## **FullyConnectedNets**

2021年5月14日

#### 1 全连接神经网络

在前面的作业中,你在 CIFAR-10 上实现了一个两层的全连接神经网络。那个实现很简单,但不是很模块化,因为损失和梯度计算在一个函数内。对于一个简单的两层网络来说,还可以人为处理,但是当我们使用更大的模型时,人工处理损失和梯度就变得不切实际了。理想情况下,我们希望使用更加模块化的设计来构建网络,这样我们就可以独立地实现不同类型的层,然后将它们整合到不同架构的模型中。

在本练习中,我们将使用更模块化的方法实现全连接网络。对于每一层,我们将实现一个 forward 和一个 backward 的函数。forward 函数将接收输入、权重和其他参数,并返回一个输出和一个 cache 对象,存储反向传播所需的数据,如下所示:

```
def layer_forward(x, w):
```

```
""" Receive inputs x and weights w """
# Do some computations ...
z = wx# ... some intermediate value
# Do some more computations ...
out = z# the output

cache = (x, w, z, out) # Values we need to compute gradients
return out, cache
```

反向传播将接收上游的梯度和 cache 对象,并返回相对于输入和权重的梯度:

```
def layer_backward(dout, cache):
```

11 11 11

Receive dout (derivative of loss with respect to outputs) and cache, and compute derivative with respect to inputs.

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```
# Unpack cache values
x, w, z, out = cache

# Use values in cache to compute derivatives
dx = dout.dot(w.T).reshape(x.shape)# Derivative of loss with respect to x
dw = x.reshape(x.shape[0], np.prod(x.shape[1:])).T.dot(dout)# Derivative of loss with respect to the respect
```

以这种方式实现了一些层之后,我们能够轻松地将它们组合起来,以构建不同架构的分类器。

除了实现任意深度的全连接网络外,我们还将探索不同的优化更新规则,并引入 Dropout 作为正则化器和 Batch/Layer 归一化工具来更有效地优化网络。

```
[]: !ls
```

daseCV drive sample\_data

```
[4]: # As usual, a bit of setup
     from __future__ import print_function
     import time
     import numpy as np
     import matplotlib.pyplot as plt
     from daseCV.classifiers.fc_net import *
     from daseCV.data_utils import get_CIFAR10_data
     from daseCV.gradient_check import eval_numerical_gradient,_
     →eval_numerical_gradient_array
     from daseCV.solver import Solver
     %matplotlib inline
     plt.rcParams['figure.figsize'] = (10.0, 8.0) # set default size of plots
     plt.rcParams['image.interpolation'] = 'nearest'
     plt.rcParams['image.cmap'] = 'gray'
     # for auto-reloading external modules
     # see http://stackoverflow.com/questions/1907993/
      \rightarrow autoreload-of-modules-in-ipython
```

2 仿射层: 前向传播 3

```
# when changing other linked py files, this ipynb will auto-reload immediately
%load_ext autoreload
%autoreload 2

def rel_error(x, y):
    """ returns relative error """
    return np.max(np.abs(x - y) / (np.maximum(1e-8, np.abs(x) + np.abs(y))))
```

('y\_test: ', (1000,))

('y\_val: ', (1000,))

('X\_test: ', (1000, 3, 32, 32))

# 2 仿射层: 前向传播

打开 daseCV/layers.py 并实现 affine\_forward 函数。

当你完成上述函数后,你可以用下面的代码测试你的实现正确与否

```
[]: # Test the affine_forward function

num_inputs = 2
input_shape = (4, 5, 6) #120
output_dim = 3
#(2*120)(120*3)+(3*1)
input_size = num_inputs * np.prod(input_shape)
weight_size = output_dim * np.prod(input_shape)

x = np.linspace(-0.1, 0.5, num=input_size).reshape(num_inputs, *input_shape)
```

2 仿射层: 前向传播 4

```
w = np.linspace(-0.2, 0.3, num=weight_size).reshape(np.prod(input_shape),_
     →output_dim)
    b = np.linspace(-0.3, 0.1, num=output_dim)
    out, _ = affine_forward(x, w, b)
    correct_out = np.array([[ 1.49834967, 1.70660132, 1.91485297],
                             [ 3.25553199, 3.5141327, 3.77273342]])
    # Compare your output with ours. The error should be around e-9 or less.
    print('Testing affine_forward function:')
    print('difference: ', rel_error(out, correct_out))
    Testing affine_forward function:
    difference: 9.769849468192957e-10
[]: x.shape[1:]
[]: (4, 5, 6)
[]: list(x.shape)[1:]
[]: [4, 5, 6]
[]: np.ones([6,3,2,1]).shape[0]
[]: 6
[]: np.ones([2,3]).dot(np.ones([3,1]))
[]: array([[3.],
            [3.]])
[]: np.ones([3,2])+np.ones([2,])
[]: array([[2., 2.],
            [2., 2.],
            [2., 2.]])
```

3 仿射层: 反向传播 5

### 3 仿射层: 反向传播

实现 affine\_backwards 函数,并使用数值梯度检查测试你的实现。

```
[51]: # Test the affine backward function
      np.random.seed(231)
      x = np.random.randn(10, 2, 3) #N*D
      w = np.random.randn(6, 5) #D*M
      b = np.random.randn(5)#M*
      dout = np.random.randn(10, 5) #N*M
      During the backward pass through the linear layer, we assume that \Box
       \hookrightarrow the derivative L Y
      has already been computed. For example if the linear layer ispart \sqcup
       \hookrightarrow of a linear classifier,
        then the matrixY gives class scores; these scoresare fed to a loss ...
       \hookrightarrow function
        (such as the softmax or multiclass SVM loss) which computes the scalar {}_{\sqcup}
       {\scriptstyle \hookrightarrow \, lossLand \quad derivative \, L \, \, Y}
        of the loss with respect to thescores.
       111
      dx_num = eval_numerical_gradient_array(lambda x: affine_forward(x, w, b)[0], x,_u
      dw_num = eval_numerical_gradient_array(lambda w: affine_forward(x, w, b)[0], w,__
       →dout)
      db num = eval numerical gradient array(lambda b: affine forward(x, w, b)[0], b, u
       →dout)
      _, cache = affine_forward(x, w, b)
      dx, dw, db = affine_backward(dout, cache)#out:dout (x,w,b):cache
      # The error should be around e-10 or less
      print('Testing affine_backward function:')
      print('dx error: ', rel_error(dx_num, dx))
      print('dw error: ', rel_error(dw_num, dw))
```

```
print('db error: ', rel_error(db_num, db))

Testing affine_backward function:
    dx error: 5.399100368651805e-11
    dw error: 9.904211865398145e-11
    db error: 2.4122867568119087e-11

[48]: x.reshape(x.shape[0], *x.shape[1:]).T.shape

[48]: (3, 2, 10)

[43]: x.shape[1:]

