IEMS 5780 / IERG 4080 Building and Deploying Scalable Machine Learning Services

Lecture 5 - Recommender Systems

Albert Au Yeung 4th October, 2018

Agender

- Introduction
- Content-based Recommendation Systems
- Collaborative Filtering
 - User-based Neighbourhood Model
 - o Item-based Neighbourhood Model
 - Matrix Factorization
- Recommendation as Classification

- We make a lot of **decisions** every day
 - Transportation
 - o Restaurant reservation
 - Hotel reservation
 - Music
 - Movies
- We usually rely on some suggestions or recommendations
 - Family and friends
 - Supervisors, teachers, seniors
 - Experts
 - The general public (word-of-mouth)

Recommender Systems

What are the factors that affect our decisions?

- Our own **preferences** (of the content, the characteristics, the price, etc.)
- What do **most people like**? (which is the blockbuster movie recently?)
- What do **people around us like**? (friends and family)
- What do people **similar to us** like?

Example: Mobile App User Demographics

Gender (Male)					Age (33–100)			
Coef	Share	n	App name	Coef	Share	n	App name	
0.81	85 %	150	ESPN	0.53	80 %	42	Great Clips Online Check-in	
0.73	80 %	142	Geek - Smarter Shopping	0.48	53 %	1687	Email	
0.63	78 %	277	Tinder	0.46	58 %	318	New Words With Friends	
0.59	80 %	172	Fallout Shelter	0.44	80 %	65	BINGO Blitz	
0.56	86 %	106	WatchESPN	0.43	60 %	380	iHeartRadio - Music & Radi	
0.52	72 %	190	Clash of Clans	0.41	54 %	197	Field Agent	
0.52	97 %	41	Grindr - Gay chat, meet & date	0.40	55 %	690	Lookout Security & Antiviru	
0.49	84 %	96	Yahoo Fantasy Football & More	0.40	92 %	41	DoubleUCasino	
Gender (Female)				Age (18–32)				
-1.03	76 %	736	Pinterest	-1.17	78 %	1066	Snapchat	
-0.73	84 %	182	Etsy	-0.52	59 %	113	Perk Word Search	
-0.61	97 %	79	Period Tracker	-0.49	64 %	88	Summoners War	
-0.54	96 %	58	Period Calendar / Tracker	-0.46	59 %	98	Clash of Kings	
-0.50	76 %	346	Cartwheel by Target	-0.45	86 %	90	iFunny:)	
-0.49	66 %	258	Wish - Shopping Made Fun	-0.45	81 %	158	GroupMe	
-0.49	74 %	325	Checkout 51 - Grocery Coupons	-0.42	80 %	68	GIPHY for Messenger	
-0.45	74 %	178	Photo Grid - Collage Maker	-0.42	80 %	183	Vine	

Ref: You Are What Apps You Use: Demographic Prediction Based on User's Apps

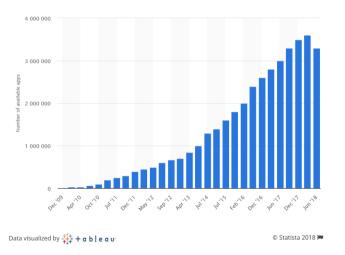
Example: Mobile App User Demographics

Married (Married)					Income (\geq \$50K)			
Coef	Share	n	App name	Coef	Share	n	App name	
0.55	67 %	200	Zillow Real Estate & Rentals	0.58	75 %	141	Fitbit	
0.44	67 %	622	Walmart	0.45	66 %	205	LinkedIn	
0.44	60 %	823	Pinterest	0.41	65 %	41	com.ws.dm	
0.44	74 %	39	Gospel Library	0.37	52 %	141	LG Android QuickMemo+	
0.40	59 %	91	USAA Mobile	0.37	58 %	191	Redbox	
0.40	80 %	63	ClassDojo	0.36	72 %	22	Like Parent	
0.38	60 %	123	ESPN	0.34	66 %	63	Peel Smart Remote	
0.37	82 %	28	Deer Hunter 2014	0.34	61 %	220	Yelp	
Married (Single)				Income (≤ \$40 K)				
-0.89	70 %	810	Snapchat	-0.43	66 %	136	Job Search	
-0.78	89 %	114	POF Free Dating App	-0.43	63 %	97	Security policy updates	
-0.73	85 %	219	Tinder	-0.37	78 %	23	Solitaire	
-0.66	98 %	69	OkCupid Dating	-0.35	67 %	79	Prize Claw 2	
-0.48	72 %	269	Tumblr	-0.34	72 %	51	ScreenPay- Get Paid to Unloa	
-0.42	72 %	205	SoundCloud - Music & Audio	-0.33	78 %	56	MeetMe	
-0.41	65 %	331	Uber	-0.33	62 %	77	Foursquare	
-0.41	89 %	69	MeetMe	-0.32	56 %	73	Microsoft Word	

