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## 1. Introduction And Review

### Panel data (longitudinal or cross-sectional time-series data):

that combines temporal depth with cross-sectional breadth, offering a powerful framework that enhances the precision and richness of econometric inference (Hsiao, 2003).

The evolution of panel methodologies began in the mid-20th century when researchers recognized the limitations of using only cross-sectional or time-series data:

- Verbeek & Nijman (1992) and Moulton (1990) introduce fixed/random-effects and temporal-dependency models.
- Arellano & Bond (1991) develop dynamic GMM estimators to address endogeneity.

Panel data methods offer several crucial advantages over purely cross-sectional or time-series analyses:

- Controls unobservables: Fixed/Random Effects capture time-invariant factors (e.g., institutions, culture) (Baltagi, 2008). For example, Fischer (1993) showed how inflation behaves differently under various policy regimes (inflation inertia).
- **Improved efficiency:** Pooling over time increases sample size, reducing variance inflation (Wooldridge, 2010).
- Captures dynamics: Lagged variables model persistence in macro indicators (Arellano & Bond, 1991).



# 2. Study Objectives

### **Compare Panel:**

Evaluate Pooled OLS, Fixed Effects, Random Effects, and Dynamic GMM models—assessing their performance via diagnostic tests (e.g., Hausman, AR(2), Sargan).

### **Empirical Application:**

Use a balanced panel (1980–2024) of annual macroeconomic indicators for 77 countries—both developed and developing—to analyze and forecast inflation dynamics.

### **Recommendations:**

Formulate clear recommendations for selecting the most appropriate panel data technique based on data characteristics and diagnostic outcomes.

### 3. Dataset Overview

The dataset includes annual data for 77 countries from 1980 to 2024, sourced from the IMF's World Economic Outlook (WEO).

• The target variable is PCPIPCH (Inflation, average consumer prices).

### **Explanatory variables used are:**

#### Public Finance:

- **GGSB\_NPGDP:** General government structural balance (% of GDP).
- **GGXWDG\_NGDP:** General government gross debt (% of GDP).

### Economic Output, Productivity & PPP:

• **PPPPC:** GDP per capita based on purchasing power parity (international dollars).

#### International Trade & Balance:

- TX RPCH: Volume of exports of goods and services (% change).
- TM\_RPCH: Volume of imports of goods and services (% change).

### **Savings & Investment:**

• **NID\_NGDP:** Total investment (% of GDP).



# 4.1. Missing Values (MICE-BR)

### **Iterative Imputation with Bayesian Ridge (MICE-BR)**

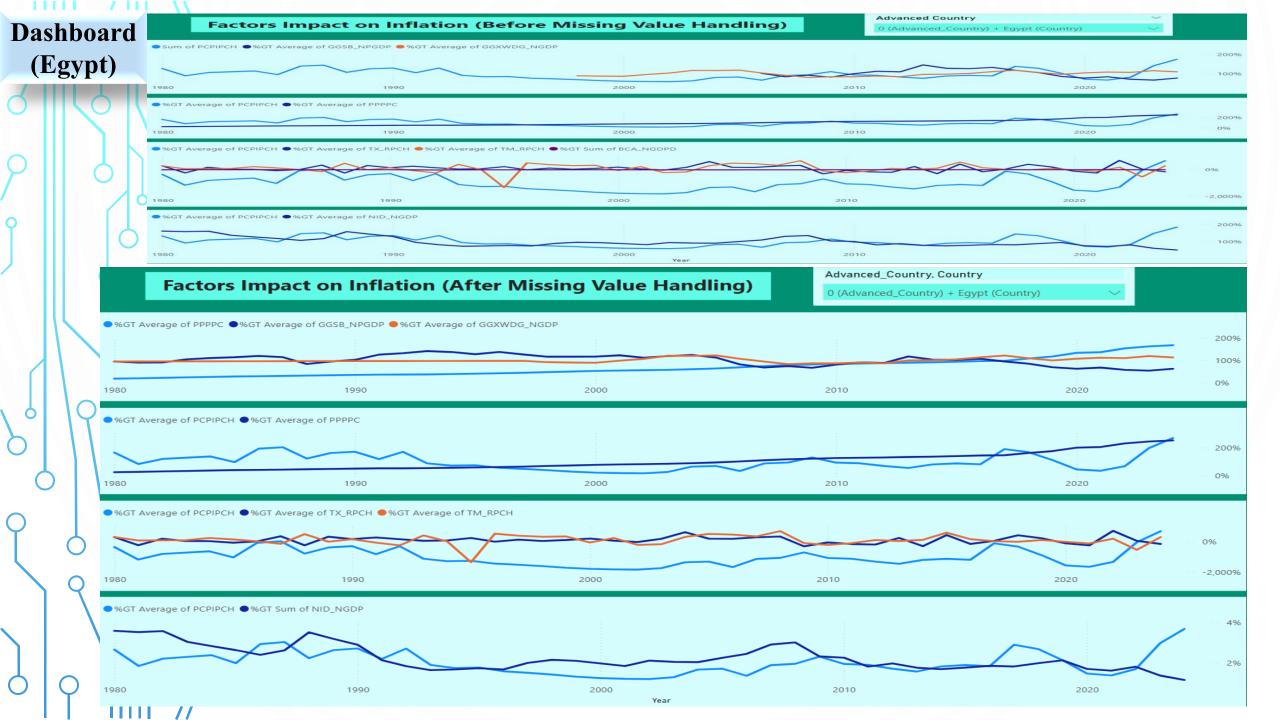
Treats each missing variable **as a regression** on the other observed variables within a **Bayesian** framework.

