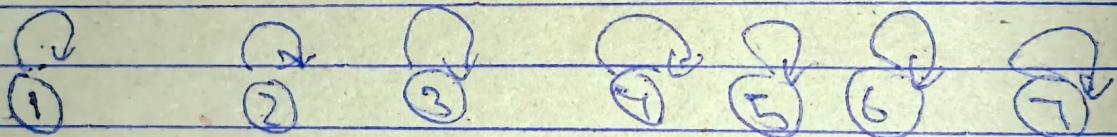


## Disjoint Set

→ We can find whether two nodes are lying in same components of graph or not

Two main opert<sup>n</sup> find parent or find set()  
union() or unioin()

## Union by Rank + path compression



union(1,2)

↳ how to do union

→ get parent of 1       $1 \rightarrow 1$

→ get parent of 2       $2 \rightarrow 2$

→ compare rank of parents

→ If both have same rank kisi ko khi

kisi ke saath attach

kardo.

find parent(1)-1

2-2

3-3

4-4

5-5

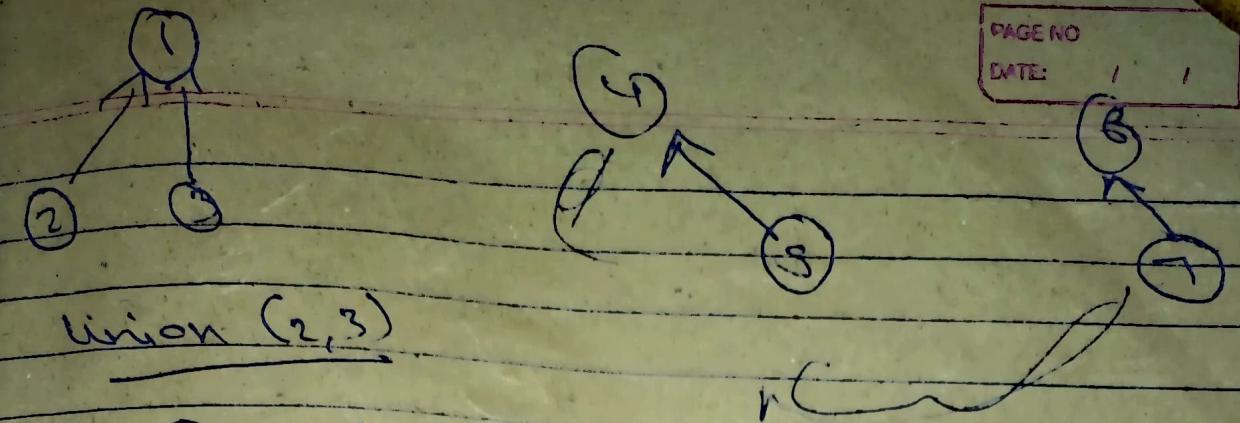
6-6

7-7

Ranks

1 2 3 4 5 6 7

x	0	0	0	0	0	0	0
0	1	2	3	4	5	6	7
1	2	3	4	5	6	7	1
2	3	4	5	6	7	1	2
3	4	5	6	7	1	2	3
4	5	6	7	1	2	3	4
5	6	7	1	2	3	4	5
6	7	1	2	3	4	5	6
7	1	2	3	4	5	6	7



$\rightarrow 2 \rightarrow 1 \rightarrow \text{parent}$

$\rightarrow 3 \rightarrow 3$

1 ki rank 1

3 ki rank 0

rank[3] < rank[1]

In this case parent[3] = 1.

### Union (4,5)

4  $\rightarrow [4] \rightarrow \text{parent}$

5  $\rightarrow [5] \rightarrow \text{parent}$

rank[4] = rank[5]

parent[5] = 4  
rank[4] ++

### Union (6,7)

6  $\rightarrow [6]$

7  $\rightarrow [7]$

rank[6] = rank[7]

parent[7] = 6  
rank[6] ++

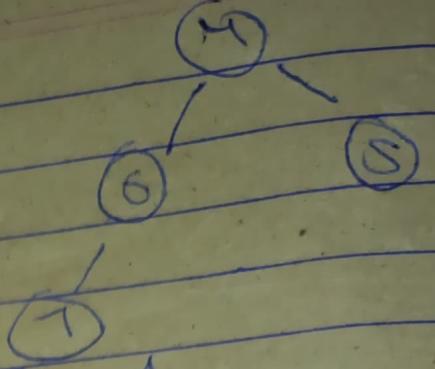
union(5,6)

