a.X <= 0 && a.Y > 0) return 2;
  if(a.X < 0 && a.Y <= 0) return 3;</pre>
  if(a.X >= 0 && a.Y < 0) return 4;
bool cmp(pll a, pll b) {
  a = a - center, b = b - center;
  if (Quadrant(a) != Quadrant(b))
    return Quadrant(a) < Quadrant(b);</pre>
  if (cross(b, a) == 0) return abs2(a) < abs2(b);</pre>
  return cross(a, b) > 0;
bool cmp(pdd a, pdd b) {
  a = a - center, b = b - center;
  if(fabs(atan2(a.Y, a.X) - atan2(b.Y, b.X)) > eps)
    return atan2(a.Y, a.X) < atan2(b.Y, b.X);</pre>
  return abs(a) < abs(b);</pre>
| }
```

8.7 Intersection of two circles*

8.8 Intersection of polygon and circle

```
// Divides into multiple triangle, and sum up
// test by HDU2892
const double PI=acos(-1);
double _area(pdd pa, pdd pb, double r){
  if(abs(pa)<abs(pb)) swap(pa, pb);</pre>
  if(abs(pb)<eps) return 0;</pre>
  double S, h, theta;
  double a=abs(pb),b=abs(pa),c=abs(pb-pa);
  double cosB = dot(pb,pb-pa) / a / c, B = acos(cosB);
  double cosC = dot(pa,pb) / a / b, C = acos(cosC);
  if(a > r){
    S = (C/2)*r*r;
    h = a*b*sin(C)/c;
    if (h < r \&\& B < PI/2) S -= (acos(h/r)*r*r - h*sqrt
         (r*r-h*h));
  else if(b > r){
    theta = PI - B - asin(sin(B)/r*a);
    S = .5*a*r*sin(theta) + (C-theta)/2*r*r;
  else S = .5*sin(C)*a*b;
  return S;
double area_poly_circle(const vector<pdd> poly,const
    pdd &0, const double r){
  double S=0;
  for(int i=0;i<SZ(poly);++i)</pre>
    S+=\_area(poly[i]-0,poly[(i+1)\%SZ(poly)]-0,r)*ori(0,
        poly[i],poly[(i+1)%SZ(poly)]);
  return fabs(S);
}
```

8.9 Intersection of line and circle

8.10 point in circle

```
// return p4 is strictly in circumcircle of tri(p1,p2,
     p3)
long long sqr(long long x) { return x * x; }
bool in_cc(const pll& p1, const pll& p2, const pll& p3,
      const pll& p4) {
     long long u11 = p1.X - p4.X; long long u12 = p1.Y -
           p4.Y;
     long long u21 = p2.X - p4.X; long long u22 = p2.Y -
           p4.Y;
     long long u31 = p3.X - p4.X; long long u32 = p3.Y -
           p4.Y;
     long long u13 = sqr(p1.X) - sqr(p4.X) + sqr(p1.Y) -
            sqr(p4.Y);
     long long u23 = sqr(p2.X) - sqr(p4.X) + sqr(p2.Y) -
           sqr(p4.Y);
     long long u33 = sqr(p3.X) - sqr(p4.X) + sqr(p3.Y) -
           sqr(p4.Y);
      _int128 det = (__int128)-u13 * u22 * u31 + (
    __int128)u12 * u23 * u31 + (__int128)u13 * u21
    * u32 - (__int128)u11 * u23 * u32 - (__int128)
    u12 * u21 * u33 + (__int128)u11 * u22 * u33;
     return det > eps;
```

8.11 Half plane intersection

```
bool isin( Line 10, Line 11, Line 12 ){
    // Check inter(L1, L2) in L0
    pdd p = intersect(l1.X,l1.Y,l2.X,l2.Y);
    return cross(l0.Y - l0.X,p - l0.X) > eps;
```