[43]: (2, 3)

[38]: dout.dot(w.T).shape

[38]: (10, 6)

[]: x.shape

[39]: (10, 2, 3)
```

# 4 ReLU 激活函数: 前向传播

在 relu\_forward 函数中实现 ReLU 激活函数的前向传播,并使用以下代码测试您的实现:

```
# Compare your output with ours. The error should be on the order of e-8
print('Testing relu_forward function:')
print('difference: ', rel_error(out, correct_out))
[[-0.5]]
             -0.40909091 -0.31818182 -0.22727273]
 [-0.13636364 -0.04545455 0.04545455 0.13636364]
 [ 0.22727273  0.31818182  0.40909091  0.5
ГГΟ.
             0.
                                             ]
                        0.
 ГО.
             0.
                        0.04545455 0.13636364]
 [0.22727273 0.31818182 0.40909091 0.5
Testing relu_forward function:
difference: 4.999999798022158e-08
```

# 5 ReLU 激活函数: 反向传播

在 relu\_back 函数中为 ReLU 激活函数实现反向传播,并使用数值梯度检查来测试你的实现

```
[53]: np.random.seed(231)
    x = np.random.randn(10, 10)
    dout = np.random.randn(*x.shape)

dx_num = eval_numerical_gradient_array(lambda x: relu_forward(x)[0], x, dout)

_, cache = relu_forward(x)
    dx = relu_backward(dout, cache)

# The error should be on the order of e-12
    print('Testing relu_backward function:')
    print('dx error: ', rel_error(dx_num, dx))
```

Testing relu\_backward function: dx error: 3.2756349136310288e-12 6 "三明治" 层 8

#### 5.1 Inline Question 1:

作业中只要求你实现 ReLU, 但是神经网络可以使用很多不同的激活函数, 每个都有它的优点和缺点。但是, 激活函数的一个常见问题是在反向传播时出现零 (或接近零) 梯度流。下列哪个激活函数会有这个问题? 如果在一维情况下考虑这些函数, 什么样的输入将会发生这种现象? 1. Sigmoid 2. ReLU 3. Leaky ReLU

#### 5.2 Answer:

ReLU 会在 x 是负数的时候出现 0 梯度流,而 leaky ReLU 则避免了这样死亡 RELU 的问题

## 6 "三明治" 层

在神经网络中有一些常用的层模式。例如,仿射层后面经常跟一个 ReLU 层。为了简化这些常见模式,我们在文件 daseCV/layer\_utils.py 中定义了几个常用的层

请查看 affine\_relu\_forward 和 affine\_relu\_backward 函数, 并且运行下列代码进行数值梯度 检查:

```
# Relative error should be around e-10 or less
print('Testing affine_relu_forward and affine_relu_backward:')
print('dx error: ', rel_error(dx_num, dx))
print('dw error: ', rel_error(dw_num, dw))
print('db error: ', rel_error(db_num, db))
```

Testing affine\_relu\_forward and affine\_relu\_backward:

dx error: 2.299579177309368e-11
dw error: 8.162011105764925e-11
db error: 7.826724021458994e-12

#### 7 损失层: Softmax and SVM

在上次作业中你已经实现了这些损失函数,所以这次作业就不用做了,免费送你了。当然,你仍然 应该通过查看 daseCV/layers.py 其中的实现来确保理解它们是如何工作的。

你可以通过运行以下程序来确保实现是正确的:

```
# Test softmax loss function. Loss should be close to 2.3 and dx error should
      ⇒be around e-8
      print('\nTesting softmax_loss:')
      print('loss: ', loss)
     print('dx error: ', rel_error(dx_num, dx))
     Testing svm_loss:
     loss: 8.999602749096233
     dx error: 1.4021566006651672e-09
     Testing softmax_loss:
     loss: 2.302545844500738
     dx error: 9.384673161989355e-09
 [6]: np.arange(3)
 [6]: array([0, 1, 2])
[21]: np.zeros_like(np.ones((2,3)))
[21]: array([[0., 0., 0.],
             [0., 0., 0.]])
[14]: np.ones((2,3))[[0,1],2].shape
[14]: (2,)
[17]: a=np.array([1,2,3,4,5])
      aa=a[:,np.newaxis]
     print(aa.shape)
      print (aa)
      #增加一个维度
     (5, 1)
     [[1]
      [2]
      [3]
      [4]
      [5]]
```

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#### 8 两层网络

在之前的作业中,你已经实现了一个简单的两层神经网络。现在你已经模块化地实现了一些层,你将使用这些模块重新实现两层网络。

打开文件 daseCV/classifiers/fc\_net。并完成 TwoLayerNet 类的实现。这个类将作为这个作业中其他网络的模块,所以请通读它以确保你理解了这个 API。你可以运行下面的单元来测试您的实现。

```
[32]: np.random.seed(231)
      N, D, H, C = 3, 5, 50, 7
      X = np.random.randn(N, D)
      y = np.random.randint(C, size=N)
      std = 1e-3
      model = TwoLayerNet(input_dim=D, hidden_dim=H, num_classes=C, weight_scale=std)
      print('Testing initialization ... ')
      W1_std = abs(model.params['W1'].std() - std)
      b1 = model.params['b1']
      W2_std = abs(model.params['W2'].std() - std)
      b2 = model.params['b2']
      assert W1_std < std / 10, 'First layer weights do not seem right'
      assert np.all(b1 == 0), 'First layer biases do not seem right'
      assert W2_std < std / 10, 'Second layer weights do not seem right'
      assert np.all(b2 == 0), 'Second layer biases do not seem right'
      print('Testing test-time forward pass ... ')
      model.params['W1'] = np.linspace(-0.7, 0.3, num=D*H).reshape(D, H)
      model.params['b1'] = np.linspace(-0.1, 0.9, num=H)
      model.params['W2'] = np.linspace(-0.3, 0.4, num=H*C).reshape(H, C)
      model.params['b2'] = np.linspace(-0.9, 0.1, num=C)
      X = np.linspace(-5.5, 4.5, num=N*D).reshape(D, N).T
      scores = model.loss(X)
      correct_scores = np.asarray(
        [[11.53165108, 12.2917344, 13.05181771, 13.81190102, 14.57198434, 15.
       \rightarrow 33206765, 16.09215096],
```

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```
[12.05769098, 12.74614105, 13.43459113, 14.1230412, 14.81149128, 15.
 \rightarrow49994135, 16.18839143],
   [12.58373087, 13.20054771, 13.81736455, 14.43418138, 15.05099822, 15.
 →66781506, 16.2846319 ]])
scores_diff = np.abs(scores - correct_scores).sum()
assert scores_diff < 1e-6, 'Problem with test-time forward pass'
print('Testing training loss (no regularization)')
y = np.asarray([0, 5, 1])
loss, grads = model.loss(X, y)
correct_loss = 3.4702243556
assert abs(loss - correct_loss) < 1e-10, 'Problem with training-time loss'</pre>
model.reg = 1.0
loss, grads = model.loss(X, y)
correct_loss = 26.5948426952
assert abs(loss - correct_loss) < 1e-10, 'Problem with regularization loss'
# Errors should be around e-7 or less
for reg in [0.0, 0.7]:
  print('Running numeric gradient check with reg = ', reg)
  model.reg = reg
  loss, grads = model.loss(X, y)
  for name in sorted(grads):
    f = lambda _: model.loss(X, y)[0]
    grad_num = eval_numerical_gradient(f, model.params[name], verbose=False)
    print('%s relative error: %.2e' % (name, rel_error(grad_num, grads[name])))
Testing initialization ...
Testing test-time forward pass ...
Testing training loss (no regularization)
Running numeric gradient check with reg = 0.0
W1 relative error: 1.83e-08
W2 relative error: 3.12e-10
b1 relative error: 9.83e-09
```