5 → 4 → parent  
6 → 6

rank[4] = rank[6] = 1

parent[6] = 4

rank[4]++



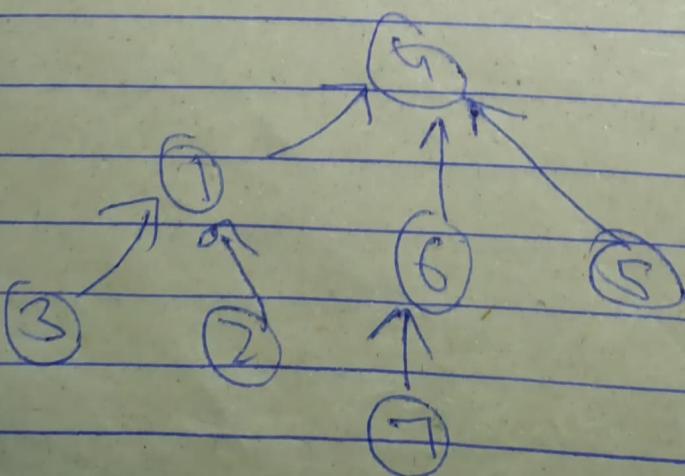
union(3,7)

3 → 1      Rank 1 = 1

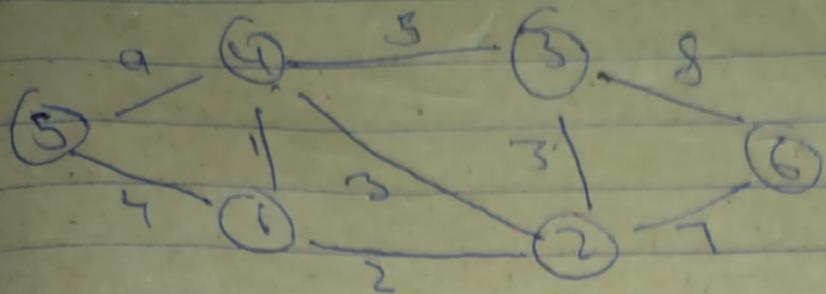
7 → 4      Rank 4 = 2

rank[i] < rank[4]  
1 L 2

parent[7] = 4



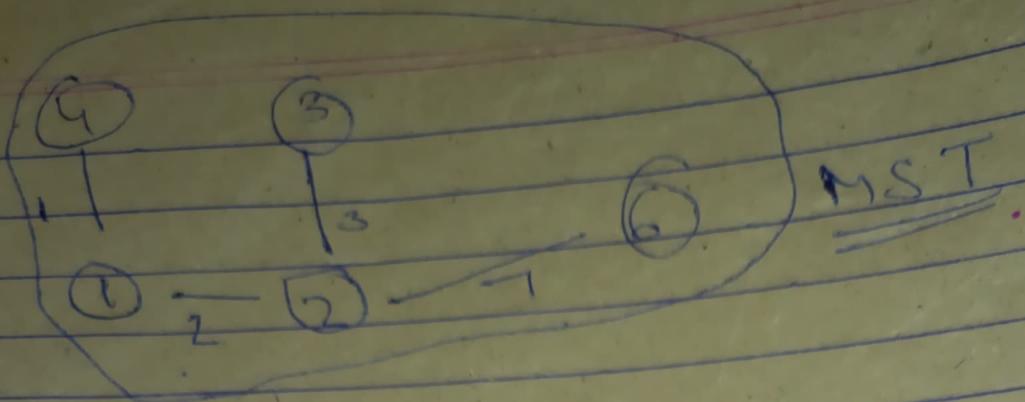
## KRUSKAL'S ALGO



→ No need of adjacency matrix X

We will be requiring a linear data structure that will store edges i.e. ~~two~~ nodes & weight b/w them which will be sorted according to their weight.

4  
1 4  
→ parent 1 ↗  
4 → parent 4 ↘  
If parent different  
then merge/union of  
same then do nothing  
zero different



1 not same comp  $\Rightarrow$  merged

2

2 + 3  $\rightarrow$  not same  $\Rightarrow$  merge

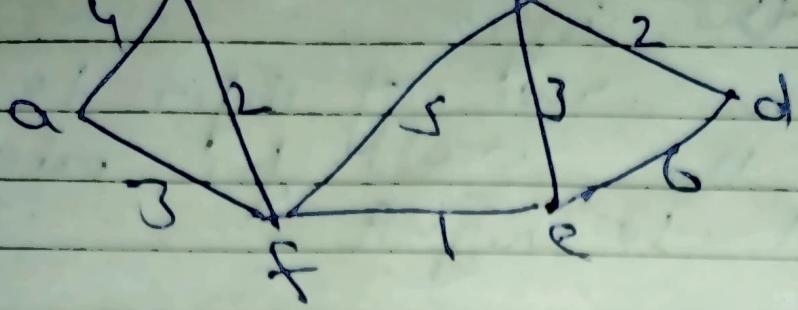
2 ~~+ 4~~ 4 same comp  $\Rightarrow$  ignored

