
 MODULE *SPA_Attack*

This is a specification of the SDP architecture and algorithm. The specification is based on the following materials:

<https://cloudsecurityalliance.org/artifacts/software-defined-perimeter-zero-trust-specification-v2/> <http://www.cipherdyne.org/fwknop/>

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EXTENDS *FiniteSets, Sequences, Naturals, Integers, TLC, Bitwise*

The end point user's (*SDP* client) configuration, includes local *IP* and account *Info*.

CONSTANT *ClientCfg* @type: [*LoginID* \mapsto String, *Key* \mapsto Integer, *SrcIp* \mapsto Integer];

The *SDP* controller's exposure service info, includes listening *IP* and port.

CONSTANT *SDPSvrCfg* @type: [*IP* \mapsto Integer, *Port* \mapsto Integer];

The target server's exposure service info, includes server *IP* and listening port.

CONSTANT *SvrCfg* @type: [*IP* \mapsto Integer, *Port* \mapsto Integer];

The attacker's configuration, includes local *IP*.

CONSTANT *AttackerCfg* @type: [*SrcIp* \mapsto Integer];

The match any type value for a *ACL Rule*.

CONSTANT *MATCH_ANY* @type: Integer;

For an user's socket link , the random local port range.

CONSTANT *USER_BASEPORT* @type: Integer;

For an attacker's socket link , the random local port range.

CONSTANT *ATTACKER_BASEPORT* @type: Integer;

If the attacker and user are in the same *LAN* with a shared public *IP* for *NAT*.

CONSTANT *NAT_FLAG* @type: *BOOL*;

The invalid authentication session *ID* value.

If a data access link with an invalid authentication session *ID*, it means we don't know the data access is resulted by which *Auth* session.

CONSTANT *UNKNOWN_AUTH_ID* @type: Integer;

If the legal user and attacker are in the same *LAN* with shared public *IP*, then the local port range after *SNAT* must not conflict with the attacker's.

ASSUME (*NAT_FLAG* = TRUE \Rightarrow *AttackerCfg.SrcIp* = *ClientCfg.SrcIp* \wedge *USER_BASEPORT* \neq *ATTACKER_BASEPORT*)

ASSUME ($SDPSvrCfg.IP \neq ClientCfg.SrcIp \wedge SDPSvrCfg.IP \neq AttackerCfg.SrcIp$)

ASSUME ($SvrCfg.IP \neq ClientCfg.SrcIp \wedge SvrCfg.IP \neq AttackerCfg.SrcIp$)

ASSUME ($SvrCfg.IP \neq SDPSvrCfg.IP$)

The variables related to legal user's state machine

The legal user's status indicates which session it is undergoing now.

VARIABLE $uState$ @type: { "Start_Auth", "Auth_End", "Connecting", "Connected" };

The legal user's IP address get from configuration.

VARIABLE uIP @type: Integer;

The legal user's ID for authentication.

VARIABLE uID @type: String;

The legal user's Secret Key for authentication.

VARIABLE Key @type: Integer;

The legal user's Sync counter value (Time Stamp) for SDP authentication, the counter increases randomly each authentication.

VARIABLE $uTstamp$ @type: Integer;

The legal user's knowledge for SDP controller's info got from configuration.

VARIABLE $uSDPSvrInfo$ @type: [$IP \mapsto$ Integer, $Port \mapsto$ Integer];

The legal user's knowledge for target server's info got from configuration.

VARIABLE $uSvrInfo$ @type: [$IP \mapsto$ Integer, $Port \mapsto$ Integer];

The legal user's TCP links connected with target server for access.

VARIABLE $uTCPLinkSet$ @type: Set([$sIP \mapsto$ Integer,
 $dIP \mapsto$ Integer,
 $dPort \mapsto$ Integer,
 $State \mapsto$ { "SYN-SENT", "ESTABLISHED" }]);

The legal user's Authenticaiton sessions in history recorded in Log. Each session identified by a SPA message.

VARIABLE $uAuthSession$ @type: Set([$MsgID \mapsto$ "SPA_AUTH",
 $sIP \mapsto uIP$,
 $sPort \mapsto RandomPort(uTstamp, USER_BASEPORT)$,
 $dIP \mapsto uSDPSvrInfo.IP$, \ *The SDP Controller's IP and port for SPA protocol

$dPort \mapsto uSDPSvrInfo.Port,$
 $ClientID \mapsto uID, Tstamp \mapsto uTstamp, \setminus * \text{ increased each session to anti Replay}$
 $SvrIP \mapsto Encrypt(uSvrInfo.IP, Key), \setminus * \text{ Target Server's exposure service Info, need to kept secret}$
 $SvrPort \mapsto Encrypt(uSvrInfo.Port, Key),$
 $HMAC \mapsto CalcHMAC(uIP, uID, uTstamp, Encrypt(uSvrInfo.IP, Key), Encrypt(uSvrInfo.Port, Key), Key),$
 $\setminus * \text{ HMAC of payload}$
 $Type \mapsto Set("User", "Attacker")); \setminus * \text{ Flag to indicate this message is built by legal user or attacker } \setminus * \text{ this flag not involved in inter-operation between SDP protocol entities,only for statistic}$

The legal user equipment's packets channel for receiving data plane packets, corresponds to its physical *NIC*.

VARIABLE $uChannel$ @type: Sequence of *TCP* Packets $Seq([sIP \mapsto p.dIP, \setminus * \text{ TCP packets for data access, for this model}]$

$sPort \mapsto p.dPort, \setminus * \text{ simulate the data plane access stream only by TCP connection procedure}$
 $dIP \mapsto p.sIP, \setminus * \text{ IE. if user establish a TCP connection with target server, that}$
 $dPort \mapsto p.sPort, \setminus * \text{ means a successful data access session.}$
 $Flg \mapsto Set("TCP_SYN", "TCP_SYN_ACK", "TCP_ACK"),$
 $\setminus * \text{ TCP handshake packets type.}$
 $Type \mapsto Set("User", "Attacker")); \setminus * \text{ Flag to indicate this access is initiated by legal user or attacker } \setminus * \text{ this flag not involved in inter-operation between SDP protocol entities,only for statistic}$

The legal *User*'s private variables ($uChannel$ is public variable of user, for other entity can operate and modify $uChannel$ variable)

$user_vars \triangleq \langle uState, uIP, uID, Key, uTstamp, uSDPSvrInfo, uSvrInfo, uTCPLinkSet, uAuthSession \rangle$

The variables related to SDP Server's (SDP Controller) state machine

The *SDP* controller's status indicates this entity's service is available or faulty.

VARIABLE $SDPSvrState$ @type: $Set("Work")$

The *SDP* controller successfully processed *Auth* sessions in history recorded in *Log*.

VARIABLE $SDPSucSession$ @type: $uAuthSession$

The Legal user accounts info recorded in *SDP* controller's *IAM* system.

VARIABLE $Account$ @type: $Set([ClientID \mapsto ClientCfg.LoginID, Key \mapsto ClientCfg.Key])$

The *SDP* controller's exposure SPA service info .

VARIABLE $SDPSvrInfo$ @type: $[IP \mapsto SDPSvrCfg.IP, Port \mapsto SDPSvrCfg.Port]$

The number of replay attack messages inspected by *SDP* controller

VARIABLE *ReplayCount* @type: Integer;

The number of spoof attack messages inspected by *SDP* controller

VARIABLE *SpoofCount* @type: Integer;

The replay attack *Auth* sessions inspected by *SDP* controller in history recorded in *Log*.

VARIABLE *ReplaySession* @type: *uAuthSession*;

The spoof attack *Auth* sessions inspected by *SDP* controller in history recorded in *Log*.

VARIABLE *SpoofSession* @type: *uAuthSession*;

SDP controller's packets channel for receiving control plane *Auth* messages, corresponds to its physical *NIC*.

VARIABLE *AuthChannel* @type: Sequence of SPA *Auth* Packets *Seq*([*MsgID* \mapsto "SPA_AUTH",

sIP \mapsto *uIP*,
sPort \mapsto *RandomPort*(*uTstamp*, *USER_BASEPORT*),
dIP \mapsto *uSDPSvrInfo.IP*, \ * The *SDP* Controller's *IP* and port for SPA protocol
dPort \mapsto *uSDPSvrInfo.Port*,
ClientID \mapsto *uID*, *Tstamp* \mapsto *uTstamp*, \ * increased each session to anti Replay
SvrIP \mapsto *Encrypt*(*uSvrInfo.IP*, *Key*), \ * Target Server's exposure service *Info*, need to kept secret
SvrPort \mapsto *Encrypt*(*uSvrInfo.Port*, *Key*),
HMAC \mapsto *CalcHMAC*(*uIP*, *uID*, *uTstamp*, *Encrypt*(*uSvrInfo.IP*, *Key*), *Encrypt*(*uSvrInfo.Port*, *Key*),
\ * HMAC of payload
Type \mapsto *Set*("User", "Attacker")); \ * Flag to indicate this message is built by legal user or attacker \ * this flag not involved in inter-operation between *SDP* protocol entities, only for statistic;

The *SDP* controller's private variables (*AuthChannel* is public variable of *SDP* controller, for other entity can operate)

sdpsvr_vars \triangleq \langle *SDPSvrState*, *SDPSucSession*, *Account*, *SDPSvrInfo*, *ReplayCount*, *SpoofCount*, *SpoofSession* \rangle

The variables related to FireWall's state machine

The *FireWall*'s status indicates this entity's service is available or faulty.

The *FireWall* works in deny mode by default.

VARIABLE *FwState* @type: *Set*("Work")

Current *Acl Rule* Set maintained by the *FireWall* for data plane traffic.

