# DATA SCIENCE CLUSTERING

### **AGENDA**

- I. UNSUPERVISED LEARNING
- II. CLUSTER ANALYSIS
- III. THE K-MEANS ALGORITHM
- IV. CHOOSING K
- V. EXAMPLE

# I. UNSUPERVISED LEARNING

#### SUPERVISED VS. UNSUPERVISED LEARNING

### **Supervised learning** has clear objectives:

- Accurately predict unseen test cases
- Understand which features affect the response, and how

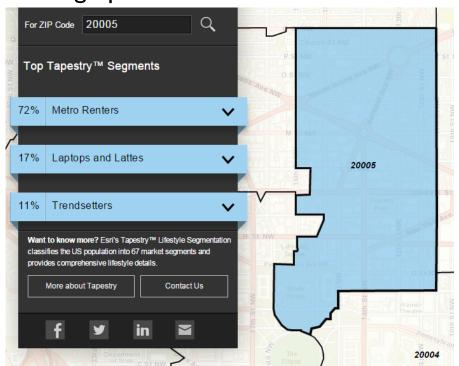
You can evaluate how well you are doing!

### Unsupervised learning has fuzzy objectives:

- Find groups of observations that behave similarly
- Find features that behave similarly

It's difficult to evaluate how well you are doing!

Classify US residential neighborhoods into 67 unique segments based on demographic and socioeconomic characteristics

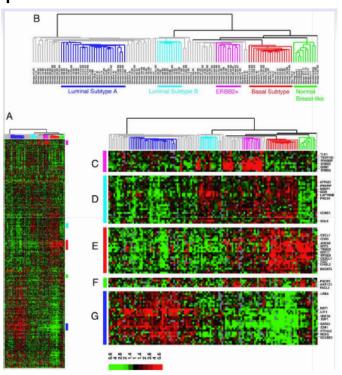


#### Metro Renters:

Young, mobile, educated, or still in school, we live alone or with a roommate in rented apartments or condos in the center of the city. Long hours and hard work don't deter us; we're willing to take risks to get to the top of our professions... We buy groceries at Whole Foods and Trader Joe's and shop for clothes at Banana Republic, Nordstrom, and Gap. We practice yoga, go skiing, and attend Pilates sessions.

#### **CLUSTERING EXAMPLE**

Classify a tissue sample into one of several cancer classes, based on gene expression data



- Each column is a woman with breast cancer (n=88)
- Each row is a gene (p=8000)
- Color represents level of gene expression

<u>Goal</u>: Locate subcategories of breast cancer showing different gene expressions

<u>Technique</u>: Hierarchical clustering applied to the columns, resulting in six sub-groups of patients

# II. CLUSTER ANALYSIS

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In general, greater similarity between points leads to better clustering.

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The goal is to extract and enhance the natural structure of the data

There are many kinds of clustering procedures. For our class, we will be focusing on K-means clustering, which is one of the most popular clustering algorithms.

K-means is an iterative method that partitions a data set into k clusters.

# III. K-MEANS CLUSTERING

### **K-MEANS CLUSTERING**

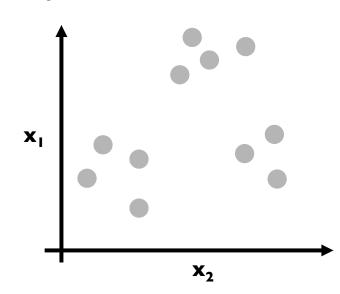
Q: How does the algorithm work?

- 2) for each point:
  - find distance to each centroid
  - assign point to nearest centroid

- 3) recalculate centroid positions
- 4) repeat steps 2-3 until stopping criteria met

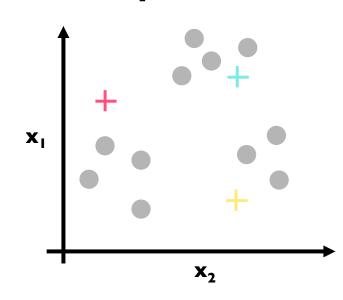
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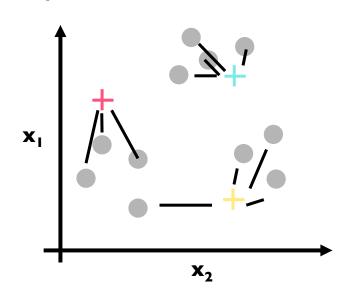
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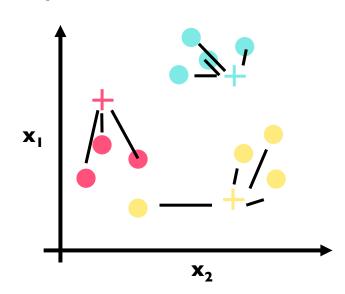
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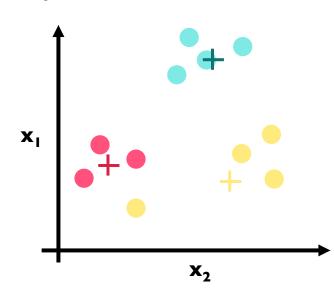
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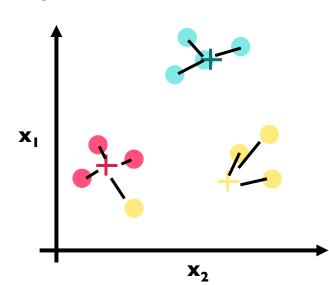


