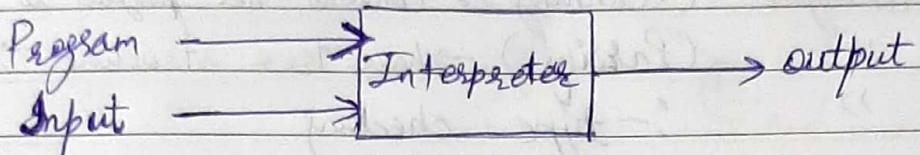
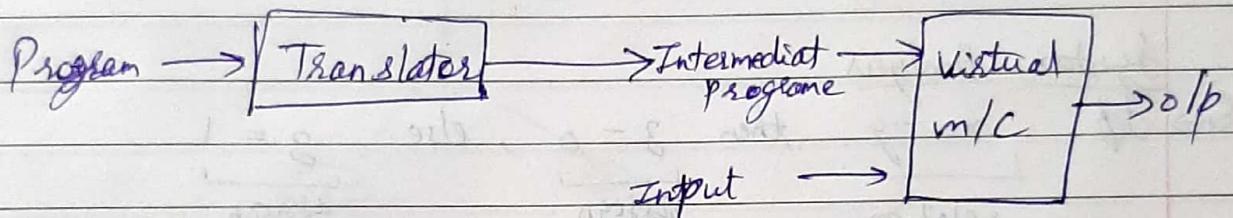


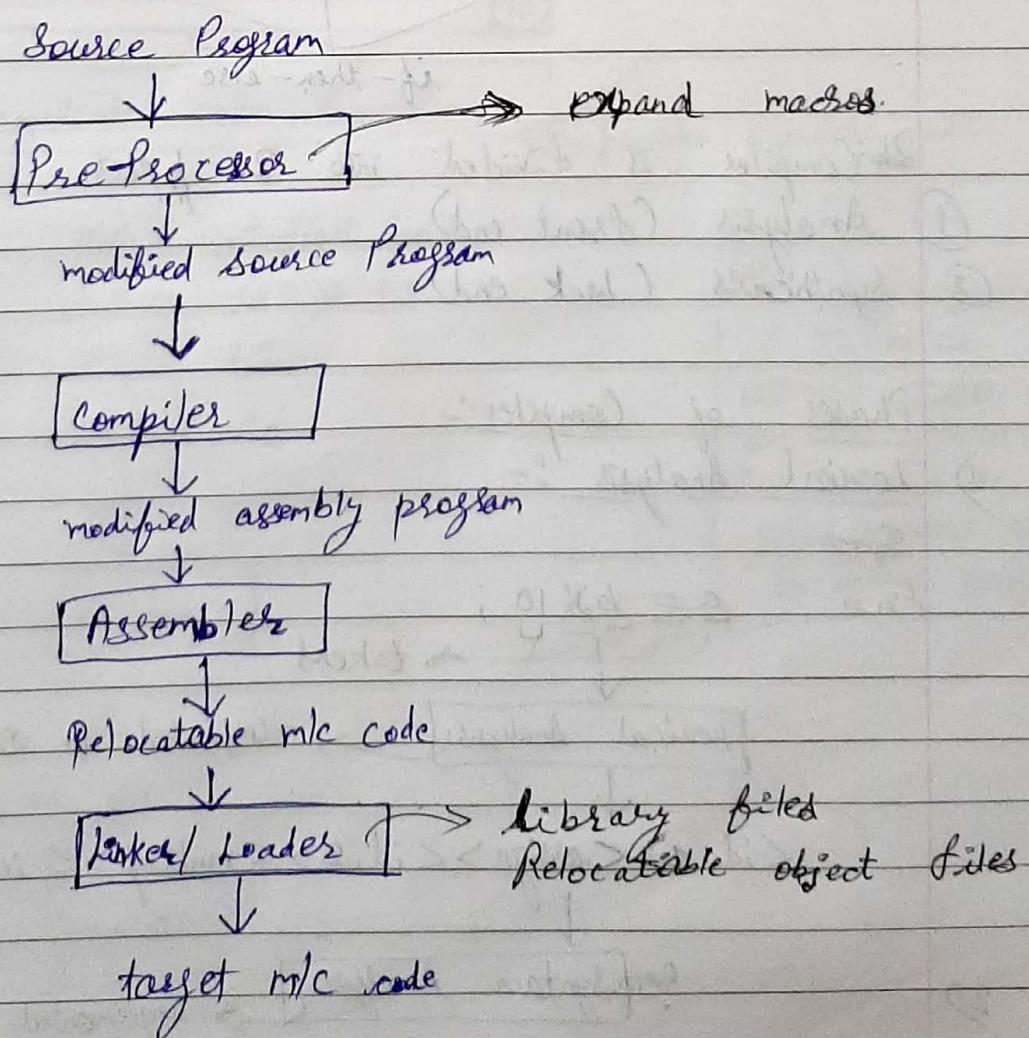
Compiler \rightarrow Convert given file to executable file/code (program)



Hybrid Compiler:



A language Processing system:



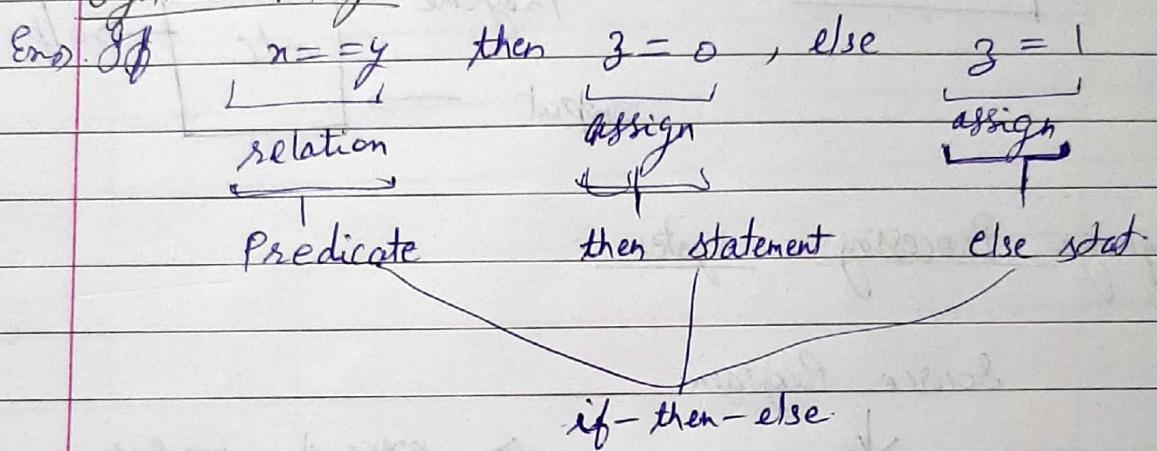
First compiler is designed for FORTRAN.

Phases for any compiler or FORTRAN

- | | |
|---|---|
| Analysis
{
(i) Lexical Analysis
(ii) Syntax
(iii) Semantic

synthesis
{
(iv) Optimisation
(v) Code generation. | Recanning :- converts src program to tokens.
(Parsing) → have tree structure → PDA
:- type checking |
|---|---|

Syntax Analysis



Compiler is divided into 2 parts

- (1) Analysis (front end)
- (2) Synthesis (back end)

Phases of Compiler:-

- 1) Lexical Analysis :-

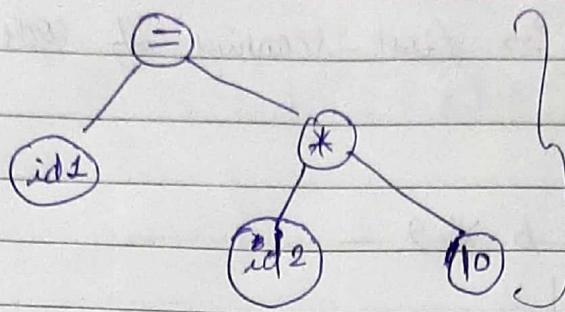
Ex. $a \equiv b * 10 ;$

↓
Lexical Analysis → tokens

implemented by DFA (Deterministic finite automata)

$\langle id, 1 \rangle \langle assign \rangle \langle id, 2 \rangle \langle multop \rangle \langle iconst, 10 \rangle$ → tokens

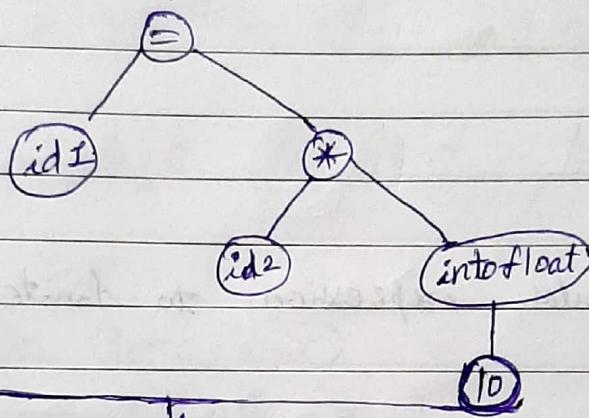
- 2) Semantic Analysis → implemented by pda



syntax tree
(derivation tree in CFG).

3)

Semantic Analysis



4)

Intermediate code Generation

provides standard code.

$t1 = \text{intofloat}(10)$

$t2 = id2 * t1$

$t3 = t2$

$id1 = t3$

5) e

Optimization

Ex:- In languages
n m/c's.
without Inter. code
we need $m \times n$ compiler
But intermediate code
give standard code
 $\Rightarrow m+n$ compiler

$t1 = id2 * 10.0$

$id1 = t1$.