```
/* If no solution, check: 1. ret.size() < 3
* Or more precisely, 2. interPnt(ret[0], ret[1])
* in all the lines. (use (L.Y - L.X) ^ (p - L.X) > 0
/* --^-- Line.X --^-- Line.Y --^-- */
vector<Line> halfPlaneInter(vector<Line> lines){
  int sz = lines.size();
  vector<double> ata(sz),ord(sz);
  for(int i=0; i<sz; ++i) {</pre>
    ord[i] = i;
    pdd d = lines[i].Y - lines[i].X;
    ata[i] = atan2(d.Y, d.X);
  sort(ord.begin(), ord.end(), [&](int i,int j){
      if( fabs(ata[i] - ata[j]) < eps )</pre>
      return (cross(lines[i].Y-lines[i].X,
             lines[j].Y-lines[i].X))<0;</pre>
      return ata[i] < ata[j];</pre>
      });
  vector<Line> fin;
  for (int i=0; i<sz; ++i)</pre>
    if (!i || fabs(ata[ord[i]] - ata[ord[i-1]]) > eps)
      fin.pb(lines[ord[i]]);
  deque<Line> dq;
  for (int i=0; i<SZ(fin); i++){</pre>
    while(SZ(dq)>=2&&!isin(fin[i],dq[SZ(dq)-2],dq.back
        ()))
      dq.pop_back();
    while(SZ(dq)>=2&&!isin(fin[i],dq[0],dq[1]))
      dq.pop_front();
    dq.push_back(fin[i]);
 while (SZ(dq) >= 3\&\&! isin(dq[0], dq[SZ(dq)-2], dq.back()))
    dq.pop_back();
  while(SZ(dq) >= 3\&\&!isin(dq.back(), dq[0], dq[1]))
    dq.pop_front();
  vector<Line> res(ALL(dq));
  return res;
```

8.12 CircleCover*

```
const int N = 1021;
struct CircleCover {
  int C;
  Cir c[N];
  bool g[N][N], overlap[N][N];
  // Area[i] : area covered by at least i circles
  double Area[ N ];
  void init(int _C){ C = _C;}
  struct Teve {
    pdd p; double ang; int add;
    Teve() {}
    Teve(pdd _a, double _b, int _c):p(_a), ang(_b), add
         (_c){}
    bool operator < (const Teve &a)const
    {return ang < a.ang;}
  }eve[N * 2];
 // strict: x = 0, otherwise x = -1
bool disjuct(Cir &a, Cir &b, int x)
  {return sign(abs(a.0 - b.0) - a.R - b.R) > x;}
  bool contain(Cir &a, Cir &b, int x)
  {return sign(a.R - b.R - abs(a.O - b.O)) > x;}
  bool contain(int i, int j) {
    /* c[j] is non-strictly in c[i]. */
    return (sign(c[i].R - c[j].R) > 0 \mid \mid (sign(c[i].R - c[i].R) \mid c[i].R
          c[j].R) == 0 && i < j)) && contain(c[i], c[j],
          -1);
  void solve(){
    fill_n(Area, C + 2, 0);
    for(int i = 0; i < C; ++i)</pre>
       for(int j = 0; j < C; ++j)</pre>
         overlap[i][j] = contain(i, j);
    for(int i = 0; i < C; ++i)
  for(int j = 0; j < C; ++j)</pre>
         g[i][j] = !(overlap[i][j] || overlap[j][i] ||
             disjuct(c[i], c[j], -1));
    for(int i = 0; i < C; ++i){</pre>
```

```
int E = 0, cnt = 1;
for(int j = 0; j < C; ++j)</pre>
         if(j != i && overlap[j][i])
           ++cnt;
      for(int j = 0; j < C; ++j)</pre>
        if(i != j && g[i][j]) {
           pdd aa, bb;
           CCinter(c[i], c[j], aa, bb);
           double A = atan2(aa.Y - c[i].0.Y, aa.X - c[i]
               ].O.X);
           double B = atan2(bb.Y - c[i].0.Y, bb.X - c[i
               1.0.X);
           eve[E++] = Teve(bb, B, 1), eve[E++] = Teve(aa)
                , A, -1);
           if(B > A) ++cnt;
      if(E == 0) Area[cnt] += pi * c[i].R * c[i].R;
      else{
        sort(eve, eve + E);
         eve[E] = eve[0];
         for(int j = 0; j < E; ++j){</pre>
           cnt += eve[j].add;
           Area[cnt] += cross(eve[j].p, eve[j + 1].p) *
           double theta = eve[j + 1].ang - eve[j].ang;
           if (theta < 0) theta += 2. * pi;</pre>
           Area[cnt] += (theta - sin(theta)) * c[i].R *
               c[i].R * .5;
        }
      }
    }
  }
}:
```

8.13 3Dpoint*