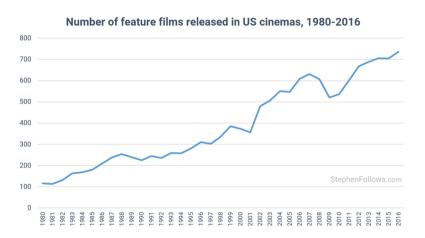
Ref: You Are What Apps You Use: Demographic Prediction Based on User's Apps

- There are **many** items out there for us to choose
 - Tens of thousands of movies and songs
 - o More than 1 million apps in the Android and iPhone app stores
 - Millions of books published every year
- We need more efficient way to filter information, and identify items most relevant to us
- On the other hand, producers also want to provide consumers things that they really want (targetted marketing)

Mobile Apps



Movies



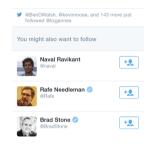
(https://stephenfollows.com/how-many-films-are-released-each-year/)

Solution: Recommender Systems

- Use computers and algorithms to process the huge amount of inforamtion and do the filtering for us
- Analyse the **tastes** and **preferences** of different people
- Analyse the **characteristics** of different items/products
- Generate personalized recommendation based on users' past activities and feedback
- Systems performing the above tasks are referred to as recommender systems / recommendation systems

Examples of Recommender Systems









- Music recommendation
- Suggested connections in social networks
- Recommended items in ecommerce Websites
- Recommended travel destinations and accommodations

• ...

How should recommendations be generated?

https://goo.gl/vz15y9

Common Strategies

Popularity

o Recommend items most people like

• Item Similarity

Recommend items that are similar to what the user has already shown interest

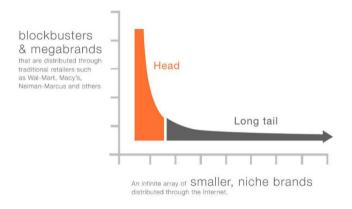
User Similarity

 Recommend items that are preferred by users who are similar the the target user in some ways

Diversity

o Recommend items that are least known to the uuser

The Long Tail



 $\frac{https://www.forbes.com/sites/robinlewis/2016/05/31/the-long-tail-theory-can-be-reality-for-traditional-megabrands/\#2b77afbc6372$

Assumptions

- Every user has his/her own interests / tastes / preferences
- Each user's preferences can be represented as a summary of what he/she has seen/read/watched/liked in the past
- A user will prefer something he or she is interested in
- We can compare the **content** or **characteristics** of the items
- Recommend items that are **similar** to what the user has consumed before

Two Steps

- 1. Learn user **preferences** (what does the user like?)
- 2. Find items that **match** these preferences

Problems

- 1. How do we **learn** user preferences?
- 2. How do we **represent** user interests?
- 3. How do we **represent** items?
- 4. How to measure **similarity**?

Similarity-based

Steps

- Define features to represent the items (e.g. bag-of-words, author, publish date/time, etc.)
- Construct user profile by the items liked by the user (e.g. average of feature vectors)
- Calculate **similarity** between user profile and the new items
- Return a ranked list of items
- What is important here is the user profile
 - How can we **represent** a user?
 - A user may have **multiple interests**, or his/her interests may **change over time**

Limitations of Content-based Methods

- Content (including meta-data) might not be available or enough in some domains
- It is difficult to represent some items by their 'content' (e.g. movies, books, music)
- Content-based methods tend to return very similar items

What is Collaborative Filtering (CF)?

