# Union Find! (Disjoint Set)

William Fiset

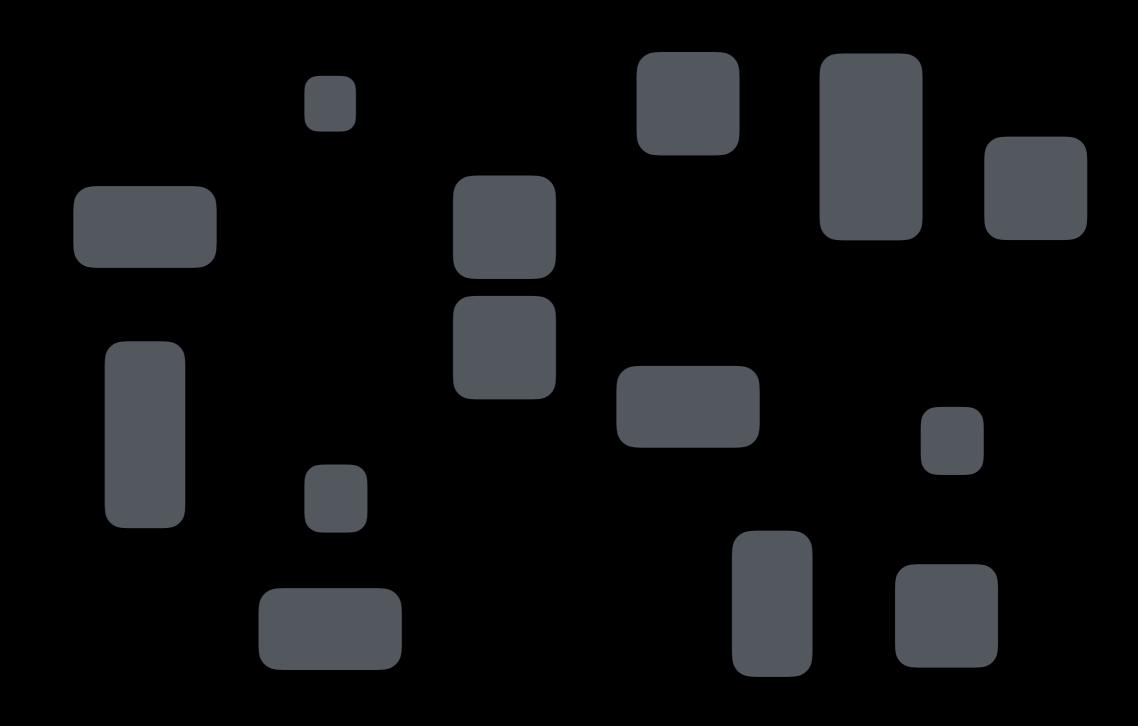
#### Outline

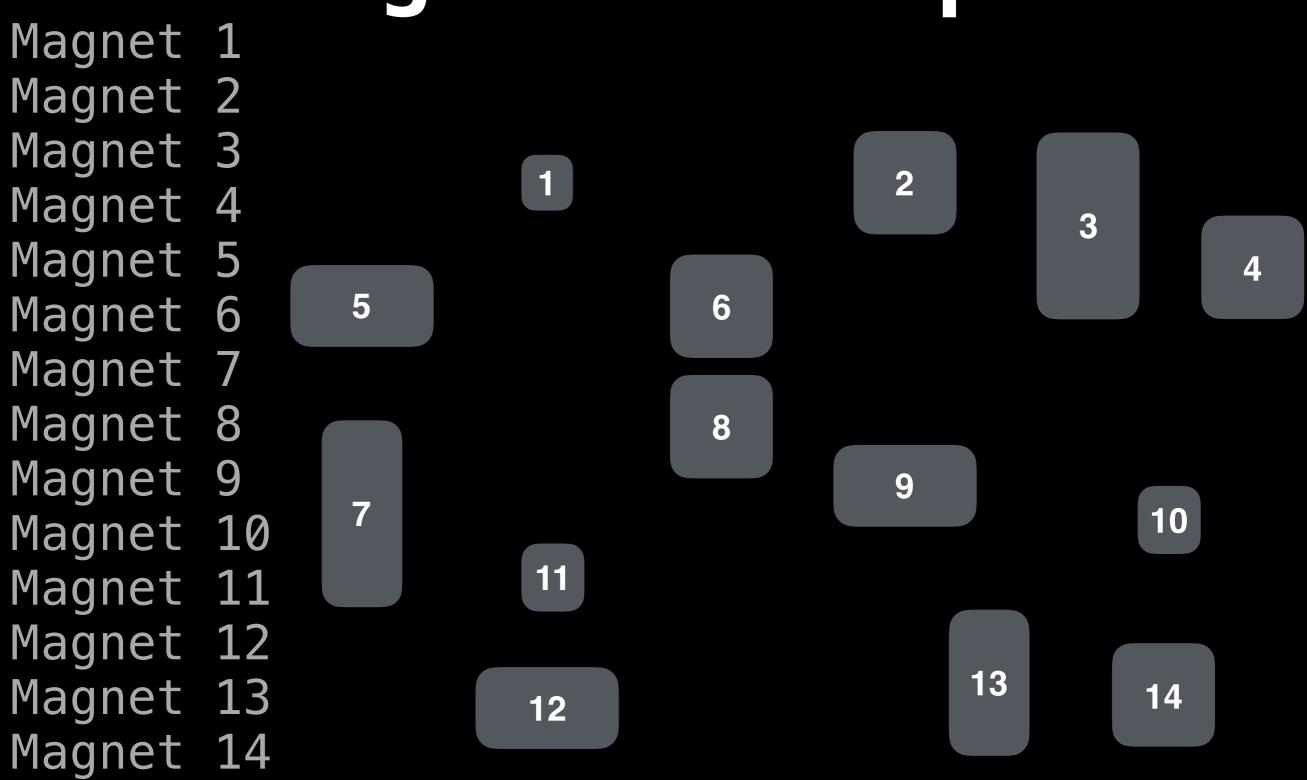
- Discussion & Examples
  - What is Union Find?
  - Magnets example
  - When and where is a Union Find used?
  - Kruskal's minimum spanning tree algorithm
  - Complexity analysis
- Implementation Details
  - Find & Union operations
  - Path compression
- Code Implementation

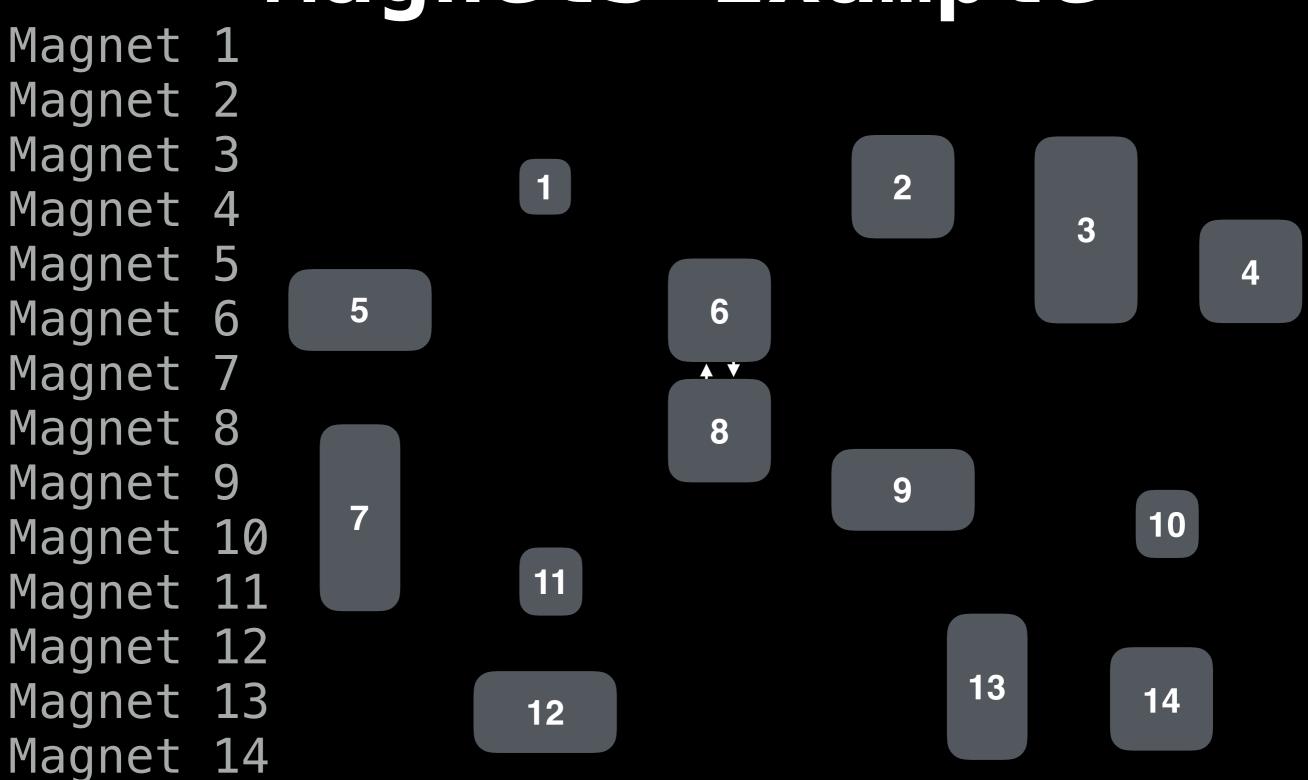
# Discussion and Examples

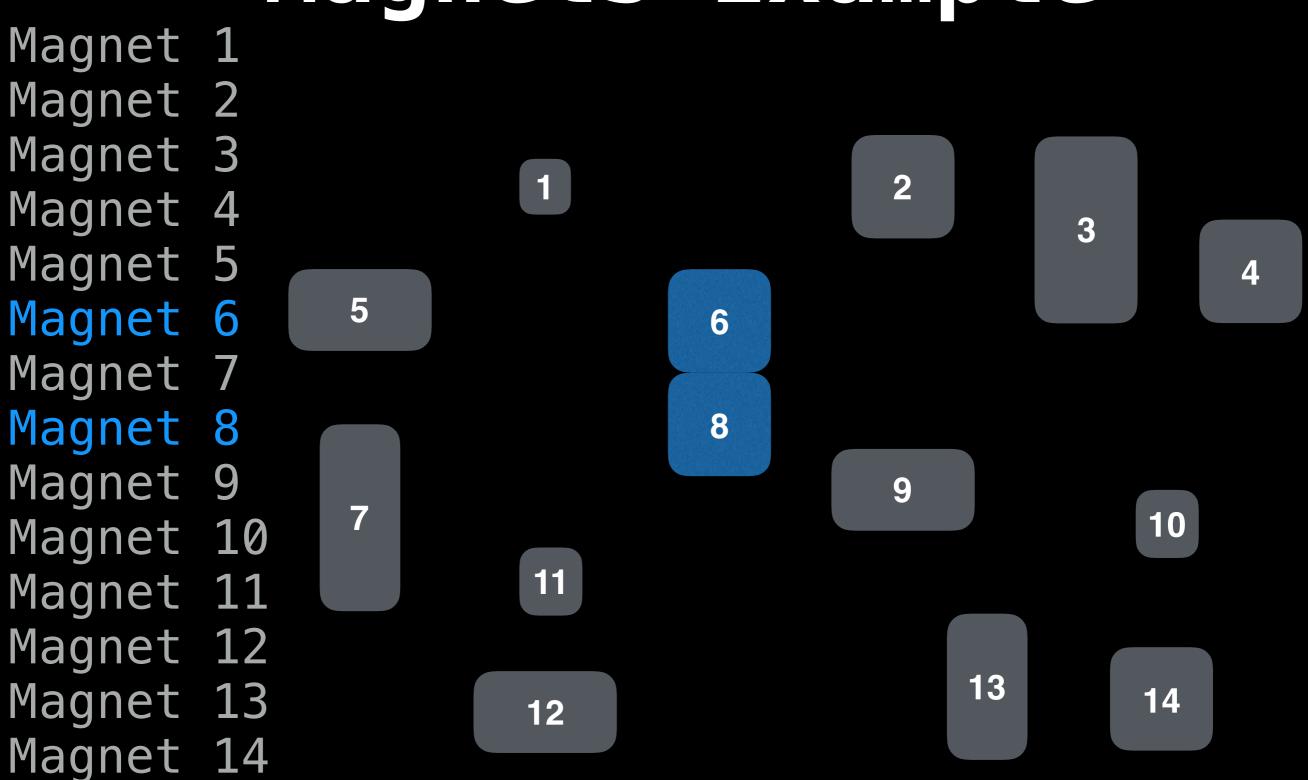
#### What is Union Find?

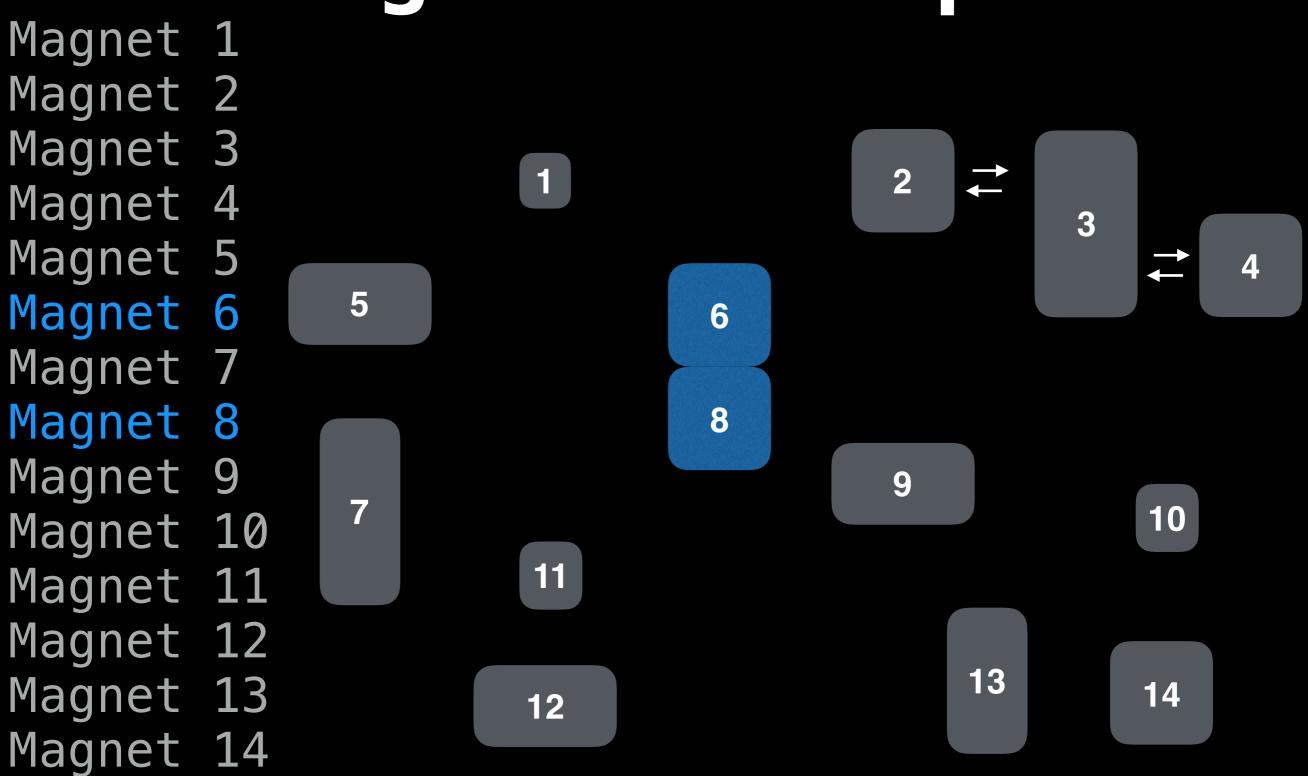
Union Find is a data structure that
 keeps track of elements which are
split into one or more disjoint sets.
 Its has two primary operations:
 find and union.

