



Word Embeddings

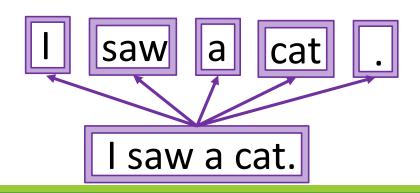
SEPTEMBER 13, 2018

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Plan

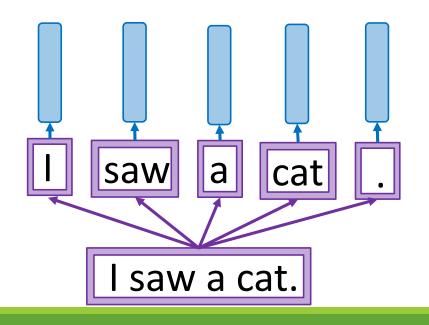
- Why do we need word representations?
- Distributional semantics
- Word2Vec in detail
- Glove overview
- Let's take a walk!
- > Further directions: subword information
- > Further directions: abstract the ideas to sentence-level
- > Further directions: exploiting the structure of semantic spaces
- Hack of the day!

I saw a cat.



Sequence of tokens

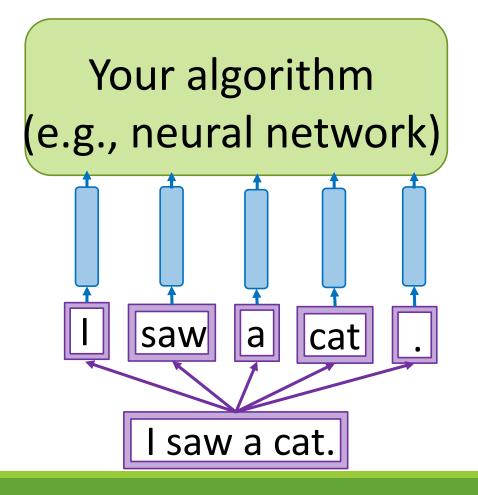
Text



Word representation - vector (word embedding)

Sequence of tokens

Text



Any algorithm for solving any task

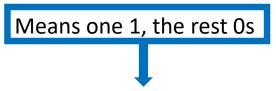
Word representation - vector (word embedding)

Sequence of tokens

Text

Representing words as discrete symbols

In traditional NLP, we regard words as discrete symbols: hotel, conference, motel



Words can be represented by **one-hot** vectors:

Vector dimension = number of words in vocabulary (e.g. 500,000)

Problem with words as discrete symbols

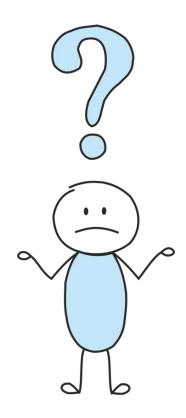
<u>Example</u>: in web search, if user searches for "Seattle motel", we would like to match documents containing "Seattle hotel".

But:

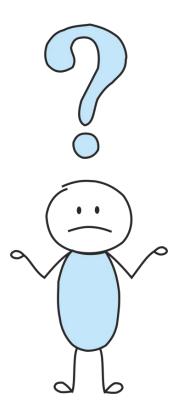
These two vectors are orthogonal.

There is no natural notion of **similarity** for one-hot vectors!

These vectors do not contain information about a **meaning** of a word.



What is bardiwac?



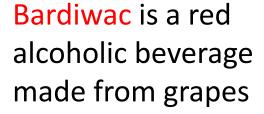
What is bardiwac?

- > He handed her a glass of bardiwac.
- > Beef dishes are made to complement the bardiwac.
- ➤ Nigel staggered to his feet, face flushed from too much bardiwac.
- Malbec, one of the lesser-known bardiwac grapes, responds well to Australia's sunshine.
- > I dined off bread and cheese and this excellent bardiwac.
- The drinks were delicious: blood-red bardiwac as well as light, sweet Rhenish.

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- ➤ A bottle of <u>bardiwac</u> is on the table.
- > Everybody likes <u>bardiwac</u>.
- ➤ Don't have <u>bardiwac</u> before you drive.
- ➤ We make <u>bardiwac</u> out of corn.

- > A bottle of _____ is on the table.
- Everybody likes ______.
- Don't have _____ before you drive.
- We make _____ out of corn.

What other words fit into these contexts?

> A bottle of _____ is on the table. (1)

Everybody likes ______. (2)

> Don't have _____ before you drive. (3)

> We make _____ out of corn. (4)

	(1)	(2)	(3)	(4)	•••
bardiwac	1	1	1	1	
loud	0	0	0	0	
motor oil	1	0	0	1	
tortillas	0	1	0	1	
wine	1	1	1	0	
choices	0	1	0	0	

What other words fit into these contexts?

> A bottle of _____ is on the table. (1)

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What other words fit into these contexts?

Does vector similarity imply semantic similarity?

Does vector similarity imply semantic similarity?



The distributional hypothesis, stated by Firth (1957):

"You shall know a word by the company it keeps."

Corpus sentences

He also found five fish swimming in murky water in an old **bathtub**.

We do abhor dust and dirt, and stains on the **bathtub**, and any kind of filth.

Above At the far end of the garden room a **bathtub** has been planted with herbs for the winter.

They had been drinking Cisco, a fruity, wine-based fluid that smells and tastes like a mixture of cough syrup and **bathtub** gin.

Science finds that a surface tension on the water can draw the boats together, like toy boats in a **bathtub**.

In fact, the godfather of gloom comes up with a plot that takes in Windsor Davies (the ghost of sitcoms past), a **bathtub** and a big box of concentrated jelly.

'I'll tell him,' said the Dean from the bathroom above the sound of bathwater falling from a great height into the ample Edwardian **bathtub**.

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Co-occurrence counts

the	12	
a	9	
of	7	
and	6	
in	5	
like	2	
water	2	
boat	2	
from	2	
stain	1	
toy	1	
god- father	1	
Cisco	1	

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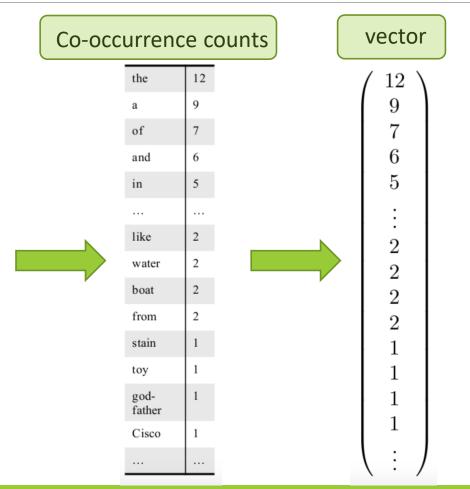
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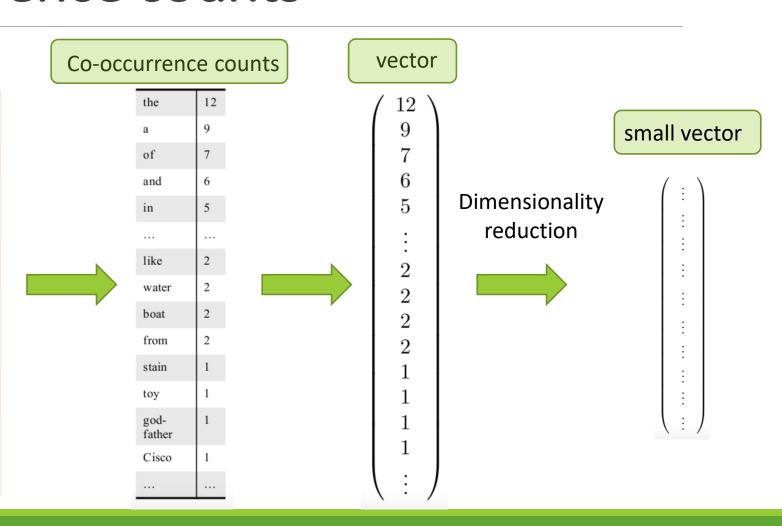
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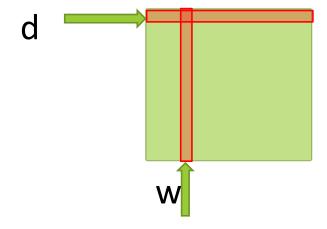
Latent semantic analysis (LSA)

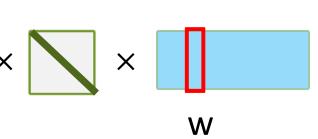
X - document-term co-occurrence matrix

$$X \approx \hat{X} = U \Sigma V^T$$

- > co-occurrence counts
- > tf-idf
- > filter stop-words
- > lemmatize
- > ...

