ABV-Indian Institute of Information Technology and Management, Gwalior

End-Term Examination (Session 2023-24) Subject- Probability & Statistics (ES103)

Maximum Time: 3 Hours

Max Marks: 50

Attempt all the questions

- (a) Three individuals A, B, and C have applied for a job at a private firm. Their Three individuals A. D. the ratio 1:2:4. The probabilities that A. B. and C. can bring about changes to boost the company's profits are 0.8, 0.5, and 0.3, respectively. If the desired change doesn't occur, find the probability that it is
 - (b) A random variable X has the following probability distribution.

(x = x)
0
k
2k
2k
3k
ς^2
k^2
+ k

- 1. Find k.
- 2. Find the Mean.
- 3. Find P(0 < X < 5).

(3)

(4)

- (c) If six dice are thrown 729 times, how many times would you expect at least three dice to show a five or six?
- (3)
- 2. (a) If X is a Poisson random variable such that P(X = 2) = 9P(X = 4) + 90P(X = 6), find the variance of X.
- (2)
- (b) Let X be a discrete random variable (DRV) with mass points given by

$$x_n = (-1)^n \frac{2^n}{n}$$
, for $n = 1, 2, ...$

and the Probability Mass Function (PMF) defined as

$$f(x_n) = \frac{1}{2^n}$$
, for $n = 1, 2, ...$

Check whether the PMF is well-defined or not.

- (3)
- 3. (a) The weight of an almond is normally distributed with a mean of 0.05 ounce and a standard deviation of 0.015 ounce. Suppose a package of 100 almonds is a random sample.

(i) Find the probability that the sample mean will weigh between 0.048 and 0.053 ounce. (ii) Find the probability that a package of 100 almonds will weigh between 4.8 and 5.3 ounce. (3+3)(b) The mean of a certain normal population is equal to the standard error of the mean of the samples of 64 from that distribution. Find the probability that the mean of the sample size 36 will be negative. (4)(a) In a study to determine whether a certain stimulant produces hyperactivity, 55 mice were injected with 10 microg ams of the stimulant. Afterwards, each mouse was given a hyperactivity rating score. The mean score was $\bar{x}=14.9$ and s=2.8. Give a 95% confidence interval for the population mean score μ . (5) (b) Mark is a shot putter. The distances, in metres, for 8 of his throws are shown below: 15.82, 16.07, 15.37, 19.01, 17.52, 14.98, 15.64, 16.28(i) Find a 99% confidence interval for the mean distance thrown. (ii) Mark claims that his mean throwing distance is 17 metres. Test at the 5% level of significance whether Mark's claim is justified. (5)(c) In a sample of 1,000 people in Maharashtra, 540 are rice eaters and the rest are wheat eaters. Can we assume that both rice and wheat are equally popular in this state at the 1% level of significance? (5)5. (a) Find the lines of regression from the following data: (b) A computer while calculating the correlation coefficient between two variables (5)X and Y from 25 pairs of observations obtained the following results: n = 25, $\sum X = 125$, $\sum X^2 = 650$, $\sum Y = 100$, $\sum Y^2 = 460$, $\sum XY = 508$ However, it was later discovered during checking that two pairs were copied

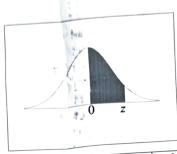
While the correct values should have been:

$$\begin{array}{c|cc}
X & Y \\
\hline
8 & 12 \\
6 & 8
\end{array}$$

Obtain the correct value of the correlation coefficient.