VARIABLE *AclRuleSet* @type: *Set*([*sIP* \mapsto Integer,

sPort \mapsto Integer, \ * the value can be *MATCH_ANY*,
dIP \mapsto Integer,

```

dPort ↦ Integer,
protocol ↦ "TCP",
action ↦ "Accept"]

```

The aged *Acl* Rules in history recorded in *FireWall*'s log.

```

VARIABLE AgedRuleSet @type: Set([sIP ↦ Integer,
sPort ↦ Integer, \ * the value can be MATCH_ANY,
dIP ↦ Integer,
dPort ↦ Integer,
protocol ↦ "TCP",
action ↦ "Accept"])

```

The dropped packets by *FireWall* in history recorded in log.

```

VARIABLE DropPackets @type: Set([sIP ↦ p.dIP, \ * Only data plane TCP packets are processed by FireWall
sPort ↦ p.dPort,
dIP ↦ p.sIP,
dPort ↦ p.sPort,
Flg ↦ Set("TCP_SYN", "TCP_SYN_ACK", "TCP_ACK"), \ * TCP
handshake packets type.
Type ↦ Set("User", "Attacker")]);)

```

FireWall's control plane channel for receiving *Openflow* instruction from *SDP* controller to configure data access *Acl Rule*, corresponds to one of its physical *NIC*.

```

VARIABLE FwCtlChannel @type: Sequence of Acl config instructions Seq([Rule ↦ AclRule, op ↦ Set("Add", "Del")])

```

FireWall's ingress data plane channel for receiving packets from end point entities, corresponds to one of its physical *NIC*.

```

VARIABLE FwDataChannel @type: Sequence of Data Packets Seq([sIP ↦ p.dIP, \ * Only data plane TCP packets are processed by FireWall
sPort ↦ p.dPort,
dIP ↦ p.sIP,
dPort ↦ p.sPort,
Flg ↦ Set("TCP_SYN", "TCP_SYN_ACK", "TCP_ACK"), \ * TCP
handshake packets type.
Type ↦ Set("User", "Attacker")]);)

```

The *FireWall*'s private variables (*FwDataChannel* and *FwCtlChannel* are public variable of *FW*, for other entity can operate and access them).

$fw_vars \triangleq \langle FwState, AclRuleSet, AgedRuleSet, DropPackets \rangle$

The variables related to Attacker's state machine

The *Attacker*'s status indicates this entity's is spying or not.

```

VARIABLE aState @type: Set("Listen")

```

The *Attacker*'s current knowledge about legal user's auth action learned by sniffing legal user's auth message.

```

VARIABLE AuthKnowledge @type: uAuthSession

```

The *Attacker* initiated SPA attack sessions in history recorded in log. Each session is identified by a fake SPA message.

VARIABLE *aSession* @type: *uAuthSession*

The *Attacker* initiated *TCP* connections towards the target server. Each link corresponds to an inspection attack to t

VARIABLE *aTCPLinkSet* @type: *Set*([*sIP* \mapsto Integer,
 sPort \mapsto Integer,
 dIP \mapsto Integer,
 dPort \mapsto Integer,
 State \mapsto { "SYN_SENT", "ESTABLISHED" }
 AuthID \mapsto Integer] \ * The *AuthID* is used for relating to a captured
 auth message
) \ * For this model, once the attacker spy a SPA message, it will undertake
 a data attack to the target server.
 \ * The value *UNKNOWN_AUTH_ID* indicates the attack is not originate
 from a captured auth message, but a captured data message

The number of sucessfully sniffed SPA messages by attacker

VARIABLE *sniffCount* @type: Integer;

All the successfully sniffed SPA messages by attacker in history recorded in log

VARIABLE *CapAuthMsg* @type: *uAuthSession*;

Attacker maintained increasing sequence number to build local port field for *TCP* links of different *Detection* attack.

VARIABLE *aCounter* @type: Integer;

Attacker's *IP* address, which is got by configuration.

If *NAT_FLAG* = TRUE, then attacker and legal user located in the same *LAN* and share same public *IP* (*aIP* = *uIP*).

VARIABLE *aIP* @type: Integer;

The *Attacker*'s current knowledge about legal user's data access learned by sniffing legal user's *TCP* handshake packets

VARIABLE *DataKnowledge* @type: *Set*([*sIP* \mapsto *p.dIP*, \ * Only data plane *TCP* packets are processed by F
 sPort \mapsto *p.dPort*,
 dIP \mapsto *p.sIP*,
 dPort \mapsto *p.sPort*,
 Flg \mapsto *Set*("TCP_SYN", "TCP_SYN_ACK", "TCP_ACK"), \ * *TCP*
 handshake packets type.
 Type \mapsto *Set*("User", "Attacker")])

All the successfully sniffed user data packets by attacker in history recorded in log

VARIABLE *CapDataMsg* @type: *DataKnowledge*

The attacker's packets channnel for recieving data plane packets, corresponds to its physical *NIC*.

VARIABLE *aChannel* @type: *uChannel*

The attacker's private variables ($aChannel$ is public variable of attacker, for other entity can operate and modify $aChannel$ variable)
 $attacker_vars \triangleq \langle aState, AuthKnowledge, aSession, aTCPLinkSet, sniffCount, CapAuthMsg, aCounter, aIP \rangle$

The variables related to target service server's state machine

The target server's status indicates this entity's service is available or faulty.

VARIABLE $sState$ @type: $Set("Listen")$

The TCP socket maintained in server side initiated from end points towards target server.

VARIABLE $sTCPLinkSet$ @type: $Set([sIP \mapsto p.dIP, \setminus * \text{Only data plane TCP packets are processed by FireWall}$
 $sPort \mapsto p.dPort,$
 $dIP \mapsto p.sIP,$
 $dPort \mapsto p.sPort,$
 $Flg \mapsto Set("TCP_SYN", "TCP_SYN_ACK", "TCP_ACK"), \setminus * \text{TCP}$
 $\text{handshake packets type.}$
 $Type \mapsto Set("User", "Attacker")])$

The target server's exposure service info got from configuration.

VARIABLE $sSvrInfo$ @type: $[IP \mapsto SvrCfg.IP, Port \mapsto SvrCfg.Port]$

The server's packets channel for receiving data plane packets from endpoint equipments, corresponds to its physical NIC .

VARIABLE $sChannel$ @type: $uChannel$

The target server's private variables ($sChannel$ is public variable of server, for other entity can operate and modify $sChannel$ variable)
 $server_vars \triangleq \langle sState, sTCPLinkSet, sSvrInfo \rangle$

All the public variables of the model

$uChannel : Intf1, aChannel : Intf2, AuthChannel : Intf3, FwCtlChannel : Intf4, FwDataChannel : Intf5, sChannel : Intf6$
 $Public_vars \triangleq \langle uChannel, AuthChannel, FwCtlChannel, FwDataChannel, aChannel, sChannel \rangle$

All the variables that constitute the global state machine

$vars \triangleq \langle user_vars, sdpsvr_vars, fw_vars, attacker_vars, server_vars, Public_vars \rangle$

Common functions and operators

Sequence to Set

RECURSIVE $Seq2Set(-)$

$Seq2Set(S) \triangleq$

IF $S = \langle \rangle$ THEN $\{\}$

ELSE

```

LET  $i \triangleq \text{Head}(S)$ 
IN    $\{i\} \cup \text{Seq2Set}(\text{Tail}(S))$ 

```

Select local port randomly when client create socket connection

```

RandomPort(count, base)  $\triangleq$  (CHOOSE  $x \in (\text{count} + \text{base}) .. (\text{base} + 100) : \text{TRUE}$ )

```

simulate Symmetric-key algorithm: *Encrypt* function, this operator simplified by *XOR* operation

```

Encrypt( $d, k$ )  $\triangleq$ 
  LET RECURSIVE XorPureR( $-, -, -, -$ )
  XorPureR( $x, y, n, m$ )  $\triangleq$ 
    IF  $m = 0$ 
    THEN 0
    ELSE LET  $exp \triangleq 2^n$ 
          IN  $exp * (((x \div exp) + (y \div exp)) \% 2)$ 
              + XorPureR( $x, y, n + 1, m \div 2$ )
  IN IF  $d \geq k$  THEN XorPureR( $d, k, 0, d$ ) ELSE XorPureR( $k, d, 0, k$ )

```

simulate Symmetric-key algorithm: *Decrypt* function

```

DeCrypt( $d, k$ )  $\triangleq$  Encrypt( $d, k$ )

```

simulate *HMAC* function for SPA message

```

CalcHMAC( $n1, n2, n3, n4, n5, key$ )  $\triangleq$  Encrypt( $n1 + n2 + n3 + n4 + n5, key$ )

```

Init state description of legal user

User *Init*: Read configuration and ready to launch an access to target server

the init state is ready to start a auth session.

```

UsrInit  $\triangleq$   $\wedge uState = \text{"Start\_Auth"}$ 
            $\wedge uID = \text{ClientCfg.LoginID}$ 
            $\wedge Key = \text{ClientCfg.Key}$ 
            $\wedge uIP = \text{ClientCfg.SrcIp}$ 
            $\wedge uTstamp = 0$ 
            $\wedge uSDPSvrInfo = [IP \mapsto \text{SDPSvrCfg.IP}, Port \mapsto \text{SDPSvrCfg.Port}]$ 
            $\wedge uSvrInfo = [IP \mapsto \text{SvrCfg.IP}, Port \mapsto \text{SvrCfg.Port}]$ 
            $\wedge uTCPLinkSet = \{\}$ 
            $\wedge uChannel = \langle \rangle$ 

```


$$\wedge uAuthSession = \{\}$$

Next state actions of legal user

Action 1: *UsrCommitSpaAuth*

Legal user perform SPA (Single Packet Authentication) session by sending a SPA packet to *SDP* controller.

Variables changed: $\langle uState, uAuthSession, uTstamp, AuthChannel \rangle$

UsrCommitSpaAuth \triangleq

$\wedge uState = \text{"Start_Auth"}$

$\wedge uState' = \text{"Auth_End"}$

$\wedge uTstamp' = uTstamp + 1$ *uTstamp increases each session for anti-replay.*

$\wedge AuthChannel' = Append(AuthChannel,$

$[MsgID \mapsto \text{"SPA_AUTH"},$

$sIP \mapsto uIP,$

$sPort \mapsto RandomPort(uTstamp, USER_BASEPORT),$

$dIP \mapsto uSDPSvrInfo.IP,$

$dPort \mapsto uSDPSvrInfo.Port,$

$ClientID \mapsto uID,$

$Tstamp \mapsto uTstamp,$

$SvrIP \mapsto Encrypt(uSvrInfo.IP, Key),$

$SvrPort \mapsto Encrypt(uSvrInfo.Port, Key),$

$HMAC \mapsto CalcHMAC(uIP, uID, uTstamp, Encrypt(uSvrInfo.IP, Key),$

$Encrypt(uSvrInfo.Port, Key), Key),$

$Type \mapsto \text{"User"}]$

$)$

$\wedge uAuthSession' = uAuthSession \cup \{Head(AuthChannel')\}$ *Auth session is recorded in Log*

$\wedge UNCHANGED \langle uIP, uID, Key, uSDPSvrInfo, uSvrInfo, uTCPLinkSet \rangle$

$\wedge UNCHANGED sdpsvr_vars$

$\wedge UNCHANGED fw_vars$

$\wedge UNCHANGED attacker_vars$

$\wedge UNCHANGED server_vars$

$\wedge UNCHANGED \langle uChannel, FwCtlChannel, FwDataChannel, aChannel, sChannel \rangle$

$\wedge UNCHANGED \langle vars \setminus (uState, uTstamp, AuthChannel, uAuthSession) \rangle$

Action 2: *UsrConnectSvr*

Legal user try to access target service server after perform SPA (Single Packet Authentication) session.

the first action to connect the server is sending *TCP SYN* packets.

