

▢ **Overview of SHA-256 Hashing Process for Input "red block blue"**

- The input string
- The explanation covers the

▢ **Step 1: ASCII to Binary Conversion**

- Each character in the input is converted to its
- For the 12 characters in "red block blue", this results in a
- These bits are concatenated into one long binary string.
- The bits are then

▢ **Step 2: Pre-processing and Padding**

- SHA-256 requires input length to be a
- Current input length:
- Round up to nearest multiple of 512 →
- Padding procedure:
- Final padded input length:

Step	Bit Length	Description
Original input	96	ASCII binary of "red block blue"
Append '1' bit	+1	Single '1' bit appended
Append zeros	+440	Padding zeros to reach 448 bits
Append length (64-bit)	+64	Binary representation of 96
Total	512	Padded input length

▮ Step 3: Splitting into Blocks and Words

- The padded input is split into
- Since input is exactly 512 bits, there is
- Each 512-bit block is split into
- These words are labeled

⚙ Step 4: Initialization of Hash Values (h0 to h7)

- Initialize
- These initial values are derived from the
- Purpose: To ensure
- Example:
- These constants are fixed and standardized.

▮ Step 5: Constants k0 to k63

- 64 constants
- Derived from the
- These constants are fixed and standardized.
- Examples:

▮ Step 6: Message Schedule Preparation (w0 to w63)

- Prepare a
- First 16 words:
- Remaining words (w16 to w63) are computed iteratively using the formula:

$$[w_t = \sigma_1(w_{t-2}) + w_{t-7} + \sigma_0(w_{t-15}) + w_{t-16} \bmod 2^{32}]$$

- Where:

▮ Explanation of (σ_0) and (σ_1) Functions

- For a 32-bit word (x):

Function	Operations
$(\sigma_0(x))$	$((x \text{ ROTR } 7) \oplus (x \text{ ROTR } 18) \oplus (x \text{ SHR } 3))$
$(\sigma_1(x))$	$((x \text{ ROTR } 17) \oplus (x \text{ ROTR } 19) \oplus (x \text{ SHR } 10))$

- ROTR n

- SHR n
- (\oplus) denotes

▮ Step 7: Compression Loop (t = 0 to 63)

- Initialize working variables (a, b, c, d, e, f, g, h) with initial hash values (h₀) to (h₇).
- For each iteration (t) from 0 to 63:

Step	Calculation
(T ₁)	$(h + \Sigma_1(e) + \text{Ch}(e, f, g) + k_t + w_t)$
(T ₂)	$(\Sigma_0(a) + \text{Maj}(a, b, c))$
Update	$(h = g), (g = f), (f = e), (e = d + T_1), (d = c), (c = b), (b = a), (a = T_1 + T_2)$

- Where:

Function	Description
$(\Sigma_0(x))$	$((x \text{ ROTR } 2) \oplus (x \text{ ROTR } 13) \oplus (x \text{ ROTR } 22))$
$(\Sigma_1(x))$	$((x \text{ ROTR } 6) \oplus (x \text{ ROTR } 11) \oplus (x \text{ ROTR } 25))$
Ch(x,y,z)	Choose function: bitwise selection based on bits of (x) to choose bits from (y) or (z)
Maj(x,y,z)	Majority function: bitwise majority of bits among (x, y, z)

▮ Details of Choose (Ch) and Majority (Maj) Functions

- Choose (Ch)
- Majority (Maj)

▮ Example Calculation for (w_{16})

- $(w_{16} = \Sigma_1(w_{14}) + w_9 + \Sigma_0(w_1) + w_0 \bmod 2^{32})$
- Given many of these (w_i) are zero, the calculation simplifies.
- Bitwise operations and modulo addition ensure (w_{16}) remains 32 bits.

▮ Step 8: Final Hash Value Update

- After completing all 64 rounds, update the hash values:

[h_i = h_i + working variable_i \square for i=0 \cdots 7]

- This produces the final

Step 9: Output

- Concatenate the eight 32-bit words to form the
- Output is typically represented in
- For input "red block blue", the final SHA-256 hash is a

Summary Table of Key Components

Component	Description
Input	"red block blue" (12 characters, 96 bits ASCII)
Padding	Append '1' bit, zeros, and 64-bit length encoding to reach 512 bits
Blocks	1 block of 512 bits
Words	16 initial 32-bit words (m0 to m15), extended to 64 words (w0 to w63)
Initial Hash Values (h0-h7)	Derived from fractional parts of square roots of first 8 primes
Constants (k0-k63)	Derived from fractional parts of cube roots of first 64 primes
Functions	(\sigma_0, \sigma_1, \Sigma_0, \Sigma_1, Ch, Maj)
Compression Rounds	64 iterations updating working variables and hash values
Final Output	256-bit hash (eight 32-bit words concatenated), shown in hexadecimal

⚠ Important Notes

- All additions are
- Bitwise operations (rotations, shifts, XOR) are fundamental to the transformations.
- The use of prime number roots ensures
- The process is deterministic: same input → same output.
- The example input is simple, so only one 512-bit block is processed.