```
struct Point {
  double x, y, z;
  Point(double _x = 0, double _y = 0, double _z = 0): x
      (_x), y(_y), z(_z){}
  Point(pdd p) { x = p.X, y = p.Y, z = abs2(p); }
Point operator-(const Point &p1, const Point &p2)
{ return Point(p1.x - p2.x, p1.y - p2.y, p1.z - p2.z);}
Point cross(const Point &p1, const Point &p2)
{ return Point(p1.y * p2.z - p1.z * p2.y, p1.z * p2.x -
     p1.x * p2.z, p1.x * p2.y - p1.y * p2.x);}
double dot(const Point &p1, const Point &p2)
{ return p1.x * p2.x + p1.y * p2.y + p1.z * p2.z;}
double abs(const Point &a)
{ return sqrt(dot(a, a));}
Point cross3(const Point &a, const Point &b, const
    Point &c)
{ return cross(b - a, c - a);}
double area(Point a, Point b, Point c)
{ return abs(cross3(a, b, c));}
double volume(Point a, Point b, Point c, Point d)
{return dot(cross3(a, b, c), d - a);}
```

8.14 Convexhull3D*

```
void dfs(int p, int now) {
  F[now].ok = 0;
  deal(p, F[now].b, F[now].a), deal(p, F[now].c, F[
      now].b), deal(p, F[now].a, F[now].c);
bool same(int s,int t){
  Point &a = P[F[s].a];
  Point &b = P[F[s].b];
  Point &c = P[F[s].c];
  return fabs(volume(a, b, c, P[F[t].a])) < eps &&</pre>
      fabs(volume(a, b, c, P[F[t].b])) < eps && fabs(</pre>
      volume(a, b, c, P[F[t].c])) < eps;</pre>
}
void init(int _n){n = _n, num = 0;}
void solve() {
  face add:
  num = 0;
  if(n < 4) return;</pre>
  if([&](){
      for (int i = 1; i < n; ++i)</pre>
      if (abs(P[0] - P[i]) > eps)
      return swap(P[1], P[i]), 0;
      return 1;
      }() || [&](){
      for (int i = 2; i < n; ++i)</pre>
      if (abs(cross3(P[i], P[0], P[1])) > eps)
      return swap(P[2], P[i]), 0;
      return 1;
      }() || [&](){
      for (int i = 3; i < n; ++i)</pre>
      if (fabs(dot(cross(P[0] - P[1], P[1] - P[2]), P
          [0] - P[i])) > eps)
      return swap(P[3], P[i]), 0;
      return 1;
      }())return;
  for (int i = 0; i < 4; ++i) {</pre>
    add.a = (i + 1) % 4, add.b = (i + 2) % 4, add.c =
         (i + 3) % 4, add.ok = true;
    if (dblcmp(P[i],add) > 0) swap(add.b, add.c);
    g[add.a][add.b] = g[add.b][add.c] = g[add.c][add.
        al = num;
    F[num++] = add;
  for (int i = 4; i < n; ++i)</pre>
    for (int j = 0; j < num; ++j)
      if (F[j].ok && dblcmp(P[i],F[j]) > eps) {
        dfs(i, j);
        break;
  for (int tmp = num, i = (num = 0); i < tmp; ++i)</pre>
    if (F[i].ok) F[num++] = F[i];
double get_area() {
  double res = 0.0;
  if (n == 3)
    return abs(cross3(P[0], P[1], P[2])) / 2.0;
  for (int i = 0; i < num; ++i)</pre>
    res += area(P[F[i].a], P[F[i].b], P[F[i].c]);
  return res / 2.0;
double get_volume() {
  double res = 0.0:
  for (int i = 0; i < num; ++i)</pre>
    res += volume(Point(0, 0, 0), P[F[i].a], P[F[i].b
        ], P[F[i].c]);
  return fabs(res / 6.0);
int triangle() {return num;}
int polygon() {
  int res = 0;
  for (int i = 0, flag = 1; i < num; ++i, res += flag</pre>
       , flag = 1)
    for (int j = 0; j < i && flag; ++j)</pre>
      flag &= !same(i,j);
  return res;
Point getcent(){
  Point ans(0, 0, 0), temp = P[F[0].a];
  double v = 0.0, t2;
  for (int i = 0; i < num; ++i)</pre>
    if (F[i].ok == true) {
```

