

Solving all Examples in Lecture 2.

* PERT weighted average =

$$\frac{\text{optimistic time} + 4 * \text{most likely time} + \text{pessimistic time}}{6}$$

Example:

optimistic time = 8 days

most likely time = 10 days

pessimistic time = 12 days

$$\therefore \text{PERT weighted average} = \frac{8 + 4 * 10 + 12}{6} = 10 \text{ days}$$

Therefore, we use 10 days on the network diagram instead of 12 when using PERT.

2) Critical Path Method (CPM) Problem - Question

Start

ES	D	EF
0	2	2
	A	
4	4	6
LS	TF	LF

0	2	2
	B	
0	0	2

0	4	4
	C	
5	5	9

0	8	8
	D	
1	1	9

$$* TF = LF - EF \text{ or } = LS - ES$$

2	4	6
	F	
2	0	6

6	3	9
	E	
6	0	9

9	3	12
	G	
9	0	12

9	7	16
	I	
11	2	18

12	6	18
	J	
12	0	18

12	2	14
	H	
18	4	18

Finish

Alaziz

$$FF = ES \text{ of successor} - EF \text{ of Present}$$

Answering the following Questions:

1) What is the minimum time required to complete the project?
→ minimum time = 18 days.

2) What is the critical path for this project?

→ The critical path is: B F E G J

3) What is the Early start (ES) date for activity E?

(ES) for E is = ~~6~~ 6

4) What is the late start (LS) date for activity A?

(LS) for A is = 4

5) What is the Late finish (LF) date for activity F?

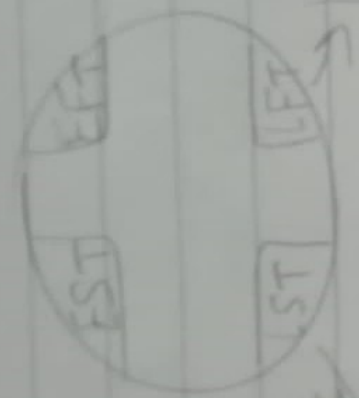
(LF) for F is = 6

6) What is the total float/slack for activity H?

∴ total float (TF) for H = 4

7) What is the free float/slack between activities D & G?

