

# Inferència

Estimadors:  $\bar{y} = \sum_{i=1}^n Y_i / n$   $s^2 = \frac{\sum_{i=1}^n (Y_i - \bar{Y})^2}{n-1} = \frac{\sum_{i=1}^n Y_i^2 - n(\bar{Y})^2}{n-1} = \frac{\sum_{i=1}^n Y_i^2 - \frac{(\sum_{i=1}^n Y_i)^2}{n}}{n-1}$

Estadístics: “senyal / soroll” o “diferència / s.e.” segueixen una  $N$  o  $t_v$  “quocient variàncies” segueixen una  $\chi_v^2$  o  $F_v$

Paràmetre	Estadístic (i se*)	Premisses	Distribució	Interval de Confiança (1-α)% (risc α%)
$\mu$	$Z = \frac{(\bar{y} - \mu)}{\sigma / \sqrt{n}} = \frac{(\bar{y} - \mu)}{se}$	[ $Y \sim N$ o n “gran” ] i $\sigma$ coneguda	$Z \sim N(0,1)$	$[\bar{y} \pm z_{1-\frac{\alpha}{2}} se]$
$\mu$	$T = \frac{(\bar{y} - \mu)}{s / \sqrt{n}} = \frac{(\bar{y} - \mu)}{se}$	$Y \sim N$	$T \sim t_{n-1}$	$[\bar{y} \pm t_{n-1, 1-\frac{\alpha}{2}} se]$
$\pi$	$Z = \frac{(p - \pi)}{\sqrt{\hat{\pi}(1 - \hat{\pi})/n}} = \frac{(p - \pi)}{se}$ $\hat{\pi} = P$ o $\hat{\pi} = 0.5$	$(1-\pi) n \geq \approx 5$ $\pi n \geq \approx 5$	$Z \sim N(0,1)$	$[p \pm z_{1-\frac{\alpha}{2}} se]$
$\sigma^2$	$X^2 = \frac{s^2(n-1)}{\sigma^2}$	$Y \sim N$	$X^2 \sim \chi_{n-1}^2$	$\left[ \frac{s^2(n-1)}{\chi_{n-1, 1-\alpha/2}^2}, \frac{s^2(n-1)}{\chi_{n-1, \alpha/2}^2} \right]$
$\mu_1 - \mu_2$ (o $\mu_D$ )	$T = \frac{(\bar{d} - \mu_D)}{s_D / \sqrt{n}} = \frac{(\bar{d} - \mu_D)}{se}$	$D \sim N$ (2 grups aparellats)	$T \sim t_{n-1}$	$[\bar{d} \pm t_{n-1, 1-\frac{\alpha}{2}} se]$
$\mu_1 - \mu_2$	$T = \frac{(\bar{y}_1 - \bar{y}_2) - (\mu_1 - \mu_2)}{s \sqrt{1/n_1 + 1/n_2}} = \frac{(\bar{y}_1 - \bar{y}_2) - (\mu_1 - \mu_2)}{se}$ $s^2 = \frac{(n_1 - 1)s_1^2 + (n_2 - 1)s_2^2}{n_1 + n_2 - 2}$	$Y_1, Y_2 \sim N$ $\sigma_1 = \sigma_2$ desconegudes (2 grups independents)	$T \sim t_{n_1 + n_2 - 2}$	$[(\bar{y}_1 - \bar{y}_2) \pm t_{(n_1 + n_2 - 2), 1-\frac{\alpha}{2}} se]$
$\pi_1 - \pi_2$	$Z = \frac{(P_1 - P_2) - (\pi_1 - \pi_2)}{se}$ $se = \sqrt{P_1(1 - P_1)/n_1 + P_2(1 - P_2)/n_2}$	$(1-\pi) n \geq \approx 5$ $\pi n \geq \approx 5$ (2 grups independents)	$Z \sim N(0,1)$	$[(P_1 - P_2) \pm z_{1-\frac{\alpha}{2}} se]$
$\frac{\sigma_1^2}{\sigma_2^2}$	$F = \frac{s_1^2 / \sigma_1^2}{s_2^2 / \sigma_2^2}$	$Y_1, Y_2 \sim N$ (2 grups independents)	$F \sim F_{n_1-1, n_2-1}$	$\left[ \frac{s_1^2 / s_2^2}{F_{(n_1-1, n_2-1), 1-\frac{\alpha}{2}}}, \frac{s_1^2 / s_2^2}{F_{(n_1-1, n_2-1), \frac{\alpha}{2}}} \right]$

\* se (standard error o error tipus)