```
Point p1 = P[F[i].a], p2 = P[F[i].b], p3 = P[F[i].b]
             i].c];
         t2 = volume(temp, p1, p2, p3) / 6.0;
        if (t2>0)
           ans.x += (p1.x + p2.x + p3.x + temp.x) * t2,
               ans.y += (p1.y + p2.y + p3.y + temp.y) *
               t2, ans.z += (p1.z + p2.z + p3.z + temp.z
) * t2, v += t2;
      }
    ans.x /= (4 * v), ans.y /= (4 * v), ans.z /= (4 * v)
         );
    return ans;
  double pointmindis(Point p) {
    double rt = 99999999;
     for(int i = 0; i < num; ++i)</pre>
      if(F[i].ok == true) {
         Point p1 = P[F[i].a], p2 = P[F[i].b], p3 = P[F[i].b]
             i].c];
         double a = (p2.y - p1.y) * (p3.z - p1.z) - (p2.
             z - p1.z) * (p3.y - p1.y);
         double b = (p2.z - p1.z) * (p3.x - p1.x) - (p2.
             x - p1.x) * (p3.z - p1.z);
         double c = (p2.x - p1.x) * (p3.y - p1.y) - (p2.
             y - p1.y) * (p3.x - p1.x);
         double d = 0 - (a * p1.x + b * p1.y + c * p1.z)
         double temp = fabs(a * p.x + b * p.y + c * p.z
             + d) / sqrt(a * a + b * b + c * c);
        rt = min(rt, temp);
    return rt;
  }
};
```

8.15 DelaunayTriangulation*

```
/* Delaunay Triangulation:
Given a sets of points on 2D plane, find a
triangulation such that no points will strictly
inside circumcircle of any triangle.
find : return a triangle contain given point
add_point : add a point into triangulation
A Triangle is in triangulation iff. its has_chd is 0.
Region of triangle u: iterate each u.edge[i].tri,
each points are u.p[(i+1)\%3], u.p[(i+2)\%3]
Voronoi diagram: for each triangle in triangulation,
the bisector of all its edges will split the region.
nearest point will belong to the triangle containing it
const 11 inf = MAXC * MAXC * 100; // Lower_bound
    unknown
struct Tri;
struct Edge {
    Tri* tri; int side;
    Edge(): tri(0), side(0){}
    Edge(Tri* _tri, int _side): tri(_tri), side(_side)
struct Tri {
    pll p[3];
    Edge edge[3];
    Tri* chd[3];
    Tri() {}
    Tri(const pll& p0, const pll& p1, const pll& p2) {
        p[0] = p0; p[1] = p1; p[2] = p2;
        chd[0] = chd[1] = chd[2] = 0;
    bool has_chd() const { return chd[0] != 0; }
    int num_chd() const {
        return !!chd[0] + !!chd[1] + !!chd[2];
    bool contains(pll const& q) const {
        for (int i = 0; i < 3; ++i)</pre>
            if (ori(p[i], p[(i + 1) % 3], q) < 0)</pre>
                return 0;
        return 1:
} pool[N * 10], *tris;
void edge(Edge a, Edge b) {
```