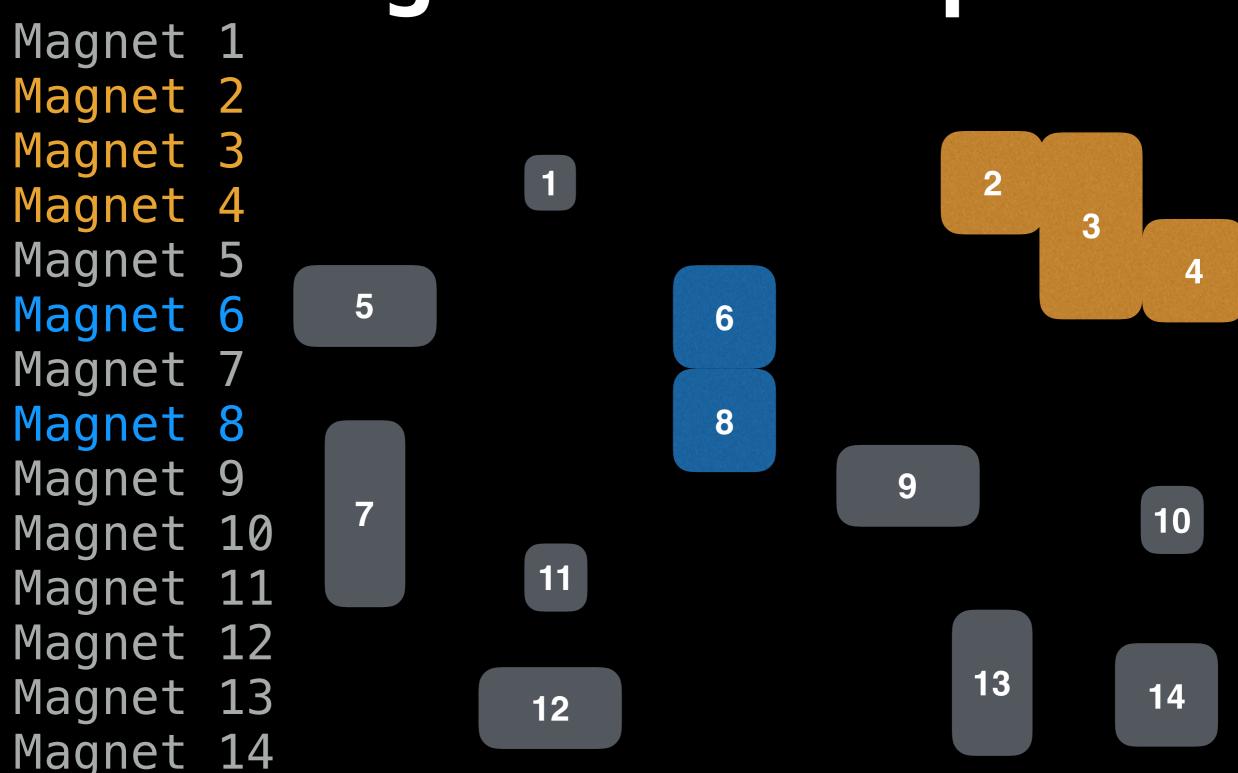


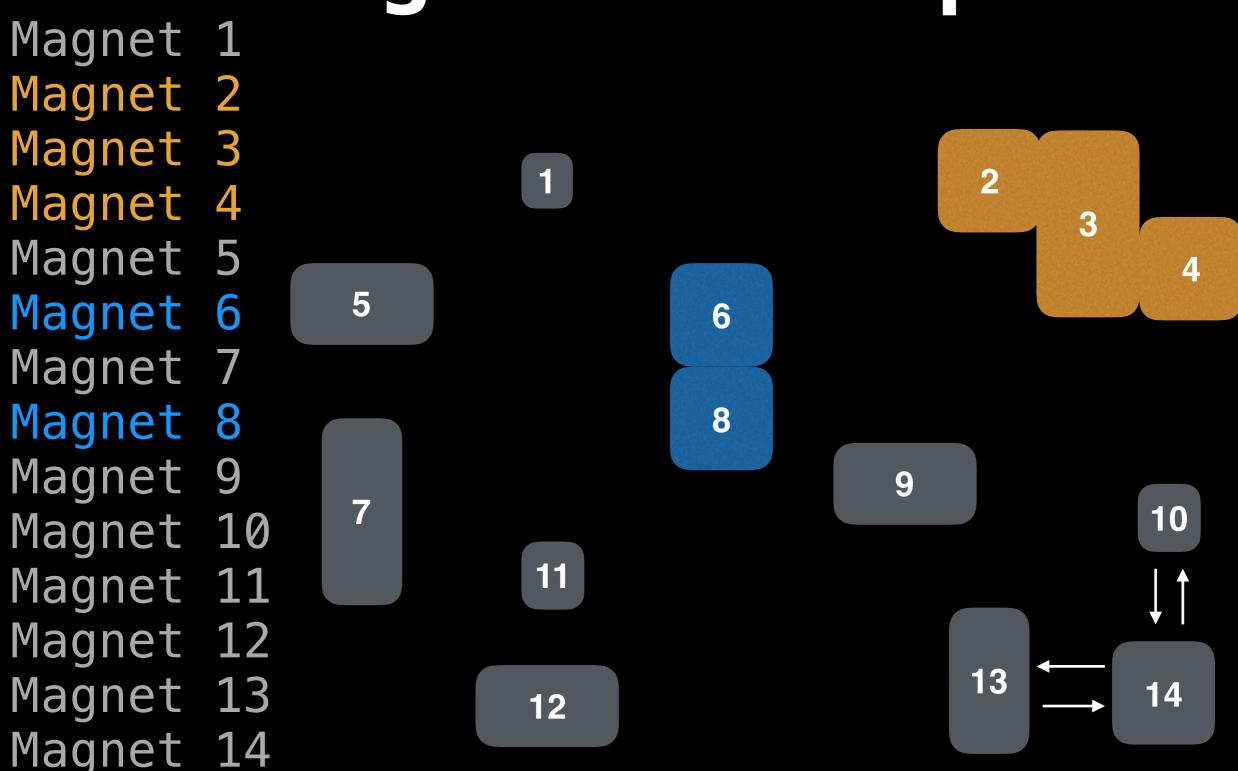


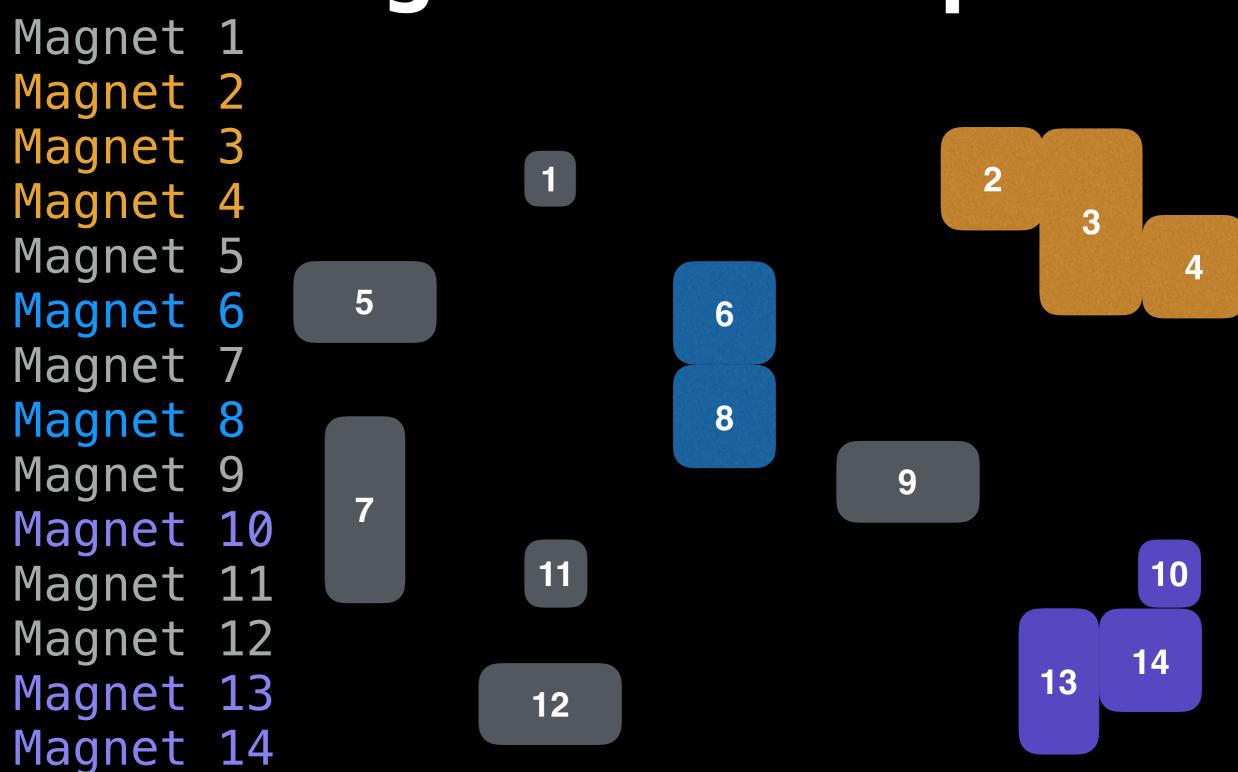


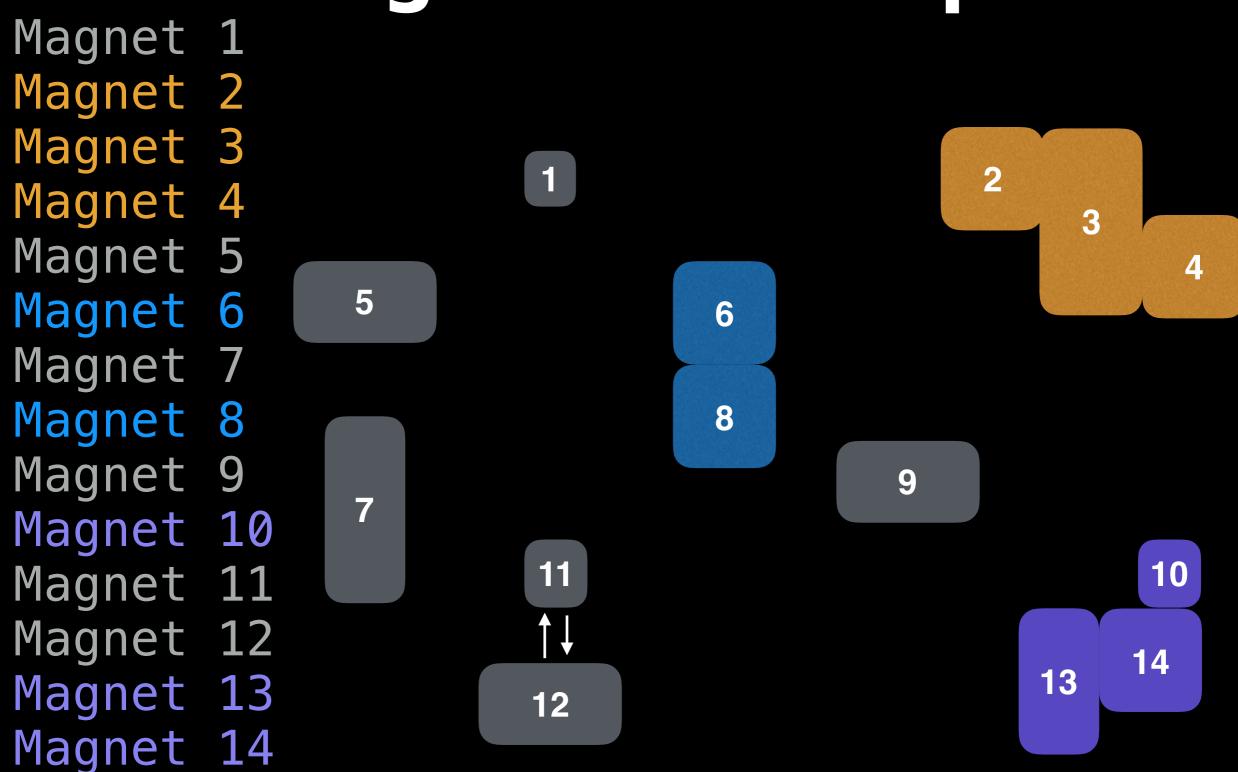


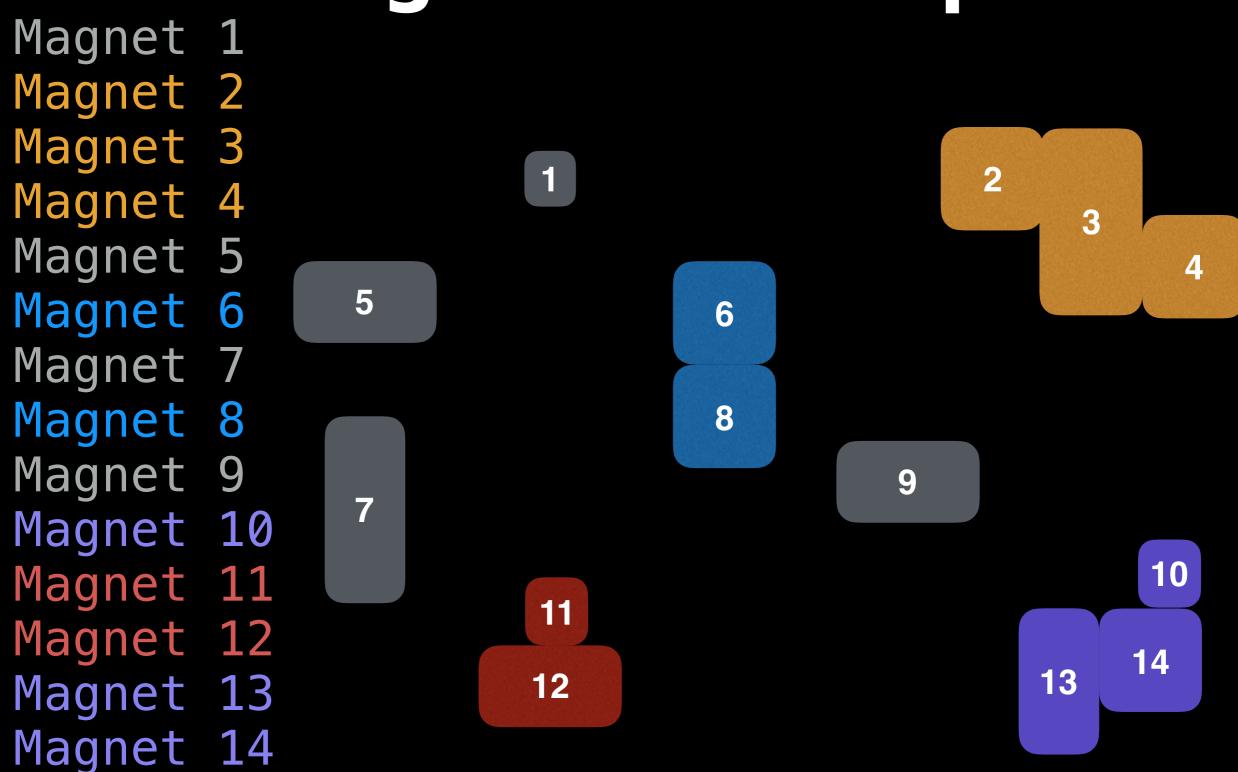


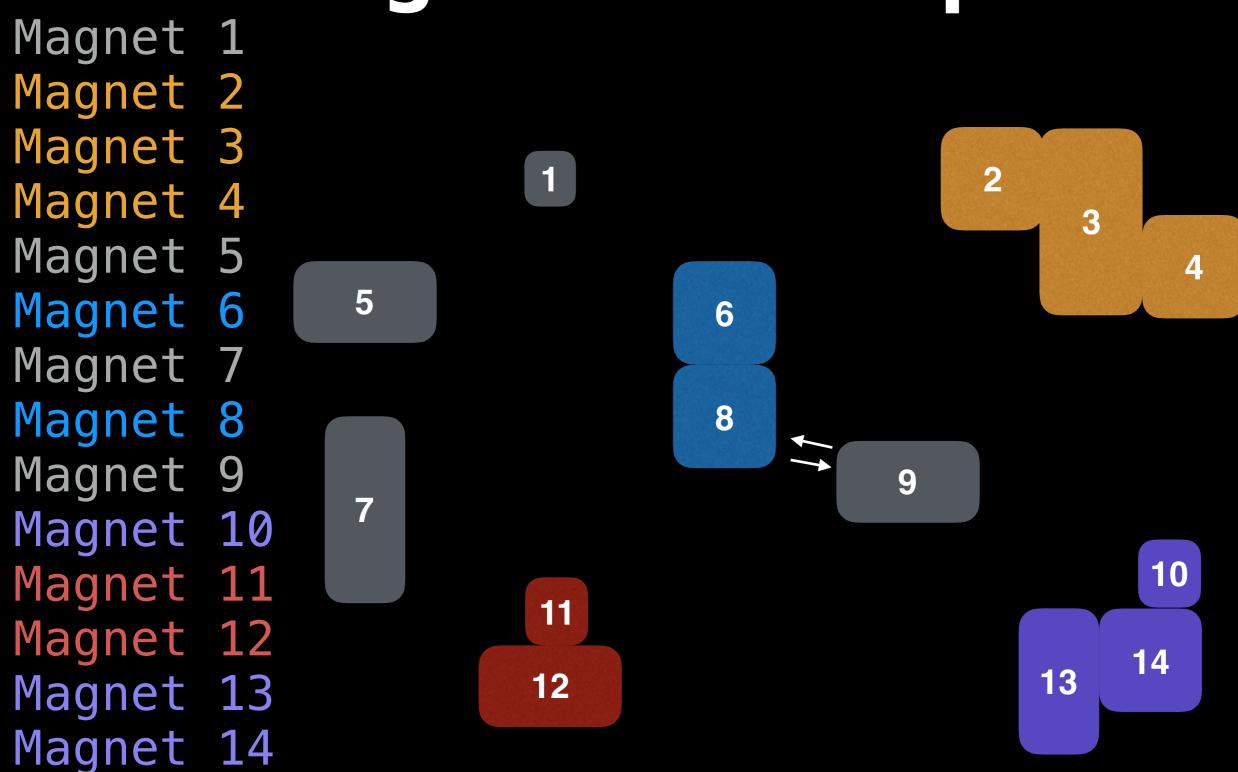


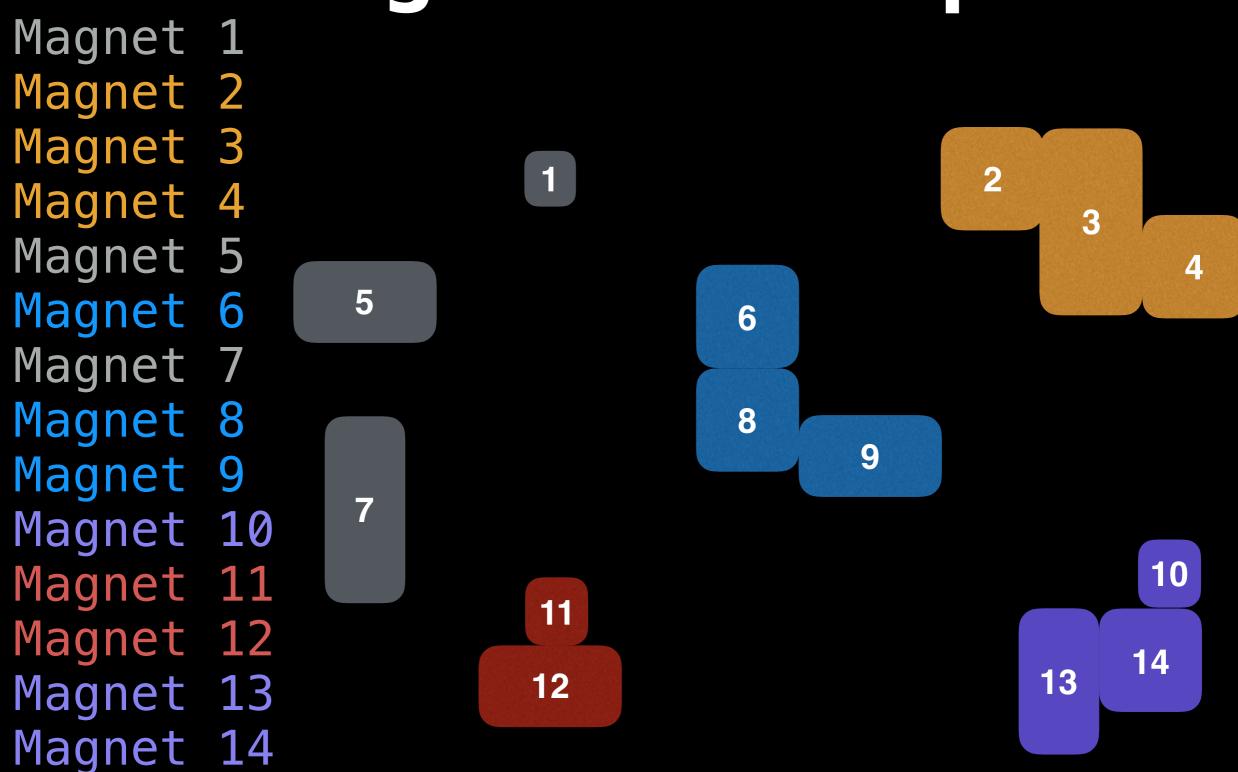


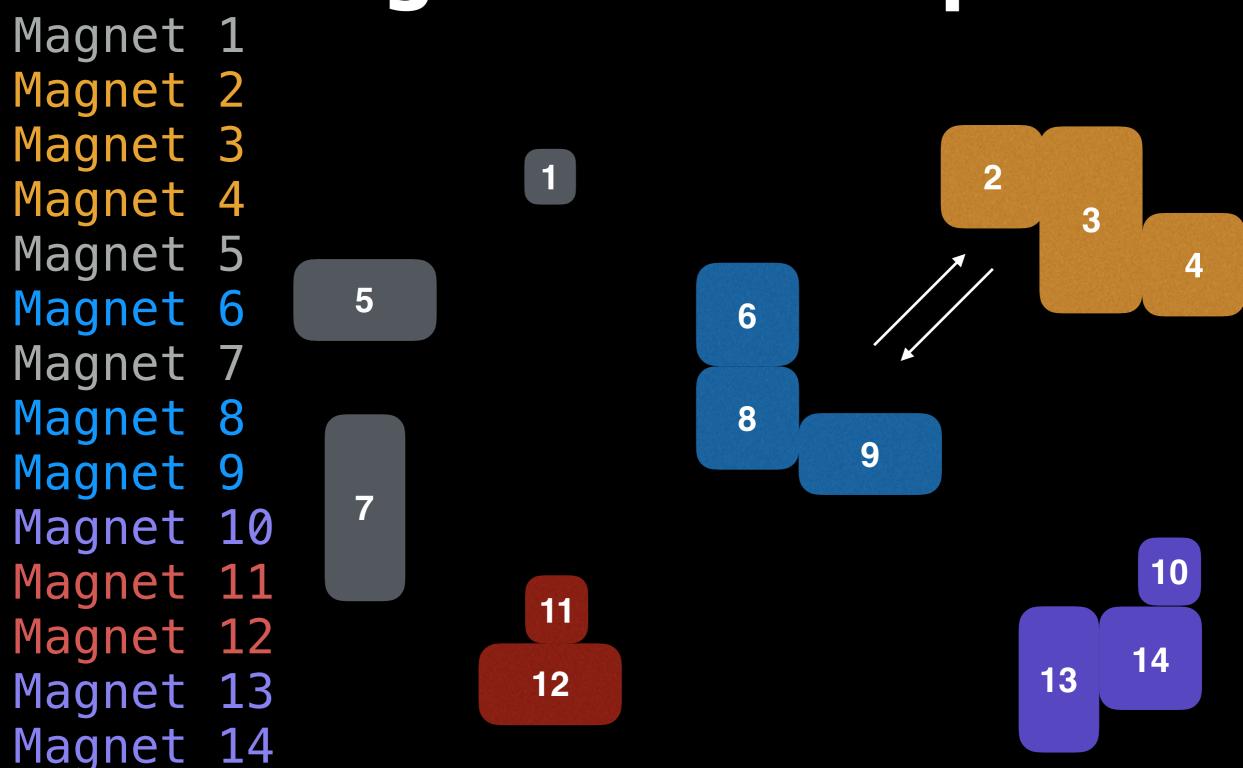


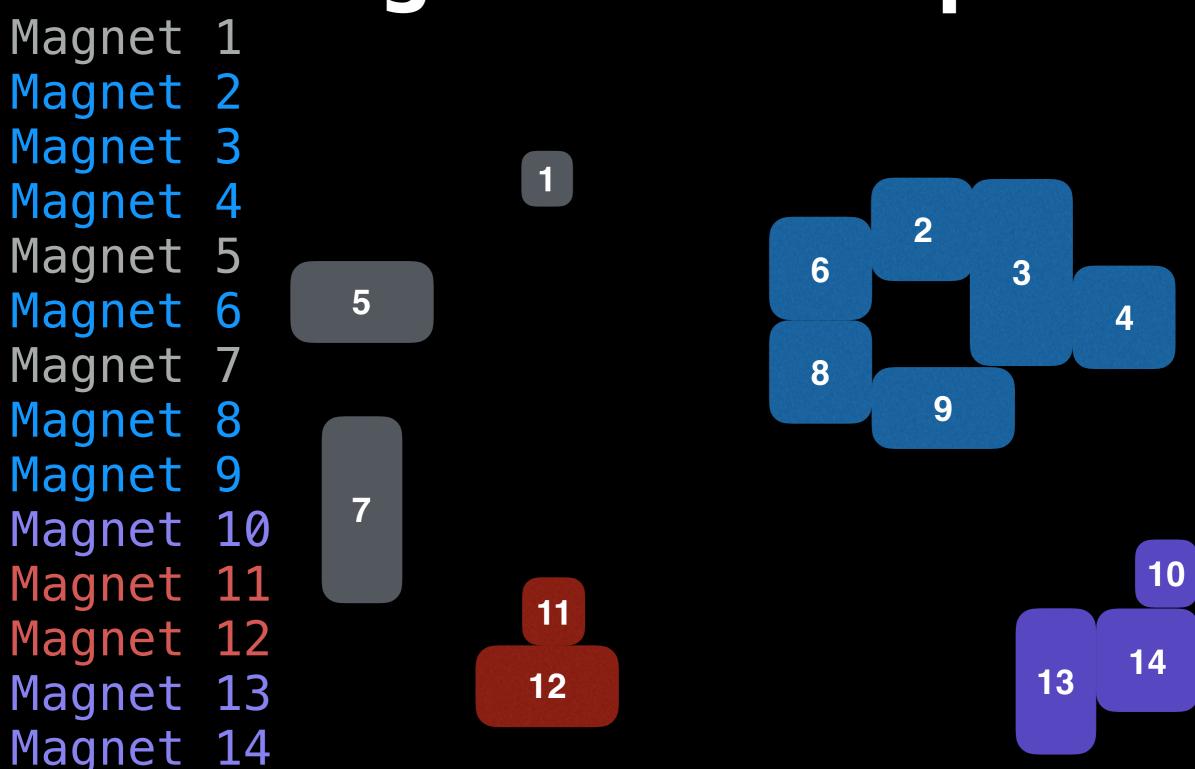


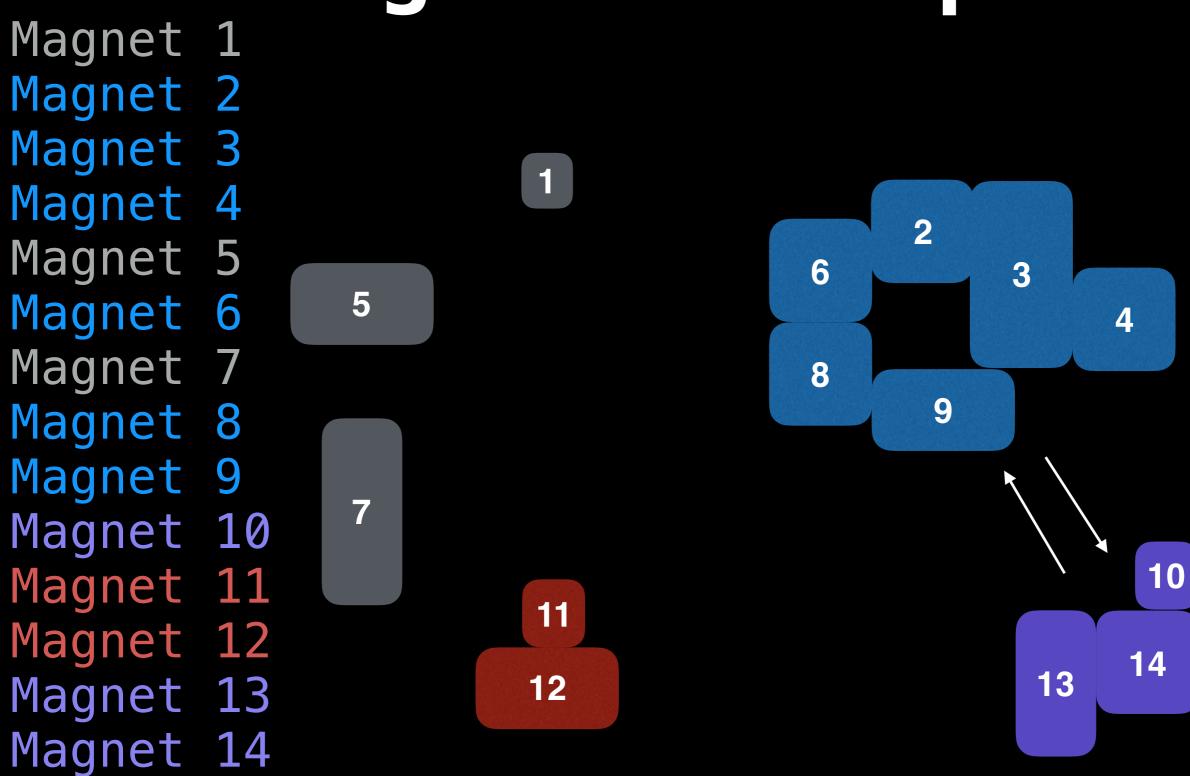


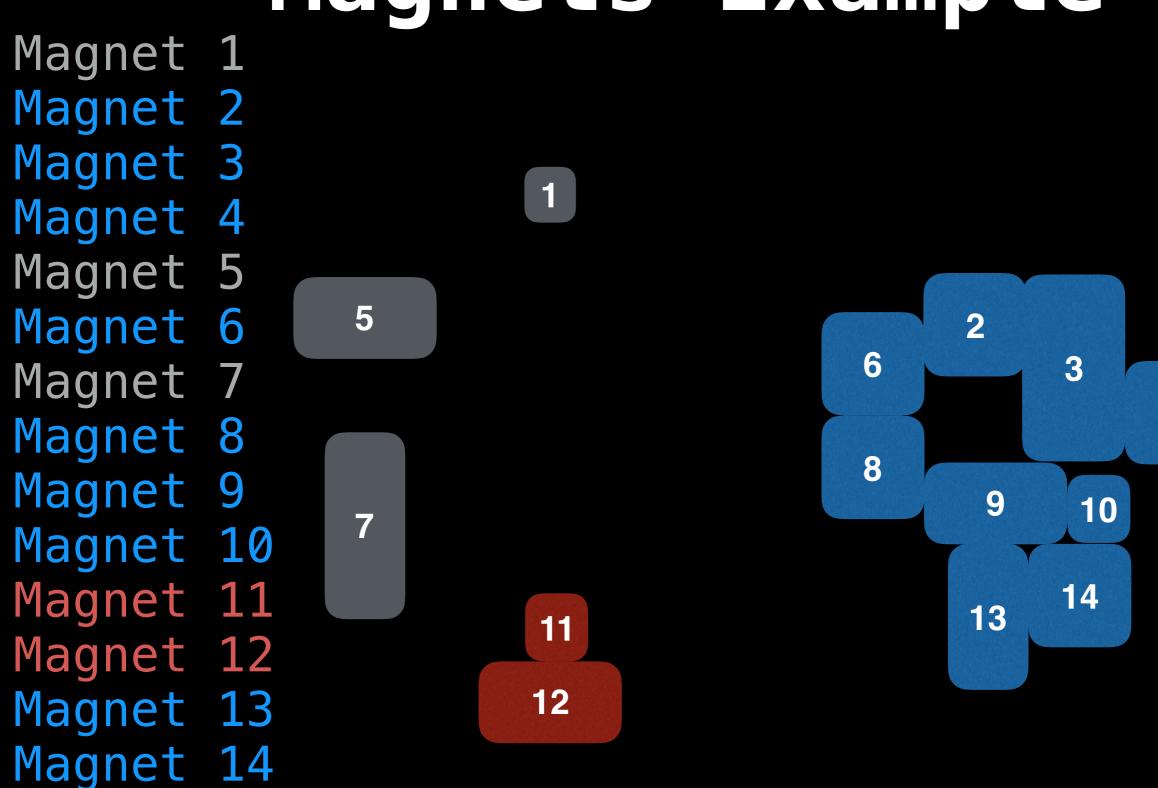








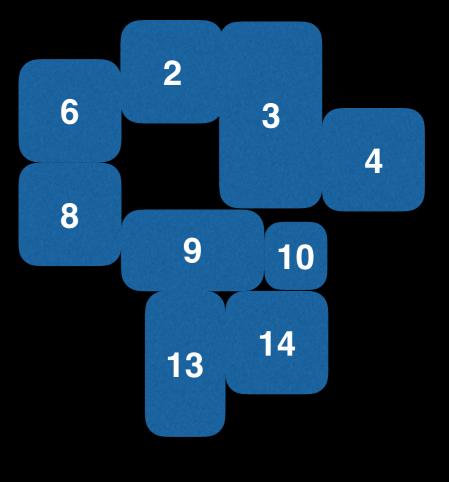


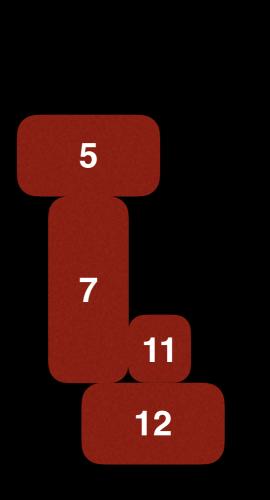


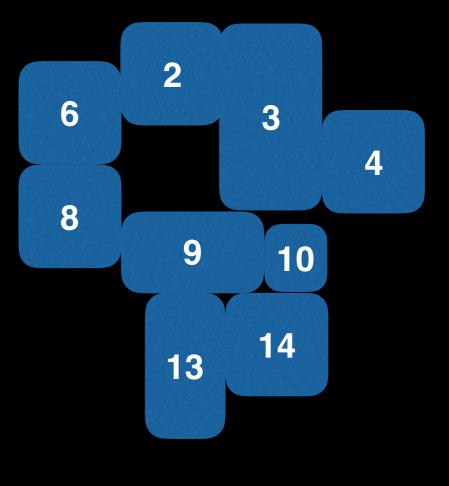
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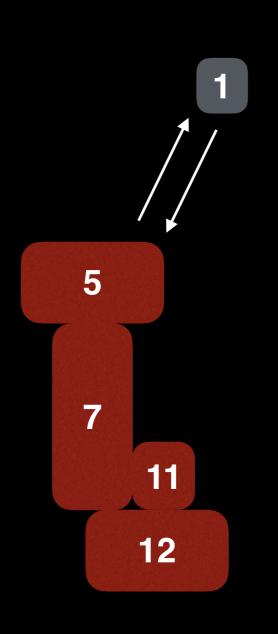
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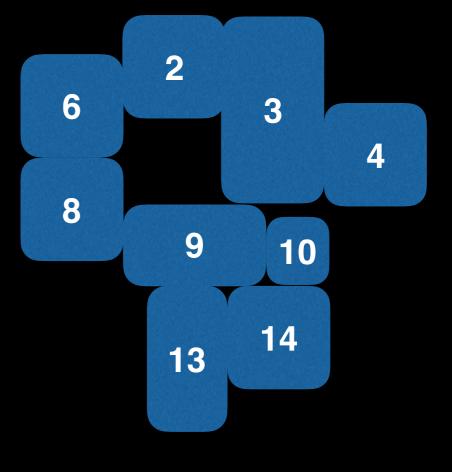


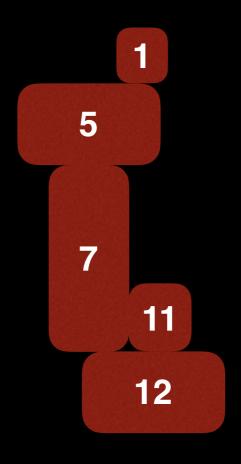


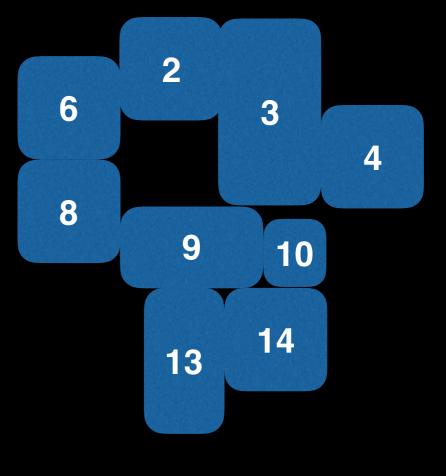


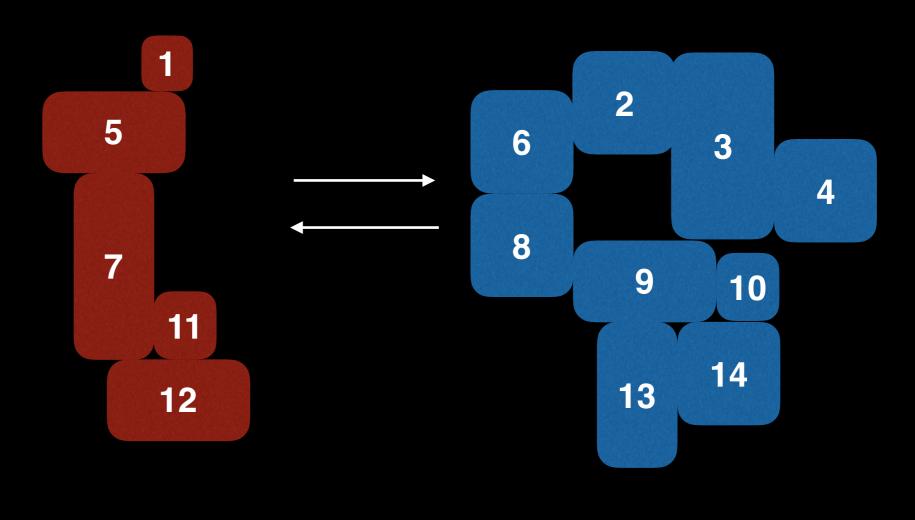




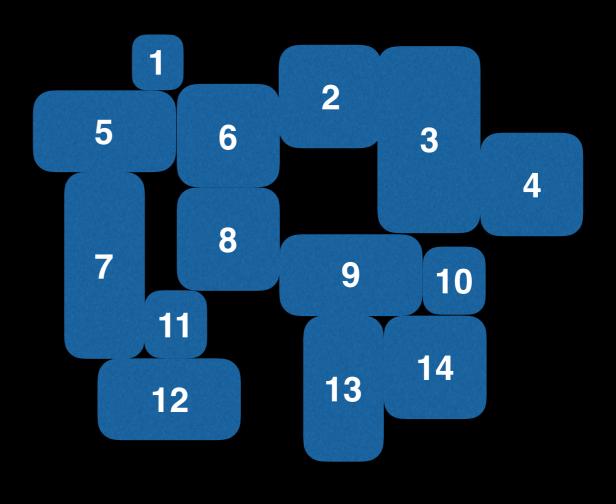








```
Magnet 1
Magnet 2
Magnet 3
Magnet 4
Magnet 5
Magnet 6
Magnet 7
Magnet 8
Magnet 9
Magnet 10
Magnet 11
Magnet 12
Magnet 13
Magnet 14
```



# When and where is a Union Find used?

Kruskal's minimum spanning tree algorithm

Grid percolation

Network connectivity

Least common ancestor in trees

Image processing

# Complexity

Construction	0(n)
Union	α(n)
Find	α(n)
Get component size	α(n)
Check if connected	α(n)
Count components	0(1)

α(n) - Amortized constant time

# Kruskal's Minimum Spanning Tree Algorithm in the next video

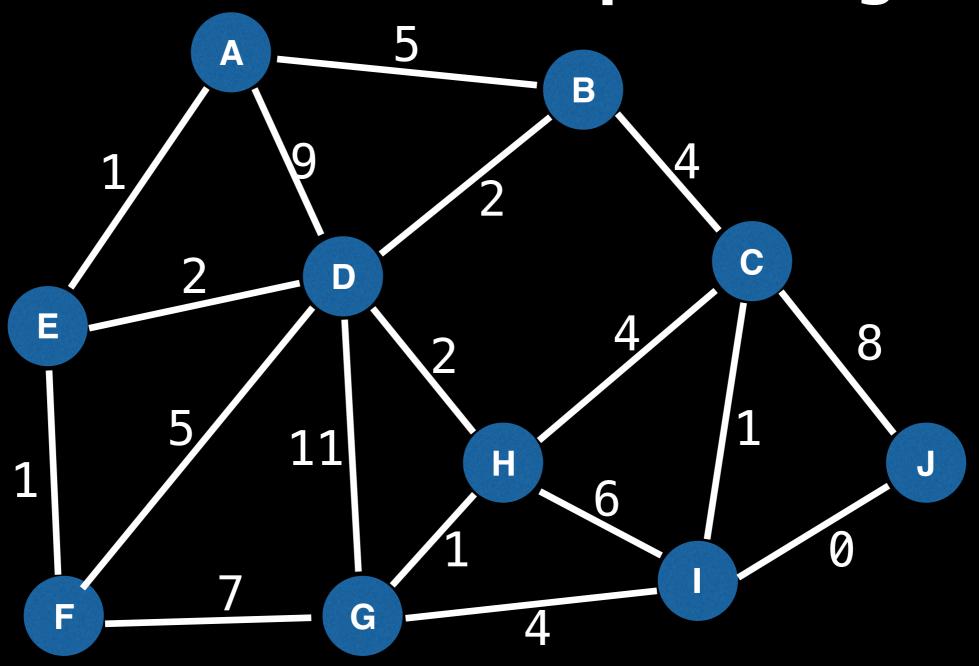
Implementation source code and tests
 can all be found at the following link:
 github.com/williamfiset/data-structures

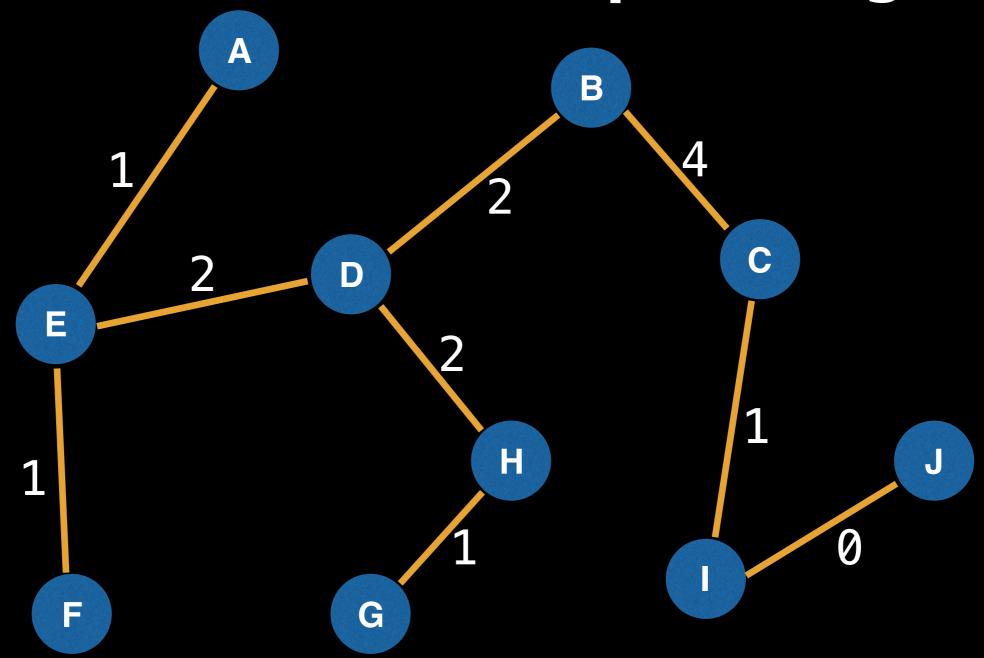
# Union Find

# Kruskal's Algorithm

William Fiset

Given a graph G = (V,E) we want to find a Minimum Spanning Tree in the graph (it may not be unique). A minimum spanning tree is a subset of the edges which connect all vertices in the graph with the minimal total edge cost.

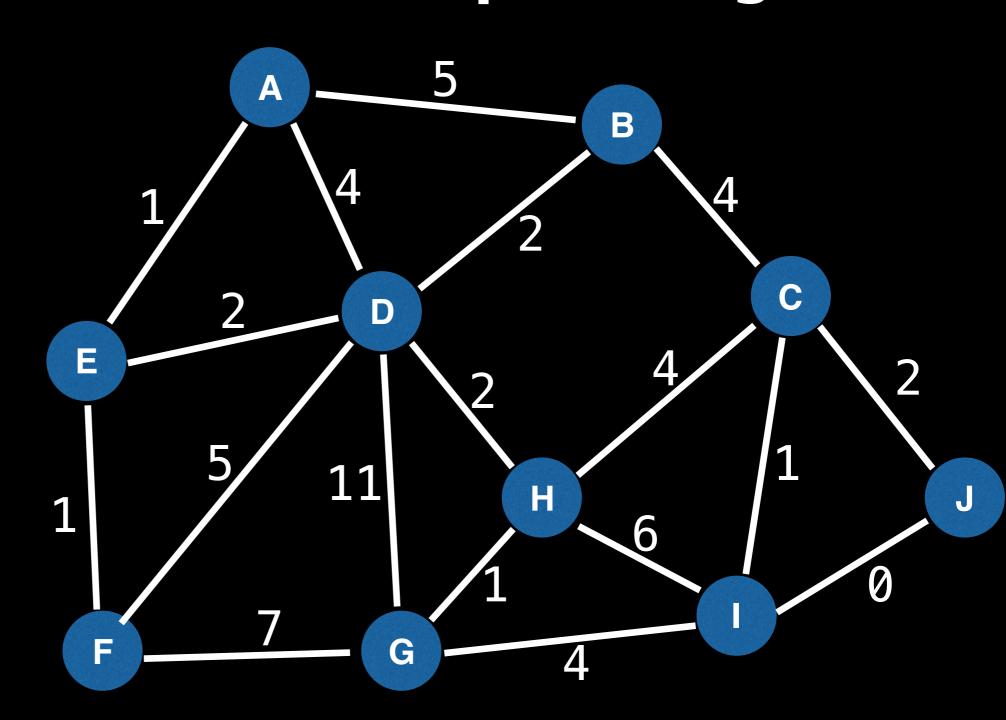




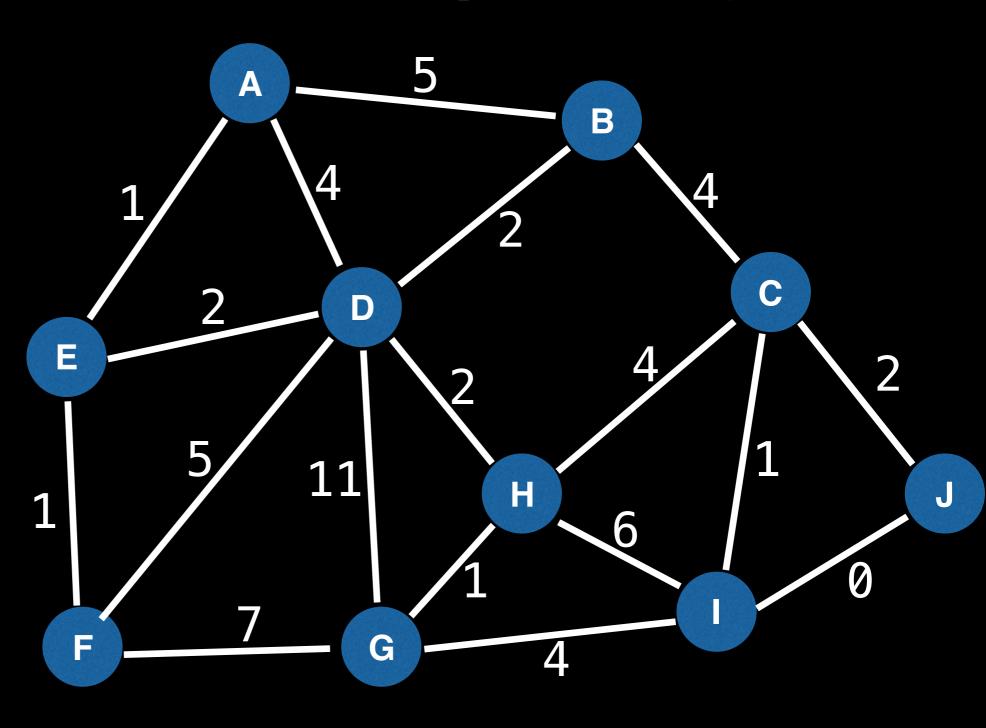
Minimum spanning tree with weight 14

1) Sort edges by ascending edge weight.

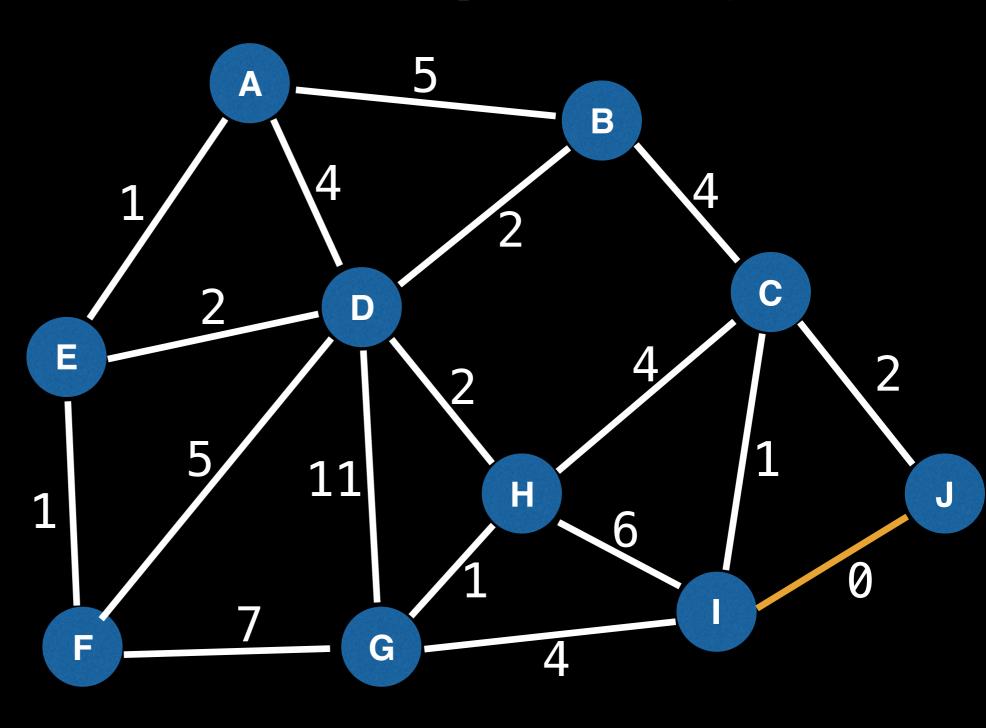
- 2) Walk through the sorted edges and look at the two nodes the edge belongs to, if the nodes are already unified we don't include this edge, otherwise we include it and unify the nodes.
  - 3) The algorithm terminates when every edge has been processed or all the vertices have been unified.



