PAR – In-Term Exam – Course 2021/22-Q1

November 8^{th} , 2021

Problem 1 (2 points)

We have a sequential code that we want to parallelize. Our code has four disjoint parts executed one after the other, namely *Start*, *Init*, *Compute* and *End*, which take 1, 10, 100 and 2 time units, respectively.

- 1. If we only parallelize the Compute phase, which would be the value for the parallel fraction ϕ ? Assuming that Compute can be perfectly parallelized, and there are no overheads resulting from its parallelization, which would be the value for the ideal speed—up $S_{p\to\infty}$?
- 2. Our system, however, has a parallelization overhead proportional to the number of processors being used. Which would be the value for the speed–up when using 10 processors (S_{10}) if the parallelization of *Compute* can be perfectly parallelized but incurs in an overhead of 0.001 time units per processor being used?

3. Next, we parallelize the *Init* phase on two processors. Regrettably, in this *Init* phase the parallelization cannot be scaled beyond two processors. Assuming again that there are no overheads due to the parallelization, which would be the new value for S_{10} in this case?

Problem 2 (2.5 points)

Assume a program composed of two parallel regions: $Region\ A$ and $Region\ B$; both regions scale ideally when executed with P processors. There is no code outside these two regions in the program. The first region, $Region\ A$, is basically a double nested loop reading matrix $Matrix_a$ and writing into matrix $Matrix_b$:

For this region the programmer has implemented a task decomposition in which each task computes N/P consecutive iterations of the row loop, with tasks computing blocks of rows assigned to processors in ascending order. Once the execution of $Region\ A$ is finished, the program proceeds with $Region\ B$, which is also a double nested loop reading matrix $Matrix_b$ and writing into matrix $Matrix_c$:

For this region the programmer has implemented a task decomposition in which each task computes N/P consecutive iterations of the col loop, again with tasks computing blocks of columns assigned to processors in ascending order. After the execution of $Region\ B$ the program terminates.

The three matrices have N rows and N columns, but are distributed in three different ways: Matrix_a is totally stored in the memory of processor 0; Matrix_b is distributed by rows among all P processors, so that each processor stores N/P consecutive rows in its memory (blocks of rows mapped to processors in ascending order); and Matrix_c is distributed by columns among all P processors, so that each processor stores N/P consecutive columns in its memory (blocks of columns mapped to processors in ascending order).

You can assume the data sharing model explained in class in which the overhead to perform a remote access is $t_s + t_w \times m$, being t_s the start-up time, t_w the time to transfer one element and m the number of elements to be transferred. At any time, each processor can simultaneously make one remote access to a different processor and serve one remote access from another processor. You can also assume that the execution of body of each innermost loop takes t_{body} .

We ask you to:

1.	Draw the	Task Dependence	Graph (TDG) for the progra	m described abov	e, indicating	the cost of ea	ch
	task.							

2. Identify which remote accesses have to be performed during the execution of the parallel program, clearly identifying the processors involved in each remote access, the number of elements that need to be transferred and when the remote accesses should occur.

3. Write the expression that determines the execution time with P processors, T_P , clearly identifying the contribution of the computation time and the overheads caused by data sharing.

Problem 3 (3 points) Assume a multiprocessor system with a hybrid NUMA/UMA architecture. The multiprocessor is composed of 2 identical NUMAnodes, each with 12 Gbytes of main memory. Each NUMAnode has 2 processors, each with its own private cache of 16 Mbytes. Memory and cache lines are 128 bytes wide. Data coherence is maintained using *Write-Invalidate MSI protocol* within each NUMAnode and using a *Write-Invalidate MSU Directory-based* cache coherency protocol among NUMAnodes. **First, we ask you to** answer the following two questions:

- 1. Compute the total number of bits that are necessary **in each cache memory** to maintain the coherence between caches **inside a NUMAnode**. Indicate also the function of those bits.
- 2. Compute the total number of bits that are necessary **in each NUMAnode's directory** to maintain the coherence **among NUMAnodes**. Indicate also the function of those bits.

Now, given the following declaration for vector x:

```
#define N 1024 int x[N];
```

and assuming that: 1) the initial memory address of vector x is aligned to the start of a memory/cache line; 2) the size of an int data type is 4 bytes; and 3) processors 0 and 1 belong to NUMAnode0 and processors 2 and 3 belong to NUMAnode1. We ask you to:

3. Complete the table in the provided answer sheet with the necessary missing information: type of memory access (read/write), affected cache line (numbered from the first position where vector x is allocated), access in cache (hit/miss), CPU command for processor k (PrRdk/PrWrk), Bus transaction(s) from Snoopy in processor k (BusRdk/BusRdXk/BusUpgrk/Flushk/Nothing), cache line states (I/S/M), NUMA commands (yes/no), directory entry state (U/S/M) and presence bits (0/1, where the lowest ordered bit, the rightmost one, corresponds to NUMAnode0), to keep cache coherence, AFTER the execution of each memory access. Note: We are not asking for the coherence commands exchanged between NUMAnodes, we are only asking the Bus transactions within NUMAnodes to keep coherence resulted from local or remote memory access to NUMAnodes.

Problem 4 (2.5 points) Given the following OpenMP code:

```
/* 256*1024 */
#define N
                  (1 << 18)
#define N_THREADS (1<<4)</pre>
                          /*
                                16 */
int b[N];
int a[N];
#pragma omp parallel num_threads(N_THREADS)
 int thid = omp_get_thread_num();
 int chunk = 2;
  for (int ii = thid * chunk; ii < N; ii+= chunk*N_THREADS) {
   for (int i = ii; i < ii+chunk; i++) {</pre>
          b[i] = a[i];
    }
 }
```

Assume an SMP system with 16 CPUs, each with its own cache memory initially empty. To keep caches coherent the system uses a Snoopy-based write-invalidate MSI coherence protocol. Also assume cache lines of 128 bytes, that int size is 4 bytes, first element of vectors a and b are placed at the first position of memory line and rest of variables are stored in registers. Finally, we know that thread i runs on CPU i.

Although the code above is correct, its execution generates a lot of bus coherence transactions due to false sharing and bad exploitation of spatial locality, and as a consequence, high execution overheads. We ask you:

- 1. Indicate which threads are accessing to the first 6 elements of vector a and b.
- 2. Assuming all processor caches are empty at the beginning of the code. Which types of coherence commands are generated by the snoopy controllers when the code is executed in parallel? Just indicate the name of the coherence transactions and which accesses to variables provoke them. Would it be possible to count the number of coherence transactions of each type? Reason your answer.

3. Briefly desc a lack of sp at once.	ribe the reason why atial locality exploit	the execution of the ation. Propose a m	code above leads to odification in the co	a a false sharing situation de that avoids both situa

Student name:	
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Answer sheet for **Question 3.3**.

Memory	Affected		CPU	Bus	Cache line state			ate	NUMA Dir		rectory entry	
access	line	$\mathrm{Hit}/\mathrm{Miss}$	command	transaction(s)	0	1	2	3	commands	State	Presence bits	
Processor 1 x[4]		Miss			I		I	I	No	М		
Processor 2 x[16]							S		ı.			
Processor 3 x[32]		Hit		$BusUpgr_3$	Ι	Ι	I		Yes	M		
Processor 0 x[32]					М							
Processor 2 writes x[20]									ı.			