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```
b2 relative error: 4.33e-10

Running numeric gradient check with reg = 0.7

W1 relative error: 2.53e-07

W2 relative error: 2.85e-08

b1 relative error: 1.56e-08

b2 relative error: 7.76e-10
```

#### 9 Solver

在之前的作业中,模型的训练逻辑与模型本身是耦合的。在这次作业中,按照更加模块化的设计, 我们将模型的训练逻辑划分为单独的类。

打开文件 daseCV/solver, 通读一遍以熟悉 API。然后使用一个 Sovler 实例来训练一个 TwoLayerNet, 它可以在验证集上达到至少 50% 的精度。

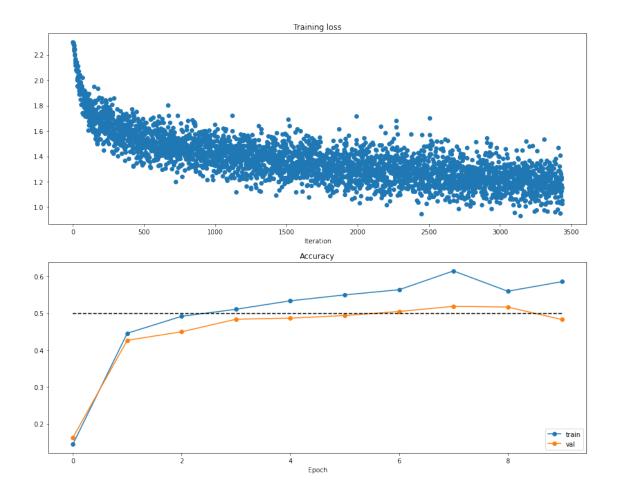
```
[36]: model = TwoLayerNet()
   #solver = None
   # TODO: Use a Solver instance to train a TwoLayerNet that achieves at least #
   # 50% accuracy on the validation set.
   # *****START OF YOUR CODE (DO NOT DELETE/MODIFY THIS LINE)****
   solver = Solver(model, data,
             update_rule='sgd',
             lr_decay=0.98,
             batch_size=128,
             print_every=100,
             optim_config={'learning_rate': 1e-3},
             num_epochs = 9)
   solver.train()
   # *****END OF YOUR CODE (DO NOT DELETE/MODIFY THIS LINE)****
   END OF YOUR CODE
```

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```
(Iteration 1 / 3438) loss: 2.299875
(Epoch 0 / 9) train acc: 0.145000; val_acc: 0.163000
(Iteration 101 / 3438) loss: 1.746332
(Iteration 201 / 3438) loss: 1.733316
(Iteration 301 / 3438) loss: 1.580383
(Epoch 1 / 9) train acc: 0.446000; val acc: 0.427000
(Iteration 401 / 3438) loss: 1.499206
(Iteration 501 / 3438) loss: 1.479629
(Iteration 601 / 3438) loss: 1.460441
(Iteration 701 / 3438) loss: 1.359739
(Epoch 2 / 9) train acc: 0.492000; val_acc: 0.450000
(Iteration 801 / 3438) loss: 1.611551
(Iteration 901 / 3438) loss: 1.440300
(Iteration 1001 / 3438) loss: 1.324513
(Iteration 1101 / 3438) loss: 1.522455
(Epoch 3 / 9) train acc: 0.511000; val_acc: 0.484000
(Iteration 1201 / 3438) loss: 1.538411
(Iteration 1301 / 3438) loss: 1.293379
(Iteration 1401 / 3438) loss: 1.539784
(Iteration 1501 / 3438) loss: 1.230064
(Epoch 4 / 9) train acc: 0.534000; val_acc: 0.487000
(Iteration 1601 / 3438) loss: 1.599137
(Iteration 1701 / 3438) loss: 1.325792
(Iteration 1801 / 3438) loss: 1.435145
(Iteration 1901 / 3438) loss: 1.390626
(Epoch 5 / 9) train acc: 0.550000; val_acc: 0.494000
(Iteration 2001 / 3438) loss: 1.204316
(Iteration 2101 / 3438) loss: 1.253460
(Iteration 2201 / 3438) loss: 1.327926
(Epoch 6 / 9) train acc: 0.564000; val_acc: 0.505000
(Iteration 2301 / 3438) loss: 1.097801
(Iteration 2401 / 3438) loss: 1.226286
(Iteration 2501 / 3438) loss: 1.119927
(Iteration 2601 / 3438) loss: 1.269149
(Epoch 7 / 9) train acc: 0.615000; val_acc: 0.519000
(Iteration 2701 / 3438) loss: 1.355638
(Iteration 2801 / 3438) loss: 1.301551
```

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```
(Iteration 2901 / 3438) loss: 1.326050
     (Iteration 3001 / 3438) loss: 1.310682
     (Epoch 8 / 9) train acc: 0.560000; val_acc: 0.517000
     (Iteration 3101 / 3438) loss: 1.181888
     (Iteration 3201 / 3438) loss: 1.113038
     (Iteration 3301 / 3438) loss: 1.277730
     (Iteration 3401 / 3438) loss: 1.230148
     (Epoch 9 / 9) train acc: 0.586000; val_acc: 0.483000
[37]: # Run this cell to visualize training loss and train / val accuracy
      plt.subplot(2, 1, 1)
      plt.title('Training loss')
      plt.plot(solver.loss_history, 'o')
      plt.xlabel('Iteration')
      plt.subplot(2, 1, 2)
      plt.title('Accuracy')
      plt.plot(solver.train_acc_history, '-o', label='train')
      plt.plot(solver.val_acc_history, '-o', label='val')
      plt.plot([0.5] * len(solver.val_acc_history), 'k--')
      plt.xlabel('Epoch')
      plt.legend(loc='lower right')
      plt.gcf().set_size_inches(15, 12)
      plt.show()
```



## 10 多层网络

接下来,请实现一个带有任意数量的隐层的全连接网络。

阅读 daseCV/classifiers/fc\_net.py 中的 FullyConnectedNet 类。

实现初始化、前向传播和反向传播的函数,暂时不要考虑实现 dropout 或 batch/layer normalization,我们将在后面添加上去。

## 10.1 初始化 loss 和梯度检查

刚开始要做完整性检查,运行以下代码来检查初始 loss,并对有正则化和无正则化的网络进行梯度检查。请问初始的 loss 合理吗?

在梯度检查中, 你应该期望得到 1e-7 或更少的 errors。

