

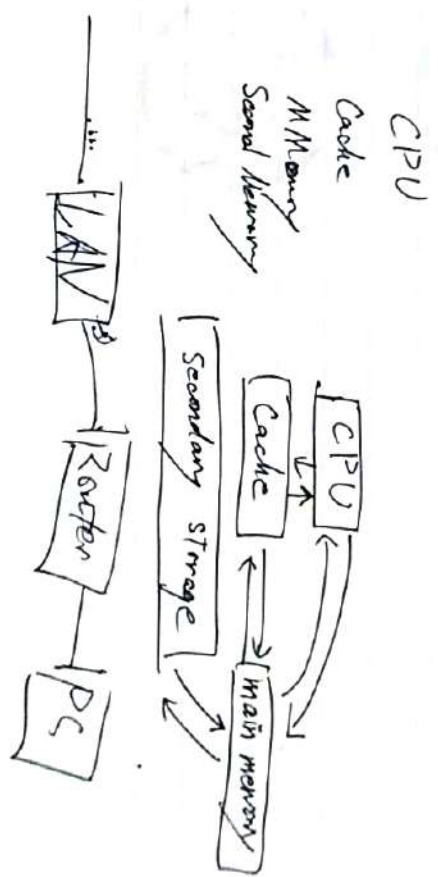
资料结构

Chapter 1 Recursion.

- Recursive Functions.

- Factorials! 阶乘
- Greatest Common ~~Factor~~ Divisor
- Search in array
- Fibonacci Series
- Combinatorial numbers 组合数
- Towers of Hanoi 河内塔

⇒ Break problem into smaller identical problem.
(Divide AND Conquer)



三 匪首 刑口 彭瑞 1990.11.15

3 remove last character

```
void Writebackward(string s, int size) {
```

$$\text{cout} \ll \text{s.substr}(\text{size}-1, 1);$$

3
4
(
.
.
(
.



```
void mergeFromBackward (const char arr1[], int first, int last) {
    if (first == last) {
```

cast (author [last]);

writing backward (antway, first, last - 1)

—

3

ex, given a, b , add a to b and return a sum.

```
void sum (int a, int b) {
```

$$\{ \text{if } (a \leq b)$$
$$\text{return sum}(a+1, b) + a$$

{ else {

return a

3

$$\sum$$

Greatist Common Diver

$$= \gcd(x, y \bmod x) \text{ if } y > x$$
$$= \gcd(1, x \bmod y) \text{ if else.}$$
$$gcd(x, y) = y$$

if $x \bmod y = 0$

$$\gcd(x, y) \text{ otherwise.}$$

2

$\text{gcd}(3, 6963)$

new 4-0

$$\text{int_gcd} \frac{2}{n} (\text{int } x, \text{int } y) \{$$

14 (20%) 42

of winter

return gcd2(x, x%y)

3 // end page 2

```
int gcd1(int x, int y) {
```

$$\text{if } (y = 0)$$

24 May 1964

$$\{ \text{else if } (x < 4) \}$$

```
return gcd1(x, y mod x)
```

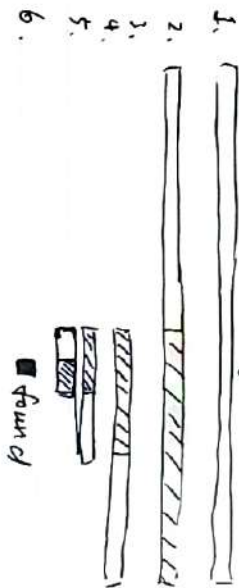
3
else

return gcc11 y, x mod y)

$$9 \times 4 = 6$$
$$\Rightarrow \text{ped}(9, 6)$$
$$\Rightarrow gcd(1(6, 9 \bmod 6))$$
$$y_{cd} \equiv 6 \pmod{5}$$

$\Rightarrow H = 0$, return 3

Binary Search in array: target



Recursive Solution for finding max item in array.

```

if (array has only one item) {
    return maxArray (array) is the only item in array.
} else if (array > 1 item) {
    return max (maxArray (left half of array),
                maxArray (right half of array))
}
    
```

Find k^{th} smallest item

need pivot item
cleverly arranging / partitioning the items in the array about this pivot.

