

# Machine Learning for Programming

Peter Norvig



# What is Programming?

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- Implement  $f$  that meets the specification

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Other things too...

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- Induce  $f$  such that  $y \simeq f(x)$ ,  
for given pairs,  
and generalizes well for unseen  $x$

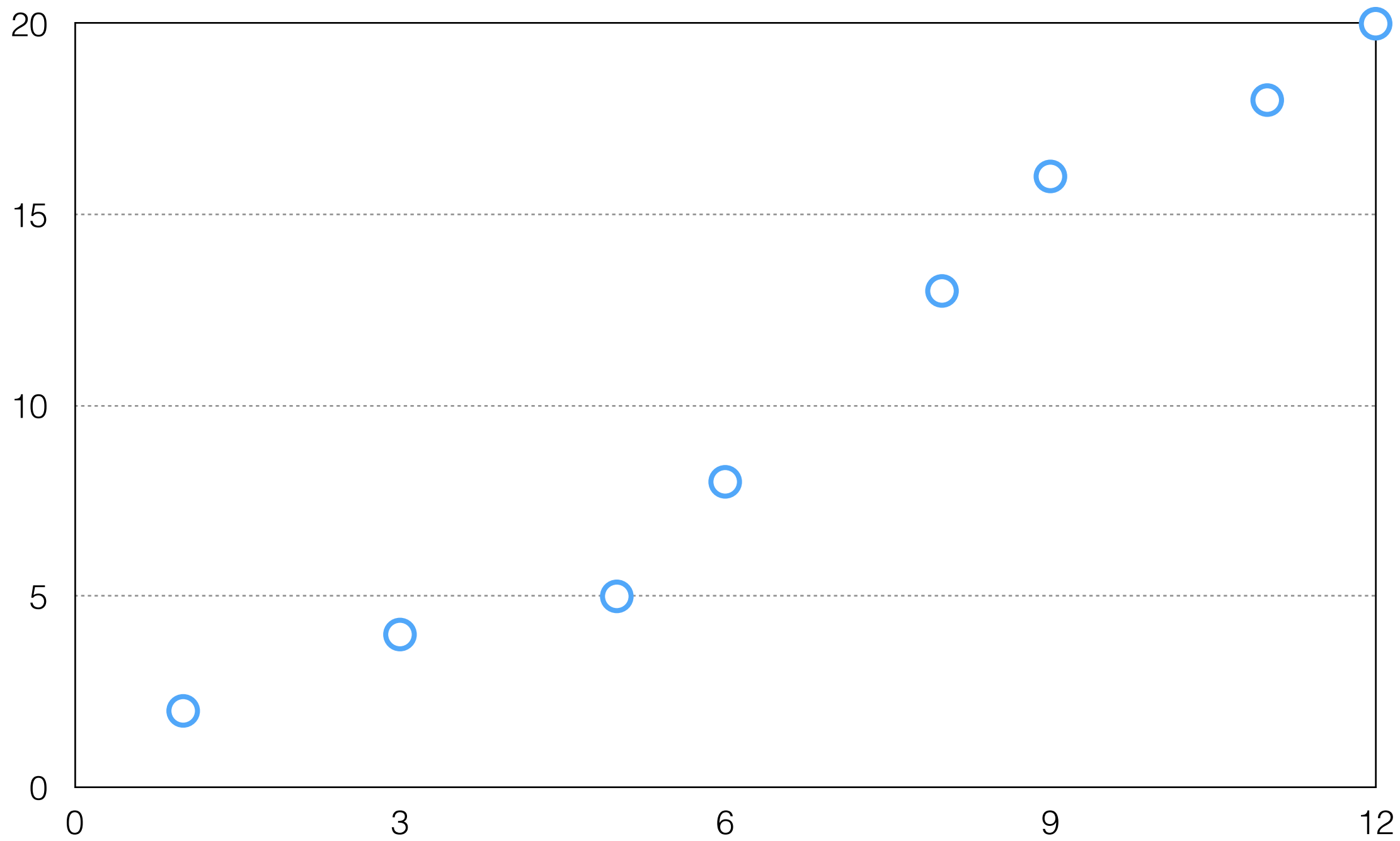


# What is Machine Learning?

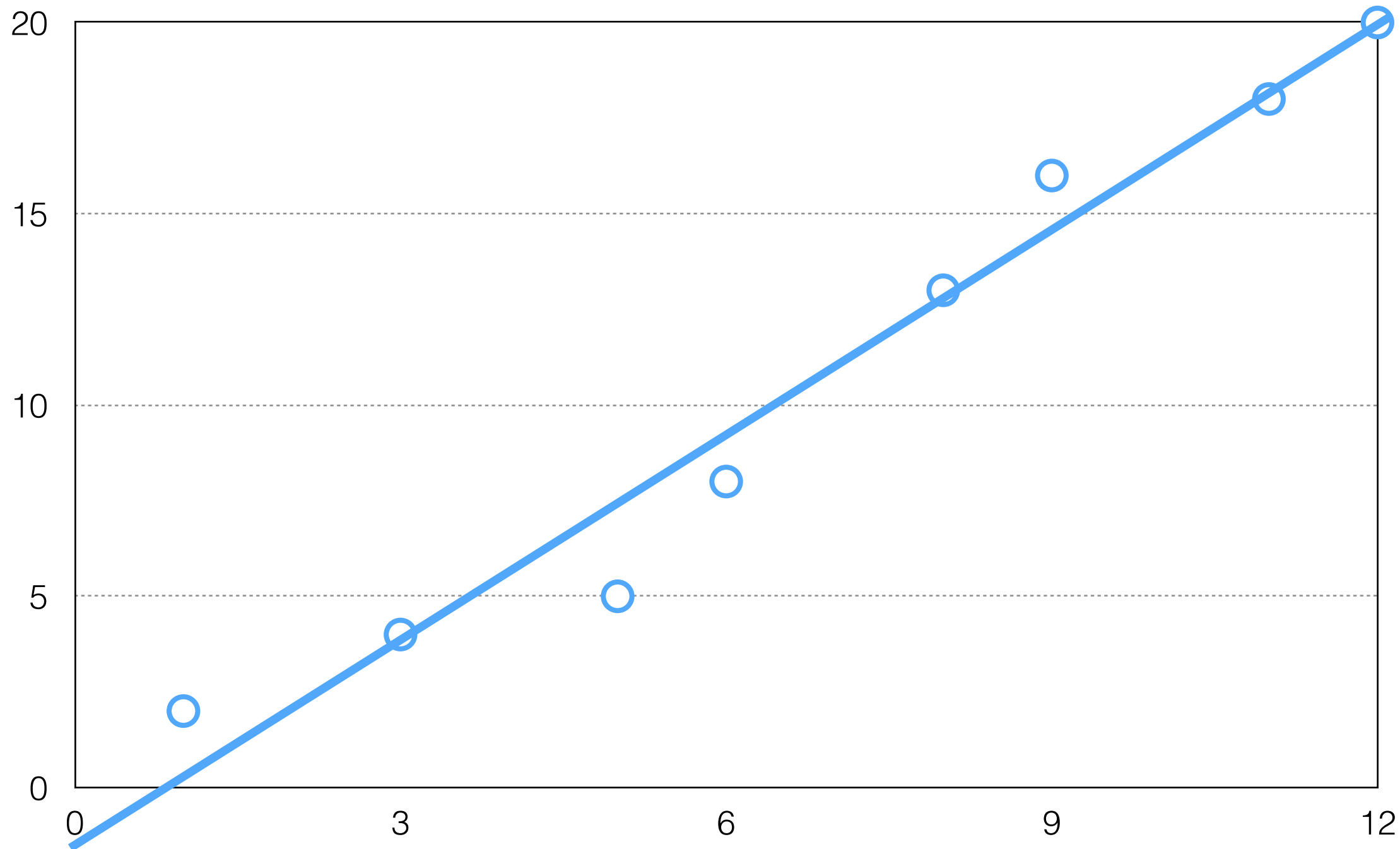
- Given some example  $(x, y)$  pairs
- Induce  $f$  such that  $y \simeq f(x)$ ,  
for given pairs,  
and generalizes well for unseen  $x$

Other kinds of ML too...

Q: Can we learn  
**functions** from  
examples?



$$y = f(x) = 1.75x - 1.2$$



# Other $(x, y)$ pairs

- $x =$



$y =$  “manta ray”

- $x =$



$y =$  “spotted eagle ray”

- $x =$  “This is a short sentence.”

$y =$  “Esta es una frase corta.”

Q: Can we learn  
**functions** from  
examples?

A: **YES**, for many kinds  
of functions

Q: Can we learn  
**parts of programs**  
from examples?

```
import collections, re

def words(text): return re.findall('[a-z]+', text.lower())

WORDS = collections.Counter(words(file('big.txt').read()))
alphabet = 'abcdefghijklmnopqrstuvwxyz'

def edits1(word):
    splits      = [(word[:i], word[i:]) for i in range(len(word) + 1)]
    deletes     = [a + b[1:] for a, b in splits if b]
    transposes  = [a + b[1] + b[0] + b[2:] for a, b in splits if len(b)>1]
    replaces    = [a + c + b[1:] for a, b in splits for c in alphabet if b]
    inserts     = [a + c + b      for a, b in splits for c in alphabet]
    return set(deletes + transposes + replaces + inserts)

def known_edits2(word):
    return [e2 for e1 in edits1(word) for e2 in edits1(e1) if e2 in WORDS]

def known(words): return [w for w in words if w in WORDS]

def correct(word):
    candidates = known([word]) or known(edits1(word)) or known_edits2(word) or [word]
    return max(candidates, key=WORDS.get)
```



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def words(text): return re.findall('[a-z]+', text.lower())

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17 lines

