

PAR – In-Term Exam – Course 2021/22-Q2

April 6th, 2022

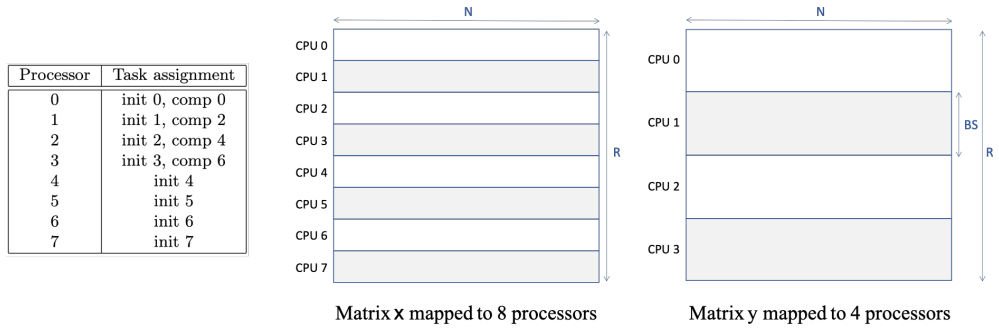
Problem 1 (4 points) Given the following code using *Tareador* for task annotations:

```
#define R 8
#define BS 2
int x[R][N], y[R][N];
...
// initialization phase
for (int i=0; i<R; i++) {
    tareador_start_task ("init");
    for (int k=0; k<N; k++)
        x[i][k] = foo (i); // no other memory accesses inside foo
    tareador_end_task ("init");
}
// computation phase
for (int i=0; i<R; i+=BS) {
    tareador_start_task ("comp");
    for (int ii=max(1,i); ii<min(R-1,i+BS); ii++)
        for (int k=0; k<N; k++)
            y[ii][k] = compute (x[ii][k], x[ii-1][k], x[ii+1][k]);
            // no other memory accesses inside compute
    tareador_end_task ("comp");
}
```

Assume that the execution time for functions `foo` and `compute` is 2 and 20 time units, respectively, and that the execution cost in time for the rest of the code is negligible. **We ask you to:**

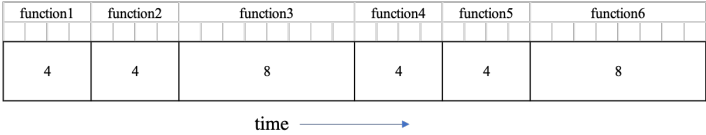
1. Draw the *Task Dependence Graph* (TDG) based on the above *Tareador* task definitions. Include for each task its name followed by the iteration number that generates it and its cost in time units (as a function of N).
2. Calculate the values for T_1 , T_∞ and amount of *Parallelism* (as a function of N).

3. Given the following task allocation for $P = 8$ processors (CPUs) and mapping of matrices x and y by rows to processors ($R = 8$ and $BS = 2$):



Write the expression that determines the execution time, T_8 as a function of N , clearly identifying the contribution of the computation time and the data sharing overheads, assuming the data sharing model explained in class in which the overhead to perform a remote memory access is $t_s + t_w \times m$, being t_s the start-up time, t_w the time to transfer one element and m the number of elements to be transferred; at any time, each processor can simultaneously make one remote access to a different processor and serve one remote access from another processor.

Problem 2 (2 points) The following figure shows the timing diagram for the sequential execution of an application on 1 processor:



The figure has a set of rectangles, each rectangle representing the serial execution of a function with its associated cost in time units. In a first attempt the programmer has been able to parallelize functions 1, 2, 3, 4 and 5, which can be ideally decomposed; **function 6 remains sequential. We ask you to answer the following questions:**

1. What is the parallel fraction ϕ ?
2. Which would be the maximum speedup that you could achieve based on Amdahl's law ($S_{p \rightarrow \infty}$)?
3. Draw the time diagram of an ideal parallel execution of the application to obtain maximum speed-up with 4 processors. Which is the value for S_4 that is achieved?

In a second attempt the programmer has been able to fully parallelize all funtions in the application (total workload of 32 time units), with ideal scalability. Please **answer the following two questions:**

4. Which should be the workload assigned to each processor when parallelized with $P = 8$ processors and strong scaling?
5. Which should be the workload assigned to each processor when parallelized with $P = 8$ processors and weak scaling?