$$V^{T}$$

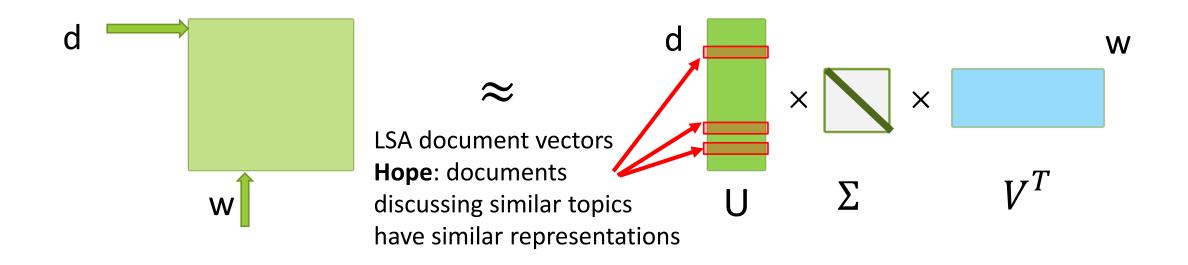




Latent semantic analysis (LSA)

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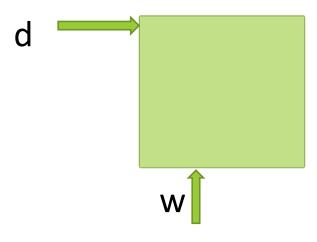
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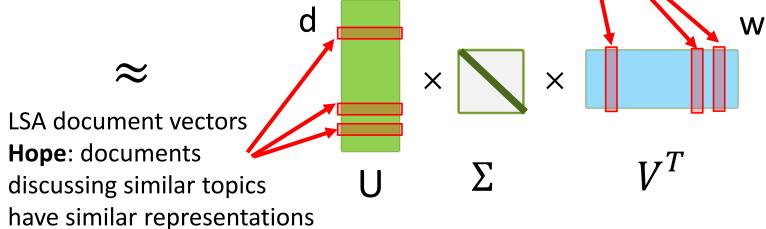


Latent semantic analysis (LSA)

X - document-term co-occurrence matrix

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LSA term vectors

same direction

Hope: term having common

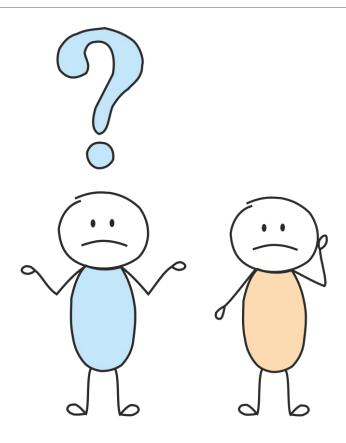
meaning are mapped to the

Count-based methods

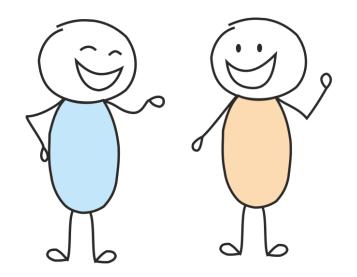
However, this is not the only way to induce distributional representations

(and not the best one)

Why not to learn distributed representations?



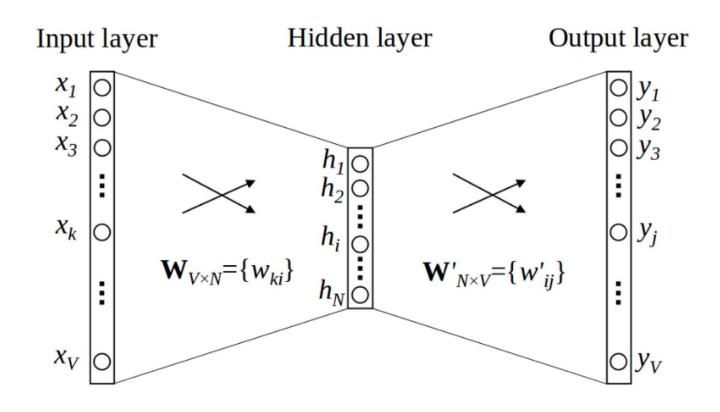
I mean, really, why?



We will learn a dense vector for each word, chosen so that it is similar to vectors of words that appear in similar contexts.

This word vectors are called word embeddings or word representations

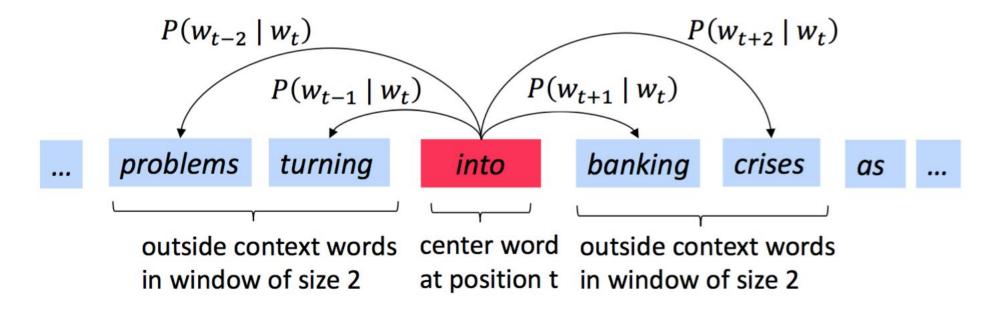
Word2Vec



- > a large corpus of text
- > Every word in a fixed vocabulary is represented by a vector
- ➤ Go through each position t in the text, which has a center word c and context ("outside") words o
- ➤ Use the similarity of the word vectors for *c* and *o* to calculate the probability of *o* given *c* (or vice versa)
- Keep adjusting the word vectors to maximize this probability

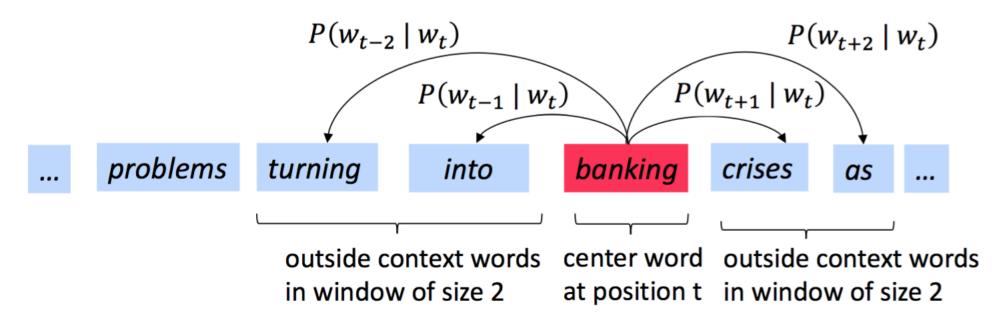
Word2Vec

 \geq Examples windows and and process for computing $P(w_{t+j}|w_j)$



Word2Vec

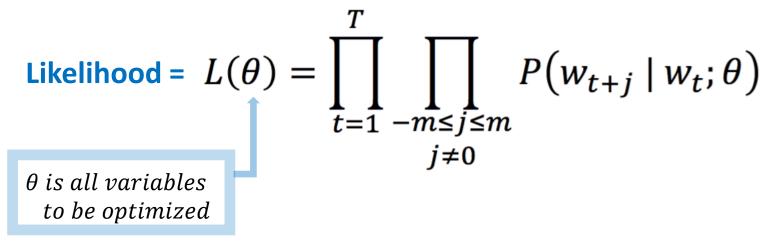
 \geq Examples windows and and process for computing $P(w_{t+j}|w_i)$



For each position t = 1, ..., T, predict context words within a window of fixed size m, given center word w_t .

$$L(\theta) = \prod_{t=1}^{T} \prod_{-m \le j \le m} P(w_{t+j} \mid w_t; \theta)$$

For each position t = 1, ..., T, predict context words within a window of fixed size m, given center word w_t .



The **objective function (or loss, or cost function)** $J(\theta)$ is the (average) negative log likelihood

$$J(\theta) = -\frac{1}{T} \log L(\theta) = -\frac{1}{T} \sum_{t=1}^{T} \sum_{-m \le j \le m} \log P(w_{t+j} \mid w_t; \theta)$$

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Minimizing objective function \longleftrightarrow Maximizing predictive accuracy

We want to minimize objective function
$$J(\theta) = -\frac{1}{T} \sum_{t=1}^{T} \sum_{-m \le j \le m} \log P(w_{t+j} \mid w_t; \theta)$$

Word2Vec: objective function

We want to minimize objective function $J(\theta) = -\frac{1}{T} \sum_{t=1}^{I} \sum_{-m \le j \le m} \log P(w_{t+j} \mid w_t; \theta)$

i≠0

 \triangleright Question: How to calculate $P(w_{t+j}|w_j,\theta)$?

