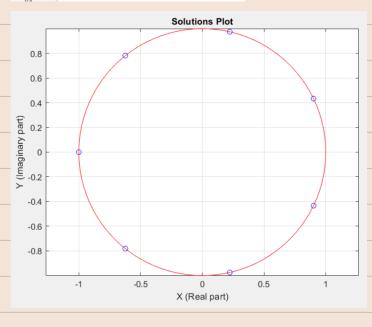
## DAN OTIENO - HW 1

1. (10 points) Write the formula and plot the roots of  $z^7 + 1 = 0$ 

$$Z^{7} = -1$$
following the form  $Z_{K} = e^{j(2k+1)T/n}$ , for  $n = 7$ 
 $Z_{K} = e^{j(2k+1)T/7}$ ;  $K = (0, 1, 2, 3, 4, 5, 6)$ .

## Solutions plotted using Matlab:

```
% CPE 381-01.
           % Homework 1 - Q1.
 4
           % 01/27/2023.
           k = 0:1:6;
           z = \exp(1i*pi.*(2*k+1)/7);
           plot(real(z),imag(z),'bo')
title('Solutions Plot');
9
10
           axis equal
11
           ylabel('Y (Imaginary part)');
xlabel('X (Real part)');
13
14
15
           z1 = abs(z(1));
c = linspace(0,2*pi,100);
16
           hold on
           plot(z1*cos(c),z1*sin(c),'r-')
18
19
```



```
2. (15 points)
                      Represent the following complex numbers in alternative form (polar \leftarrow \rightarrow \{\text{Re,lm}\}\ z=x+iy)
```

a) 
$$1 + j$$

c) 
$$5 e^{j210^{\circ}}$$

Magnitude = 
$$J1^2 + 1^2 = J2$$
.

$$\theta = \tan^{-1}(\frac{9}{x}) = \tan^{-1}(\frac{1}{2}) = \tan^{-1}(1) \approx 0.785$$

$$Z = \sqrt{2}e^{j0.785}$$

Magnitude = 
$$\int 1^2 + (-1)^2 = \int 2$$

B 1-j; 
$$x = 1$$
,  $y = -1$   
Magnitude =  $\int 1^2 + (-1)^2 = \int 2^4$   
 $\theta = tan^{-1} (-1/2) = tan^{-1} (-1) \approx -0.785$ 

$$e^{5e^{j_2(e^{\circ})}}$$
=  $5e^{j(180^{\circ}+30^{\circ})}$  =  $5e^{j_180^{\circ}}$   $e^{j_30^{\circ}}$ 

$$5e^{j180^{\circ}} \cdot e^{j30^{\circ}} = 5(-1) \cdot e^{j30^{\circ}} = -5e^{j30^{\circ}}$$

= 
$$-5\cos(30^\circ) - j5\sin(30^\circ) = -4.33 - j2.5$$

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- 3. (20 points) Use Euler's identity to find trigonometric identities in terms of  $sin(\alpha)$ ,  $sin(\beta)$ ,  $cos(\alpha)$ , and  $cos(\beta)$ :
  - a)  $sin(\alpha + \beta)$
  - b)  $cos(\alpha + \beta)$

Demonstrate all the steps in formula evaluation.

(a) 
$$\sin(\alpha + \beta)$$
:

$$= \underbrace{e^{j(\alpha+\beta)}}_{-e} - \underbrace{e^{-j(\alpha+\beta)}}_{-e} = \underbrace{e^{-e} \cdot e^{-e} \cdot e^{-e}}_{-e}$$

$$= \underbrace{[(\omega s \alpha + j \sin \alpha)(\omega s \beta + j \sin \beta)]}_{-e} - \underbrace{[(\omega s \alpha - j \sin \alpha)(\omega s \beta - j \sin \beta)]}_{-e}$$

(cos of Cosptj Sinp Cosatj Sina Cosp) tj Singlj Sinp

= jens cosa + jena coss + jens cosa + jena coss

$$\frac{b}{a} \cos(\alpha + \beta)$$

$$= e^{j(\alpha+\beta)} + e^{-j(\alpha+\beta)}$$

\* (wsatjsna) (cosptjsnib) = wsacosptjsnib cosatjsnib.