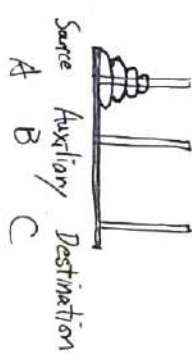


```

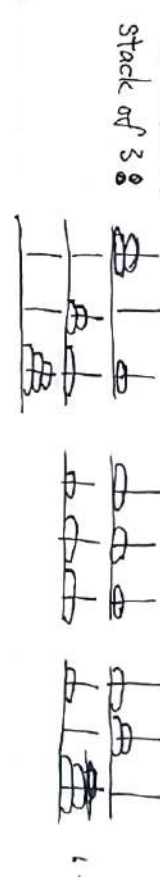
kSmall (k, array, first, last)
= kSmall (k, array, first, pivotIndex - 1) // 左半邊
if k < pivotIndex - first + 1
= P // k = pivotIndex - first + 1 終止條件
if k > pivotIndex - first + 1
    pivotIndex++
    kSmall (k - (pivotIndex - first + 1), array, pivotIndex + 1, last)
if k > pivotIndex - first + 1
    pivotIndex--
    kSmall (k - (pivotIndex - first + 1), array, pivotIndex - 1, last)
    
```

int kSmall (int k, string array, int first, int last) {
if (first > last) return -1;
}

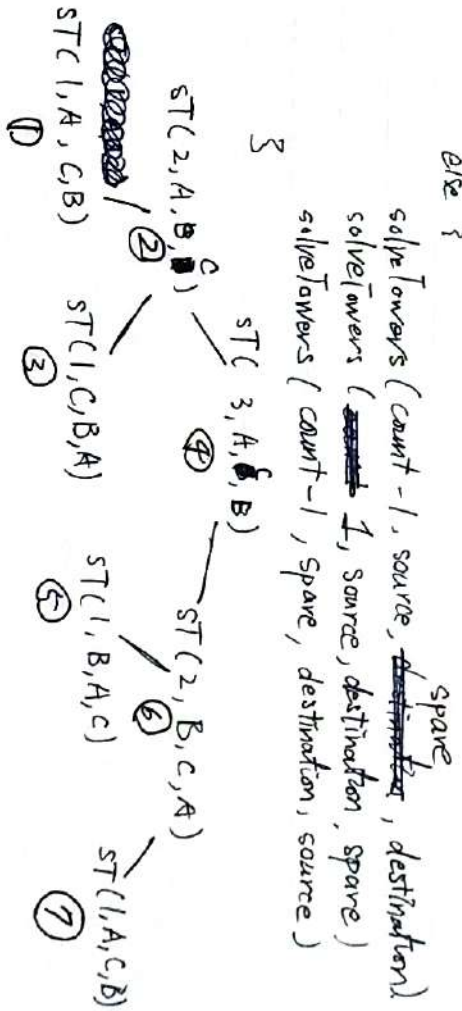
Tower of Hanoi 河內塔



for stack of 2, move time: $3 = 2^2 - 1$
for stack of 3, move time: $7 = 2^3 - 1$



void solveTowers (count, source, destination, spare) {
if (count is 1)
move a disk from source to destination.
else {
solveTowers (count - 1, source, spare, destination);
solveTowers (count - 1, source, destination, spare);
solveTowers (count - 1, spare, destination, source);
}}



Binary Recursion 二次遞迴

2 Recursive call for non-base case.

刻度尺

- 劃 4 個虛線前中間有個 3 虛線。
- 劃 3 " 前劃 2 " "
- 劃 2 " 前劃 1 " "
- base case : 1 個 " "

drawTicks (length) { \Leftarrow 畫 N 刻度

if (length > 0) {

drawTicks (length - 1)

draw ticks with length.

drawTicks (length - 1)

void drawRuler (int inches, int majorLength) {

drawOneTick (majorLength, 0); \Leftarrow 主刻 1 度

for (int i = 1; i < inches; i++) {

drawTicks (majorLength - 1); \Leftarrow 主刻度

drawOneTicks (majorLength, i);

把一個數 a 加到 b.

Linear Recursion.

int sum (int a, int b) {

if (a == b)

return a;

return a + sum (a + 1, b);

binary recursion.

int sumB (int a, int n) {

if (n == 1)

return a;

return sumB (a, $\frac{n}{2}$) + sumB (a + $\frac{n}{2}$, $n - \frac{n}{2}$);

Linear called ⁸ times, 1 times addition.

binary called 15 times, 7 times addition.

which is more efficient ?? depend on the perspective.