Problem 3 (4 points) Given the following code excerpt, including OpenMP directives, to be executed on a UMA architecture with 8 processors, each one with a 1 MB fully-associative cache memory, and cache coherence maintained with the simplest write-invalidate MSI protocol explained in class, sharing the access to 16 GB of main memory:

```
#define NUM_THREADS 8
#define N 262144 // N multiple of NUM_THREADS

int a[N], b[N];
struct {
    int zeros[NUM_THREADS];
    int positives;
} count;

#pragma omp parallel num_threads(NUM_THREADS)
{
    int id = omp_get_thread_num();
    int num_elems = N / NUM_THREADS;
    for (int i=id*num_elems; i < (id+1)*num_elems; i++) {
        a[i] = a[i] * b[i];
        if (a[i] == 0) count.zeros[id]++;
        if (a[i]>0)
            #pragma omp atomic
            count.positives++;
    }
}
```

Observe that each implicit task executes a chunk of `num_elems` consecutive iterations of the loop. Assume that processor i executes implicit task with $id = i$. Also assume that each integer (`int`) variable occupies 4 bytes, a memory (cache) line occupies 32 bytes, and that the initial address of vectors `a` and `b` as well as structure `count` are aligned with the start of a cache line. All other variables are stored in registers (not in memory). Processors have no cached copies of `a`, `b` and `count` in their private cache memories before starting the execution of the parallel region. We ask you to **answer the following questions**:

1. How many *BusRd*, *BusRdX*, *BusUpgr* and *Flush* commands will be placed BY EACH ONE of the 8 processors on the shared interconnection network (bus) due to accesses to **vectors `a` and `b`**.
2. How many memory lines does **structure `count`** occupy? Does the access to `count` in the program causes *true* and/or *false* sharing? Briefly reason your answer.
3. In order to reduce the coherence traffic that is caused by the accesses to **vector `count.zeros`** the programmer has changed the definition of `count` and the access to it, as follows:

```

struct {
    int zeros[NUM_THREADS*PADDING];
    int positives;
} count;
...
    if (a[i] == 0) count.zeros[id*PADDING]++;
...

```

Which would be the most appropriate value for constant `PADDING`? How many *BusRd*, *BusRdX*, *BusUpgr* and *Flush* commands will be placed BY EACH ONE of the 8 processors on the shared interconnection network (bus) due to accesses to `count.zeros`?

If the multiprocessor architecture is upgraded to a NUMA system with 8 nodes, each node with a single processor, a private cache memory of 1 MB, and a portion of main memory of 2 GB, and all variables (vectors `a` and `b` and structure `count`) are physically mapped to NUMA node 0 by the operating system (first touch policy) before starting the execution of the parallel region, with no cached copies in any of the nodes. We ask you to **answer the following questions**:

4. How many entries in the directory of each NUMA node will be used to store the coherence information for **vectors `a` and `b`**? After the execution of the parallel region, how many bits in the *sharers list* of each of these directory entries will be set to 1 and in which state will those memory lines be?

5. After executing the program the programmer realized that the access to `count.positives` was creating a performance bottleneck, so she/he proposed the following program transformation for the parallel region, making use of a per-thread copy `tmppos` of the shared variable `count.positives`, which is accumulated into it before exiting the parallel region:

```

#pragma omp parallel num_threads(NUM_THREADS)
{
    int tmppos = 0;
    int id = omp_get_thread_num();
    int num_elems = N / NUM_THREADS;
    for (int i=id*num_elems; i < (id+1)*num_elems; i++) {
        a[i] = a[i] * b[i];
        if (a[i] == 0) count.zeros[id]++;
        if (a[i]>0) tmppos++;
    }
    #pragma omp atomic
    count.positives = count.positives + tmppos;
}

```

Assume that the processor in NUMA node 0 is the first executing `#pragma omp atomic` and that its execution ensures read/write atomicity in the access to `count.positives` (i.e. while one processor is accessing to it inside the `pragma` no other processors will be able to access it). Which of the following statements is/are true? (**selected wrong statements penalize the mark that you can obtain in this question**)

- (a) The proposed transformation can never improve performance since the number of positives found in vector `a` does not change.
- (b) If the number of positive results in vector `a` is much larger than 1, the ONLY improvement in performance comes from the fact that `#pragma omp atomic` has been removed from the loop body.
- (c) The last processor x executing `#pragma omp atomic` will first send a $RdReq_{x \rightarrow 0}$ command, which will provoke a $Fetch_{0 \rightarrow y}$ command to the remote node y that performed the previous update. As a consequence, $Dreply_{y \rightarrow 0}$ and $Dreply_{0 \rightarrow x}$ will be generated in order to get the updated line in processor x . The line is also updated in main memory of node 0.
- (d) After that, the same processor x will send an $UpgrReq_{x \rightarrow 0}$ to change the state of the line in the home node and an $Invalidate_{x \rightarrow y}$ command to invalidate the copy in cache of node y , which will reply with an $Ack_{y \rightarrow x}$ to notify the completion of the command.
- (e) At the end of the parallel region the directory entry associated to the memory line containing `count.positives` will be in state M with only the bit associated to node x in the sharers list active to 1.

Note: $Command_{a \rightarrow b}$ refers to a NUMA command sent from node a to node b .