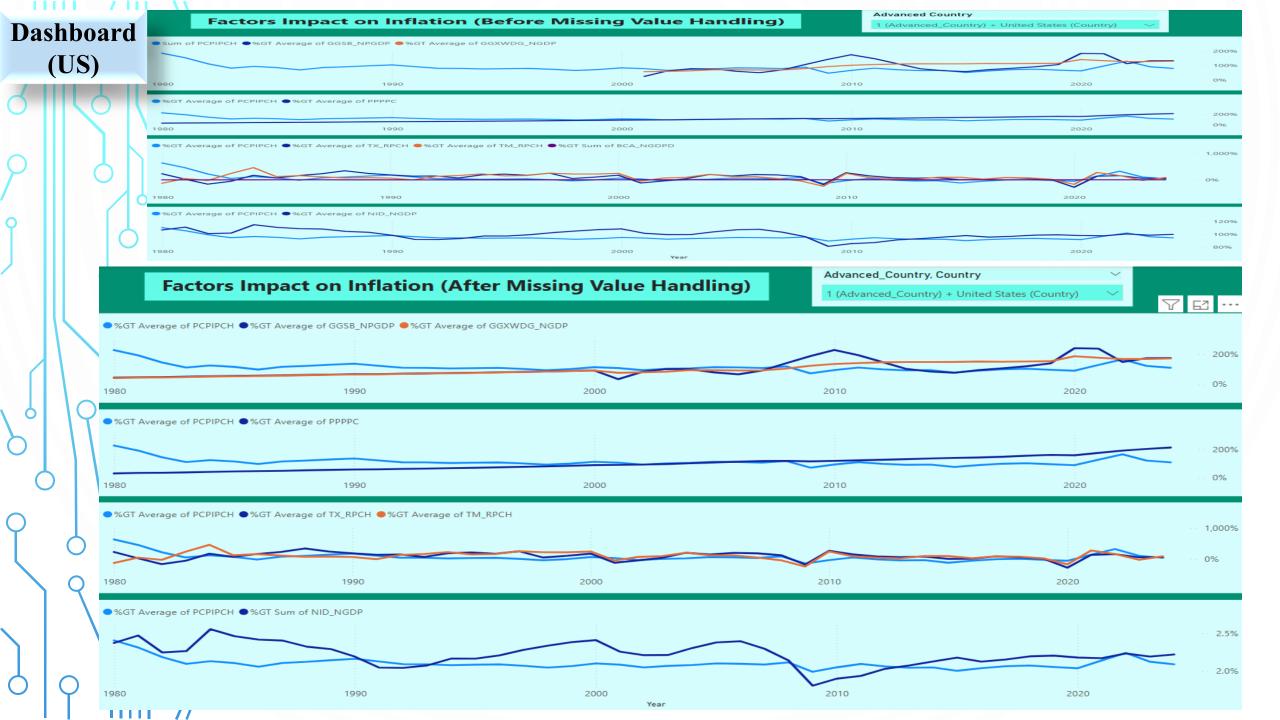
Applied separately for each country to preserve country-specific heterogeneity.