1 + 5 diff comp  $\Rightarrow$  merged

2 + 6 diff comp  $\Rightarrow$  merged

3 + 6 same comp  $\Rightarrow$  ignore d

4 + 5 same comp  $\Rightarrow$  ignore d.



a	b	c	d	e	f
0	$\infty$	$\infty$	$\infty$	$\infty$	$\infty$

0	1	4	$\infty$	$\infty$	$\infty$
---	---	---	----------	----------	----------

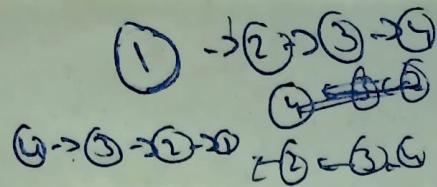
a Se b or  
 Cope ja sake  
 main to hukki  
 distance  
 mark ka  
 di

then we took minimum of distance  
 & fixed it & then repeated the  
~~algo~~ if at some position we reach  
 from a certain node & the distance  
 is less than the value present in  
 array then we do not do anything  
 else update -

0	1	3	8	6	$\infty$
---	---	---	---	---	----------

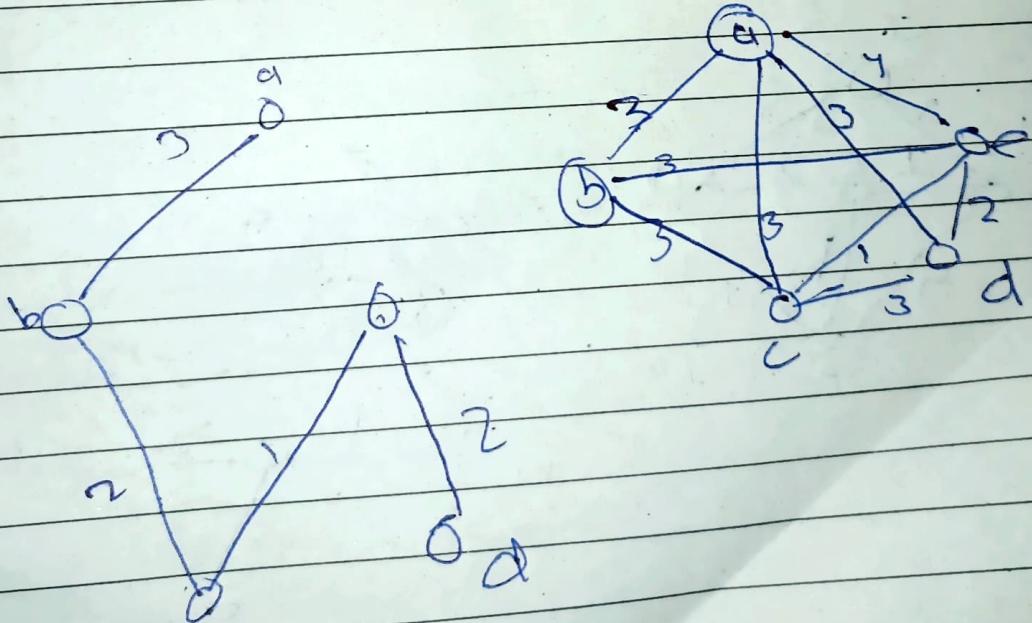
0	1	3	8	14	$\infty$
---	---	---	---	----	----------