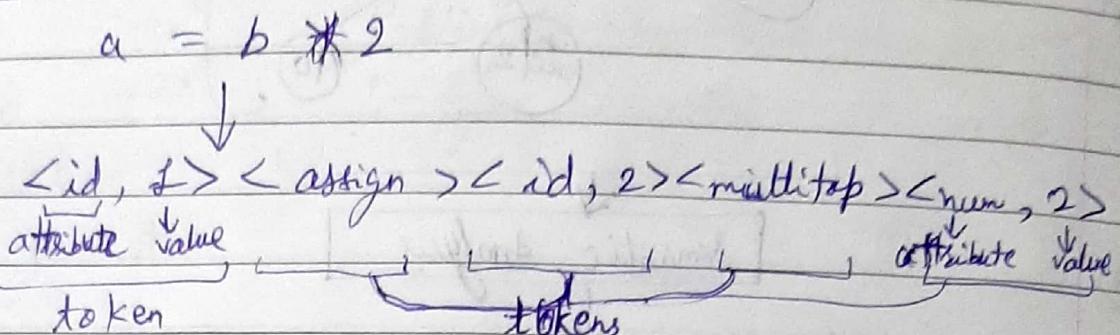
6)

Code Generation

\downarrow
m/c code

1) Lexical Analysis \rightarrow first scanning of code then Lexical Analysis

(1) Tokens



(2) Lexemes

(3) Pattern - Regular expression to finite automata

Lexical Error :-

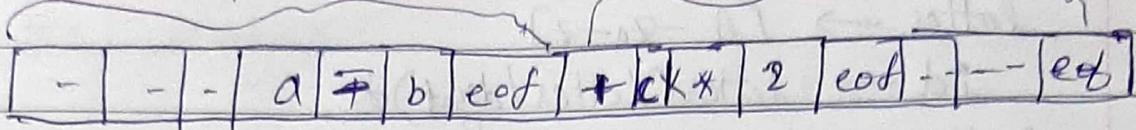
- ↳ Error - Recovery mechanism \rightarrow inserting character
- ↳ Error may be type of
- ↳ for in place of for \rightarrow $\{ \text{for } i=0 \text{ to } n \}$ $\{ \text{wrong pattern} \}$
- ↳ $\langle \text{id}, 1 \rangle \langle \text{id}, 2 \rangle$ $\{ \text{no error} \}$

(4) int roll = 5

\downarrow
no pattern available.

Input Buffering :- use to speed up the reading

Emp \nearrow rolling = b * c * 2
 lexical beginning pointer lexical forwarder pointer

B₁B₂Regular Expression :-

$$a^* = \{\phi, a, aa, \dots\} \quad 3$$

$$a^+ = \{a, aa, aaa, \dots\} \quad 3$$

$$a^? = \{\phi, a\} \quad = a/\epsilon \Rightarrow a \text{ or } \epsilon$$

$$[abc] = a \underset{a}{|} b \underset{a}{|} c \quad \text{and } A/B/C/\dots/z = A-z$$

C-identifier

letter (letter/digit)

where letter $\rightarrow [A-Za-zA-Z]$ digit $\rightarrow [0-9]$ Env- grammar \rightarrow if-then-elsestmt \rightarrow if expr then stmt /

if expr then stmt else stmt /

E

expr \rightarrow term ~~rel op~~ term /
term ^{↳ Relation operator}term \rightarrow id/number

pattern for tokens

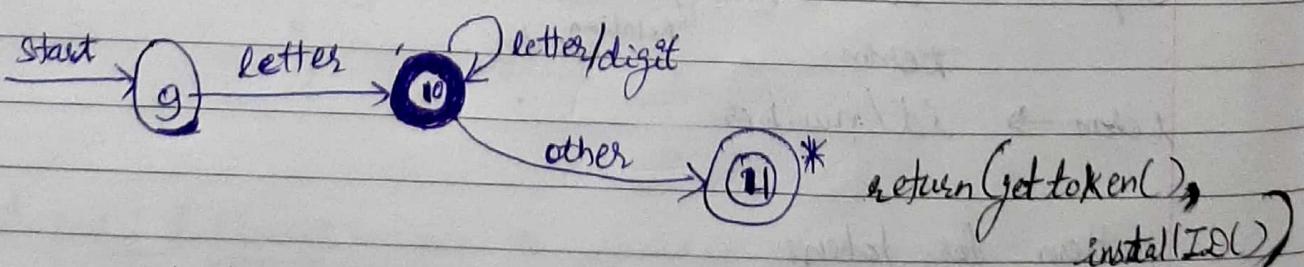
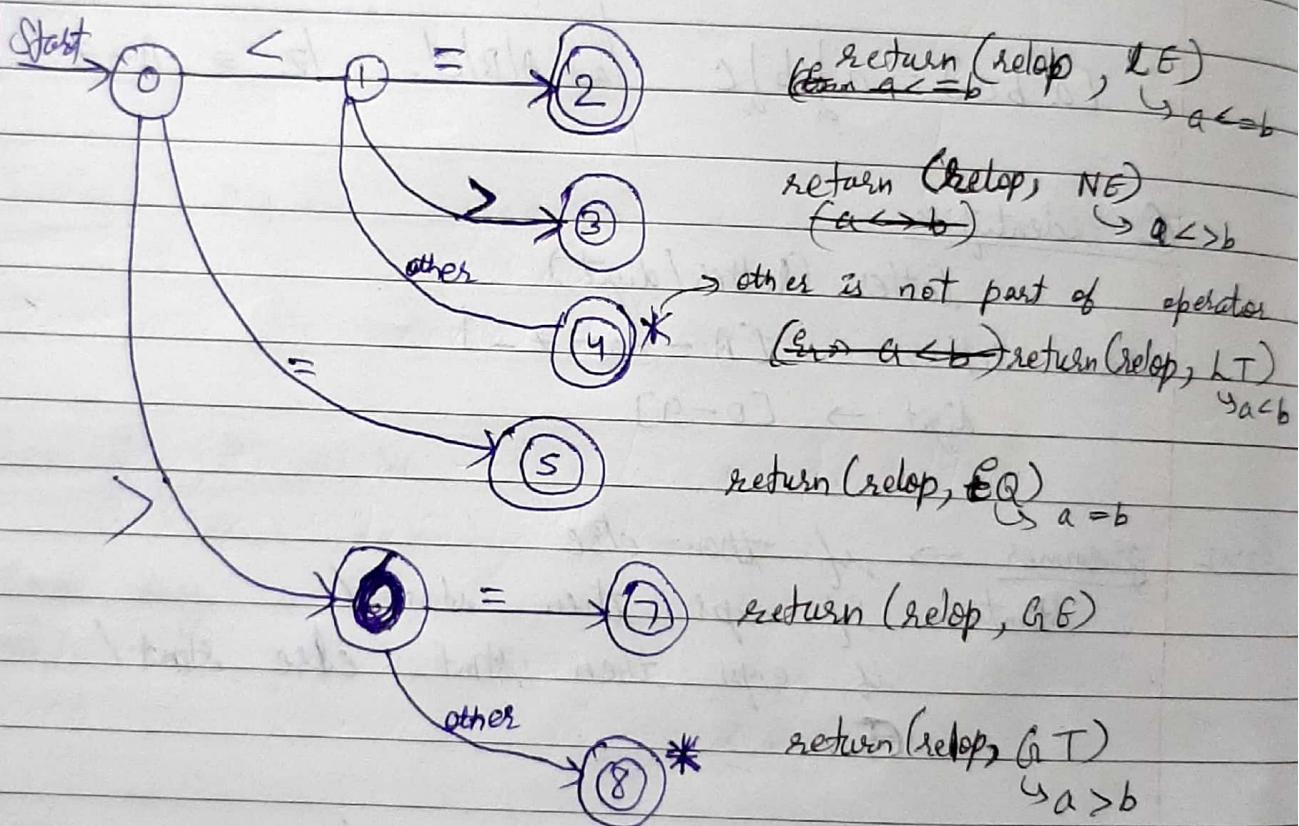
digit $\rightarrow [0-9]$ digits $\rightarrow [0-9]^+$ number \rightarrow digits (digits)? $(E[+,-]? \text{ digits})?$
 \uparrow
exponential