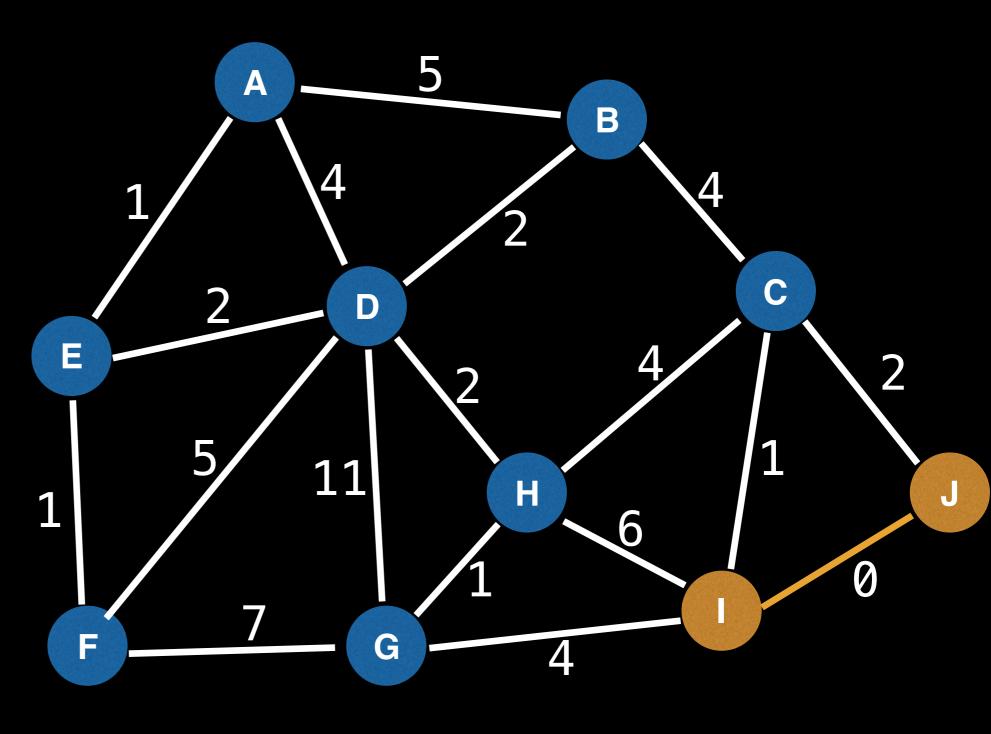
to J = 0A to E = 1to to F = 1G to H = 1to D = 2to J = 2to E = 2to H = 2to D = 4to C = 4to H = 4to I = 4to B = 5G =to G = 11to



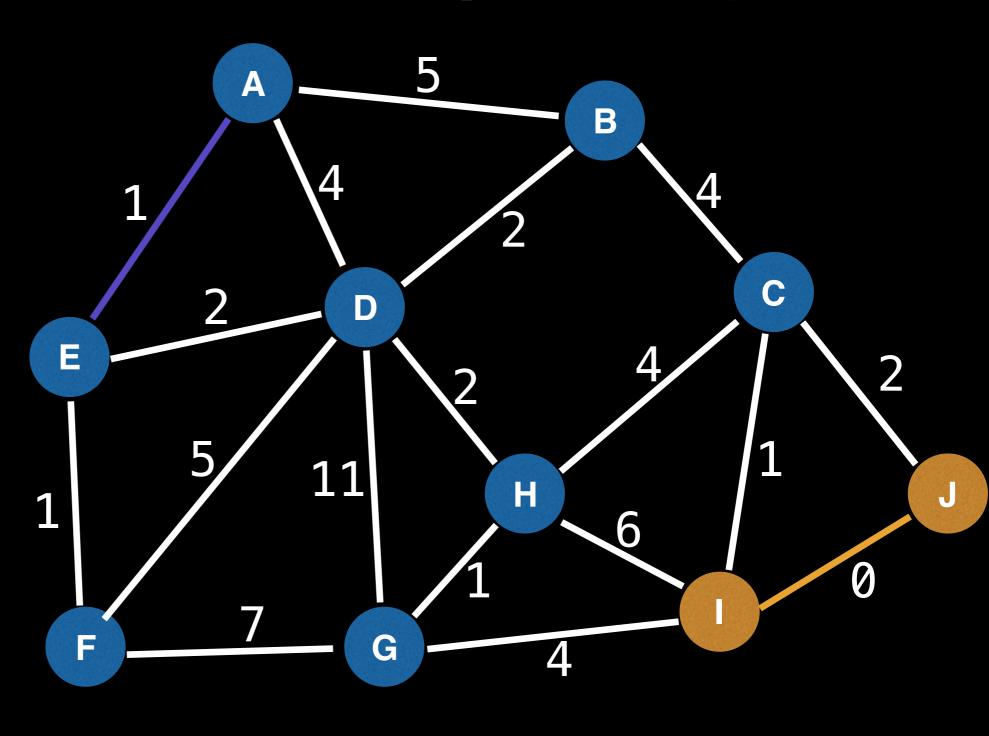
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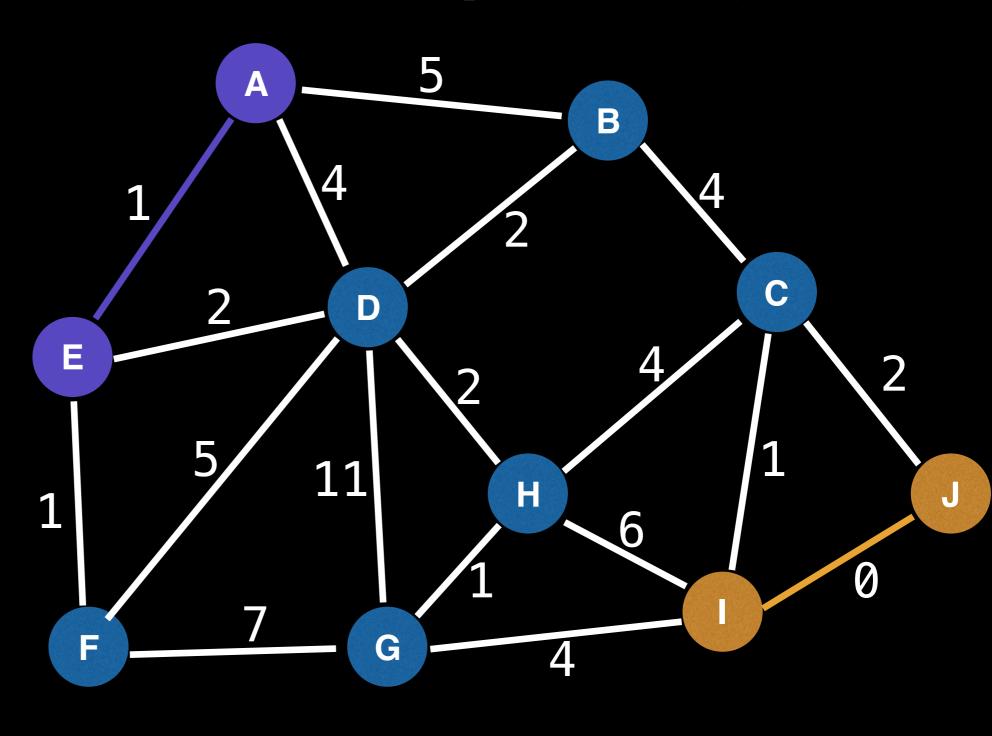
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  to
  to F = 1
G to H = 1
 to D = 2
  to J = 2
 to E = 2
  to H = 2
  to D = 4
 to C = 4
  to H = 4
  to I = 4
  to B = 5
     G =
  to
     G = 11
```



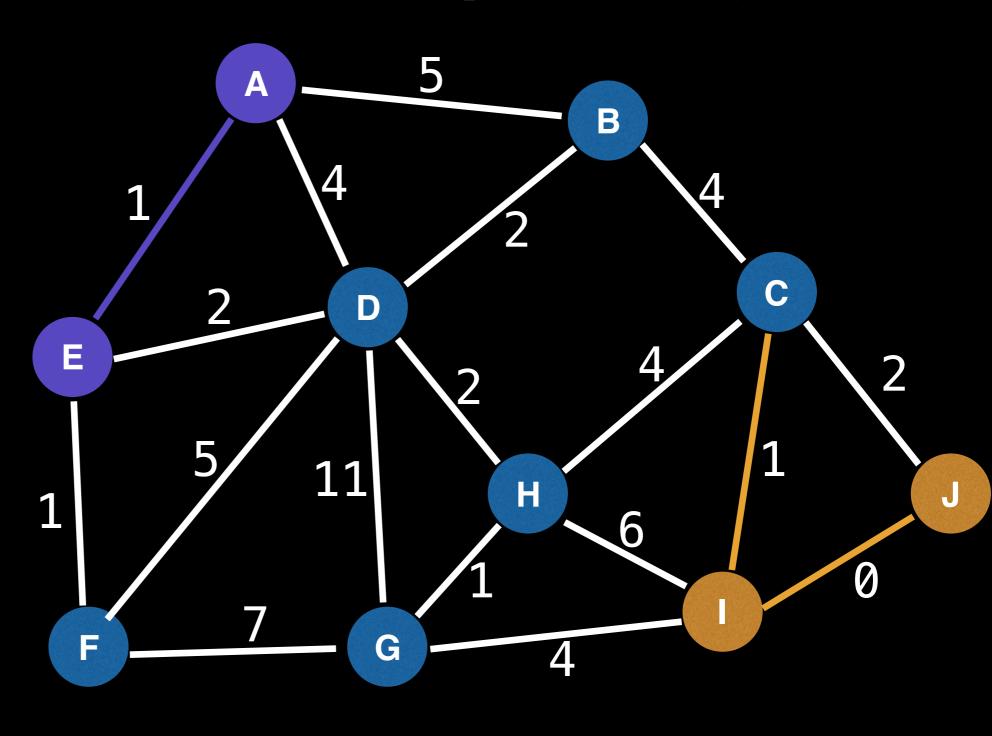
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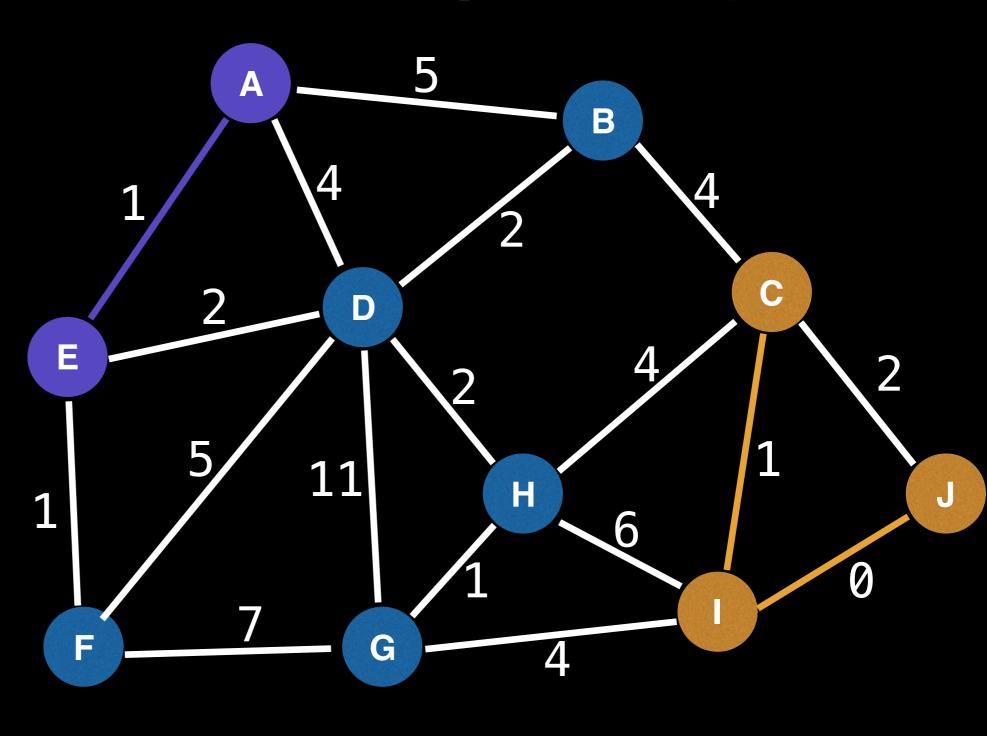
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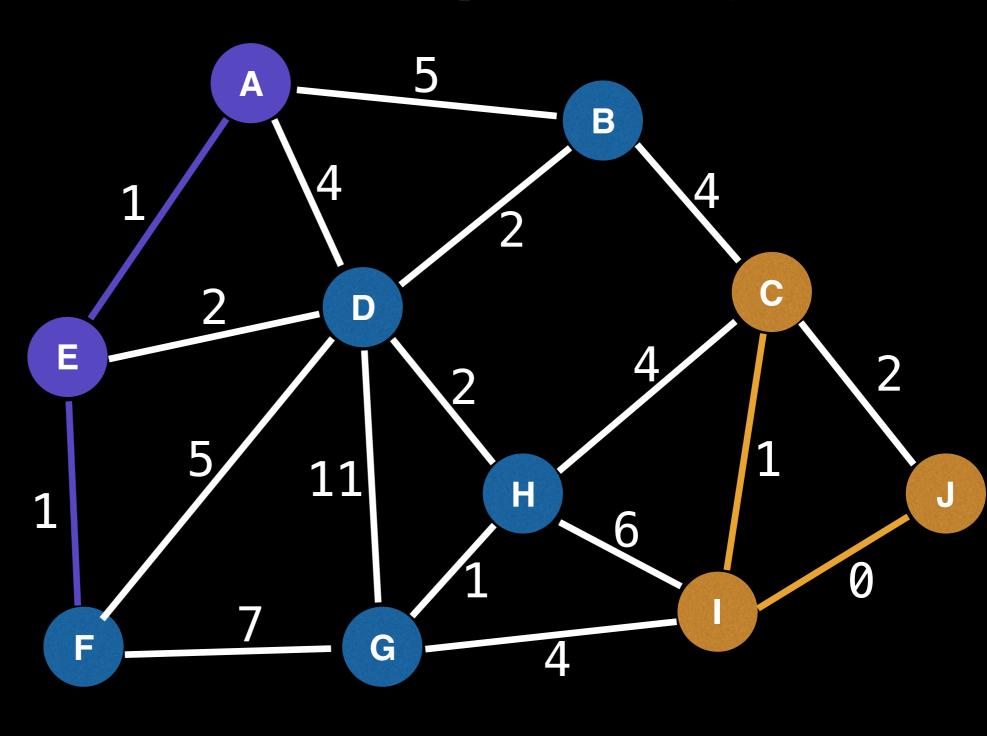
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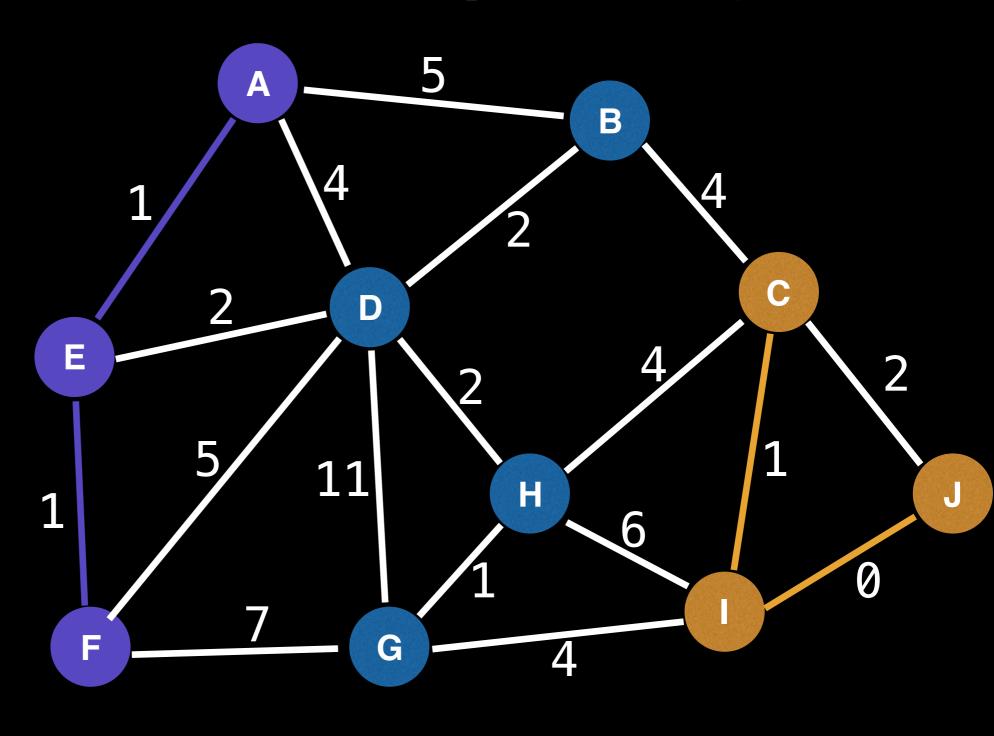
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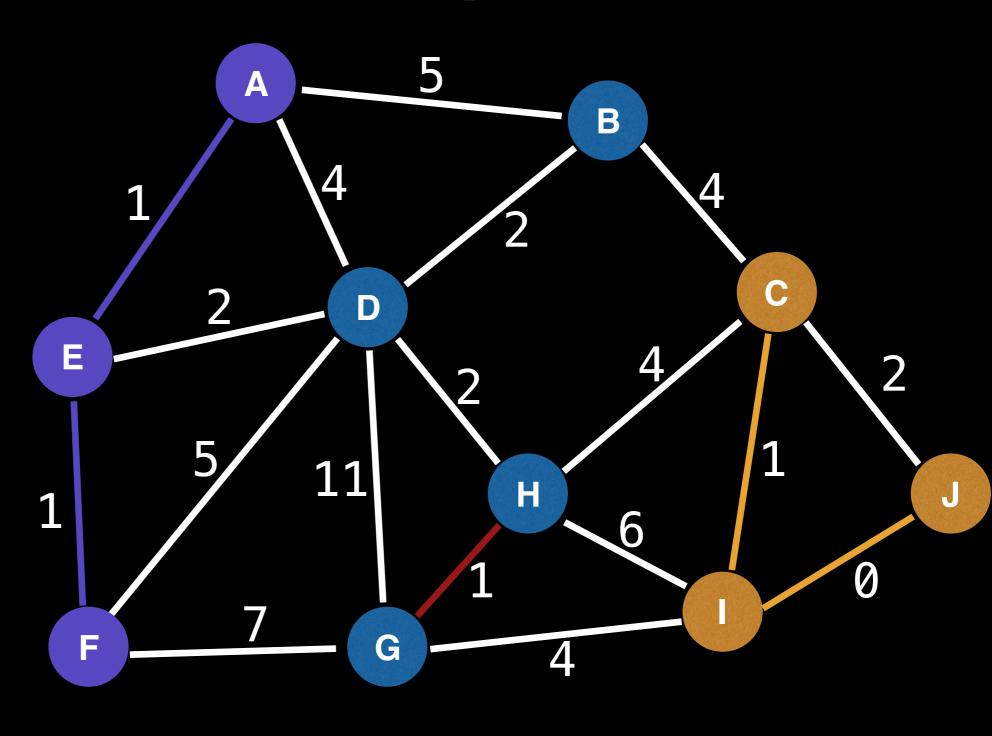
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```



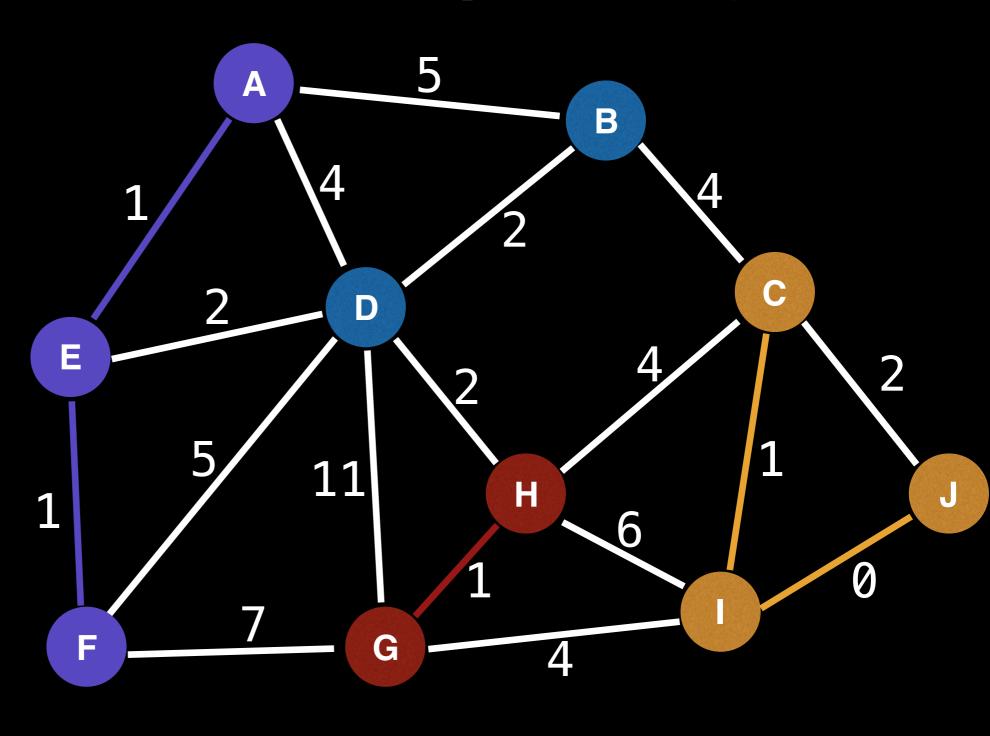
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```



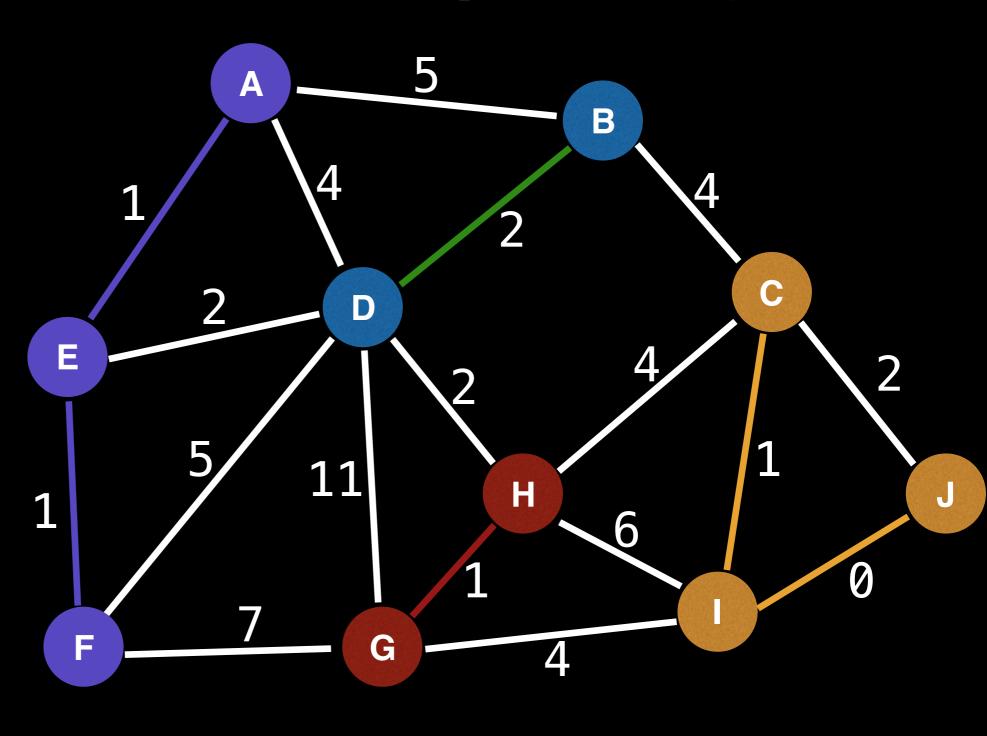
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  to F = 1
 to H = 1
  to D = 2
  to J = 2
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```



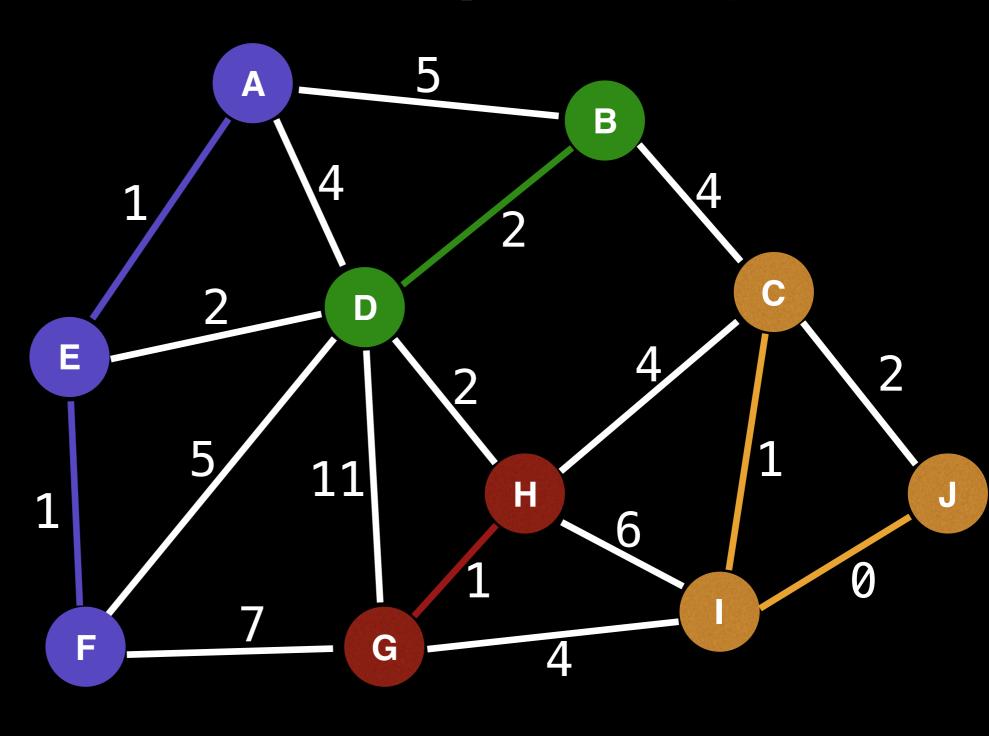
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```



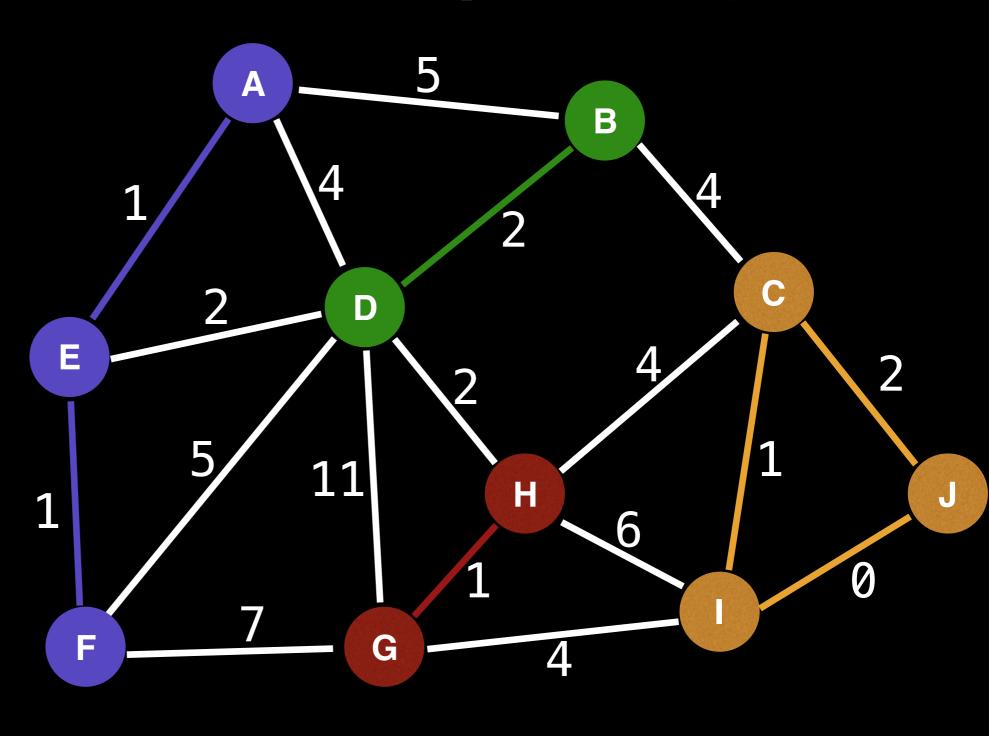
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G to H = 1
  to D = 2
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 to E = 2
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  to I = 4
  to B = 5
     G =
  to
     G = 11
```



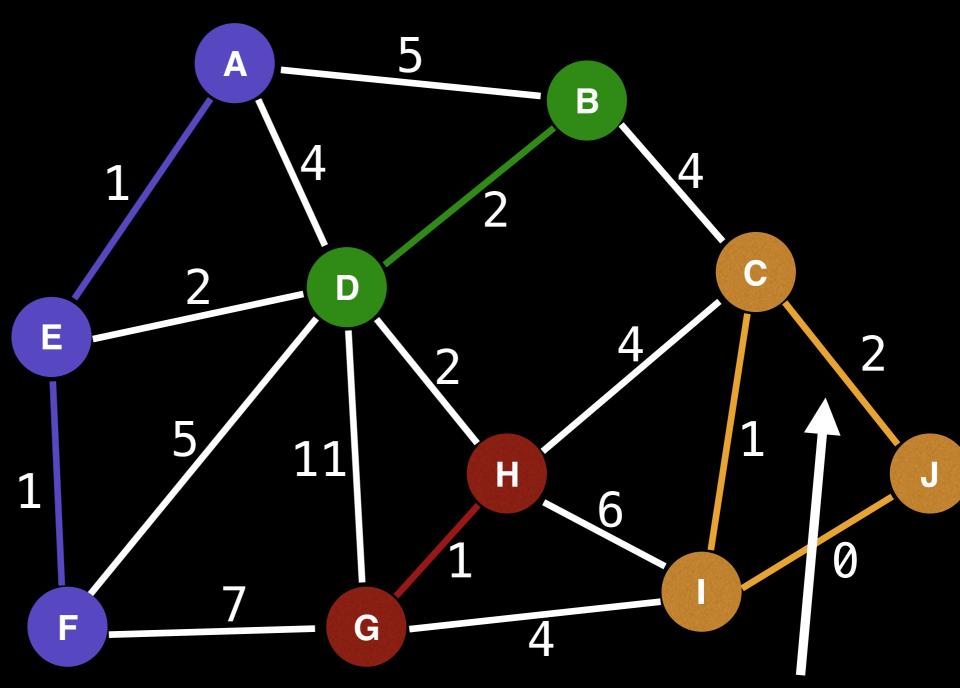
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G to H = 1
  to D = 2
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B to C = 4
  to H = 4
  to I = 4
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     G =
  to
     G = 11
```



```
to E = 1
  to
  to F = 1
G to H = 1
  to D = 2
  to J = 2
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  to H = 2
  to D = 4
B to C = 4
  to H = 4
  to I = 4
  to B = 5
     G =
  to
     G = 11
```

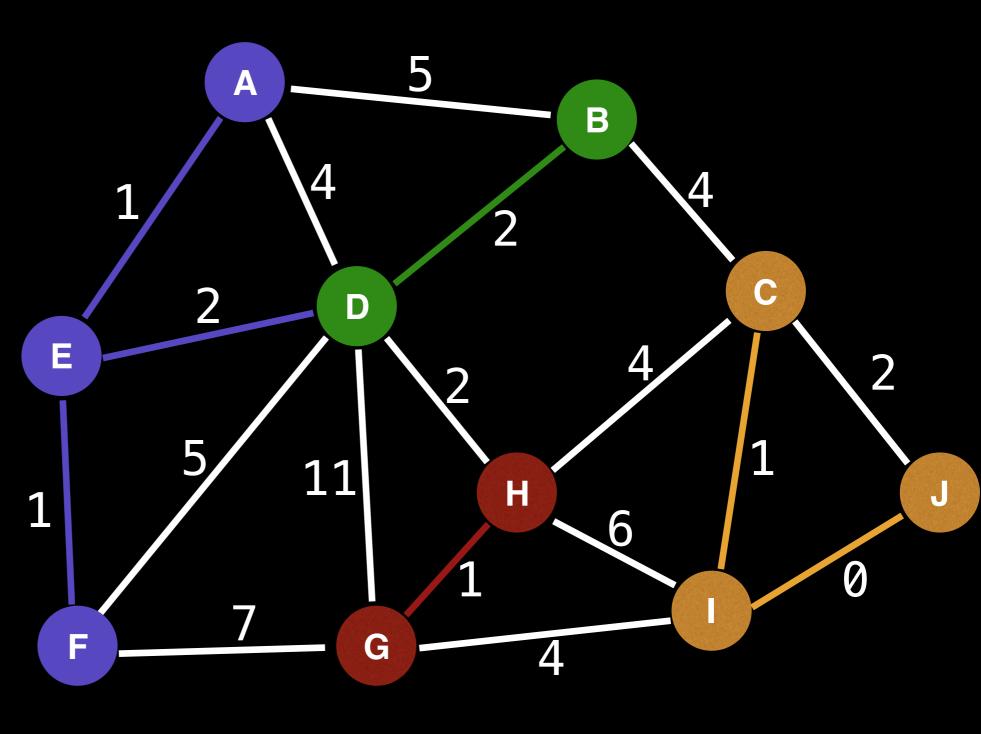


```
A to E = 1
  to I = 1
E to F = 1
G to H = 1
 to D = 2
  to J = 2
 to E = 2
 to H = 2
  to D = 4
B to C = 4
C \text{ to } H = 4
  to I = 4
 to B = 5
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  to
     G = 7
  to
     G = 11
  to
```

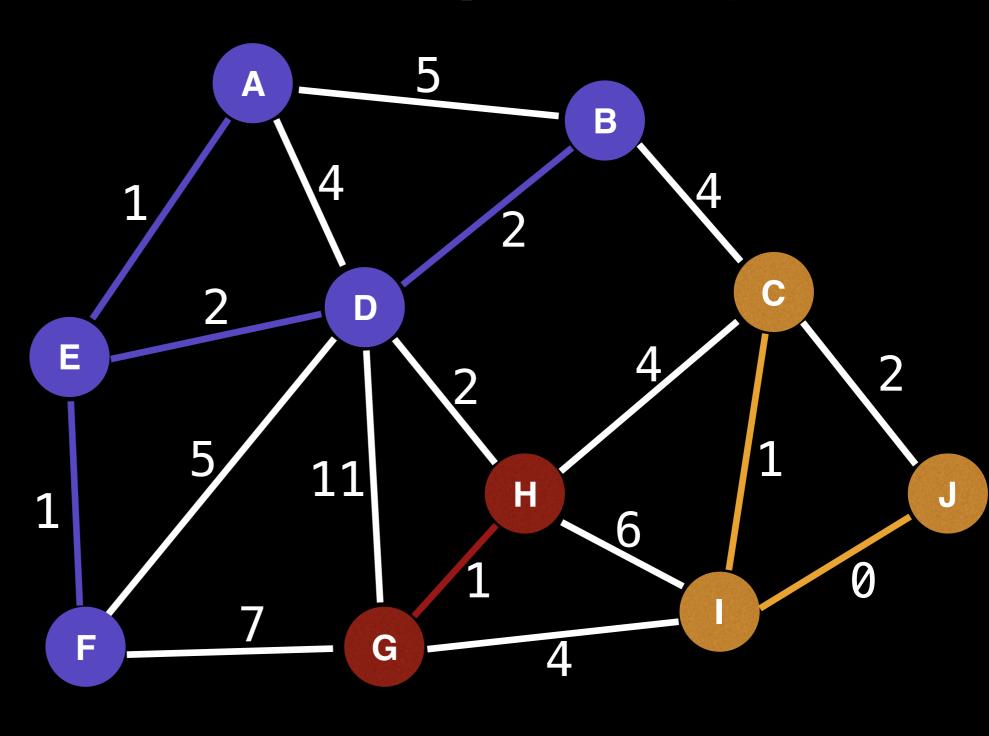


Nodes C,J are already connected in yellow group. This creates a cycle

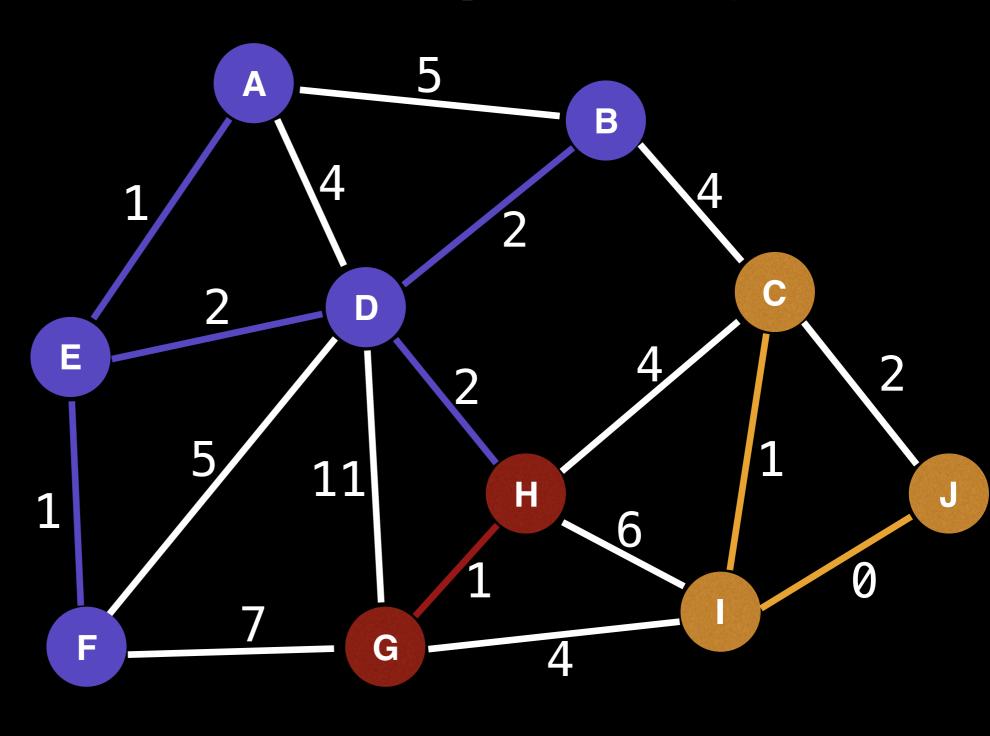
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  to I = 4
  to B = 5
     G =
  to
     G = 11
```