• From Wikipedia:

In the newer, narrower sense, collaborative filtering is a method of making automatic predictions (filtering) about the interests of a user by collecting preferences or taste information from many users (collaborating). The underlying assumption of the collaborative filtering approach is that if a person A has the same opinion as a person B on an issue, A is more likely to have B's opinion on a different issue than that of a randomly chosen person.

Basic Idea

- Instead of relying on the content of the items, we can analyse people's tastes and preferences
- Each person is NOT totally different from another
- There are different **kinds** of people, for example:
 - People who like action movies
 - People who read literature
 - People who like spicy food
- By grouping **similar users**, we can recommend similar items to similar users
- This does not require a lot of information about the users and items themselves

Two Types of Collaborative Filtering

1. Memory-based

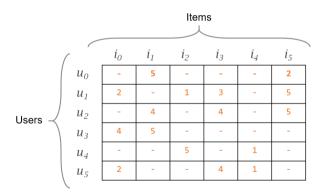
- Directly use ratings from similar users or items
- Also called **neighbourhood-based** methods

2. Model-based

- o Mathematical models are used to represent users, items and their relations
- o E.g. **matrix factorization**, Bayesian networks, probabilistic models

User-item Interaction

• In the following discussion, we assume that a user may **rate** an item on a **1 to 5** scale

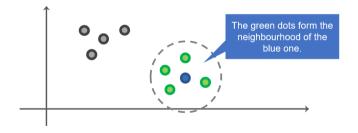


Memory-based Collaborative Filtering

Neighbourhood

What is neighbourhood?

- Consider again the vector space model
- Users and items can be represented as **vectors** in a high dimensional space
- More similar items/users will appear **closer** to each other



Neighbourhood Models

Two Types of Neighbourhood Models

1. User-based

- We consider **similar users**
- The neighbourhood of a user consists of users who like similar items

2. Item-based

- We consider **similar items**
- The neighbourhood of an item consists of items that are preferred by similar users

User-based Collaborative Filtering

• **Task**: Predict the **extent** to which user u likes item i

Procedures:

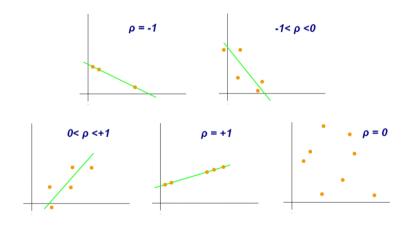
- \circ We have user u, and item i
- \circ Find a set of users who are similar to u and have rated i
- \circ Get the **average rating** on i given by this set of users
- o Do this for all items, come up with a **ranking** based on the predict rating

User-based Collaborative Filtering

- In doing user-based CF, we made the following assumptions:
 - o If users had similar tastes in the past, they should have similar tastes in the future
 - User preferences remain **stable and consistent** over time
- Furthermore, we need to define similarity
- Similarity
 - Should reflect how **close** the tastes and preferences of two users are
 - Similar users should assign similar ratings to the same set of items

Similarity - Pearson Correlation

• One way of computing similarity between two users is to use the **pearson correlation**



Similarity - Pearson Correlation

- *x*, *y*: users
- $r_{x,i}$: rating assigned to i by x
- I: the set of items rated by both x and y
- sim(x, y) has a value between -1 and 1

$$sim(x,y) = \frac{\sum_{i \in I} (r_{x,i} - \overline{r_x})(r_{y,i} - \overline{r_y})}{\sqrt{\sum_{i \in I} (r_{x,i} - \overline{r_x})^2} \sqrt{\sum_{i \in I} (r_{y,i} - \overline{r_y})^2}}$$

Similarity - Pearson Correlation

In Python, you can easily compute the correlation using the scipy module's pearsonr function

```
>>> from scipy.stats import pearsonr
>>> a = [5,2,1,4,3,1]
>>> b = [1,5,4,2,1,2]
>>> pearsonr(a,b)
(-0.59628479399994383, 0.21157899460007421)
>>>
>> a = [5,2,1,4,3,1]
>>> b = [4,3,1,5,4,2]
>>> pearsonr(a,b)
(0.85978530414910515, 0.028111919656069226)
>>>
```

Predicting Ratings

- How to predict a user's rating for an item?
- Use the equation below:

Similarity between x and u

Deviation from mean of ratings of user u

$$\operatorname{pred}(x,i) = \overline{r_x} + \frac{\sum_{u \in U} \operatorname{sim}(x,u) \times (r_{u,i} - \overline{r_u})}{\sum_{u \in U} \operatorname{sim}(x,u)}$$

Normalization

• Example: see 15-user-based-cf.ipynb

Limitations

Data sparsity

• When there are a lot of users and items, very few overlap between users

Does not scale

- When there are 10 million users, how can you generate all their neighbourhoods?
- Two users may have similar taste in one domain but very different taste in another

Item-based Collaborative Filtering

Procedures

- We have user u and item i
- Find a set of **items**, which are
 - \circ rated by u
 - \circ given **similar ratings** as i by other users
- $\bullet \;$ Get the ${\bf average} \; {\bf rating} \; {\bf of} \; {\bf this} \; {\bf set} \; {\bf of} \; {\bf items} \; {\bf given} \; {\bf by} \; u$
- ullet Use that as the predicted rating of i by u

Item-based Collaborative Filtering

- In doing **item-based CF**, we made the following **assumptions**:
 - If two items are given similar ratings by the users, they should have similar characteristics
- Consider movies:
 - Movies of the same genre, by the same director, or feature the same actor/actress will be assigned similar ratings
- Ref: <u>Amazon.com Recommendations: Item-to-Item Collaborative Filtering</u>

Predicting Ratings

ullet One way to implement item-based CF is to compute a **weighted combination of ratings** given by u to other items

Similarity between two items

Rating given by the user to other items

$$\operatorname{pred}(u,j) = \frac{\sum_{i \in I} \operatorname{sim}(j,i) \times r_{u,i}}{\sum_{i \in I} \operatorname{sim}(j,i)}$$

Normalization

Neighbourhood-based Collaborative Filtering

- Neighbourhood and recommended items are usually calculated offline
- In order to reduce the amount of computation needed, the size of the neighbourhood is usually limited
- Previous research shows that a neighbourhood size of **20-50** is quite enough
- Ref: <u>Empirical Analysis of Design Choices in Neighborhood-based Collaborative Filtering</u>
 <u>Algorithms</u>, Herlocker et al., 2002.

Food for Thought

TED Talk How Algorithms Shape Our World

TEDGlobal 2011, By Kevin Slavin

http://www.ted.com/talks/kevin slavin how algorithms shape our world.html

- What we have discussed so far are called memory-based collaborative filtering
- We have not trained any model that can be used to describe the relationship between inputs and outputs
- Memory-based models are easy to implement, but usually are NOT very accurate and NOT scalable
- Instead, we can consider a **machine learning approach** to the task of recommendation:
 - Create a model that explains how ratings are generated, or how items are ranked
 - Use past data to **train/optimize** the parameters of the model

We can roughly categorize model-based CF into two types:

Matrix Factorization Approach

- Assume that there are latent factors that determine how users rate items
- Decompose the user-item matrix using matrix factorization techniques

Classification Approach

- o Consider the task of recommendation as a **classification** problem
- For each given pair of user and item, we determine whether the user will be interested in the item (binary classification)
- Can take into account contextual information and implicit feedbacks

Parameter Optimization

- Training machine learning models usually means optimizing parameters in the model using the training data
- Each model is characterized by a set of **parameters**
- Consider linear regression as an example:

$$y = b_0 + b_1 x_1 + b_2 x_2 + \ldots + b_n x_n$$

- Each b_i is a parameter of the model
- How exactly do we find the most suitable values of these parameters given the training data?