Ex, number = 34, 57.38, 27.5E2

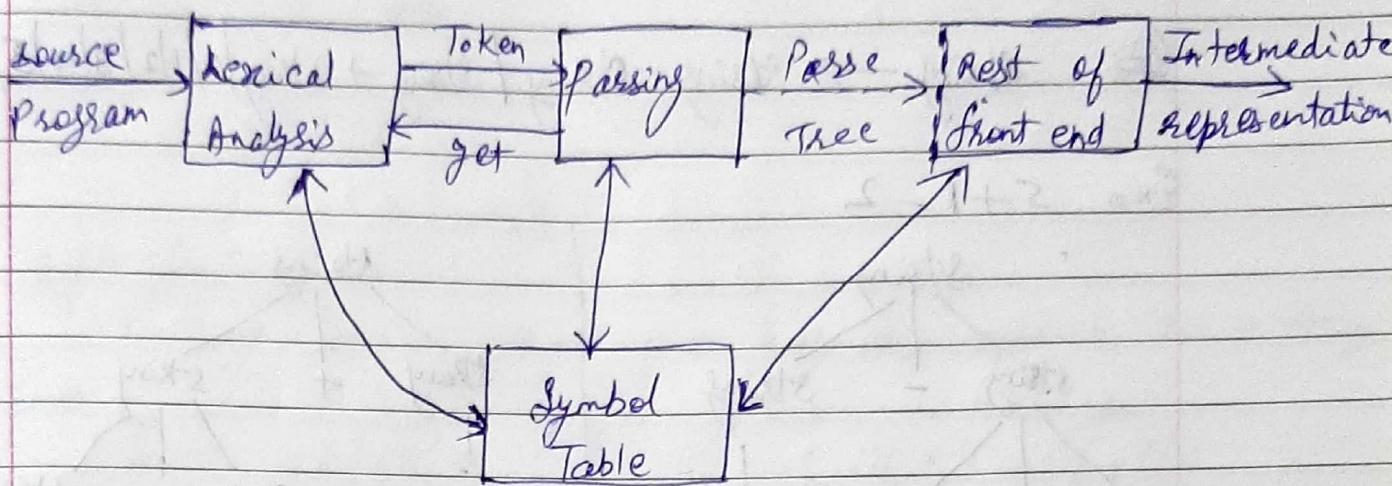
letter $\rightarrow [A - z_a - z]$ id $\rightarrow \text{letter}(\text{letter/digit})^*$ if $\rightarrow \text{if}$ else $\rightarrow \text{else}$ then $\rightarrow \text{then}$ relOp $\rightarrow </> / <= / > = /$

not equal

F8

Transition Diagram:-gettoken() \rightarrow return id no.installID() \rightarrow pointer to that id no.

(2) Syntax Analysis



- 1) Top - Down Parsing
- 2) Bottom - Up Parsing

Type of Errors :-

- (1) Lexical Errors :- No pattern matching.
- (2) Syntax Errors :- curly ({ }) bracket , switch case etc.
- (3) Semantics :- type is not matching (int ≠ char).
- (4) Logical :-

Error Recovery Strategies :-

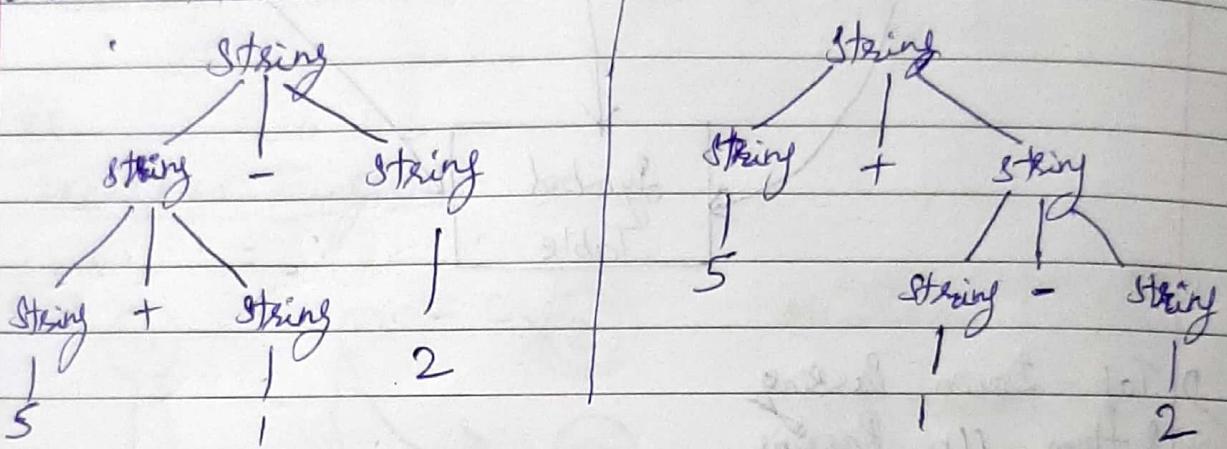
- (1) Panic - Mode Recovery
- (2) Phase - level Recovery :
- (3) Error Production :-
- (4) Global Correction

Crammer:

$$G = (V, T, P, S)$$

~~String~~ → String - String / String + string [0/1/2/3/4/5/6/7/8/9]

Eno 5+1-2



→ Ambiguous grammar

~~→~~ need to convert to non-ambiguous grammar
by,

String → String - digit / string + digit / digit
digit → 0/1/2/3/4/5/6/7/8/9.

→ Top-down approach ~~uses~~ uses left-most derivative

→ need to remove left-excursion.

Essays

if $A \rightarrow A \times B$

$$A \rightarrow \underline{B} B$$

$$\beta \rightarrow \alpha \beta / e$$

~~End~~ Remove left-recursion from

$$E \rightarrow E + T/T$$

$$T \rightarrow T * F / F$$

$$f \rightarrow (E)/\text{id}$$

$$\begin{aligned} E &\rightarrow T B \\ B &\rightarrow + T B / C \\ T &\rightarrow F \cdot C \\ C &\rightarrow * F C / \epsilon \\ F &\rightarrow (E) / id \end{aligned}$$

Left factoring:

↳ Have more than one way to approach for a string

(ex)

$$A \rightarrow aB/aA/a$$

$$B \rightarrow b$$

↓ Left factoring

$$A \rightarrow aC$$

$$C \rightarrow B/A/E$$

$$B \rightarrow b$$

en.

$$S \rightarrow aEts/ies/a$$

$$E \rightarrow b$$

$$S \rightarrow iEtsA/a$$

$$A \rightarrow eS/E$$

$$E \rightarrow b$$

* Top-Down Parsing \Rightarrow (uses left-most derivation)

Recursive-Descent Parsing \Rightarrow

void A() {

choose an A-production, $A \rightarrow X_1 X_2 \dots X_k$;

for ($i = 1$ to k) {

if (X_i is a non terminal)

call procedure $X_i()$;

else if (X_i equals the current i/p symbol 'a')

advance the i/p to the next symbol;

else

/* an error has occurred */ ;

$\text{first}(S) \& \text{follow}(S)$

Era

$$S \rightarrow aAb/b$$

$$A \rightarrow bB$$

$$B \rightarrow a$$

$$\begin{aligned}\text{first}(S) &= \text{first}(aAb) \cup \text{first}(b) \\ &= \{a\} \cup \{b\} \\ &= \{a, b\}\end{aligned}$$

$$\text{first}(A) = \{b\}$$

$$\text{first}(B) = \{a\}$$

* $\text{First}(X)$

1. If X is a terminal, then $\text{first}(X) = \{X\}$.

2. If X is non-terminal, and $X \rightarrow Y_1 \cup Y_2 \cup \dots \cup Y_k$.

Eg. \therefore If $\text{first}(Y_i)$ does not derive ϵ , then $\text{first}(X) = \text{first}(Y_i)$

But if $\text{first}(Y_j)$ derives ϵ , then

$$\text{first}(X) = \text{first}(Y_i) \cup \text{first}(Y_j)$$

and so on.

3. If $X \rightarrow E$ is a production then add E to $\text{first}(X)$

Q. ① Find $\text{first}(E)$ for given grammar.

$$E \rightarrow TE'$$

$$E' \rightarrow +TE'/E$$

$$T \rightarrow FT'$$

$$T' \rightarrow *FT'/E$$

$$F \rightarrow (E)/\text{id}$$

$$\text{First}(E) = \{\$, \text{id}\}$$

$$\text{first}(E') = \{+, *\}$$

$$\text{First}(T) = \{C, \text{id}\}$$

$$\text{First}(T') = \{*, E\}$$

$$\text{first}(F) = \{C, \text{id}\}$$

* follow() \rightarrow for acceptance of string

(1) ~~follow~~ Place \$ in follow(S) where S is start symbol

(2) If $A \rightarrow \alpha B \beta$, then

$$\text{FOLLOW}(B) = \text{FIRST}(\beta) - \{\epsilon\}$$

(3) If $A \rightarrow \alpha B \beta$ and $\text{FIRST}(\beta)$ contain ϵ ,
then $\text{FOLLOW}(B) = \text{FOLLOW}(A)$.

Ans \Rightarrow follow for previous question

$$\text{FOLLOW}(E) = \{\$\}$$

$$\text{FOLLOW}(T) = \text{FIRST}(E') - \{\epsilon\} \cup \text{follow}(E)$$

$$= \text{FIRST}(\{+, *\}) - \{\epsilon\} \cup \{\$\}$$

$$= \{+, \$\}$$

$$= \{+, \$\} \quad \text{--- (1)}$$

$$\text{FOLLOW}(E') = \text{FOLLOW}(E) = \{\$\} \quad \text{--- (2)}$$

for $E' \rightarrow +TE'$

$$\text{FOLLOW}(T) = \text{FIRST}(E') - \{\epsilon\} \cup \text{follow}(E)$$

$$= \{+, \$\}$$

$$= \{+, \$\} \quad \text{--- (3)}$$

for $T \rightarrow FT'$

$$\begin{aligned}\text{FOLLOW}(F) &= \text{FIRST}(T') - \{\epsilon\} \cup \text{FOLLOW}(T) \\ &= \{\ast, \}, \cup \{\epsilon, +, \$\} \\ &= \{\ast, +, \$\}.\end{aligned}$$
(4)

$$\text{FOLLOW}(T') = \text{FOLLOW}(T) = \{\epsilon, +, \$\}$$
(5)

for $T' \rightarrow *FT'$

$$\begin{aligned}\text{FOLLOW}(F) &= \text{FIRST}(T') - \{\epsilon\} \cup \text{FOLLOW}(T') \\ &= \{\ast, \}, \cup \{\epsilon, +, \$\} \\ &= \{\ast, +, \$\}.\end{aligned}$$
(6)

for $F \rightarrow CE$

$$\begin{aligned}\text{FOLLOW}(C) &= \text{First}(E) \\ &= \{\epsilon\}.\end{aligned}$$
(7)

For eq. (2) & (7)

$$\text{FOLLOW}(E) = \{\epsilon, \$\}.$$

Iterate till ^{Follow of}
~~start symbol~~ symbol is fixed.