\* (cos & - j sin &) (cos \beta - j sin \beta) =

cos & cos \beta - j sin \beta cos \beta - j sin \beta cos \beta

+ j sin \beta j sin \beta.

Add:

COS & COSB + j sings cosa + j singl cosp + j sind j singl cosa CosB - j sings cosa - j singl cosp + j sind j singl cosa CosB - j singl cosa - j singl cosp + j sind j singl cosa cosp + j sind c

= 2 Cos & Cos B - 2 (Sind Sin B)

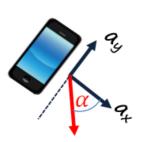
= & ((cosd cosp) - (sind sin b))

= (cosd cosp) - (sind sing)

### 6. (30 points)

Accelerometer with analog output, sensitivity ±2g, and power supply of +3V is used in smartphone to determine orientation of the smartphone according to the figure below.





What are the values of X and Y components [in Volts] for the following positions









a)

X =

Y =

*b)* 

Y =

c) X =

X = Y =

d) X =

Y =

What is the angle of the smartphone if:

Please draw a phone as a part of the solution to avoid confusion.

# Sensitivity: $1g \Rightarrow S = \frac{\sqrt{cc}}{2ange} = \frac{3\sqrt{4g}}{5\sqrt{2g}}$ $= 0.75 \left[\frac{\sqrt{2g}}{3}\right]$

A culevation:

$$A_0 = 0g = 1.5V$$
  
 $A_1 = (+1g) = 1.5V + 0.75 [ \frac{1}{9} \cdot 1g = 2.25V$   
 $A_{-1} = (-1g) = 1.5V + 0.75 [ \frac{1}{9} \cdot (-1g) = 0.75V$ 

$$\begin{array}{c} \text{(a)} \\ \text{(b)} \\ \text{(c)} \\ \text{(c)$$

$$\begin{array}{c} \text{(b)} \\ \text{(c)} \\ \text{(c)$$

$$A \longrightarrow X = 1g = 2.25V$$

$$Y = 0g = 1.5V$$

- Angle of smartphone is:

aueleration 
$$(a_x) = A - A_0$$
  

$$= (1.875V - 1.5V) = 0.5g$$

$$0.75 [7/g]$$

$$(ay) = (0.8505 V - 1.5 V) = -0.866 g$$
  
 $0.75 [V/g]$ 

$$d = tan^{-1} (as/ax) = tan^{-1} (-0.866/0.5)$$

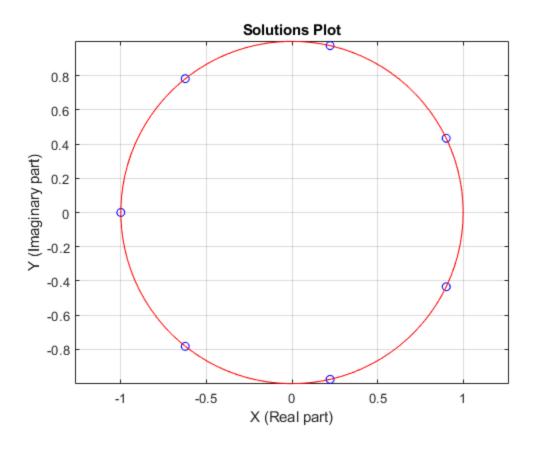
$$\approx [-\pi/3] \approx -60^{\circ}$$