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**Files** | [Outline](#) New!

[..](#)  
[Accents.cc](#)  
[Accents.h](#)  
[Endings.cc](#)  
[Endings.h](#)  
[EndingsDB.cc](#)  
[Exact.cc](#)  
[Exact.h](#)  
[Fuzzy.cc](#)  
[Fuzzy.h](#)  
[Makefile.am](#)  
[Makefile.in](#)  
[Makefile.win32](#)  
**Metaphone.cc**  
[Metaphone.h](#)  
[Prefix.cc](#)  
[Prefix.h](#)  
[Regexp.cc](#)  
[Regexp.h](#)  
[Soundex.cc](#)  
[Soundex.h](#)  
[Speling.cc](#)  
[Speling.h](#)  
[Substring.cc](#)  
[Substring.h](#)  
[SuffixEntry.cc](#)  
[SuffixEntry.h](#)  
[Synonym.cc](#)  
[Synonym.h](#)  
[htfuzzy.cc](#)

## Metaphone.cc

```
144
145     for (; *n && key.length() < MAXPHONEMELEN; n++)
146     {
147         /* Drop duplicates except for CC */
148         if (*(n - 1) == *n && *n != 'C')
149             continue;
150         /* Check for F J L M N R or first letter vowel */
151         if (same(*n) || *(n - 1) == '\0' && vowel(*n))
152             key << *n;
153         else
154         {
155             switch (*n)
156             {
157             case 'B':
158                 /*
159                  * B unless in -MB
160                  */
161                 if (*(n + 1) || *(n - 1) != 'M')
162                     key << *n;
163                 break;
164             case 'C':
165                 /*
166                  * X if in -CIA-, -CH- else S if in
167                  * -CI-, -CE-, -CY- else dropped if
168                  * in -SCI-, -SCE-, -SCY- else K
169                  */
170                 if (*(n - 1) != 'S' || !frontv(*(n + 1)))
171                 {
172                     if (*(n + 1) == 'I' && *(n + 2) == 'A')
173                         key << 'X';
174                     else if (frontv(*(n + 1)))
175                         key << 'S';
176                     else if (*(n + 1) == 'H')
177                         key << (((*(n - 1) == '\0' && !vowel(*
178                                     || *(n - 1) == 'S')
179                                     ? 'K' : 'X'));
180                     else
181                         key << 'K';
182                 }
183             }
```

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2000+ lines

Q: Can we learn  
**parts of programs**  
from examples?