Here starting symbol E has updated at last so, need to iterate whole production with updated value of $\text{FOLLOW}(E)$.

for $E \rightarrow TE'$

$$\begin{aligned}\text{FOLLOW}(T) &= \text{First}(E') - \{\epsilon\} \cup \text{FOLLOW}(E) \\ &= \{\epsilon\} \cup \{\epsilon, \$\} \\ &= \{\epsilon, \$\}.\end{aligned}$$

$$\text{FOLLOW}(E') = \text{FOLLOW}(E) = \{\epsilon, \$\}.$$

Q2 Find FIRST() & FOLLOW() for given grammar

$$S \rightarrow ACB \mid CbB \mid Ba$$

$$A \rightarrow da \mid BC$$

$$B \rightarrow g \mid e$$

$$C \rightarrow h \mid e$$

$$\Rightarrow FIRST(C) = \{h, \epsilon\}$$

$$FIRST(B) = \{g, \epsilon\}$$

$$FIRST(A) = \{d\} \cup FIRST(B) = \{d\} \cup \{g, \epsilon\} = \{d, g, \epsilon\}$$

$$FIRST(S) = FIRST(A) \cup FIRST(C) = \{d, g, \epsilon\} \cup \{h, \epsilon\} = \{d, g, h, \epsilon\}$$

$$= \{d, g, h, \epsilon\}$$

$$FIRST(A) = \{d\} \cup FIRST(B) - \{\epsilon\} \cup FIRST(C)$$

$$= \{d, g, h, \epsilon\}$$

$$FIRST(S) =$$

$$= \{d, g, h, \epsilon\}$$

$$follow(S) = \$$$

$$follow(A) = first(C) - \{\epsilon\} \cup first(B) - \{\epsilon\} \cup follow(S)$$

LL(1) grammar :- $L \rightarrow \text{left-to-right}$ $L \rightarrow \text{Leftmost derivation}$ $L \rightarrow \text{one step symbol of lookahead.}$

Condition:-

$$\boxed{E} \quad A \rightarrow \alpha/B$$

1) for terminal 'a', both α & B should not derive strings begining with 'a'.

2.

2) Atmost one of α & B can derive ~~the~~ empty string
 $\hookrightarrow \text{first}(\alpha) \& \text{first}(B)$ are disjoint set.

3) If $B \not\Rightarrow \epsilon$, then α does not derive any string begining with a terminal in a terminal in $\text{follow}(A)$
 likewise, if $\alpha \not\Rightarrow \epsilon$

H.W. check is Q-② is LL(1) grammar or not?

Parsing Table →

Errr.

$$E \rightarrow TE'$$

$$E' \rightarrow +TE''/\epsilon$$

$$T \rightarrow FT'$$

$$T' \rightarrow *FT'/\epsilon$$

$$F \rightarrow (E)/\text{id}$$

So,

$$\text{first}(E) = \{ C, \text{id} \}$$

$$\text{first}(E') = \{ +, E \}$$

$$\text{FIRST}(T) = \{ C, \text{id} \}$$

$$\text{FIRST}(T') = \{ *, E \}$$

$$\text{FIRST}(F) = \{ C, \text{id} \}$$

$$\text{FOLLOW}(E) = \{ \}, \$ \}$$

$$(E') = \{ +, \$ \}$$

$$(T) = \{ +, \}, \$ \}$$

$$(T') = \{ +, \}, \$ \}$$

$$(F) = \{ +, *, \}, \$ \}$$

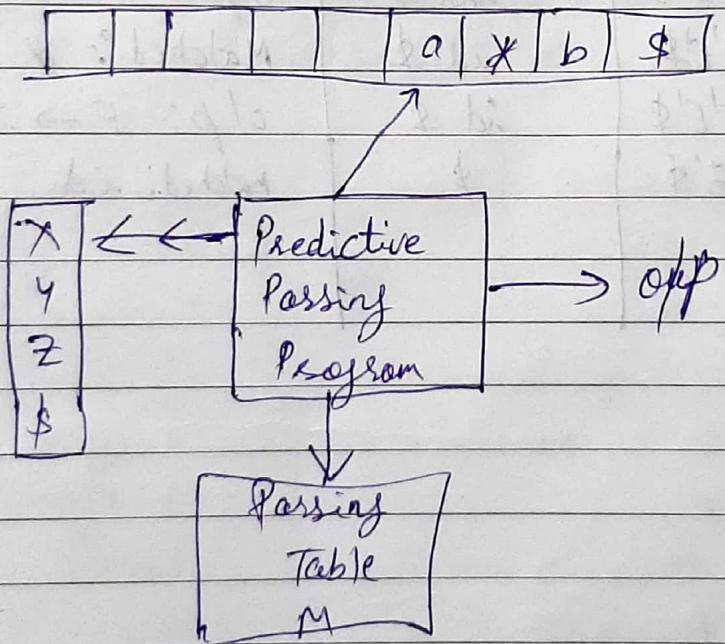
(1) first see the FIRST(E) of product $\times \rightarrow T \rightarrow E \rightarrow TE'$.
 for all FIRST(E) value, insert the entry in table.
 If $E \rightarrow E$ then see FOLLOW of (E), do same for FOLLOW(E) values.

Ex:

Non-Terminal	id	$+$	$*$	C	$)$	$\$$
E	$E \rightarrow TE'$			$E \rightarrow TE'$		
E'		$E' \rightarrow +TE'$			$E' \rightarrow *TE$	$E' \rightarrow TE$
T	$T \rightarrow FT'$			$T \rightarrow FT'$		
T'		$T' \rightarrow C$	$T' \rightarrow *FT'$		$T' \rightarrow E$	$T' \rightarrow E$
F	$F \rightarrow id$			$F \rightarrow (E)$		

Ans:

Non-recurssive Predictive Parsing :-



~~matched string~~: - id + id * id

Match	Stack	Input	Output/Action
E \$		id + id * id \$	o/p: E → T E'
TE' \$	"	"	o/p: E → TE'
FT'E' \$	"	"	T → FT'
id T'E' \$	id + id * id \$	id + id * id \$	o/p: F → id
id	T'E' \$	id * id \$	Matched: id
id	E' \$	+ id * id \$	o/p: T → E
id *	+ T'E' \$	+ id * id \$	o/p: E → TE'
id +	TE' \$	id * id \$	Matched: +
"	FT'E' \$	id * id \$	o/p: T → FT'
	id T'E' \$	id * id \$	o/p: F → id
id + id	T'E' \$	* id \$	Matched: id
"	* FT'E' \$	* id \$	o/p: T → * FT'
id + id *	FT'E' \$	id \$	Matched: *
id + id *	id T'E' \$	id \$	o/p: F → id
id + id * id	T'E' \$	\$	Matched: id.
id + id * id			

* Bottom-up Parsing \Rightarrow Right-most derivatives.

Let the grammar be \hookrightarrow Left-to-right scanning.

$$E \rightarrow E + T$$

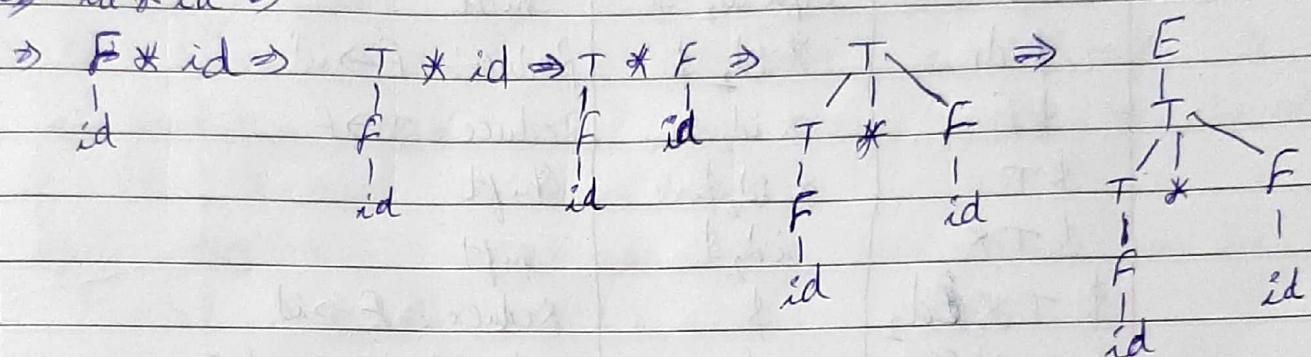
$$E \rightarrow T$$

$$T \rightarrow T * F$$

$$T \rightarrow F$$

$$F \rightarrow id$$

$\Rightarrow id * id \Rightarrow$



Handle :- symbol of string which is replaced by single non-terminal.

$$S \rightarrow a A c B e$$

$$A \rightarrow A b / b$$

$$B \rightarrow d$$

String = abbcde

$$S \rightarrow a A c B e \uparrow \text{RMD}$$

$$\rightarrow a A c \underline{d} e$$

$$\rightarrow a \underline{A} b c d e$$

$$\rightarrow a b b c d e$$

Handle

$$E \rightarrow E + E$$

$$E \rightarrow E * E$$

$$E \rightarrow (E)$$

$$E \rightarrow id$$

String = id + id * id w/ RMD

$$\Rightarrow E \rightarrow E + E$$

$$\rightarrow E + \underline{E * E}$$

$$\rightarrow E + E * \underline{id}$$

$$\rightarrow E + \cancel{E + id} * id$$

$$\rightarrow \underline{id} + id * id$$

$$E \rightarrow E * E$$

$$\rightarrow E * id$$

$$\rightarrow E + F * id$$

$$\rightarrow E + id * id$$

$$\rightarrow id + id * id$$

\rightarrow Need unambiguous grammar for parsing.