Variables changed: $\langle uState, uTCPLinkSet, FwDataChannel \rangle$

$LatestAuthSession \triangleq \text{CHOOSE } x \in uAuthSession : (\forall y \in uAuthSession : x.Tstamp \geq y.Tstamp)$

$UshrBulidTcpSynPkt \triangleq$

$[sIP \mapsto uIP,$
 $sPort \mapsto LatestAuthSession.sPort + 1,$ the new data access corresponds to the latest auth session by
 $dIP \mapsto uSvrInfo.IP,$
 $dPort \mapsto uSvrInfo.Port,$
 $Flg \mapsto \text{"TCP_SYN"},$
 $Type \mapsto \text{"User"}]$

$UshrConnectSvr \triangleq$

$\wedge uState = \text{"Auth_End"}$
 $\wedge uState' = \text{"Connecting"}$ the user now waiting for *TCP* handshakes over.
 $\wedge uAuthSession \neq \{\}$
 $\wedge uTCPLinkSet = \{\}$
 $\wedge uTCPLinkSet' = \{$ We assume the user only launch one data access session.
 $[sIP \mapsto UshrBulidTcpSynPkt.sIP,$
 $sPort \mapsto UshrBulidTcpSynPkt.sPort,$
 $dIP \mapsto UshrBulidTcpSynPkt.dIP,$
 $dPort \mapsto UshrBulidTcpSynPkt.dPort,$
 $State \mapsto \text{"SYN_SENT"}$ Create new *TCP* socket corresponds to the latest *Auth* session, *TCP* link
 $] \}$
 $\wedge FwDataChannel' = \text{Append}(FwDataChannel, UshrBulidTcpSynPkt)$ Send *TCP SYN* packet to *Fw*
 $\wedge \text{UNCHANGED } \langle uIP, uID, Key, uTstamp, uSDPSvrInfo, uSvrInfo, uAuthSession \rangle$
 $\wedge \text{UNCHANGED } sdpsvr_vars$
 $\wedge \text{UNCHANGED } fw_vars$
 $\wedge \text{UNCHANGED } attacker_vars$
 $\wedge \text{UNCHANGED } server_vars$
 $\wedge \text{UNCHANGED } \langle uChannel, AuthChannel, FwCtlChannel, aChannel, sChannel \rangle$

Action 3: *UshrRcvSynAck*

Legal user receive *TCP SYN Ack* packet from target server which indicates data *TCP* link established. This represents the user has successfully fulfilled a data access.

Variables changed: $\langle uState, uTCPLinkSet, uChannel, FwDataChannel \rangle$

$$\begin{aligned}
 HasMatchLink(p, LinkSet) &\triangleq \\
 \exists x \in LinkSet : &\quad \wedge p.sIP = x.dIP \\
 &\quad \wedge p.sPort = x.dPort \\
 &\quad \wedge p.dIP = x.sIP \\
 &\quad \wedge p.dPort = x.sPort
 \end{aligned}$$

$$\begin{aligned}
 GetMatchLink(p, LinkSet) &\triangleq \quad \text{get match } TCB \text{ (TCP control Block) for a received } TCP \text{ packet} \\
 \text{CHOOSE } x \in LinkSet : &\quad \wedge p.sIP = x.dIP \\
 &\quad \wedge p.sPort = x.dPort \\
 &\quad \wedge p.dIP = x.sIP \\
 &\quad \wedge p.dPort = x.sPort
 \end{aligned}$$

$$\begin{aligned}
 EndPointBulidTcpAckPkt(p, t) &\triangleq \quad \text{End point equipments might be a legal user or attacker} \\
 [sIP &\mapsto p.dIP, \\
 sPort &\mapsto p.dPort, \\
 dIP &\mapsto p.sIP, \\
 dPort &\mapsto p.sPort, \\
 Flg &\mapsto \text{"TCP_ACK"}, \\
 Type &\mapsto t]
 \end{aligned}$$

$$\begin{aligned}
 UstrcvSynAck &\triangleq \\
 \wedge uState = &\quad \text{"Connecting"} \\
 \wedge uTCPLinkSet &\neq \{\} \\
 \wedge uChannel &\neq \langle \rangle \\
 \wedge Head(uChannel).Flg &= \text{"TCP_SYN_ACK"} \\
 \wedge Head(uChannel).Type &= \text{"User"} \\
 \wedge HasMatchLink(Head(uChannel), uTCPLinkSet) &\quad \text{Receive } TCP_SYN_ACK \text{ from target server and match the conne} \\
 \wedge uTCPLinkSet' = (uTCPLinkSet \setminus \{GetMatchLink(Head(uChannel), uTCPLinkSet)\}) & \\
 \cup \{[sIP &\mapsto GetMatchLink(Head(uChannel), uTCPLinkSet).sIP,
 \end{aligned}$$

$$\begin{aligned}
& sPort \mapsto GetMatchLink(Head(uChannel), uTCPLinkSet).sPort, \\
& dIP \mapsto GetMatchLink(Head(uChannel), uTCPLinkSet).dIP, \\
& dPort \mapsto GetMatchLink(Head(uChannel), uTCPLinkSet).dPort, \\
& State \mapsto \text{"ESTABLISHED"} \quad \text{Update TCP link status to established} \\
&] \\
& \} \\
& \wedge uState' = \text{"Connected"} \quad \text{The user successfully access the target server} \\
& \wedge uChannel' = Tail(uChannel) \quad \text{Send TCP ACK packet (the last step of hand shake) to target server} \\
& \wedge FwDataChannel' = Append(FwDataChannel, EndPointBulidTcpAckPkt(Head(uChannel), " \\
& \wedge \text{UNCHANGED } \langle uIP, uID, Key, uTstamp, uSDPSvrInfo, uSvrInfo, uAuthSession \rangle \\
& \wedge \text{UNCHANGED } sdpsvr_vars \\
& \wedge \text{UNCHANGED } fw_vars \\
& \wedge \text{UNCHANGED } attacker_vars \\
& \wedge \text{UNCHANGED } server_vars \\
& \wedge \text{UNCHANGED } \langle AuthChannel, FwCtlChannel, aChannel, sChannel \rangle
\end{aligned}$$

Init state description of SDP Controller

SDP Controller Init: Read configuration and ready to provide SPA auth service.

$$\begin{aligned}
SDPSvrInit & \triangleq \wedge SDPSvrState = \text{"Work"} \\
& \wedge SDPSucSession = \{\} \\
& \wedge Account = \{[ClientID \mapsto ClientCfg.LoginID, Key \mapsto ClientCfg.Key]\} \quad \text{Load user} \\
& \wedge SDPSvrInfo = [IP \mapsto SDPSvrCfg.IP, Port \mapsto SDPSvrCfg.Port] \quad \text{Service IP and p} \\
& \wedge AuthChannel = \langle \rangle \\
& \wedge ReplayCount = 0 \\
& \wedge SpoofCount = 0 \\
& \wedge ReplaySession = \{\} \\
& \wedge SpoofSession = \{\}
\end{aligned}$$

Next state actions of SDP Controller

Action 4: *SDPSvrProcSpaAuth*

SDP Controller process received SPA message.

Scenario 3: Request from legal user, controller then instruct firewall to admit data access after authentication.

Scenario 1 2: controller recognize spoof and replay attack.

Variables changed: $\langle AuthChannel, SDPSucSession, ReplaySession, SpoofSession, ReplayCount, SpoofCount, FwCtlChannel \rangle$

if a coming SPA message SN match the history message recorded in anti-replay window

then it must be recognized as a replay attack packet.

$FindAntiReplay(msg, wnd) \triangleq$

IF $\exists r \in wnd : (msg.ClientID = r.ClientID \wedge msg.Tstamp = r.Tstamp)$

THEN

TRUE

ELSE

FALSE

For a recognized replay attack message, SDP controller drop it and recorded in the log.

$SDPSvrAntiReplayAtk \triangleq$

$\wedge AuthChannel' = Tail(AuthChannel)$ Drop packet

$\wedge ReplayCount' = ReplayCount + 1$ Increase statistics

$\wedge ReplaySession' = ReplaySession \cup \{Head(AuthChannel)\}$ Update log

For a recognized spoof attack message, SDP controller drop it and recorded in the log.

$SDPSvrAntiSpoof \triangleq$

$\wedge AuthChannel' = Tail(AuthChannel)$ Drop packet

$\wedge SpoofCount' = SpoofCount + 1$ Increase statistics

$\wedge SpoofSession' = SpoofSession \cup \{Head(AuthChannel)\}$ Update log

SDP controller implement authenticaiton triggered by a received SPA message

The authentication is implemented by recaculate the $HMAC$ according the user account $Info$

$SpaProcAuth(msg, accounts) \triangleq$

$\exists a \in accounts : (\wedge a.ClientID = msg.ClientID$ user ID must match

Recaculate the $HMAC$ value by using local stored user Key and then compare the value of corresponding field in SPA packet.