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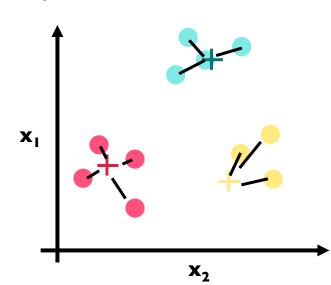
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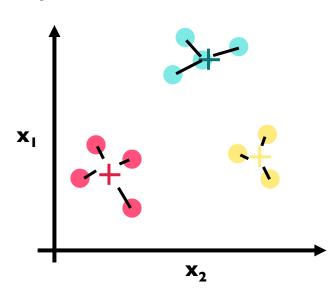
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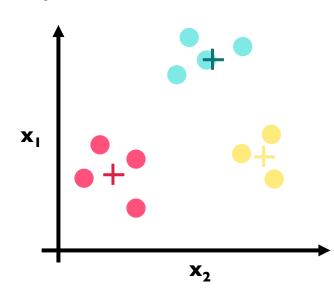
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  - randomly (but may yield divergent behavior)
  - perform alternative clustering task, use resulting centroids as initial k-means centroids
  - start with global centroid, choose point at max distance, repeat (but might select outlier)

### STEP 2 – ASSESS SIMILARITY

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### **Euclidian distance:**

$$d(x_1, x_2) = \sqrt{\sum_{i=1}^{N} (x_{1i} - x_{2i})^2}$$

#### **STEP 3 — RECOMPUTING THE CENTER**

Q: How do we recompute the positions of the centers at each iteration of the algorithm?

A: By calculating the centroid (i.e., the geometric center)

#### STEP 4 - CONVERGENCE

We iterate until some stopping criteria are met; in general, suitable convergence is achieved in a small number of steps.

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Stopping criteria can be based on the centroids (eg, if positions change by no more than  $\varepsilon$ ) or on the points (eg, if no more than x% change clusters between iterations).

# IV. CLUSTER VALIDATION

#### **CLUSTER VALIDATION**

In general, k-means will converge to a solution and return a partition of k clusters, even if no natural clusters exist in the data.

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We will look at two validation metrics useful for partitional clustering, **cohesion** and **separation**.

## **Cohesion** measures clustering effectiveness within a cluster.

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Separation measures clustering effectiveness between clusters.

$$\hat{S}(C_i, C_j) = d(c_i, c_j)$$

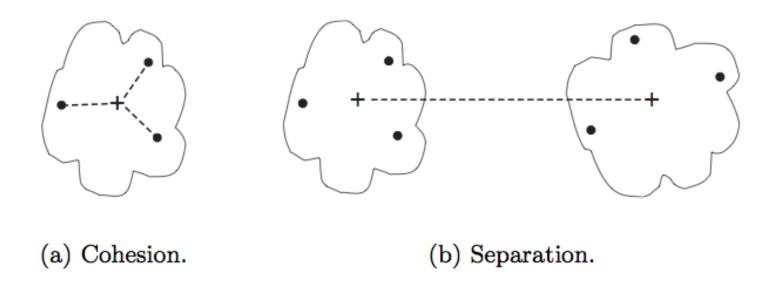


Figure 8.28. Prototype-based view of cluster cohesion and separation.

One useful measure than combines the ideas of cohesion and separation is the **silhouette coefficient**. For point  $x_i$ , this is given by:

$$SC_i = \frac{b_i - a_i}{max(a_i, b_i)}$$

such that:

 $a_i$  = average in-cluster distance to  $x_i$   $b_{ij}$  = average between-cluster distance to  $x_i$  $b_i$  =  $min_i(b_{ij})$  The silhouette coefficient can take values between -1 and 1.

In general, we want separation to be high and cohesion to be low. This corresponds to a value of SC close to +1.

A negative silhouette coefficient means the cluster radius is larger than the space between clusters, and thus clusters overlap. The silhouette coefficient for the cluster  $C_i$  is given by the average silhouette coefficient across all points in  $C_i$ :

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NOTE

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#### **CLUSTER VALIDATION**

One useful application of cluster validation is to determine the best number of clusters for your dataset. One useful application of cluster validation is to determine the best number of clusters for your dataset.

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Q: How would you do this?

A: By computing the SC for different values of k.

#### **CLUSTER VALIDATION**

Ultimately, cluster validation and clustering in general are suggestive techniques that rely on human interpretation to be meaningful.

## **Strengths:**

K-means is a popular algorithm because of its computational efficiency and simple and intuitive nature.

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### Weaknesses:

However, K-means is highly scale dependent, and is not suitable for data with widely varying shapes and densities.

# V. EXAMPLE