Ambiguous grammar.

Shift-Reduce Parsing \rightarrow

$$E \rightarrow E + T/T$$

$$T \rightarrow T * F/F$$

$$F \rightarrow (E)/id$$

String: - id₁*id₂

Stack	input	Action
\$	id ₁ *id ₂ \$	Shift
\$ id ₁	* id ₂ \$	Reduce: - F \rightarrow id
\$ F	* id ₂ \$	Reduce: T \rightarrow F
\$ T	* id ₂ \$	Shift
\$ T *	id ₂ \$	Shift
\$ T * id ₂	\$	Reduce: - F \rightarrow id
\$ T * F	\$	Reduce: T \rightarrow T * F
\$ T	\$	Reduce: - E \rightarrow T
\$ E	\$	Accept

Simple LR \Rightarrow (SLR) :- first create DFA for parsing table.

LR(k)

L = Left-to-right

R = Right Most derivative

k = no. of ~~s~~ if symbol for stack head.

for default k=1 i.e. LR = LR(1).

Items for $A \rightarrow XYZ$ are

$$A \rightarrow \cdot XYZ$$

$$A \rightarrow X \cdot YZ$$

$$A \rightarrow XY \cdot Z$$

$$A \rightarrow XYZ.$$

For SLR \rightarrow need canonical LR \rightarrow canonical items.

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For LR(0) ~~automata~~ ^{DFA}, two funcⁿ needed

- (1) Closure ()
- (2) GOTO ()

\rightarrow If I is a set of items of some grammar G, the CLOSURE(I) is set of items constructed from 2 rules:-

- (1) Initially, add every item in I to closure (I)
- (2) If $A \rightarrow \alpha \cdot BB$ is in CLOSURE(I) and $B \rightarrow \gamma$ is a production, then add the item $B \rightarrow \gamma \cdot$ to closure(I) if it is not already there.

Apply this rule until no more new items can be added to CLOSURE(I).

Ex:-

$$E \rightarrow E + T / T$$

$$T \rightarrow T * F / F$$

$$F \rightarrow id$$

Add $S \rightarrow E \rightarrow \cdot$ (b/c starting symbol E may appear in RHS) ^{Augmented grammar}

$$\text{Now } \text{closure}(S \rightarrow \cdot E) = \{ S \rightarrow \cdot E, E \rightarrow \cdot E + T, E \rightarrow \cdot T, T \rightarrow \cdot T + F, T \rightarrow \cdot F, F \rightarrow \cdot id \}$$

Apply GOTO() on all which have \cdot before Terminal Variables.

GOTO(I_0, E) \Rightarrow

$$= \text{closure}(S \rightarrow E \cdot, E \rightarrow E \cdot + T)$$

$$= \{ S \rightarrow E \cdot, E \rightarrow E \cdot + T \} \quad \text{--- } (I_1)$$

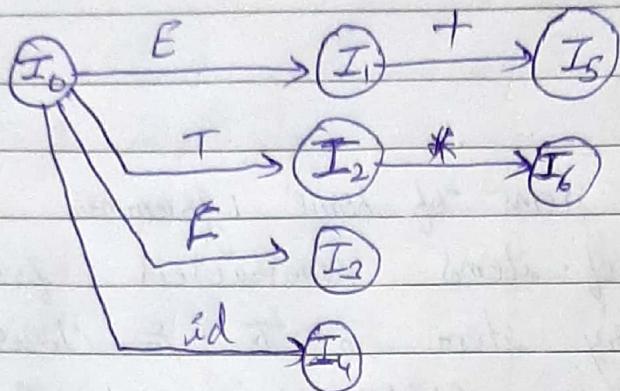
GOTO(I_0, T) = closure($E \rightarrow T \cdot, T \rightarrow T \cdot * F$)

$$= \{ E \rightarrow T \cdot, T \rightarrow T \cdot * F \} \quad \text{--- } (I_2)$$

GOTO(I_0, F) = closure($T \rightarrow F \cdot$)

$$= \{ T \rightarrow F \cdot \} \quad \text{--- } (I_3)$$

$$\text{GOTO}(I_0, \text{id}) = \text{closure}(F \rightarrow \text{id.}) \\ = \{ F \rightarrow \text{id.} \} \quad \dots \quad I_4$$



$$\text{GOTO}(I_1, +) = \text{closure}(E \rightarrow E + \cdot T) \\ = \{ E \rightarrow E + \cdot T, \\ T \rightarrow \cdot T * F, \\ T \rightarrow \cdot F, F \rightarrow \cdot id \} \quad \dots \quad I_5$$

$$\text{GOTO}(I_2, *) = \text{closure}(T \rightarrow T * \cdot F) \\ = \{ T \rightarrow T * \cdot F, F \rightarrow \cdot id \} \quad \dots \quad I_6$$

$$\text{GOTO}(I_3, F) = \text{closure}(T \rightarrow E + T, T \rightarrow T \cdot * F) \\ = \{ T \rightarrow T * \cdot F, F \rightarrow \cdot id \} \quad \dots \quad I_7$$

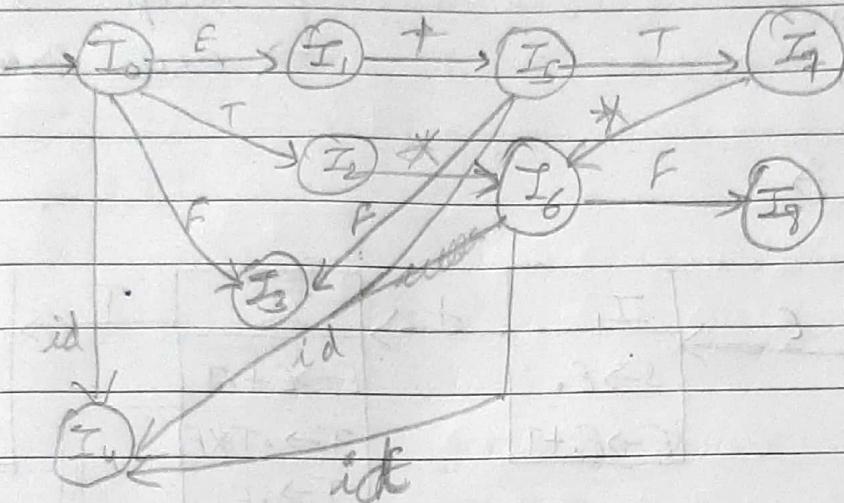
$$\text{GOTO}(I_4, F) = \text{closure}(T \rightarrow F \cdot) \\ = \{ T \rightarrow F \cdot \} \quad \dots \quad I_8$$

$$\text{GOTO}(I_5, \text{id}) = \text{closure}(F \rightarrow \text{id.}) \\ = \{ F \rightarrow \text{id.} \} \quad \dots \quad I_4$$

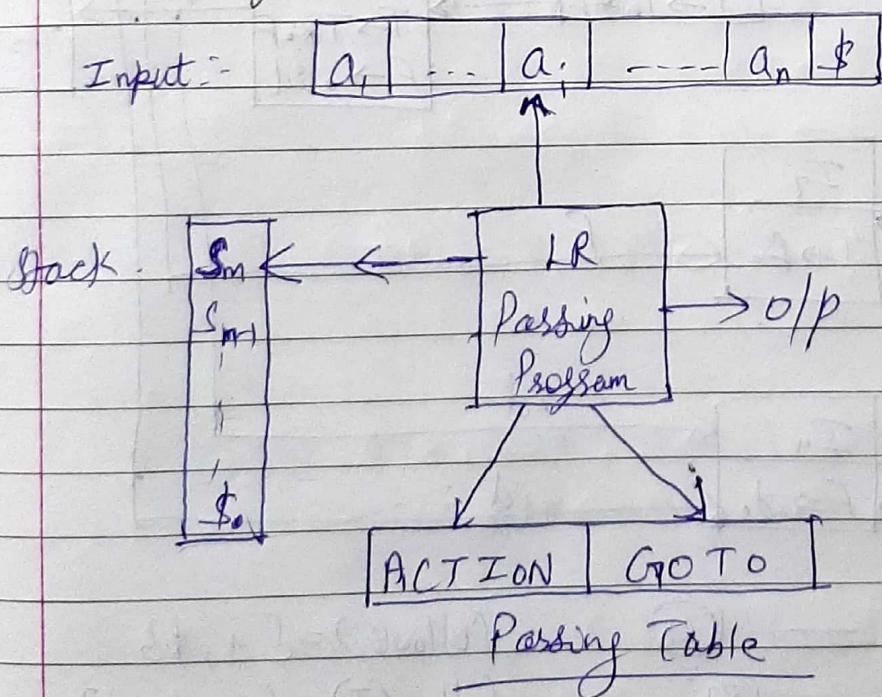
$$\text{GOTO}(I_6, F) = \text{closure}(T \rightarrow T * F \cdot) \\ = \{ T \rightarrow T * F \cdot \} \quad \dots \quad I_8$$

$$\text{GOTO}(I_7, \text{id}) = \text{closure}(F \rightarrow \text{id.}) \\ = \{ F \rightarrow \text{id.} \} \quad \dots \quad I_4$$

$$\begin{aligned}
 \text{GOTO}(I_7, *) &= \text{close}(T \rightarrow T * .F) \\
 &= \{ T \rightarrow T * .F \}, \\
 &\quad F \rightarrow .\text{id}^3 \quad \dots \quad \dots \quad (I_6)
 \end{aligned}$$