```
if(a.tri) a.tri -> edge[a.side] = b;
    if(b.tri) b.tri -> edge[b.side] = a;
struct Trig { // Triangulation
    Trig() {
         the_root = // Tri should at least contain all
             points
             new(tris++) Tri(pll(-inf, -inf), pll(inf +
                  inf, -inf), pll(-inf, inf + inf));
    Tri* find(pll p) { return find(the_root, p); }
    void add_point(const pll &p) { add_point(find(
         the_root, p), p); }
    Tri* the_root;
    static Tri* find(Tri* root, const pll &p) {
         while (1) {
             if (!root -> has_chd())
                  return root;
             for (int i = 0; i < 3 && root -> chd[i]; ++
                  i)
                  if (root -> chd[i] -> contains(p)) {
                      root = root -> chd[i];
                      break;
         assert(0); // "point not found"
    void add_point(Tri* root, pll const& p) {
         Tri* t[3];
         /* split it into three triangles */
         for (int i = 0; i < 3; ++i)</pre>
             t[i] = new(tris++) Tri(root -> p[i], root
                  -> p[(i + 1) % 3], p);
         for (int i = 0; i < 3; ++i)
             edge(Edge(t[i], 0), Edge(t[(i + 1) % 3], 1)
         for (int i = 0; i < 3; ++i)</pre>
             edge(Edge(t[i], 2), root \rightarrow edge[(i + 2) %]
                  3]);
         for (int i = 0; i < 3; ++i)</pre>
             root -> chd[i] = t[i];
         for (int i = 0; i < 3; ++i)</pre>
             flip(t[i], 2);
    void flip(Tri* tri, int pi) {
   Tri* trj = tri -> edge[pi].tri;
   int pj = tri -> edge[pi].side;
         if (!trj) return;
         if (!in_cc(tri -> p[0], tri -> p[1], tri -> p
              [2], trj -> p[pj])) return;
         /* flip edge between tri,trj */
         Tri* trk = new(tris++) Tri(tri -> p[(pi + 1) %
             3], trj -> p[pj], tri -> p[pi]);
         Tri* trl = new(tris++) Tri(trj -> p[(pj + 1) %
         3], tri -> p[pi], trj -> p[pj]);
edge(Edge(trk, 0), Edge(trl, 0));
         edge(Edge(trk, 1), tri->edge[(pi + 2) % 3]);
         edge(Edge(trk, 2), trj->edge[(pj + 1) % 3]);
edge(Edge(trl, 1), trj->edge[(pj + 2) % 3]);
         edge(Edge(trl, 2), tri->edge[(pi + 1) % 3]);
         tri -> chd[0] = trk; tri -> chd[1] = trl; tri
              -> chd[2] = 0;
         trj -> chd[0] = trk; trj -> chd[1] = trl; trj
              -> chd[2] = 0;
         flip(trk, 1); flip(trk, 2);
         flip(trl, 1); flip(trl, 2);
    }
vector<Tri*> triang; // vector of all triangle
set<Tri*> vst;
void go(Tri* now) { // store all tri into triang
    if (vst.find(now) != vst.end())
        return;
    vst.insert(now);
    if (!now -> has_chd())
         return triang.push_back(now);
    for (int i = 0; i < now->num_chd(); ++i)
         go(now -> chd[i]);
void build(int n, pll* ps) { // build triangulation
    tris = pool; triang.clear(); vst.clear();
    random\_shuffle(ps, ps + n);
```

```
Trig tri; // the triangulation structure
for (int i = 0; i < n; ++i)
    tri.add_point(ps[i]);
go(tri.the_root);</pre>
```

8.16 Triangulation Vonoroi*

```
vector<Line> ls[N];
pll arr[N];
Line make_line(pdd p, Line 1) {
    pdd d = 1.Y - 1.X; d = perp(d);
pdd m = (1.X + 1.Y) / 2;
    l = Line(m, m + d);
    if (ori(1.X, 1.Y, p) < 0)
        l = Line(m + d, m);
    return 1;
double calc_area(int id) {
    // use to calculate the area of point "strictly in
         the convex hull"
    vector<Line> hpi = halfPlaneInter(ls[id]);
    vector<pdd> ps;
    for (int i = 0; i < SZ(hpi); ++i)</pre>
         ps.pb(intersect(hpi[i].X, hpi[i].Y, hpi[(i + 1)
              % SZ(hpi)].X, hpi[(i + 1) % SZ(hpi)].Y));
    double rt = 0;
    for (int i = 0; i < SZ(ps); ++i)</pre>
        rt += cross(ps[i], ps[(i + 1) % SZ(ps)]);
    return fabs(rt) / 2;
void solve(int n, pii *oarr) {
    map<pll, int> mp;
    for (int i = 0; i < n; ++i)</pre>
         arr[i] = pll(oarr[i].X, oarr[i].Y), mp[arr[i]]
    build(n, arr); // Triangulation
for (auto *t : triang) {
         vector<int> p;
        for (int i = 0; i < 3; ++i)
             if (mp.find(t -> p[i]) != mp.end())
                 p.pb(mp[t -> p[i]]);
         for (int i = 0; i < SZ(p); ++i)</pre>
             for (int j = i + 1; j < SZ(p); ++j) {</pre>
                 Line l(oarr[p[i]], oarr[p[j]]);
                 ls[p[i]].pb(make_line(oarr[p[i]], 1));
                 ls[p[j]].pb(make_line(oarr[p[j]], 1));
```

8.17 Tangent line of two circles