A: **Yes**, Machine Learning  
is the Ultimate  
Agile Programming.

Q: Can we learn  
**entire programs**  
from examples?

# Program Induction

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- $(x, y) = ([3, 2, 1], [1, 2, 3])$   
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- $f_1 = \text{lambda } x: f_1(x[1:]) + x[0:1] \text{ if } x \text{ else } []$   
 $f_2 = \text{lambda } x: [\min(x)] + f_2(\text{remove}(\min(x), x, 1)) \text{ if } x \text{ else } []$



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- $(x, y) = ([3, 1, 4, 1, 5, 9], [9, 5, 1, 4, 1, 3])$   
 $(x, y) = ([2, 7, 1, 8, 2, 8, 1, 8], [8, 1, 8, 2, 8, 1, 7, 2])$

# Program Induction

- $(x, y) = ([3, 2, 1], [1, 2, 3])$   
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- $f_1 = \text{lambda } x: f_1(x[1:]) + x[0:1] \text{ if } x \text{ else } []$   
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- $(x, y) = ([3, 1, 4, 1, 5, 9], [9, 5, 1, 4, 1, 3])$   
 $(x, y) = ([2, 7, 1, 8, 2, 8, 1, 8], [8, 1, 8, 2, 8, 1, 7, 2])$
- $f_1$  (*i.e.*, reverse), not  $f_2$  (*i.e.*, sort)

# Program Induction

- 1980s: Logical/Functional languages; GP, ILP  
2000s: Probabilistic search rather than logical  
2010s: Deep; LSTM: intermediate representations
- TOOWTDI languages (more or less)  
Only one of “ $a + 1$ ” or “ $1 + a$ ” is allowed/pursued
- Stronger type systems
- Total functional programming:  
Only allow recursion that provably terminates
- DSLs, such as regular expressions

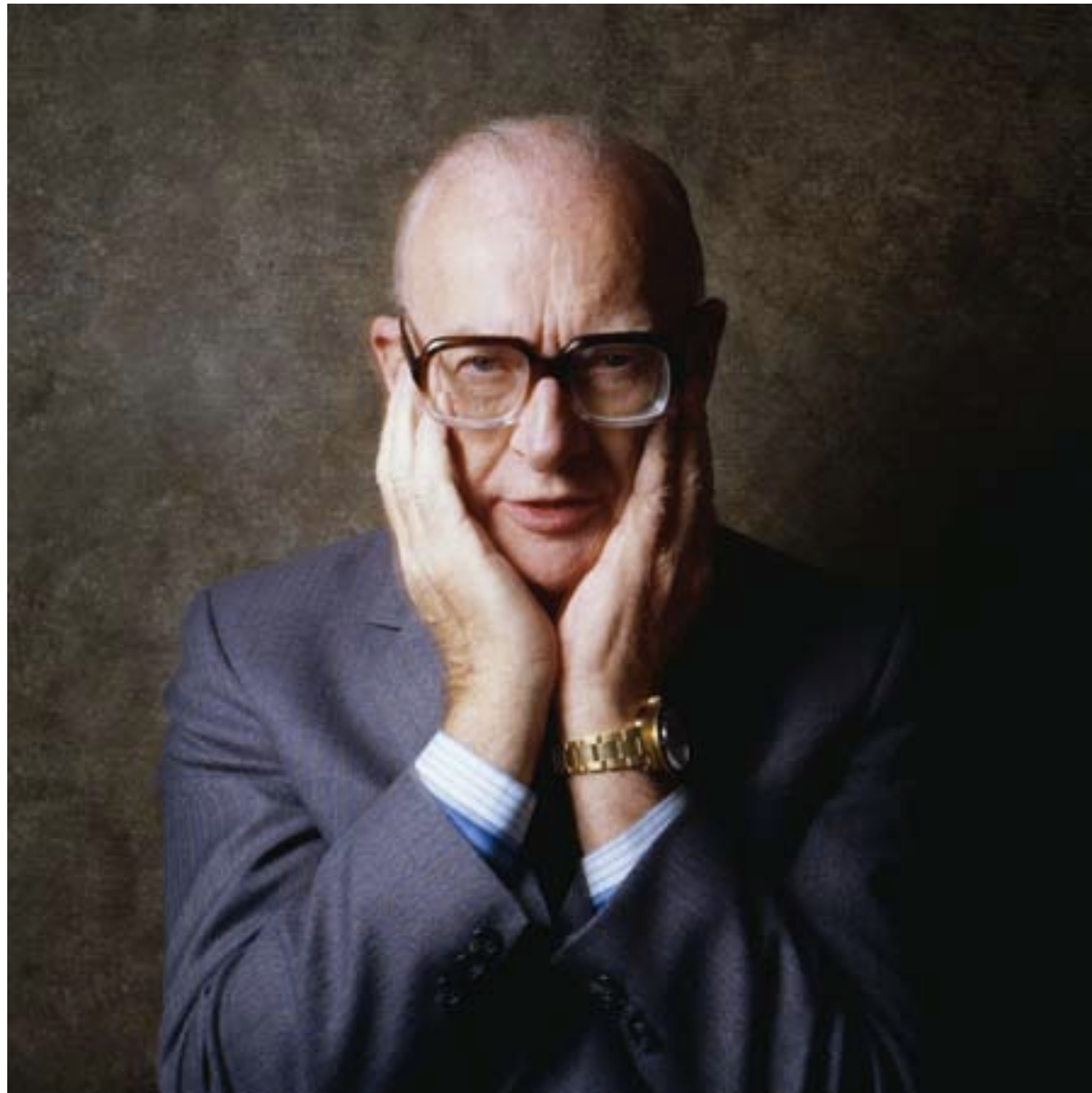
Q: Can we learn  
**entire programs**  
from examples?

A: **Yes**, for short programs;  
**No**, for complex programs.