Word2Vec: objective function

- We want to minimize objective function $J(\theta) = -\frac{1}{T} \sum_{t=1}^{I} \sum_{-m \le j \le m} \log P(w_{t+j} \mid w_t; \theta)$ *i*≠0
- \triangleright Question: How to calculate $P(w_{t+i}|w_i,\theta)$?
- > Answer: We will use two vectors per word w
- \mathbf{v}_{w} is a center word
- u_w is a context word

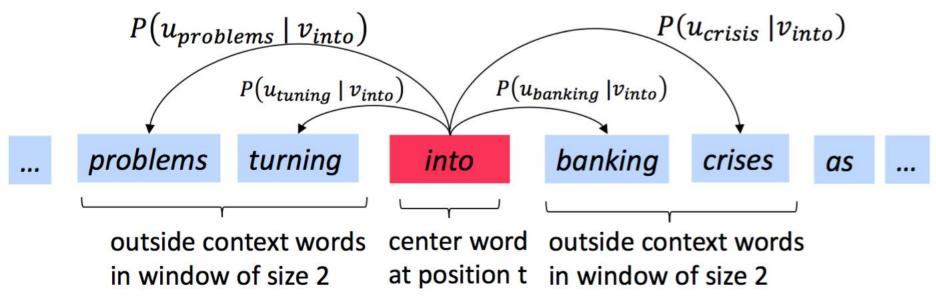
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- > We want to minimize objective function $J(\theta) = -\frac{1}{T} \sum_{t=1}^{I} \sum_{-m \le j \le m} \log P(w_{t+j} \mid w_t; \theta)$
- ightharpoonup Question: How to calculate $P(w_{t+j}|w_j,\theta)$?
- \triangleright Answer: We will use two vectors per word $w = v_w$ is a center word
 - u_w is a context word
- > Then for a center word c and a context word o:

$$P(o|c) = \frac{\exp(u_o^T v_c)}{\sum_{w \in V} \exp(u_w^T v_c)}$$

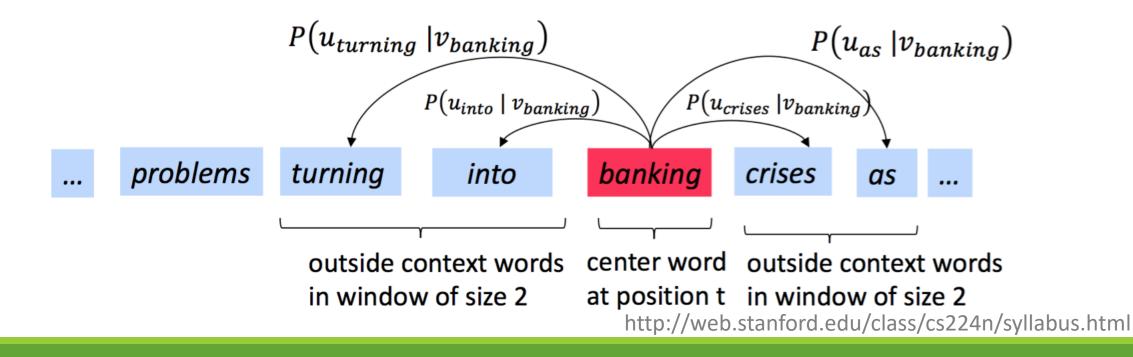
Word2Vec

- \triangleright Examples windows and and process for computing $P(w_{t+j}|w_j)$
- $> P(u_{problems}|v_{into})$ is short for $P(problems|into; u_{problems}, v_{into}, \theta)$



Word2Vec

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Word2Vec: prediction function

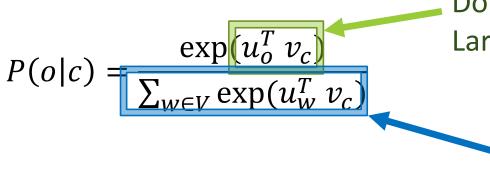
$$P(o|c) = \frac{\exp(u_o^T v_c)}{\sum_{w \in V} \exp(u_w^T v_c)}$$

Word2Vec: prediction function

$$P(o|c) = \frac{\exp[u_o^T v_c]}{\sum_{w \in V} \exp(u_w^T v_c)}$$

Dot product measures similarity of **o** and **c**Larger dot product = larger probability

Word2Vec: prediction function



Dot product measures similarity of **o** and **c** Larger dot product = larger probability

After taking exponent, normalize over entire vocabulary

This is softmax!

Softmax function $\mathbb{R}^n \to \mathbb{R}^n$:

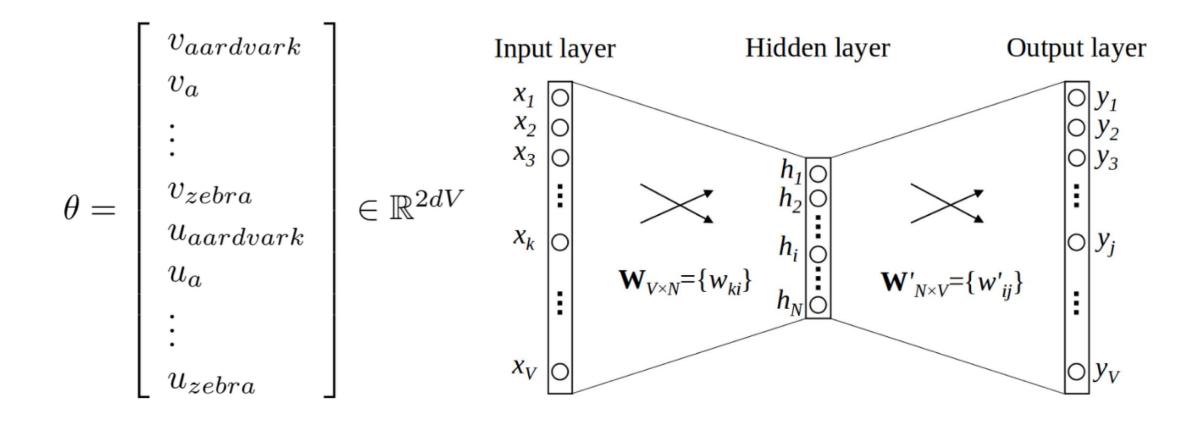
$$softmax(\mathbf{x})_i = \frac{\exp(x_i)}{\sum_{j=1}^n \exp(x_j)} = p_i$$

- \succ maps arbitrary values x_i to a probability distribution p_i
- \geq "max" because amplifies probability of largest x_i
- \succ "soft" because still assigns some probability to smaller x_i
- often used in Deep Learning!

Where is θ ?

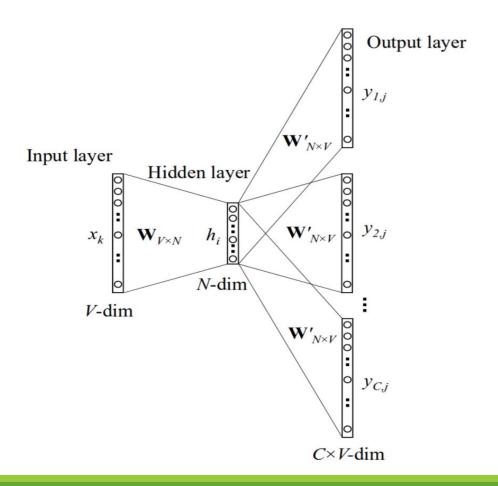
```
    θ - d-dimensional vectors for V words
    every word has two vectors!
    we optimize these parameters
```

Where is θ ?



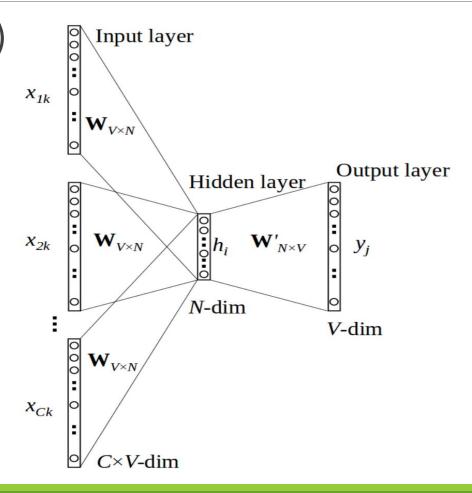
Word2Vec: Skip-gram (SG)

Predict context ("outside") words (position independent) given center word



Word2Vec: Continuous Bag of Words (CBOW)

Predict center word from (bag of) context words



Word2Vec: Additional efficiency in training

$$P(o|c) = \frac{\exp(u_o^T v_c)}{\sum_{w \in V} \exp(u_w^T v_c)}$$

Huge sum! Time for calculating gradients is proportional to |V|

Word2Vec: Additional efficiency in training

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Huge sum! Time for calculating gradients is proportional to |V|

Possible solutions:

- Hierarchical softmax
- Negative sampling

Word2Vec: Additional efficiency in training

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Huge sum! Time for calculating gradients is proportional to |V|

Possible solutions:

- > Hierarchical softmax
- Negative sampling

$$\sum_{w \in V} \exp(u_w^T v_c) \longrightarrow \sum_{w \in \{o\} \cup S_k} \exp(u_w^T v_c)$$