0	1	3	7	4	5	10
---	---	---	---	---	---	----



## Brim's Algo

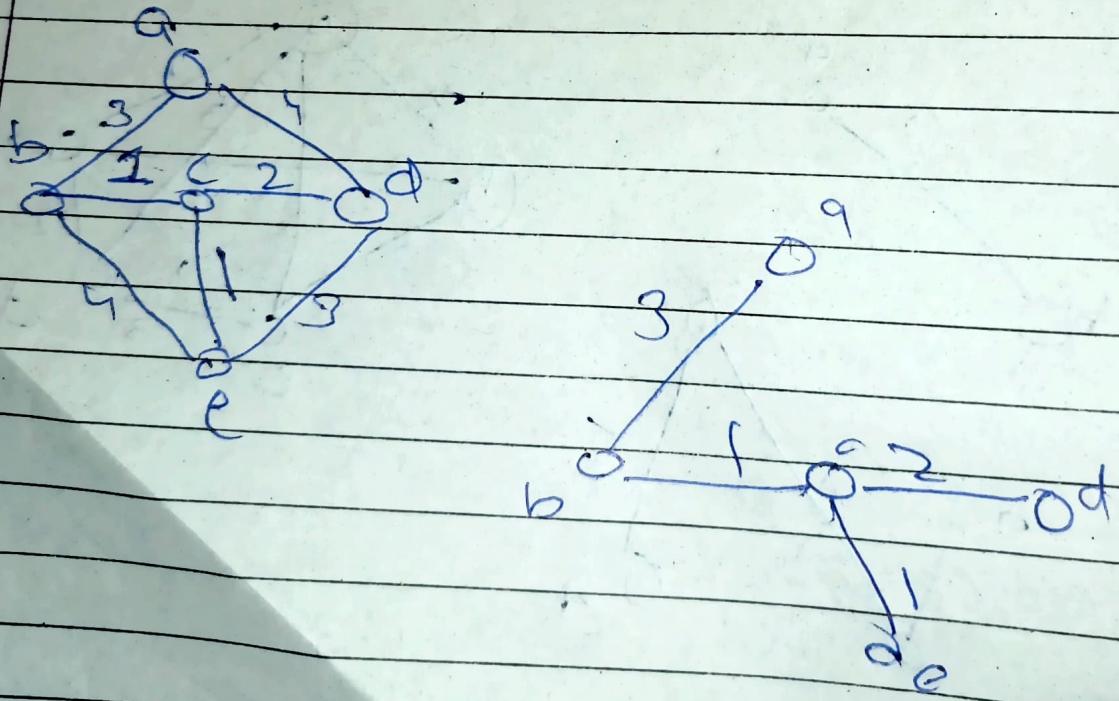
- Select any vertex & choose the edge of smallest weight from G.
- At each stage, choose the edge of smallest weight joining a vertex already included to vertex not yet included.
- Continue until all vertices are included.



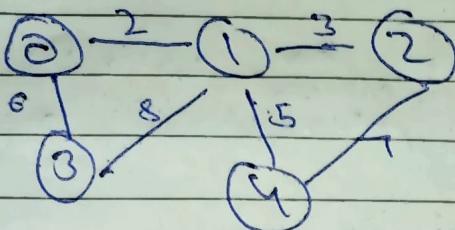
## KRUSKAL'S ALGO

### Working Rule

- (i) choose an edge of minimum weight;
- (ii) at each step choose the edge whose inclusion will not create a circuit
- (iii) If G has  $n$  vertices stop after  $n-1$  edges



## Prim's AIGO



Key

0	1	2	3	4
0	∞	∞	∞	∞

MST  $\rightarrow$  To track MST we know

0	1	2	3	4	Kon hai
F	F	F	F	F	0

Parent

0	1	2	3	4
-1	1	-1	-1	-1

Shraddha  $\leftarrow$

mei sadka

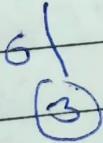
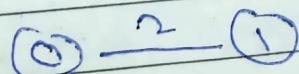
parent -1

Key[0] = 0

parent[0] = -1

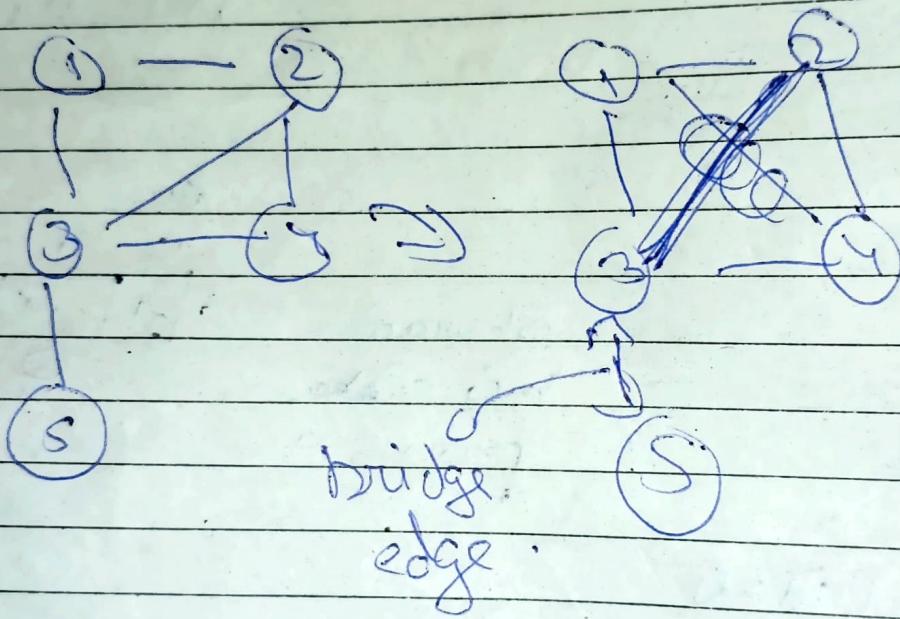
$\leftarrow$  minimum  
 $0 \rightarrow 0$