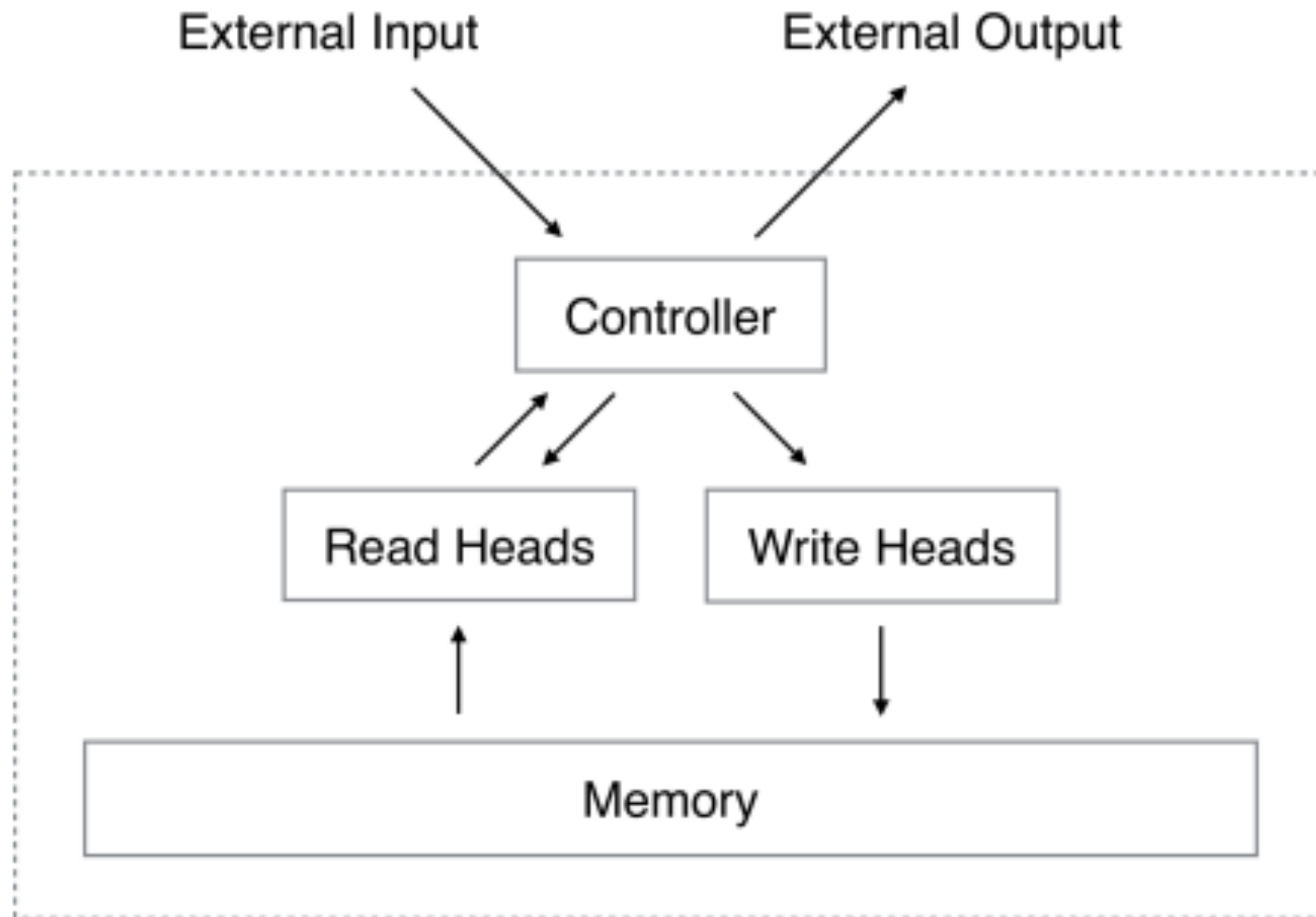
“In the discrete world of computing, there is no meaningful metric in which ‘small’ changes and ‘small’ effects go hand in hand, and there never will be.”  
— Edsger Dijkstra





When a distinguished  
but elderly scientist  
states that something is  
possible, he is almost  
certainly right. When he  
states that something is  
impossible, he is very  
probably wrong.  
— Arthur C. Clarke

# Neural Turing Machines



Graves, Wayne, Danihelka

# Mini Lesson in ML

- Regression
- Gradient Descent
- Neural Networks



# Regression

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- Find a function,  $f$ , to minimize error on examples, and generalization (previously unseen) error