(5)

Standard Normal Distribution Table



							2.5	06)7	.08	.09	
Г	z	.00	.01	.02	.03	.04	.05	.06			0319	.0359	1
F		.0000	.0040	.0080	.0120	.0160	.0199	.0239			0714	.0753	
- 1	0.0	.0398	.0438	.0478	.0517	.0557	.0596	.0636	1		1103	.1141	
		.0793	.0832	.0871	.0910	.0948	.0987	.1026			.1480	.1517	
- 1	-	.1179	.1217	.1255	.1293	.1331	.1368	.1406	1		.1844	.1879	
- 1		.1554	.1591	.1628	.1664	.1700	.1736	.1772	1	000	.2190	.2224	
		.1915	.1950	.1985	.2019	.2054	.2088	.2123			.2517	.2549	_
	0.6	.2257	.2291	.2324	.2357	.2389	.2422	.2454	- 1		.2823	.2852	
	0.7	.2580	.2611	.2642	.2673	.2704	.2734	.2764	- 1		.2823	.3133	
	0.8	.2881	.2910	.2939	.2967	.2995	.3023	.3051			.3365	.3389	
	0.0	.3159	.3186	.3212	.3238_	.3264	.3289	.3315			.3599	.3621	- 1
1	1.0	.3413	.3438	.3461	.3485	.3308	.3531	.3554		3790	.3810	.3830	
1	1.1	.3643	.3665	.3686	.3708	.3729	.3749	.3770		3980	.3997	.401	
	1.2	.3849	.3869	.3888	.3907	.3925	.3944	.3962		4147	.4162	.417	
	1.3	.4032	.4049	.4066	.4082	.4099	.4115	.413		4292	.4306	.431	
	1.4	.4192	.4207	.4222	.4236	.4251	.4265	100000		4418	.4429	.444	1
	1.5	.4332	.4345	.4357	.4370	.4382	.4394			4525	.4535		
	1.6	.4452	.4463	.4474	.4484	.4495	.4505		- 1	.4616	.4625		1
	1.7	.4554	.4564	.4573	.4582	.4591	.4599			.4693	.4699		1
	1.8	.4641	.4649	.4656	.4664	.4671	.4678	1	1	.4756	.4761		
	1.9	.4713	.4719	.4726	.4732	.4738	.4744		- 1	.4808	.481		1
1	2.0	.4772	.4778	.4783	.4788	.4793	.4798	_	_			_	357
-		.4821	.4826	.4830	.4834	.4838			- 1	.4850	1		390
	2.1	.4861	.4864	.4868	.4871	.4875			- 1	.4884			916
	2.2		.4896	.4898	.4901	.4904	.490		1	.4911	1		
1	2.3	.4893	.4920	.4922	.4925	.4927	.492	9 .49	31	.4932	1	.	936
	2.4	.4918	.4940	.4941	.4943	10 March 1981	1	6 .49	948	.4949			952
	2.5	.4953				1		0 .49	961	.496			1964
	2.7	.4965	1	1	1	100			971	.497			1974
		.4903	1	1	1	100		18 .49	979	.497			1981
	2.8						' `		985	.498			986 990
	2.9	.4981				,490	'	39 .49	989	.498		-	993
	3.0	.4987			7 7 4 4 7	,498	0	2 .4	992	,499		-	995
	3.1	.4990	- 1		. ,	1 ,499	-	04 .4	994	.499			997
	3.2	.4993	1			4 ,499	7 1	6 .4	996	.499			998
	3.3	.499				6 ,499		97 .4	997	,499			998
	3.4	1	1		, , , , ,	7 499	' \	98 .4	998	.499	8 .499	70 .4	,,,,
	3.5	.499	8 .499	8 .499	8 .499	8 499)8 .49						