Sum over a small subset: *negative sample*, $|S_k|=k$

Word2Vec: (Near) equivalence to matrix factorization

$$PMI(w,c) = \log \frac{N(w,c) \times |V|}{N(w)N(c)}$$

$$PMI = X \approx \hat{X} = V_d \Sigma_d U_d^T$$

$$V_d \qquad \Sigma_d \qquad U_d^T$$

$$\approx \qquad \qquad \times \qquad \times \qquad \times \qquad \times$$

$$c$$

Levy et al, TACL 2015 http://www.aclweb.org/anthology/Q15-1016

Word2Vec: (Near) equivalence to matrix factorization

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$$PMI = X \approx \hat{X} = V_d \Sigma_d U_d^T$$

$$W$$

$$C$$

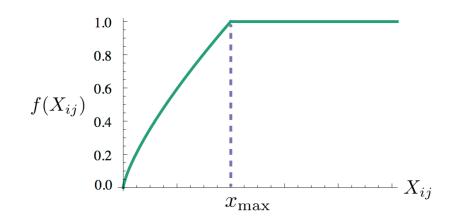
$$V_d \Sigma_d U_d^T$$

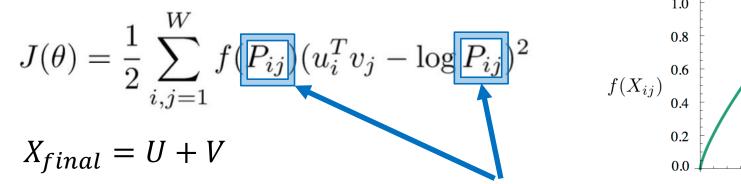
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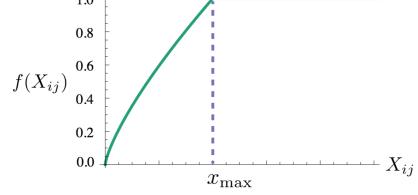
Levy et al, TACL 2015 http://www.aclweb.org/anthology/Q15-1016

$$J(\theta) = \frac{1}{2} \sum_{i,j=1}^{W} f(P_{ij}) (u_i^T v_j - \log P_{ij})^2$$

$$X_{final} = U + V$$



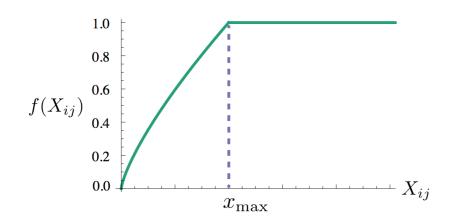




probability that word *j* appear in the context of word *i*

$$J(\theta) = \frac{1}{2} \sum_{i,j=1}^{W} f(P_{ij}) (u_i^T v_j - \log P_{ij})^2$$

$$X_{final} = U + V$$



the idea is close to factorizing the log of the cooccurrence matrix (closely related to LSA)

$$J(\theta) = \frac{1}{2} \sum_{i,j=1}^{W} \underbrace{f(P_{ij})}_{u_i^T v_j} (u_i^T v_j - \log P_{ij})^2$$

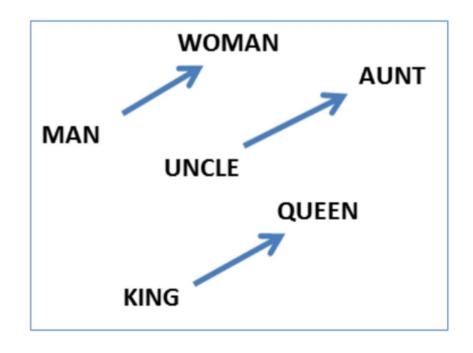
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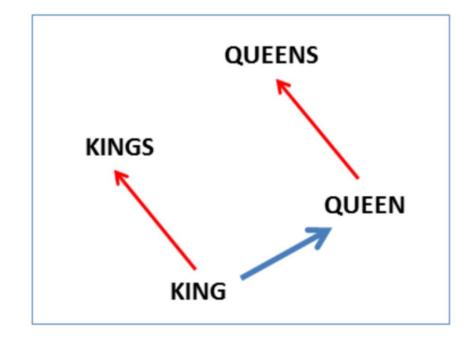
$$x_{max}$$

discard rare noisy co-occurrences

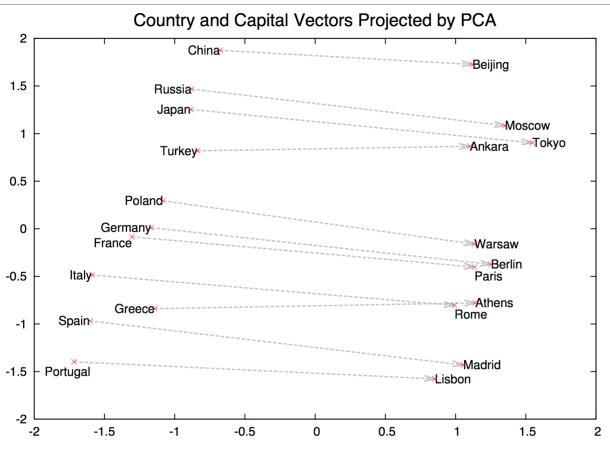
Word2Vec: what are relations between vectors?

 $v(\text{king}) - v(\text{man}) + v(\text{woman}) \approx v(\text{queen})$

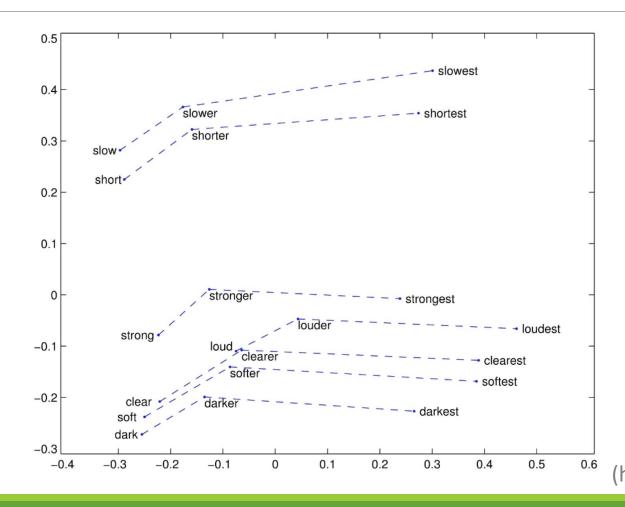




What are relations between vectors?



What are relations between vectors?



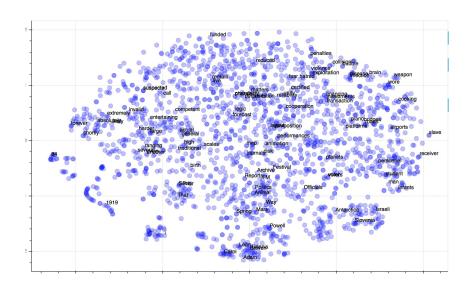
(http://nlp.stanford.edu/projects/glove/)

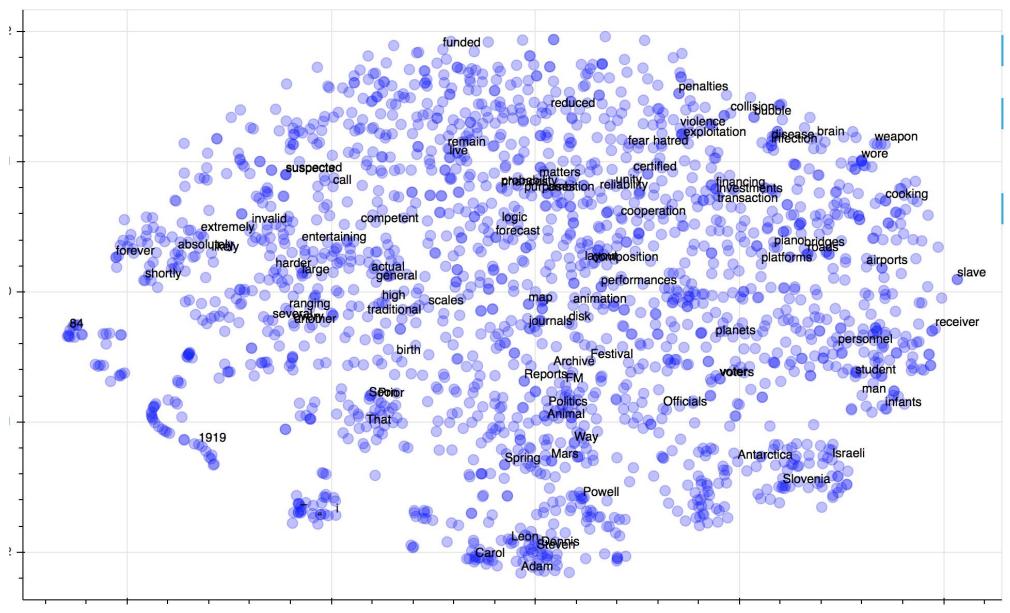
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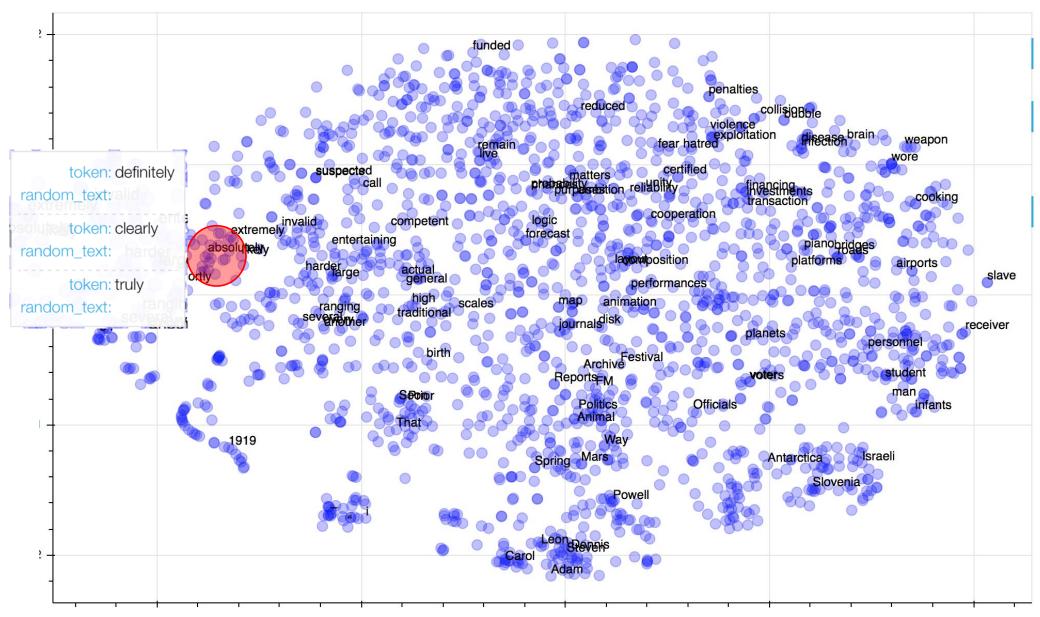
nearest neighbors of frog	Litoria	Leptodactylidae	Rana	Eleutherodactylus
Pictures				