$\wedge CalcHMAC(msg.sIP, msg.ClientID, msg.Tstamp, msg.SvrIP, msg.SvrPort, a.Key) =$
 $)$

Get the correspond key by user ID from IAM stored accounts

$GetKey(id, accounts) \triangleq (\text{CHOOSE } a \in accounts : a.ClientID = id).Key$

SDP controller instruct $FireWall$ to config Acl Rule by sending instruction message to $FireWall$'s control plane channel

$$SDPSvrCfgFw(Acl, op) \triangleq$$

$$\wedge FwCtlChannel' = Append(FwCtlChannel, [Rule \mapsto Acl, op \mapsto op])$$

$$SDPSvrProcSpaAuth \triangleq$$

$$\wedge SDPSvrState = \text{"Work"}$$

$$\wedge AuthChannel \neq \langle \rangle$$

$$\wedge Head(AuthChannel).MsgID = \text{"SPA_AUTH"} \quad \text{check the packet is SPA message}$$

$$\wedge Head(AuthChannel).dIP = SDPSvrInfo.IP$$

$$\wedge Head(AuthChannel).dPort = SDPSvrInfo.Port$$

$$\wedge \text{IF } FindAntiReplay(Head(AuthChannel), SDPSucSession) = \text{TRUE} \quad \text{case 1: the packet is a replay message}$$

$$\text{THEN}$$

$$\wedge SDPSvrAntiReplayAtk \quad \text{drop packets and record exception into log}$$

$$\wedge \text{UNCHANGED } user_vars$$

$$\wedge \text{UNCHANGED } \langle SDPSvrState, SDPSucSession, Account, SDPSvrInfo, SpoofCount, SpoofSource \rangle$$

$$\wedge \text{UNCHANGED } fw_vars$$

$$\wedge \text{UNCHANGED } attacker_vars$$

$$\wedge \text{UNCHANGED } server_vars$$

$$\wedge \text{UNCHANGED } \langle uChannel, FwCtlChannel, FwDataChannel, aChannel, sChannel \rangle$$

$$\text{ELSE}$$

$$\wedge \text{IF } SpaProcAuth(Head(AuthChannel), Account) = \text{FALSE} \quad \text{case 2: it is a spoof message or from unauthorized source}$$

$$\text{THEN}$$

$$\wedge SDPSvrAntiSpoof \quad \text{drop packets and record exception into log}$$

$$\wedge \text{UNCHANGED } user_vars$$

$$\wedge \text{UNCHANGED } \langle SDPSvrState, SDPSucSession, Account, SDPSvrInfo, ReplayCount, SpoofSource \rangle$$

$$\wedge \text{UNCHANGED } fw_vars$$

$$\wedge \text{UNCHANGED } attacker_vars$$

$$\wedge \text{UNCHANGED } server_vars$$

$$\wedge \text{UNCHANGED } \langle uChannel, FwCtlChannel, FwDataChannel, aChannel, sChannel \rangle$$

$$\text{ELSE} \quad \text{case 3: Authenticated successfully, then send instruction to FW to allow data access towards source}$$

$$\wedge SDPSvrCfgFw([sIP \mapsto Head(AuthChannel).sIP,$$

$$sPort \mapsto MATCH_ANY, \quad \text{this Acl Rule is 3 tuple, for data access source}]$$

$$dIP \mapsto DeCrypt(Head(AuthChannel).SvrIP, GetKey(Head(AuthChannel).SvrKey)),$$

$$dPort \mapsto DeCrypt(Head(AuthChannel).SvrPort, GetKey(Head(AuthChannel).SvrKey))])$$

$$\begin{aligned}
& protocol \mapsto \text{"TCP"}, \\
& action \mapsto \text{"Accept"}], \\
& \text{"Add"} \quad \text{The instruction code is to Add a new rule.} \\
&) \\
& \wedge SDPSucSession' = SDPSucSession \cup \{Head(AuthChannel)\} \quad \text{record in log} \\
& \wedge AuthChannel' = Tail(AuthChannel) \\
& \wedge \text{UNCHANGED } user_vars \\
& \wedge \text{UNCHANGED } \langle SDPSvrState, Account, SDPSvrInfo, ReplayCount, SpoofCount, ReplaySession, S \rangle \\
& \wedge \text{UNCHANGED } fw_vars \\
& \wedge \text{UNCHANGED } attacker_vars \\
& \wedge \text{UNCHANGED } server_vars \\
& \wedge \text{UNCHANGED } \langle uChannel, FwDataChannel, aChannel, sChannel \rangle
\end{aligned}$$

Init state description of FireWall

Fire wall init: power on and enter work state, by default, it works in deny mode and will drop any ingress data packets.

$$\begin{aligned}
FwInit & \triangleq \wedge FwCtlChannel = \langle \rangle \\
& \wedge FwDataChannel = \langle \rangle \\
& \wedge FwState = \text{"Work"} \\
& \wedge AclRuleSet = \{\} \\
& \wedge AgedRuleSet = \{\} \\
& \wedge DropPackets = \{\}
\end{aligned}$$

Next state actions of FireWall

Action 5: *FwProcAclCfg*

FireWall receive *Acl Rule* config instruction from control plane channel, and hence create a 3 Tuple rule for data access

Variables changed: $\langle FwCtlChannel, AclRuleSet \rangle$

$$\begin{aligned}
FwProcAclCfg & \triangleq \\
& \wedge FwState = \text{"Work"} \\
& \wedge FwCtlChannel \neq \langle \rangle \\
& \wedge Head(FwCtlChannel).op = \text{"Add"} \quad \text{Check instruction message format} \\
& \wedge AclRuleSet' = AclRuleSet \cup \{Head(FwCtlChannel).Rule\} \quad \text{Update local maintained rule table} \\
& \wedge FwCtlChannel' = Tail(FwCtlChannel)
\end{aligned}$$

$\wedge \text{UNCHANGED } user_vars$
 $\wedge \text{UNCHANGED } sdpsvr_vars$
 $\wedge \text{UNCHANGED } attacker_vars$
 $\wedge \text{UNCHANGED } server_vars$
 $\wedge \text{UNCHANGED } \langle FwState, AgedRuleSet, DropPackets \rangle$
 $\wedge \text{UNCHANGED } \langle uChannel, AuthChannel, FwDataChannel, aChannel, sChannel \rangle$

Action 6: *FwProcEndPointAccess*

FireWall receive a ingress data packet from end point side and implement filtering function according to *L3 ACL Rule*

Variables changed: $\langle sChannel, AclRuleSet, FwDataChannel, DropPackets \rangle$

Whether the *TCP* packet match a given 3 tuple rule.

$AclMatch3Tuple(p, Acl) \triangleq$
 $\exists r \in Acl : (\wedge p.sIP = r.sIP$
 $\wedge p.dIP = r.dIP$
 $\wedge r.sPort = MATCH_ANY$ don't care source port value
 $\wedge p.dPort = r.dPort$
 $\wedge r.action = \text{"Accept"})$

Whether the *TCP* packet match a given 4 tuple rule.

$AclMatch4Tuple(p, Acl) \triangleq$
 $\exists r \in Acl : (\wedge p.sIP = r.sIP$ (*sIP,sPort,dIP,dPort*) must match exactly
 $\wedge p.dIP = r.dIP$
 $\wedge r.sPort \neq MATCH_ANY$
 $\wedge r.sPort = p.sPort$
 $\wedge p.dPort = r.dPort$
 $\wedge r.action = \text{"Accept"})$

The firewall automatically create an exactly matched 4 tuple rule according to a received new *TCP* link packets

The 3 tuple rule configed by *SDP* controller by default with RELATED attribute, which means a new *TCP* link packets can trigger creating of a exactly matched 4 tuple rule.

$CreateRelatedRule(p) \triangleq$
 $[sIP \quad \mapsto p.sIP,$
 $sPort \quad \mapsto p.sPort,$

$dIP \mapsto p.dIP,$
 $dPort \mapsto p.dPort,$
 $protocol \mapsto \text{"TCP"},$
 $action \mapsto \text{"Accept"}]$

$FwProcEndPointAccess \triangleq$

$\wedge FwState = \text{"Work"}$

$\wedge FwDataChannel \neq \langle \rangle$

$\wedge (\vee Head(FwDataChannel).Flg = \text{"TCP_SYN"} \quad \text{to simplify the model, we only consider } TCP \text{ connection procedure for}$
 $\vee Head(FwDataChannel).Flg = \text{"TCP_ACK"} \quad \text{the end point equipments as } TCP \text{ client, only send } TCP_SYN \text{ and } TCP_ACK$
 $)$

$\wedge (\text{IF } AclMatch4Tuple(Head(FwDataChannel), AclRuleSet)$

THEN $CASE1$: the incoming packets exactly match a 4 tuple rule

$\wedge sChannel' = Append(sChannel, Head(FwDataChannel)) \quad \text{route the packets to target server}$

$\wedge FwDataChannel' = Tail(FwDataChannel)$

$\wedge AclRuleSet' = AclRuleSet$

$\wedge DropPackets' = DropPackets$

ELSE

$(\text{IF } AclMatch3Tuple(Head(FwDataChannel), AclRuleSet)$

THEN $CASE2$: the incoming packets only match a 3 tuple rule

$\wedge sChannel' = Append(sChannel, Head(FwDataChannel)) \quad \text{route the packets to target server}$

$\wedge AclRuleSet' = AclRuleSet \cup \{CreateRelatedRule(Head(FwDataChannel))\}$

$\wedge FwDataChannel' = Tail(FwDataChannel) \quad \text{This is a new } TCP \text{ link, so create a exactly matched 4 tuple rule and}$

$\wedge DropPackets' = DropPackets$

ELSE $CASE3$: the incoming packets not match any rule

$\wedge FwDataChannel' = Tail(FwDataChannel)$

$\wedge AclRuleSet' = AclRuleSet$

$\wedge sChannel' = sChannel \quad \text{just drop the packets}$

$\wedge DropPackets' = DropPackets \cup \{Head(FwDataChannel)\} \quad \text{record it into exception log}$

$)$

$)$

$\wedge \text{UNCHANGED } user_vars$

$\wedge \text{UNCHANGED } sdpsvr_vars$

$\wedge \text{UNCHANGED } \textit{attacker_vars}$
 $\wedge \text{UNCHANGED } \langle \textit{FwState}, \textit{AgedRuleSet} \rangle$
 $\wedge \text{UNCHANGED } \textit{server_vars}$
 $\wedge \text{UNCHANGED } \langle \textit{uChannel}, \textit{AuthChannel}, \textit{FwCtlChannel}, \textit{aChannel} \rangle$

Action 7: *FwProcAclTimeOut*

A 3 Tuple *Acl* rule configed by *SDP* controller automatically deleted due to aging mechanism.

Variables changed: $\langle \textit{AclRuleSet}, \textit{AgedRuleSet} \rangle$

FwProcAclTimeOut \triangleq

$\wedge \textit{FwState} = \text{"Work"}$
 $\wedge \textit{AclRuleSet} \neq \{\}$
 $\wedge \exists r \in \textit{AclRuleSet} : r.\textit{sPort} = \textit{MATCH_ANY}$ only 3 tuple rule with aging mechanism
 $\wedge \textit{AclRuleSet}' = \textit{AclRuleSet} \setminus \{\text{CHOOSE } r \in \textit{AclRuleSet} : r.\textit{sPort} = \textit{MATCH_ANY}\}$ aging and
 $\wedge \textit{AgedRuleSet}' = \textit{AgedRuleSet} \cup \{\text{CHOOSE } r \in \textit{AclRuleSet} : r.\textit{sPort} = \textit{MATCH_ANY}\}$ record
 $\wedge \text{UNCHANGED } \textit{user_vars}$
 $\wedge \text{UNCHANGED } \textit{sdpsvr_vars}$
 $\wedge \text{UNCHANGED } \textit{attacker_vars}$
 $\wedge \text{UNCHANGED } \langle \textit{FwState}, \textit{DropPackets} \rangle$
 $\wedge \text{UNCHANGED } \textit{server_vars}$
 $\wedge \text{UNCHANGED } \textit{Public_vars}$

Init state description of target service server

Target *TCP* server init and begin listening on its service *IP* and *Port*.

