

Exercise Sheet 6

1 Markov Model Forward Problem

$$\begin{aligned} q) \quad P(q_{t+1} = s_j) &= P(q_1) \cdot P(q_2 | q_1) \cdot \dots \cdot P(q_t | q_{t-1}) \cdot P(q_{t+1} = s_j | q_t) \\ &= \sum_{i=1}^M \underbrace{P(q_1) P(q_2 | q_1) \cdot \dots \cdot P(q_t = s_i | q_{t-1})}_{P(q_t = s_i)} \cdot P(q_{t+1} = s_j | q_t = s_i) \end{aligned}$$

2 Hidden Markov Model Forward Problem

$$\begin{aligned} P(o_1, \dots, o_t, o_{t+1}, q_{t+1} = s_j) &= P(q_1) P(q_2 | q_1) \cdot \dots \\ &\cdot P(o_1 | q_1) P(o_2 | q_2) \cdot \dots \cdot P(o_{t+1} | q_{t+1} = s_j) \\ &= \sum_{i=1}^M P(q_1) \cdot P(q_2 | q_1) \cdot \dots \cdot P(q_t = s_i | q_{t-1}) \\ &\quad \cdot P(o_1 | q_1) \cdot P(o_2 | q_2) \cdot \dots \cdot P(o_t | q_t = s_i) \cdot P(q_{t+1} = s_j | q_t = s_i) \\ &\quad \cdot P(o_{t+1} | q_{t+1} = s_j) \end{aligned}$$