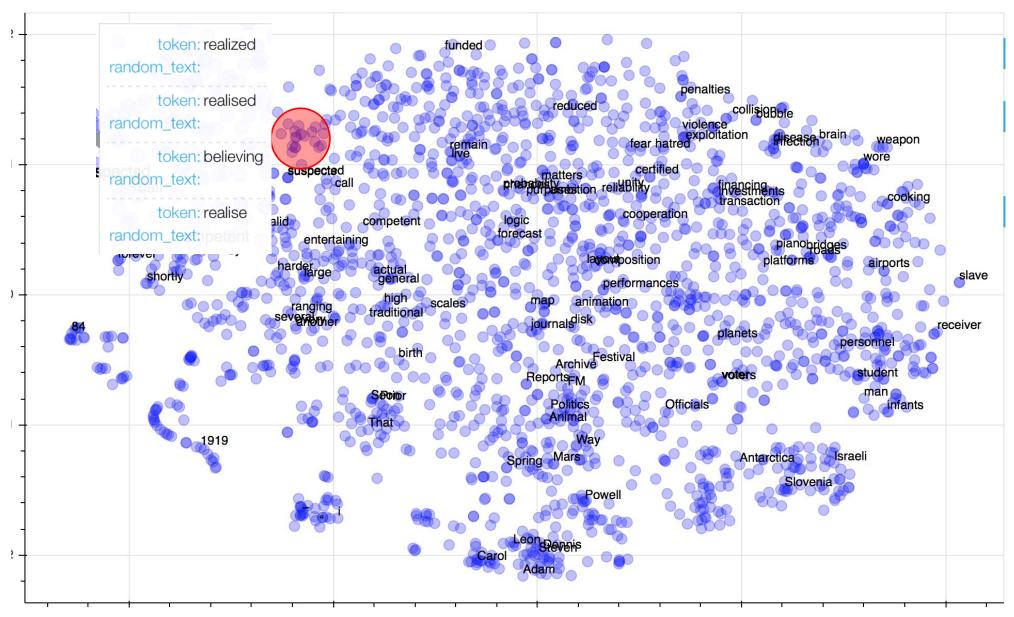
Let's walk through space...

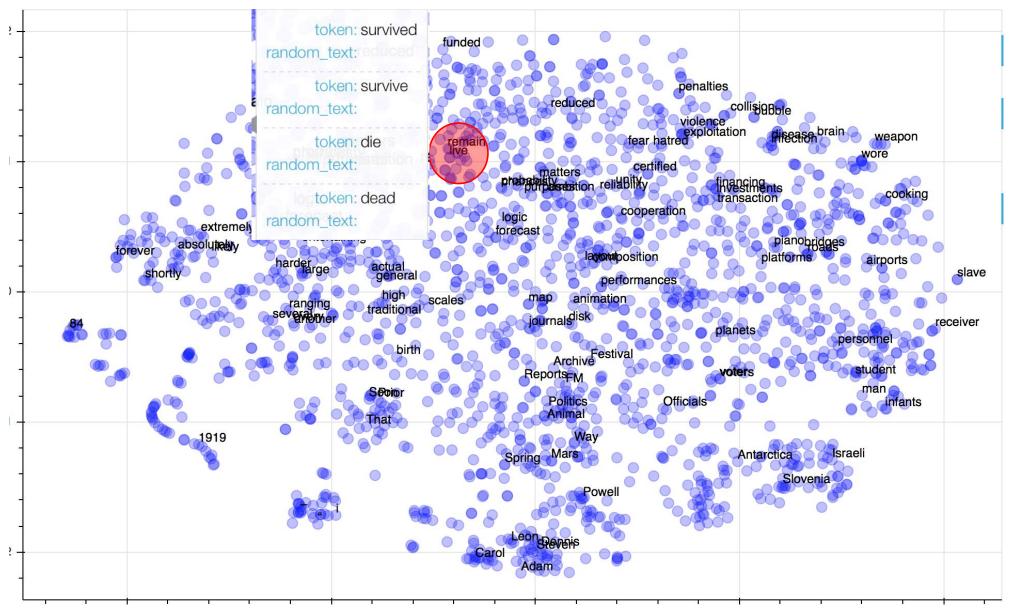
Let's walk through space... Semantic space!