ServerInit \triangleq $\wedge \textit{sState} = \text{"Listen"}$
 $\wedge \textit{sSvrInfo} = [\textit{IP} \mapsto \textit{SvrCfg.IP}, \textit{Port} \mapsto \textit{SvrCfg.Port}]$ Load configuration
 $\wedge \textit{sTCPLinkSet} = \{\}$
 $\wedge \textit{sChannel} = \langle \rangle$

Next state actions of target service server

Action 8: *ServerRcvTCPSyn*

Target server recieve a *TCP SYN* packet from client side and try to allocate a new *TCB*.

Because the Firewall dose not filter server to endpoint direction packets, so to simplify the model, the server directly se

uChannel.

Variables changed: $\langle sTCPLinkSet, sChannel, uChannel, aChannel \rangle$

Whether the coming packet indicates a new connection

$$NewLink(p, LinkSet) \triangleq$$

```

  IF  $LinkSet = \{\}$ 
  THEN
    TRUE
  ELSE
    (IF  $\forall x \in LinkSet : ($  without matching  $TCB$  ( $TCP$  Control Block)
       $\vee x.sIP \neq p.sIP$ 
       $\vee x.dIP \neq p.dIP$ 
       $\vee x.sPort \neq p.sPort$ 
       $\vee x.dPort \neq p.dPort)$ 
    THEN
      TRUE
    ELSE
      FALSE)

```

$$ServerRcvTCPSyn \triangleq$$

```

   $\wedge sState = \text{"Listen"}$ 
   $\wedge sChannel \neq \langle \rangle$ 
   $\wedge Head(sChannel).Flg = \text{"TCP\_SYN"}$ 
   $\wedge Head(sChannel).dIP = sSvrInfo.IP$  check incoming packets format
   $\wedge Head(sChannel).dPort = sSvrInfo.Port$ 
   $\wedge sChannel' = Tail(sChannel)$ 
   $\wedge (IF NewLink(Head(sChannel), sTCPLinkSet)$ 
    THEN CASE1 : New  $TCP$  SYN packets
       $\wedge sTCPLinkSet' = sTCPLinkSet \cup \{$  create a  $TCB$  and update local link set.
         $[dIP \mapsto Head(sChannel).sIP,$ 
         $dPort \mapsto Head(sChannel).sPort,$ 
         $sIP \mapsto Head(sChannel).dIP,$ 
         $sPort \mapsto Head(sChannel).dPort,$ 
         $Type \mapsto Head(sChannel).Type,$ 

```

```

    State    ↦ "SYN_RCVD"    the TCB 's state is SYN_RCVD
  ]]
  ∧ (IF Head(sChannel).Type = "User"
    THEN  If the client is legal user, then send TCP_SYN_ACK packet to legal user.
    ( ∧ uChannel' = Append(uChannel, [
      sIP      ↦ Head(sChannel).dIP,
      sPort    ↦ Head(sChannel).dPort,
      dIP      ↦ Head(sChannel).sIP,
      dPort    ↦ Head(sChannel).sPort,
      Flg      ↦ "TCP_SYN_ACK",
      Type     ↦ Head(sChannel).Type]
    )
    ∧ aChannel' = aChannel
  )
  ELSE  If the client is attacker, then send TCP_SYN_ACK packet to attacker.
  ( ∧ aChannel' = Append(aChannel, [
    sIP      ↦ Head(sChannel).dIP,
    sPort    ↦ Head(sChannel).dPort,
    dIP      ↦ Head(sChannel).sIP,
    dPort    ↦ Head(sChannel).sPort,
    Flg      ↦ "TCP_SYN_ACK",
    Type     ↦ Head(sChannel).Type]
  )
  ∧ uChannel' = uChannel
  )
  )
  )
  ELSE  CASE2 : duplicated TCP SYN packet,just neglect it for we don't focus on TCP SYN Flood attack.
  ∧ sTCPLinkSet' = sTCPLinkSet
  ∧ aChannel' = aChannel
  ∧ uChannel' = uChannel
  )
  ∧ UNCHANGED user_vars
  ∧ UNCHANGED sdpsvr_vars

```

\wedge UNCHANGED $attacker_vars$
 \wedge UNCHANGED $\langle sState, sSvrInfo \rangle$
 \wedge UNCHANGED fw_vars
 \wedge UNCHANGED $\langle AuthChannel, FwCtlChannel, FwDataChannel \rangle$

Action 9: *ServerRcvTCPSyn*

Target server receive a *TCP ACK* packet that acknowledge the last *SYN_ACK*, then establish the *TCP* link with the client.

Variables changed: $\langle sTCPLinkSet, sChannel \rangle$

$ServerRcvTcpAck \triangleq$

$\wedge sState = \text{"Listen"}$
 $\wedge sChannel \neq \langle \rangle$
 $\wedge Head(sChannel).Flg = \text{"TCP_ACK"}$ check incoming packets format
 $\wedge HasMatchLink(Head(sChannel), sTCPLinkSet)$
 $\wedge GetMatchLink(Head(sChannel), sTCPLinkSet).State = \text{"SYN_RCVD"}$ the matched *TCB* state must be *SYN*
 $\wedge sChannel' = Tail(sChannel)$
 $\wedge sTCPLinkSet' = (sTCPLinkSet \setminus \{GetMatchLink(Head(sChannel), sTCPLinkSet)\})$
 $\quad \cup \{ [\begin{array}{ll} sIP & \mapsto GetMatchLink(Head(sChannel), sTCPLinkSet).sIP, \\ sPort & \mapsto GetMatchLink(Head(sChannel), sTCPLinkSet).sPort, \\ dIP & \mapsto GetMatchLink(Head(sChannel), sTCPLinkSet).dIP, \\ dPort & \mapsto GetMatchLink(Head(sChannel), sTCPLinkSet).dPort, \\ Type & \mapsto GetMatchLink(Head(sChannel), sTCPLinkSet).Type, \\ State & \mapsto \text{"ESTABLISHED"} \end{array} \quad \begin{array}{l} \text{Update } TCP \text{ link state to } ESTABLISHED. \\ \text{This indicates the client has successfully accessed target server} \end{array}] \}$
 \wedge UNCHANGED $user_vars$
 \wedge UNCHANGED $sdpsvr_vars$
 \wedge UNCHANGED $attacker_vars$
 \wedge UNCHANGED $\langle sState, sSvrInfo \rangle$
 \wedge UNCHANGED fw_vars
 \wedge UNCHANGED $\langle uChannel, AuthChannel, FwCtlChannel, FwDataChannel, aChannel \rangle$

Init state description of Attacker

Attacker init and capable of sniffing the packets on the local network.

$AttackerInit \triangleq \wedge aState = \text{"Listen"}$

$$\begin{aligned}
& \wedge AuthKnowledge = \{\} \\
& \wedge aSession = \{\} \\
& \wedge aTCPLinkSet = \{\} \\
& \wedge aChannel = \langle \rangle \\
& \wedge sniffCount = 0 \\
& \wedge CapAuthMsg = \{\} \\
& \wedge aCounter = 0 \\
& \wedge aIP = AttackerCfg.SrcIp \\
& \wedge DataKnowledge = \{\} \\
& \wedge CapDataMsg = \{\}
\end{aligned}$$

Next state actions of attacker

Action 10: *AttackerSniffAuthChannel*

Attacker eavesdropping SPA message from legal user to *SDP* controller by sniffing the *Auth* channel.

Once a new SPA message is captured,attacker will duplicate it into its current Auth-knowledge set.

We don't guarantee every new SPA message can be captured by attacker, it only has the opportunity to get each message.

Variables changed: $\langle AuthKnowledge, CapAuthMsg, sniffCount \rangle$

Select a new (which means unknown to attacker till now) SPA message from the *Auth* channel

to simulate a successful sniff.

$SelectNewAuthMsg(MsgQ, known) \triangleq$

IF $known \neq \{\}$

THEN for a dedicate user, the difference among SPA messages is the value of *SN* (counter) field.

CHOOSE $S \in \text{SUBSET } Seq2Set(MsgQ) : (\forall x \in S : (\forall y \in known : x.Timestamp \neq y.Timestamp))$

ELSE

$Seq2Set(MsgQ)$

For the attacker can also insert fake messages into channel, but

for both data and auth channel, attacker only wants to capture messages from legal user.

so the *PureChannel()* function is to select the set of user's messages.

$PureChannel(S) \triangleq SelectSeq(S, \text{LAMBDA } x : x.Type = \text{"User"})$

$AttackerSniffAuthChannel \triangleq$

$\wedge aState = \text{"Listen"}$

$\wedge \text{PureChannel}(\text{AuthChannel}) \neq \langle \rangle$ pre-condition: there exists attacker unknown legal user originated SPA messages on t
 $\wedge \exists i \in 1 \dots \text{Len}(\text{PureChannel}(\text{AuthChannel})) :$
 $(\forall x \in \text{CapAuthMsg} : \text{PureChannel}(\text{AuthChannel})[i].\text{Tstamp} \neq x.\text{Tstamp})$
 $\wedge \text{AuthKnowledge}' = \text{AuthKnowledge} \cup$ post-condition: attacker learned new intelligence by a successful sniffing.
 $\text{SelectNewAuthMsg}(\text{PureChannel}(\text{AuthChannel}), \text{CapAuthMsg})$
 $\wedge \text{CapAuthMsg}' = \text{CapAuthMsg} \cup$ All the captured message in history recorded in *Log*.
 $\text{SelectNewAuthMsg}(\text{PureChannel}(\text{AuthChannel}), \text{CapAuthMsg})$
 $\wedge \text{sniffCount}' = \text{sniffCount} + 1$ increase statistics
 $\wedge \text{UNCHANGED } \text{user_vars}$
 $\wedge \text{UNCHANGED } \text{sdpsvr_vars}$
 $\wedge \text{UNCHANGED } \text{fw_vars}$
 $\wedge \text{UNCHANGED } \text{server_vars}$
 $\wedge \text{UNCHANGED } \langle aState, aSession, aTCPLinkSet, aCounter, aIP, \text{DataKnowledge}, \text{CapDataMsg} \rangle$
 $\wedge \text{UNCHANGED } \text{Public_vars}$

Action 11: *AttackerSniffDataChannel*

Attacker eavesdropping data access from legal user to target server by sniffing the data channel.

Once a new data packet is captured, it will duplicate it into its current data-knowledge set.

We don't guarantee every new data packets can be captured by attacker, it only has the opportunity to get each packets.

Variables changed: $\langle \text{DataKnowledge}, \text{CapDataMsg} \rangle$

Select a new (which means unknown to attacker till now) data packets being sent from user to *FireWall*

to simulate a successful sniff.