Rabbits

month n.

rabbit (n) = rabbit (n - 1) + rabbit (n - 2);

rabbit (2) = 1

rabbit (1) = 1

Fibonacci sequence. 1, 1, 2, 3, 5, 8, 13, 21, 34...

nth num equals to the sum of the 2 numbers before n.

low efficiency.

int rabbit (int n) {

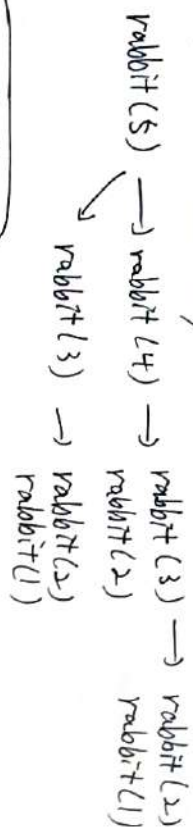
if (n <= 2) {

return 1

return rabbit (n - 1) + rabbit (n - 2);

Fibonacci Sequence.

if $n = 5$, how many times did rabbit call?



called 9 times

n_k be num of recursive calls.

$$\begin{aligned}
 n_1 &= 1 & n_2 &= 1 \\
 n_3 &= n_1 + n_2 + 1 = 3 \\
 n_4 &= n_3 + n_2 + 1 = 5 \\
 n_5 &= n_4 + n_3 + 1 = 9 \\
 n_6 &= n_5 + n_4 + 1 = 15 \\
 n_7 &= n_6 + n_5 + 1 = 25 \\
 n_8 &= n_7 + n_6 + 1 = 41
 \end{aligned}$$

n_k ~~state~~ at least other time.
DOUBLE
 隨 k 增加時叫次數大增

or $n_k \geq 2^{\frac{k}{2}}$, exponential growth.
 可用空間換時間，把算到的答案存下，下次可查表。

Linear recursion Fibonacci

Algorithm LinearFibonacci(k) {

if ($k=1$)

return ($k, 0$)

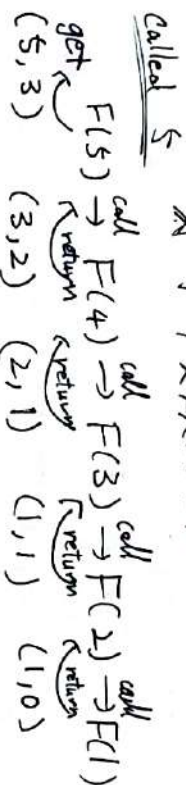
else

(i, j) = LinearFibonacci($k-1$)

return ($i+j, i$)

}

呼叫次數線性成長



Computing Power. $n+k$ times.

$$\begin{aligned}
 x^0 &= 1 \\
 x^n &= (x^{\frac{n}{2}})^2 \quad \text{for even } n. \\
 x^n &= x \cdot (x^{\frac{n-1}{2}})^2 \quad \text{for odd } n.
 \end{aligned}$$

double power ~~algorithm~~ (double x , int n) {

if ($n == 0$)

return x ;

else {

double halfpower = power($x, \frac{n}{2}$);

if ($n \% 2 == 0$) { // even

return (halfpower * halfpower)

} else { // odd

return x * halfpower * halfpower }

} // big else.
 } power

ex: $9^4 \Rightarrow$ power($9, 4$)

$$\begin{aligned}
 \text{power}(9, 2) &\Rightarrow 81 \times 81 = 81^2 = 9^4 \\
 &\quad \swarrow \searrow \\
 &\quad 9 \quad 9
 \end{aligned}$$

2 multiplication

3 recursive calls

k multiplication count

32(1) → 16(1) → 8(1) → 4(1) → 2(1) → 1(1) → 0(0)

17 times multiplication

$9^{10} \Rightarrow$
 19(2) → 9(2) → 4(1) → 2(1) → 1(1) → 0(0)

8 times multiplication

Ex. 哪个整数最接近且小于 30

get Value (int first, int last, int n)
get Value (1, 30, 30)

```
int get Value (int a, int b, int n) {
    int return Value;
    int c = (a+b)/2;
    if (c * c <= n) && (n < ((c+1)*(c+1)))
        return value = c;
    else if (c * c > n) {
        return Value = get Value (a, c-1, n);
    }
    else {
        return Value = get Value (c+1, b, n);
    }
}
```

~~return return Value;~~
return return Value;
} // get Value.