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# Regression

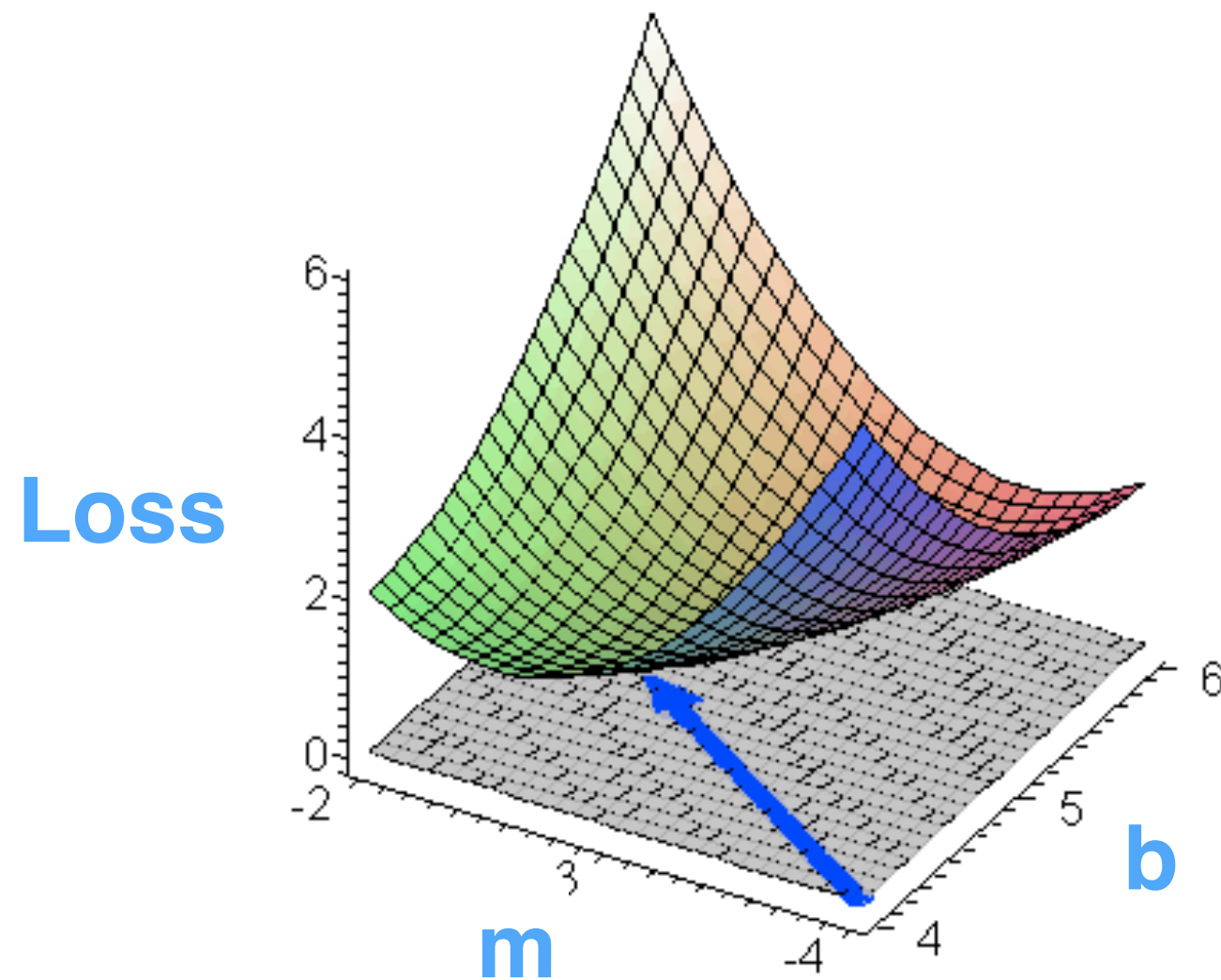
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- $\text{EmpiricalLoss}(f) = \sum_i (y_i - f(x_i))^2$

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- $\text{Loss}(f) = \text{EmpiricalLoss}(f) + \text{GeneralizeLoss}(f)$
- $\text{EmpiricalLoss}(f) = \sum_i (y_i - f(x_i))^2$
- Linear Regression: calculate exact answer (Gauss)