mst[0] = true

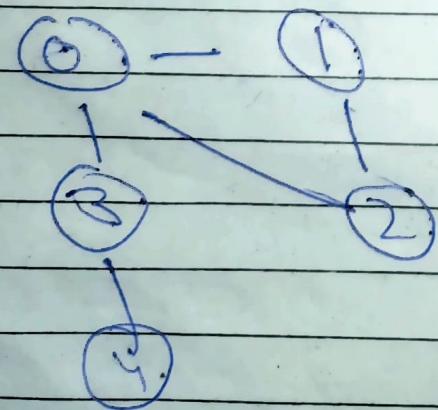


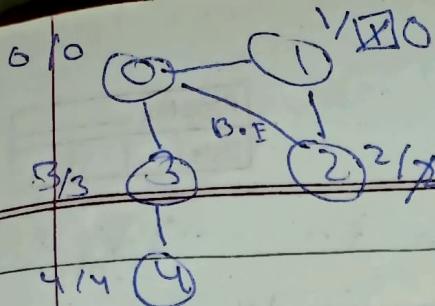
# BRIDGE IN A GRAPH

Bridge is an edge ~~which~~ which remaining no. of components increase connected component increases.



## AICAO





discovery 1 2

Page No.			
Date	4		

	1	2	3	4
0	X	X	X	X

now 0	X	0	X	0	B.E.	3	4
1	X	X	X	X	X	X	X

parent	0	1	0	3
1	X	X	X	X

visited	T	T	T	T	T
1	X	X	X	X	X

time = 9, 1/2, 3/4

discovery time is the time at which we first found the node

the array is to store earliest possible time to reach that node the time taken to reach may vary from path to path

Q

Jab timer bhadda or num 2 se 0 tak pahunchne ka try kiyya toh humneek dekha ki wo already visited hai iska matras  $\odot - 2$  wali edge back edge jo iske 2 tak ram-line mei pahucha ja sakte usko joh ~~iske~~ 2 ka now time update karne padega. discovery time of neighbour

Back edge case

$now[\text{node}] = \min(\text{now}[\text{node}], \text{disc}[\text{neighbour}])$

If neighbour == parent ignore wohhi ta  
Save the back edge no jayengiji

In Back Edge Case

$$\text{low}[node] = \min(\text{low}[node], \text{disc}[neighbour])$$

neighbour  
jiske sathe  
back edge barhi  
rahi

While returning

$$\text{low}[node] = \min(\text{low}[node], \text{low}[child])$$

To check Bridge

$$\boxed{\text{low}[neighbour] > \text{disc}[node]}$$

→ Bridge present

for ① - ②

neighbour = node = 1

$$\text{low}[neighbour] = 0$$

$$\text{disc}_0[1] = 01$$

$$0 \not> 01$$

∴ no Bridge present

This condition works because if

$\text{low}[\text{neighbour}] > \text{disc}[\text{node}]$  it means  
there was only a single way through  
which we could have reached that  
node. Thus it is a Bridge edge.

ANUSUT

TO Check A.P.

$\text{if } \text{child} = \text{parent}$   
ignore

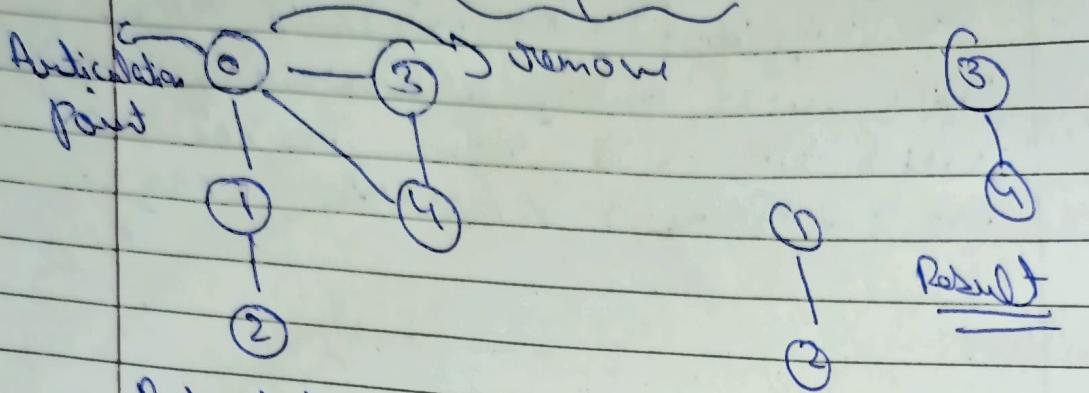
$\text{down}[node] \geq \text{disc}[node]$