Imputes missing values without discarding the rich **relationships** among variables.

### **Python Code**

```
# Handle missing values for each country
def handle_missing_country(country):
    imputer = IterativeImputer(estimator=BayesianRidge(), max_iter=20,
    random_state=0, verbose=2)
        country[cols_with_na] = imputer.fit_transform(country[cols_with_na])
        return country
# Apply the imputation process by country
df_interpolated = df_panel_b.groupby('Country',
    group_keys=False).apply(handle_missing_country)
```



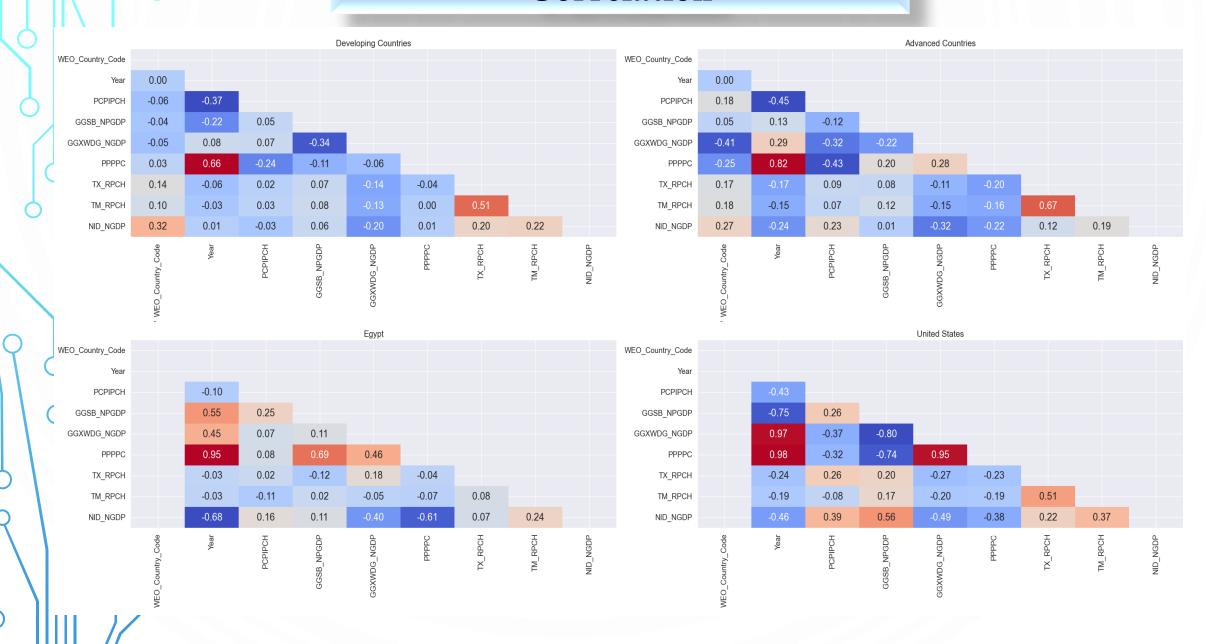


# 4.2 Correlation And (VIF)



Feature	VIF	Feature	VIF	Feature	VIF
GGSB_NPGDP	1.752526	GGXWDG_NGDP	3.403836	PPPPC	3.457779
TX_RPCH	2.082648	TM_RPCH	2.119305	NID_NGDP	4.473428

## Correlation



### 5. Panel Data Models

**Pooled OLS:** Ignores both country-specific and time-specific heterogeneity.

**Fixed Effects (FE):** Assumes country effects are time-invariant, country-specific characteristics (intercept for each country).

**Random Effects (RE):** Assumes country effects are randomly distributed (treated as random parameters).

### **Two-Step Difference GMM (Arellano–Bond):**

- Addresses endogeneity using internal instruments (e.g., past values).
- Adds **lagged** dependent variables to model persistence over time.
- Suitable for panels with many countries (N) and a few years (T) ( $N\gg T$ ).
- Robust to autocorrelation and heteroskedasticity with proper diagnostics.

# 5.1 (POLS), (FE), and(RE)

**The Pooled OLS model** explains approximately 45% of the variation in inflation rates across the sample, as indicated by the R-squared value of 0.4525.

The overall model is statistically significant (F = 454.25, p < 0.001), suggesting that the selected regressors jointly explain inflation variation across countries and time.