$$(a_x) = (2.1495 V - 1.5V) = 0.866 g$$
  
 $0.75 [V/g]$ 

$$(ay) = (1.875V - 1.5V) = 0.59$$

$$\alpha = \tan^{-1}(0.5/0.866) = \pi/6 = 30^{\circ}$$

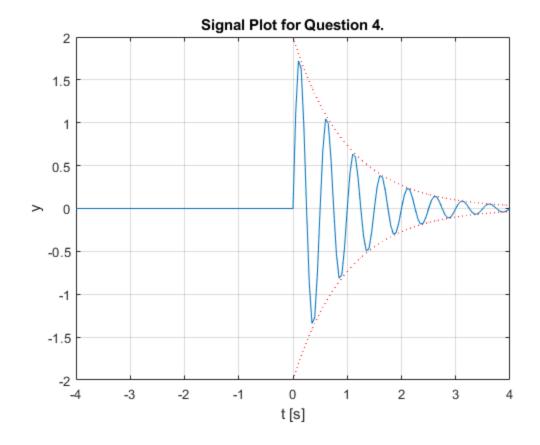
```
% Dan Otieno.
% CPE 381-01.
% Homework 1 - Q1.
% 01/27/2023.
%========%
k = 0:1:6;
z = \exp(1i*pi.*(2*k+1)/7);
%=========%
plot(real(z),imag(z),'bo')
title('Solutions Plot');
axis equal
grid on
ylabel('Y (Imaginary part)');
xlabel('X (Real part)');
z1 = abs(z(1));
c = linspace(0, 2*pi, 100);
hold on
plot(z1*cos(c),z1*sin(c),'r-')
%=========%
```

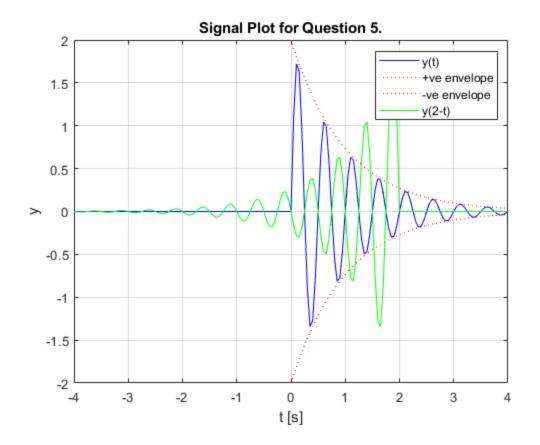


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```
% Dan Otieno.
% CPE 381-01.
% Homework 1 - Q4 & Q5.
% 01/30/2023.
% Both Questions 4 and 5 of Homework 1 are included in this MATLAB script.
%==============================%
            START QUESTION 4: INITIALIZATION.
%========================%
Fs = 20;%<-----Sampling frequency.
Ts = 1/Fs;%<-----Sampling interval.
f = 2;%<-----Signal frequency 2Hz.
tmax = 4;%<------Maximum time.
t = -tmax:Ts:tmax;%<-----Time [s].
N = length(t); %<------Number of elements in Vector.
i0 = round(4*Fs)+1;%<-----Index of time 0 (4s after -4s).
t1 = 0:Ts:4;%<-----Time > 0 [s].
%===============================%
             SIGNAL.
%========================%
A = 2;%<-----Amplitude.
xenv = A*exp(-t1); %<------Envelope A*e^(-t).
x = xenv.*sin(2*pi*f*t1); %<-----Signal for t>0.
y = zeros(1,N);%<-----Initialize all elements to 0.
y(i0:N) = x; %<------Add values from time 0.
SIGNAL PLOT: END QUESTION 4.
figure%<-----New Figure.
plot(t,y,t1,xenv,'r:',t1,-xenv,'r:'), xlabel('t [s]'), ylabel('y'), grid on;
title('Signal Plot for Question 4.');
START QUESTION 5: SIGNAL IS y(2-Tau).
%===============================%
tau = 2;%<-----Tau (delay) = 2[s].
t3 = 0:Ts:(tmax+tau);%<-----New time to include with original plot.
N3 = length(t3); %<----Number of elements.
y3 = zeros(1,N); %<-----Initialize elements to 0.
xenv3 = exp(-t3); %<-----This is our envelope.
x3 = A*xenv3.*sin(2*pi*f.*t3);%<---Signal for t3>0.
y3(1:N3) = fliplr(x3);
%==============================%
             SIGNAL PLOT.
figure%<-----New Figure.
plot(t,y,'b',t1,xenv,'r:',t1,-xenv,'r:',t,y3,'g');
xlabel('t [s]'), ylabel('y'), grid on;
title('Signal Plot for Question 5.');
legend('y(t)','+ve envelope', '-ve envelope', 'y(2-t)');
%==============================%
             End of Script.
```

**%=======================**%





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