```
[41]: np.random.seed(231)
      N, D, H1, H2, C = 2, 15, 20, 30, 10
      X = np.random.randn(N, D)
      y = np.random.randint(C, size=(N,))
      for reg in [0, 3.14]:
        print('Running check with reg = ', reg)
        model = FullyConnectedNet([H1, H2], input dim=D, num classes=C,
                                  reg=reg, weight_scale=5e-2, dtype=np.float64)
        loss, grads = model.loss(X, y)
        print('Initial loss: ', loss)
        # Most of the errors should be on the order of e-7 or smaller.
        # NOTE: It is fine however to see an error for W2 on the order of e-5
        # for the check when reg = 0.0
        for name in sorted(grads):
          f = lambda _: model.loss(X, y)[0]
          grad_num = eval_numerical_gradient(f, model.params[name], verbose=False,_u
       \rightarrowh=1e-5)
          print('%s relative error: %.2e' % (name, rel_error(grad_num, grads[name])))
```

Initial loss: 2.3004790897684924
W1 relative error: 1.48e-07
W2 relative error: 2.21e-05
W3 relative error: 3.53e-07
b1 relative error: 5.38e-09
b2 relative error: 2.09e-09
b3 relative error: 5.80e-11
Running check with reg = 3.14
Initial loss: 7.052114776533016
W1 relative error: 7.36e-09
W2 relative error: 6.87e-08
W3 relative error: 3.48e-08

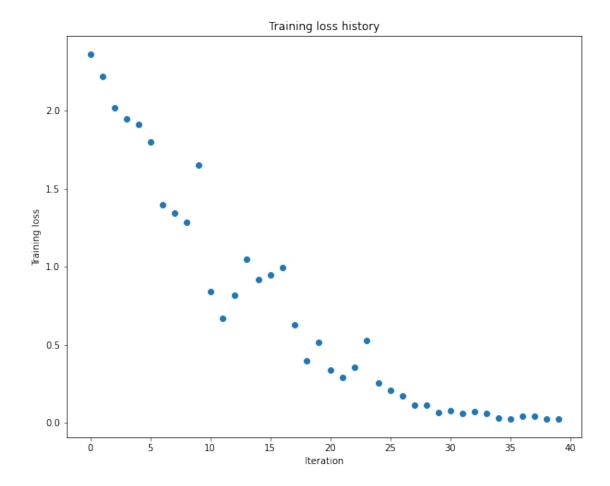
Running check with reg = 0

```
b1 relative error: 1.48e-08
b2 relative error: 1.72e-09
b3 relative error: 1.80e-10
```

实现另一个完整性检查,请确保你可以过拟合 50 个图像的小数据集。首先,我们将尝试一个三层网络,每个隐藏层有 100 个单元。在接下来的代码中,调整 learning rate 和 weight initialization scale 以达到过拟合,在 20 epoch 内达到 100% 的训练精度。

```
[42]: # TODO: Use a three-layer Net to overfit 50 training examples by
      # tweaking just the learning rate and initialization scale.
      num_train = 50
      small data = {
        'X_train': data['X_train'][:num_train],
        'y_train': data['y_train'][:num_train],
        'X_val': data['X_val'],
        'y_val': data['y_val'],
      }
      weight_scale = 1e-2  # Experiment with this!
      learning_rate = 1e-2 # Experiment with this!
      model = FullyConnectedNet([100, 100],
                    weight_scale=weight_scale, dtype=np.float64)
      solver = Solver(model, small_data,
                      print_every=10, num_epochs=20, batch_size=25,
                      update_rule='sgd',
                      optim_config={
                        'learning_rate': learning_rate,
                      }
      solver.train()
      plt.plot(solver.loss_history, 'o')
      plt.title('Training loss history')
      plt.xlabel('Iteration')
      plt.ylabel('Training loss')
      plt.show()
```

```
(Iteration 1 / 40) loss: 2.363364
(Epoch 0 / 20) train acc: 0.180000; val_acc: 0.108000
(Epoch 1 / 20) train acc: 0.320000; val_acc: 0.127000
(Epoch 2 / 20) train acc: 0.440000; val_acc: 0.172000
(Epoch 3 / 20) train acc: 0.500000; val_acc: 0.184000
(Epoch 4 / 20) train acc: 0.540000; val_acc: 0.181000
(Epoch 5 / 20) train acc: 0.740000; val_acc: 0.190000
(Iteration 11 / 40) loss: 0.839976
(Epoch 6 / 20) train acc: 0.740000; val_acc: 0.187000
(Epoch 7 / 20) train acc: 0.740000; val_acc: 0.183000
(Epoch 8 / 20) train acc: 0.820000; val_acc: 0.177000
(Epoch 9 / 20) train acc: 0.860000; val_acc: 0.200000
(Epoch 10 / 20) train acc: 0.920000; val_acc: 0.191000
(Iteration 21 / 40) loss: 0.337174
(Epoch 11 / 20) train acc: 0.960000; val_acc: 0.189000
(Epoch 12 / 20) train acc: 0.940000; val_acc: 0.180000
(Epoch 13 / 20) train acc: 1.000000; val_acc: 0.199000
(Epoch 14 / 20) train acc: 1.000000; val_acc: 0.199000
(Epoch 15 / 20) train acc: 1.000000; val_acc: 0.195000
(Iteration 31 / 40) loss: 0.075911
(Epoch 16 / 20) train acc: 1.000000; val_acc: 0.182000
(Epoch 17 / 20) train acc: 1.000000; val_acc: 0.201000
(Epoch 18 / 20) train acc: 1.000000; val_acc: 0.207000
(Epoch 19 / 20) train acc: 1.000000; val_acc: 0.185000
(Epoch 20 / 20) train acc: 1.000000; val_acc: 0.192000
```



现在尝试使用一个五层的网络,每层 100 个单元,对 50 张图片进行训练。同样,你将调整 learning rate 和 weight initialization scale 比例,你应该能够在 20 个 epoch 内实现 100% 的训练精度。

```
[43]: # TODO: Use a five-layer Net to overfit 50 training examples by
# tweaking just the learning rate and initialization scale.

num_train = 50
small_data = {
    'X_train': data['X_train'][:num_train],
    'y_train': data['y_train'][:num_train],
    'X_val': data['X_val'],
    'y_val': data['y_val'],
}
```