$\text{if } \text{parent} = -1$

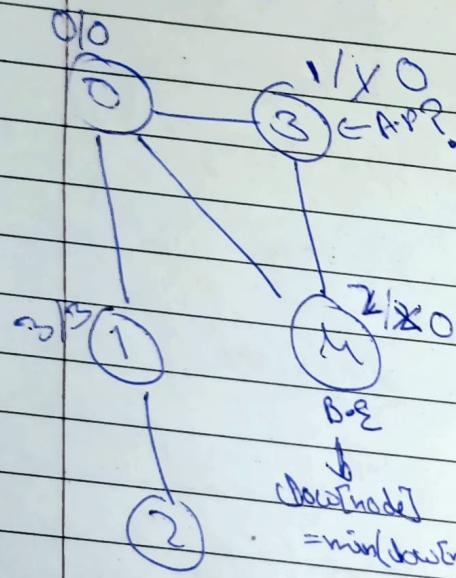
Page No. \_\_\_\_\_

Date \_\_\_\_\_

## ARTICULATION POINTS IN A GRAPH



Articulation point is a node jisko agar remove kardo toh graph do ya toh se jyada components mil tatt Jayega.



	0	3	u	1	2
disc	x	x	x	x	x

	0	3	u	1	2
down	1	1	1	1	1

$= \min(\text{down}[node], \text{disc}[node])$

	0	1	0	3
parent	-1	0	1	1

write returning

$\text{down}[node] = \min(\text{down}[node],$

$\text{down}[child])$

is T + T + T + T

0	1	2	3	4
x	x	x	x	x

Checking for 3 A.P

$$\text{Now}[\text{nbr}] \geq \text{dis}[\text{node}] + 1 \text{ parent}$$

for 3

$$0 \geq 1 \text{ False}$$

$\therefore 3$  is not an A.P

This condition means that there is only one way to reach that particular node  $\therefore$  it will be distorted into components (or remaining that)

for 0+node

$$\text{Now}[\text{nbr}] \geq \text{dis}[\text{node}] + 1 \text{ parent } f = -1$$

