

# My Notes

Important Concepts worth keeping

Today: / /

## Priority Queues

- 和 selection sort 類似 ↗ selection sort: Unsorted List
- 它的 Insert() 為  $O(1)$ , Delete 為  $O(n)$
- 和 Insertion sort 類似 ↗ Insertion sort: sorted List
- 它的 Insert() 為  $O(n)$ , Delete 為  $O(1)$
- Tree sort = Binary search Tree.

## Heap

→ Balanced Binary Tree.

- 有 min-heap, max-heap (基本堆積)

What is a heap?

- ① a complete binary tree.
- ② a node is greater (smaller) or equal to the values sorted at the children (最大 or 最小)

If you don't know where you're going it doesn't matter what path you take.

- Lewis Carroll

## My Questions

Problems & Difficulties needing exploration

- max-heap  $\rightarrow$  最大的元素一定在樹根
- min-heap  $\rightarrow$  最小的元素一定在樹根

如何插入元素到 heap 裡？

- ① 插入新的元素在 next bottom right most place
- ② 呼叫堆積的 function.

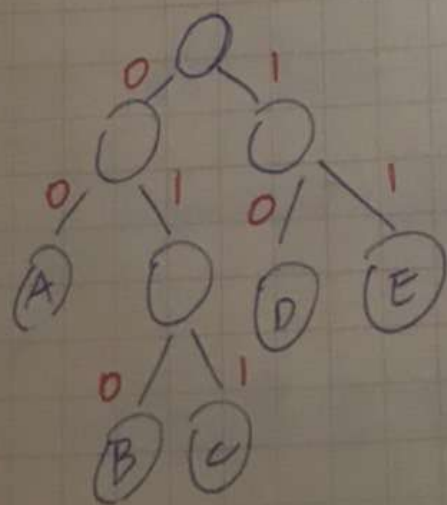
如何移除最大的元素？

- ① 先將 bottom 的資料複製到樹根
- ② 刪除 bottom
- ③ 呼叫堆積的 function.

## My Opinions

Thoughts, inspirations, and suggestions

Huffman coding 霍夫曼編碼



A = 00

B = 010

C = 011

D = 10

E = 11

$\rightarrow$  出現次數越高，  
編碼的數字要  
比較少

密碼  
cipher key

如果你不知道你要去哪裡，那麼現在你在哪裡一點都不重要。

《愛麗斯夢遊記》



# My Notes

Important Concepts worth keeping

Today: / /

Heap sort 的方法

- 問  $n$  次，可以知道排序的結果  $O(n \times \log n)$  <sup>問  $n$  次</sup>
- 移除 root，一開始為 swap  $O(1)$ ，而後來為排序  $O(\log n)$ ，所以時間複雜度為  $O(n)$

## Min-max Heap

① decide which level  $\rightarrow$  min or max

② 確認需不需要交換

- 效率為  $O(\log n)$
- 如不需交換還是需要往上比。

△ Heap 不適合做搜尋

## My Questions

Problems & Difficulties needing exploration

### • unsorted array - based

- Insertion  $O(1)$
- Deletion  $O(n)$  → shifting data 和資料量成正比
- Retrieval  $O(n)$  → sequential search 和資料量成正比

### • sorted array - based.

- Insertion & deletion  $O(n)$  → shifting data
- Retrieval  $O(\log n)$  → binary search

### • unsorted pointer - based

- No data shift
- Insertion  $O(1)$  → 直接加入
- Deletion & Retrieval  $O(n)$  → sequential search

### • sorted pointer - based

- No data shift
- Insertion, Deletion & Retrieval  $O(n)$

△ 不一定要先做排序





# My Notes

Important Concepts worth keeping

Today: / /

## △ Binary Search Tree

tree Height 無法保證

→ Maximum  $\sim n$

→ Minimum  $\sim \log_2(n+1)$

## 2-3 Tree

- Have 2-nodes and 3-nodes

→ A 2-node has one data item and two children

→ A 3-node has two data item and three children

- 不是二元樹

- 樹比較矮，因有些可放兩個 key.

- 左邊小，右邊大.

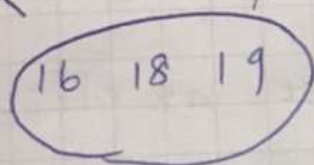
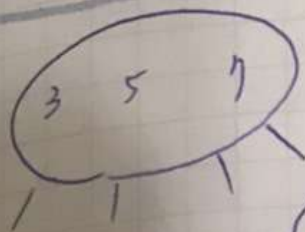
- a leaf may contain either one or two data items

- 2-3-4 樹效率比 2-3 樹效率高

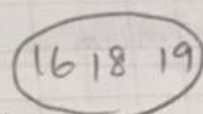
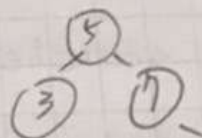
## My Questions

Problems & Difficulties needing exploration

2-3-4 樹



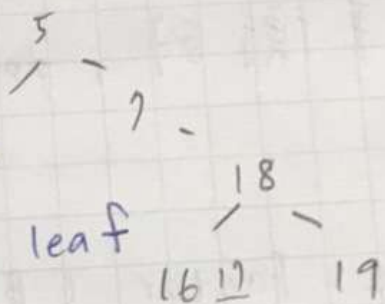
16 17 18 19



→ 避免遞迴，遇到有三個的就分裂

→ 保證  $\log n$  做完

• splits occur only at the path from the root to a leaf



• No recursion (upward)

## My Opinions

Thoughts, inspirations, and suggestions

△ 效率好，樹高矮。!!!