```
vector<Line> go( const Cir& c1 , const Cir& c2 , int
    sign1 ){
  // sign1 = 1 for outer tang, -1 for inter tang
  vector<Line> ret;
  double d_sq = norm2( c1.0 - c2.0 );
  if( d_sq < eps ) return ret;</pre>
  double d = sqrt( d_sq );
  Pt v = (c2.0 - c1.0) / d;
  double c = ( c1.R - sign1 * c2.R ) / d;
  if( c * c > 1 ) return ret;
  double h = sqrt( max( 0.0 , 1.0 - c * c ) );
  for( int sign2 = 1 ; sign2 >= -1 ; sign2 -= 2 ){
    Pt n = { v.X * c - sign2 * h * v.Y ,
v.Y * c + sign2 * h * v.X };
    Pt p1 = c1.0 + n * c1.R;
    Pt p2 = c2.0 + n * (c2.R * sign1);
    if( fabs( p1.X - p2.X ) < eps and</pre>
        fabs( p1.Y - p2.Y ) < eps )
      p2 = p1 + perp(c2.0 - c1.0);
    ret.push_back( { p1 , p2 } );
  }
  return ret;
```

8.18 minMaxEnclosingRectangle

```
pdd solve(vector<pll> &dots){
  vector<pll> hull;
  const double INF=1e18,qi=acos(-1)/2*3;
  cv.dots=dots;
 hull=cv.hull();
 double Max=0,Min=INF,deg;
 11 n=hull.size();
 hull.pb(hull[0]);
  for(int i=0,u=1,r=1,l;i<n;++i){</pre>
    pll nw=hull[i+1]-hull[i];
    while(cross(nw, hull[u+1]-hull[i])>cross(nw, hull[u]-
        hull[i]))
      u=(u+1)%n;
    while(dot(nw,hull[r+1]-hull[i])>dot(nw,hull[r]-hull
        [i]))
      r=(r+1)%n;
    if(!i) l=(r+1)%n;
    while(dot(nw,hull[1+1]-hull[i])<dot(nw,hull[1]-hull</pre>
        [i]))
      1=(1+1)%n;
   Min=min(Min,(double)(dot(nw,hull[r]-hull[i])-dot(nw
        ,hull[1]-hull[i]))*cross(nw,hull[u]-hull[i])/
        abs2(nw));
    deg=acos((double)dot(hull[r]-hull[l],hull[u]-hull[i
        ])/abs(hull[r]-hull[l])/abs(hull[u]-hull[i]));
    deg=(qi-deg)/2;
   {\tt Max=max(Max,(double)abs(hull[r]-hull[l])*abs(hull[u])}
        ]-hull[i])*sin(deg)*sin(deg));
 }
  return pdd(Min,Max);
```

8.19 minDistOfTwoConvex

```
// p, q is convex
double TwoConvexHullMinDist(Point P[], Point Q[], int n
     int m) {
  int YMinP = 0, YMaxQ = 0;
  double tmp, ans = 999999999;
 for (i = 0; i < n; ++i) if(P[i].y < P[YMinP].y) YMinP</pre>
       = i;
  for (i = 0; i < m; ++i) if (Q[i].y > Q[YMaxQ].y) YMaxQ
       = i;
  P[n] = P[0], Q[m] = Q[0];
 for (int i = 0; i < n; ++i) {
   while (tmp = Cross(Q[YMaxQ + 1] - P[YMinP + 1], P[
        YMinP] - P[YMinP + 1]) > Cross(Q[YMaxQ] - P[
        YMinP + 1, P[YMinP] - P[YMinP + 1])) <math>YMaxQ = (
        YMaxQ + 1) % m;
    if (tmp < 0) ans = min(ans, PointToSegDist(P[YMinP</pre>
        ], P[YMinP + 1], Q[YMaxQ]));
    else ans = min(ans, TwoSegMinDist(P[YMinP], P[YMinP
         + 1], Q[YMaxQ], Q[YMaxQ + 1]));
    YMinP = (YMinP + 1) % n;
  return ans;
```

8.20 Minkowski Sum*

```
vector<pll> Minkowski(vector<pll> A, vector<pll> B) {
  hull(A), hull(B);
  vector<pll> C(1, A[0] + B[0]), s1, s2;
  for(int i = 0; i < SZ(A); ++i)
    s1.pb(A[(i + 1) % SZ(A)] - A[i]);
  for(int i = 0; i < SZ(B); i++)
    s2.pb(B[(i + 1) % SZ(B)] - B[i]);
  for(int p1 = 0, p2 = 0; p1 < SZ(A) || p2 < SZ(B);)
  if (p2 >= SZ(B) || (p1 < SZ(A) && cross(s1[p1], s2[
      p2]) >= 0))
    C.pb(C.back() + s1[p1++]);
  else
    C.pb(C.back() + s2[p2++]);
  return hull(C), C;
}
```

9 Else

9.1 Mo's Alogrithm(With modification)