$\text{SelectNewDataMsg}(\text{MsgQ}, \text{known}) \triangleq$

IF $\text{known} \neq \{\}$

THEN The aim of capturing user data access packets is to get the exposure service info about the target server
so $(dIP, dPort)$ is the key knowledge.

CHOOSE $S \in \text{SUBSET } \text{Seq2Set}(\text{MsgQ}) : (\forall x \in S : (\forall y \in \text{known} : (x.dIP \neq y.dIP \wedge x.dPort \neq y.dPort)))$

ELSE

$\text{Seq2Set}(\text{MsgQ})$

AttackerSniffDataChannel \triangleq

$\wedge aState = \text{"Listen"}$

$\wedge \text{PureChannel}(\text{FwDataChannel}) \neq \langle \rangle$ pre-condition: there exists attacker unknown target server service info.

$$\begin{aligned}
& \wedge \exists i \in 1 \dots \text{Len}(\text{PureChannel}(\text{FwDataChannel})) : \\
& \quad (\forall x \in \text{CapDataMsg} : \quad \wedge \text{PureChannel}(\text{FwDataChannel})[i].dIP \neq x.dIP \\
& \quad \quad \wedge \text{PureChannel}(\text{FwDataChannel})[i].dPort \neq x.dPort \\
& \quad \quad \wedge \text{PureChannel}(\text{FwDataChannel})[i].Flg = \text{"TCP_SYN"} \quad \text{A new TCP} \\
& \quad) \\
& \wedge \text{DataKnowledge}' = \text{DataKnowledge} \cup \quad \text{post-condition: attacker learned new intelligence by a successful} \\
& \quad \text{SelectNewDataMsg}(\text{PureChannel}(\text{FwDataChannel}), \text{CapDataMsg}) \\
& \wedge \text{CapDataMsg}' = \text{CapDataMsg} \cup \quad \text{All the captured packets in history recorded in Log.} \\
& \quad \text{SelectNewDataMsg}(\text{PureChannel}(\text{FwDataChannel}), \text{CapDataMsg}) \\
& \wedge \text{sniffCount}' = \text{sniffCount} + 1 \quad \text{increase statistics} \\
& \wedge \text{UNCHANGED } \text{user_vars} \\
& \wedge \text{UNCHANGED } \text{sdpsvr_vars} \\
& \wedge \text{UNCHANGED } \text{fw_vars} \\
& \wedge \text{UNCHANGED } \text{server_vars} \\
& \wedge \text{UNCHANGED } \langle aState, \text{AuthKnowledge}, aSession, aTCPLinkSet, \text{CapAuthMsg}, aCounter, a \rangle \\
& \wedge \text{UNCHANGED } \text{Public_vars}
\end{aligned}$$

Action 12: *AttackerSpoofAuth*

Attacker build and send fake SPA messages to *SDP* controller by spoofing legal user.

The making of each fake message is based on one corresponding element in the Auth-Knowledge set, one element in the can only be used to produce one spoof message.

The spoof message re-use the legal user's *ID* and all other fields except *SN* (*Tstamp*) field increasing to avoid anti-rep

Variables changed: $\langle aSession, \text{AuthChannel}, \text{AuthKnowledge} \rangle$

make a spoof message according a captured auth knowledge

$\text{SpoofAuthMsg}(m) \triangleq$

$$\begin{aligned}
& [\text{MsgID} \mapsto \text{"SPA_AUTH"}, \\
& \quad \text{sIP} \mapsto m.\text{sIP}, \\
& \quad \text{sPort} \mapsto m.\text{sPort}, \\
& \quad \text{dIP} \mapsto m.\text{dIP}, \\
& \quad \text{dPort} \mapsto m.\text{dPort}, \\
& \quad \text{ClientID} \mapsto m.\text{ClientID}, \\
& \quad \text{Tstamp} \mapsto m.\text{Tstamp} + 1, \quad \text{SN number increase}
\end{aligned}$$

$SvrIP \mapsto m.SvrIP,$
 $SvrPort \mapsto m.SvrPort,$
 $HMAC \mapsto m.HMAC,$
 $Type \mapsto \text{"Attacker"}$

$AttackerSpoofAuth \triangleq$

$\wedge AuthKnowledge \neq \{\}$ pre-condition: there exists intellicence about user's auth message learned by sniffing.
 $\wedge AuthChannel' = Append(AuthChannel, SpoofAuthMsg(CHOOSE $x \in AuthKnowledge : TRUE$))$ send new bui
 $\wedge aSession' = aSession \cup \{SpoofAuthMsg(CHOOSE $x \in AuthKnowledge : TRUE$)\}$ new Attack session is recorded
 $\wedge AuthKnowledge' = AuthKnowledge \setminus \{CHOOSE $x \in AuthKnowledge : TRUE$ \}$ one knowledge item can be only be
 $\wedge UNCHANGED\ user_vars$
 $\wedge UNCHANGED\ sdpsvr_vars$
 $\wedge UNCHANGED\ fw_vars$
 $\wedge UNCHANGED\ server_vars$
 $\wedge UNCHANGED\ \langle aState, aTCPLinkSet, sniffCount, CapAuthMsg, aCounter, aIP, DataKnowledge, CapData$
 $\wedge UNCHANGED\ \langle uChannel, FwCtlChannel, FwDataChannel, aChannel, sChannel \rangle$

Action 13: *AttackerReplayAuth*

Attacker build and send fake SPA messages to *SDP* controller by replay legal user's message.

The making of each fake message is based on one corrsponding element in the Auth-Knowledge set, one element in the knowledge set can only be used to produce one replay message.

Variables changed: $\langle aSession, AuthChannel, AuthKnowledge \rangle$

$ReplayAuthMsg(m) \triangleq$ make replay message by duplication.

$[MsgID \mapsto \text{"SPA_AUTH"},$
 $sIP \mapsto m.sIP,$
 $sPort \mapsto m.sPort,$
 $dIP \mapsto m.dIP,$
 $dPort \mapsto m.dPort,$
 $ClientID \mapsto m.ClientID,$
 $Tstamp \mapsto m.Tstamp,$
 $SvrIP \mapsto m.SvrIP,$
 $SvrPort \mapsto m.SvrPort,$

$HMAC \mapsto m.HMAC,$
 $Type \mapsto \text{"Attacker"}$

$AttackerReplayAuth \triangleq$

$\wedge AuthKnowledge \neq \{\}$ pre-condition: there exists intellicence about user's auth message learned by sniffing.
 $\wedge AuthChannel' = Append(AuthChannel, ReplayAuthMsg(CHOOSE $x \in AuthKnowledge : TRUE$))$
 $\wedge aSession' = aSession \cup \{ReplayAuthMsg(CHOOSE $x \in AuthKnowledge : TRUE$)\}$ new Attack sess
 $\wedge AuthKnowledge' = AuthKnowledge \setminus \{CHOOSE $x \in AuthKnowledge : TRUE$ \}$ one knowledge item
 $\wedge UNCHANGED \ user_vars$
 $\wedge UNCHANGED \ sdpsvr_vars$
 $\wedge UNCHANGED \ fw_vars$
 $\wedge UNCHANGED \ server_vars$
 $\wedge UNCHANGED \langle aState, aTCPLinkSet, sniffCount, CapAuthMsg, aCounter, aIP, DataKnowled$
 $\wedge UNCHANGED \langle uChannel, FwCtlChannel, FwDataChannel, aChannel, sChannel \rangle$

Action 14: *AttackerBrutalAttck*

Attacker try to brutally connect the target server only by the intelligence got from user's *Auth* message.

The making of each tcp connection is based on one auth attack session, one element in the history auth attack session can only be used to produce one brutal attack message.

Variables changed: $\langle aSession, AuthChannel, AuthKnowledge, FwDataChannel \rangle$

$AttckerBulidTcpSynPktByAuthMsg(m) \triangleq$ attack try to connect target service server as a *TCP* client, send

$[sIP \mapsto aIP,$
 $sPort \mapsto RandomPort(aCounter, ATTACKER_BASEPORT),$ local port generated randomly
 $dIP \mapsto m.SvrIP,$ target server info directly get from previously auth message m .
 $dPort \mapsto m.SvrPort,$
 $Flg \mapsto \text{"TCP_SYN"},$
 $Type \mapsto \text{"Attacker"}]$

$Exist_aSession4Battck \triangleq$

$\exists x \in aSession : (\forall y \in aTCPLinkSet : x.Tstamp \neq y.AuthID)$

$Get_aSession4Battck \triangleq$

choose an historic auth attack session to make a brutal data access attack

$CHOOSE x \in aSession : (\forall y \in aTCPLinkSet : x.Tstamp \neq y.AuthID)$

$$\begin{aligned}
& AttackerBrutalAttck \triangleq \\
& \quad \wedge aSession \neq \{\} \\
& \quad \wedge (\vee aTCPLinkSet = \{\} \\
& \quad \quad \vee (\wedge aTCPLinkSet \neq \{\} \quad \text{pre-condition: there exists at least one auth attack session without brutal attack had happened} \\
& \quad \quad \quad \wedge Exist_aSession4Battck \\
& \quad \quad) \\
& \quad) \\
& \quad \wedge aCounter' = aCounter + 1 \quad \text{acounter is used to build the local port value of the } TCP \text{ connection, increase each time to a} \\
& \quad \wedge FwDataChannel' = Append(FwDataChannel, AttckerBulidTcpSynPktByAuthMsg(Get_aSession4Battck)), \\
& \quad \wedge aTCPLinkSet' = aTCPLinkSet \cup \{ \quad \text{maintain local } TCP \text{ socket} \\
& \quad \quad [sIP \quad \mapsto AttckerBulidTcpSynPktByAuthMsg(Get_aSession4Battck).sIP, \\
& \quad \quad \quad sPort \quad \mapsto AttckerBulidTcpSynPktByAuthMsg(Get_aSession4Battck).sPort, \\
& \quad \quad \quad dIP \quad \mapsto AttckerBulidTcpSynPktByAuthMsg(Get_aSession4Battck).dIP, \\
& \quad \quad \quad dPort \quad \mapsto AttckerBulidTcpSynPktByAuthMsg(Get_aSession4Battck).dPort, \\
& \quad \quad \quad State \quad \mapsto "SYN_SENT", \quad \text{the tcp link's state now is } SYN_SENT \\
& \quad \quad \quad AuthID \quad \mapsto Get_aSession4Battck.Tstamp \quad \text{this field is used to relate to the corresponding auth attack session.} \\
& \quad \quad] \} \\
& \quad \wedge \text{UNCHANGED } user_vars \\
& \quad \wedge \text{UNCHANGED } sdpsvr_vars \\
& \quad \wedge \text{UNCHANGED } fw_vars \\
& \quad \wedge \text{UNCHANGED } server_vars \\
& \quad \wedge \text{UNCHANGED } \langle aState, AuthKnowledge, aSession, sniffCount, CapAuthMsg, aIP, DataKnowledge, CapDa \\
& \quad \wedge \text{UNCHANGED } \langle uChannel, AuthChannel, FwCtlChannel, aChannel, sChannel \rangle
\end{aligned}$$

Action 15: *AttackerInspectSvr*

Attacker try to connect target server according to intelligence of previously captured data plane traffic info by sending *TCP SYN* pa

The making of each tcp connection is based on one element in the Data Knowledge set which is learned by sniffing legal user's data a
with target server.

one knowledge can only be used to produce one inspection attempt.