# My Notes

Important Concepts worth keeping

Today: / /

## AVL tree

- A balanced binary search tree.
- Can be searched almost as efficiently as a "minimum-height" binary search tree.
- Maintains the tree height close to the minimum

→ 要是平衡的，如果不是要利用 rotate 使它平衡。

### △ Balance Factor (BF)

$$BF(\text{a node}) = h(\text{left subtree}) - h(\text{right subtree})$$

→ any node in a binary search tree differ by no more than **1**

→ 如果不是 1 或 -1 代表它不平衡。



## My Questions

Problems & Difficulties needing exploration

有四種情況

$$BF(x) = +2, BF(x \rightarrow \text{left}) = +1 \text{ or } 0$$

① Height of  $x \rightarrow \text{left}$  為  $2$ , Height of  $x \rightarrow \text{left} \rightarrow \text{left}$

為  $1 \Rightarrow$  它為 single rotation with left child (LL)

$$BF(x) = -2, BF(x \rightarrow \text{right}) = -1, 0$$

② Height of  $x \rightarrow \text{right}$  為  $2$ , Height of  $x \rightarrow \text{right} \rightarrow \text{right}$

為  $1 \Rightarrow$  它為 single rotation with right child (RR)

$$BF(x) = +2, BF(x \rightarrow \text{left}) = -1$$

③ Height of  $x \rightarrow \text{left}$  為  $2$ , Height of  $x \rightarrow \text{left} \rightarrow \text{right}$

為  $1 \Rightarrow$  它為 double rotation with left child (LR)

$$BF(x) = -2, BF(x \rightarrow \text{right}) = +1$$

④ Height of  $x \rightarrow \text{right}$  為  $2$ , Height of  $x \rightarrow \text{right} \rightarrow \text{left}$

為  $1 \Rightarrow$  它為 double rotation with right child (RL)



# My Notes

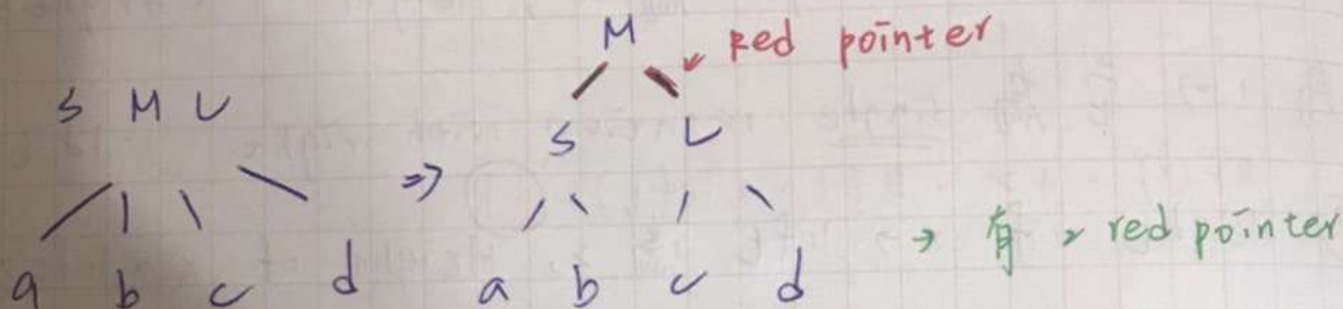
Important Concepts worth keeping

Today: / /

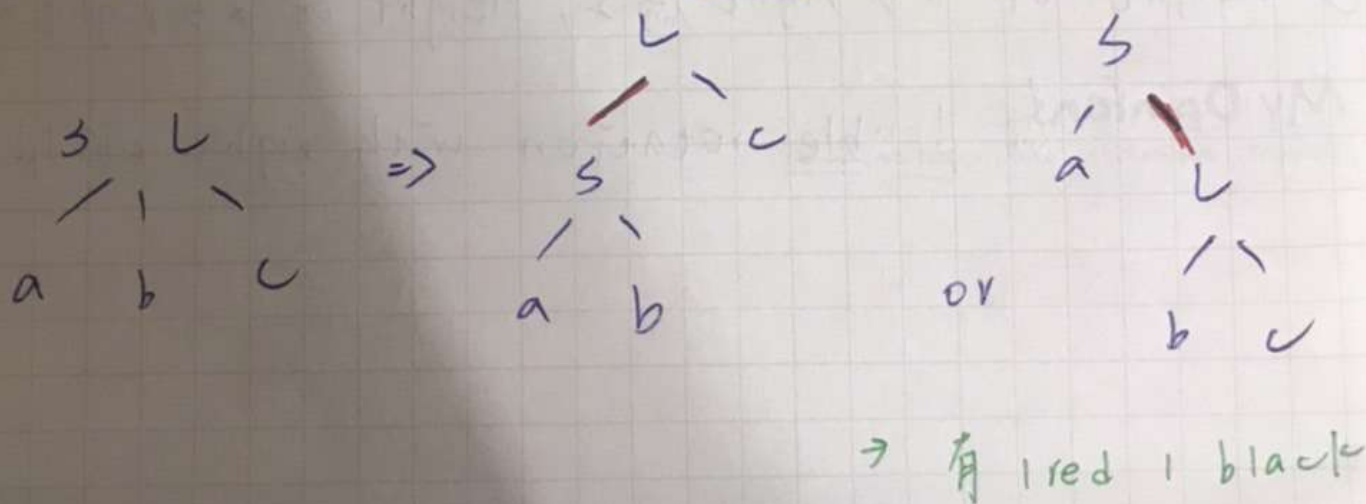
## red-black tree

• 每一個紅黑樹對應一個 2-3-4 樹

△ 4-node



△ 3-node → Two choices → Not a unique representation



△ 2-node

→ 2 black