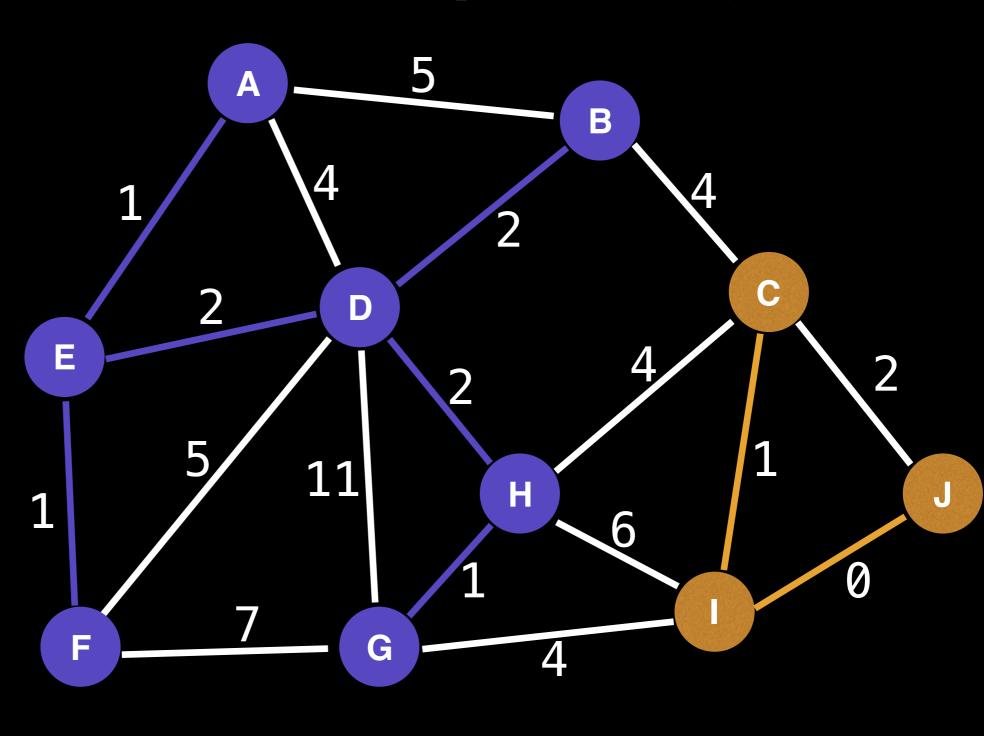
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  to
```



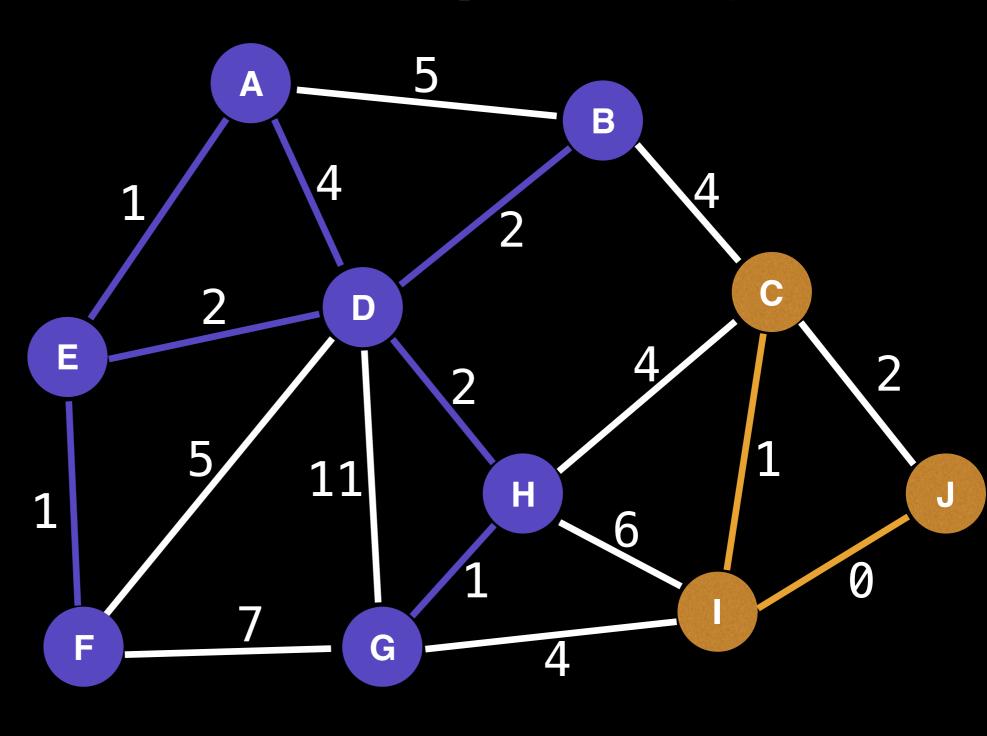
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     G =
  to
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  to
```



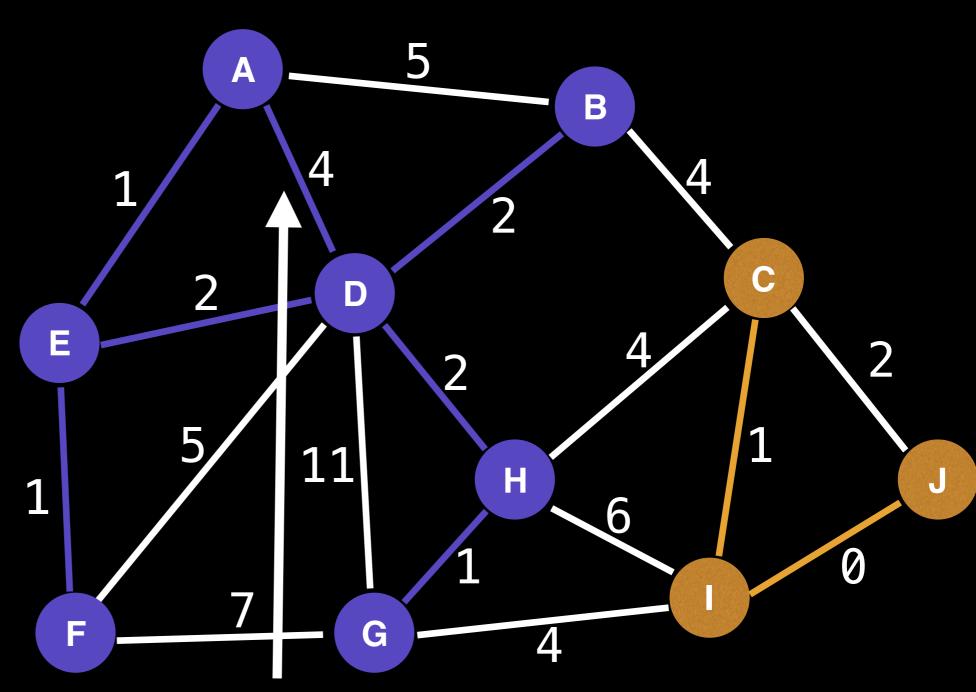
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  to H = 4
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  to B = 5
     G =
  to
     G = 11
  to
```



```
A to E = 1
  to
  to F = 1
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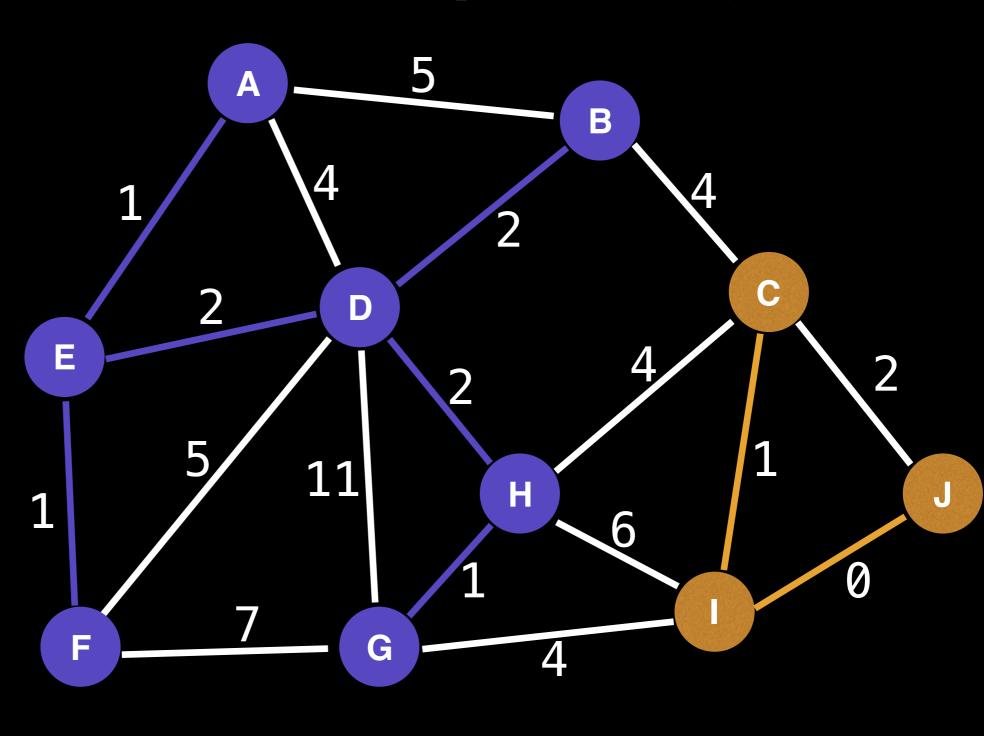


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 to E = 2
  to H = 2
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B to C = 4
C \text{ to } H = 4
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  to
  to
     G = 7
  to
     G = 11
  to
```

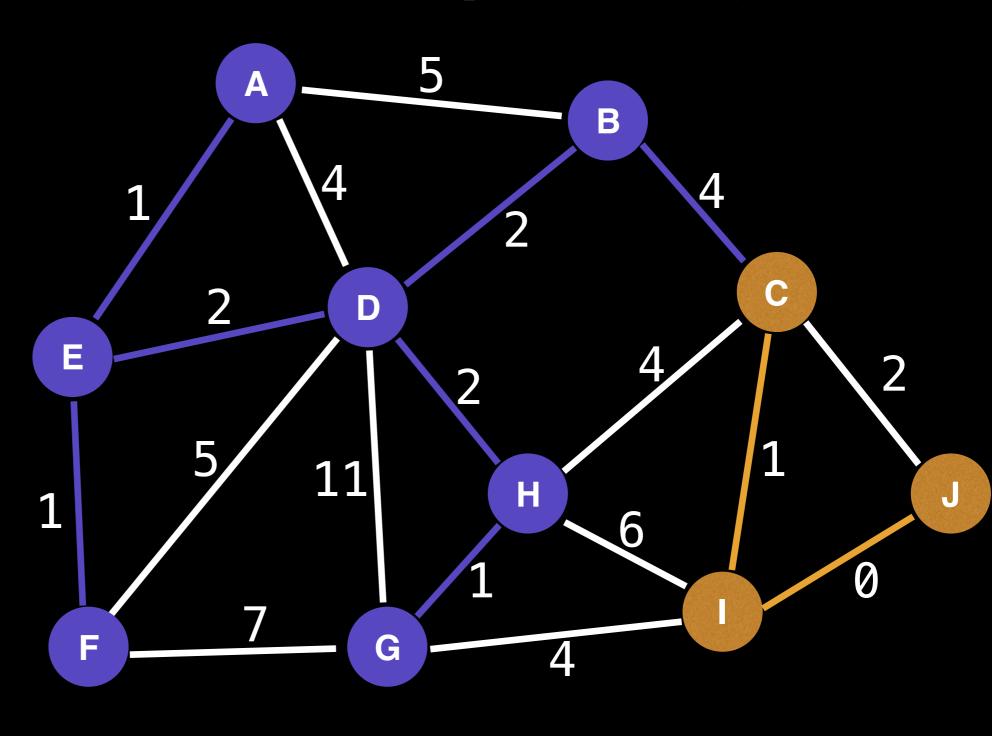


Nodes A,D are already connected in purple group. This creates a cycle

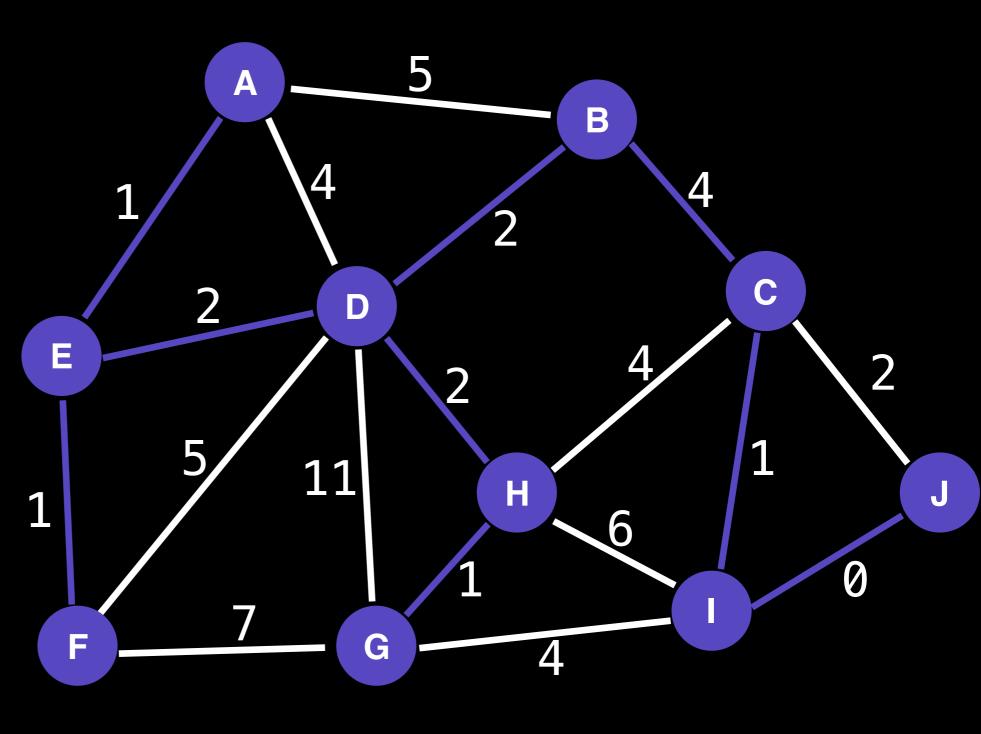
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  to
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  to J = 2
 to E = 2
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  to D = 4
B to C = 4
  to H = 4
  to I = 4
  to B = 5
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  to
     G = 11
  to
```



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A to E = 1
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 to E = 2
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A to E = 1
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  to
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  to
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  to
```



to E = 1to I = 1to F = 1G to H = 1to D = 2to J = 2D to E = 2E to H = 2to D = 4to C = 4to H = 4to I = 4to B = 5G to G = 7to

G = 11

to

## Union and Find operations in the next video

Implementation source code and tests
 can all be found at the following link:
 github.com/williamfiset/data-structures

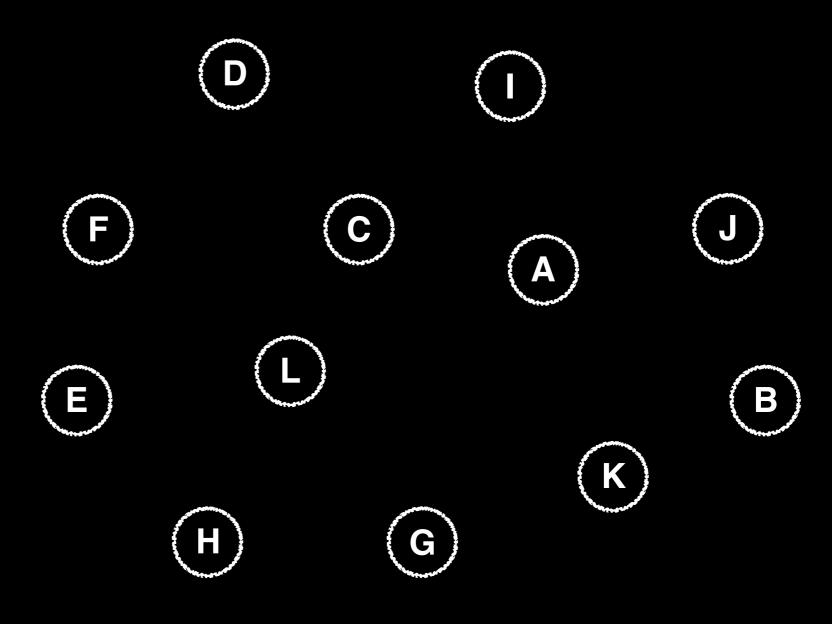
## Union Find

# Union and Find Operations

William Fiset

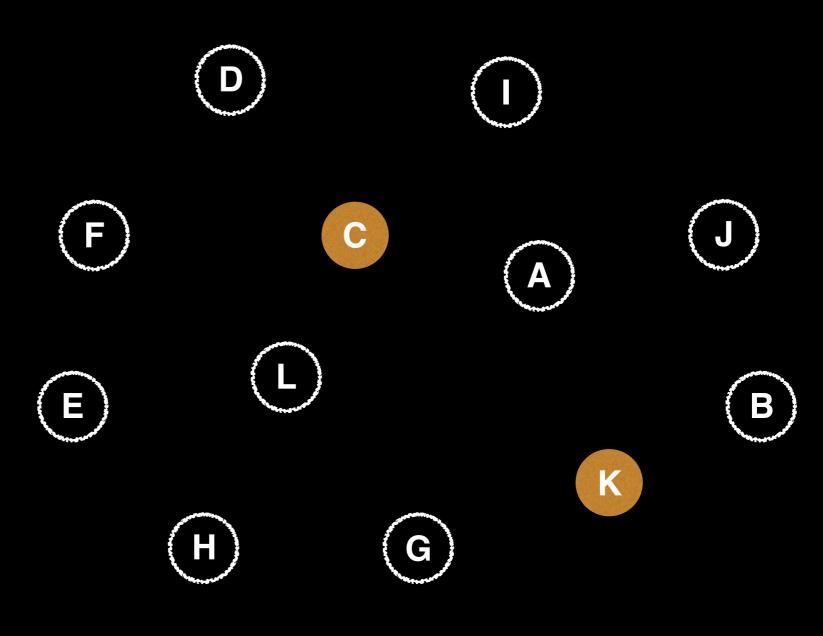
### **Instructions**:

```
Union(C,K)
Union(F,E)
Union(A,J)
Union(A,B)
Union(C,D)
Union(D,I)
Union(L,F)
Union(C,A)
Union(A,B)
Union(H,G)
Union(H,F)
Union(H,B)
```



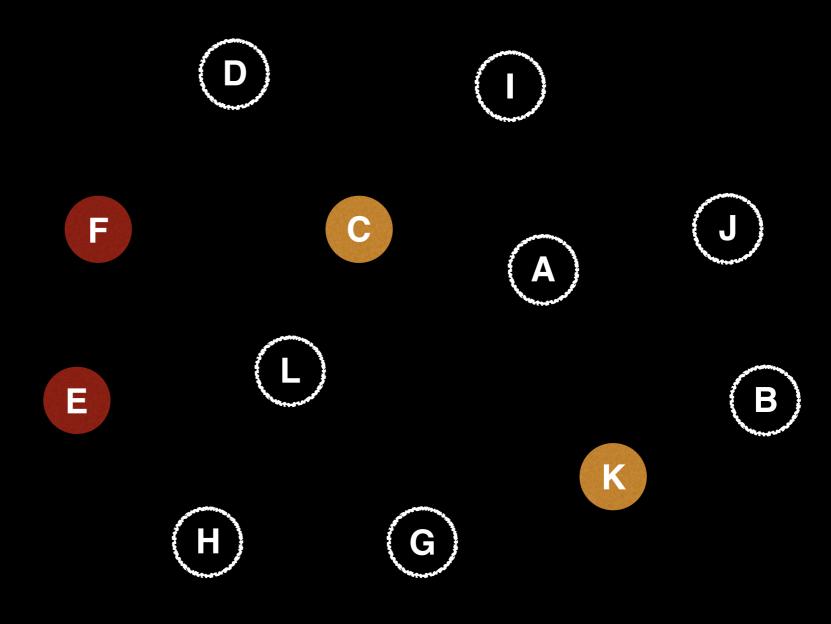
### **Instructions**:

```
→Union(C,K)
  Union(F,E)
  Union(A,J)
  Union(A,B)
  Union(C,D)
  Union(D,I)
  Union(L,F)
  Union(C,A)
  Union(A,B)
  Union(H,G)
  Union(H,F)
  Union(H,B)
```



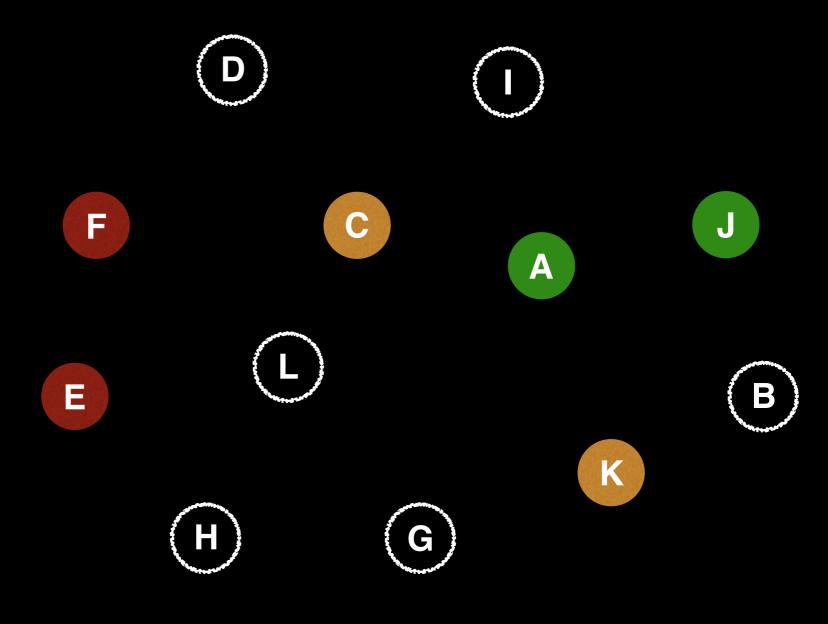
### **Instructions**:

```
Union(C,K)
→Union(F,E)
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  Union(D,I)
  Union(L,F)
  Union(C,A)
  Union(A,B)
  Union(H,G)
  Union(H,F)
  Union(H,B)
```



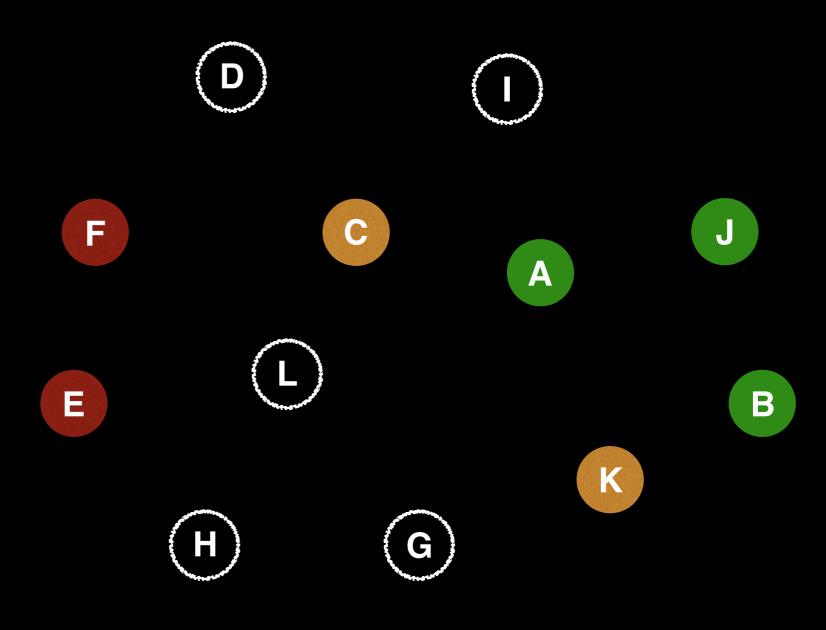
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```
Union(C,K)
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  Union(L,F)
  Union(C,A)
  Union(A,B)
  Union(H,G)
  Union(H,F)
  Union(H,B)
```



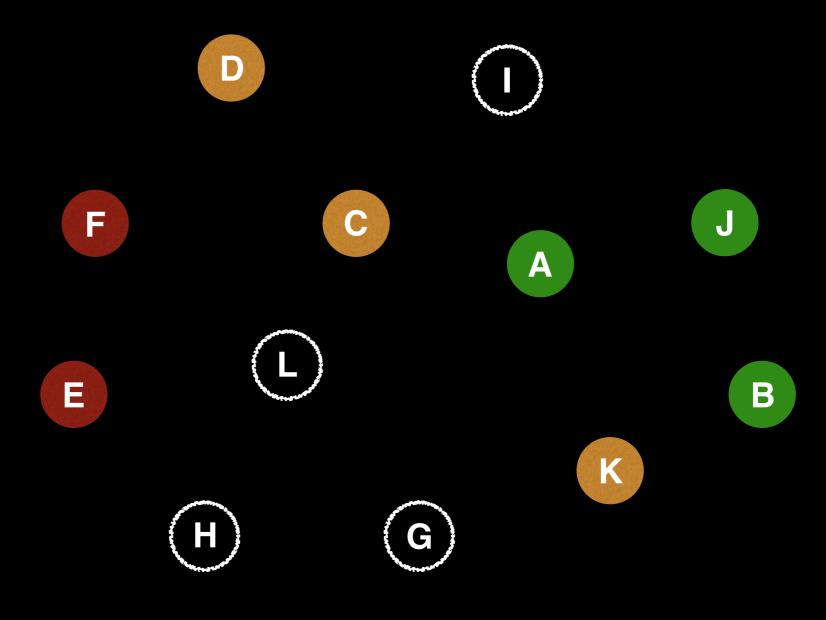
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```
Union(C,K)
  Union(F,E)
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→Union(A,B)
  Union(C,D)
  Union(D,I)
  Union(L,F)
  Union(C,A)
  Union(A,B)
  Union(H,G)
  Union(H,F)
  Union(H,B)
```



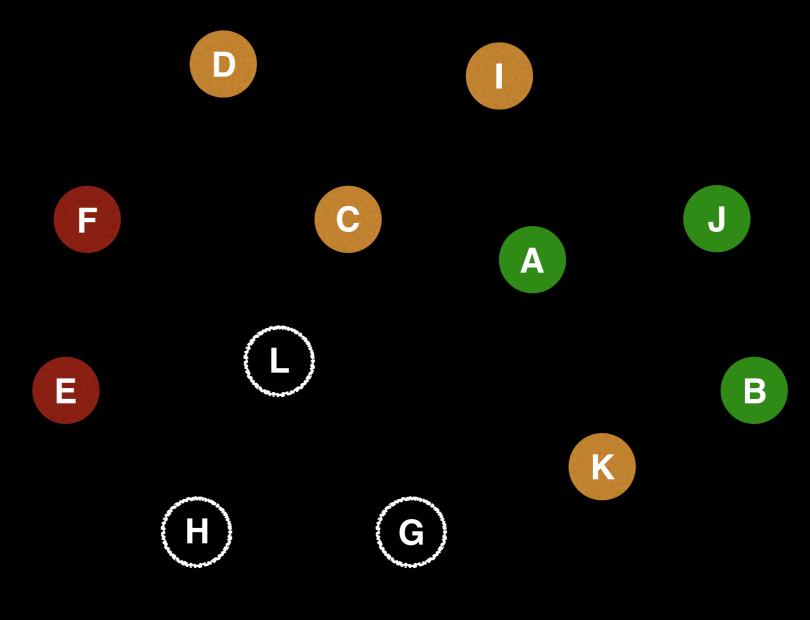
#### **Instructions**:

```
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  Union(F,E)
  Union(A,J)
  Union(A,B)
→Union(C,D)
  Union(D,I)
  Union(L,F)
  Union(C,A)
  Union(A,B)
  Union(H,G)
  Union(H,F)
  Union(H,B)
```



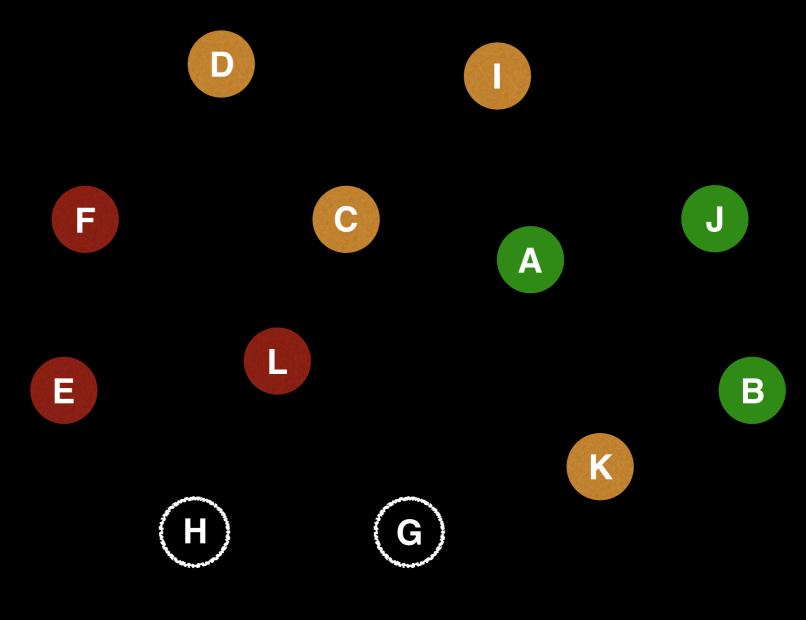
### **Instructions**:

```
Union(C,K)
  Union(F,E)
  Union(A,J)
  Union(A,B)
  Union(C,D)
→Union(D,I)
  Union(L,F)
  Union(C,A)
  Union(A,B)
  Union(H,G)
  Union(H,F)
  Union(H,B)
```



### Instructions:

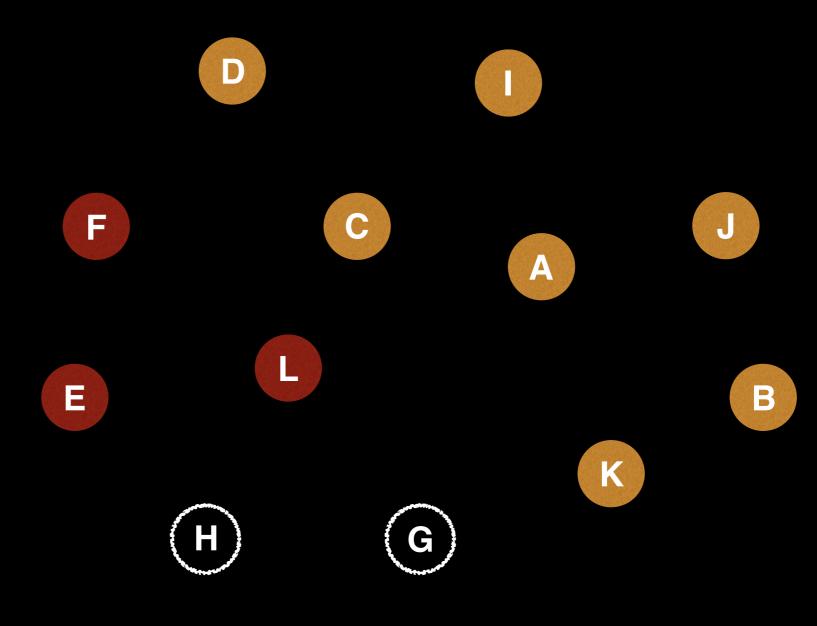
```
Union(C,K)
  Union(F,E)
  Union(A,J)
  Union(A,B)
  Union(C,D)
  Union(D,I)
→Union(L,F)
  Union(C,A)
  Union(A,B)
  Union(H,G)
  Union(H,F)
  Union(H,B)
```



### Instructions:

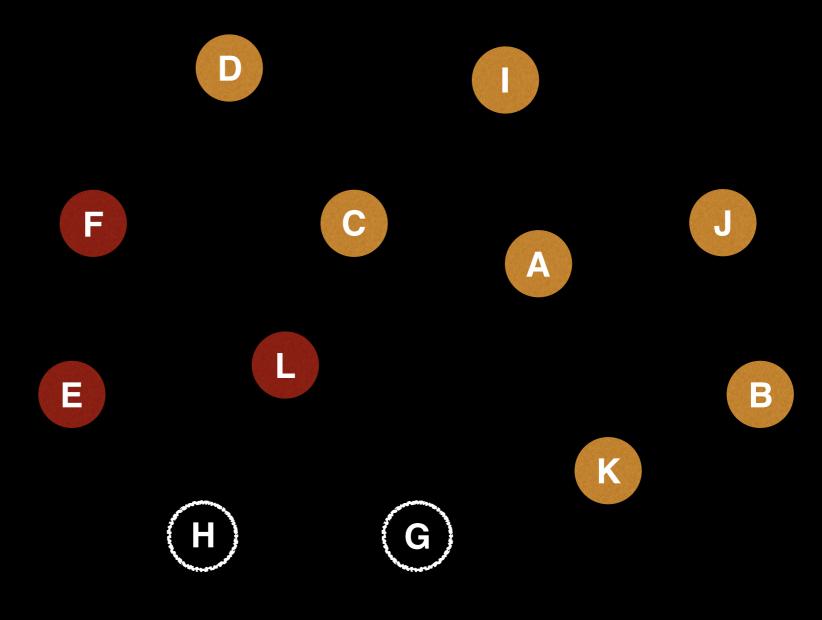
Union(C,K)

```
Union(F,E)
  Union(A,J)
  Union(A,B)
  Union(C,D)
  Union(D,I)
  Union(L,F)
→Union(C,A)
  Union(A,B)
  Union(H,G)
  Union(H,F)
  Union(H,B)
```



### Instructions:

```
Union(C,K)
  Union(F,E)
  Union(A,J)
  Union(A,B)
  Union(C,D)
  Union(D,I)
  Union(L,F)
  Union(C,A)
→Union(A,B)
  Union(H,G)
  Union(H,F)
  Union(H,B)
```

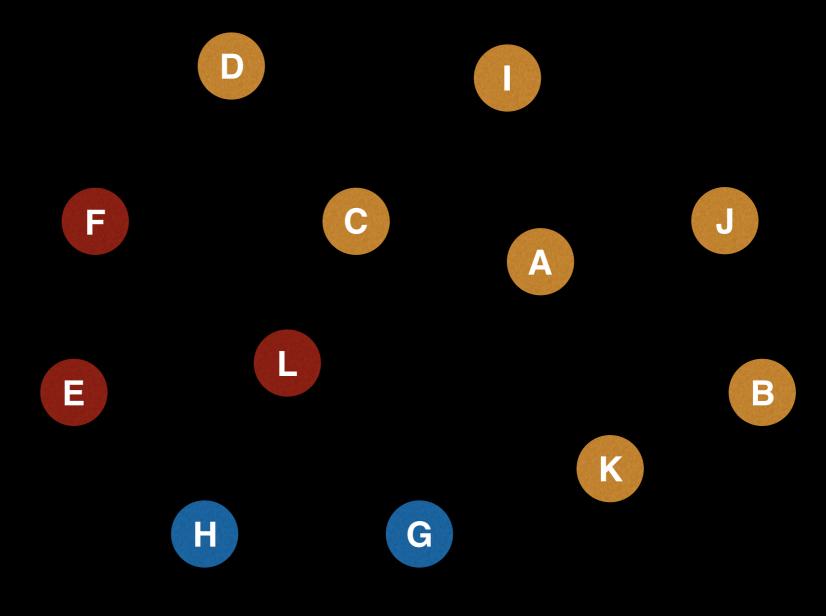


# Union and Find

### Instructions:

```
Union(C,K)
  Union(F,E)
  Union(A,J)
  Union(A,B)
  Union(C,D)
  Union(D,I)
  Union(L,F)
  Union(C,A)
  Union(A,B)
→Union(H,G)
  Union(H,F)
```

Union(H,B)

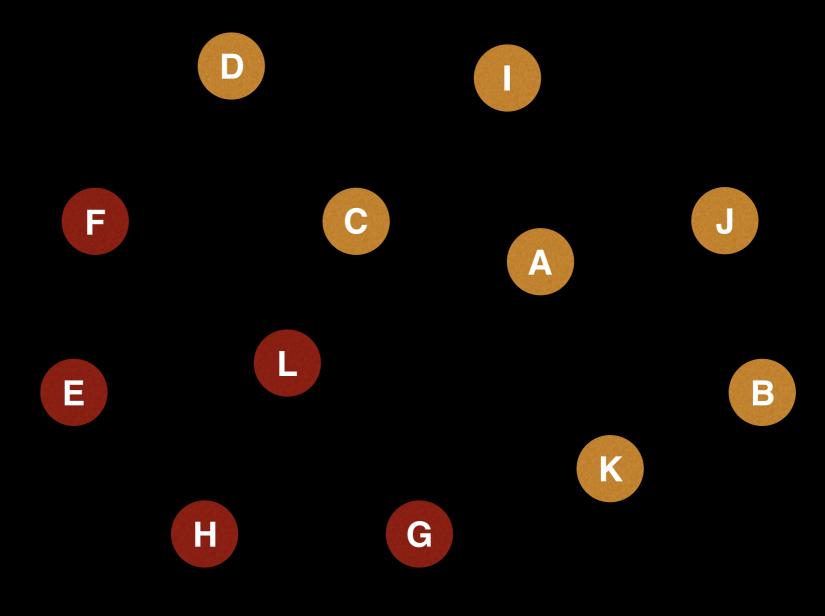


White chalk circles represent groups by themselves. Coloured circles belong to the group with the same colour.

# Union and Find

### Instructions:

```
Union(C,K)
  Union(F,E)
  Union(A,J)
  Union(A,B)
  Union(C,D)
  Union(D,I)
  Union(L,F)
  Union(C,A)
  Union(A,B)
  Union(H,G)
→Union(H,F)
  Union(H,B)
```

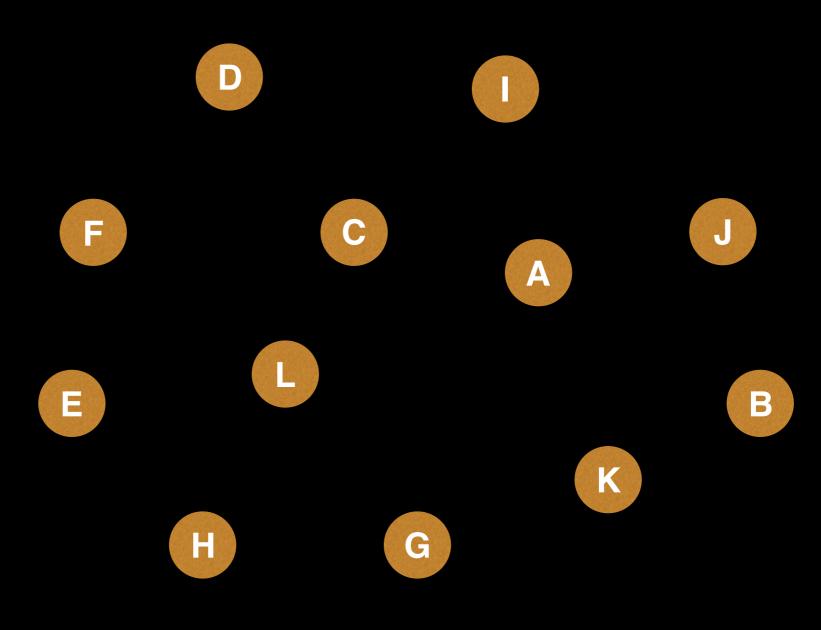


White chalk circles represent groups by themselves. Coloured circles belong to the group with the same colour.

# Union and Find

### Instructions:

```
Union(C,K)
  Union(F,E)
  Union(A,J)
  Union(A,B)
  Union(C,D)
  Union(D,I)
  Union(L,F)
  Union(C,A)
  Union(A,B)
  Union(H,G)
  Union(H,F)
→Union(H,B)
```

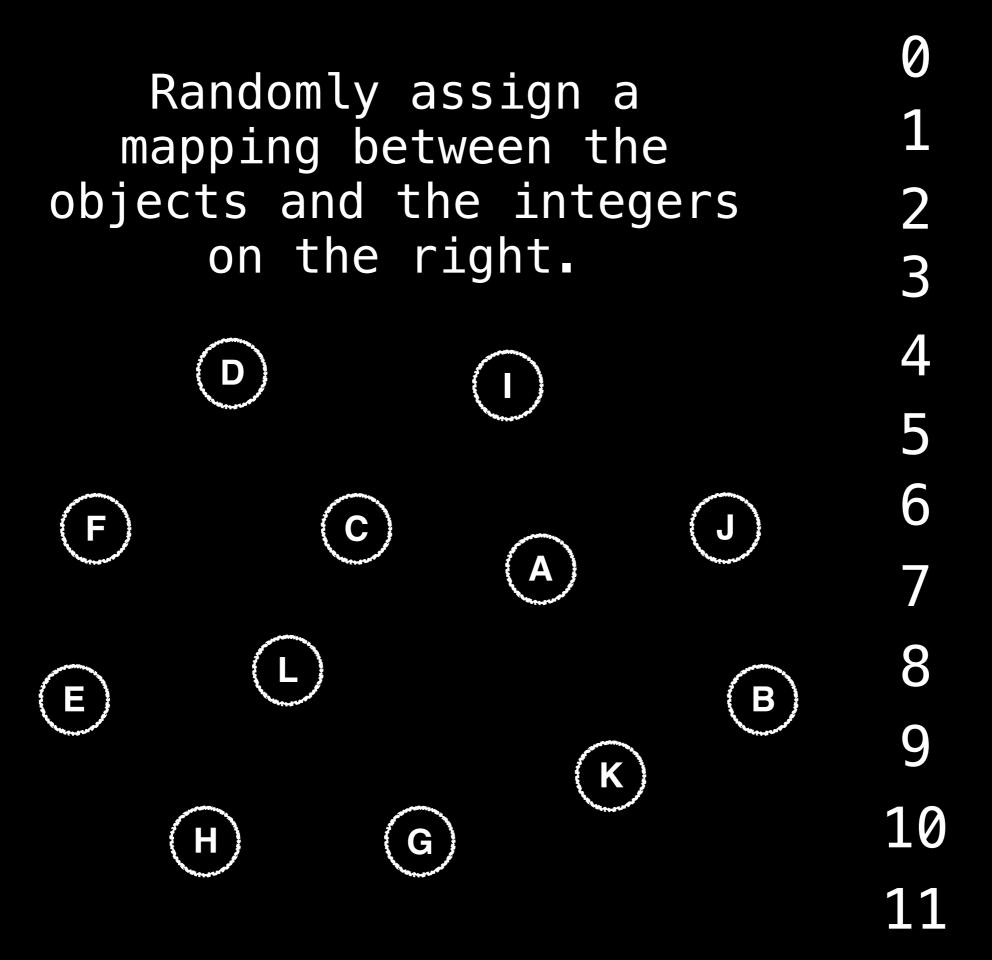


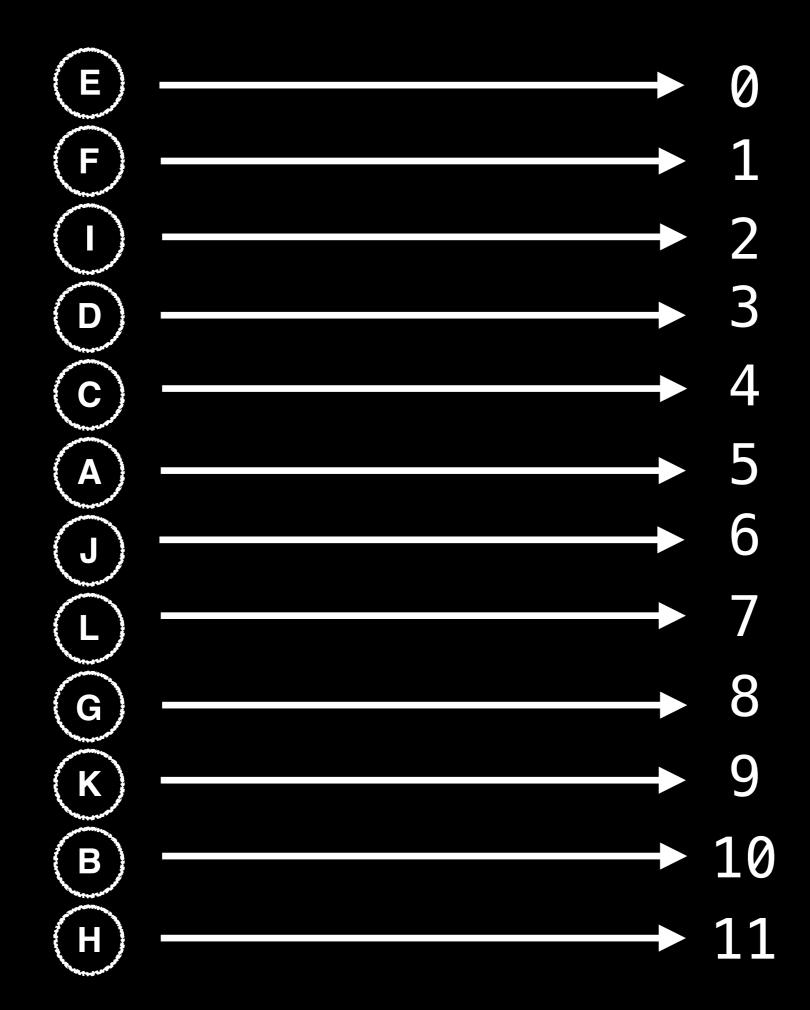
White chalk circles represent groups by themselves. Coloured circles belong to the group with the same colour.

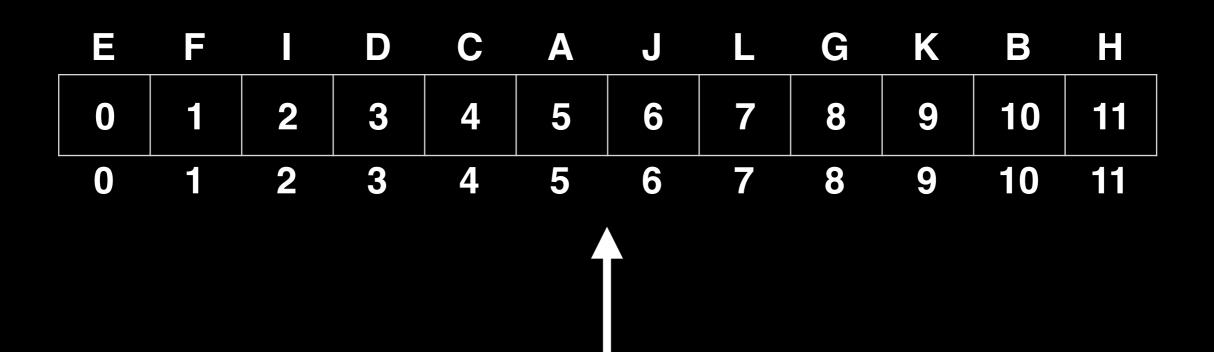
# Creating Union Find

To begin using Union Find, first construct a bijection (a mapping) between your objects and the integers in the range [0, n).

NOTE: This step is not necessary in general, but it will allow us to construct an array-based union find.







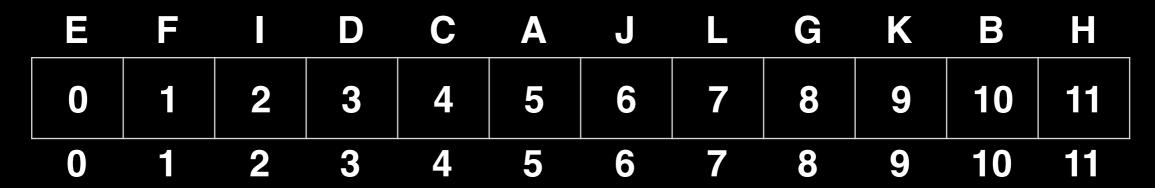
Store Union Find information in an array. Each index has an associated object (letter in this example) we can lookup through our mapping.

Ε	F		D	C	A	J	L	G	K	В	Н
0	1	2	3	4	5	6	7	8	9	10	11
0											

### <u> Instructions</u>:

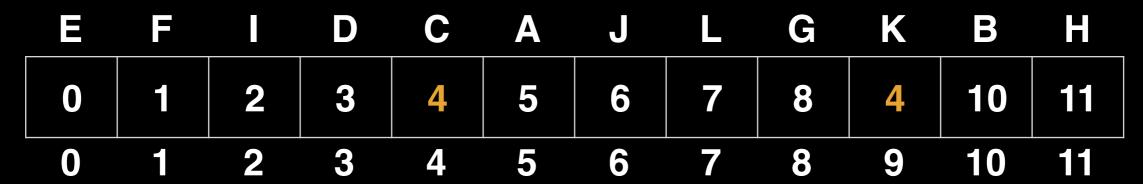
Union(C,K)
Union(F,E)
Union(A,J)
Union(A,B)
Union(C,D)
Union(D,I)

Union(C,D)
Union(D,I)
Union(L,F)
Union(C,A)
Union(A,B)
Union(H,G)
Union(H,F)
Union(H,F)



#### <u> Instructions</u>:

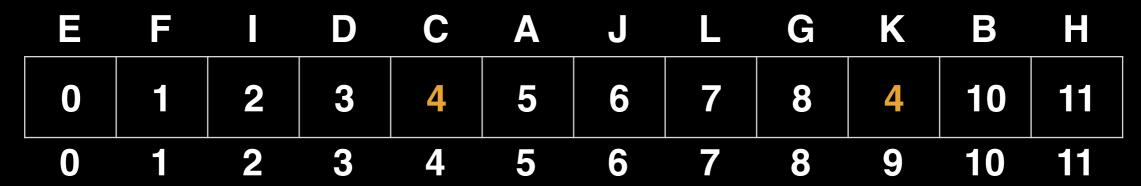
Union(C,K) $\leftarrow$ Union(F,E) Union(A,J) Union(A,B) Union(C,D) Union(D,I) Union(L,F) Union(C,A) Union(A,B) Union(H,G) Union(H,F) Union(H,B)



Union(H,F)

Union(H,B)

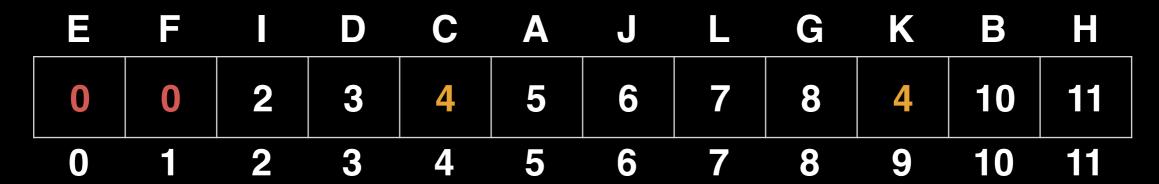
```
Instructions:
Union(C,K)\leftarrow
Union(F,E)
Union(A,J)
Union(A,B)
Union(C,D)
Union(D,I)
Union(L,F)
Union(C,A)
Union(A,B)
Union(H,G)
```



Union(H,F)

Union(H,B)

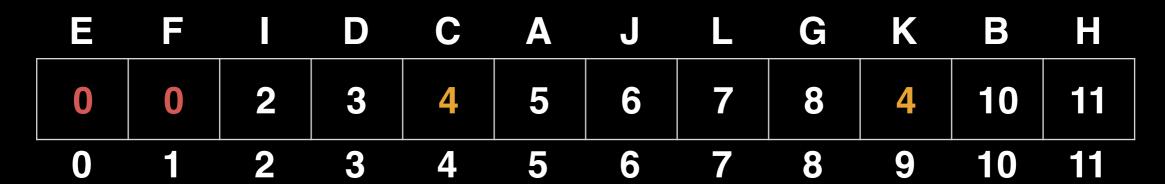
```
Instructions:
Union(C,K)
Union(F,E)◀
Union(A,J)
Union(A,B)
Union(C,D)
Union(D,I)
Union(L,F)
Union(C,A)
Union(A,B)
Union(H,G)
```



Union(H,F)

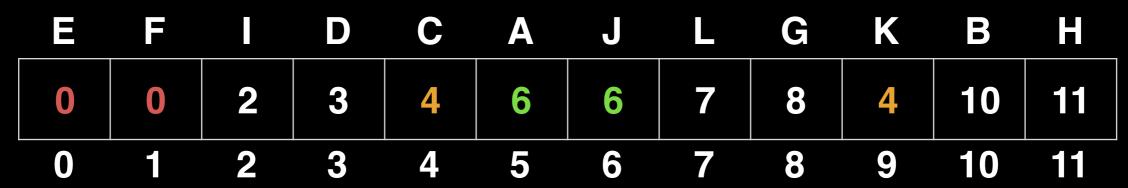
Union(H,B)

```
Union(C,K)
Union(F,E)◀
Union(A,J)
Union(A,B)
               E
Union(C,D)
Union(D,I)
Union(L,F)
               F
Union(C,A)
Union(A,B)
Union(H,G)
```



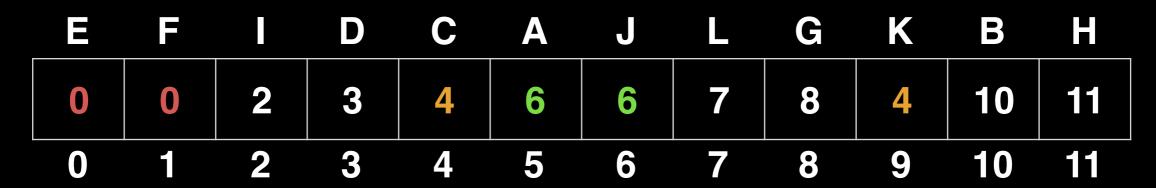
Union(H,F)

Union(H,B)



Union(H,B)

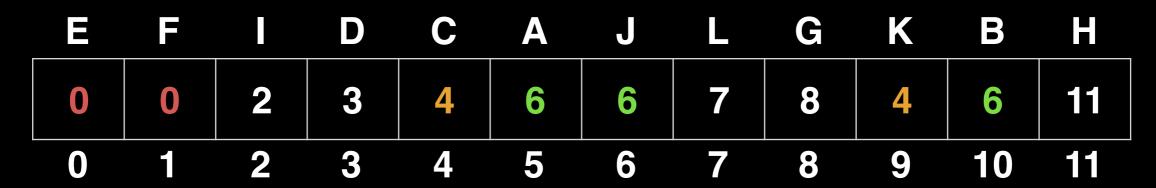
```
Union(C,K)
Union(F,E)
Union(A,J)←
Union(A,B)
               E
Union(C,D)
Union(D,I)
Union(L,F)
               F
Union(C,A)
Union(A,B)
Union(H,G)
Union(H,F)
```

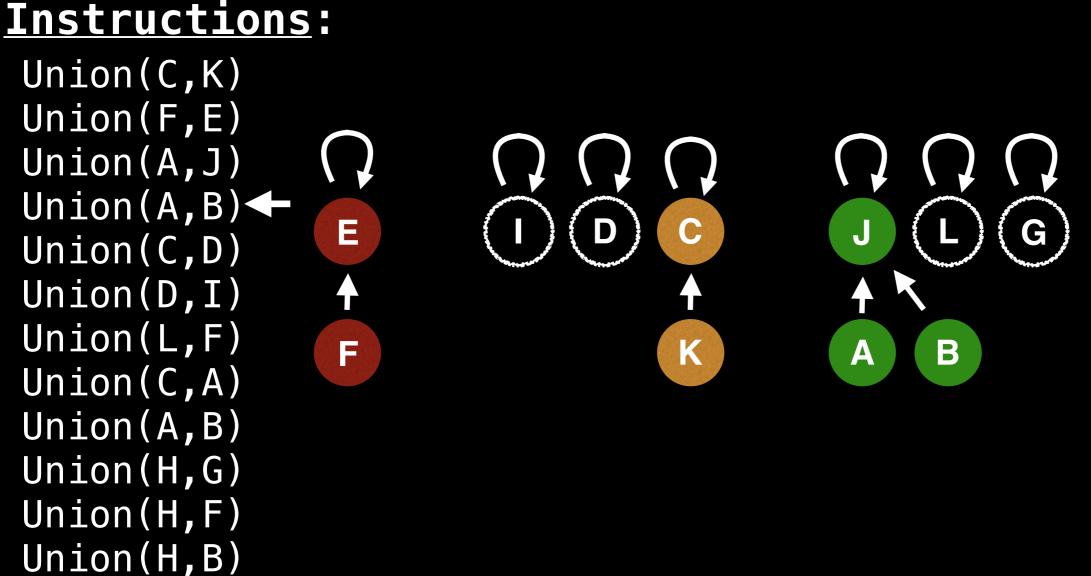


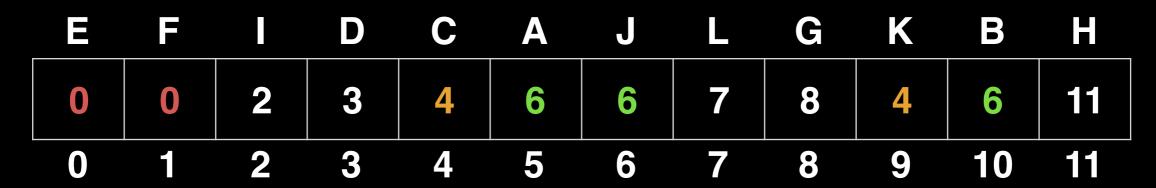
Union(H,F)

Union(H,B)

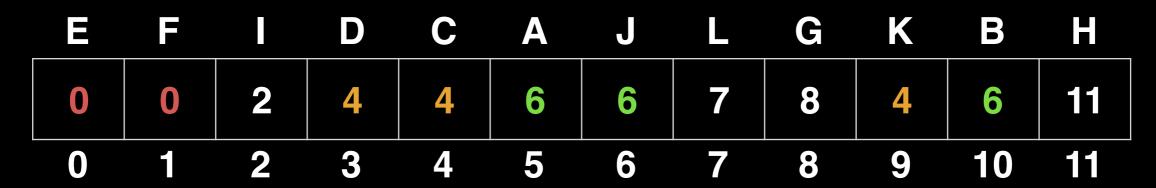
```
Union(C,K)
Union(F,E)
Union(A,J)
Union(A,B)◀
               E
Union(C,D)
Union(D,I)
Union(L,F)
               F
Union(C,A)
Union(A,B)
Union(H,G)
```

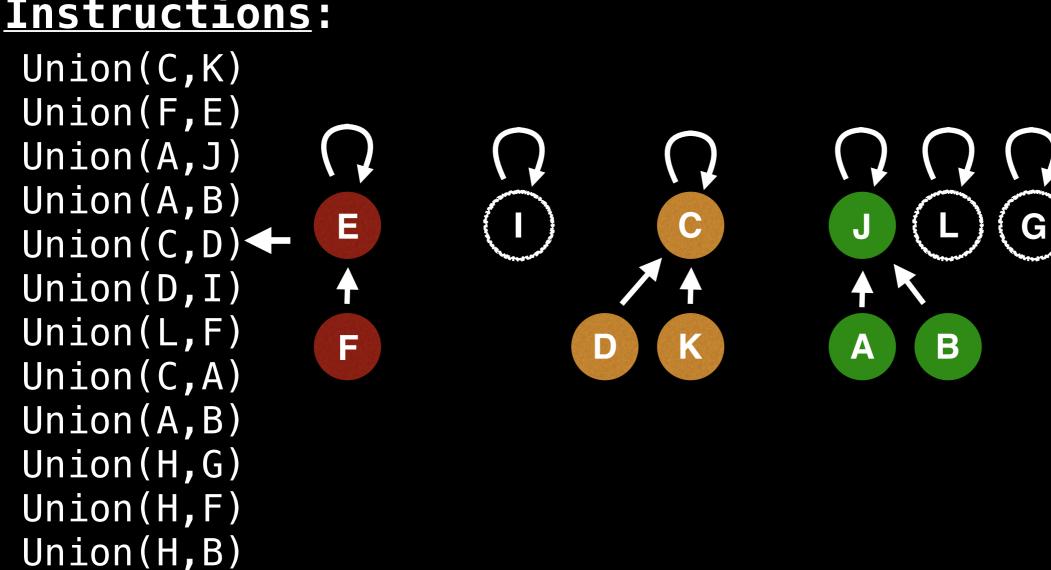


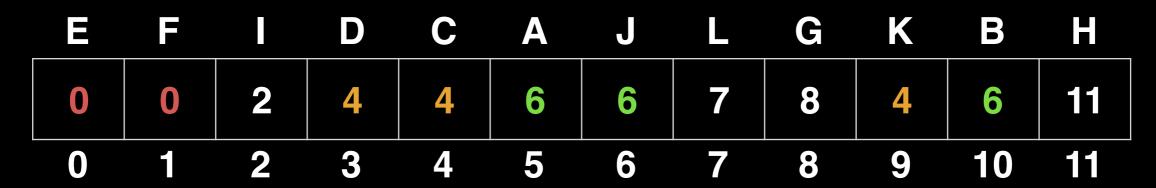


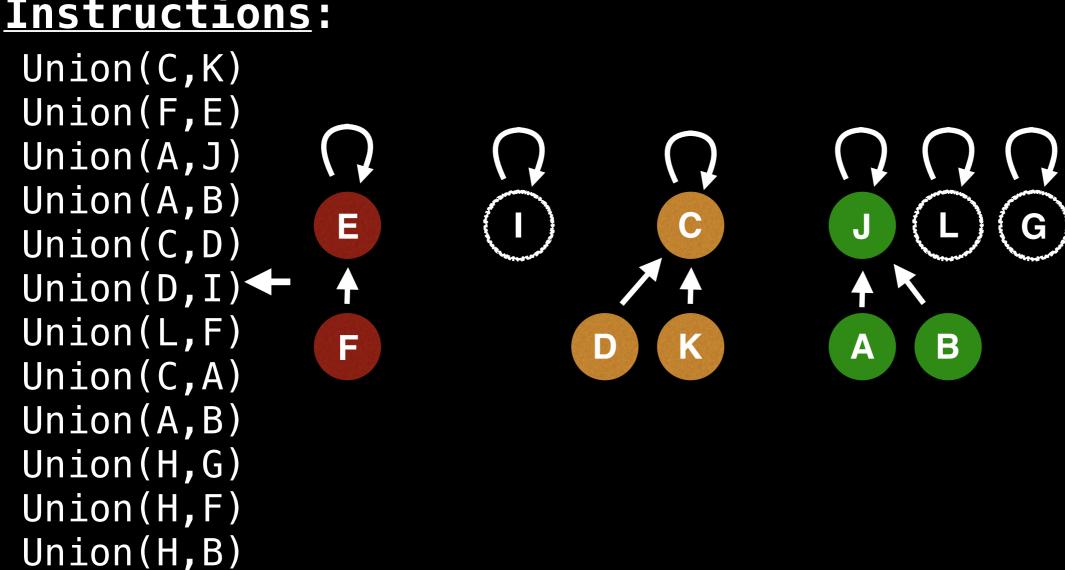


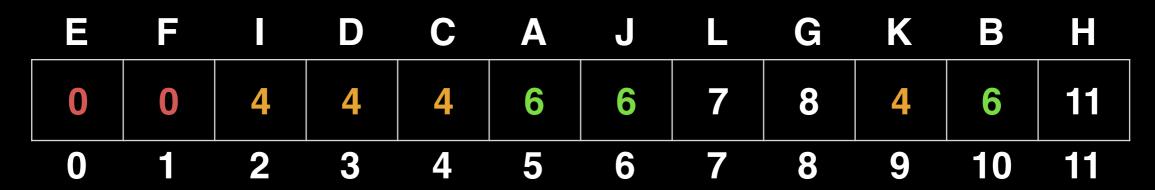
```
Union(C,K)
Union(F,E)
Union(A,J)
Union(A,B)
               E
Union(C,D)◀
Union(D,I)
Union(L,F)
                                            B
               F
Union(C,A)
Union(A,B)
Union(H,G)
Union(H,F)
Union(H,B)
```

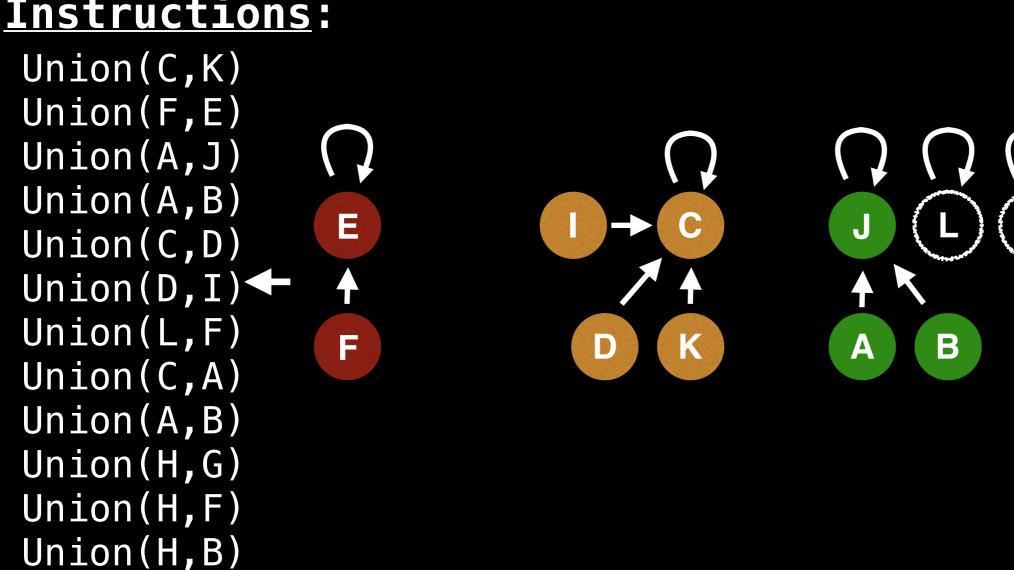


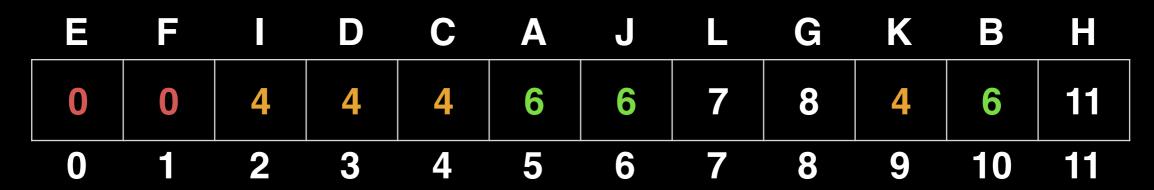




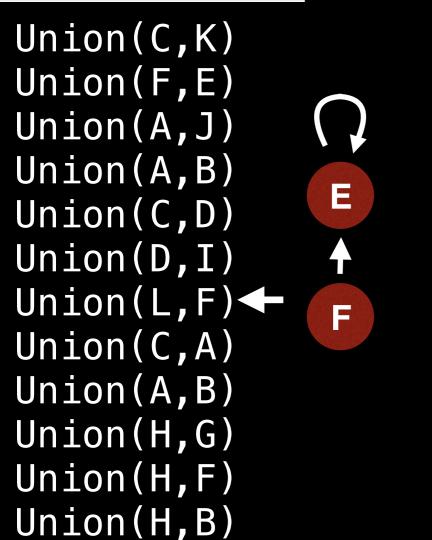


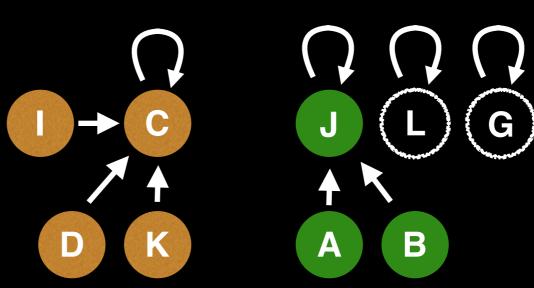


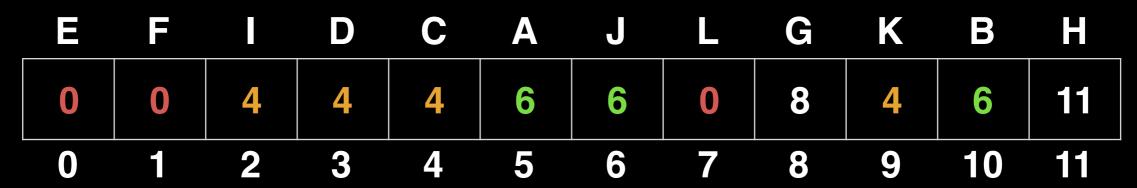


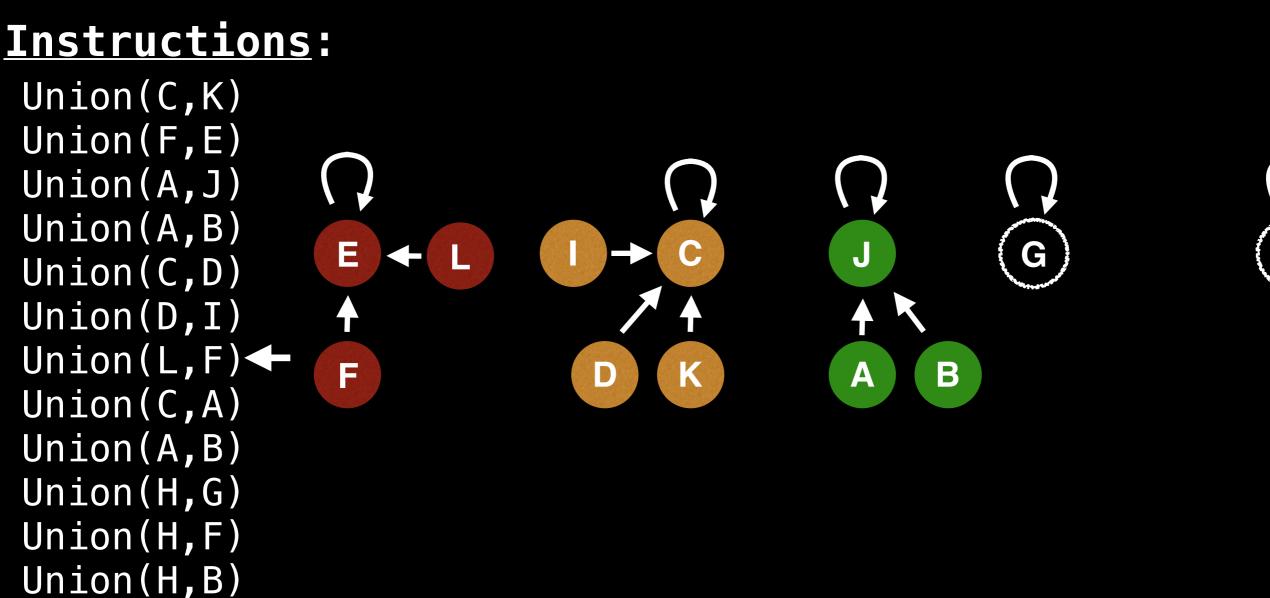


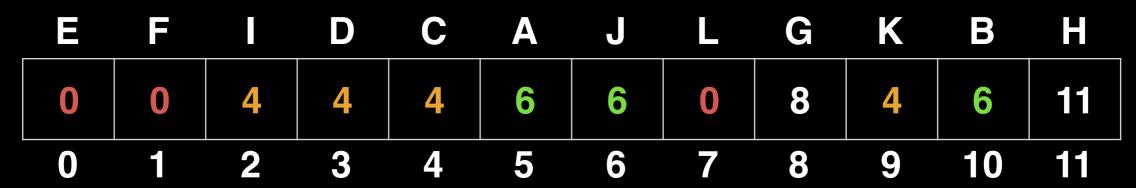
### <u> Instructions</u>:

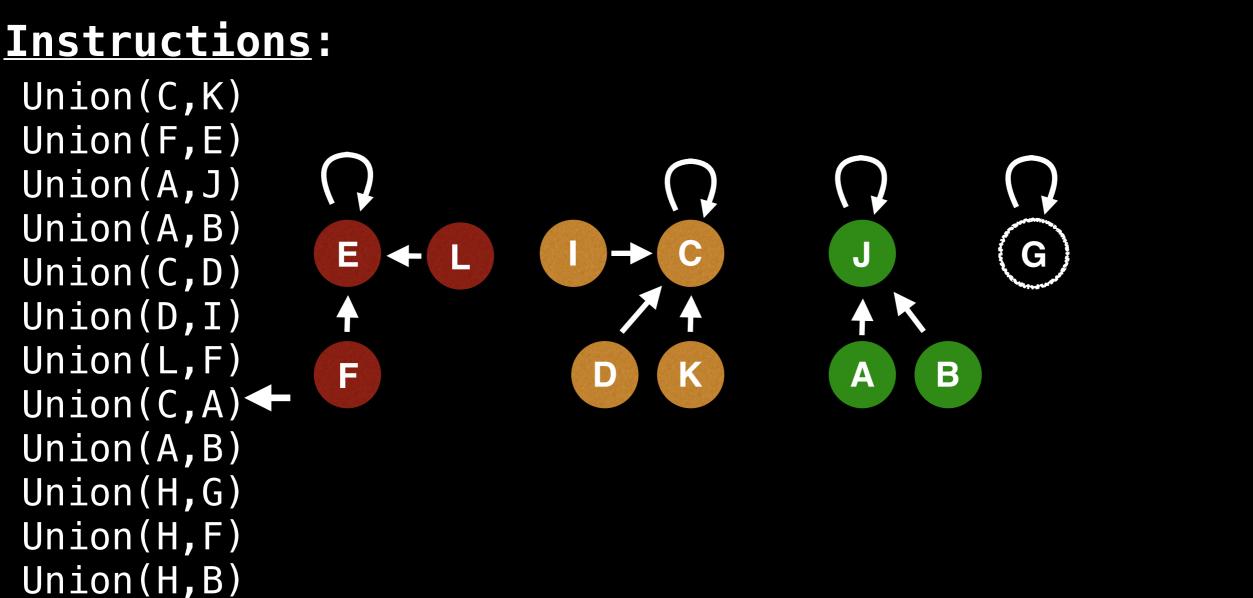


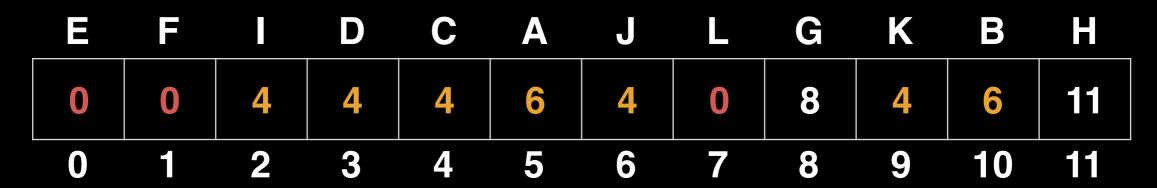




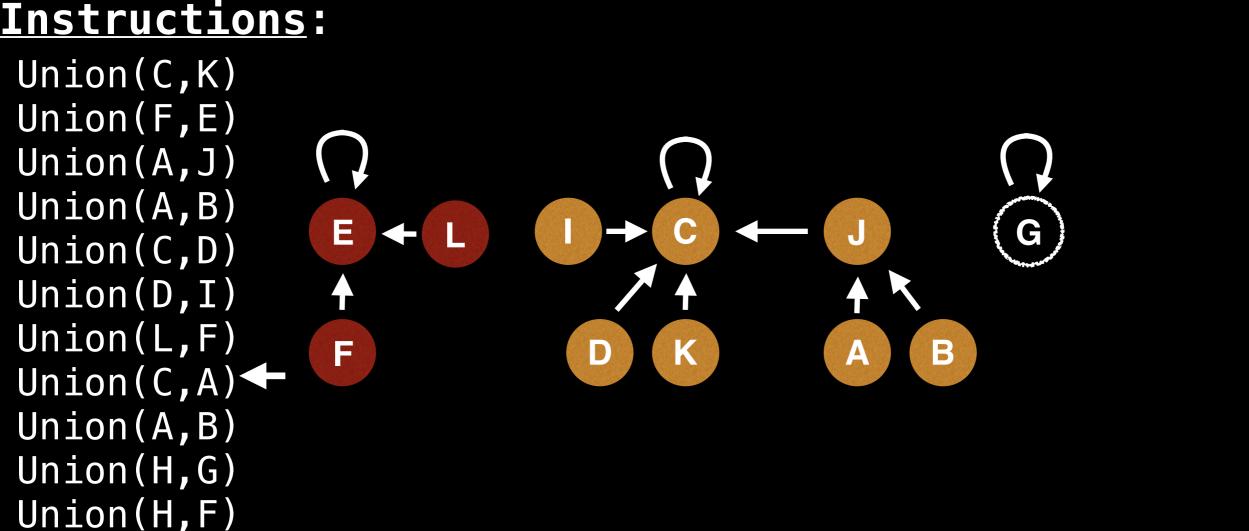


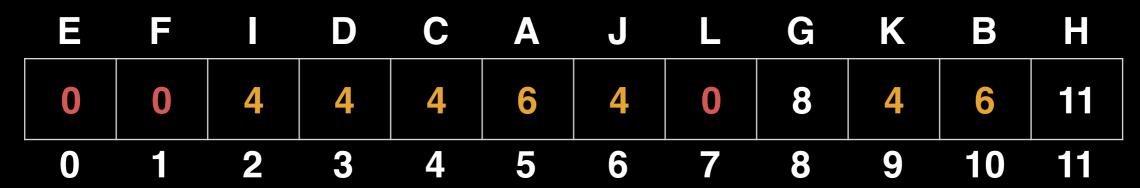




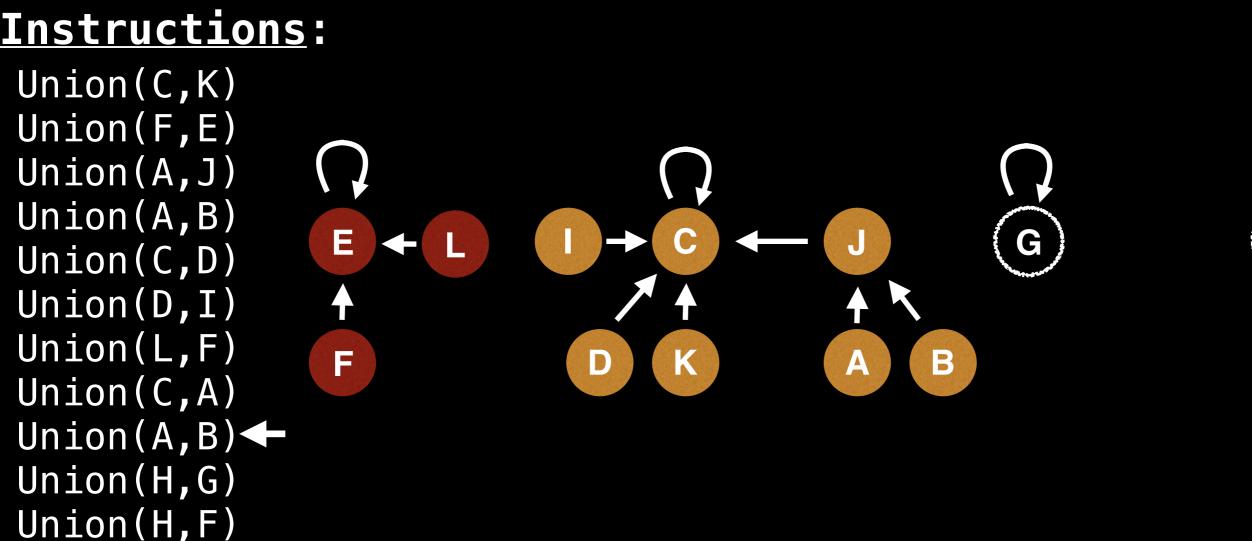


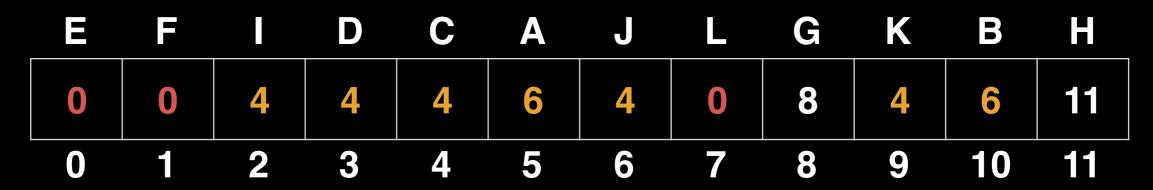
Union(H,B)



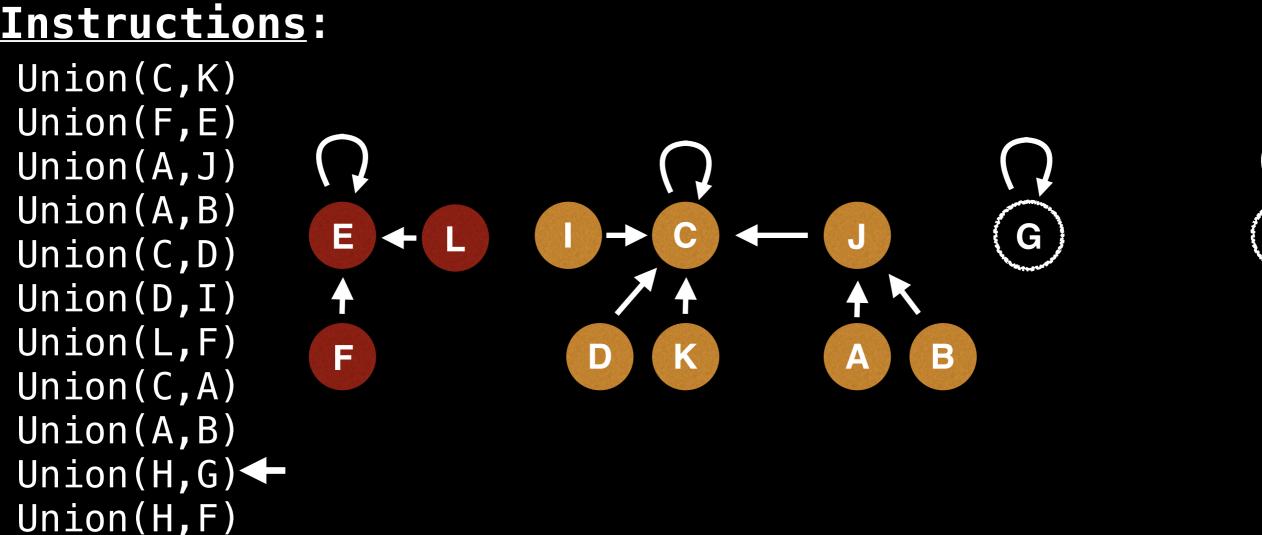


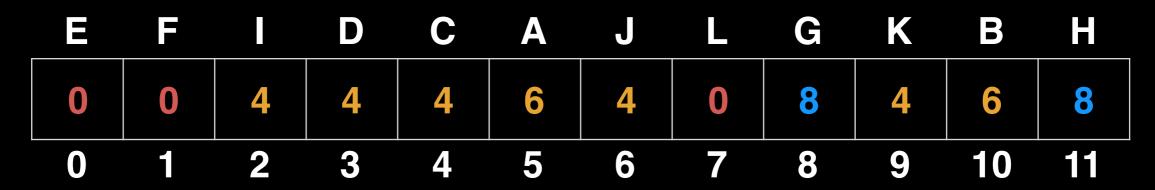
Union(H,B)



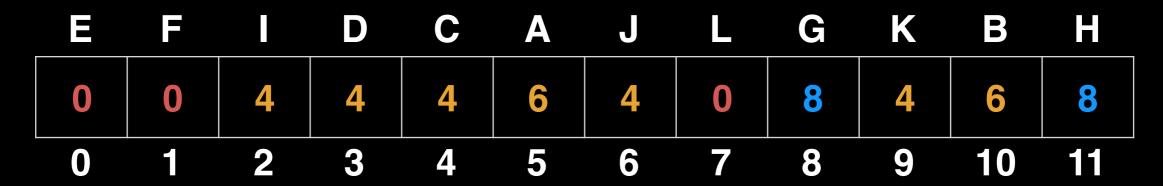


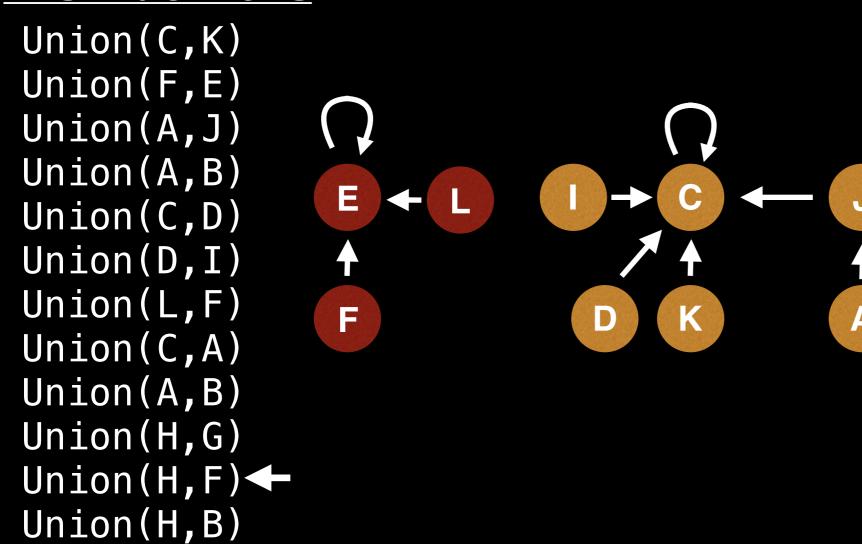
Union(H,B)