```
weight scale = 1e-1 # Experiment with this!
learning_rate = 2e-3 # Experiment with this!
model = FullyConnectedNet([100, 100, 100, 100],
                weight_scale=weight_scale, dtype=np.float64)
solver = Solver(model, small_data,
                print_every=10, num_epochs=20, batch_size=25,
                update_rule='sgd',
                optim_config={
                  'learning_rate': learning_rate,
                }
         )
solver.train()
plt.plot(solver.loss_history, 'o')
plt.title('Training loss history')
plt.xlabel('Iteration')
plt.ylabel('Training loss')
plt.show()
```

```
(Iteration 1 / 40) loss: 166.501707
(Epoch 0 / 20) train acc: 0.100000; val_acc: 0.107000
(Epoch 1 / 20) train acc: 0.320000; val_acc: 0.101000
(Epoch 2 / 20) train acc: 0.160000; val_acc: 0.122000
(Epoch 3 / 20) train acc: 0.380000; val_acc: 0.106000
(Epoch 4 / 20) train acc: 0.520000; val_acc: 0.111000
(Epoch 5 / 20) train acc: 0.760000; val_acc: 0.113000
(Iteration 11 / 40) loss: 3.343141
(Epoch 6 / 20) train acc: 0.840000; val_acc: 0.122000
(Epoch 7 / 20) train acc: 0.920000; val_acc: 0.113000
(Epoch 8 / 20) train acc: 0.940000; val_acc: 0.125000
(Epoch 9 / 20) train acc: 0.960000; val_acc: 0.125000
(Epoch 10 / 20) train acc: 0.980000; val_acc: 0.121000
(Iteration 21 / 40) loss: 0.039138
(Epoch 11 / 20) train acc: 0.980000; val_acc: 0.123000
(Epoch 12 / 20) train acc: 1.000000; val_acc: 0.121000
(Epoch 13 / 20) train acc: 1.000000; val_acc: 0.121000
```

```
(Epoch 14 / 20) train acc: 1.000000; val_acc: 0.121000 (Epoch 15 / 20) train acc: 1.000000; val_acc: 0.121000 (Iteration 31 / 40) loss: 0.000644 (Epoch 16 / 20) train acc: 1.000000; val_acc: 0.121000 (Epoch 17 / 20) train acc: 1.000000; val_acc: 0.121000 (Epoch 18 / 20) train acc: 1.000000; val_acc: 0.121000 (Epoch 19 / 20) train acc: 1.000000; val_acc: 0.121000 (Epoch 20 / 20) train acc: 1.000000; val_acc: 0.121000
```

# 

**Inline Question 2:** 你注意到训练三层网和训练五层网难度的区别了吗?根据你的经验,哪个网络对 initalization scale 更敏感?为什么会这样呢?

Iteration

11 更新规则 23

#### 10.2 Answer:

五层网,初始网络规模更大时,为了学到更多特征,学习会变得更复杂困难,所以网络越深,对更大的网络规模会更敏感。

#### 11 更新规则

到目前为止,我们使用了普通的随机梯度下降法 (SGD) 作为我们的更新规则。更复杂的更新规则可以更容易地训练深度网络。我们将实现一些最常用的更新规则,并将它们与普通的 SGD 进行比较。

#### 12 SGD+Momentum

带动量的随机梯度下降法是一种广泛使用的更新规则,它使深度网络的收敛速度快于普通的随机梯度下降法。更多信息参见 http://cs231n.github.io/neural-networks-3/#sgd 动量更新部分。

打开文件 daseCV/optim, 并阅读该文件顶部的文档, 以确保你理解了该 API。在函数 sgd\_momentum 中实现 SGD+ 动量更新规则, 并运行以下代码检查你的实现。你会看到 errors 小于 e-8。

next\_w error: 8.882347033505819e-09 velocity error: 4.269287743278663e-09

当你完成了上面的步骤,运行以下代码来训练一个具有 SGD 和 SGD+momentum 的六层网络。你应该看到 SGD+momentum 更新规则收敛得更快。

```
[46]: num_train = 4000
      small data = {
        'X_train': data['X_train'][:num_train],
        'y_train': data['y_train'][:num_train],
       'X_val': data['X_val'],
        'y_val': data['y_val'],
      }
      solvers = {}
      for update_rule in ['sgd', 'sgd_momentum']:
        print('running with ', update_rule)
        model = FullyConnectedNet([100, 100, 100, 100, 100], weight_scale=5e-2)
        solver = Solver(model, small_data,
                        num_epochs=5, batch_size=100,
                        update_rule=update_rule,
                        optim_config={
                          'learning_rate': 5e-3,
                        },
                        verbose=True)
        solvers[update_rule] = solver
```

(Iteration 21 / 200) loss: 2.214091

```
solver.train()
  print()
plt.subplot(3, 1, 1)
plt.title('Training loss')
plt.xlabel('Iteration')
plt.subplot(3, 1, 2)
plt.title('Training accuracy')
plt.xlabel('Epoch')
plt.subplot(3, 1, 3)
plt.title('Validation accuracy')
plt.xlabel('Epoch')
for update_rule, solver in solvers.items():
  plt.subplot(3, 1, 1)
  plt.plot(solver.loss_history, 'o', label="loss_%s" % update_rule)
  plt.subplot(3, 1, 2)
  plt.plot(solver.train_acc_history, '-o', label="train_acc_%s" % update_rule)
  plt.subplot(3, 1, 3)
  plt.plot(solver.val_acc_history, '-o', label="val_acc_%s" % update_rule)
for i in [1, 2, 3]:
  plt.subplot(3, 1, i)
  plt.legend(loc='upper center', ncol=4)
plt.gcf().set_size_inches(15, 15)
plt.show()
running with sgd
(Iteration 1 / 200) loss: 2.559978
(Epoch 0 / 5) train acc: 0.104000; val_acc: 0.107000
(Iteration 11 / 200) loss: 2.356069
```