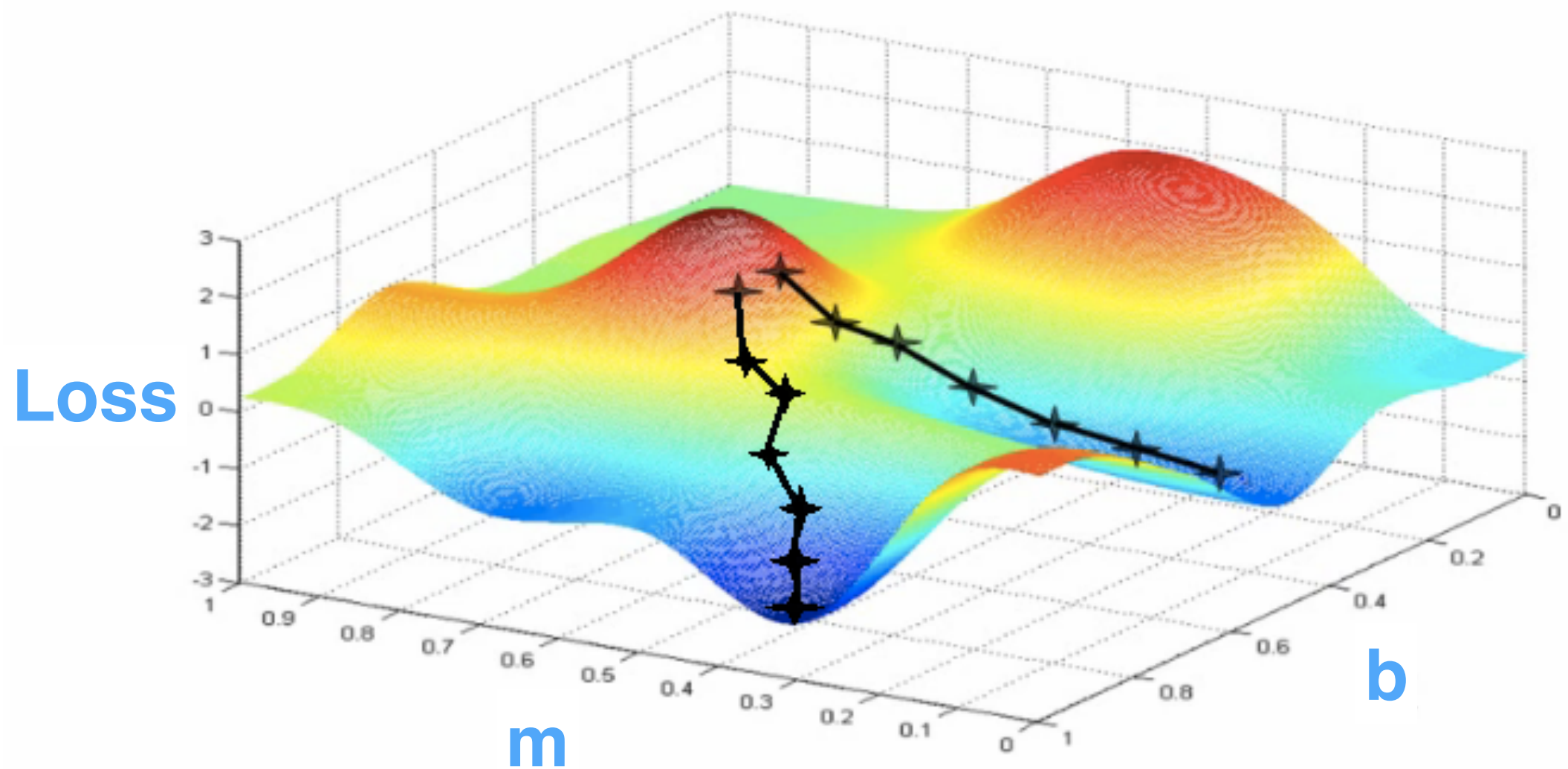
# Gradient Descent

$$f(x) = mx + b$$



# Gradient Descent

$f(x)$  = *nonlinear function of  $x$*



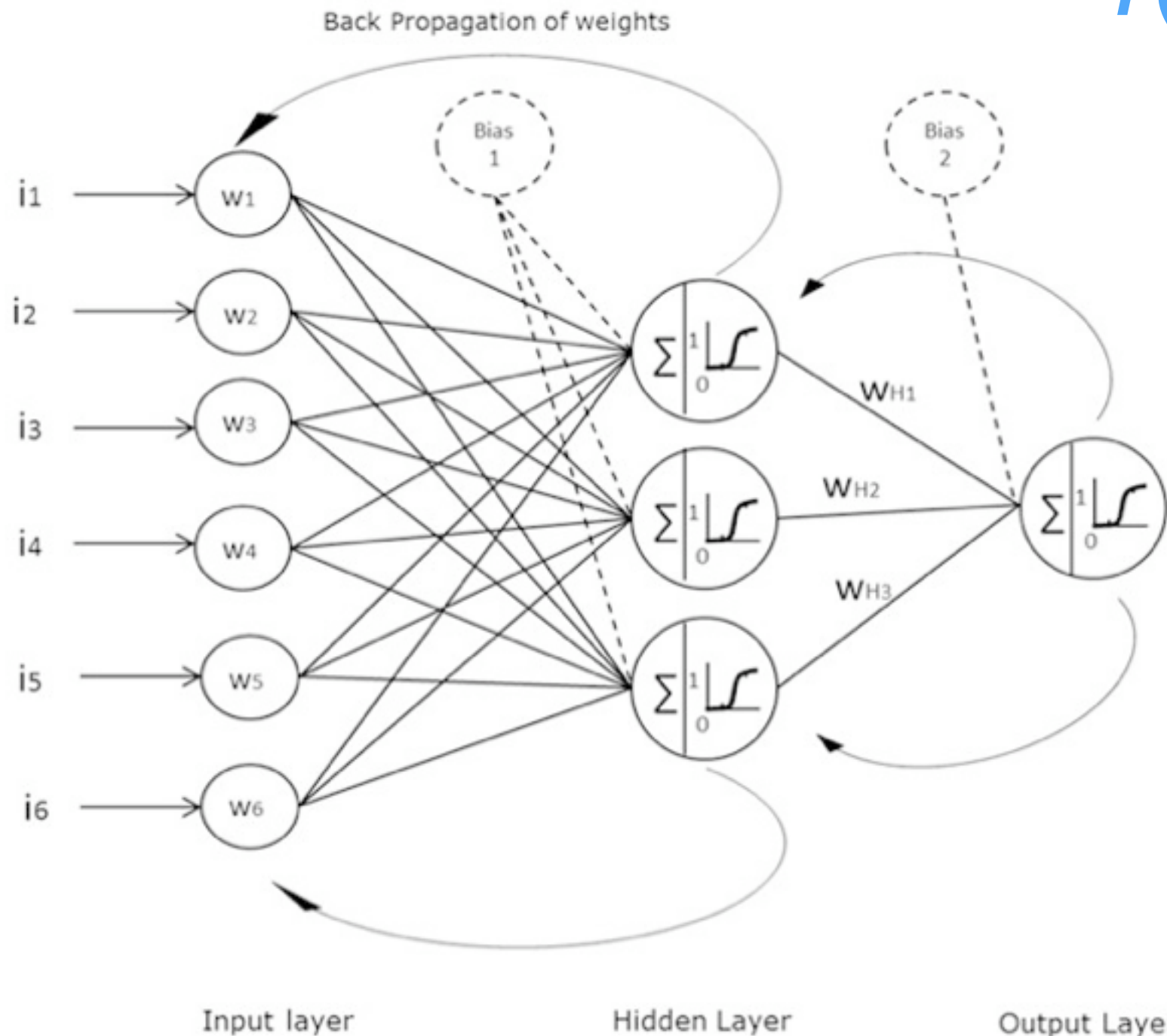


# Neural Network

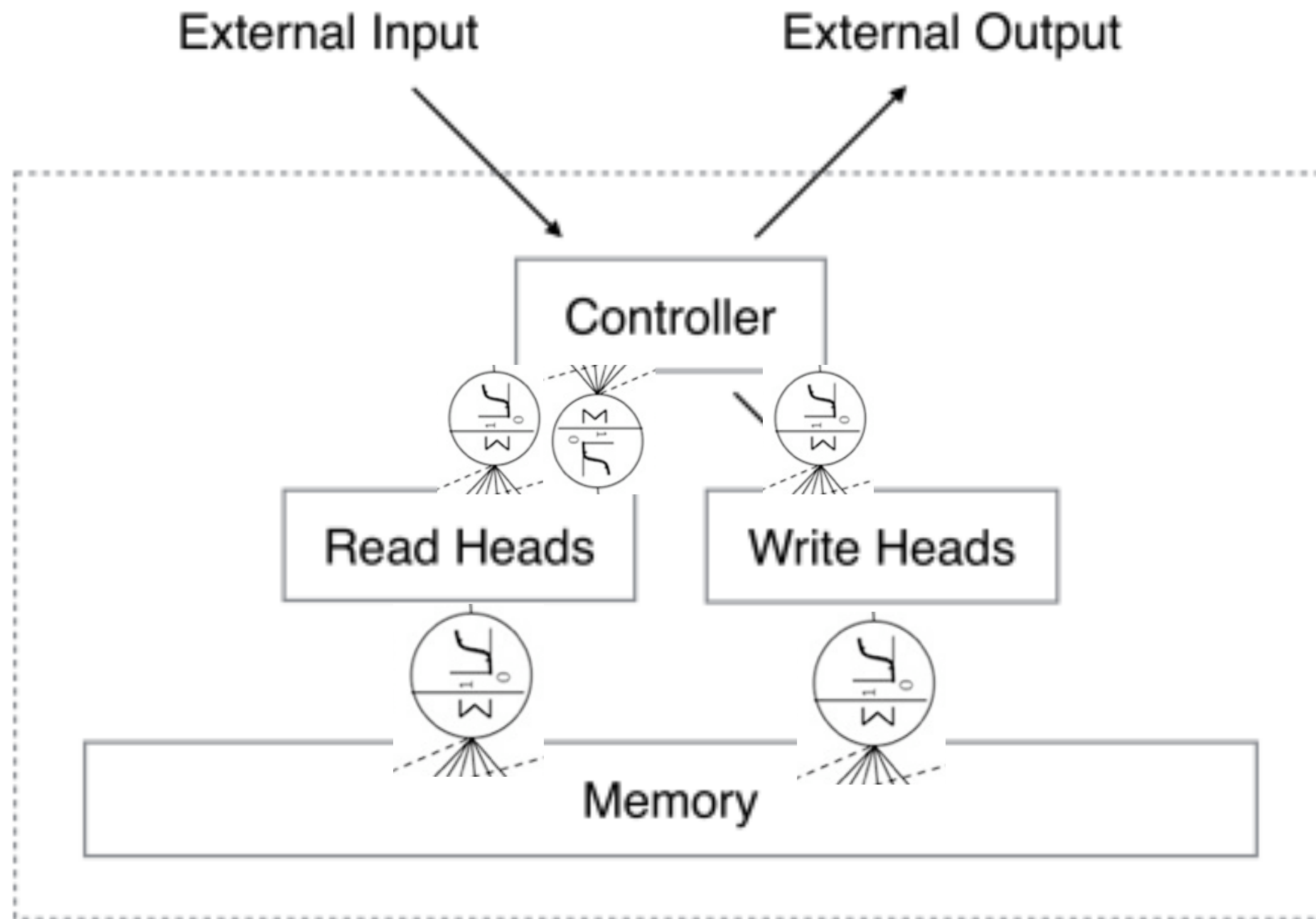
$f(X)$  = nonlinear function  
composed of

$\Sigma, \Pi, S$

$$S(x) = 1 / (1 - e^x)$$



# Neural Turing Machines



Learns programs like “copy input array to output”

Q: Can we learn **complex nontraditional programs** from examples?

A: **Not yet,**  
maybe someday.

Q: Can we learn to  
**optimize** programs?



When in doubt,  
use brute force  
— Ken Thompson

# Superoptimization

- Henry Massalin, 1987  
Given a short function  $f$ , try all sequences a few assembler instructions long
- Alex Aiken 2006  
Slightly longer  $f$ ; more clever and less brute force

Q: Can we learn to  
**optimize** programs?

A: **Yes**, short parts.

Q: Can we learn to  
**efficiently execute**  
**declarative programs?**



# Program Optimization: Crossing the Math/CS Chasm

$$\begin{aligned} \mathbf{e}_{\text{best}} &= \operatorname{argmax}_{\mathbf{e}} p(\mathbf{e}|\mathbf{f}) \\ &= \operatorname{argmax}_{\mathbf{e}} p(\mathbf{f}|\mathbf{e}) p_{\text{LM}}(\mathbf{e}) \omega^{\text{length}(\mathbf{e})} \end{aligned}$$

- A few lines of math
- Tens of thousands of lines of C++

<b>Package</b>	<b>Files</b>	<b>SLOC</b>	<b>Language</b>	<b>Application area</b>
SRILM	285	48967	C++	Language modeling
Charniak parser	266	42464	C++	Parsing
Stanford parser	417	134824	Java	Parsing
cdec	178	21265	C++	Machine translation
Joshua	486	68160	Java	Machine translation
MOSES	351	37703	C++	Machine translation
GIZA++	122	15958	C++	Bilingual alignment
OpenFST	157	20135	C++	Weighted FSAs & FSTs
NLTK	200	46256	Python	NLP education
HTK	111	81596	C	Speech recognition
MALLET	620	77155	Java	Conditional Random Fields
GRMM	90	12926	Java	Graphical model add-on
Factorie	164	12139	Scala	Graphical models