```
Union(C,K)
Union(F,E)
Union(A,J)
Union(A,B)
                                                G
               E
Union(C,D)
Union(D,I)
Union(L,F)
                                                H
               F
                                            B
Union(C,A)
Union(A,B)
Union(H,G)◀
Union(H,F)
Union(H,B)
```



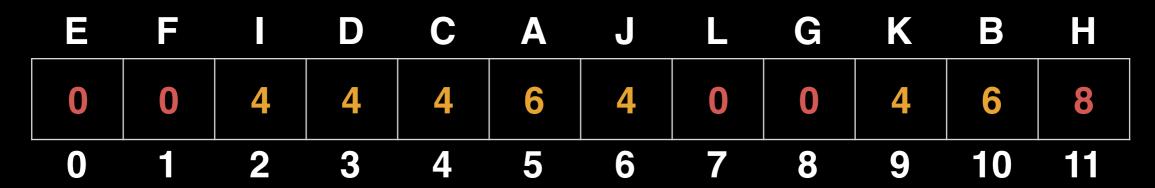


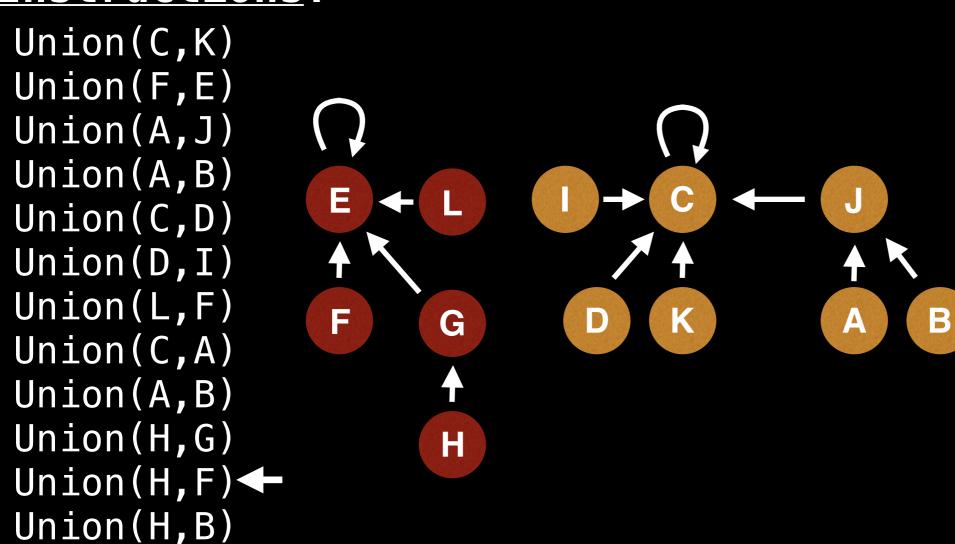
(This example does not use path compression)

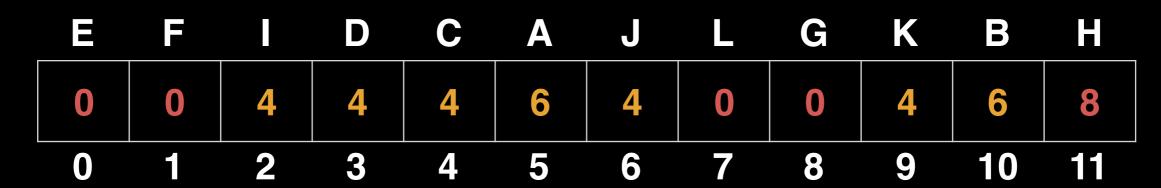
G

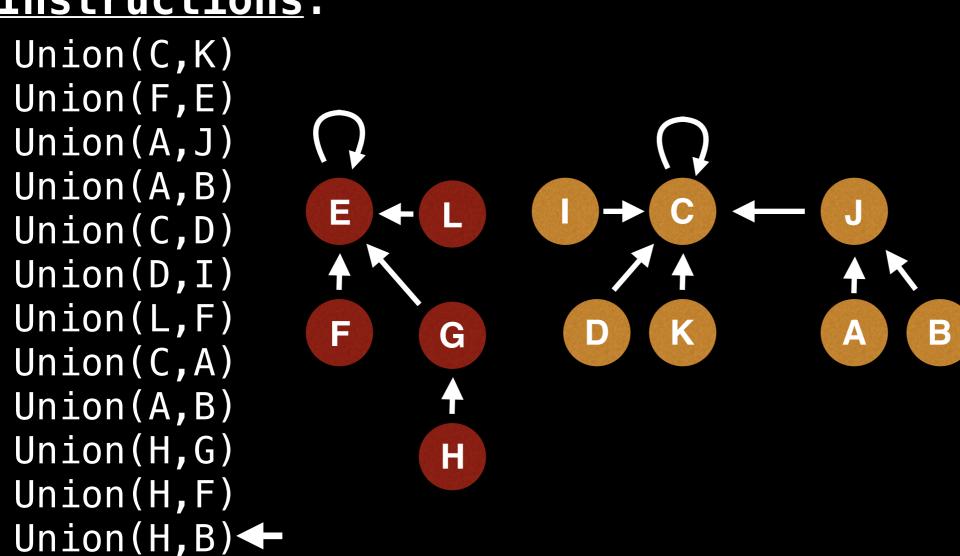
H

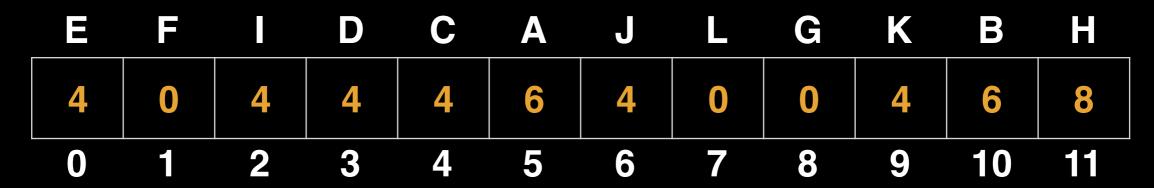
B

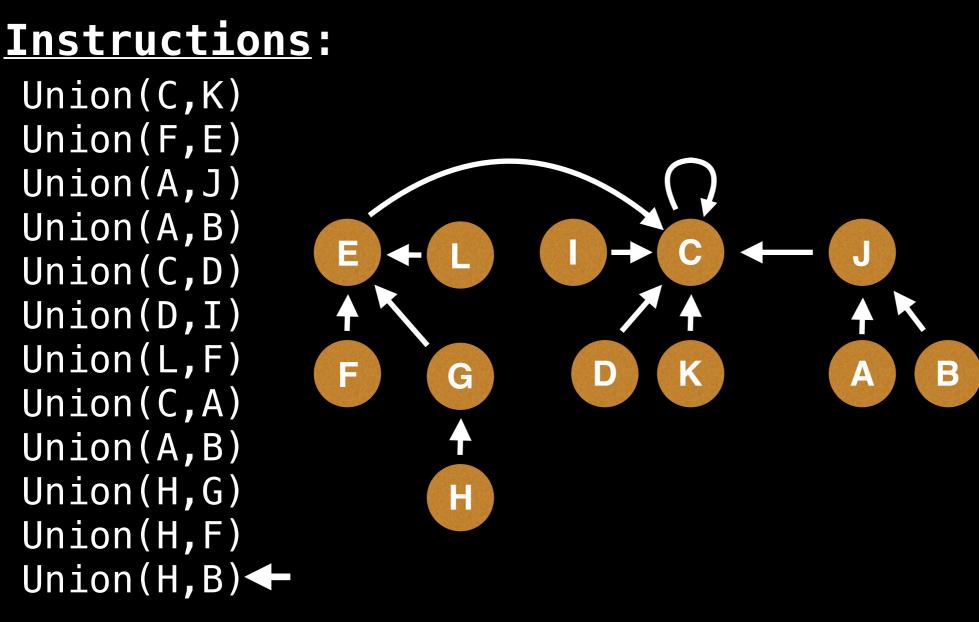












# Summary

### Find Operation

To **find** which component a particular element belongs to find the root of that component by following the parent nodes until a self loop is reached (a node who's parent is itself)

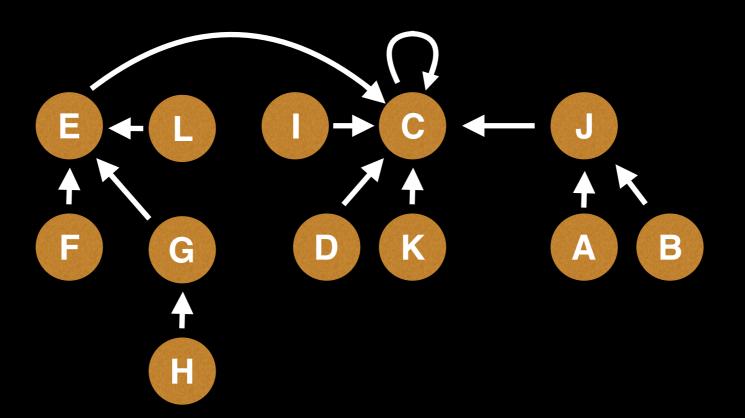
## Union Operation

To unify two elements find which are the root nodes of each component and if the root nodes are different make one of the root nodes be the parent of the other.

The number of components is equal to the number of roots remaining. Also, remark that the number of root nodes never increases.

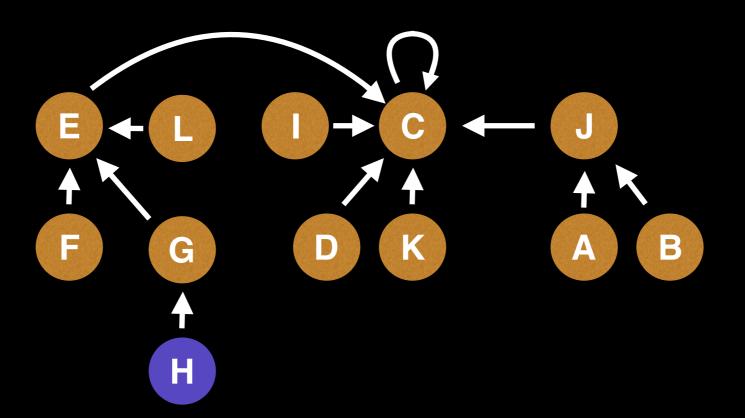
Our current version of Union Find does not support the nice  $\alpha(n)$  time complexity we want.

Checking if H and B belong to the same group takes five hops and in the worst case this is potentially much more.



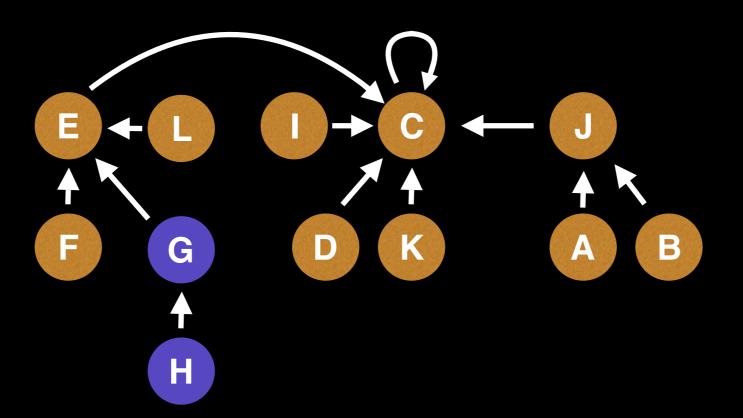
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Checking if H and B belong to the same group takes five hops and in the worst case this is potentially much more.

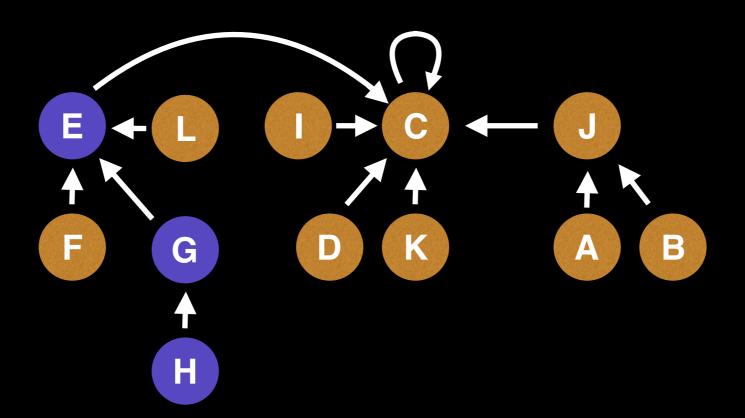


Our current version of Union Find does not support the nice  $\alpha(n)$  time complexity we want.

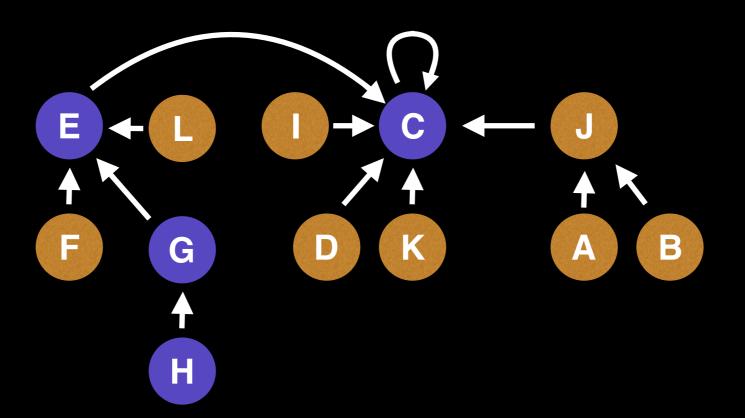
Checking if H and B belong to the same group takes five hops and in the worst case this is potentially much more.



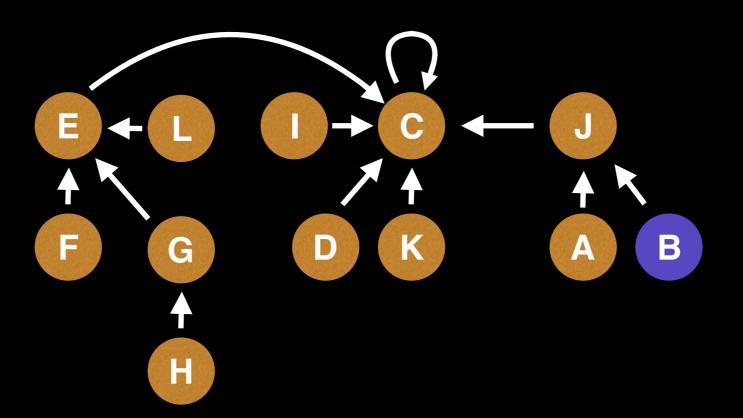