```
(Iteration 31 / 200) loss: 2.205928
(Epoch 1 / 5) train acc: 0.225000; val_acc: 0.193000
(Iteration 41 / 200) loss: 2.132095
(Iteration 51 / 200) loss: 2.118950
(Iteration 61 / 200) loss: 2.116443
(Iteration 71 / 200) loss: 2.132549
(Epoch 2 / 5) train acc: 0.298000; val_acc: 0.260000
(Iteration 81 / 200) loss: 1.977227
(Iteration 91 / 200) loss: 2.007528
(Iteration 101 / 200) loss: 2.004762
(Iteration 111 / 200) loss: 1.885342
(Epoch 3 / 5) train acc: 0.343000; val_acc: 0.287000
(Iteration 121 / 200) loss: 1.891517
(Iteration 131 / 200) loss: 1.923677
(Iteration 141 / 200) loss: 1.957743
(Iteration 151 / 200) loss: 1.966736
(Epoch 4 / 5) train acc: 0.322000; val_acc: 0.305000
(Iteration 161 / 200) loss: 1.801483
(Iteration 171 / 200) loss: 1.973780
(Iteration 181 / 200) loss: 1.666572
(Iteration 191 / 200) loss: 1.909494
(Epoch 5 / 5) train acc: 0.372000; val_acc: 0.319000
running with sgd_momentum
(Iteration 1 / 200) loss: 3.153778
(Epoch 0 / 5) train acc: 0.099000; val_acc: 0.088000
(Iteration 11 / 200) loss: 2.227203
(Iteration 21 / 200) loss: 2.125706
(Iteration 31 / 200) loss: 1.932695
(Epoch 1 / 5) train acc: 0.307000; val_acc: 0.260000
(Iteration 41 / 200) loss: 1.946488
(Iteration 51 / 200) loss: 1.778584
(Iteration 61 / 200) loss: 1.758119
(Iteration 71 / 200) loss: 1.849137
(Epoch 2 / 5) train acc: 0.382000; val_acc: 0.322000
(Iteration 81 / 200) loss: 2.048671
(Iteration 91 / 200) loss: 1.693223
```

(Iteration 101 / 200) loss: 1.511693 (Iteration 111 / 200) loss: 1.390754 (Epoch 3 / 5) train acc: 0.458000; val\_acc: 0.338000 (Iteration 121 / 200) loss: 1.670614 (Iteration 131 / 200) loss: 1.540271 (Iteration 141 / 200) loss: 1.597365 (Iteration 151 / 200) loss: 1.609851 (Epoch 4 / 5) train acc: 0.490000; val\_acc: 0.327000 (Iteration 161 / 200) loss: 1.472687 (Iteration 171 / 200) loss: 1.378620 (Iteration 181 / 200) loss: 1.378175 (Iteration 191 / 200) loss: 1.306439 (Epoch 5 / 5) train acc: 0.529000; val\_acc: 0.369000

/usr/local/lib/python3.7/dist-packages/ipykernel\_launcher.py:39:

MatplotlibDeprecationWarning: Adding an axes using the same arguments as a previous axes currently reuses the earlier instance. In a future version, a new instance will always be created and returned. Meanwhile, this warning can be suppressed, and the future behavior ensured, by passing a unique label to each axes instance.

/usr/local/lib/python3.7/dist-packages/ipykernel\_launcher.py:42:

MatplotlibDeprecationWarning: Adding an axes using the same arguments as a previous axes currently reuses the earlier instance. In a future version, a new instance will always be created and returned. Meanwhile, this warning can be suppressed, and the future behavior ensured, by passing a unique label to each axes instance.

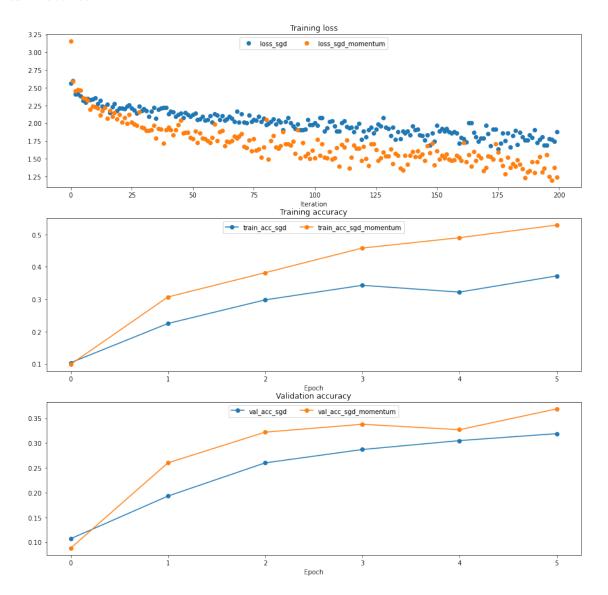
/usr/local/lib/python3.7/dist-packages/ipykernel\_launcher.py:45:

MatplotlibDeprecationWarning: Adding an axes using the same arguments as a previous axes currently reuses the earlier instance. In a future version, a new instance will always be created and returned. Meanwhile, this warning can be suppressed, and the future behavior ensured, by passing a unique label to each axes instance.

/usr/local/lib/python3.7/dist-packages/ipykernel\_launcher.py:49:

MatplotlibDeprecationWarning: Adding an axes using the same arguments as a previous axes currently reuses the earlier instance. In a future version, a new instance will always be created and returned. Meanwhile, this warning can be

suppressed, and the future behavior ensured, by passing a unique label to each axes instance.



# 13 RMSProp and Adam

RMSProp [1] 和 Adam [2] 是另外两个更新规则,它们通过使用梯度的二阶矩平均值来设置每个参数的学习速率。

在文件 daseCV/optim 中实现 RMSProp 函数和 Adam 函数,并使用下面的代码来检查您的实现。

- [1] Tijmen Tieleman and Geoffrey Hinton. "Lecture 6.5-rmsprop: Divide the gradient by a running average of its recent magnitude." COURSERA: Neural Networks for Machine Learning 4 (2012).
- [2] Diederik Kingma and Jimmy Ba, "Adam: A Method for Stochastic Optimization", ICLR 2015.

```
[48]: # Test RMSProp implementation
     from daseCV.optim import rmsprop
     N, D = 4, 5
     w = np.linspace(-0.4, 0.6, num=N*D).reshape(N, D)
     dw = np.linspace(-0.6, 0.4, num=N*D).reshape(N, D)
     cache = np.linspace(0.6, 0.9, num=N*D).reshape(N, D)
     config = {'learning_rate': 1e-2, 'cache': cache}
     next_w, _ = rmsprop(w, dw, config=config)
     expected_next_w = np.asarray([
       [-0.39223849, -0.34037513, -0.28849239, -0.23659121, -0.18467247],
       [-0.132737, -0.08078555, -0.02881884, 0.02316247, 0.07515774],
       [ 0.12716641, 0.17918792, 0.23122175, 0.28326742, 0.33532447],
       [ 0.38739248, 0.43947102, 0.49155973, 0.54365823, 0.59576619]])
     expected_cache = np.asarray([
       [0.67329252, 0.68859723, 0.70395734, 0.71937285, 0.73484377],
       [ 0.75037008, 0.7659518, 0.78158892, 0.79728144, 0.81302936],
       [ 0.82883269, 0.84469141, 0.86060554, 0.87657507, 0.8926
                                                                  ]])
     # You should see relative errors around e-7 or less
     print('next_w error: ', rel_error(expected_next_w, next_w))
     print('cache error: ', rel_error(expected_cache, config['cache']))
```

next\_w error: 9.524687511038133e-08
cache error: 2.6477955807156126e-09

```
[50]: # Test Adam implementation
from daseCV.optim import adam
N, D = 4, 5
```