This detailed breakdown covers the entire SHA-256 hashing process as applied to the input "red block blue," including all intermediate steps, constants, and functions involved.

Here is a cleanly formatted version of your Markdown text, using best practices for section breaks, headers, and tables:

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- Since input is exactly 512 bits, there is
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- 64 constants
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Step 6: Message Schedule Preparation (w0 to w63)

- Prepare a
- First 16 words:
- Remaining words (w16 to w63) are computed iteratively using:

$$w_t = \sigma_1(w_{t-2}) + w_{t-7} + \sigma_0(w_{t-15}) + w_{t-16} \pmod{2^{32}}$$

- Where:

Explanation of (σ0) and (σ1) Functions

- For a 32-bit word (x):

Function	Operations
σ0(x)	(x ROTR 7) ⊕ (x ROTR 18) ⊕ (x SHR 3)
σ1(x)	(x ROTR 17) ⊕ (x ROTR 19) ⊕ (x SHR 10)

- ROTR n
- SHR n
- (⊕) denotes

Step 7: Compression Loop (t = 0 to 63)

- Initialize working variables (a, b, c, d, e, f, g, h) with initial hash values (h_0) to (h_7).
- For each iteration (t) from 0 to 63:

Step	Calculation
(T1)	$h + \Sigma_1(e) + Ch(e, f, g) + k_t + w_t$
(T2)	$\Sigma_0(a) + Maj(a, b, c)$
Update	$h = g, g = f, f = e, e = d + T_1, d = c, c = b, b = a, a = T_1 + T_2$

- Where:

Function	Description
$\Sigma_0(x)$	$(x \text{ ROTR } 2) \oplus (x \text{ ROTR } 13) \oplus (x \text{ ROTR } 22)$
$\Sigma_1(x)$	$(x \text{ ROTR } 6) \oplus (x \text{ ROTR } 11) \oplus (x \text{ ROTR } 25)$
$\text{Ch}(x, y, z)$	Choose function: bitwise selection based on bits of x to choose from y, z
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Details of Choose (Ch) and Majority (Maj) Functions

- Choose (Ch)
- Majority (Maj)

Example Calculation for w_{16}

- $w_{16} = \sigma_1(w_{14}) + w_9 + \sigma_0(w_1) + w_0 \pmod{2^{32}}$
- Given many of these w_i are zero, the calculation simplifies.
- Bitwise operations and modulo addition ensure w_{16} remains 32 bits.

Step 8: Final Hash Value Update

- After completing all 64 rounds, update the hash values:

```
h_i = h_i + working_variable_i  for i = 0..7
```

- This produces the final

Step 9: Output

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Summary Table of Key Components

Component	Description
Input	"red block blue" (12 characters, 96 bits ASCII)
Padding	Append '1' bit, zeros, and 64-bit length encoding to 512 bits
Blocks	1 block of 512 bits
Words	16 initial 32-bit words (m0 to m15), extended to 64 (w0 to w63)

Component	Description
Initial Hash Values (h0-h7)	Derived from square roots of first 8 primes
Constants (k0-k63)	Derived from cube roots of first 64 primes
Functions	σ_0 , σ_1 , Σ_0 , Σ_1 , Ch, Maj
Compression Rounds	64 iterations updating hash values
Final Output	256-bit hash (eight 32-bit words), shown in hexadecimal

Important Notes

- All additions are
- Bitwise operations (rotations, shifts, XOR) are fundamental to the transformations.
- The use of prime number roots ensures
- The process is deterministic: same input → same output.
- The example input is simple, so only one 512-bit block is processed.

This detailed breakdown covers the entire SHA-256 hashing process as applied to the input "red block blue," including all intermediate steps, constants, and functions involved.

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SHA-256 Hashing Process for Input "red block blue"

Overview

- Input string: "red block blue"
- Explanation covers all major stages of SHA-256, from input to final hash.

Step 1: ASCII to Binary Conversion

- Each character in the input is converted to its ASCII binary representation.
- For the 12 characters in "red block blue", this produces a 96-bit binary string.
- These binary values are concatenated into one long bit sequence.
- The bits are then used for padding.