Variables changed: $\langle aCounter, FwDataChannel, aTCPLinkSet, DataKnowledge \rangle$

$$\begin{aligned}
& AttckerBulidTcpSynPktByData(p) \triangleq \\
& \quad [sIP \quad \mapsto aIP,
\end{aligned}$$

$$\begin{aligned}
sPort &\mapsto \text{RandomPort}(aCounter, \text{ATTACKER_BASEPORT}), \\
dIP &\mapsto p.dIP, \\
dPort &\mapsto p.dPort, \\
Flg &\mapsto \text{"TCP_SYN"}, \\
Type &\mapsto \text{"Attacker"}]
\end{aligned}$$

$$\text{AttackerInspectSvr} \triangleq$$

$$\begin{aligned}
&\wedge \text{DataKnowledge} \neq \{\} \quad \text{pre-condition: there exists learned data knowledge that still not used to make a inspection} \\
&\wedge aCounter' = aCounter + 1 \quad \text{aCounter is used to build the local port value of the TCP connection, increase} \\
&\wedge \text{FwDataChannel}' = \text{Append}(\text{FwDataChannel}, \text{AttckerBulidTcpSynPktByData}(\text{CHOOSE } x \in \text{DataKnowledge} : \text{TRUE}).sIP, \\
&\quad \text{AttckerBulidTcpSynPktByData}(\text{CHOOSE } x \in \text{DataKnowledge} : \text{TRUE}).sPort, \\
&\quad \text{AttckerBulidTcpSynPktByData}(\text{CHOOSE } x \in \text{DataKnowledge} : \text{TRUE}).dIP, \\
&\quad \text{AttckerBulidTcpSynPktByData}(\text{CHOOSE } x \in \text{DataKnowledge} : \text{TRUE}).dPort, \\
&\quad \text{"SYN_SENT"}, \quad \text{the tcp link's state now is SYN_SENT}) \\
&\quad \text{UNKNOWN_AUTH_ID} \quad \text{This tcp connection is built accroding to captured data plane}) \\
&] \} \\
&\wedge \text{DataKnowledge}' = \text{AuthKnowledge} \setminus \{\text{CHOOSE } x \in \text{DataKnowledge} : \text{TRUE}\} \quad \text{one knowledge item is used} \\
&\wedge \text{UNCHANGED } user_vars \\
&\wedge \text{UNCHANGED } sdpsvr_vars \\
&\wedge \text{UNCHANGED } fw_vars \\
&\wedge \text{UNCHANGED } server_vars \\
&\wedge \text{UNCHANGED } \langle aState, \text{AuthKnowledge}, aSession, sniffCount, CapAuthMsg, aIP, CapDataMsg \rangle \\
&\wedge \text{UNCHANGED } \langle uChannel, \text{AuthChannel}, FwCtlChannel, aChannel, sChannel \rangle
\end{aligned}$$

Action 16: *AttackerRcvSynAck*

Attacker's inspection TCP connection established triggered by receiving TCP SYN ACK packet from target server.

This indicates the attacker fulfilled a inspection attack to the target server.

Because the Firewall dose not filter server to endpoint direction packets, so to simplify the model, the server directly send packets to *uChannel* or *aChannel* to simplify the model.

Variables changed: $\langle aTCPLinkSet, aChannel, FwDataChannel \rangle$

$$\text{AttackerRcvSynAck} \triangleq$$

$$\begin{aligned}
& \wedge aTCPLinkSet \neq \{\} \\
& \wedge aChannel \neq \langle \rangle \\
& \wedge Head(aChannel).Flg = \text{"TCP_SYN_ACK"} \\
& \wedge Head(aChannel).Type = \text{"Attacker"} \\
& \wedge HasMatchLink(Head(aChannel), aTCPLinkSet) \\
& \wedge GetMatchLink(Head(aChannel), aTCPLinkSet).State = \text{"SYN_SENT"} \quad \text{pre-condition: local } TCP \text{ client in the} \\
& \wedge aTCPLinkSet' = (aTCPLinkSet \setminus \{GetMatchLink(Head(aChannel), aTCPLinkSet)\}) \quad \text{Post-condition: The} \\
& \quad \cup \{[sIP \mapsto GetMatchLink(Head(aChannel), aTCPLinkSet).sIP, \\
& \quad \quad sPort \mapsto GetMatchLink(Head(aChannel), aTCPLinkSet).sPort, \\
& \quad \quad dIP \mapsto GetMatchLink(Head(aChannel), aTCPLinkSet).dIP, \\
& \quad \quad dPort \mapsto GetMatchLink(Head(aChannel), aTCPLinkSet).dPort, \\
& \quad \quad State \mapsto \text{"ESTABLISHED"}, \\
& \quad \quad AuthID \mapsto GetMatchLink(Head(aChannel), aTCPLinkSet).AuthID \\
& \quad \quad]\} \\
& \wedge aChannel' = Tail(aChannel) \\
& \wedge FwDataChannel' = Append(FwDataChannel, EndPointBulidTcpAckPkt(Head(aChannel), \text{"Attacker"})) \\
& \wedge \text{UNCHANGED } user_vars \\
& \wedge \text{UNCHANGED } sdpsvr_vars \\
& \wedge \text{UNCHANGED } fw_vars \\
& \wedge \text{UNCHANGED } \langle aState, AuthKnowledge, aSession, sniffCount, CapAuthMsg, aCounter, aIP, DataKnowl \\
& \wedge \text{UNCHANGED } server_vars \\
& \wedge \text{UNCHANGED } \langle uChannel, AuthChannel, FwCtlChannel, sChannel \rangle
\end{aligned}$$

The init description of the whole system

$$\begin{aligned}
Init & \triangleq \wedge UsrInit \\
& \wedge SDPSvrInit \\
& \wedge FwInit \\
& \wedge AttackerInit \\
& \wedge ServerInit
\end{aligned}$$

Next state transtion of the whole system

The next state actions of the whole system is the disjunction of each entity's next state action.

$$\begin{aligned}
Next \triangleq & \text{User's next state actions} \\
& \vee \textit{UsrCommitSpaAuth} \\
& \vee \textit{UsrConnectSvr} \\
& \vee \textit{UsrRcvSynAck} \\
& \text{SDP controller's next state actions} \\
& \vee \textit{SDPSvrProcSpaAuth} \\
& \text{Fire Wall's next state actions} \\
& \vee \textit{FwProcAclCfg} \\
& \vee \textit{FwProcEndPointAccess} \\
& \vee \textit{FwProcAclTimeOut} \\
& \text{Attacker's next state actions} \\
& \vee \textit{AttackerSniffAuthChannel} \\
& \vee \textit{AttackerSpoofAuth} \\
& \vee \textit{AttackerReplayAuth} \\
& \vee \textit{AttackerBrutalAttck} \\
& \vee \textit{AttackerSniffDataChannel} \\
& \vee \textit{AttackerInspectSvr} \\
& \vee \textit{AttackerRcvSynAck} \\
& \text{Target service server's next state actions} \\
& \vee \textit{ServerRcvTCPSyn} \\
& \vee \textit{ServerRcvTcpAck}
\end{aligned}$$

The specification of the whole system

$$Spec \triangleq Init \wedge \Box[Next]_{vars}$$

The Fair specification of the whole system

$$\begin{aligned}
FairSpec \triangleq & \text{WF means weak fairness, gurantee once the action is enabled, it will be triggered sooner or later.} \\
& \wedge Spec \quad \text{Use the fairness attribute to eliminate unnecessary stuttering states.} \\
& \wedge WF_{vars}(\textit{UsrCommitSpaAuth}) \\
& \wedge WF_{vars}(\textit{SDPSvrProcSpaAuth}) \\
& \wedge WF_{vars}(\textit{FwProcAclCfg}) \\
& \wedge WF_{vars}(\textit{AttackerSniffAuthChannel}) \\
& \wedge WF_{vars}(\textit{AttackerSpoofAuth}) \\
& \wedge WF_{vars}(\textit{AttackerReplayAuth})
\end{aligned}$$

$$\begin{aligned}
& \wedge \text{WF}_{vars}(\text{UsrConnectSvr}) \\
& \wedge \text{WF}_{vars}(\text{FwProcEndPointAccess}) \\
& \wedge \text{WF}_{vars}(\text{FwProcAclTimeOut}) \\
& \wedge \text{WF}_{vars}(\text{ServerRcvTCPSyn}) \\
& \wedge \text{WF}_{vars}(\text{UsrRcvSynAck}) \\
& \wedge \text{WF}_{vars}(\text{ServerRcvTcpAck}) \\
& \wedge \text{WF}_{vars}(\text{AttackerBrutalAttck}) \\
& \wedge \text{WF}_{vars}(\text{AttackerSniffDataChannel}) \\
& \wedge \text{WF}_{vars}(\text{AttackerInspectSvr}) \\
& \wedge \text{WF}_{vars}(\text{AttackerRcvSynAck})
\end{aligned}$$

```

AuthSessionHasMatchAcl(s, AclSet)  $\triangleq$ 
  IF AclSet = {}
  THEN
    FALSE
  ELSE
     $\exists r \in \text{AclSet}:$ 
      (  $\wedge r.sIP = s.sIP$ 
         $\wedge ( \vee r.sPort = \text{MATCH\_ANY}$ 
           $\vee (r.sPort \neq \text{MATCH\_ANY} \wedge r.sPort = s.sPort)$ 
        )
         $\wedge r.dIP = s.dIP$ 
         $\wedge r.dPort = s.dPort$ 
         $\wedge r.action = \text{"Accept"}$ 
      )
  )

```

Invariants to be verified

$\text{DataAccessSafeLaw} \triangleq$ attacker can not find target server service at anytime

$\wedge \forall x \in aTCPLinkSet : x.State \neq \text{"ESTABLISHED"}$

$\text{SPASafeLaw} \triangleq$ attacker can not launch a successful SPA auth at anytime