# Declarative Languages for AI, ML Applications

- DYNA (Jason Eisner)  
Probabilistic Context Free Parser:

```
% A single word is a phrase (given an appropriate grammar rule).  
phrase(X,I,J) += rewrite(X,W) * word(W,I,J).  
% Two adjacent phrases make a wider phrase (given an appropriate rule).  
phrase(X,I,J) += rewrite(X,Y,Z) * phrase(Y,I,Mid) * phrase(Z,Mid,J).  
% An phrase of the appropriate type covering the whole sentence is a parse.  
goal          += phrase(start_nonterminal,0,length).
```

```
rewrite("S","NP","VP")=0.9
```

```
word("spring",5,6)=1
```

```
start_nonterminal="S"
```

# Declarative Languages for AI, ML Applications

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rewrite("S","NP","VP")=0.9  
word("spring",5,6)=1  
start_nonterminal="S"
```

**Probabilistic / Relational  
Languages: any variable  
can be input or output**



Q: Can we learn to  
**efficiently execute  
declarative programs?**

A: **Maybe.** So far,  
not done via learning.  
Need help with languages.

Q: Can we learn an  
**interpreter?**

# Recurrent Neural Net Learning with LSTM

**Input:**

```
f=(8794 if 8887<9713 else (3*8334))  
print((f+574))
```

**Target:** 9368.**Model prediction:** 9368.**Input:**

```
j=8584  
for x in range(8):  
    j+=920  
b=(1500+j)  
print((b+7567))
```

**Target:** 25011.**Model prediction:** 23011.**Input:**

```
c=445  
d=(c-4223)  
for x in range(1):  
    d+=5272  
print((8942 if d<3749 else 2951))
```

**Target:** 8942.**Model prediction:** 8942.

Zaremba &  
Sutskever:  
Learning to Execute

Q: Can we learn an  
**interpreter?**

A: **Partly**, but that's not  
the point.



Q: Can we learn a  
**user's language?**



Enter what you want to calculate or know about:

$x^{1/2}$



≡ Examples

Input:

$\sqrt{x}$



$x^2/2$



Examples

Input:

$$\frac{x^2}{2}$$

Q: Can we learn a  
**user's language?**

A: **Interesting idea,**  
but so far done by hand.

Q: Can we learn  
**tutoring feedback**  
from examples?

