

$$\begin{aligned}
 1. \quad \theta' &= \theta^0 + 2\alpha \left[ \frac{1}{m} \sum_{i=1}^m (y^i - h(x_1^i, x_2^i)) \nabla_{\theta} h \right] \\
 &= (4, 5, 6) + 2\alpha (3 - h(1, 2)) \nabla_{\theta} h \\
 &= (4, 5, 6) + 2\alpha (3 - \sigma(21)) \left( \frac{\partial h}{\partial b}, \frac{\partial h}{\partial w_1}, \frac{\partial h}{\partial w_2} \right) \\
 &= (4, 5, 6) + \alpha \left( 6 - \frac{2}{1+e^{21}} \right) \cdot \frac{e^{21}}{(1+e^{21})^2} (1, 1, 2)
 \end{aligned}$$

$$2. (a) \frac{d}{dx} \sigma = \frac{e^{-x}}{(1+e^{-x})^2} = \sigma - \sigma^2 = \sigma(1-\sigma)$$

$$\frac{d^2}{dx^2} \sigma = \frac{d}{dx} \sigma(1-\sigma) = \sigma(1-\sigma)^2 - \sigma^2(1-\sigma) = \sigma(1-\sigma)(1-2\sigma)$$

$$\frac{d^3}{dx^3} \sigma = \frac{d}{dx} \sigma(1-\sigma)(1-2\sigma)$$

$$= \sigma(1-\sigma)^2(1-2\sigma) - \sigma^2(1-\sigma)(1-2\sigma) - 2\sigma^2(1-\sigma)^2$$

$$2. (b) \tanh(x) = \frac{e^x - e^{-x}}{e^x + e^{-x}} = \frac{1 - e^{-2x}}{1 + e^{-2x}} = \frac{2}{1 + e^{-2x}} - 1$$

$$= 2\sigma(2x) - 1$$