LR - Parsing Model :

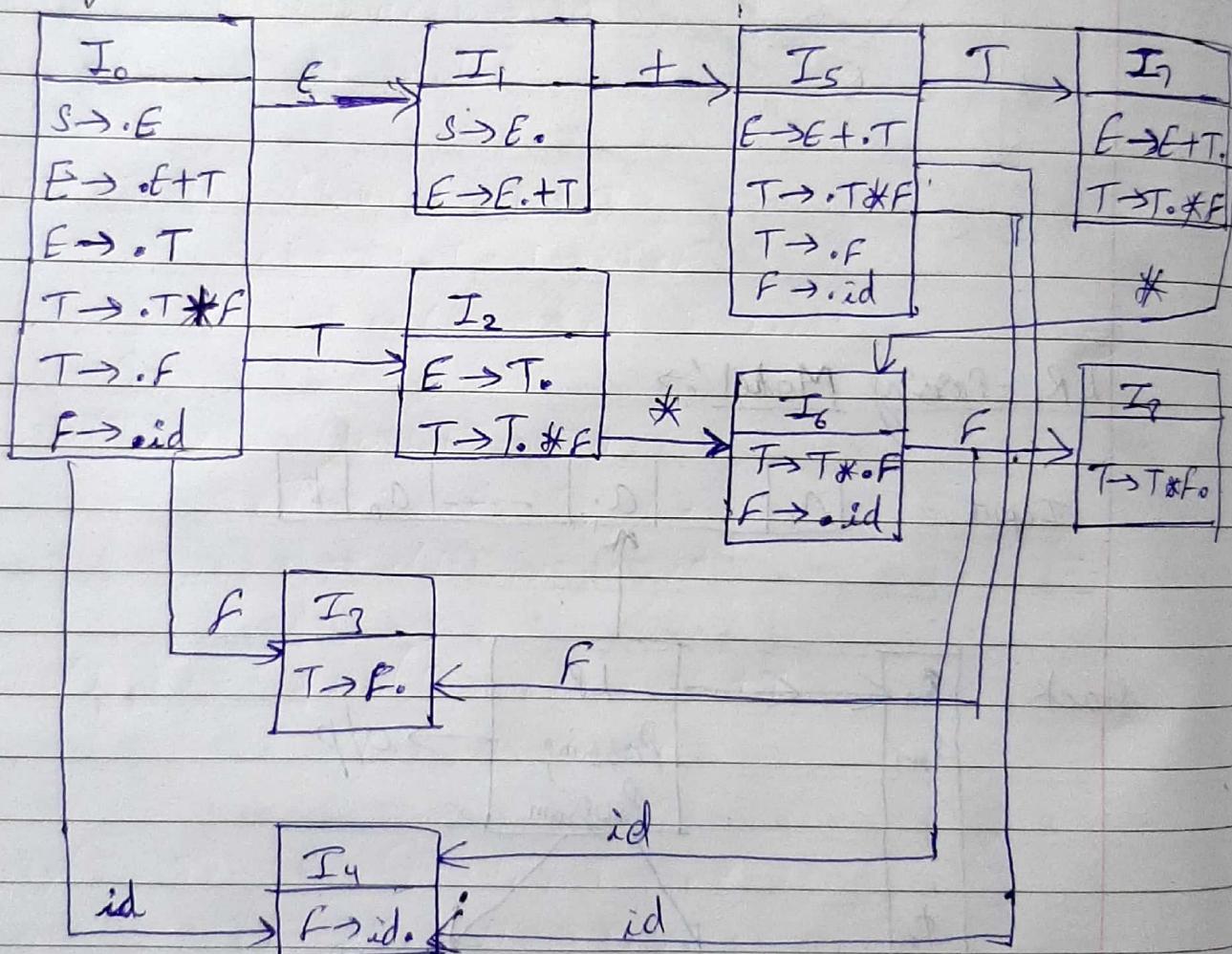


LR Parser Configuration \Rightarrow

$(S_0, \dots, S_m, a_i, a_{i+1}, \dots, a_n)$
 Stack symbols
 (States)

Input symbol

$\rightarrow (S_0, \dots, S_m, a_i, a_{i+1}, \dots, a_n)$
 $\rightarrow (S_0, \dots, S_m, a_i, a_{i+1}, \dots, a_n)$
 accept $\rightarrow E \text{ or } \$$
 error \rightarrow empty cell

Parsing Table \Rightarrow R1, $E \rightarrow E + T$ ---R2, $E \rightarrow T$ ---R3, $T \rightarrow T * F$ ---R4, $T \rightarrow F$ -----R5, $F \rightarrow id$ ----- $\text{follow}(E) = \{ +, \$ \}$ $\text{follow}(T) = \{ +, *, \$ \}$ $\text{follow}(F) = \{ +, *, \$ \}$

→ If an item has * at end of production in any state then reduce that item.
 For ex:- in $T_2 : E \rightarrow T_0$ then Reduce it in its follow (E)

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states	Action	GOTO					
	id	+	*	\$	E	T	F
I ₀	S ₄				1	2	3
I ₁		S ₅		accept			
I ₂		R ₂	S ₆	R ₂			
I ₃		R ₄	R ₄	R ₄			
I ₄		R ₅	R ₅	R ₅			
I ₅	S ₄					7	3
I ₆	S ₄						8
I ₇		R ₁	S ₆	R ₁			
I ₈		R ₃	R ₃	R ₃			

HW:- $E \rightarrow E + T$ create LR(1) parsing table for given grammar
 $E \rightarrow T$

$T \rightarrow T * F$

$T \rightarrow F$

$F \rightarrow (E)$

$F \rightarrow id$.

Adding more production, $S \rightarrow E$

Now

Closure ($S \rightarrow \cdot E$)

$$= \{ S \rightarrow \cdot E, E \rightarrow \cdot E + T, E \rightarrow \cdot T, T \rightarrow \cdot T * F, T \rightarrow \cdot F \\ F \rightarrow \cdot (E), F \rightarrow \cdot id \}$$

(I)

$$\text{Closure GOTO}(I_0, E) = \text{closure}(S \rightarrow E \cdot, E \rightarrow E \cdot + T) \\ = \{ S \rightarrow E \cdot, E \rightarrow E \cdot + T \} \quad \text{--- } (I_1)$$

$$\text{GOTO}(I_0, T) = \text{closure}(E \rightarrow T \cdot, T \rightarrow T \cdot * F) \\ = \{ E \rightarrow T \cdot, T \rightarrow T \cdot * F \} \quad \text{--- } (I_2)$$

$$\text{GOTO}(I_0, F) = \text{Closure}(T \rightarrow F.) \\ = \{ T \rightarrow F. \}$$

$$\begin{aligned}
 GOTO(I_0, C) &= \text{closure}(F \rightarrow (.E)) \\
 &= \{ F \rightarrow (.E), E \rightarrow .E + T, E \rightarrow .T, \\
 &\quad T \rightarrow .T * F, T \rightarrow .F, \\
 &\quad F \rightarrow .(E), F \rightarrow .\text{id} \} \quad \dots \quad (I_4)
 \end{aligned}$$

$$\text{GOTO}(I_0, \text{id}) = \text{Closure}(F \rightarrow \text{id.}) \\ = \{ F \rightarrow \text{id.} \}$$

$$\begin{aligned} \text{GOTO}(I_1, +) &= \text{Closure}(E \rightarrow E + \cdot T) \\ &= \{E \rightarrow E + \cdot T, \quad T \rightarrow \cdot T * F, \\ &\quad T \rightarrow \cdot F, \quad F \rightarrow \cdot (E), \quad F \rightarrow .\text{id}\} \quad \dots \quad (I_1) \end{aligned}$$

$$\begin{aligned}
 \text{GOTO}(I_2, *) &= \text{Closure}(T \rightarrow T * . F) \\
 &= \{ T \rightarrow T * . F, \quad \\
 &\quad F \rightarrow .(E), \quad F \rightarrow .\text{id} \} \quad \text{--- } \text{I}
 \end{aligned}$$

$$\begin{aligned} \text{GOTO}(I_4, E) &= (\text{closure}(F \rightarrow (E.), E \rightarrow E.+T)) \\ &= \{F \rightarrow (E.), E \rightarrow E.+T\} \quad - - - (I_8) \end{aligned}$$

$$\text{GOTO}(I_4, T) = \text{Closure}(E \rightarrow T_0, T \rightarrow T_0 * F) \\ = \{ E \rightarrow T_0, T \rightarrow T_0 * F \} \quad \dots \quad (I_2)$$

$$GOTO(I_4, F) = \text{Closure}(T \rightarrow F.) = \{ T \rightarrow F. \} - - \quad (I_2)$$

$$\text{GroTo}(I_4, C) = \text{closure}(F \rightarrow C \cdot E)$$

$$\text{GroTo}(\mathcal{I}_4, \text{id}) = (\text{gruel } f \rightarrow \text{id} \circ) = \{ \quad \} \quad \text{--- I5}$$

$$\text{GOTO}(I_6, T) = \text{closure}(E \rightarrow E + T., T \rightarrow T * F) \\ = \{ E \rightarrow E + T., T \rightarrow T * F \} \quad \text{--- } I_9$$

$$\text{GOTO}(I_8, F) = \text{closure}(T \rightarrow F.) = \{ \} \quad \text{--- } I_2$$

$$\text{GOT}(I_6, C) = \text{closure}(F \rightarrow C.E) = \{ \} \quad \text{--- } I_4$$

$$\text{GOTO}(I_6, id) = \text{closure}(F \rightarrow id.) = \{ \} \quad \text{--- } I_5$$

$$\text{GOTO}(I_7, F) = \text{closure}(T \rightarrow T * F.) \\ = \{ T \rightarrow T * F. \} \quad \text{--- } I_{10}$$