```
if x = 1:  
    ^
```

SyntaxError: invalid syntax

```
if x == 0  
    print( 'x is zero' )
```

```
if x == 0
    ^
```

SyntaxError: invalid syntax

```
    print('x is zero')
    ^
```

IndentationError: unexpected indent



```
def qsort(A):  
    if len(A) <= 1:  
        return A  
    LT, EQ, GT = []  
    pivot = A[0]  
    for x in A:  
        if x < pivot:    LT.append(x)  
        elif x > pivot:  GT.append(x)  
        else:            EQ.append(x)  
    return qsort(LT) + EQ + qsort(GT)
```

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```

python eror correctoin

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About 181,000 results (0.60 second...)

Showing results for [python \*\*error correction\*\*](#)

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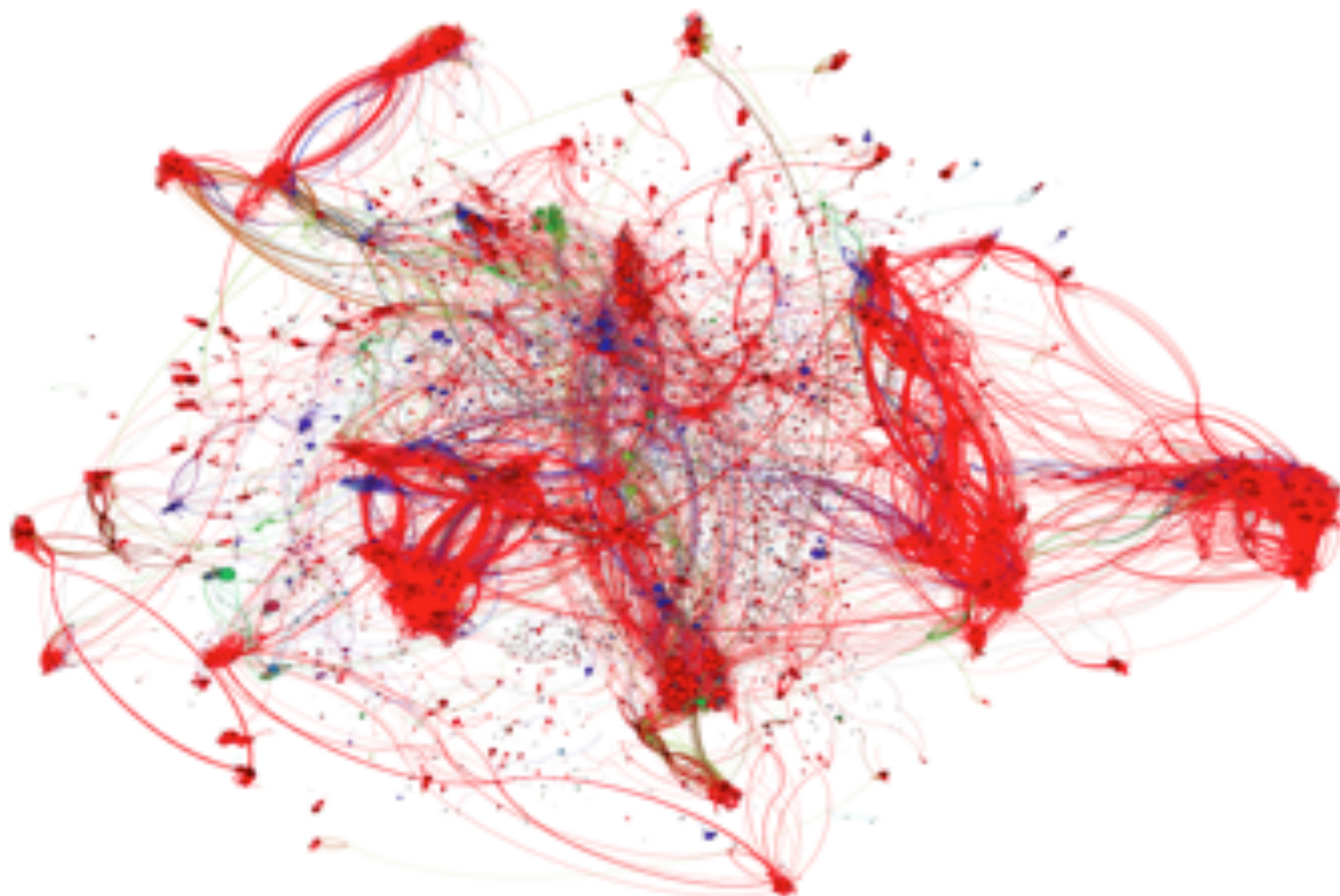
[\*\*error correction\*\* - Reed-Solomon Decoding - Stack Overflow](#)

[stackoverflow.com/questions/1672447/reed-solomon-decoding](https://stackoverflow.com/questions/1672447/reed-solomon-decoding)

1 answer - Nov 4, 2009

I've tried the **Python** ReedSolomon module, but I'm not even sure how to configure ...

When is forward **error correction** a good idea for packets?



Piech & Huang

Group together similar errors;  
Give advice for all in class

$\text{sum}(\text{transpose}(X * \text{theta} - y) * X)$

$\text{sum}(X' * (X * \text{theta} - y))$

$\text{sum}(((\text{theta}' * X')' - y)' * X)$



# Force Multiplication Results using learned program embeddings

After having an expert grade 500:

Algorithm	Submissions Covered	True Positive Rate	Force Multiplication
None	500	100%	1.0
Logistic Regression	35,052	98.7%	70.1
Kmeans Active Learning + Logistic Regression	47,397	98.8%	<b>94.8</b>

Feedback for all 71,000 unique programs was generated automatically from a complex script. Feedback was chosen from 14 different discrete labels.

[piech et al]

Q: Can we learn **tutoring feedback** from examples?

A: **Yes!** Works better as a  
human/machine  
partnership.



# Discussion