Our current version of Union Find does not support the nice  $\alpha(n)$  time complexity we want.



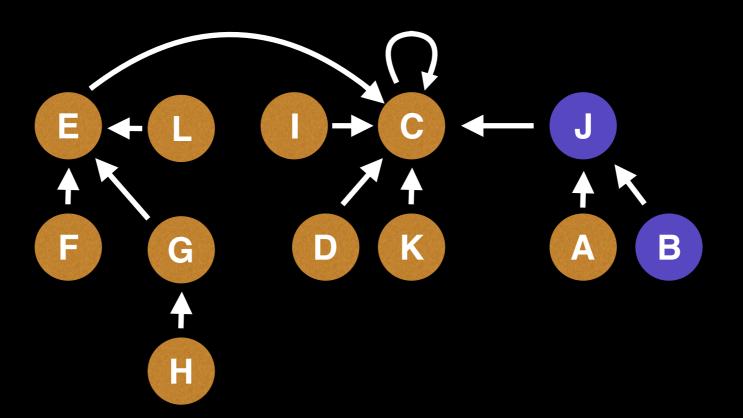
Our current version of Union Find does not support the nice  $\alpha(n)$  time complexity we want.



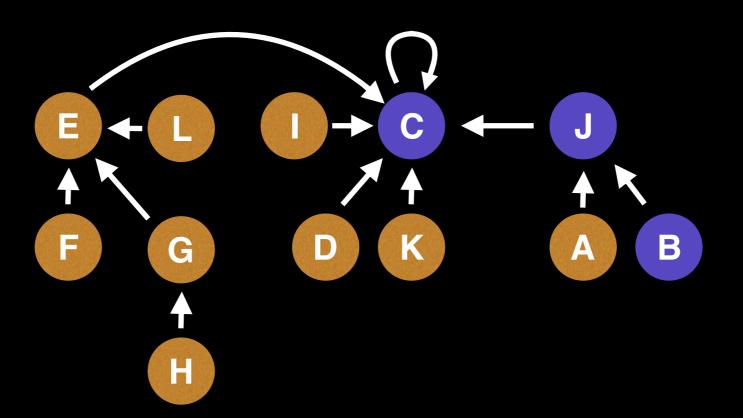
Our current version of Union Find does not support the nice  $\alpha(n)$  time complexity we want.



Our current version of Union Find does not support the nice  $\alpha(n)$  time complexity we want.



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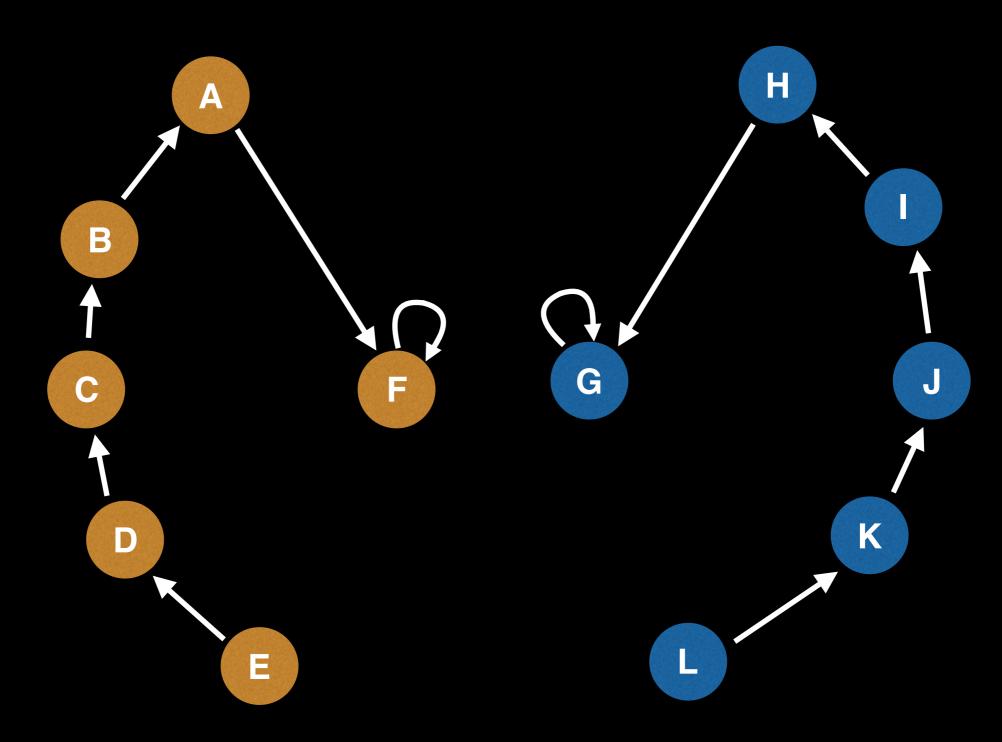
# Path Compression follows in the next video

Implementation source code and tests
 can all be found at the following link:
 github.com/williamfiset/data-structures

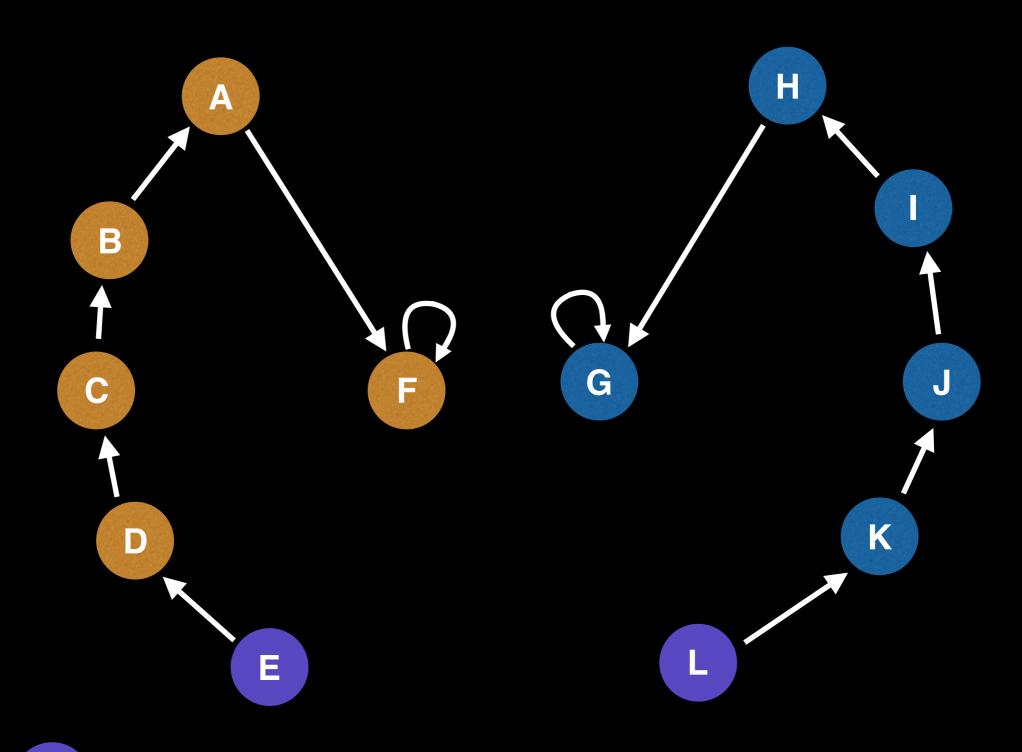
# Path Compression Union Find

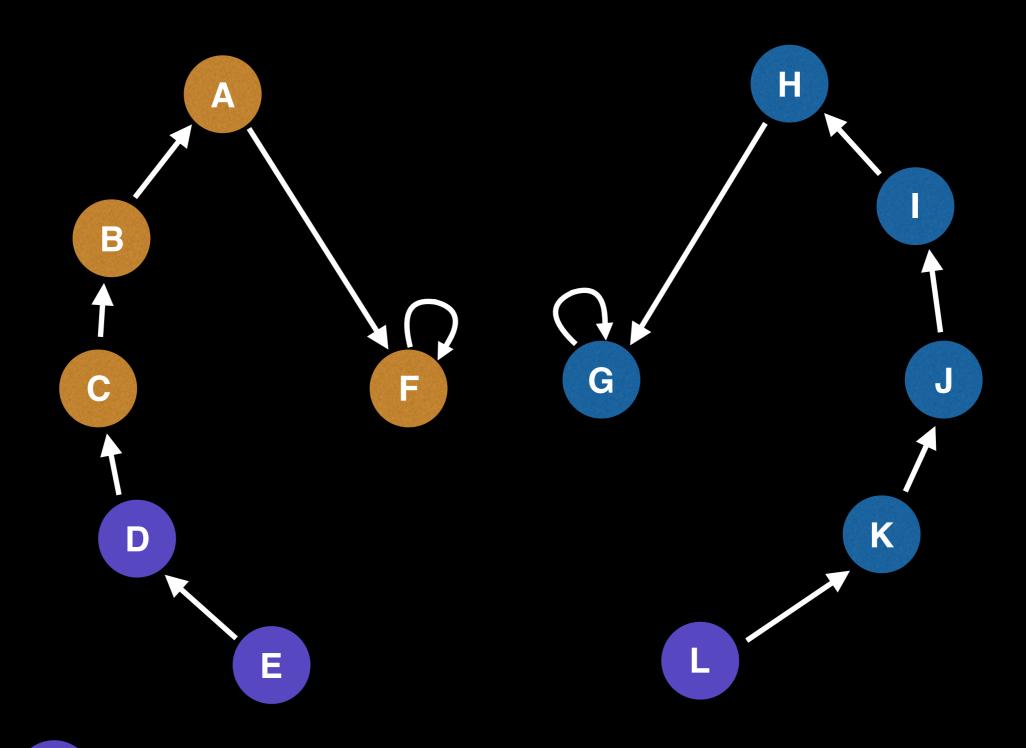
William Fiset

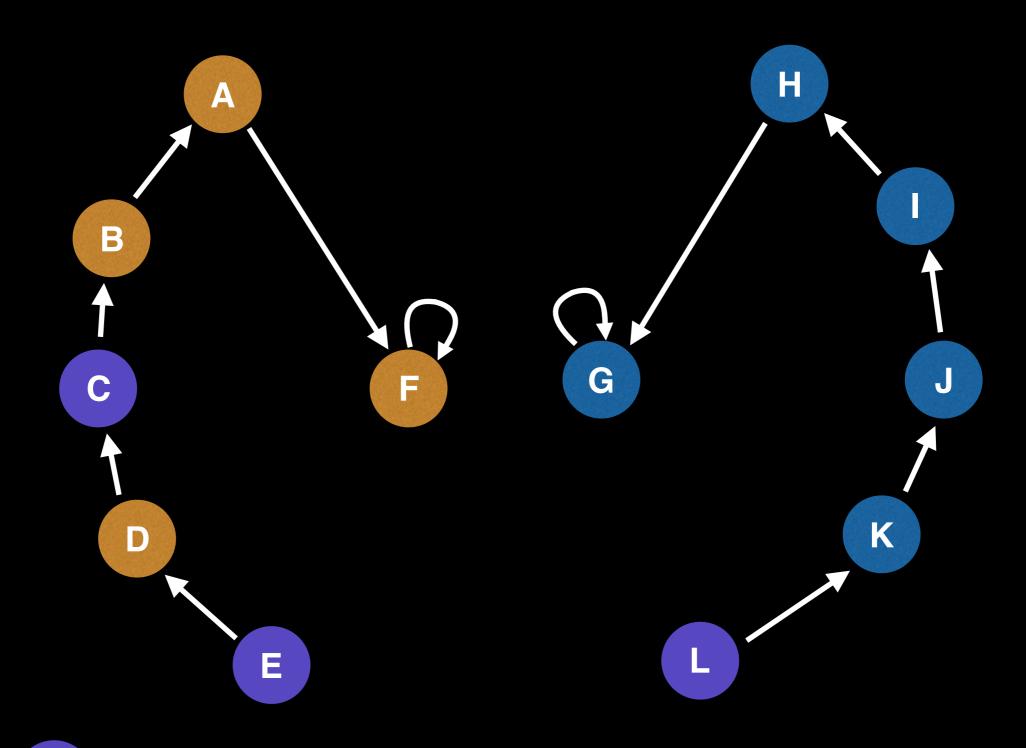
# Last Video: Union and Find Operations

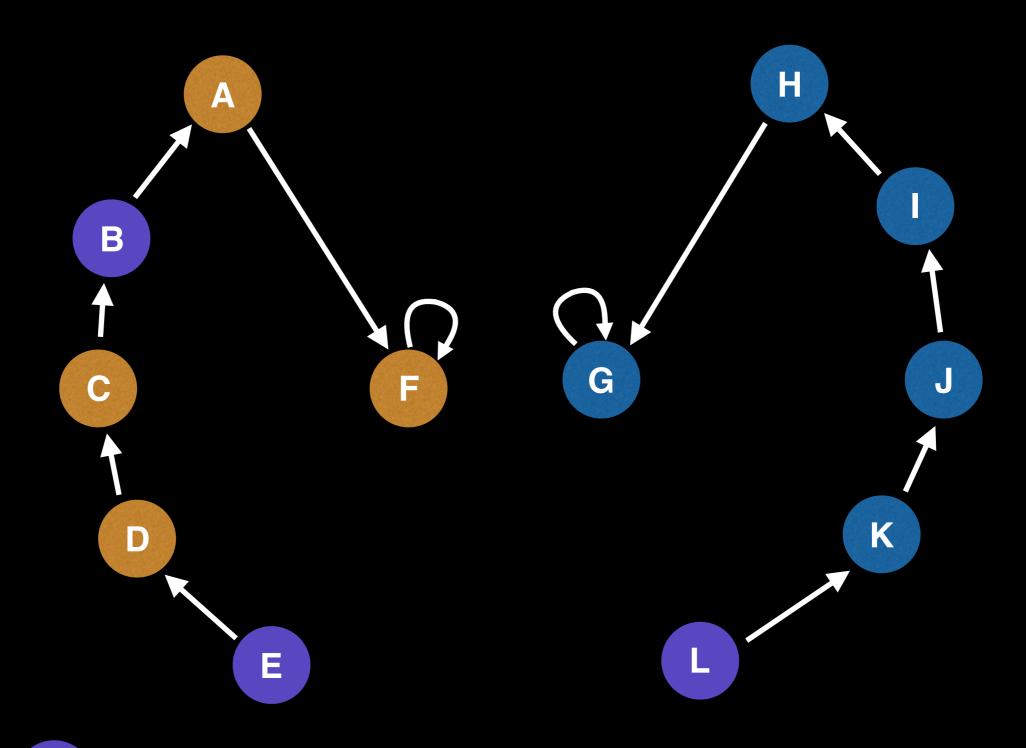


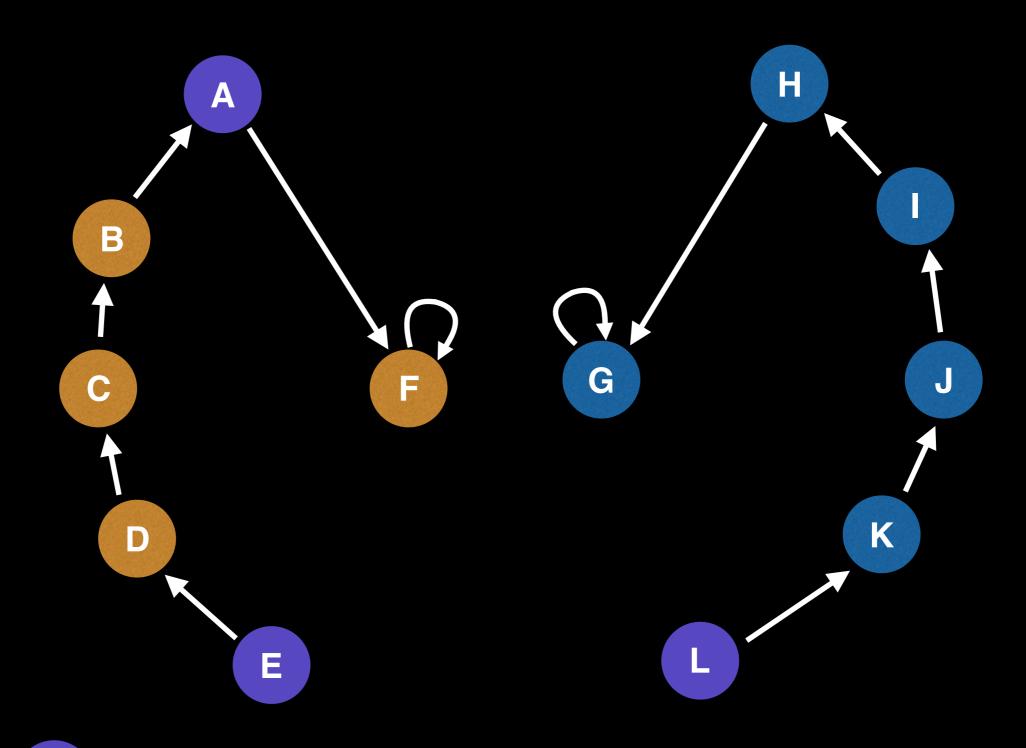
Operation: Take the union of E and L

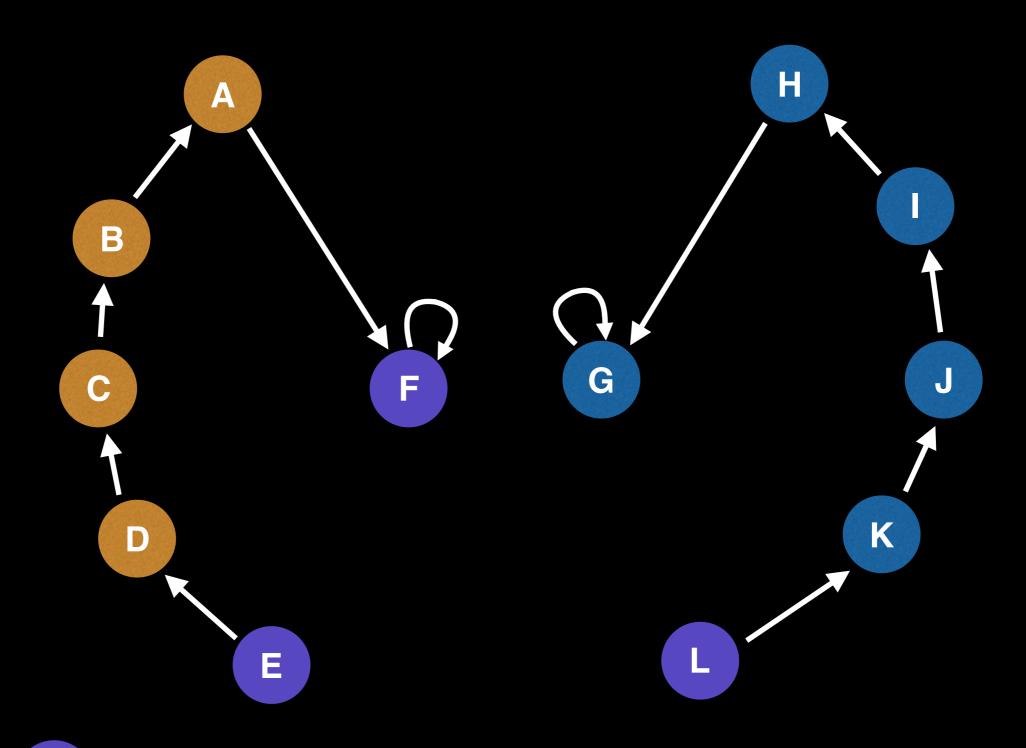


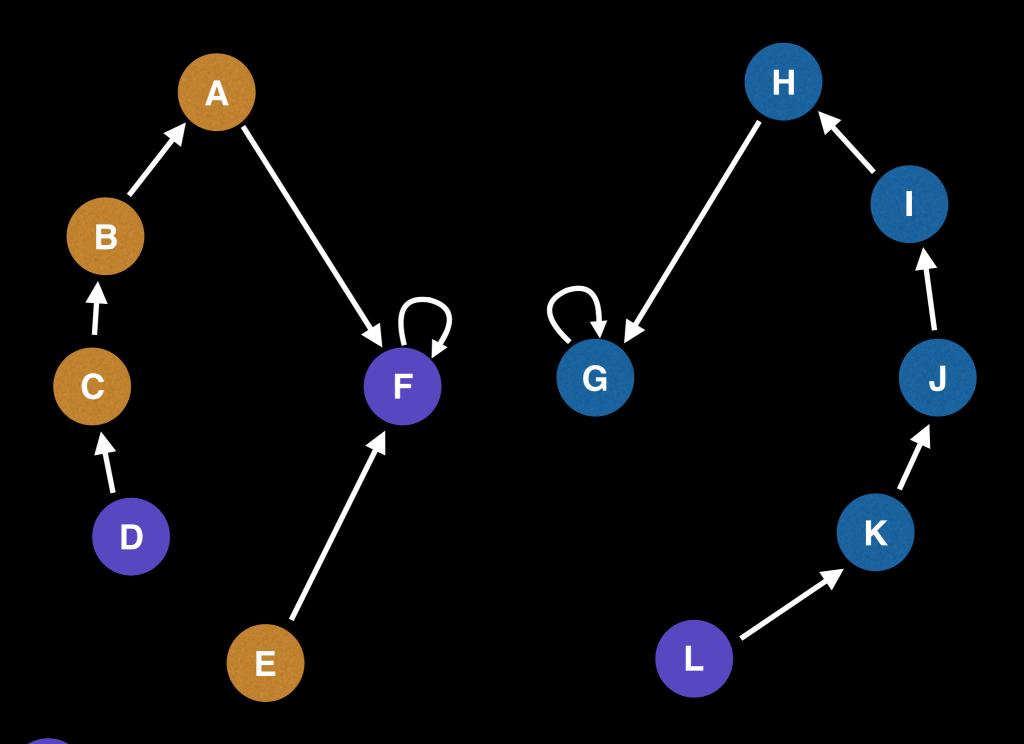


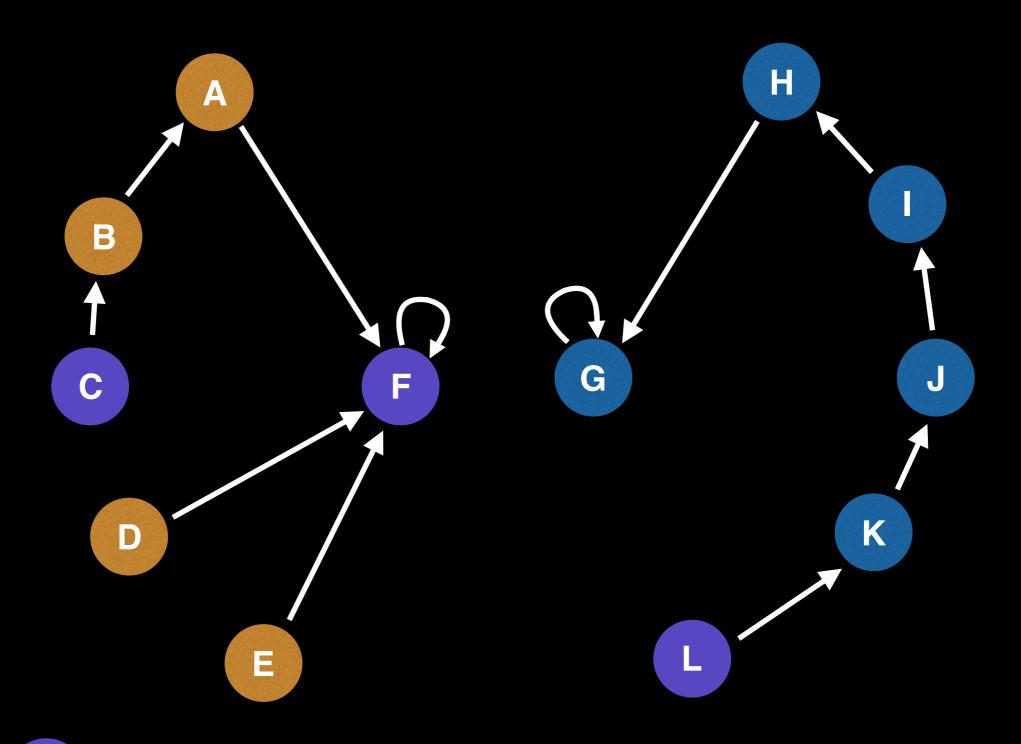


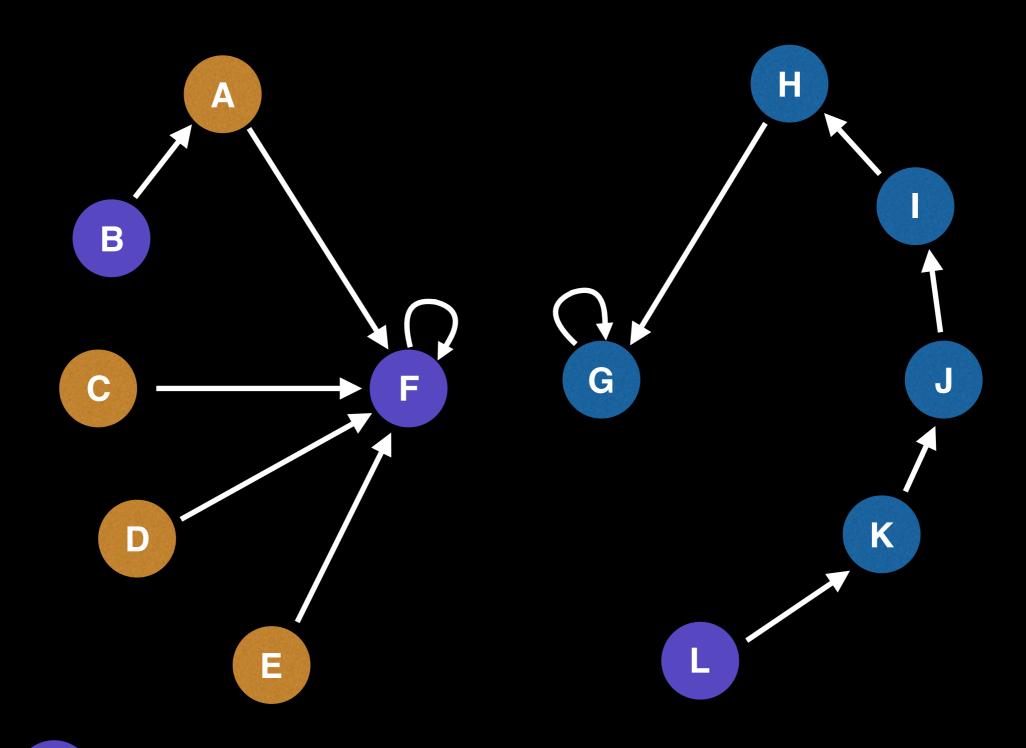


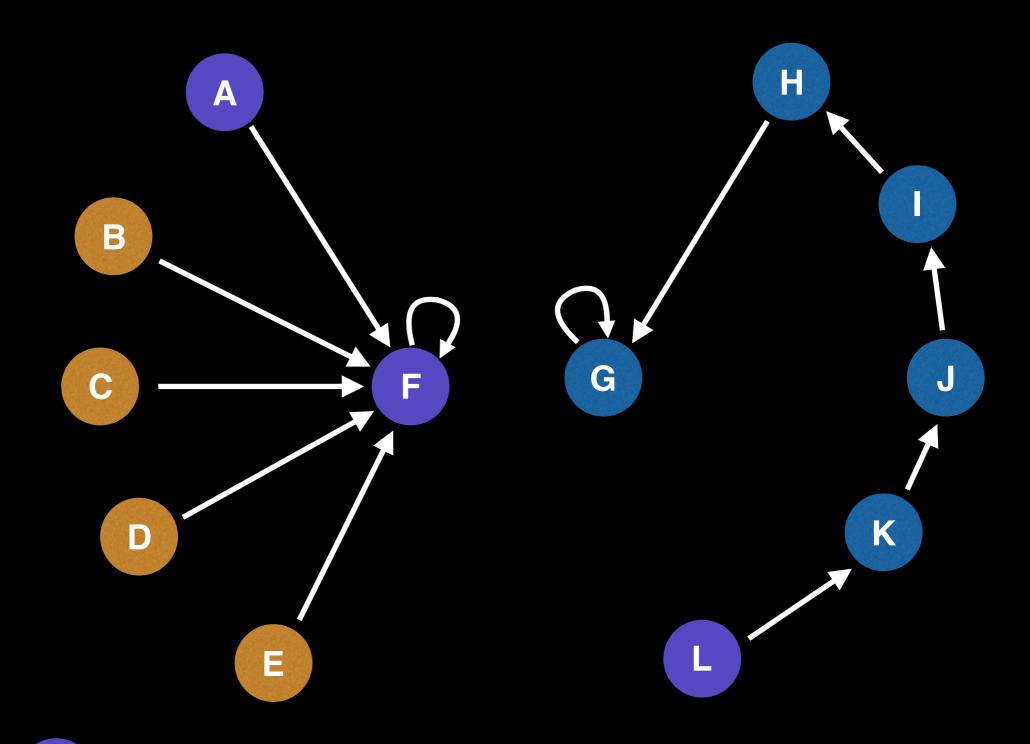


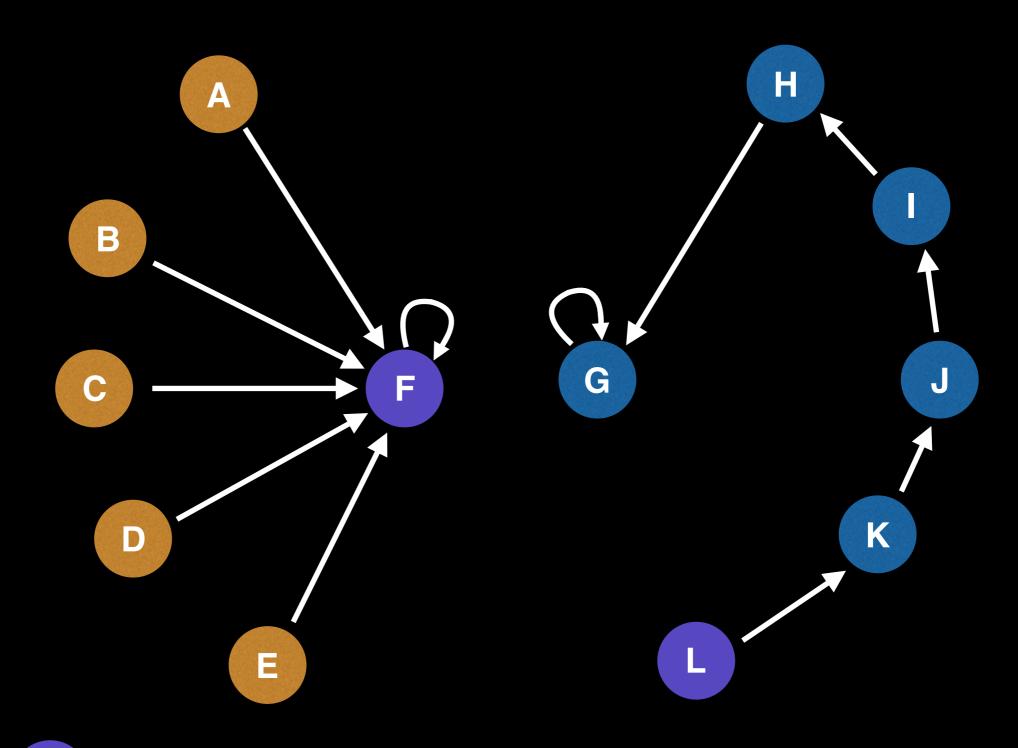


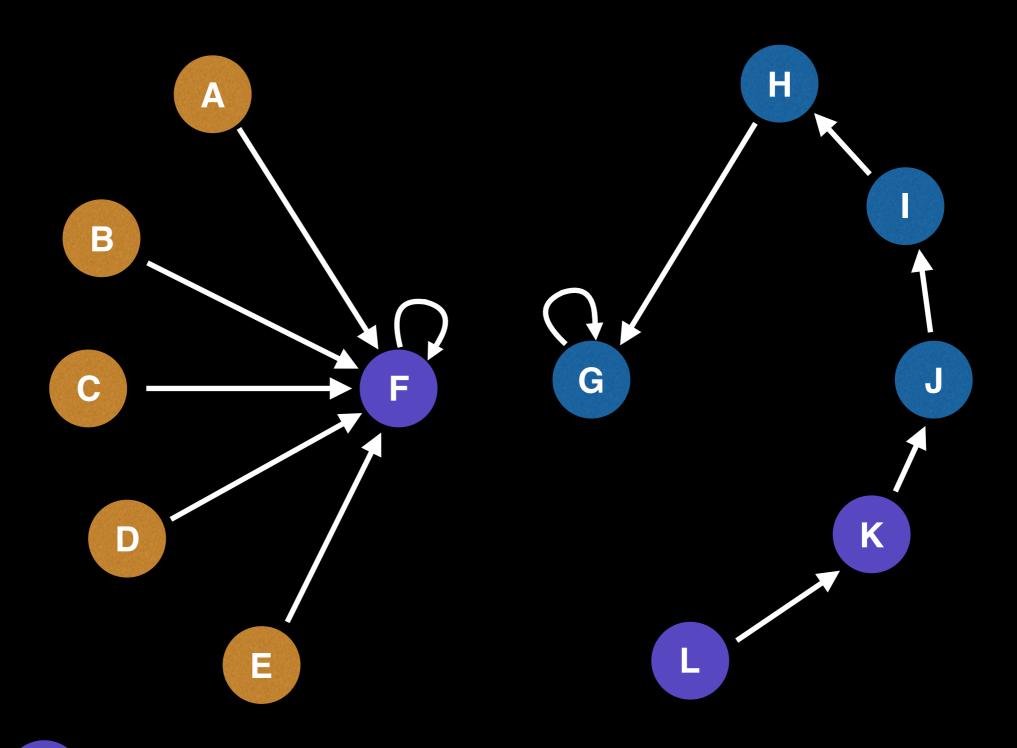


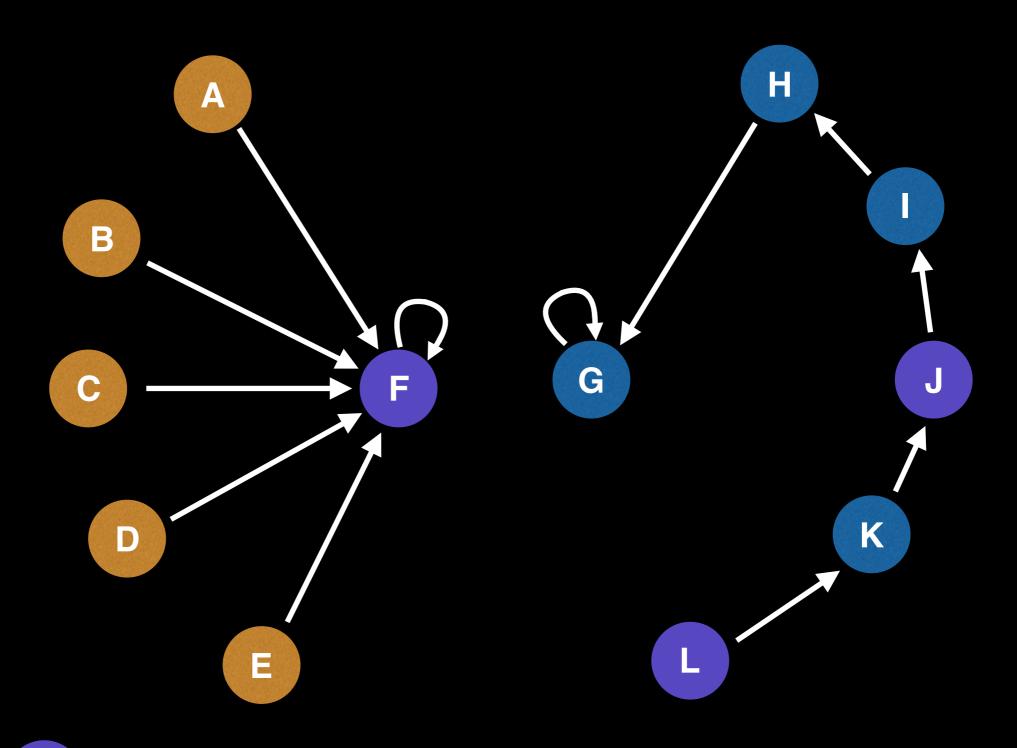


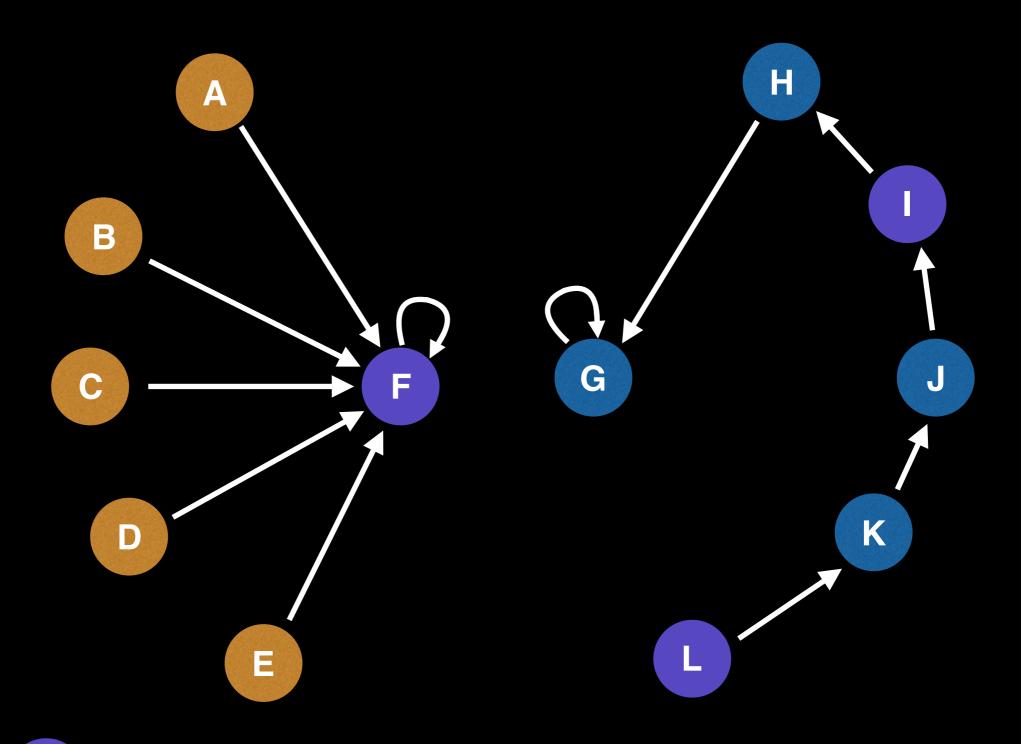


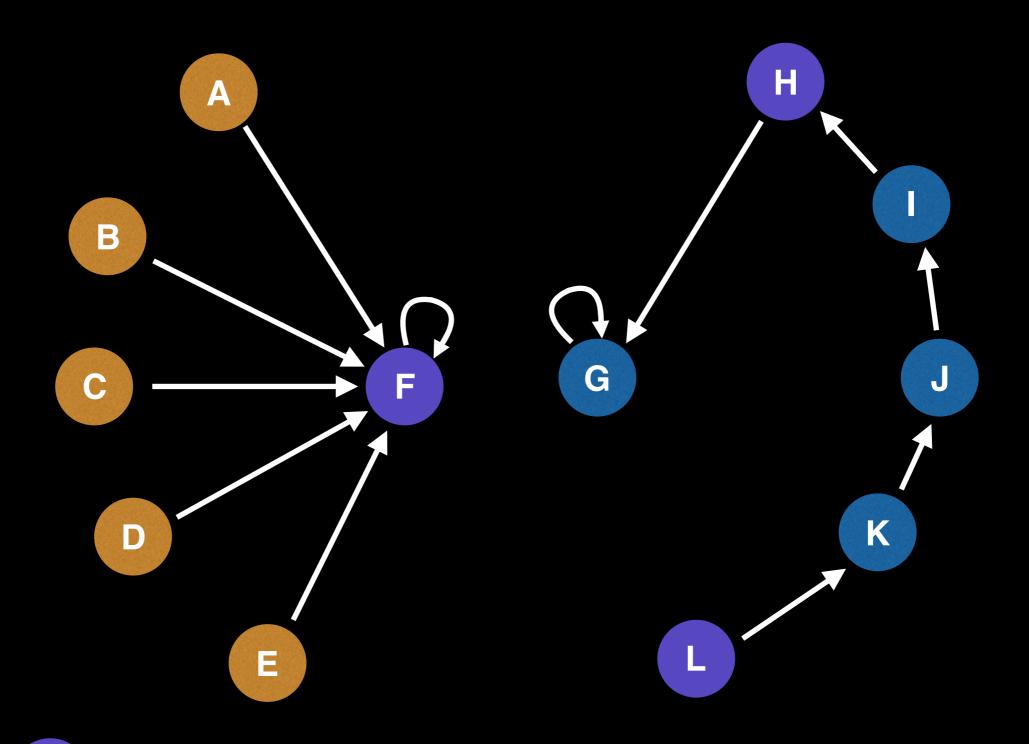


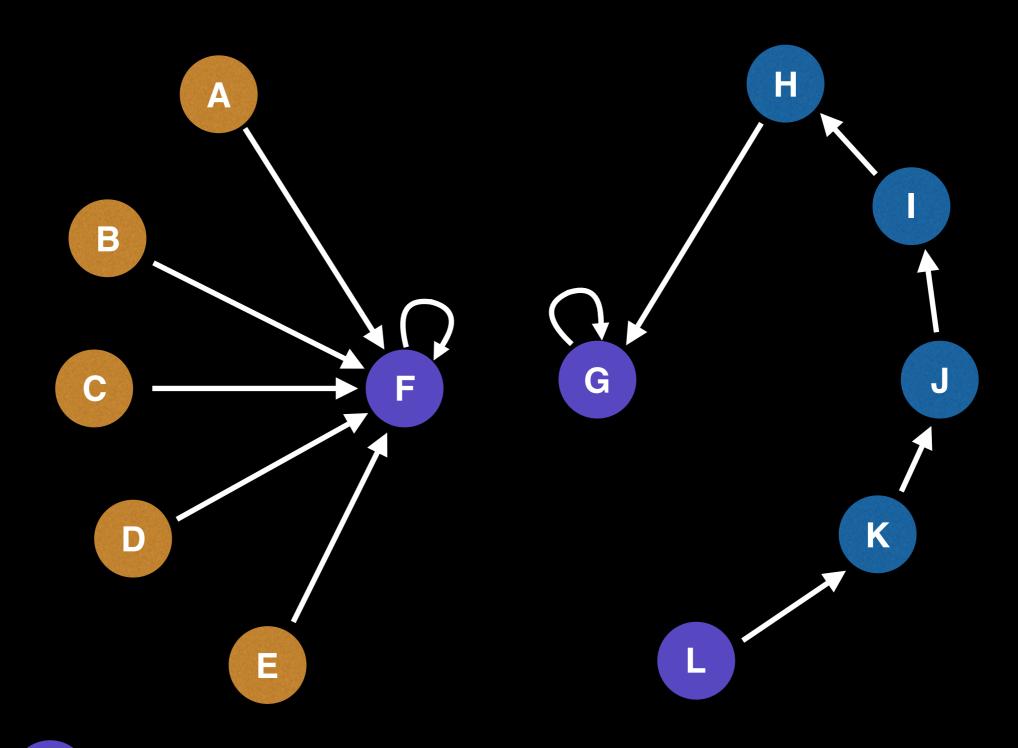


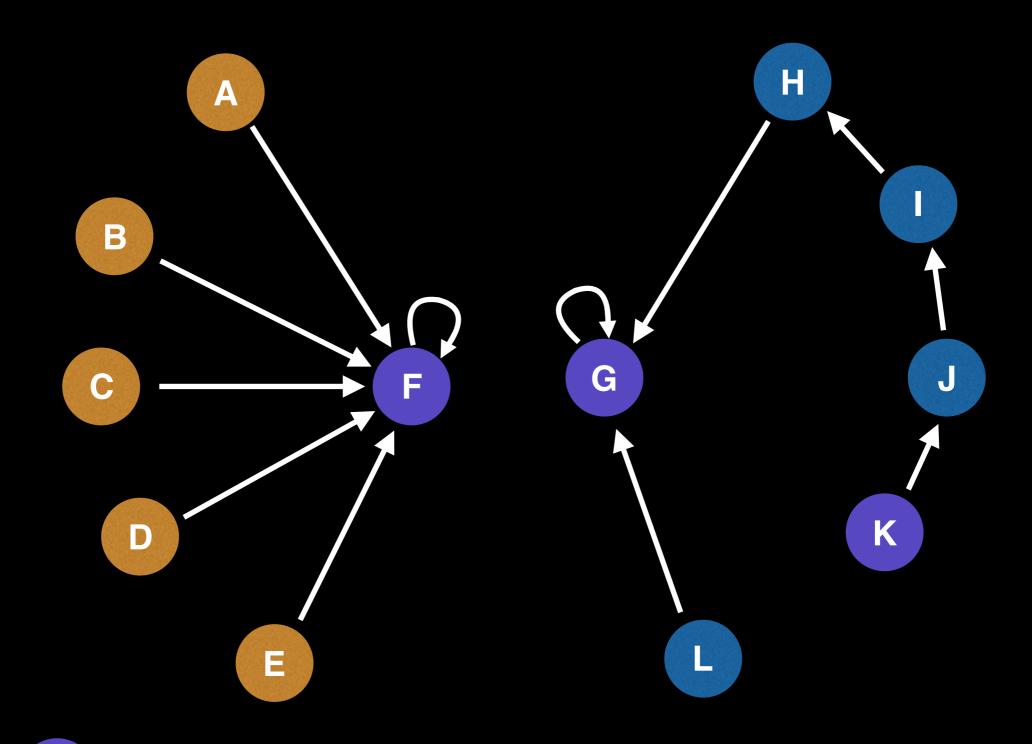


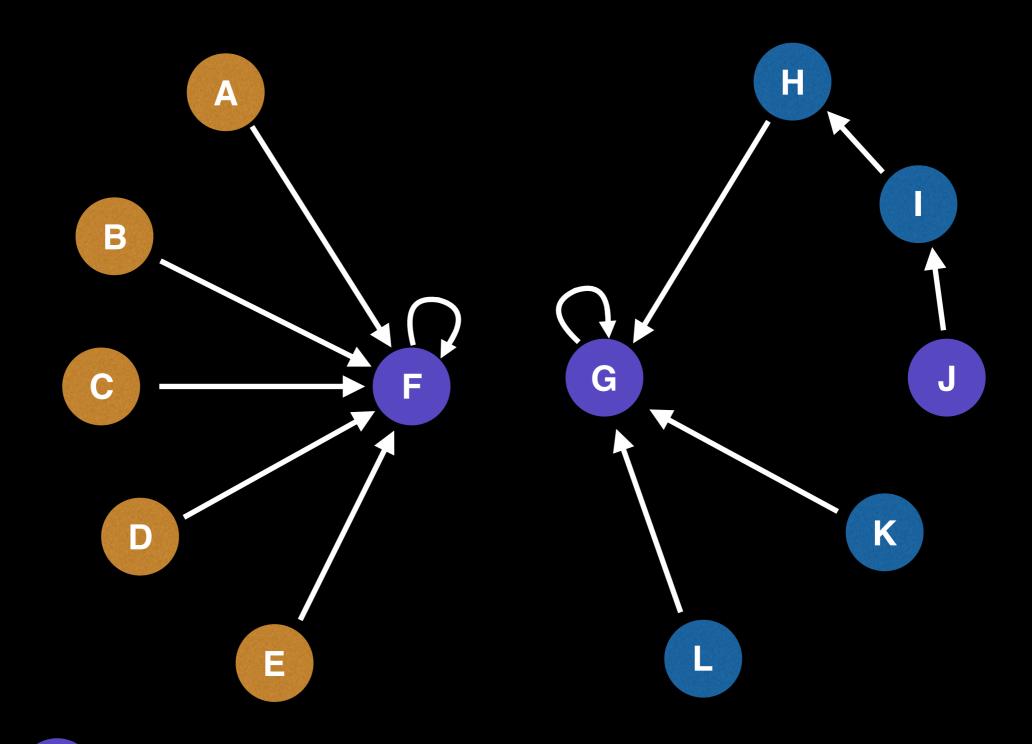


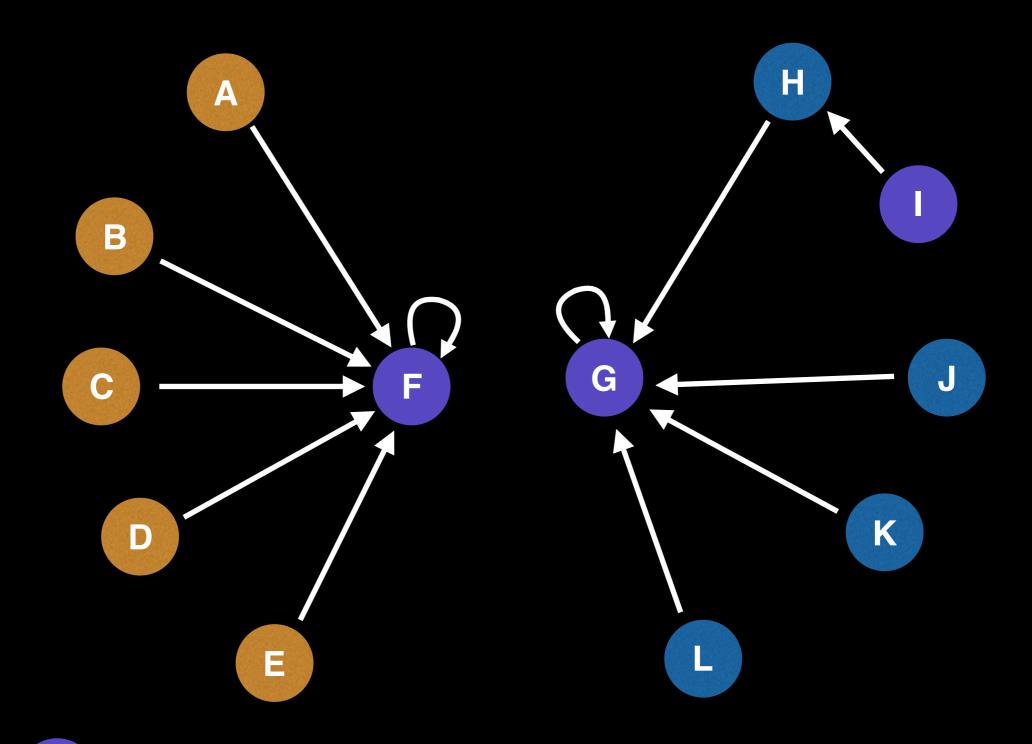


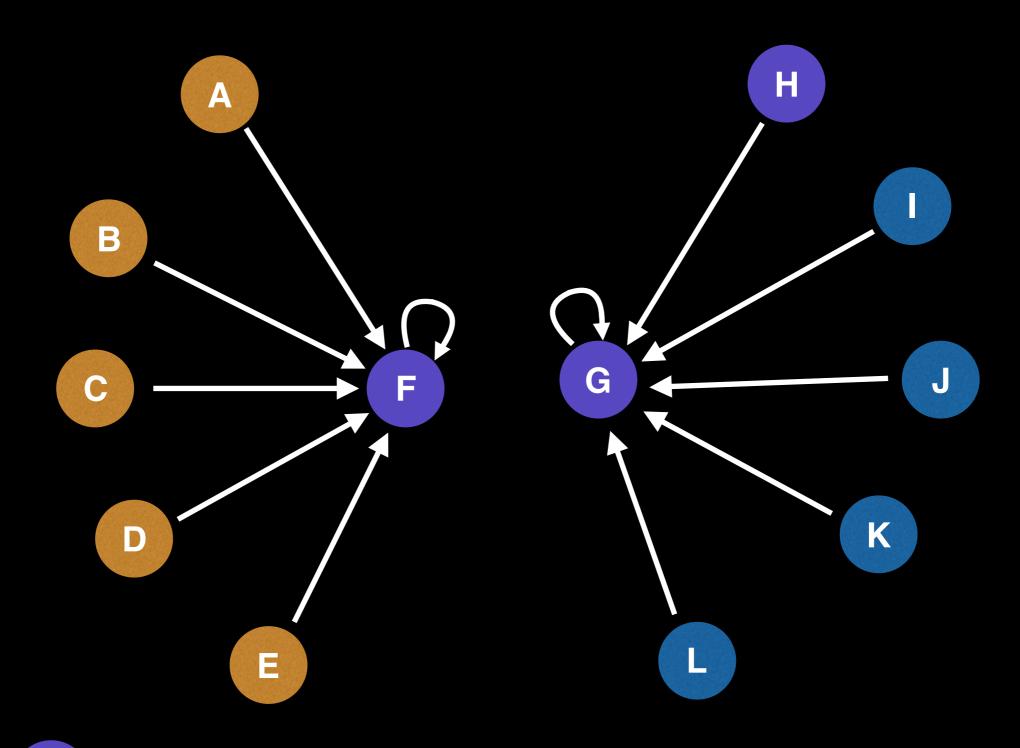


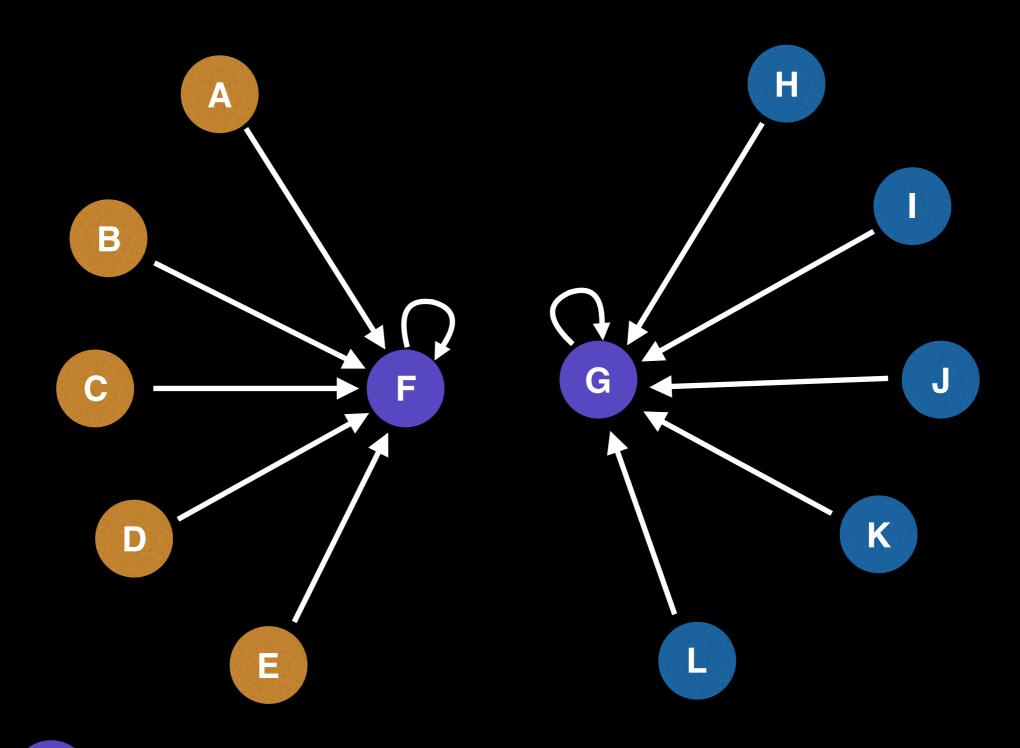


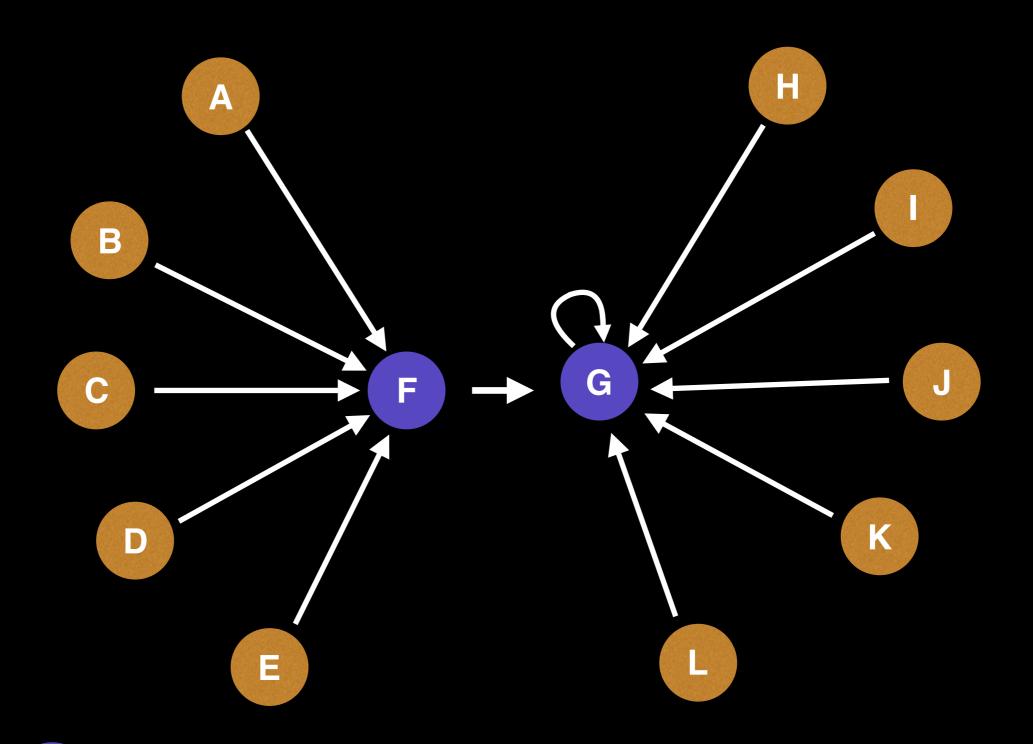


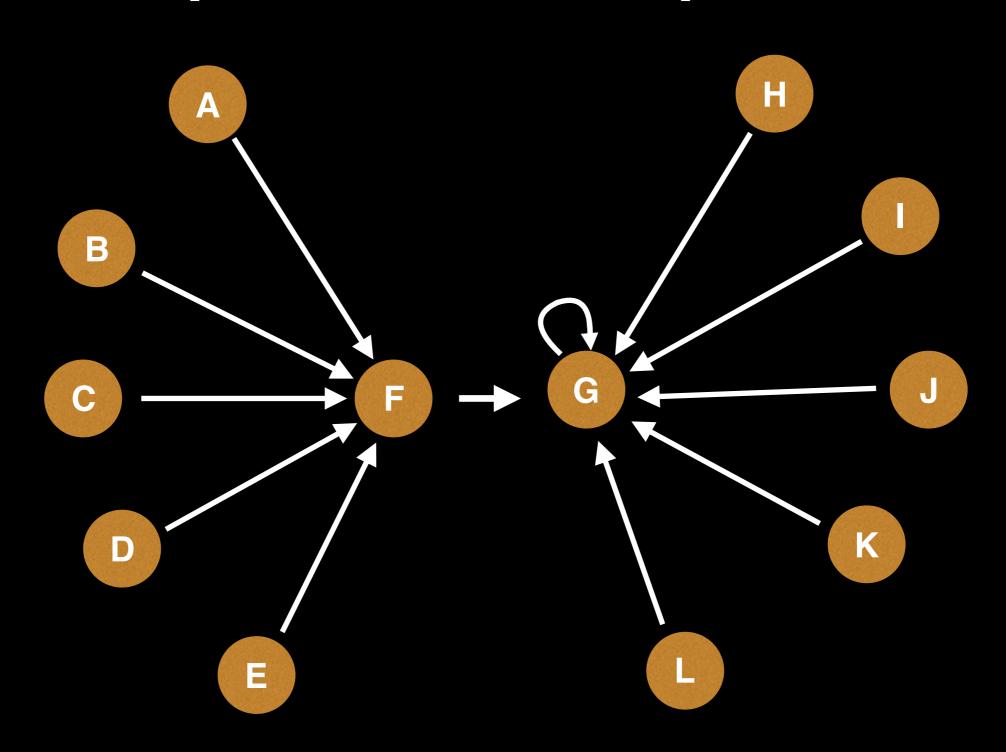


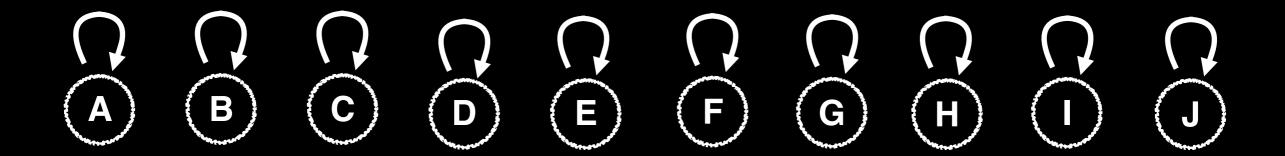






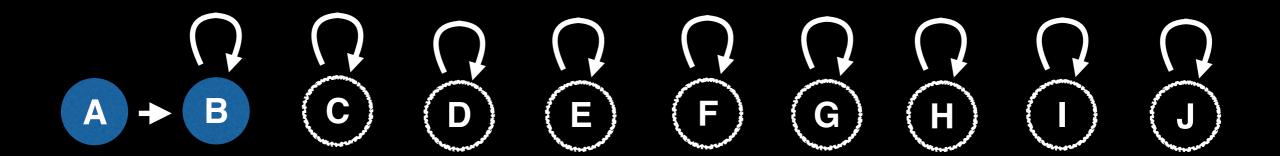






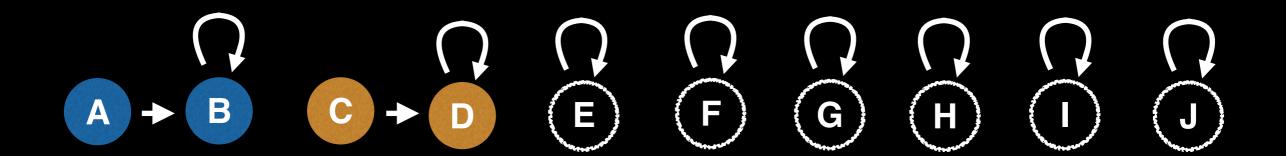
#### <u>Instructions</u>:

```
Union(A,B)
Union(J,G)
Union(C,D)
Union(E,F)
Union(E,F)
Union(G,H)
Union(G,B)
Union(I,J)
```



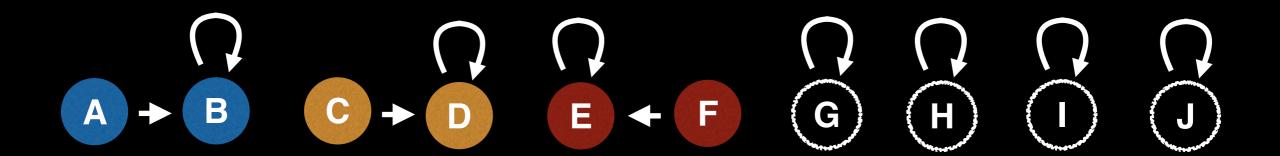
#### Instructions:

Union(A,B)
Union(J,G)
Union(C,D)
Union(E,F)
Union(E,F)
Union(G,H)
Union(G,B)
Union(I,J)



#### **Instructions**:

<pre>Union(A,B) Union(C,D) Union(E,F) Union(G,H) Union(I,J)</pre>	Union(J,G) Union(H,F) Union(A,C) Union(D,E) Union(G,B)
OHITOH(I,J)	Union(I,J)



#### <u>Instructions</u>:

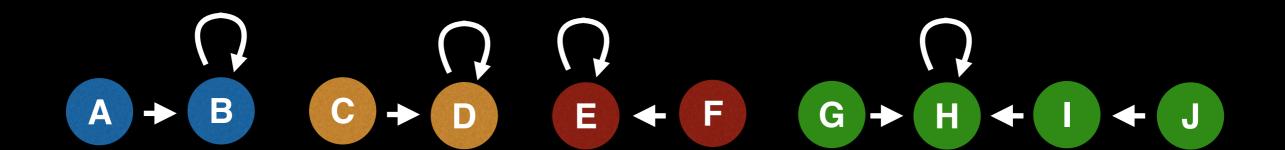
```
Union(A,B)
Union(J,G)
Union(C,D)
Union(C,D)
Union(E,F)
Union(A,C)
Union(D,E)
Union(G,B)
Union(I,J)
```



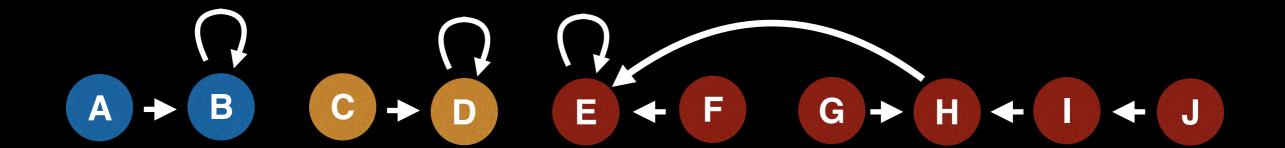
Union(C,D) Union(E,F) Union(G,H) Union(T,1)	<pre>Union(H,F) Union(A,C) Union(D,E) Union(G,B) Union(T,T)</pre>
	Union(I,J)



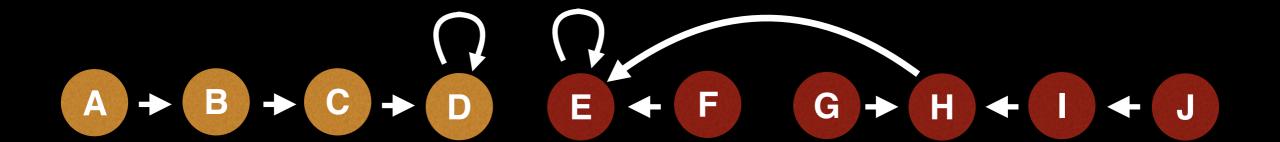
<pre>Union(A,B) Union(C,D) Union(E,F) Union(G,H) Union(I,J)</pre>	Union(J,G) Union(H,F) Union(A,C) Union(D,E) Union(G,B)
Uniton(I,J)	Union(I,J)



Union(C,D) Union(E,F) Union(G,H) Union(T,1)	Jnion(H,F) Jnion(A,C) Jnion(D,E) Jnion(G,B) Jnion(I,J)
	) IITOII(T, J)

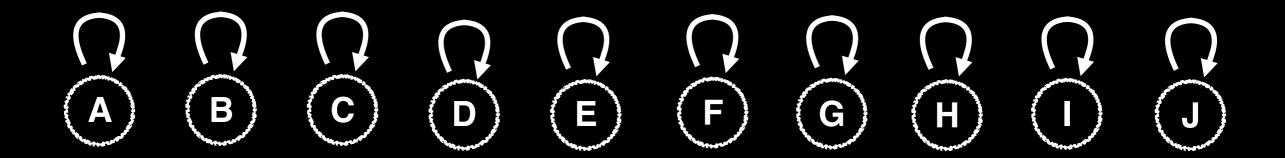


<pre>Union(A,B) Union(C,D) Union(E,F) Union(G,H) Union(I,J)</pre>	Union(J,G) Union(H,F) Union(A,C) Union(D,E) Union(G,B)
OHITOH(I,J)	Union(I,J)

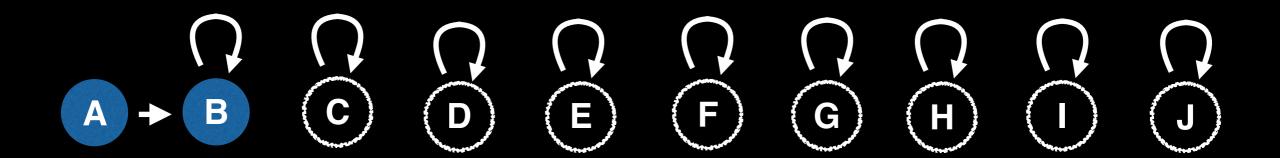


<pre>Union(A,B) Union(C,D) Union(E,F) Union(G,H) Union(I,J)</pre>	Union(J,G) Union(H,F) Union(A,C) Union(D,E) Union(G,B)
OHITOH(I,J)	Union(I,J)

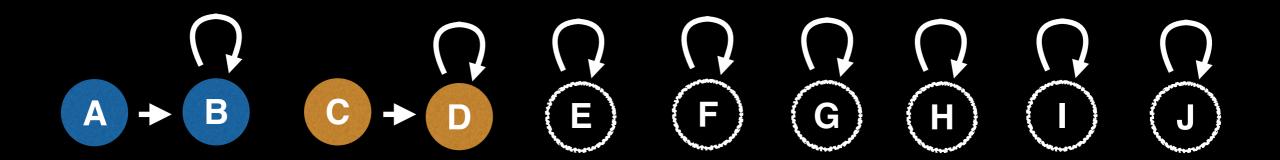
<pre>Union(A,B) Union(C,D) Union(E,F) Union(G,H) Union(I,J)</pre>	Union(J,G) Union(H,F) Union(A,C) Union(D,E) Union(G,B)
OHITOH(I,J)	Union(I,J)



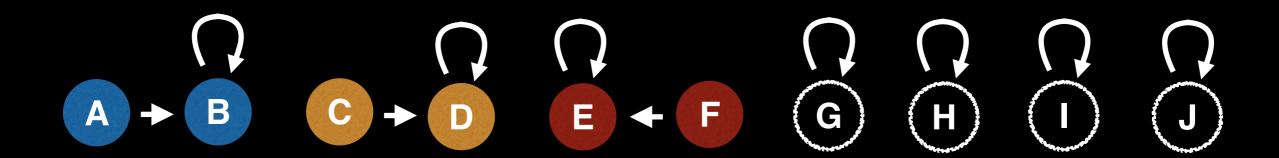
```
Union(A,B)
Union(J,G)
Union(C,D)
Union(E,F)
Union(G,H)
Union(G,H)
Union(G,B)
Union(I,J)
```



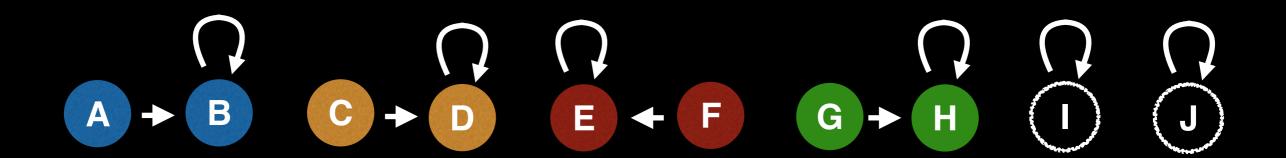
```
Union(A,B)
Union(J,G)
Union(C,D)
Union(E,F)
Union(G,H)
Union(G,H)
Union(G,B)
Union(I,J)
```



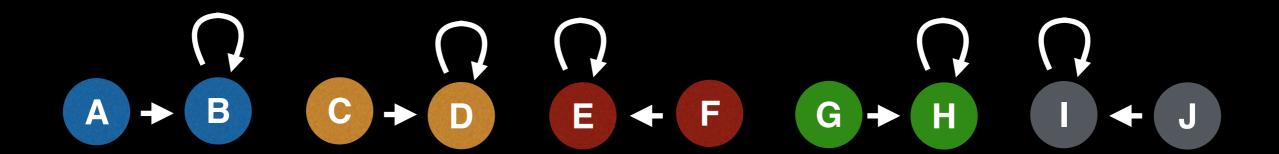
```
Union(A,B)
Union(J,G)
Union(C,D)
Union(E,F)
Union(G,H)
Union(G,H)
Union(G,B)
Union(I,J)
```



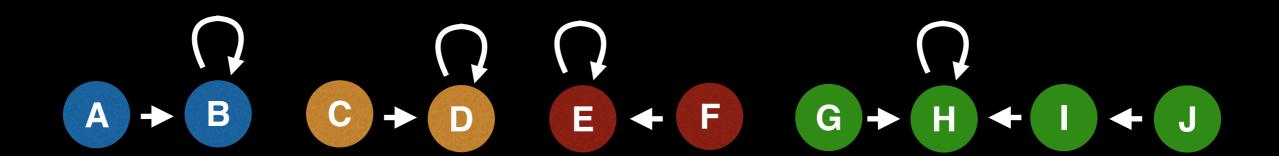
#### **Instructions:**



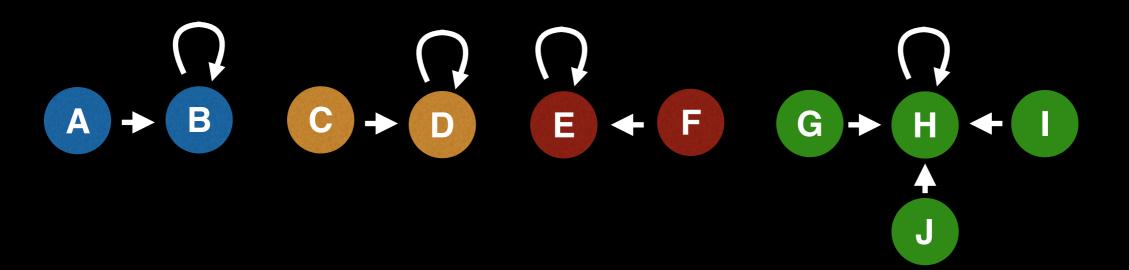
#### Instructions:



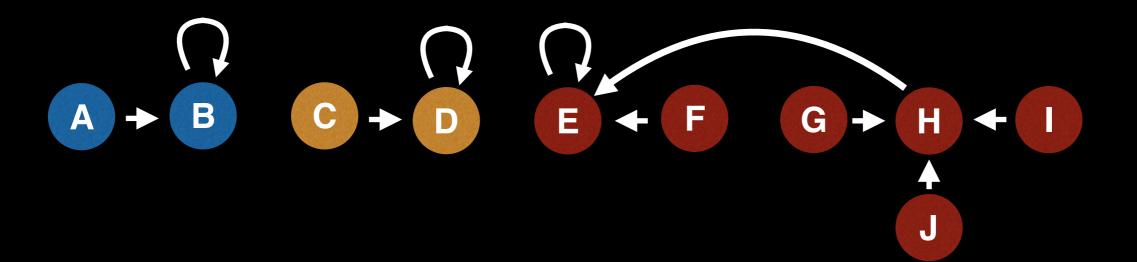
#### **Instructions:**



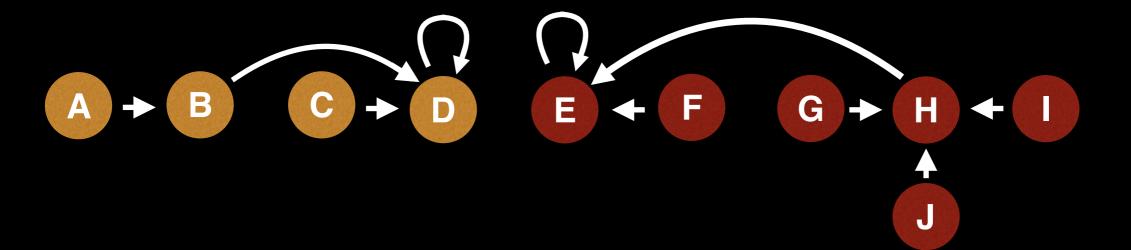
#### **Instructions:**



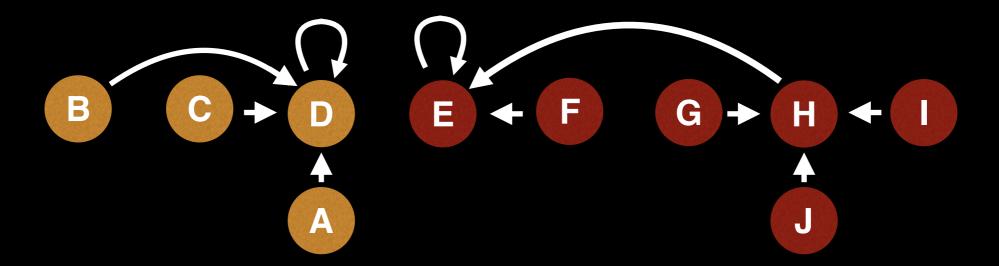
#### <u>Instructions</u>:



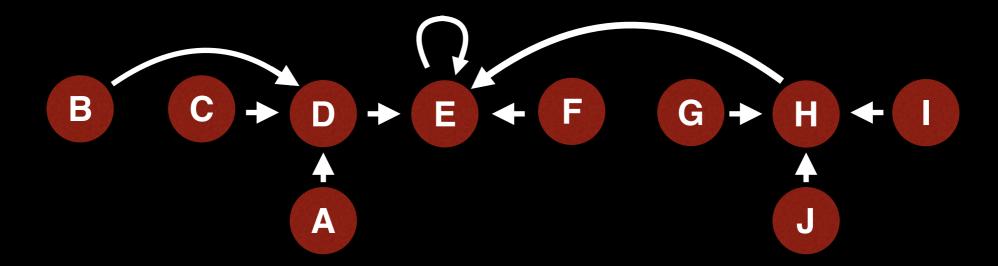
#### **Instructions:**



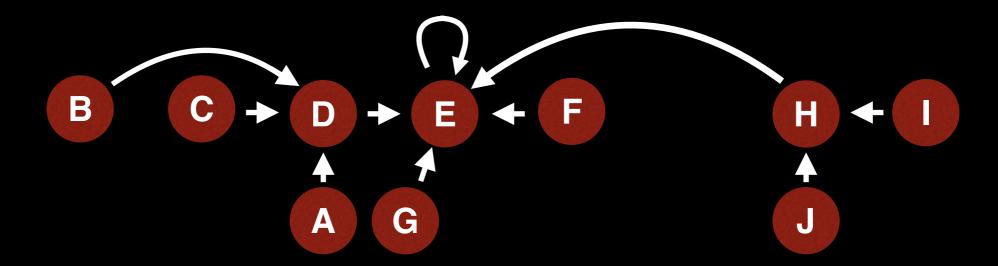
on(J,G) on(H,F) on(A,C) on(D,E) on(G,B) on(I,J)



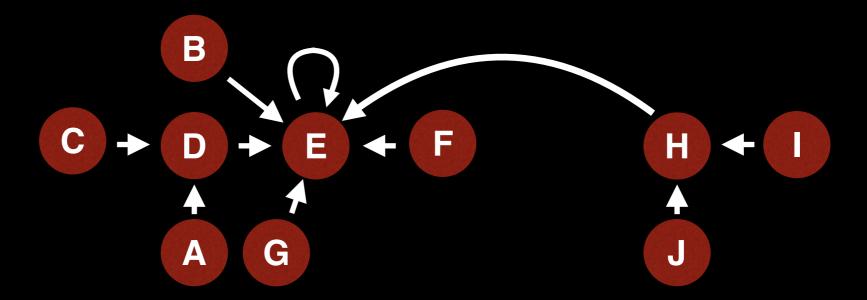
#### Instructions:



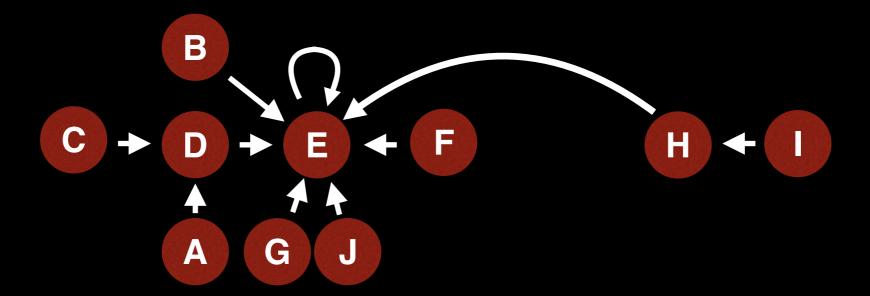
#### **Instructions:**



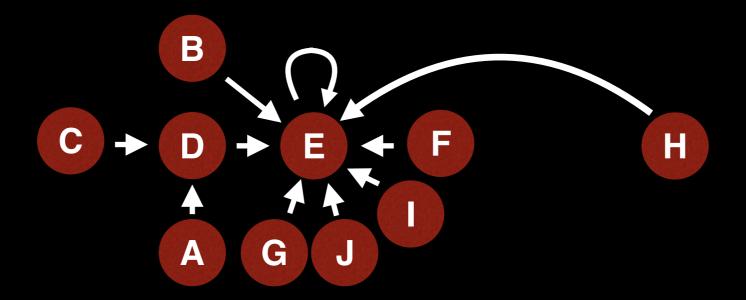
#### **Instructions:**



<pre>nion(J,G) nion(H,F) nion(A,C) nion(D,E) nion(G,B) nion(I,J)</pre>



#### **Instructions:**



<pre>Union(A,B) Union(C,D) Union(E,F) Union(G,H) Union(I,J)</pre>	Union(J,G) Union(H,F) Union(A,C) Union(D,E) Union(G,B)
Union(I,J)	Union(I,J)

# Source Code in the next video

Implementation source code and tests
 can all be found at the following link:
 github.com/williamfiset/data-structures

# Union Find Source Code

William Fiset

# Source Code Link

Implementation source code
and tests can all be found
 at the following link:

github.com/williamfiset/data-structures

NOTE: Make sure you have understood the previous video sections explaining how a Union Find works before continuing!