Ex Practice 15.

Acker(m, n) = n + 1 if m = 0
= Acker(m-1, 1), if n = 0
= Acker(m-1, Acker(m, n-1)), otherwise

what is (1, 2)
A(0, A(1, 1)) → A(0, 3) = 4
A(0, A(1, 0)) → A(0, 2) → 3
A(0, 1) → 2

Ex.

Mr. Spock's Dilemma
choosing k out of n things

in terms of Earth: $k \subset n$.

$C(n, k)$ = the number of groups of k planets that include Earth
+ the number of groups of k planets that do not include Earth.

$C(n, k)$ = ways of choosing k-1 out of n-1 things + ways of choosing k out of n-1 things

$C(n, k) = C(k-1, n-1) + C(n-1, k)$
what's the base case?

$C(1, 1) = 1$, $C(k, k) = 1$ only one choice.
 $C(n, 0) = 0$ don't go, so only one choice.
 $C(n, k) = 0$ if $k > n$ 怎么.

ex: $C(4, 2)$
 $C(3, 1) + C(3, 2)$
 $C(2, 0) + C(2, 1)$
 $C(1, 0) + C(1, 1)$
 $C(1, 0) + C(1, 1)$
1 1 1 1 1 1 1 1 1 1

result: 6 combination.
total recursive called: 11
2 $C(n, k) - 1$ = num of recursive calls
because base case = 1 and
leaf node - internal node = 1

Observation from $C(n, k)$

- base case return 1
- num of recursive calls to non-base cases is equal to internal node $= C(n, k) - 1$.

Chapter 2.

Data Abstraction.

Classes \rightarrow encapsulation, inheritance.

Cohesion - module performs a single task well. (high)
Coupling - measure of dependence among modules. (low)

Operation Contracts

1. Document limitation of the method.
2. Specify data flow
3. Do not specify how module will perform its tasks.
4. Specify pre- and post-condition.
5. unusual conditions
 - something that causes problems / throw exception.
6. begin the contract during analysis, finish during design.
1. used to document code, particularly in header file.

Key Issues in programming.

1. Modularity 模組化
2. Style
3. Modifiability
4. Ease of Use
5. Fail-safe programming
6. Debugging
7. Testing

ADT: modularity

- 模組化, systematically control
- 可以將問題獨立出來, 方便解決
- eliminate redundancies 重複
- 好讀、寫、改

2 Solution: Cohesion or Coupling
高內聚 低耦合

ADT: Function abstraction 函式/功能抽象化

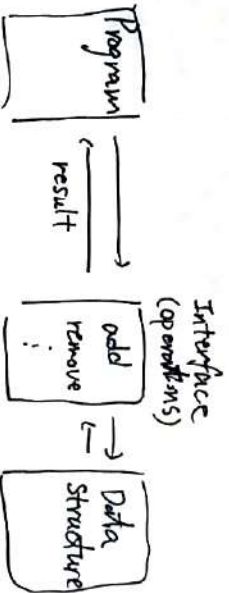
- 封裝性 & 實作分離
- module specification 講 module 怎麼運作
- 資訊隱藏: 只實作隱藏
- 引未來換成更佳的寫法

ADT: Goals.

- R operation
 - Insert, Deletion, Search, Modify, etc, interface.
- Data Abstraction
 - allow each data structure in relative isolation from rest of the solution.
 - natural extension of functional abstraction.

ADT: 有 Data / Collection of Data.

- have operations
- 封裝性: what it does
- 實作, how it does it, & include specific data structure.



Implementation

- implementation detail (data structure, how, etc) should be hidden behind ADT operations.

C++ Classes.

- Class define a new data type, etc.
- contain data members and methods.

header file: Classname.h

implementation: Classname.cpp

Constructor → initializes the object with/without value.

- scope resolution operator " :: "

e.g. Sphere :: getRadius () {}

→ a operation outside declaration of the class.

e.g. an initializer

Sphere :: Sphere () : theRadius (1.0) {}

Destructor

destrays an instance of an object when object's life time ends.