Parameter Optimization

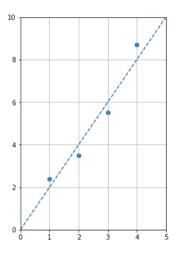
- In some cases, we can find a solution analytically
 - The solution can be represented by a equation
 - \circ The best parameters can be obtained by substituting the training data X and y into the equation
- However, in many cases, the model is complicated and we cannot do that analytically
- Another approach: trial and error
 - 1. Initialize the paraemeters randomly
 - 2. Use the model to **generate predictions** for the training data
 - 3. Computer the **error** of the predictions
 - 4. Use the error to **adjust** the parameters
 - 5. Go to Step 1 if model is not good enough

- Let's consider a very simple example
- We want to learn a linear model y = mx
- Our training data:

$$\circ X = (1, 2, 3, 4)$$

 $\circ y = (2.4, 3.5, 5.5, 8.7)$

- Obviously the value of m can be determined analytically
- Let's try our **gradient descent** on this example



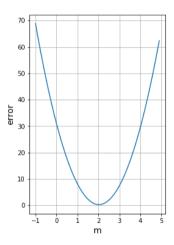
- To perform gradient descent, we need to first have an error function that allows us to
 understand how much error we are making using current values of the parameters (also called
 objective function or loss function)
- Our error function:

$$egin{aligned} error &= rac{1}{N} \sum_{i=1}^N (y_i - \hat{y}_i)^2 \ &= rac{1}{N} \sum_{i=1}^N (y_i - mx_i)^2 \end{aligned}$$

- where N is number of training samples
- (note that we use the **mean squared error** in this case)

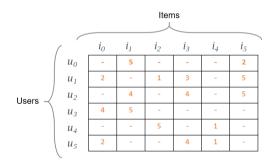
- The objective is to adjust the value of our parameter
 m such that next time the error will be smaller
- By adjusting we mean either increase or decrease its value
- To know to which direction we should adjust m, we need to know the gradient of the error
- In our case:

$$rac{\partial e}{\partial m} = rac{1}{N} \sum_{i=1}^N (-2x_i y_i + 2m x_i^2)$$



- ullet Once we know the gradient, we know how to adjust m
- If gradient is **positive**, we need to **reduce** *m*
- If gradient is **negative**, we need to **increase** m
- We use a hyperparameter called the learning rate to determine how much do we adjust m
 each time
 - o If we change the value too much, we may **miss** the optimal value
 - o If we cannge the value too little, we may never arrive at the optimal value
- Implementation in Python: 15-gradient-descent-example.ipynb

- Recall that in recommender systems, we usually deal with a matrix of user-item ratings
- In **memory-based methods**, we directly compute a prediction based on the other ratings
- In model-based methods, we come up with a model of how ratings are generated
- Matrix factorization is a commonly used model-based methods in recommendations



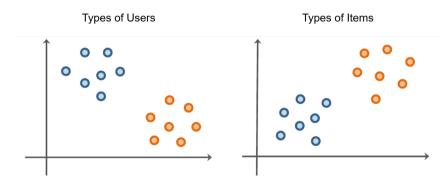
Matrix Factorization - Basic Idea

- We assume that users and items can be grouped into different types
- Take **movies** as an example:
 - Some users like action movies, while some like romantic movies
 - Some movies are romantic, while some are exciting and full of suspense



Challenge

- How can we discover **types** of users and items from our data?
- Clustering?



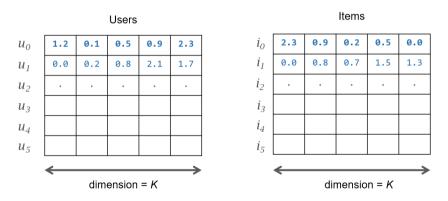
- Clustering users and items separately does NOT work well
 - We need to **manually inspect** the meaning of each group (cluster)
 - We do not know which user groups correspond to which item groups
 - There is no guarantee that we will obtain exact correspondence between user groups and item groups
 - E.g. there might be a group of users who like animations, but animations might be grouped under different clusters according to their content

- We can approach this problem differently
- ullet Let's assume in advance that there are K different types of users and items
- ullet We use **vectors of length** K to represent users and items
- Each component (factor) in a vector represents the extent to which the user/item belongs to that type

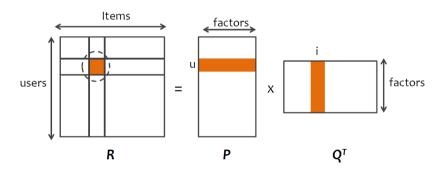
$$user_1 = (0.0, 0.1, 0.2, 1.2, 2.3)$$

 $user_2 = (3.1, 0.0, 0.1, 0.2, 0.4)$
 $item_1 = (0.2, 0.9, 1.5, 0.2, 0.8)$
 $item_2 = (1.5, 2.3, 0.0, 0.9, 0.0)$