```
w = np.linspace(-0.4, 0.6, num=N*D).reshape(N, D)
dw = np.linspace(-0.6, 0.4, num=N*D).reshape(N, D)
m = np.linspace(0.6, 0.9, num=N*D).reshape(N, D)
v = np.linspace(0.7, 0.5, num=N*D).reshape(N, D)
config = {'learning_rate': 1e-2, 'm': m, 'v': v, 't': 5}
next_w, _ = adam(w, dw, config=config)
expected_next_w = np.asarray([
 [-0.40094747, -0.34836187, -0.29577703, -0.24319299, -0.19060977],
 [-0.1380274, -0.08544591, -0.03286534, 0.01971428, 0.0722929],
 [0.1248705, 0.17744702, 0.23002243, 0.28259667, 0.33516969],
  [ 0.38774145, 0.44031188, 0.49288093, 0.54544852, 0.59801459]])
expected_v = np.asarray([
  [0.69966, 0.68908382, 0.67851319, 0.66794809, 0.65738853,],
  [ 0.64683452, 0.63628604, 0.6257431, 0.61520571, 0.60467385,],
 [ 0.59414753, 0.58362676, 0.57311152, 0.56260183, 0.55209767,],
  [ 0.54159906, 0.53110598, 0.52061845, 0.51013645, 0.49966, ]])
expected_m = np.asarray([
  [ 0.48, 0.49947368, 0.51894737, 0.53842105, 0.55789474],
 [ 0.57736842, 0.59684211, 0.61631579, 0.63578947, 0.65526316],
 [0.67473684, 0.69421053, 0.71368421, 0.73315789, 0.75263158],
  [ 0.77210526, 0.79157895, 0.81105263, 0.83052632, 0.85 ]])
# You should see relative errors around e-7 or less
print('next_w error: ', rel_error(expected_next_w, next_w))
print('v error: ', rel_error(expected_v, config['v']))
print('m error: ', rel_error(expected_m, config['m']))
```

next\_w error: 0.20720703668629928
v error: 4.208314038113071e-09
m error: 4.214963193114416e-09

当你完成了上面 RMSProp 和 Adam 函数后,运行下面的代码训练一对网络,其中分别使用了上述 两个方法

```
[51]: learning_rates = {'rmsprop': 1e-4, 'adam': 1e-3}
      for update_rule in ['adam', 'rmsprop']:
        print('running with ', update_rule)
        model = FullyConnectedNet([100, 100, 100, 100, 100], weight_scale=5e-2)
        solver = Solver(model, small_data,
                        num_epochs=5, batch_size=100,
                        update_rule=update_rule,
                        optim_config={
                          'learning_rate': learning_rates[update_rule]
                        },
                        verbose=True)
        solvers[update_rule] = solver
        solver.train()
        print()
      plt.subplot(3, 1, 1)
      plt.title('Training loss')
      plt.xlabel('Iteration')
      plt.subplot(3, 1, 2)
      plt.title('Training accuracy')
      plt.xlabel('Epoch')
      plt.subplot(3, 1, 3)
      plt.title('Validation accuracy')
      plt.xlabel('Epoch')
      for update_rule, solver in list(solvers.items()):
       plt.subplot(3, 1, 1)
        plt.plot(solver.loss_history, 'o', label=update_rule)
        plt.subplot(3, 1, 2)
        plt.plot(solver.train_acc_history, '-o', label=update_rule)
        plt.subplot(3, 1, 3)
```

(Iteration 141 / 200) loss: 1.668342 (Iteration 151 / 200) loss: 1.719504

(Iteration 161 / 200) loss: 1.691765 (Iteration 171 / 200) loss: 1.416469 (Iteration 181 / 200) loss: 1.620160 (Iteration 191 / 200) loss: 1.578580

(Epoch 4 / 5) train acc: 0.426000; val acc: 0.358000

(Epoch 5 / 5) train acc: 0.405000; val\_acc: 0.347000

```
plt.plot(solver.val_acc_history, '-o', label=update_rule)
for i in [1, 2, 3]:
  plt.subplot(3, 1, i)
  plt.legend(loc='upper center', ncol=4)
plt.gcf().set_size_inches(15, 15)
plt.show()
running with adam
(Iteration 1 / 200) loss: 3.476928
(Epoch 0 / 5) train acc: 0.105000; val_acc: 0.100000
(Iteration 11 / 200) loss: 2.036672
(Iteration 21 / 200) loss: 2.231720
(Iteration 31 / 200) loss: 1.986361
(Epoch 1 / 5) train acc: 0.290000; val_acc: 0.234000
(Iteration 41 / 200) loss: 1.965305
(Iteration 51 / 200) loss: 1.855719
(Iteration 61 / 200) loss: 1.983865
(Iteration 71 / 200) loss: 1.688213
(Epoch 2 / 5) train acc: 0.319000; val acc: 0.295000
(Iteration 81 / 200) loss: 1.735082
(Iteration 91 / 200) loss: 1.653525
(Iteration 101 / 200) loss: 1.709237
(Iteration 111 / 200) loss: 1.905604
(Epoch 3 / 5) train acc: 0.335000; val_acc: 0.307000
(Iteration 121 / 200) loss: 1.661850
(Iteration 131 / 200) loss: 1.769786
```

