

$$D_1 = \begin{cases} \text{This one, I think, is called a Yink.} \\ \text{He likes to wink, he likes to drink.} \end{cases}$$

$$D_2 = \begin{cases} \text{He likes to drink, and drink, and drink.} \\ \text{The thing he likes to drink is ink.} \end{cases}$$

$$D_3 = \begin{cases} \text{The ink he likes to drink is pink.} \\ \text{He links to wink and drink pink ink.} \end{cases}$$

Q1 = drink Q2=wink drink Q3=pink ink

This one,I think, is called a Yink.

He likes to wink, he likes to drink.

- D1 长度为 16

词表

this	one	I	think	is	called	a	yink	he	likes	to	wink	drink	pink	ink
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共 15 个词

修正之前:

$$P(\text{drink}|D1)=1/16$$

$$P(\text{wink}|D1)=1/16$$

$$P(\text{pink}|D1)=0$$

$$P(\text{ink}|D1)=0$$

$$P(Q1|D1) = 1/16$$

$$P(Q2|D1) = 1/16 * 1/16 = 1/256 = 0.004$$

$$P(Q3|D1) = 0*0=0$$

修正后:

(1)Laplace correction:

$$P(\text{drink}|D1)=(1+1)/(16+15)=2/31$$

$$P(\text{wink}|D1)=(1+1)/(16+15)=2/31$$

$$P(\text{pink}|D1)=(0+1)/(16+15)=1/31$$

$$P(\text{ink}|D1)= (0+1)/(16+15)=1/31$$

$$P(Q1|D1) = 2/31$$

$$P(Q2|D1) = 2/31 * 2/31 = 4/961$$

$$P(Q3|D1) = 1/31 * 1/31 = 1/961$$

(2)Lindstone corrention:

$$P(\text{drink}|D1)=(1+0.001)/(16+15*0.001)=1001/16015$$

$$P(\text{wink}|D1)=(1+0.001)/(16+15*0.001)= 1001/16015$$

$$P(\text{pink}|D1)=(0+0.001)/(16+15*0.001)= 1/16015$$

$$P(\text{ink}|D1)= (0+0.001)/(16+15*0.001)= 1/16015$$

$$P(Q1|D1) = 1001/16015$$

$$P(Q2|D1) = 1001/16015 * 1001/16015 = 0.004$$

$$P(Q3|D1) = 1/16015 * 1/16015 = 4*10^{-9}$$

(3)Absolute Discounting:

$$P(\text{drink}|D1)=(1-0.001)/16=999/16000$$

$$P(\text{wink}|D1)=(1-0.001)/16=999/16000$$

$$P(\text{pink}|D1)=(0+0.001)/16=1/16000$$

$$P(\text{ink}|D1)= (0+0.001)/16=1/16000$$

$$P(Q1|D1) = 999/16000$$

$$P(Q2|D1) = 999/16000 * 999/16000 = 0.004$$

$$P(Q3|D1) = 1/16000 * 1/16000 = 4*10^{-9}$$

● D2 长度为 16

词表

he	likes	to	drink	and	the	thing	is	ink	wink	pink
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共 11 个词

修正之前:

$$P(\text{drink}|D2)=4/16$$

$$P(\text{wink}|D2)=0$$

$$P(\text{pink}|D2)=0$$

$$P(\text{ink}|D2)=1/16$$

$$P(Q1|D2) = 4/16$$

$$P(Q2|D2) = 0 * 4/16 = 0$$

$$P(Q3|D2) = 0 * 1/16 = 0$$

修正后:

(1)Laplace correction:

$$P(\text{drink}|D2)=(4+1)/(16+11)=5/27$$

$$P(\text{wink}|D2)=(0+1)/(16+11)=1/27$$

$$P(\text{pink}|D2)=(0+1)/(16+11)=1/27$$

$$P(\text{ink}|D2)= (1+1)/(16+11)=2/27$$

$$P(Q1|D2) = 5/27$$

$$P(Q2|D2) = 1/27 * 5/27 = 5/729$$

$$P(Q3|D2) = 1/27 * 2/27 = 2/729$$

(2)Lindstone correction:

$$P(\text{drink}|D2)=(4+0.001)/(16+11*0.001)=4001/16011$$

$$P(\text{wink}|D2) = (0 + 0.001) / (16 + 11 * 0.001) = 1/16011$$

$$P(\text{pink}|D2) = (0 + 0.001) / (16 + 11 * 0.001) = 1/16011$$

$$P(\text{ink}|D2) = (1 + 0.001) / (16 + 11 * 0.001) = 1001/16011$$

$$P(Q1|D2) = 4001/16011$$

$$P(Q2|D2) = 1/16011 * 4001/16011 = 1.6 * 10^{-5}$$

$$P(Q3|D2) = 1/16011 * 1001/16011 = 4 * 10^{-6}$$

(3) Absolute Discounting:

$$P(\text{drink}|D2) = (4 - 0.001) / 16 = 3999/16000$$

$$P(\text{wink}|D2) = (0 + 0.001) / 16 = 1/16000$$

$$P(\text{pink}|D2) = (0 + 0.001) / 16 = 1/16000$$

$$P(\text{ink}|D2) = (1 - 0.001) / 16 = 999/16000$$

$$P(Q1|D2) = 3999/16000$$

$$P(Q2|D2) = 1/16000 * 3999/16000 = 1.6 * 10^{-5}$$

$$P(Q3|D2) = 1/16000 * 999/16000 = 4 * 10^{-6}$$

● D3 长度为 16

词表

the	ink	he	likes	to	drink	is	pink	links	wink	and
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共 11 个词