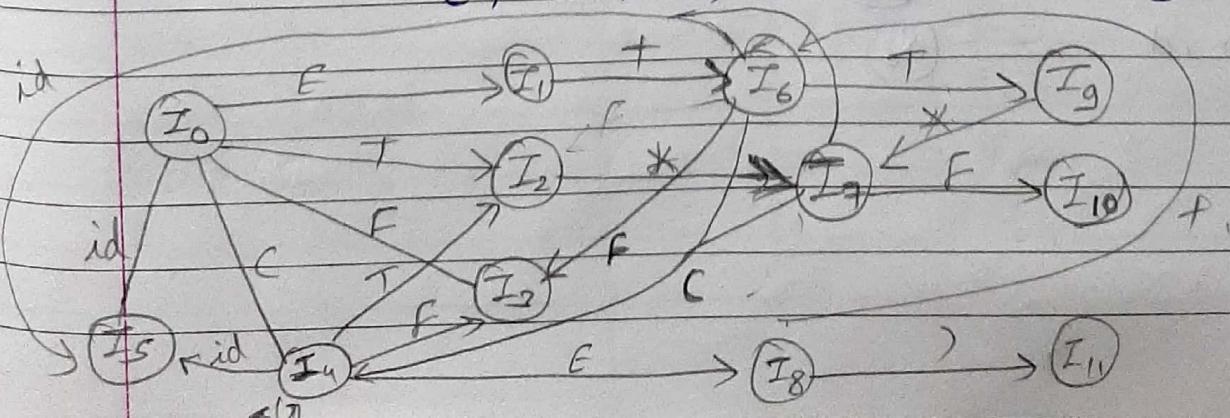
$$\text{GOTO}(I_7, C) = \text{closure}(F \rightarrow C.E) = \{ \} \quad \text{--- } I_4$$

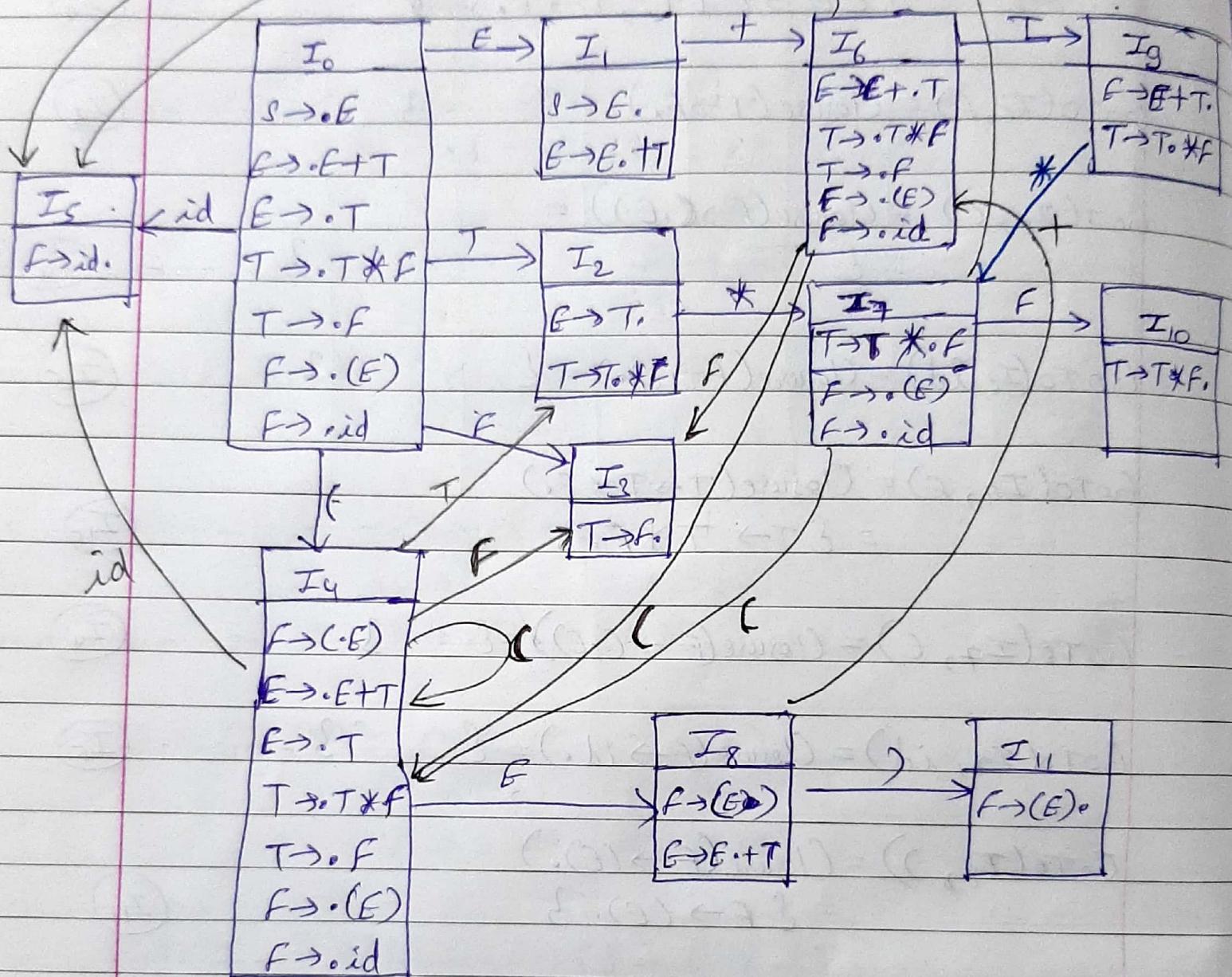
$$\text{GOTO}(I_7, id) = \text{closure}(F \rightarrow id.) = \{ \} \quad \text{--- } I_5$$

$$\text{GOTO}(I_8,)) = \text{closure}(F \rightarrow (E).) \\ = \{ F \rightarrow (E). \} \quad \text{--- } I_{11}$$

$$\text{GOTD}(I_8, +) = \text{closure}(E \rightarrow E + .T) \\ = \{ E \rightarrow E + .T, T \rightarrow .T * F, T \rightarrow .F \\ F \rightarrow .(E), F \rightarrow .id \} \quad \text{--- } I_6$$

$$\text{GOTO}(I_9, *) = \text{closure}(T \rightarrow T * .F) \\ = \{ T \rightarrow T * .F, F \rightarrow .(E), F \rightarrow .id \} \quad \text{--- } I_7$$





$E \rightarrow E + T \dashrightarrow \textcircled{R}_1$

$\text{FOLLOW}(E) = \{ +,), \$ \}$

$E \rightarrow T \dashrightarrow \textcircled{R}_2$

$\text{FOLLOW}(T) = \{ *, +,), \$ \}$

$T \rightarrow T * F \dashrightarrow \textcircled{R}_3$

$\text{FOLLOW}(F) = \{ *, +,), \$ \}$

$T \rightarrow F \dashrightarrow \textcircled{R}_4$

$F \rightarrow (E) \dashrightarrow \textcircled{R}_5$

$F \rightarrow id \dashrightarrow \textcircled{R}_6$

States	Action							GOTO		
	id	()	+	*	'	\$	E	T	F
I ₀	S ₅	S ₄						1	2	3
I ₁			R ₁	S ₆				accept		
I ₂			R ₂	R ₂	S ₇	R ₂				
I ₃			R ₄	R ₄	R ₄	R ₄				
I ₄	S ₅	S ₄							2	3
I ₅			R ₆	R ₆	R ₆	R ₆				
I ₆	S ₅	S ₄							9	3
I ₇	S ₅	S ₄							4	10
I ₈			S ₁₁	S ₆	R	R ₅				
I ₉			R ₁	R ₁	S ₇	R ₁				
I ₁₀			R ₃	R ₃	R ₃	R ₃				
I ₁₁										

Checking for string id * id + id

Stack	Symbol	Input	Action
0		id * id + id \$	shift
05	id	* id + id \$	Reduce : F → id
03	F	* id + id \$	Reduce : T → F
02	T	* id + id \$	shift
027	T *	id + id \$	Shift
0275	T * id	+ id \$	Reduce : F → id
02710	T * F	+ id \$	Reduce : T → T * F
02	T	+ id \$	Reduce : E → T
01-	E	+ id \$	Shift
016	E +	id \$	Shift
0165	E + id	\$	Reduce : F → id
0163	E + F	\$	Reduce : T → F
0	E + T	\$	

* Canonical LR(CLR/LR):

general item

$[A \rightarrow \alpha \cdot B, a]$

↳ Lookahead symbol

where $A \rightarrow \alpha B$

$a = \text{terminal or } \$$

if $B \neq E$

then ' a ' (Lookahead symbol) has no effect on an item

else if $B = E$ or $(A \rightarrow \alpha \cdot, a)$

then $[A \rightarrow \alpha \cdot, a]$ reduces to $A \rightarrow \alpha$, only if the i/p symbol is ' a '.

