VELAGAPUDI RAMAKRISHNA SIDDHARTHA ENGINEERING COLLEGE

(AUTONOMOUS)

II/IV B. Tech. DEGREE EXAMINATION, NOVEMBER: 2017

Third Semester

14CS3302/14IT3302 DISCRETE MATHEMATICAL STRUCTURES

Time: 3 hours

Max. Marks: 70

Part-A is compulsory

Answer One Question from each Unit of Part - B

Answer to any single question or its part shall be written at one place only

PART-A

 $10 \times 1 = 10M$

- 1. a. Define tautology and contradiction.
 - b. Write about the rules: Universal specification and Existential specification.
 - c. Define converse and contra positive.
 - d. Define generating function.
 - e. List the all permutations of $A=\{a, b, c\}$.
 - f. Draw the Hasse diagram of positive divisors of 12.
 - g. How to compute the transitive closure?
 - h. Define lattice.
 - i. What is the Hamilton path and Euler path?
 - j. What is the difference between graph and tree?

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PART-B

 $4 \times 15 = 60M$

UNIT-I

- 2. a. Show that $R \wedge (P \vee Q)$ is a valid conclusion from the premises $P \vee Q$, $Q \rightarrow R$, $P \rightarrow M$ and $\sim M$.
 - If Jack misses many classes through illness, then he fails high school.

 If Jack fails high school, then he is uneducated.

 If Jack reads a lot of books, then he is not uneducated.

 Hence, Jack misses many classes through illness and reads a lot of books.

(or

3. a. Write in detail about the quantifiers used in propositional logic.

7M

b. Obtain the PCNF of formula $(\sim P \rightarrow R) \land (Q \leftrightarrow P)$. 8M

UNIT-II

- 4. a. A multiple choice test has 15 questions and 4 choices for each answer. How many ways can the 15 questions be answered so that i) Exactly 3 answers are correct

 ii) At least 3 answers are correct

 9M
 - b. How many ways can 5 days are chosen from each of the 12 months of an ordinary year of 365 days.
 6M

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- 5. a. Solve the recurrence relation $a_{n+2} 5a_{n+1} + 6a_n = 2$, $n \ge 0$, $a_0 = 3$, $a_1 = 7$.
 - b. Find the coefficient of x^{12} in $\frac{x^2}{(1-x)^{10}}$.

UNIT-III

- 6. a. Explain the properties of binary relation with examples. 7M
 - b. Prove that meet and join operations of a lattice are commutative, associative, idempotent and absorption. 8M

(or)

- 7. a. Let $\{Z = -2, -1, 0, 1, 2, 3,\}$ and relation R is defined as $R = \{(x, y)/x y \text{ is divisible by 3}\}$. Find whether the relation R on Z is equivalence or not.
 - b. Explain Warshall's algorithm. Compute the transitive using Warshall's algorithm for the relation $R = \{(a,a), (a,b), b,c), (c,d), (c,e), (d,e)\}$.

UNIT-IV

a. State and prove Euler's formula.

9M

6M

b. Prove that every simple planar graph is 5 colourable.

(or)

9. a. State and prove Grinberg's theorem.

8M

b. Show that the complete bipartite graph of $k_{3,3}$ is non planar. 7M