The Fixed Effects model explains approximately 46.9% of the within-country variation in inflation, as indicated by the R-squared value.

The model is statistically significant overall (F = 535.95, p < 0.001), confirming that the selected regressors jointly explain meaningful within-country variation in inflation rates.

The Random Effects model explains approximately 46.5% of the variation in inflation across countries and over time.

The model is statistically significant overall ( $\chi^2 = 3,262.87$ , p < 0.001), indicating strong joint explanatory power of the selected regressors.

### 5.2.A. Wald test: Pooled OLS vs Fixed Effects

 $H_0$ : All individual (country) effects are jointly equal to zero  $\rightarrow$  Pooled OLS is sufficient.

 $H_1$ : At least one individual effect is non-zero  $\rightarrow$  Fixed Effects model is preferred.

```
# Wald test: Pooled OLS vs Fixed Effects
waldtest(pooled_model, fe_model, test = "F")
```

**Results:** F-statistic = 9.48 (p-value = 0.0021)

**Decision:** Since the p-value < 0.05, we reject the null hypothesis.

**Conclusion:** The test confirms that individual (country-specific) effects are statistically significant, and therefore, the **Fixed Effects** model is preferred over Pooled OLS.

### 5.2.B. Hausman Test: Fixed Effects vs Random Effects

 $H_0$ : Random Effects model is consistent and efficient.

 $H_1$ : Random Effects model is inconsistent

# Hausman test: fixed vs random effects
phtest(fe\_model, re\_model)

**Results:** Chi-squared = 2.58 (p-value = 0.8597)

**Decision**: Since the p-value > 0.05, we fail to reject the null hypothesis.

**Conclusion:** There is no statistical evidence of correlation between the country-specific effects and the regressors, implying that the **Random Effects model is consistent** and preferred over the Fixed Effects model in this case.

✓ (A sample of countries and a long period of time)

## 5.3.A. Diagnostic Testing and Model Validity Assessment

### **Key Assumptions of the Random Effects Model:**

A) No heteroskedasticity (Breusch-Pagan and White Test):

 $H_0$ : Homoskedasticity (constant variance).  $H_1$ : Presence of heteroskedasticity.

**Breusch–Pagan Test**: Statistic = 13.62 (p-value = 0.0182)

White Test: Statistic = 18.01 (p-value = 0.0062)

**Decision:** Since both p-values are below 0.05, we reject the null hypothesis of homoskedasticity.

### B) No autocorrelation (Breusch-Godfrey Test):

 $H_0$ : No serial correlation.  $H_1$ : Serial correlation exists.

**Results:** Chi-squared = 751.38, p-value < 2.2e-16

**Decision:** With a p-value near zero, we reject the null hypothesis of no serial correlation in the residuals.

## 5.3.B. Diagnostic Testing and Model Validity Assessment

### C) Pesaran's Cross-sectional Dependence (CD) Test:

 $H_0$ : Cross-sectional independence.  $H_1$ : Cross-sectional dependence.

**Results**: z-statistic = 22.65 (p-value < 2.2e-16)

Decision: Reject the null hypothesis significant cross-sectional dependence exists.

D) Levin, Lin, and Chu (LLC) Panel Unit Root (Stationarity) Test:

 $H_0$ : Non-stationarity (unit root present).  $H_1$ : Stationarity.

**Results:** Overall statistic = -20.16 (p-value < 2.2e-16)

**Decision:** Reject the null hypothesis the variable is stationary (PCPIPCH rate series is stationary).

- ✓ We must use robust standard errors because: (Heteroskedasticity, Serial correlation, and Cross-sectional dependence).
- ✓ **Lagged dependent variables must be included because:** the series is stationary, which supports using a dynamic panel model like Difference GMM.

