

$$(A) MR_A = MC: 100 - 2q_A = 20 \Rightarrow q_A = 40 \Rightarrow p_A = 60$$

$$MR_B = MC: 80 - 2q_B = 20 \Rightarrow q_B = 30 \Rightarrow p_B = 50$$

(B) 先将需求水平相加

$$\begin{cases} p = 100 - q, & q \leq 20 \\ p = 90 - 0.5q, & q > 20 \end{cases} \Rightarrow \begin{cases} MR_1 = 100 - 2q, & q \leq 20 \\ MR_2 = 90 - q, & q > 20 \end{cases}$$

$$\text{令 } MR_1 = MC \Rightarrow 100 - 2q = 20 \quad q = 40 \text{ (舍)} \\ \text{再令 } MR_2 = MC \Rightarrow 90 - q = 20 \quad q = 70 \text{ (舍)} \Rightarrow p = 55$$

$$\pi = 55 \times 70 - 20 \times 70 = 2450 = PS$$

$$CS = CS_A + CS_B = 1325 \quad TS = 3775$$

$$(C) F = (80 - p) \times q / 2 = (80 - p)(80 - p) / 2 = (80 - p)^2 / 2$$

$$\pi = 2F + (p - 20)(q_A + q_B) = (80 - p)^2 + (p - 20)(180 - 2p) = -p^2 + 60p + 2800$$

$$\text{由一阶条件可得: } p = 30 \text{ 故 } F = 1250 \quad q = 170 \quad \pi = 3700$$

$$CS = CS_A(p=30) + CS_B(p=30) - 2F = 2450 + 1250 - 2500 = 1200$$

$$TS = CS + PS = 1200 + 2500 = 3700$$