修正之前:

$$P(\text{drink}|D3) = 2/16$$

$$P(\text{wink}|D3) = 1/16$$

$$P(\text{pink}|D3) = 2/16$$

$$P(\text{ink}|D3) = 2/16$$

$$P(Q1|D3) = 2/16$$

$$P(Q2|D3) = 1/16 * 2/16 = 2/256$$

$$P(Q3|D3) = 2/16 * 2/16 = 4/256$$

修正后:

(1) Laplace correction:

$$P(\text{drink}|D3) = (2 + 1) / (16 + 11) = 3/27$$

$$P(\text{wink}|D3) = (1 + 1) / (16 + 11) = 2/27$$

$$P(\text{pink}|D3) = (2 + 1) / (16 + 11) = 3/27$$

$$P(\text{ink}|D3) = (2 + 1) / (16 + 11) = 3/27$$

$$P(Q1|D3) = 3/27$$

$$P(Q2|D3) = 2/27 * 3/27 = 6/729$$

$$P(Q3|D3) = 3/27 * 3/27 = 9/729$$

(2) Lindstone correction:

$$P(\text{drink}|D3) = (2 + 0.001) / (16 + 11 * 0.001) = 2001/16011$$

$$P(\text{wink}|\text{D3})=(1+0.001)/(16+11*0.001)= 1001/16011$$

$$P(\text{pink}|\text{D3})=(2+0.001)/(16+11*0.001)= 2001/16011$$

$$P(\text{ink}|\text{D3})= (2+0.001)/(16+11*0.001)= 2001/16011$$

$$P(\text{Q1}|\text{D3}) = 2001/16011$$

$$P(\text{Q2}|\text{D3}) = 1001/16011 * 2001/16011 = 0.0078$$

$$P(\text{Q3}|\text{D3}) = 2001/16011 * 2001/16011 = 0.016$$

(3)Absolute Discounting:

$$P(\text{drink}|\text{D3})=(2-0.001)/16=1999/16000$$

$$P(\text{wink}|\text{D3})=(1-0.001)/16=999/16000$$

$$P(\text{pink}|\text{D3})=(2-0.001)/16=1999/16000$$

$$P(\text{ink}|\text{D3})= (2-0.001)/16=1999/16000$$

$$P(\text{Q1}|\text{D3}) = 1999/16000$$

$$P(\text{Q2}|\text{D3}) = 999/16000 * 1999/16000 = 0.0078$$

$$P(\text{Q3}|\text{D3}) = 1999/16000 * 1999/16000 = 0.016$$

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1. 在使用文档的交叉熵进行检索时，为什么要用 $H(M_Q||M_D)$ 而不是 $H(M_D||M_Q)$?

首先，从公式上看，这两个公式是不对称的：

$$H(M_Q||M_D) = \sum_w P(w|M_Q) \log P(w|M_D)$$

$$H(M_D||M_Q) = \sum_w P(w|M_D) \log P(w|M_Q)$$

因而，采取不同的形式计算的结果并不相同。

从语义上看， $H(M_Q||M_D)$ 表示用 M_D 编码 M_Q 所需要的平均编码长度。对于一次检索而言，意指确定一个查询 Query 及其语言模型 M_Q ，使用文档集中的各个文档的语言模型 M_D 对 M_Q 进行编码，并由短到长进行排序，实现一次检索。这是 $H(M_Q||M_D)$ 的实际意义。

反之，若使用 $H(M_D||M_Q)$ ，其含义为对某一篇确定文档及其语言模型 M_D ，用多个 Query 的语言模型 M_Q 去描述，这不符合检索的定义。

2. 对一个给定的文档集，对每个文档构建其 uni-gram 模型，列出出现概率最高的 10 个词。

DOC1: Computers on display in Fuzhou. Display of a computer in Sidney. Playing a

computer in Sidney. Fuzhou computer store in debt. Sidney Science Fair .(24words)

DOC2: new home sales top forecasts. home sales rise in July. increase in home sales in July. july old home sales rise.(21words)

DOC3: breakthrough drug for schizophrenia. new schizophrenia drug. new approach for treatment of schizophrenia. new hopes for schizophrenia patients .(18words)

DOC1		DOC2		DOC3	
in	4/24	sales	4/21	schizophrenia	4/18
Sidney	3/24	home	4/21	new	3/18
computer	3/24	July	3/21	for	3/18
Fuzhou	2/24	in	3/21	drug	2/18
display	2/24	rise	2/21	treatment	1/18
a	2/24	top	1/21	patients	1/18
store,,science, playing,on, of,fair,debt, computers	1/24	old	1/21	of	1/18
		new	1/21	hopes	1/18
		increase	1/21	breakthrough	1/18
		forecasts	1/21	approach	1/18

部分 DOC 来自教材与互联网。