# **Correcting Standard Errors: Driscoll–Kraay Robust Estimation**

Variable	Estimate	Robust Std. Error	t-value	p-value	Significance
GGSB_NPGDP	-4.1547	4.3543	-0.95	0.3401	
GGXWDG_NGDP	0.3200	0.3864	0.83	0.4076	
PPPPC	-0.00059	0.00020	-2.91	0.0037	**
TX_RPCH	0.0169	0.2415	0.07	0.9442	
TM_RPCH	0.7598	0.2488	3.05	0.0023	**
NID_NGDP	0.0022	0.6100	0.0035	0.9972	

## 5.4. Two-Step Difference GMM (Arellano-bond)

### **Two-Step Difference GMM (Arellano–Bond):**

#### **Accounts for:**

- Endogeneity (lagged inflation).
- Autocorrelation (by differencing and higher-order serial correlation)
- Heteroskedasticity( by a robust weighting matrix)
- Omitted variable bias (by differencing away unobserved fixed effects)
- Efficiency (via robust two-step weighting)

# 5.4 Two-Step Difference GMM (Arellano-bond)

Variable	Estimate	Std. Error	z-value	p-value	Significance
lag(PCPIPCH, 1)	0.2741	0.0936	2.93	0.0034	**
GGSB_NPGDP	-3.2433	1.4750	-2.20	0.0279	*
GGXWDG_NGDP	0.2870	0.1456	1.97	0.0487	*
PPPPC	-0.00022	0.00019	-1.13	0.2593	
TX_RPCH	0.2467	0.3035	0.81	0.4162	
TM_RPCH	0.5278	0.2599	2.03	0.0423	*
NID_NGDP	-0.5358	0.3329	-1.61	0.1075	

# 5.5. Diagnostic Tests for the GMM Model

### **Key Assumptions of the GMM Model:**

### A) Joint Significance of Coefficients (Wald Test):

 $H_0$ : All slope coefficients are jointly zero.  $H_1$ : At least one coefficient is non-zero.

**Results:**  $\chi^2$  (7) = 660.07 (p-value < 0.001)

**Decision:** Reject the null hypothesis, the explanatory variables are jointly significant.

### B) Overidentifying Restrictions (Sargan Test):

 $H_0$ : All instruments are valid .  $H_1$ : At least one instrument is invalid.

**Results:**  $\chi^2 = 11.86$  (p-value = 0.457)

**Decision:** Fail to reject the null hypothesis, Instruments are valid.

### C) Arellano-Bond Test for First/ Second -Order Autocorrelation:

 $H_0$ : No serial correlation.  $H_1$ : Serial correlation exists.

**Results:** [AR (1)]: z = -0.99(p-value = 0.3199) & [AR (2)]: z = -0.58 (p-value = 0.5607)

Decision: Fail to reject null hypothesis, No serial correlation in the residuals. [AR (1)&(2)]

# 5.6. Conclusion: Model Comparison and Final Selection

After estimating and evaluating four model specifications—Pooled OLS, Fixed Effects, Random Effects, and Two-Step Difference GMM—we summarize the findings:

- Pooled OLS failed to account for country heterogeneity and produced biased estimates.
- Fixed Effects controlled unobserved heterogeneity but was inconsistent under endogeneity.
- Random Effects passed the Hausman test and provided a consistent structure but ignored dynamics and endogeneity.
- Difference GMM successfully addressed autocorrelation, heteroskedasticity, and endogeneity, and passed all diagnostic checks (Sargan, AR(1), AR(2)).

## 6. Recommendations and Future Work

Based on the findings, it is recommended that applied macroeconomic research and policy forecasting in inflation contexts prioritize dynamic panel estimators—particularly Two-Step Difference GMM—when dealing with persistent variables and potential endogeneity.

#### **Future Work:**

- Expansion of Dataset Coverage.
- Inclusion of Energy Price Indices.
- Extended Diagnostic Testing.
- Development and Integration of Machine Learning (ML) and Deep Learning (DL).

# **Appendix (Codes)**

(A): SQL Codes:-

**Dataset:** https://github.com/1145267383/Panal Data Inflation/tree/main/02-Dataset

Database: https://github.com/1145267383/Panal\_Data\_Inflation/blob/main/03-Clean\_Organize\_EDA/04-SQL.ipynb

(B): Python Codes:-

Clean and organize and EDA: https://github.com/1145267383/Panal\_Data\_Inflation/tree/main/03-Clean Organize EDA

**Descriptive and Correlation Analysis**: https://github.com/1145267383/Panal\_Data\_Inflation/tree/main/04-Descriptive\_Correlation\_Analysis

**Models:** https://github.com/1145267383/Panal\_Data\_Inflation/blob/main/05-Models\_Panel\_Data/01-Models\_Python.ipynb

(C): R Codes:-

Models: https://github.com/1145267383/Panal\_Data\_Inflation/blob/main/05-Models\_Panel\_Data/02-Models\_R.ipynb

### References

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