Inheritance

Super Class (base class)

inherit to Sub class (derived class)
public methods and data member

method defined / implemented outside Class.

```
void Rational :: setRational (long n, long d) {  
    if (d==0) {  
        error ("ERROR")  
    }  
    ...  
}
```

Overloading & Overriding

```
class something {  
    func1 (int a) { ... }  
    func1 (string b) { ... } ← Overloading  
}
```

⇒ same function

```
class something2 : public something {  
    func1 (long, long); ← Overriding  
}
```

C++ namespace

• A mechanism for logically grouping declarations and definitions into a common declarative region.

```
ex: namespace myNamespace {  
    // declarations  
    int a;  
}
```

ex: using namespace std;
→ allow names of the elements to be used directly.

ex: myNamespace :: a
→ Access element outside the namespace using scope resolution operator (::)

C++ standard library.
→ Item create in ↗ are declared in std namespace.
→ I/O function from c++ library.
⇒ #include <iostream.h>

Exceptions

→ handle error in execution.

→ throw exception to indicate an error has occurred.

→ try - catch ★ throw ★

```
try { ... throw (type) ... }  
catch (exception class type1) {  
    statements ...  
}
```

```
catch (type2) {  
    ...  
}
```

```
{  
    !  
}
```

→ Exception Occurred !!

1. ~~exit~~ try, local variable ← destructor.
2. catch block run
3. go to last line of try block related catch block
4. continue to run rest of the code.

→ **THROW** exception class ("string argument")

- method that throws exception have a throw clause.
- ex: void myMethod (int x) throw (MyException) {
 if ()
 throw MyException("....")
}

- use std library exception or define your own.

Define exception.

ex: # include <stdexcept>

include <string>

using namespace std;

① class ListIndexOutOfRangeException: ^{inherited from C++ std} public out_of_range {

public:

ListIndexOutOfRangeException (const string & message = "")
: out_of_range (message.c_str())

{ }
}; // end.

② class ListException: public logic_error {

public:

ListException (const string & message = "")
: logic_error (message.c_str()) { }

{ } // end

⇒ if (size > MAX_LIST) {

throw ListException ("ListException: " +
"List full on insert")

Unit 3. Linked List



- do not require the shifting of items during insertions/deletion.
- dynamically ~~memory allocated~~ expand the list / a collection of items.

Pointer

$\text{int}^* p;$ • initially undefined, not null

• static allocation.

• pointer has location (address) in memory

1. address-of operator.

$\text{int } x; \text{ int}^* p;$

$p = \&x;$ 把 x 的地址给 p.

2. $p = \text{new int};$ 申请新空间,

dynamically allocate a memory cell of size int. 要经过 new 才能正常使用内存空间.

note. can't allocate!! throw exception

std::bad_alloc in the <new> header)

3. delete p;

$p = \text{NULL};$ ← just to be safe. 彻底遗忘.

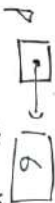
• "delete" can return dynamically allocated memory to the system for reuse. leave variable undefined.

ex: $\text{int}^* p, *q;$

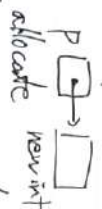
$\text{int } x;$

$p = \&x;$ → get x's address.

$*p = 6;$ → put 6 in x's address



get memory → $p = \text{new int};$



give value → $*p = ?;$ [?] → memory dynamically.

wrong → $p = \text{NULL};$ [?] → memory leak!!!

correct → delete p; $p = \text{NULL};$ [?] → deallocating memory.

• call p after delete?? dangling reference (illegal access)

delete p;

cout << *p << endl; ← wrong!

Dynamic Allocation of Arrays.

```
int arraySize = 50;
double *array = new double[arraySize];
```

一個指標指向 50 個空間

• array name is the pointer to the first element.

```
array[2] = *(array + 2)  存*才是取內容.
```

• 可±增加空間

```
double *old = array;
array = new double[3 * arraySize];  ← 重新空間
for (int i = 0; i < oldSize; i++)
    array[i] = old[i];  ← move old data to
                        new space.
```

```
delete[] old;  ← deallocate a bunch of space.
```

save File

```
#include <stdio.h>
#define STD_LEN 12
#define SR_NUM 5
typedef struct student {
    char sid[STD_LEN];
    int score;
} studentType;
```

```
int main(void) {
    FILE *outFile = NULL;
    if (outFile != NULL) {
        outFile = fopen(fileName.c_str(), "a");
        if (outFile != NULL) {
            saveFile(outFile, allS, SR_NUM);
            return 0;
        }
    }
```

```
void saveFile(FILE *fp, studentType dA[], int no) {
    for (int i = 0; i < no; i++) {
        fwrite(&dA[i], sizeof(dA[i]), 1, fp);
        cout << dA[i].sid << " " << dA[i].score << endl;
    }
    fclose(fp);
}
```

算出需要儲存元組

freelk (infile, 0, SEEK_END);
 studentNo = fteall(infile) / sizeof (studentType);
 rewind (infile);

Pointer based Linked List.

```
struct Node {
  int item;
  Node *next;
}
// has header pointer
Node *P;
// get member in node
P -> item.
```

deletion.