$$4 \geq 3$$

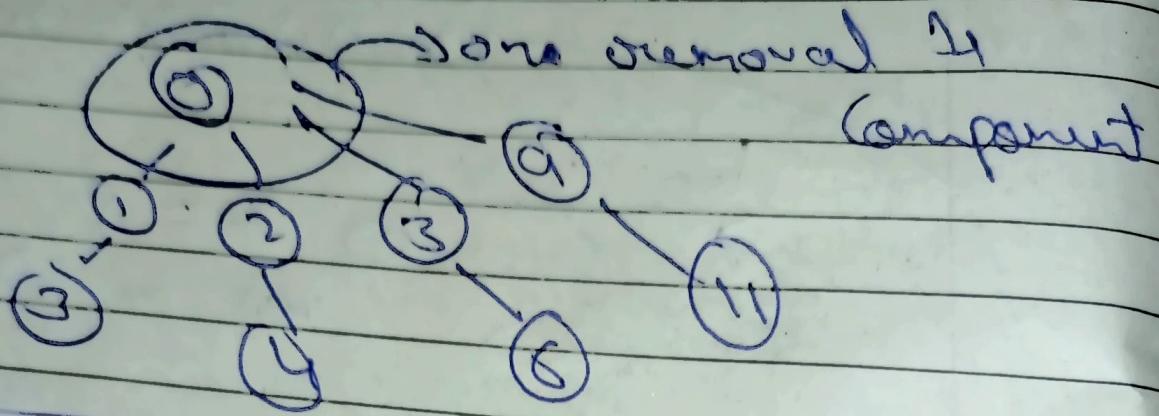
Yes  $\therefore$  It's an AP

Reason for 0  $3 \geq 0$  True but parent = -1  
 $\therefore$  false

But it was an A.P therefore we need to handle it separately

parent != -1 → reason

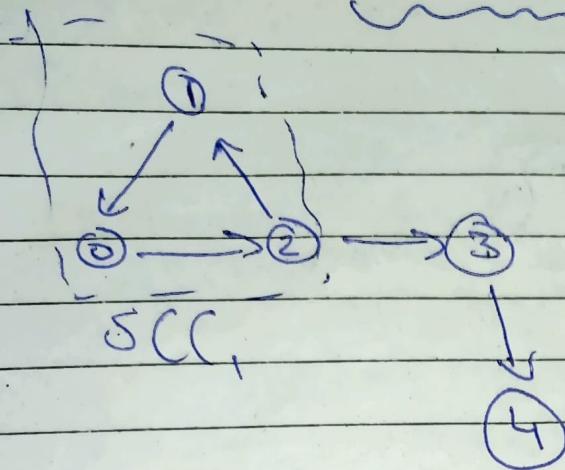
suppx



parent == -1 → child = 1

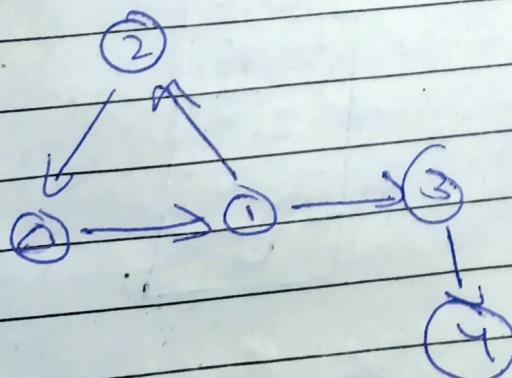
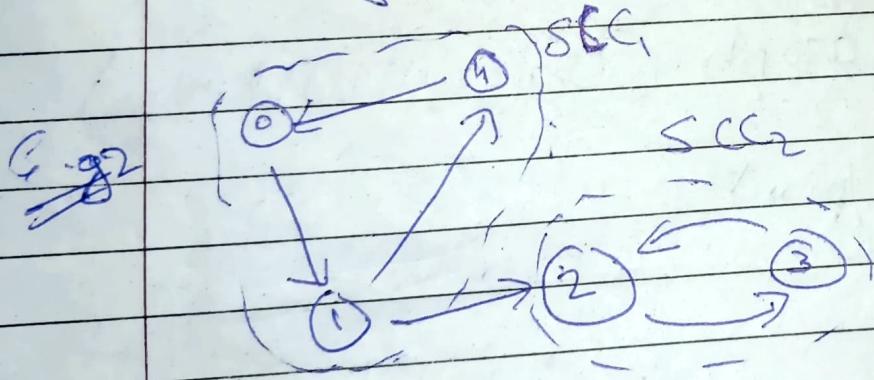
return true [H.P present]