▮ Step 2: Pre-processing and Padding

- SHA-256 requires input length to be a **multiple of 512 bits**.
- Current input length: 96 bits.
- Round up to 512 bits using SHA-256 padding rules.

Padding procedure:

1. Append 1 bit.
2. Pad with zeros until length = 448 bits.
3. Append 64-bit binary encoding of original length (96).

Step	Bit Length	Description
Original input	96	Binary of "red block blue"
Append 1 bit	+1	Adds a single '1'
Append zeros	+440	Fill with zeros to reach 448 bits
Append length (64-bit)	+64	000 . . . 11000000 (96 in 64-bit binary)
Total	512	Padded input

▮ Step 3: Splitting into Blocks and Words

- Padded input is **512 bits** → only 1 block.
- Each 512-bit block is split into 16 words of 32 bits each.
- These are labeled m_0 to m_{15} .

⚙ Step 4: Initialization of Hash Values

- Initialize eight working variables: h_0 to h_7 .
- These are derived from the **square roots of the first 8 prime numbers**.
- They ensure randomness and standardization.

▮ Step 5: Constants (k_0 to k_{63})

- 64 constants, derived from **cube roots of the first 64 primes**.
- They are fixed, predefined values.

▮ Step 6: Message Schedule Preparation

- Extend the 16 original words into 64 words (w_0 – w_{63}).
- For $t \geq 16$:

$$w_t = \sigma_1(w_{t-2}) + w_{t-7} + \sigma_0(w_{t-15}) + w_{t-16} \pmod{2^{32}}$$

▮ σ Functions

For a 32-bit word x :

Function	Formula
$\sigma_0(x)$	$(x \text{ ROTR } 7) \oplus (x \text{ ROTR } 18) \oplus (x \text{ SHR } 3)$
$\sigma_1(x)$	$(x \text{ ROTR } 17) \oplus (x \text{ ROTR } 19) \oplus (x \text{ SHR } 10)$

▮ Step 7: Compression Loop (64 rounds)

- Initialize working variables a, b, c, d, e, f, g, h with hash values.
- For each round t (0–63):

Step	Formula
T_1	$h + \Sigma_1(e) + Ch(e, f, g) + k_t + w_t$
T_2	$\Sigma_0(a) + Maj(a, b, c)$
Update	$h = g, g = f, f = e, e = d + T_1, d = c, c = b, b = a, a = T_1 + T_2$

Functions:

Function	Description
$\Sigma_0(x)$	$(x \text{ ROTR } 2) \oplus (x \text{ ROTR } 13) \oplus (x \text{ ROTR } 22)$
$\Sigma_1(x)$	$(x \text{ ROTR } 6) \oplus (x \text{ ROTR } 11) \oplus (x \text{ ROTR } 25)$
$Ch(x, y, z)$	If bit of $x=1 \rightarrow$ choose y , else z
$Maj(x, y, z)$	Majority vote of bits among x, y, z

▮ Example Expansion for w_{16}

$$w_{16} = \sigma_1(w_{14}) + w_9 + \sigma_0(w_1) + w_0 \pmod{2^{32}}$$

- Many initial values are zero, simplifying calculations.

▮ Step 8: Final Hash Value Update

After 64 rounds:

$$h_i = h_i + workingVar_i \quad (i = 0..7)$$

Eight updated 32-bit words are combined.

▮ Step 9: Output

- Concatenate all eight 32-bit words → **256-bit hash**.
- Represent in **hexadecimal** format.
- For "red block blue", the SHA-256 produces a fixed unique hash.

▮ Summary of Key Components

Component	Description
Input	"red block blue" (96 bits ASCII)
Padding	+1 bit + zeros + 64-bit length → 512 bits
Blocks	1 (512-bit block)
Words	16 → extended to 64
Initial Hash Values	Fractional square roots of first 8 primes
Constants	Fractional cube roots of first 64 primes
Functions	$\sigma_0, \sigma_1, \Sigma_0, \Sigma_1, Ch, Maj$
Compression	64 rounds
Output	256-bit hexadecimal hash

⚠ Notes

- All additions are mod 2^{32} .
- Bitwise ops (shift, rotate, XOR) are crucial.
- Prime-root constants ensure cryptographic randomness.
- Deterministic: same input → same output.
- Example here: only one block processed since input is small.

Would you like me to also include the *actual computed SHA-256 hash* of "red block blue" in the final section so the document is complete with output?