$P \rightarrow next$
 $Node * P2 = P \rightarrow next \rightarrow next;$
 $Node * P3 = P2 \rightarrow next;$

delete P2; $P2 = NULL;$ *avoid dangling reference.*
 $P \rightarrow next = P3;$

Insertion.



$Node * P2 = P \rightarrow next;$
 $P \rightarrow next = PN;$
 $PN \rightarrow next = P2;$

visit

a sorted linked list for insert/delete.
 到位置才能做事.

$Node * prev, * cur;$

for ($prev = NULL, cur = head;$ $cur != NULL$) && (new value > $cur \rightarrow item$) { $prev = cur;$; $cur = cur \rightarrow next;$ };

if ($prev = NULL$) {

$head = cur \rightarrow next;$;

else $prev \rightarrow next = cur \rightarrow next;$;

$cur \rightarrow next = NULL;$;

delete cur;

$cur = NULL;$;

delete { }

insert { }

if ($prev = NULL$) {

$newPtr \rightarrow next = head;$;

$head = newPtr;$;

else {

$newPtr \rightarrow next = cur;$;

$prev \rightarrow next = newPtr;$;

}

My Notes

Important Concepts worth keeping

Pointer - base list implementation

Today: / /

```
#include "ListException.h"
#include "ListIndexOutOfRangeException";
```

```
typedef int ListItemType;
class List {
public:
```

```
List();
```

```
bool isEmpty() const;
```

```
int getLength() const;
```

```
void insert(int index, const ListItemType & newItem);
throw (ListIndexOutOfRangeException, ListException);
```

```
void remove(int index); throw (ListIndexOutOfRangeException);
```

```
void retrieve(...);
```

```
struct Node {
```

```
ListItemType item;
```

```
Node *next;
```

```
}
```

```
Node * find(int index) const; // 找位置
```

```
}
```

dynamically allocated memory 需要自己写 destructor.

```
List::~~List() {
```

```
while (!isEmpty())
```

```
remove();
```

```
}
```

My Questions

Problems & Difficulties needing exploration

shallow copy head 复制到, 但资料还是一份

deep code 内存有两份

ex: good. List x(y);

y is a existing list, x initializes with data in y.

```
List::List(const &alist): size(alist.size)
{
if (alist.head == NULL)
```

```
head = NULL;
```

```
else
```

```
head = new ListNode;
```

```
head->Item = alist.head->Item;
```

```
for (ListNode * origPtr = alist.head->next;
```

```
origPtr != NULL; origPtr = origPtr->next)
```

```
{ newPtr->next = new ListNode;
```

```
newPtr = newPtr->next;
```

```
} newPtr->next = newPtr->next; // deep copy
```

```
} // 一个变数记 2 个地址 (newPtr, newPtr->next)
```

```
newPtr->next = NULL;
```

```
} // end else // remove number //
```

```
} // end list
```

My Opinions

Thoughts, inspirations, and suggestions

密碼 (password)

My Notes

Important Concepts worth keeping

Today: / /

Pointer - base List implementation

include "ListException.h"
include "ListIndexOutOfRangeException.h"

typedef int ListItemType;
class List {
public:

List();

bool isEmpty() const;

int getLength() const;

void insert(int index, const ListItemType & newItem)
throw (ListIndexOutOfRangeException, ListException);

void remove(int index) throw (ListIndexOutOfRangeException);

void retrieve(...);

struct Node {

ListItemType item;

Node *next;

};

Node * find(int index) const; // 找位置

}

dynamically allocated memory 需要自己写 destructor.

List::~List() {

while (!isEmpty())

remove();

}

My Questions

Problems & Difficulties needing exploration

shallow copy head 复制到, 但资料还是一份

deep code 所有东西有两份

ex: goal. List x(y);

y is a existing list, x initializes with data in y.