$\wedge \forall x \in SDPSucSession : x.Type \neq \text{"Attacker"}$

The temporal properties of the system to be verified

Temporal Property 1: $\text{SPA_AvailableProperty}$

This formula asserts the availability of SPA service provided by the *SDP* controller

$\text{AuthMessageMatch}(m, n) \triangleq$ Both *m* and *n* are auth Sessions

$\wedge m.MsgID = n.MsgID$

$$\begin{aligned}
& \wedge m.sIP = n.sIP \\
& \wedge m.sPort = n.sPort \\
& \wedge m.dIP = n.dIP \\
& \wedge m.dPort = n.dPort \\
& \wedge m.ClientID = n.ClientID \\
& \wedge m.Tstamp = n.Tstamp \\
& \wedge m.SvrIP = n.SvrIP \\
& \wedge m.SvrPort = n.SvrPort \\
& \wedge m.HMAC = n.HMAC \\
& \wedge m.Type = n.Type
\end{aligned}$$

$$\begin{aligned}
SDP_AclRuleMatch(m, r) & \triangleq \text{ } m \text{ is an auth Session, } r \text{ is a ACL Rule} \\
& \wedge m.sIP = r.sIP \\
& \wedge r.sPort = MATCH_ANY \\
& \wedge uSvrInfo.IP = r.dIP \\
& \wedge uSvrInfo.Port = r.dPort \\
& \wedge r.protocol = \text{"TCP"} \\
& \wedge r.action = \text{"Accept"}
\end{aligned}$$

This formula asserts that the system's behavior eventually always meets the underlying propositions

1. All authentication sessions launched by legal users have been successfully processed by *SDP* controller.
2. All successfully processed *Auth* sessions recorded by *SDP* controller are sessions launched by legal users.
3. For all successfully authenticated sessions, the Fire wall has been configed corresponding *ACL Rule*.

$$\begin{aligned}
SPA_AvailableProperty & \triangleq \\
& \Diamond \Box (\wedge \forall x \in uAuthSession : (\exists y \in SDPSucSession : AuthMessageMatch(x, y)) \text{ user} \rightarrow \text{contro} \\
& \quad \wedge \forall x \in SDPSucSession : (\exists y \in uAuthSession : AuthMessageMatch(x, y)) \text{ controller} \rightarrow \text{u} \\
& \quad \wedge \forall x \in uAuthSession : (\exists y \in (AclRuleSet \cup AgedRuleSet) : SDP_AclRuleMatch(x, y)) \\
&)
\end{aligned}$$

Temporal Property 2: *SPA_AntiDosProperty*

This formula asserts the Anti-Dos property of *SDP* controller, which means the controller can always inspect and defeat spoof and replay attack.

The following formula asserts that every SPA replay attack inspected by the *SDP* controller is originated from the attacker.

$SPA_AntiReplayProperty \triangleq$

IF $ReplaySession \neq \{\}$

THEN

$\forall x \in ReplaySession : (\exists y \in aSession : AuthMessageMatch(x, y))$

ELSE

TRUE

The following formula asserts that every SPA spoof attack inspected by the *SDP* controller is originated from the attacker

$SPA_AntiSpoofProperty \triangleq$

IF $SpoofSession \neq \{\}$

THEN

$\forall x \in SpoofSession : (\exists y \in aSession : AuthMessageMatch(x, y))$

ELSE

TRUE

The following formula asserts that the system's behavior eventually always meets the underlying propositions

IF attacker ever captured legal SPA packets by sniffing, then:

1. For every captured legal SPA messages, the attacker will launch a SPA attack according to the message info.
2. Every SPA attack message launched by the attacker will be inspected and blocked by the *SDP* controller.

IF attacker never captured legal SPA packets, then no SPA attack is lunched.

$SPA_AntiDosProperty \triangleq$

$\Diamond \Box (\wedge CapAuthMsg \subseteq uAuthSession$

$\wedge Cardinality(CapAuthMsg) = Cardinality(aSession)$

$\wedge \text{IF } aSession \neq \{\}$

THEN

$\wedge \forall x \in aSession : (\exists y \in (ReplaySession \cup SpoofSession) : AuthMessageMatch(x, y))$

$\wedge SPA_AntiReplayProperty$

$\wedge SPA_AntiSpoofProperty$

ELSE

$\wedge CapAuthMsg = \{\}$

$\wedge ReplaySession = \{\}$

$\wedge SpoofSession = \{\}$

)

$$CliSvrLinkMatch(c, s) \triangleq$$

$$\wedge c.dIP = s.sIP$$

$$\wedge c.sIP = s.dIP$$

$$\wedge c.dPort = s.sPort$$

$$\wedge c.sPort = s.dPort$$

Temporal Property 3: *UserAccessAvailProperty*

This formula asserts the availability of the data plane service ,which means

legal user can finally access the target server except the case that 3 tuple *Acl Rule* is aged before th *TCP* connection

$$UserAccessAvailProperty \triangleq$$

$$\Diamond \Box (\wedge (\forall x \in uTCPLinkSet : \vee (\wedge x.State = \text{"ESTABLISHED"} \quad \text{scenario1: } TCP \text{ link established, and}$$

$$\wedge \exists y \in sTCPLinkSet : (CliSvrLinkMatch(x, y) \wedge x.State = y$$

$$\wedge AclMatch4Tuple(x, AclRuleSet)$$

)

$$\vee (\wedge x.State = \text{"SYN_SENT"} \quad \text{scenario2: } TCP \text{ link half-established due}$$

$$\wedge \forall y \in sTCPLinkSet : \neg CliSvrLinkMatch(x, y)$$

$$\wedge AclMatch3Tuple(x, AgedRuleSet)$$

)

)

$$\wedge uTCPLinkSet \neq \{\}$$

)

Temporal Property 4: *SvrHidenProperty*

This formula asserts the service hidden property of the *SDP* arhitecture. which means

finally attacker can not establish any link with the target server.

$$SvrHidenProperty \triangleq$$

$$\Diamond \Box (\wedge (\forall x \in sTCPLinkSet : \wedge x.Type \neq \text{"Attacker"} \quad$$

$$\wedge x.State = \text{"ESTABLISHED"}) \quad \text{All the established link in server side are}$$

$$\wedge (\forall y \in aTCPLinkSet : \wedge y.State \neq \text{"ESTABLISHED"}) \quad \text{Attacker as a } TCP \text{ client, no established}$$

)

Temporal Property 5: *FwRuleConsistentProperty*

This formula asserts that for each successful auth session in history there exists
a corresponding 3 Tuple *Acl Rule* on *FW*, available or aged, vice versa.

$Get3TupleAclRuleSet(S) \triangleq$

get all the 3 *Tuple Acl* rule in history.

```

LET  $CS[T \in \text{SUBSET } S]$   $\triangleq$  IF  $T = \{\}$ 
    THEN  $\{\}$ 
    ELSE
    (
    IF (CHOOSE  $x \in T : \text{TRUE}$ ). $sPort = MATCH\_ANY$ 
    THEN
     $\{\text{CHOOSE } x \in T : \text{TRUE}\} \cup CS[T \setminus \{\text{CHOOSE } x \in T : \text{TRUE}\}]$ 
    ELSE
     $CS[T \setminus \{\text{CHOOSE } x \in T : \text{TRUE}\}]$ 
    )
IN  $CS[S]$ 

```

$AuthRelateAcl(s, R) \triangleq$

```

 $\exists r \in R : \wedge s.sIP = r.sIP$ 
 $\wedge r.sPort = MATCH\_ANY$ 
 $\wedge DeCrypt(s.SvrIP, Key) = r.dIP$ 
 $\wedge DeCrypt(s.SvrPort, Key) = r.dPort$ 

```

$AclRelateAuth(r, S) \triangleq$

```

 $\exists s \in S : \wedge s.sIP = r.sIP$ 
 $\wedge r.sPort = MATCH\_ANY$ 
 $\wedge DeCrypt(s.SvrIP, Key) = r.dIP$ 
 $\wedge DeCrypt(s.SvrPort, Key) = r.dPort$ 

```

$FwRuleConsistentProperty \triangleq$ the consistent between user's SPA session and ever configed *L3 tuple Acl Rule* on Fire Wall

```

 $\Diamond \Box ( \wedge Cardinality(uAuthSession) = Cardinality(Get3TupleAclRuleSet(AclRuleSet \cup AgedRuleSet))$ 
 $\wedge \forall x \in uAuthSession : AuthRelateAcl(x, Get3TupleAclRuleSet(AclRuleSet \cup AgedRuleSet))$ 
 $\wedge \forall y \in Get3TupleAclRuleSet(AclRuleSet \cup AgedRuleSet) : AclRelateAuth(y, uAuthSession)$ 
 $)$ 

```

Temporal Property 6: *FwCorrectProperty*

This formula asserts that the Fire Wall's Packets filtering function works well, which means that for any unestablished *TCP* links there must exists packets dropping by *FireWall*.

$$\begin{aligned}
 WithDropPkts(x) &\triangleq \\
 &\exists p \in DropPackets : \wedge p.sIP = x.sIP \\
 &\quad \wedge p.sPort = x.sPort \\
 &\quad \wedge p.dIP = x.dIP \\
 &\quad \wedge p.dPort = x.dPort
 \end{aligned}$$

$$WithOutDropPkts(x) \triangleq \neg WithDropPkts(x)$$

$$\begin{aligned}
 FwCorrectProperty &\triangleq \text{to simplify the model, we don't consider } TCP \text{ packets re-transport mechanism, so establish} \\
 &\diamond\Box(\wedge \forall x \in aTCPLinkSet : \text{ IF } x.State = \text{"ESTABLISHED"} \\
 &\quad \text{THEN} \\
 &\quad \quad WithOutDropPkts(x) \\
 &\quad \text{ELSE} \\
 &\quad \quad WithDropPkts(x) \\
 &\wedge \forall x \in uTCPLinkSet : \text{ IF } x.State = \text{"ESTABLISHED"} \\
 &\quad \text{THEN} \\
 &\quad \quad WithOutDropPkts(x) \\
 &\quad \text{ELSE} \\
 &\quad \quad WithDropPkts(x) \\
 &)
 \end{aligned}$$

$$test2 \triangleq uState \in \{ \text{"Start_Auth"}, \text{"Auth_End"}, \text{"Connecting"}, \text{"Connected"} \}$$

Example:

Terminal $\triangleq \diamond\Box($
 $\quad \backslash * ^$
 $\quad)$

\ * Modification History
 \ * Last modified *Thu Feb 24 15:34:13 CST 2022* by 10227694
 \ * Created *Tue Dec 28 09:34:21 CST 2021* by 10227694