t Table

cum, prob one-tail two-tails	0.50 1.00	0.25 0.50	t m 0.20 0.40	t.ss 0.15 0.30	0.10 0.20	0.05 9.10	f .575 0.025 0.05	t.ss 0.01 0.02	t.995 0.005		t 9995 0.0005
df					0.124	0.10	0.05	0.02	0.01	0.002	<u>0.001</u>
1	0.000	1.000	1.376	1.963	3.078	6.314	12.71	31.82	63.66	318.31	636.62
2	0.000	0.816	1.061	1.386	1.886	2.920	4.303	6.965	9.925	22.327	31.599
3	0.000	0.765	0.978	1.250	1.638	2.353	3.182	4.541	5.841	10.215	12.924
4	0.000	0.741	0.941	1.190	1.533	2.132	2.776	3.747	4.604	7.173	8.610
5	0.000	0.727	0.920	1.156	1.476	2.015	2.571	3.365	4.032	5.893	6.869
6	0.000	0.718	0.906	1.134	1.440	1.943	2.447	3.143	3.707	5.208	5.959
7	0.000	0.711	0.896	1.119	1.415	1.895	2.365	2.998	3.499	4.785	5.408
8	0.000	0.706	0.889	1.108	1.397	1.860	2.306	2.896	3.355	4.501	5.041
9	0.000	0.703	0.883	1.100	1.383	1.833	2.262	2.821	3.250	4.297	4.781
10	0.000	0.700	0.879	1.093	1.372	1.812	2.228	2.764	3.169	4.144	4.587
11	0.000	0.697	0.876	1.088	1.363	1.796	2.201	2.718	3.106	4.025	4.437
12	0.000	0.695	0.873	1.083	1.356	1.782	2.179	2.681	3.055	3.930	
13	0.000	0.694	0.870	1.079	1.350	1.771	2.160	2.650	3.012	3.852	
14	0.000	0.692	0.868	1.076	1.345	1.761	2.145	2.624	2.977		
15	0.000	0.691	0.866	1.074	1.341	1.753	2.131	2.602			
16	0.000	0.690	0.865	1.071	1.337	1.746	2.120	2.583			
17	0.000	0.689	0.863	1.069	1.333	1.740	2.110	2.567	2.7		
18	0.000	0.688	0.862	1.067	1.330	1.734	2.101	2.552	477	1 2	9
19	0.000	0.688	0.861	1.066	1.328	1.729	2.093	2.539			
20	0.000	0.687	0.860	1.064	1.325	1.725	2.086	2.528	2.845		
21	0.000	0.686	0.859	1.063	1.323	1.721	2.080	2.518	2.831	3.52	
22	0.000	0.686	0.858	1.061	1.321	1.717	2.074	2.508	2.819	3.505	
23	0.000	0.685	0.858	1.060	1.319	1.714	2.069	2.500	2.807	3.485	
24	0.000	0.685	0.857	1.059	1.318	1.711	2.064	2.492	2.797	3.467	
25	0.000	0.684	0.856	1.058	1.316	1.708	2.060	2.485	2.787	3.450	
26	0.000	0.684	0.856	1.058	1.315	1,706	2.056	2.479	2.779	3.435	193000000000000000000000000000000000000
27	0.000	0.684	0.855	1.057	1.314	1.703	2.052	2.473	2.771	3.421	The second secon
28	0.000	0.683	0.855	1.056	1.313	1.701	2.048	2.467	2.763	3.408	3.674
29	0.000	0.683	0.854	1.055	1.311	1.699	2.045	2.462	2.756	3.396	3.659
30	0.000	0.683	0.854	1.055	1.310	1.697	2.042	2.457	2.750	3.385	
40	0.000	0.681	0.851	1.050	1.303	1.684	2.021	2.423	2.704	3.307	
60	0.000	0.679	0.848	1.045	1.296	1.671	2.000	2.390	2.660	3.232	
80		0.678	0.846	1. 043 1.042	1 200	1.664	1.990	2.374	2.639	3.195	
100	0.000	0.677	0.845		1.282	1.646	1.984	2.364	2.626	3.174	
1000	0.000	0.675	0.842	1.037	and the six sense of	CONTRACTOR DESIGNATION AND ADDRESS OF THE PARTY OF THE PA	1.962	2.330	2.581	3.098	0.000
2	0.000	0.674	0.842	1.036	1.282		1.960	2.326	2.576	3.090	CONTRACTOR OF STREET
	0%	50%	60%	70%	80%	90%	95%	98%	99%	99.8%	
1					Conf	idence L	P.A61				20.070