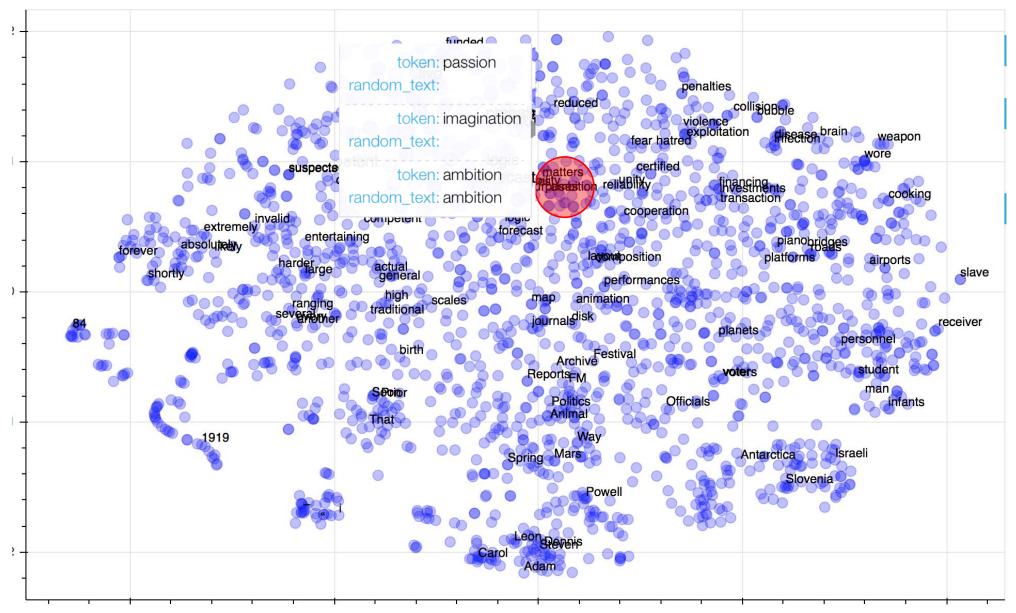


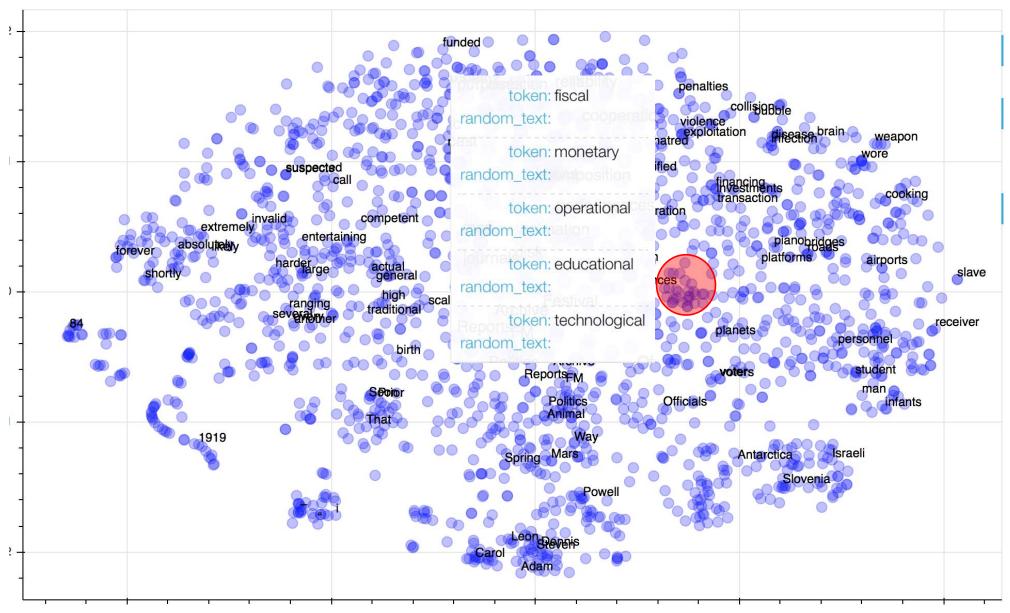


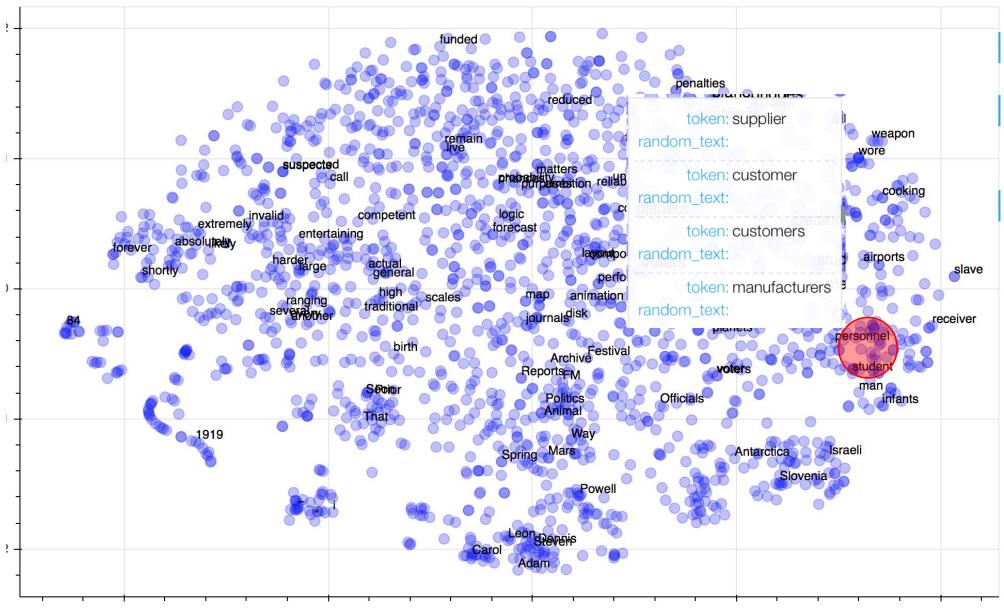


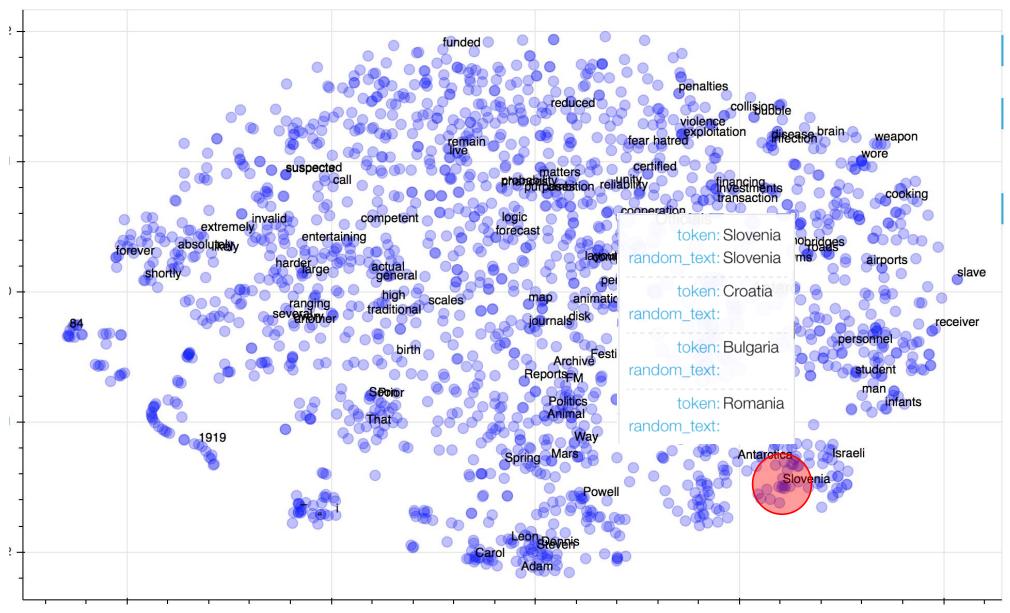


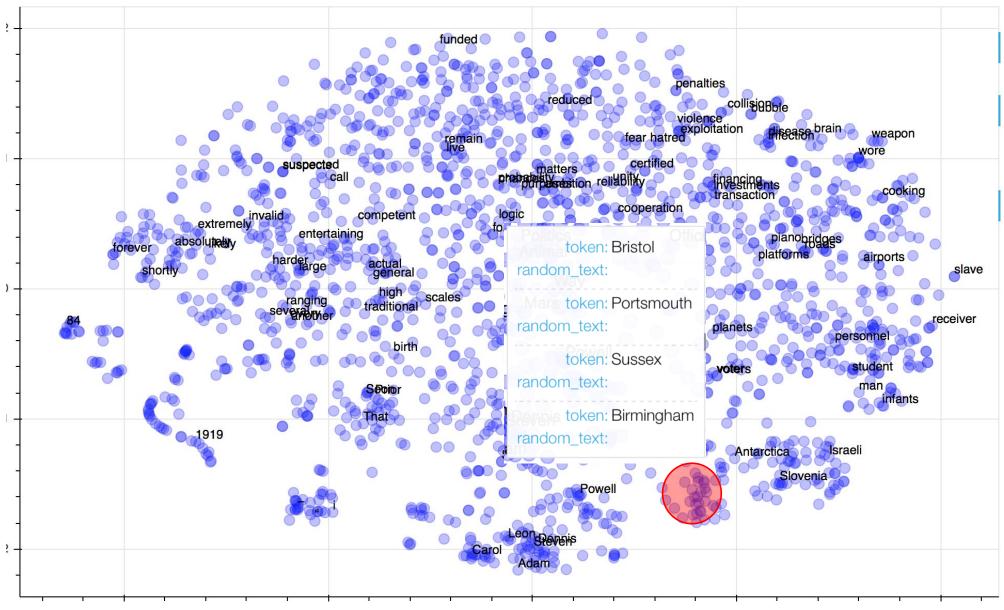


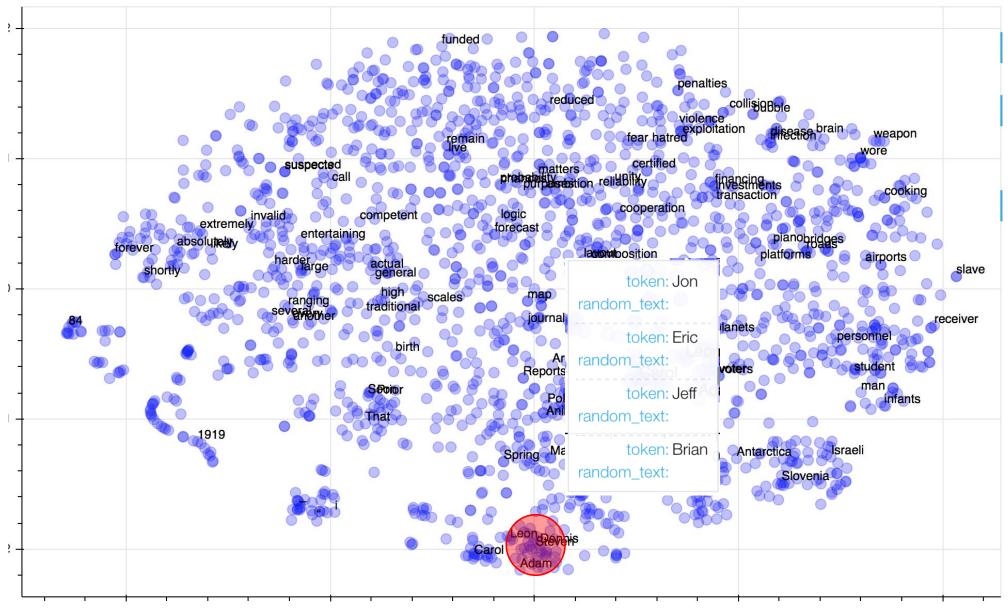


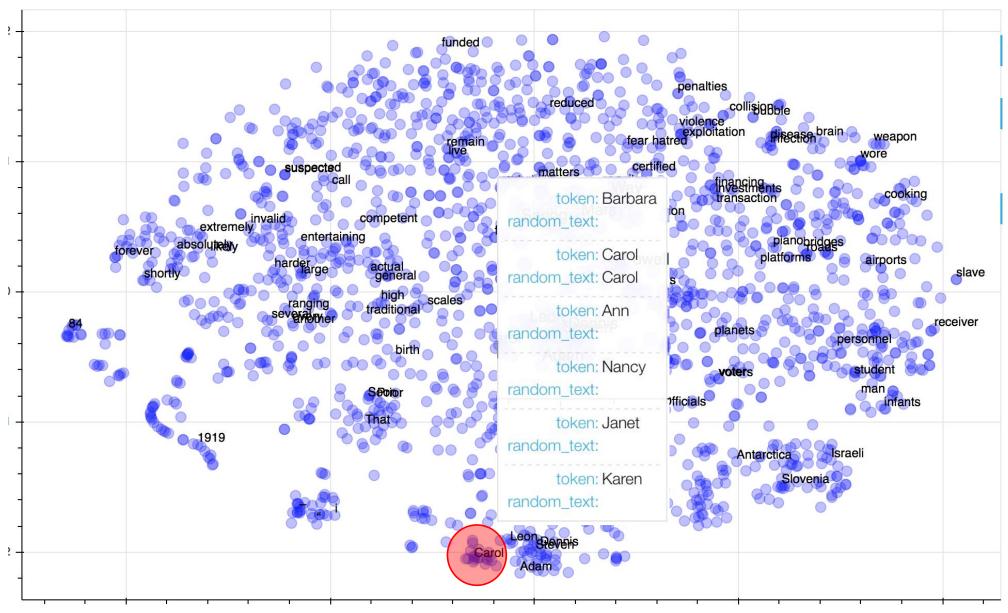


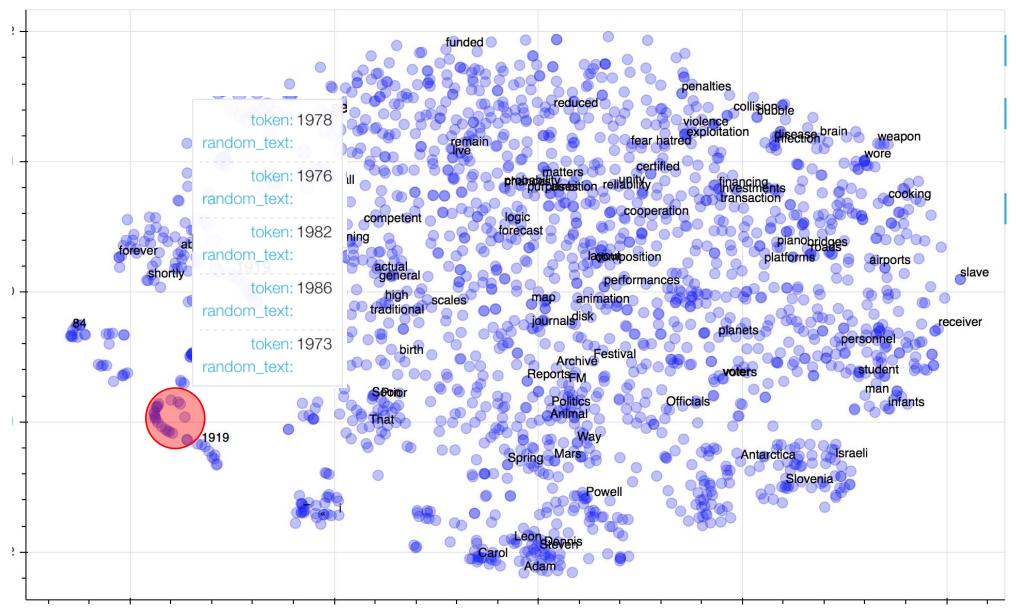












How to evaluate embeddings

Intrinsic: evaluation on a specific/intermediate subtask

- ➢ word analogies: "a is to b as c is to ____?"
- word similarity: correlation of the rankings
- **>** ...

Extrinsic: evaluation on a real task

- > take some task (MT, NER, coreference resolution, ...) or several tasks
- > train with different pretrained word embeddings
- if the task quality is better -> win!

What if...

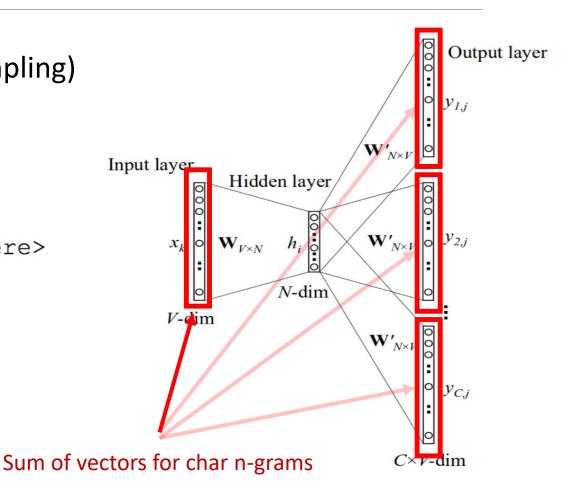
We want to use subword information?

Adding subword information: FastText

Model: SG-NS (skip-gram with negative sampling)

Change the way word vectors are formed:

- P each word represented as a bag of character
 n-gram <wh, whe, her, ere, re> <where>
- associate a vector representation to each ngram
- represent a word by the sum of the vector representations of its n-grams



Bojanovsky et al, TACL 2017 http://aclweb.org/anthology/Q17-1010

Add there any function of chars - get new embeddings!

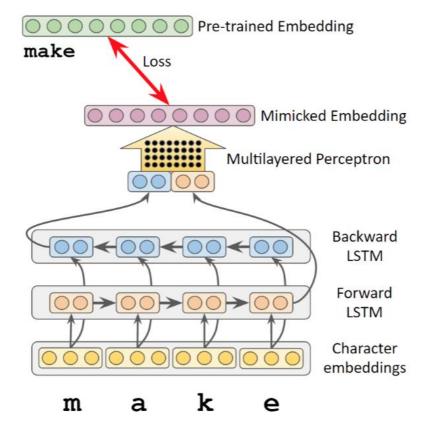
Char-aware word embedding recipe:

- > take any model that learns word embeddings