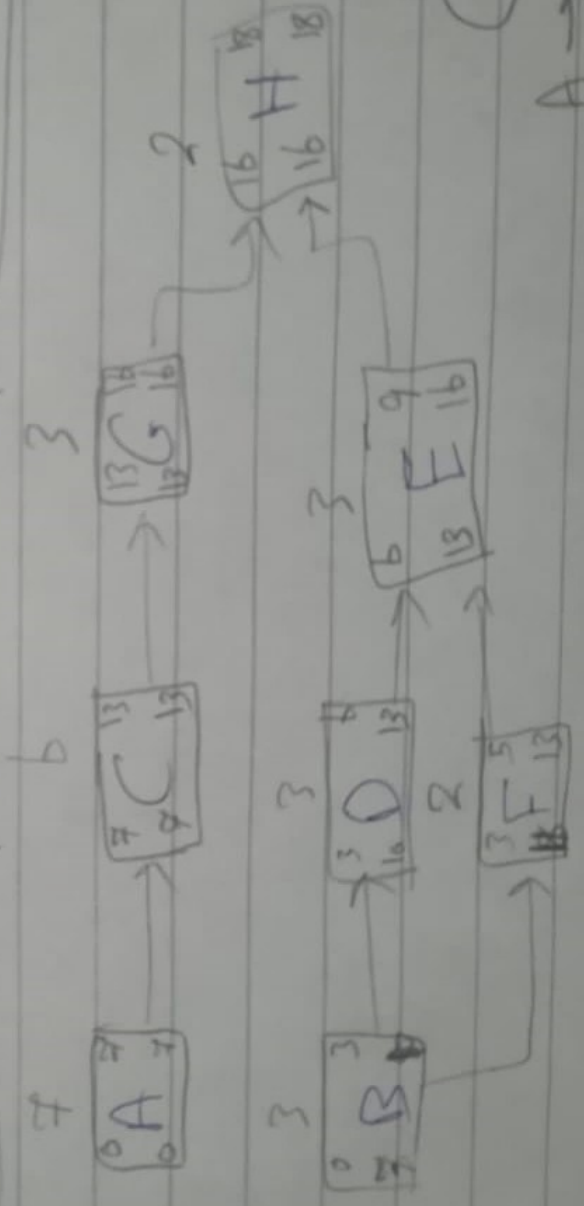
Free float (FF) = 9 - 8 = 1



Task Start Time → Last Finish Time

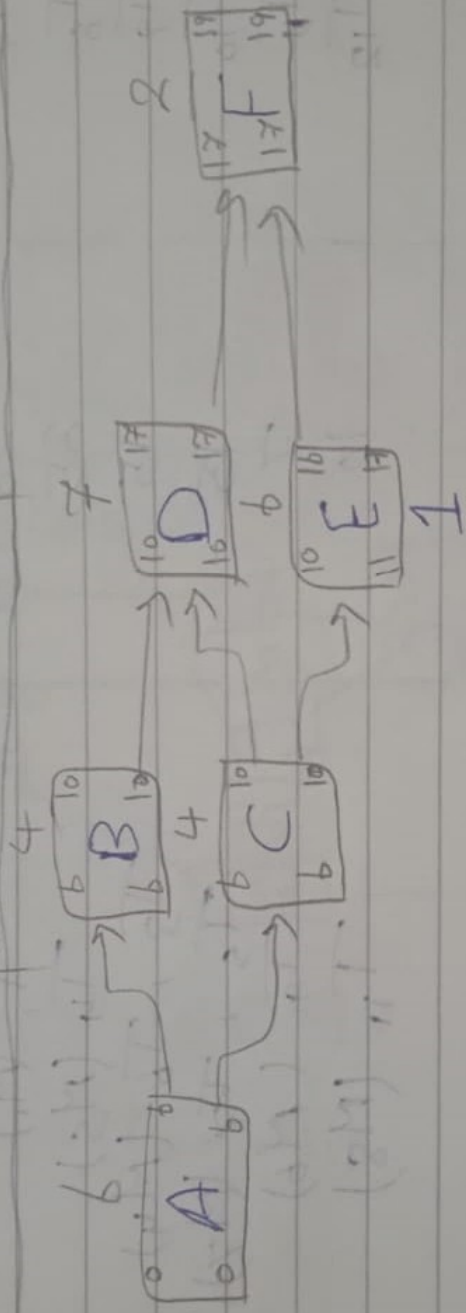
$$LS - ES = LF - EF$$

Task ID	Duration	Dependency
A	7	
B	3	A
C	6	B
D	3	B, F
E	3	B
F	2	C
G	3	E, F
H	2	G



CPM
A → C → G

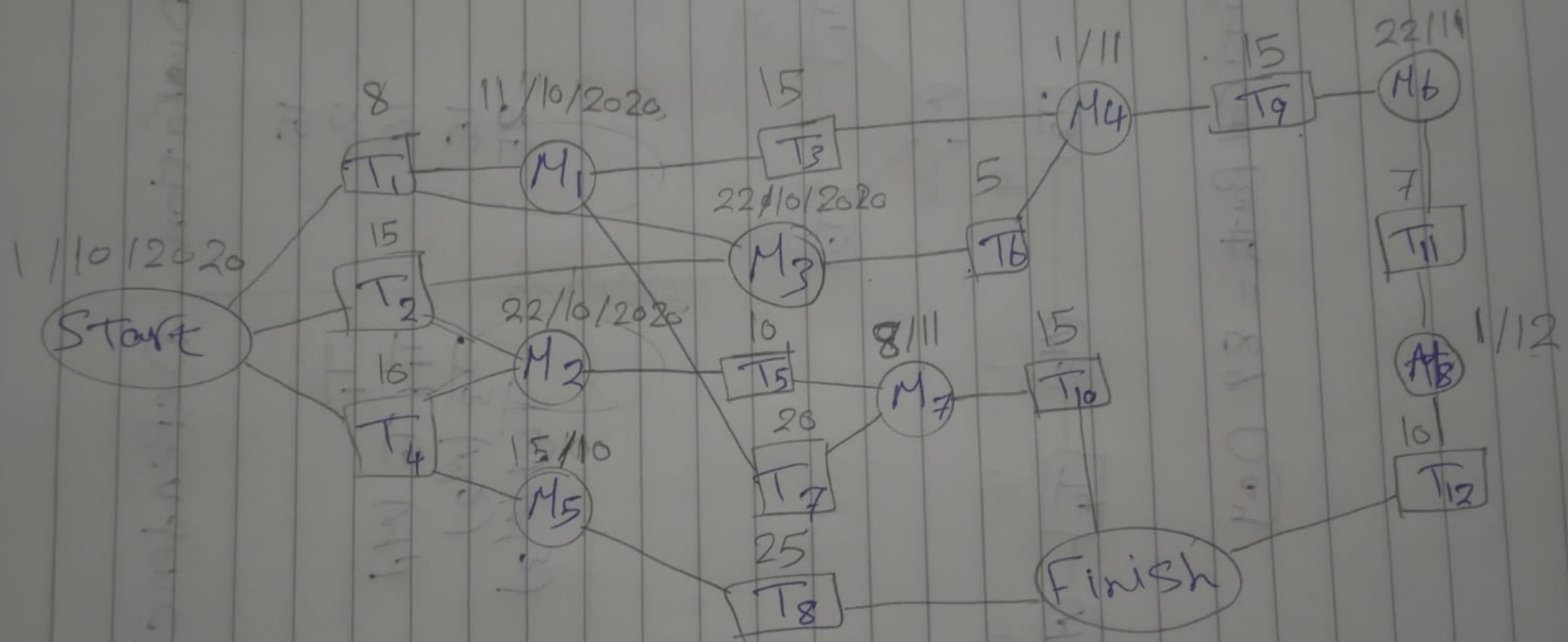
Activity	Immediate process	Normal Duration
A	None	4 weeks
B	A	4
C	A	4
D	B, C	7
E	C	6
F	D, E	2