```
struct QUERY{//BLOCK=N^{2/3}
  int L,R,id,LBid,RBid,T;
  QUERY(int l, int r, int id, int lb, int rb, int t):
    L(1),R(r),id(id),LBid(lb),RBid(rb),T(t){}
  bool operator<(const QUERY &b)const{</pre>
    if(LBid!=b.LBid) return LBid<b.LBid;</pre>
    if(RBid!=b.RBid) return RBid<b.RBid;</pre>
    return T<b.T;
  }
};
vector<QUERY> query;
int cur_ans,arr[MAXN],ans[MAXN];
void addTime(int L,int R,int T){}
void subTime(int L,int R,int T){}
void add(int x){}
void sub(int x){}
void solve(){
  sort(ALL(query));
  int L=0,R=0,T=-1;
  for(auto q:query){
    while(T<q.T) addTime(L,R,++T);</pre>
    while(T>q.T) subTime(L,R,T--);
    while(R<q.R) add(arr[++R]);</pre>
    while(L>q.L) add(arr[--L]);
    while(R>q.R) sub(arr[R--]);
    while(L<q.L) sub(arr[L++]);</pre>
    ans[q.id]=cur_ans;
}
```

9.2 Mo's Alogrithm On Tree

```
const int MAXN=40005;
vector<int> G[MAXN];//1-base
int n,B,arr[MAXN],ans[100005],cur_ans;
int in[MAXN],out[MAXN],dfn[MAXN*2],dft;
int deep[MAXN],sp[__lg(MAXN*2)+1][MAXN*2],bln[MAXN],spt
bitset<MAXN> inset;
struct QUERY{
  int L,R,Lid,id,lca;
  QUERY(int 1, int r, int _id):L(1),R(r),lca(0),id(_id){}
  bool operator<(const QUERY &b){</pre>
    if(Lid!=b.Lid) return Lid<b.Lid;</pre>
    return R<b.R;
  }
};
vector<QUERY> query;
void dfs(int u,int f,int d){
  deep[u]=d,sp[0][spt]=u,bln[u]=spt++;
  dfn[dft]=u,in[u]=dft++;
  for(int v:G[u])
    if(v!=f)
      dfs(v,u,d+1),sp[0][spt]=u,bln[u]=spt++;
  dfn[dft]=u,out[u]=dft++;
int lca(int u,int v){
  if(bln[u]>bln[v]) swap(u,v);
  int t=__lg(bln[v]-bln[u]+1);
  int a=sp[t][bln[u]],b=sp[t][bln[v]-(1<<t)+1];</pre>
  if(deep[a]<deep[b]) return a;</pre>
  return b;
}
void sub(int x){}
void add(int x){}
void flip(int x){
  if(inset[x]) sub(arr[x]);
  else add(arr[x]);
  inset[x]=~inset[x];
void solve(){
  B=sqrt(2*n),dft=spt=cur_ans=0,dfs(1,1,0);
  for(int i=1,x=2;x<2*n;++i,x<<=1)</pre>
    for(int j=0;j+x<=2*n;++j)</pre>
```

```
if(deep[sp[i-1][j]]<deep[sp[i-1][j+x/2]])</pre>
         sp[i][j]=sp[i-1][j];
       else sp[i][j]=sp[i-1][j+x/2];
  for(auto &q:query){
    int c=lca(q.L,q.R);
    if(c==q.L||c==q.R)
       q.L=out[c==q.L?q.R:q.L],q.R=out[c];
     else if(out[q.L]<in[q.R])</pre>
      q.lca=c,q.L=out[q.L],q.R=in[q.R];
    else q.lca=c,c=in[q.L],q.L=out[q.R],q.R=c;
    q.Lid=q.L/B;
  sort(ALL(query));
  int L=0,R=-1;
  for(auto q:query){
    while(R<q.R) flip(dfn[++R]);</pre>
    while(L>q.L) flip(dfn[--L]);
while(R>q.R) flip(dfn[R--]);
    while(L<q.L) flip(dfn[L++]);</pre>
    if(q.lca) add(arr[q.lca]);
    ans[q.id]=cur_ans;
    if(q.lca) sub(arr[q.lca]);
}
```

9.3 DynamicConvexTrick*