- > choose how to get word representation from representation of chars of char n-grams (RNN, CNN, pooling mean, sum, etc., anything reasonable)
- > replace word vector in the model with the representation gathered from char/subword representations
- > train as before
- > DONE!

Or just pretend to be some other embeddings!

Match the predicted embeddings $f(w_k)$ to the pre-trained word embeddings e_{w_k} , by minimizing the squared Euclidean distance:

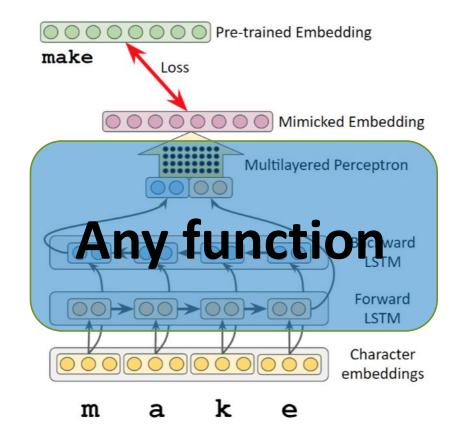
$$\mathcal{L} = \|f(w_k) - oldsymbol{e}_{w_k}\|_2^2$$



Or just pretend to be some other embeddings!

Match the predicted embeddings $f(w_k)$ to the pre-trained word embeddings e_{w_k} , by minimizing the squared Euclidean distance:

$$\mathcal{L} = \|f(w_k) - oldsymbol{e}_{w_k}\|_2^2$$



What if...

We abstract the skip-gram model to the sentence level?

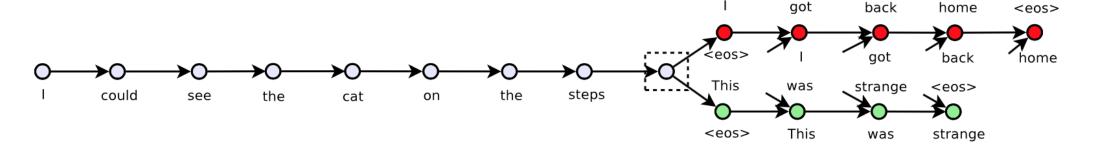
Skip-Thought Vectors

Before:

use a word to predict its surrounding context

Now:

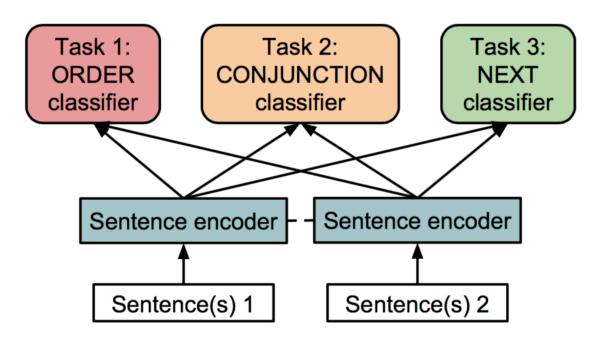
encode a sentence to predict the sentences around it



Discourse-Based Objectives

If for sentence embedding information about neighboring sentences is useful, let's predict something about them:

- Binary Ordering of Sentences
- ➤ Next Sentence (classifier)
- Conjunction Prediction (predict a conjunction phrase if the second sentence starts from any)



Jernite et al., 2017, https://arxiv.org/pdf/1705.00557.pdf

What if...