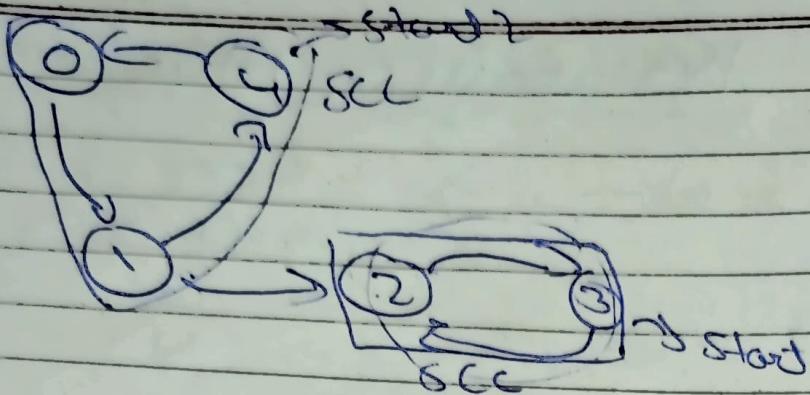
## Kosaraju's ALGO



SCC :-  
 → 0 2 1  
 → 3  
 → 4

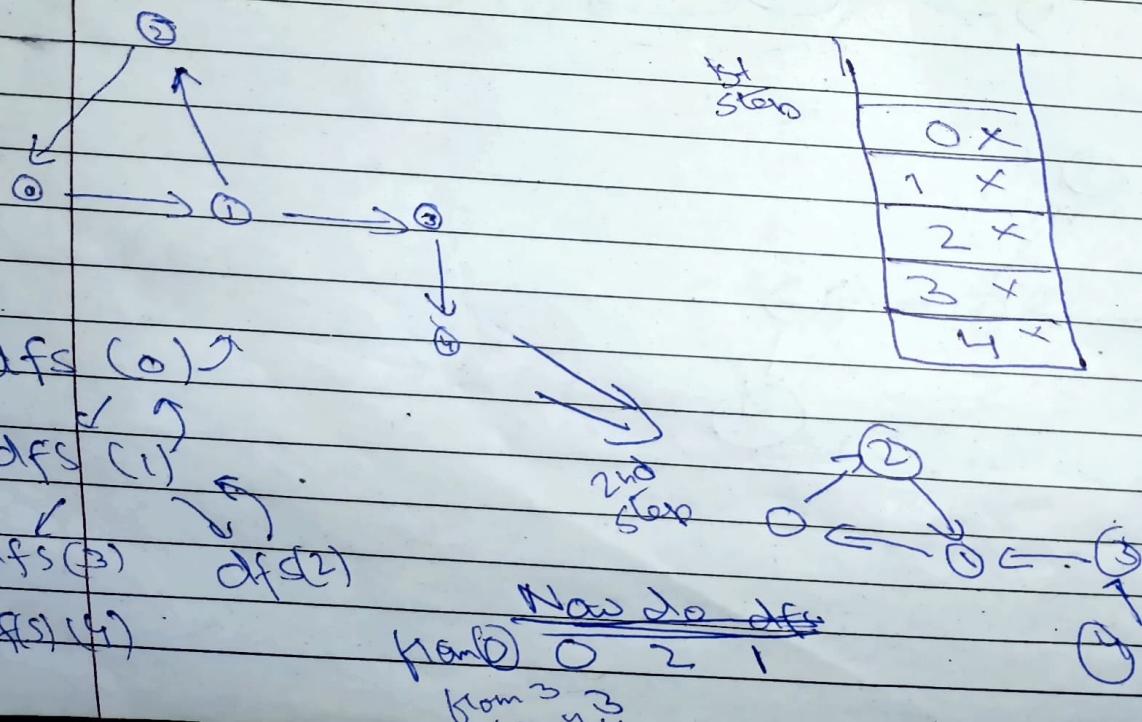
Strongly connected component is that in which we can traverse the entire component taking any node as the starting point.





Kosaraju algo

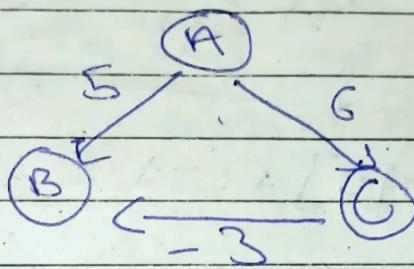
- Sort all nodes basis on their finishing time  
↓  
Topological Sort
- Transpose graph (Change direction of edge)
- dfs → count print  
SCC



# Bellmann Ford Algo

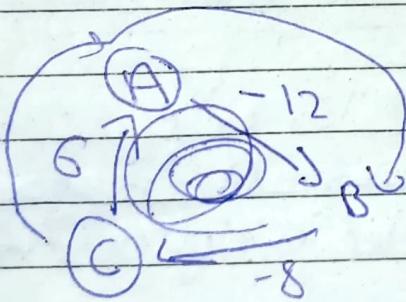
Shortest Path finding Algo

Dijkstra's Algo doesn't work for -ve weights.



↓  
Since greedy

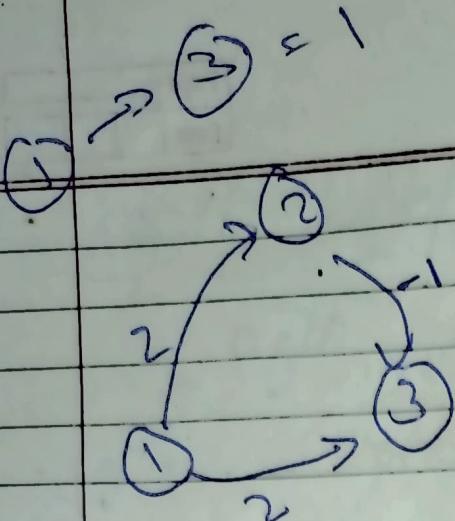
for bellman ford -ve cycle should not be present in graph.



$$\begin{array}{r}
 6 + (-12) = F(6) - 8 = -4 \\
 +6 - 8 - 12 \\
 \hline
 -20
 \end{array}$$

We can find -ve cycle within a graph.

Bellman → for directed weighted graph.



We have to apply the formula given  
 $(n-1)$  times for all edges

~~Step 1~~

if ( $\text{dist}[v] + \text{wt} < \text{dist}[v']$ )

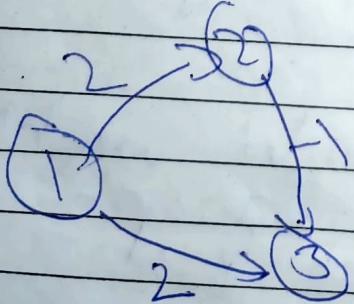
$$\text{dist}[v'] = \text{dist}[v] + \text{wt}$$

~~Step 1~~

1 more time  $\rightarrow$  [same formula]

if any distance gets updated then it means  
 one cycle is present.

$n=3$   
 2 times  
 formula  
 apply



edges

- $1 \rightarrow 2$  (2)
- $2 \rightarrow 3$  (-1)
- $1 \rightarrow 3$  (2)

1	2	3
1	2	3