List::List(const &alist): size(alist.size)

{ if (alist.head == NULL)

head = NULL;

else

{

head = newListNode;

head->item = alist.head->item;

for (ListNode* origPtr = alist.head->next;

origPtr != NULL; origPtr = origPtr->next)

{ newPtr->next = new ListNode;

newPtr = newPtr->next;

} newPtr->item = item; // deep copy

}

一个变数记 2 个地址 (newPtr, newPtr->next)

newPtr->next = NULL;

} // end else // remember

;

} // end list

My learning whether repeat



My Opinions

Thoughts, inspirations, and suggestions

newPtr->item = item; // deep copy

}

一个变数记 2 个地址 (newPtr, newPtr->next)

newPtr->next = NULL;

} // end else // remember

;

} // end list



2

We are to learn, not just to be taught; Work smarter, not just harder.

來為求學，非僅受教；不以力博，要以智取。——《三呆斜說》

3

My Notes

Important Concepts worth keeping

Today: / /

Linked list saved in a file.

- store only data, no pointers.
- treat first case differently.
- recreate list by placing each item at the end of the list.

Saving

```
ofstream outFile ( filename );
for ( Node * cur = head ; cur != NULL ; cur = cur->next )
{
    outFile << cur->item << endl;
}
```

Reading

```
ifstream inFile ( filename );
int nextItem;
if ( inFile >> nextItem )
{
    try { head = new Node;
```

```
        head->item = nextItem;
        head->next = NULL;
        tail = head;
    while ( inFile >> nextItem ) {
        tail->next = new Node;
        tail->tail->next;
        tail->item = nextItem;
        tail->next = NULL;
    } // while.
```

```
    } // try
    catch ( bad_alloc e ) { }
} // end if
inFile.close();
```

6 Right is right even if no one is doing it; wrong is wrong even if everyone is doing it.

My Questions

Problems & Difficulties needing exploration

Passing a linked list to a method.

- having access to head means having access to the whole list
- Pass head pointer to a method as a reference argument.

Linked List ~~X~~ recursion.

sorted list??

1. head == NULL;
 2. head->next == NULL;
 3. head->item < head->next->item
and head->next point to a sorted linked list
- Print list backward.
 - Write the list minus its first item backward
 - Write the first item backward.

Object as a linked list.

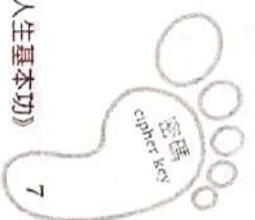
My Opinions

typed ClassName itemType;

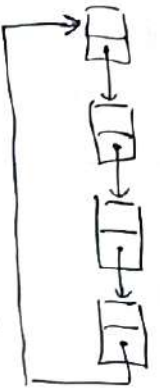
```
struct Node {
    itemType item;
    Node * next;
};
```

把多個同一個class 物件串連起來。

一件不對的事，大家都在做，仍舊是不對的事。--潘國《人生基本功》



Δ Circular linked list.



• no node in list contains NULL

• make a ptr to last node not head.

Δ Dummy head/node.

• ~~if~~ head is special case.



Node * prev, * cur;

for (prev = head, cur = head->next)

(cur != NULL) && (newval > cur->item)

prev = cur, cur = cur->next

{ if (cur != NULL) {

prev->next = cur->next;

cur->next = NULL;

delete cur;

cur = NULL;

}

{ // for

insert { newPtr->next = cur;

prev->next = newPtr;

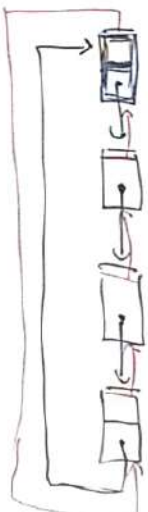
My Questions

Problems & Difficulties needing explanation

Doubly linked list.

- each node point to both predecessor & successor
- often has a dummy head node & circular to eliminate special case.

Δ Circular Doubly linked list with dummy head node.



delete

(cur->precede)->next = cur->next;

(cur->next)->precede = cur->precede;

insert

newPtr->next = cur;

newPtr->precede = cur->precede;

(cur->precede)->next = newPtr;

(cur->precede)->precede = newPtr;

My Opinions

Thoughts, inspirations, &