```
// only works for integer coordinates!!
struct Line {
    mutable 11 a, b, p;
    bool operator<(const Line &rhs) const { return a <</pre>
         rhs.a; }
     bool operator<(ll x) const { return p < x; }</pre>
struct DynamicHull : multiset<Line, less<>>> {
    static const ll kInf = 1e18;
    ll Div(ll a, ll b) { return a / b - ((a ^ b) < 0 &&
          a % b); }
     bool isect(iterator x, iterator y) {
         if (y == end()) \{ x \rightarrow p = kInf; return 0; \}
         if (x -> a == y -> a) x -> p = x -> b > y -> b
             ? kInf : -kInf;
         else x -> p = Div(y -> b - x -> b, x -> a - y
             -> a);
         return x \rightarrow p >= y \rightarrow p;
     void addline(ll a, ll b) {
         auto z = insert({a, b, 0}), y = z++, x = y;
         while (isect(y, z)) z = erase(z);
         if (x != begin() \&\& isect(--x, y)) isect(x, y =
              erase(y));
         while ((y = x) != begin() && (--x) -> p >= y ->
              p) isect(x, erase(y));
     11 query(11 x) {
         auto 1 = *lower_bound(x);
         return 1.a * x + 1.b;
    }
|};
```

9.4 DLX*

}

```
}
void restore(int c) {
  for (int i = up[c]; i != c; i = up[i]) {
    if (Exact) {
      for (int j = lt[i]; j != i; j = lt[j])
        ++s[cl[j]], up[dn[j]] = j, dn[up[j]] = j;
      lt[rg[i]] = rg[lt[i]] = i;
  if (Exact) lt[rg[c]] = c, rg[lt[c]] = c;
void init(int c) {
  columns = c;
  for (int i = 0; i < c; ++i) {
    up[i] = dn[i] = bt[i] = i;
    lt[i] = i == 0 ? c : i - 1;
    rg[i] = i == c - 1 ? c : i + 1;
    s[i] = 0;
 rg[c] = 0, lt[c] = c - 1;
  up[c] = dn[c] = -1;
 head = c, sz = c + 1;
void insert(int r, const vector<int> &col) {
  if (col.empty()) return;
  int f = sz;
  for (int i = 0; i < (int)col.size(); ++i) {</pre>
    int c = col[i], v = sz++;
    dn[bt[c]] = v;
    up[v] = bt[c], bt[c] = v;
    rg[v] = (i + 1 == (int)col.size() ? f : v + 1);
    rw[v] = r, cl[v] = c;
    ++s[c];
    if (i > 0) lt[v] = v - 1;
  lt[f] = sz - 1;
int h() {
 int ret = 0;
  memset(vis, 0, sizeof(bool) * sz);
  for (int x = rg[head]; x != head; x = rg[x]) {
    if (vis[x]) continue;
    vis[x] = true, ++ret;
    for (int i = dn[x]; i != x; i = dn[i]) {
      for (int j = rg[i]; j != i; j = rg[j])
        vis[cl[j]] = true;
   }
  }
  return ret;
void dfs(int dep) {
  if (dep + (Exact ? 0 : h()) >= ans) return;
  if (rg[head] == head) return ans = dep, void();
  if (dn[rg[head]] == rg[head]) return;
  int c = rg[head];
  int w = c;
  for (int x = c; x != head; x = rg[x]) if (s[x] < s[
      \dot{w}]) w = x;
  if (Exact) {
    remove(w);
    for (int i = dn[w]; i != w; i = dn[i]) {
      for (int j = rg[i]; j != i; j = rg[j]) remove(
          cl[j]);
      dfs(dep + 1);
      for (int j = lt[i]; j != i; j = lt[j]) restore(
          cl[i]);
    restore(w);
  } else {
    for (int i = dn[w]; i != w; i = dn[i]) {
      remove(i);
      for (int j = rg[i]; j != i; j = rg[j]) remove(j
      dfs(dep + 1);
      for (int j = lt[i]; j != i; j = lt[j]) restore(
          j);
      restore(i);
    }
 }
```

```
int solve() {
   for (int i = 0; i < columns; ++i)
     dn[bt[i]] = i, up[i] = bt[i];
   ans = 1e9, dfs(0);
   return ans;
}
};</pre>
```