```
running with rmsprop
(Iteration 1 / 200) loss: 2.589166
(Epoch 0 / 5) train acc: 0.119000; val_acc: 0.146000
(Iteration 11 / 200) loss: 2.032921
(Iteration 21 / 200) loss: 1.897278
(Iteration 31 / 200) loss: 1.770793
(Epoch 1 / 5) train acc: 0.381000; val_acc: 0.320000
(Iteration 41 / 200) loss: 1.895731
(Iteration 51 / 200) loss: 1.681091
(Iteration 61 / 200) loss: 1.487204
(Iteration 71 / 200) loss: 1.629973
(Epoch 2 / 5) train acc: 0.429000; val_acc: 0.350000
(Iteration 81 / 200) loss: 1.506686
(Iteration 91 / 200) loss: 1.610742
(Iteration 101 / 200) loss: 1.486124
(Iteration 111 / 200) loss: 1.559454
(Epoch 3 / 5) train acc: 0.492000; val_acc: 0.361000
(Iteration 121 / 200) loss: 1.497406
(Iteration 131 / 200) loss: 1.530736
(Iteration 141 / 200) loss: 1.550957
(Iteration 151 / 200) loss: 1.652046
(Epoch 4 / 5) train acc: 0.530000; val_acc: 0.361000
(Iteration 161 / 200) loss: 1.599574
(Iteration 171 / 200) loss: 1.401073
(Iteration 181 / 200) loss: 1.509365
(Iteration 191 / 200) loss: 1.365773
(Epoch 5 / 5) train acc: 0.531000; val_acc: 0.369000
```

/usr/local/lib/python3.7/dist-packages/ipykernel\_launcher.py:30:

MatplotlibDeprecationWarning: Adding an axes using the same arguments as a previous axes currently reuses the earlier instance. In a future version, a new instance will always be created and returned. Meanwhile, this warning can be suppressed, and the future behavior ensured, by passing a unique label to each axes instance.

/usr/local/lib/python3.7/dist-packages/ipykernel\_launcher.py:33:
MatplotlibDeprecationWarning: Adding an axes using the same arguments as a

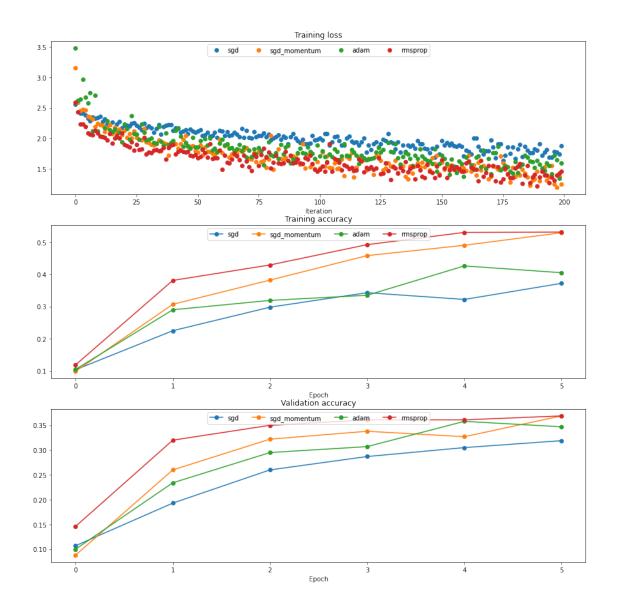
previous axes currently reuses the earlier instance. In a future version, a new instance will always be created and returned. Meanwhile, this warning can be suppressed, and the future behavior ensured, by passing a unique label to each axes instance.

/usr/local/lib/python3.7/dist-packages/ipykernel\_launcher.py:36:

MatplotlibDeprecationWarning: Adding an axes using the same arguments as a previous axes currently reuses the earlier instance. In a future version, a new instance will always be created and returned. Meanwhile, this warning can be suppressed, and the future behavior ensured, by passing a unique label to each axes instance.

/usr/local/lib/python3.7/dist-packages/ipykernel\_launcher.py:40:

MatplotlibDeprecationWarning: Adding an axes using the same arguments as a previous axes currently reuses the earlier instance. In a future version, a new instance will always be created and returned. Meanwhile, this warning can be suppressed, and the future behavior ensured, by passing a unique label to each axes instance.



#### 13.1 Inline Question 3:

AdaGrad, 类似于 Adam, 是一个 per-parameter 优化方法, 它使用以下更新规则:

```
cache += dw**2
w += - learning_rate * dw / (np.sqrt(cache) + eps)
```

当使用 AdaGrad 训练一个网络时,更新的值会变得非常小,而且他的网络学习的非常慢。利用你 对 AdaGrad 更新规则的了解,解释为什么更新的值会变得非常小? Adam 会有同样的问题吗?

#### 13.2 Answer:

根据上面的公式, adagrad 每步更新会越除越小。adam 结合了 adagrad 和动量的方法,避免了这个问题。

## 14 训练一个效果足够好的模型!

在 CIFAR-10 上尽可能训练最好的全连接模型,将最好的模型存储在 best\_model 变量中。我们要求你在验证集上获得至少 50% 的准确性。

如果你细心的话,应该是有可能得到 55% 以上精度的,但我们不苛求你达到这么高的精度。在后面的作业上,我们会要求你们在 CIFAR-10 上训练最好的卷积神经网络,我们希望你们把精力放在卷积网络上,而不是全连接网络上。

在做这部分之前完成 BatchNormalization.ipynb 和 Dropout.ipynb 可能会对你有帮助,因为这些技术可以帮助你训练强大的模型。

```
[52]: best_model = None
    # TODO: Train the best FullyConnectedNet that you can on CIFAR-10. You might
    # find batch/layer normalization and dropout useful. Store your best model in #
    # the best_model variable.
    # *****START OF YOUR CODE (DO NOT DELETE/MODIFY THIS LINE)****
    weight_scale = 4e-2
    learning_rate = 6e-4
    model = FullyConnectedNet([100, 100, 100, 100],
               weight scale=weight scale, dtype=np.float64, reg=0.001)
    solver = Solver(model, data,
                 print_every=100, num_epochs=6, batch_size=200,
                 update_rule='adam',
                 optim_config={
                   'learning_rate': learning_rate,
                 }
    solver.train()
```

15 测试你的模型! 37

```
(Epoch 0 / 6) train acc: 0.123000; val_acc: 0.132000
(Iteration 101 / 1470) loss: 1.940116
(Iteration 201 / 1470) loss: 1.814940
(Epoch 1 / 6) train acc: 0.449000; val_acc: 0.443000
(Iteration 301 / 1470) loss: 1.856808
(Iteration 401 / 1470) loss: 1.563786
(Epoch 2 / 6) train acc: 0.480000; val_acc: 0.473000
(Iteration 501 / 1470) loss: 1.600052
(Iteration 601 / 1470) loss: 1.504214
(Iteration 701 / 1470) loss: 1.457760
(Epoch 3 / 6) train acc: 0.507000; val_acc: 0.484000
(Iteration 801 / 1470) loss: 1.351943
(Iteration 901 / 1470) loss: 1.468692
(Epoch 4 / 6) train acc: 0.535000; val_acc: 0.493000
(Iteration 1001 / 1470) loss: 1.346348
(Iteration 1101 / 1470) loss: 1.329311
(Iteration 1201 / 1470) loss: 1.322137
(Epoch 5 / 6) train acc: 0.546000; val_acc: 0.495000
(Iteration 1301 / 1470) loss: 1.276124
(Iteration 1401 / 1470) loss: 1.386978
(Epoch 6 / 6) train acc: 0.583000; val_acc: 0.499000
```

## 15 测试你的模型!

在验证和测试集上运行您的最佳模型。验证集的准确率应达到50%以上。

16 重要 38

```
[53]: y_test_pred = np.argmax(best_model.loss(data['X_test']), axis=1)
    y_val_pred = np.argmax(best_model.loss(data['X_val']), axis=1)
    print('Validation set accuracy: ', (y_val_pred == data['y_val']).mean())
    print('Test set accuracy: ', (y_test_pred == data['y_test']).mean())
```

Validation set accuracy: 0.499

Test set accuracy: 0.49

#### 16 重要

这里是作业的结尾处, 请执行以下步骤:

- 1. 点击 File -> Save 或者用 control+s 组合键,确保你最新的的 notebook 的作业已经保存 到谷歌云。
- 2. 执行以下代码确保 .py 文件保存回你的谷歌云。