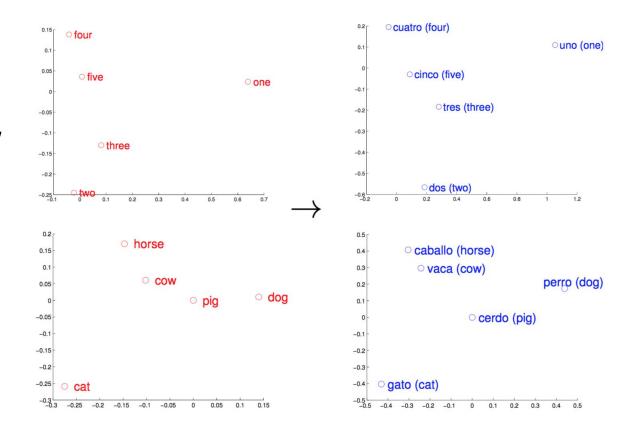
We exploit the structure of semantic space?

Exploiting Similarities among Languages for Machine Translation

- we are given a set of word pairs and their associated vector representations
- > find a transformation matrix W

$$\min_{W} \sum_{i=1}^{n} \|Wx_i - z_i\|^2$$

for any given new word we can map it to the other language space



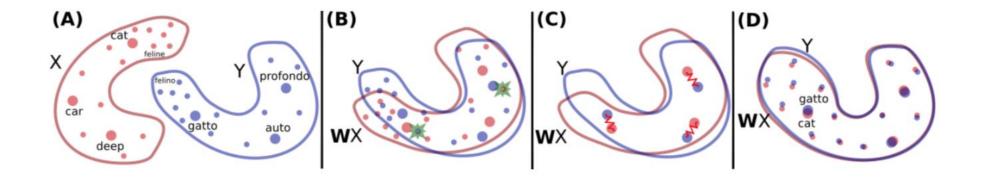
Here we supposed that we already know some word pairs.

But what if we know nothing about the languages?

Word Translation Without Parallel Data

Map semantic spaces so that their samples are indistinguishable

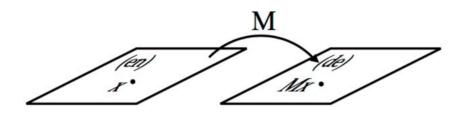
(Spoiler alert! You'll know how to do it later in the course)

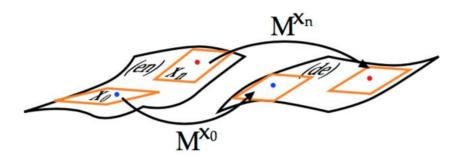


Are the underlying maps really linear?

Look at the local linear approximations:

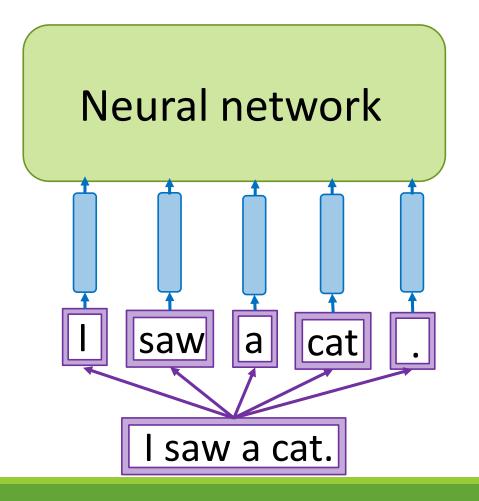
- ➤ If they're identical, then the mapping is indeed linear
- ➤ If they are not, probably not (actually, they're not)





A piece of practice: When we really need to learn word representations?

Why do we need word representation?



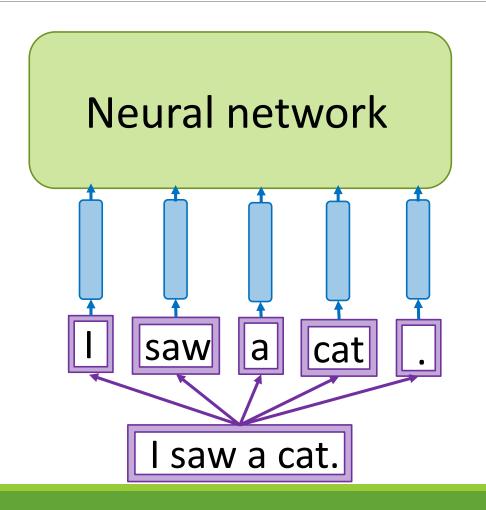
Any NN for solving any task

Word representation - vector (word embedding)

Sequence of tokens

Text

Do we REALLY need to learn word representation in advance?



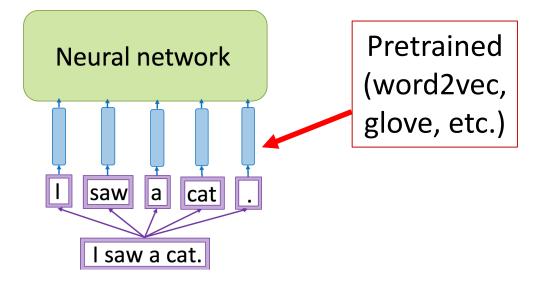
Ok, but if we already
have an NN for our task,
why do we have to learn
parameters for word
embeddings using some
other NN?

When to use pretrained embeddings?

Not enough data or the task is too simple



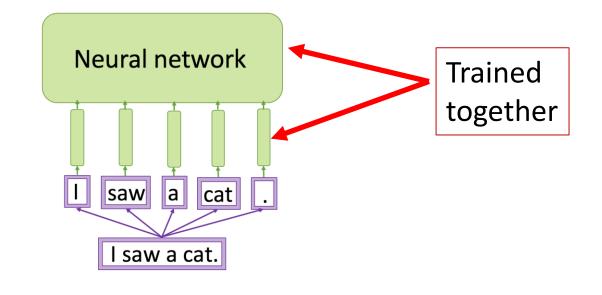
Use pretrained on the other task



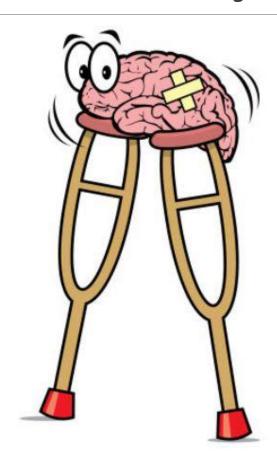
Enough data and a hard task (LM, MT, ...)



Train with the model

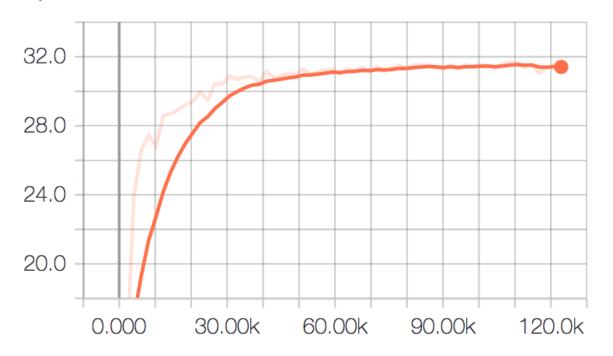


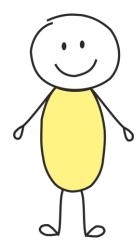
Hack of the day



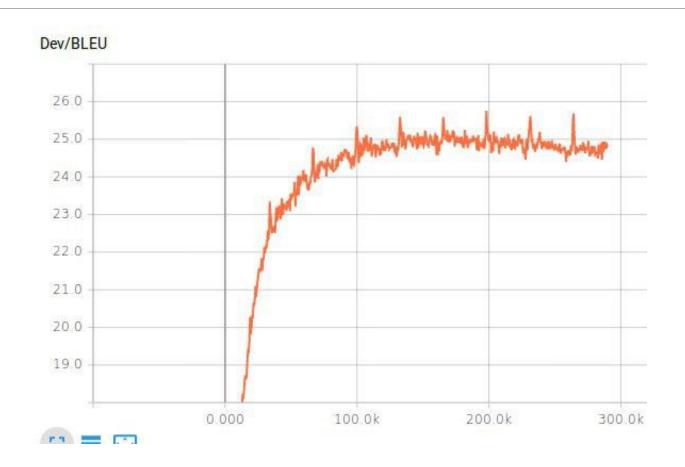
Tensorboard of a healthy man

Dev/BLEU



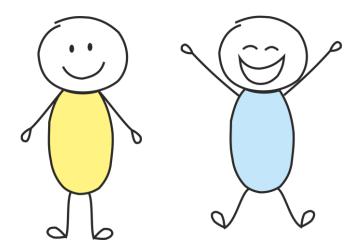


Tensorboard of a man who doesn't shuffle his data





Shuffle your data!



Congratulations, you've just survived the first NLP lecture!

Looking forward to the next week's episode...

Sincerely yours, Yandex Research