Critical Path = $A \rightarrow B \rightarrow D \rightarrow F$
 $A \rightarrow C \rightarrow D \rightarrow F$

Activity	Duration	Dependencies
T_1	8	
T_2	15	
T_3	15	$T_1 (M_1)$
T_4	10	
T_5	10	$T_2, T_4 (M_2)$
T_6	5	$T_1, T_2 (M_3)$
T_7	20	$T_1 (M_1)$
T_8	25	$T_4 (M_5)$
T_9	15	$T_3, T_6 (M_4)$
T_{10}	15	$T_5, T_7 (M_7)$
T_{11}	7	$T_9 (M_6)$
T_{12}	10	$T_{11} (M_8)$

$7 = 0 + 9 = 9$
 $7 = 0 + 0 = 0$



The Critical Path is 55 Days

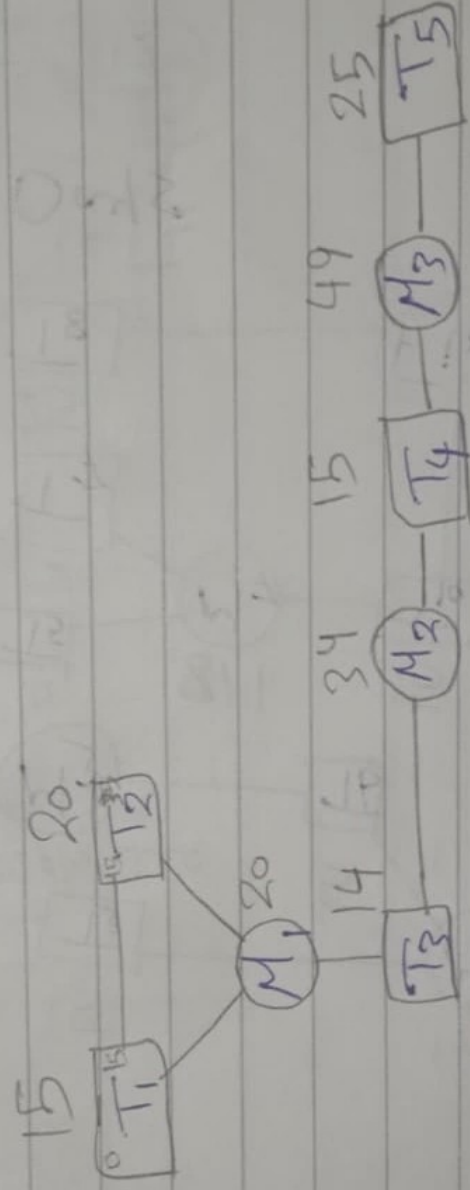
$T_1 \rightarrow T_3 \rightarrow T_9 \rightarrow T_{11} \rightarrow T_{12}$

Dependencies

Duration

Task

T ₁	15	T ₁
T ₂	20	T ₁ , T ₂ (M ₁)
T ₃	14	T ₃ (M ₂)
T ₄	15	T ₄ (M ₃)
T ₅	25	



The critical path = 89 Day