→ Formally, LR(1) item $[A \rightarrow \alpha \cdot B, a]$ is valid for a viable prefix γ if ~~deviation~~ there is a deviation.

$$S \xrightarrow[\gamma]{} S A W \xrightarrow[\gamma]{} S \alpha B$$

where

$$1. \gamma = S \alpha$$

2. Either ' a ' is first symbol of ' W ' or W is ϵ and ' a ' is $\$$

viable prefix = symbol before handle.

$$Ex \Rightarrow S \rightarrow L = R/Q$$

$$L \rightarrow \cdot *R / id$$

$$R \rightarrow L$$

$$\text{Add, } S' \rightarrow S$$

$$\text{closure}([S' \rightarrow \cdot S, \$]) = \{ [S' \rightarrow \cdot S, \$], \\ [S \rightarrow \cdot L = R, \$], [S \rightarrow \cdot R, \$], \\ [L \rightarrow \cdot *R, =], [L \rightarrow \cdot id, =], \\ [R \rightarrow \cdot L, \$], [L \rightarrow \cdot *R, \$], [L \rightarrow \cdot id, \$] \}$$

$$[L \rightarrow \cdot *R, =], [L \rightarrow \cdot id, =],$$

$$[R \rightarrow \cdot L, \$], [L \rightarrow \cdot *R, \$]$$

$$[L \rightarrow \cdot *R, \$], [L \rightarrow \cdot id, \$] \} \dots \text{--- (1)}$$

$$\text{GOTO}(I_0, S) = \text{Closure}([S' \rightarrow S_0, \$]) \\ = \{ [S' \rightarrow S_0, \$] \} \quad \text{--- } \textcircled{I}_1$$

$$\text{GOTO}(I_0, L) = \text{Closure}([S \rightarrow L_0 = R, \$], [R \rightarrow L_0, \$]) \\ = \{ [S \rightarrow L_0 = R, \$], [R \rightarrow L_0, \$] \} \quad \text{--- } \textcircled{I}_2$$

$$\text{GOTO}(I_0, R) = \text{Closure}([S \rightarrow R_0, \$]) \\ = \{ [S \rightarrow R_0, \$] \} \quad \text{--- } \textcircled{I}_3$$

$$\text{GOTO}(I_0, *) = \text{Closure}([L \rightarrow *R, R, =/\$]) \\ = \{ [L \rightarrow *R, R, =/\$], [R \rightarrow L, =/\$] \\ [L \rightarrow *R, =/\$], [L \rightarrow .id, =/\$] \} \quad \text{--- } \textcircled{I}_4$$

$$\text{GOTO}(I_0, id) = \text{Closure}([L \rightarrow id, =/\$]) \\ = \{ [L \rightarrow id, =/\$] \} \quad \text{--- } \textcircled{I}_5$$

$$\text{GOTO}(I_2, =) = \text{Closure}([S \rightarrow L = .R, \$]) \\ = \{ [S \rightarrow L = .R, \$], [R \rightarrow .L, \$], \\ [L \rightarrow *R, \$], [L \rightarrow .id, \$] \} \quad \text{--- } \textcircled{I}_6$$

$$\text{GOTO}(I_4, R) = \text{Closure}([L \rightarrow *R, R, =/\$]) \\ = \{ [L \rightarrow *R, R, =/\$] \} \quad \text{--- } \textcircled{I}_7$$

$$\text{GOTO}(I_4, L) = \text{Closure}([R \rightarrow L, =/\$]) \\ = \{ [R \rightarrow L, =/\$] \} \quad \text{--- } \textcircled{I}_8$$

$$\text{GOTO}(I_4, *) = \text{Closure}([L \rightarrow *R, R, =/\$]) \\ = \{ [L \rightarrow *R, R, =/\$], [R \rightarrow .L, =/\$] \\ [L \rightarrow *R, =/\$], [L \rightarrow .id, =/\$] \} \quad \text{--- } \textcircled{I}_9$$

$$\text{GOTO}(I_4, id) = \text{Closure}([L \rightarrow id, =/\$]) \\ = \{ [L \rightarrow id, =/\$] \} \quad \text{--- } \textcircled{I}_{10}$$

$$\text{GOTO}(I_6, R) = \text{Closure}([S \rightarrow L = R., \$]) \\ = \{ [S \rightarrow L = R., \$] \}$$

(I₉)

$$\text{GOTO}(I_6, L) = \text{Closure}([R \rightarrow L., \$]) \\ = \{ [R \rightarrow L., \$] \}$$

(I₁₀)

$$\text{GOTO}(I_6, *) = \text{Closure}([L \rightarrow * . R, \$]) \\ = \{ [L \rightarrow * . R, \$], [R \rightarrow . L, \$] \\ [L \rightarrow . * R, \$], [L \rightarrow . id, \$] \}$$

(I₁₁)

$$\text{GOTO}(I_6, id) = \text{Closure}([L \rightarrow id., \$]) \\ = \{ [L \rightarrow id., \$] \}$$

(I₁₂)

~~$\text{GOTO}(I_6, R)$~~ $= \text{Closure}([L \rightarrow * R., \$]) \\ = \{ [L \rightarrow * R., \$] \}$

(I₁₃)

$$\text{GOTO}(I_{11}, L) = \text{Closure}([R \rightarrow L., \$]) \\ = \{ [R \rightarrow L., \$] \}$$

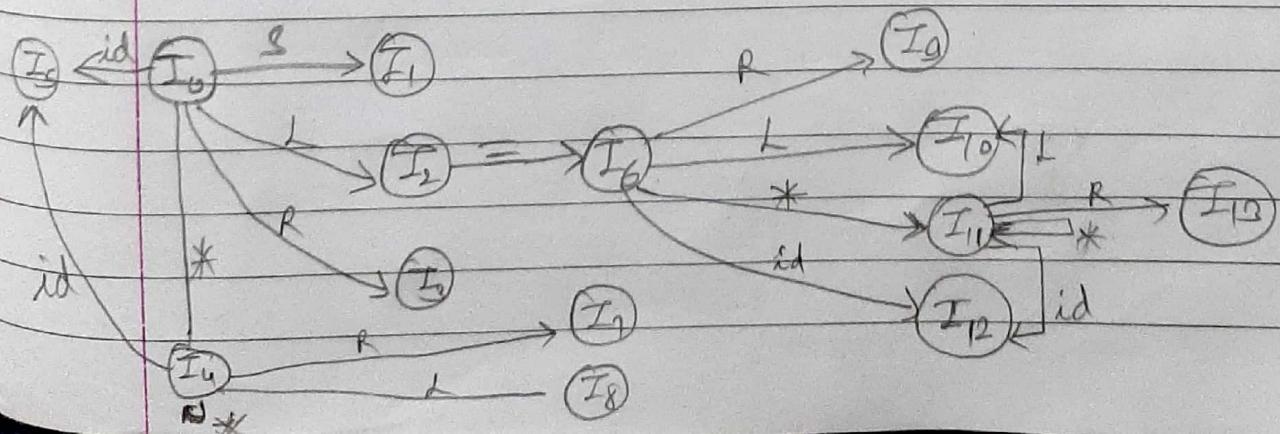
(I₁₀)

$$\text{GOTO}(I_{11}, *) = \text{Closure}([L \rightarrow * . R, \$]) \\ = \{ [L \rightarrow * . R, \$], [R \rightarrow . L, \$] \\ [L \rightarrow . * R, \$], [L \rightarrow . id, \$] \}$$

(I₁₄)

~~$\text{GOTO}(I_{11}, id)$~~ $= \text{Closure}([L \rightarrow id., \$]) \\ = \{ [L \rightarrow id., \$] \}$

(I₁₂)



$$\begin{array}{ll}
 S \rightarrow L = R & (R_1) \\
 S \rightarrow R & (R_2) \\
 L \rightarrow * R & (R_3) \\
 L \rightarrow id & (R_4) \\
 R \rightarrow L & (R_5)
 \end{array}$$

$\text{Follow}(S) = \{\$, \$\}$
 $\text{Follow}(L) = \{=, \$\}$
 $\text{Follow}(R) = \{=, \$\}$

LR

Parsing Table:

State	Action	id	*	=	\$	S	L	R
I ₀	ss	s ₄				1	2	3
I ₁					accept			
I ₂			s ₆		R ₅			
I ₃					R ₂			
I ₄	s ₅	s ₄					8	7
I ₅				R ₄	R ₄			
I ₆	s ₁₂	s ₁₁					10	9
I ₇				R ₃	R ₃			
I ₈				R ₅	R ₅			
I ₉					R ₁			
I ₁₀					R ₅			
I ₁₁	s ₁₂	s ₁₁					10	13
I ₁₂					R ₄			
I ₁₃					R ₃			