• If we consider all the **users** and **items** in our recommender system, we can represent all of them using two different **matrices**



- In such a model, the rating on item i given by user u is generated by computing the **dot product** of the corresponding user and item **vectors**
- This is equivalent to multiplying the (transpose of) the item matrix with the user matrix

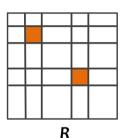


• Usually, we are given the matrix R, **matrix factorization** is the process of finding P and Q such that PxQ^T gives an approximation of R

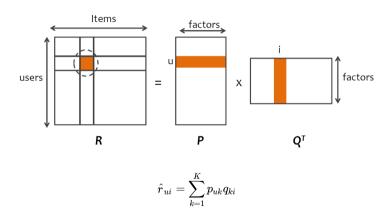
$$P \times Q^T = \hat{R} \approx R$$

- Very often *R* is **incomplete** (e.g. 99% of the cells are empty),
- Therefore, we have to estimate the values in P and Q, instead of solving for exact values The number of factors K reflects the complexity of our model

- In matrix factorization, our target is to come up with P and Q, the two **factor matrices** whose product approximates the user-item rating matrix R
- When we say approximate, we are talking about the known values in R.
- If we can approximate the known values well, our predictions of the unknown values will be accurate



• Let's focus on **one rating** at a time



• Our goal is to find all p_{ik} and q_{kj} such that

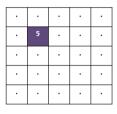
$$\sum_{k=1}^{K} p_{uk} q_{ki} pprox r_{ui}$$

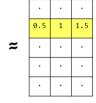
- Our data only contain the values of **some** r_{ij}
- How can we determine the values of all p_{ik} and q_{kj} ?

Basic Idea:

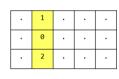
- We first initialize P and Q with some **random values**
- We measure our **error**, i.e. how far we are from the **true** values in R
- ullet We update the values in P and Q based on the error we computed
- **Repeat** the steps above until the error is sufficiently small
- In other words, we can use **gradient descent**

• Example:





Х



• The **dot product** of the user vector and the item vector is:

$$0.5 \times 1 + 1 \times 0 + 1.5 \times 2 = 3.5$$

• We can then compute our **error**

• Error is give by:

$$e_{ui} = r_{ui} - \hat{r}_{ui} = r_{ui} - \sum_{k=1}^K p_{uk} q_{ki}$$

• Squared error:

$$e_{ui}^2 = (r_{ui} - \hat{r}_{ui})^2 = (r_{ui} - \sum_{k=1}^K p_{uk} q_{ki})^2$$

• The **machine learning** problem here is to optimize all p's and q's such that e_{ui}^2 is **minimized**

$$egin{aligned} e_{ui}^2 &= (r_{ui} - \hat{r}_{ui})^2 = (r_{ui} - \sum_{k=1}^K p_{uk} q_{ki})^2 \ &rac{\partial e_{ui}^2}{\partial p_{uk}} = -2(r_{ui} - \sum_{k=1}^K p_{uk} q_{ki}) q_{ki} = -2e_{ui} q_{ki} \ &rac{\partial e_{ui}^2}{\partial q_{ki}} = -2(r_{ui} - \sum_{k=1}^K p_{uk} q_{ki}) p_{uk} = -2e_{ui} p_{uk} \end{aligned}$$

• Having obtained the gradients, we can construct our **update rules** as follows:

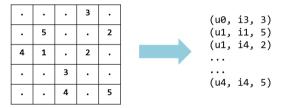
$$p'_{uk}=p_{uk}-lpha(-2e_{ui}q_{ki})=p_{uk}+2lpha e_{ui}q_{ki}$$

$$q_{ki}'=q_{ki}-lpha(-2e_{ui}p_{uk})=q_{ki}+2lpha e_{ui}p_{uk}$$

- where α is the **learning rate**
- p'_{uk} and q'_{ki} are the **new values**

Training Data

- Note that we only optimize P and Q using the **known values** in the matrix R
- We can consider transforming the user-item rating matrix into a list of tuples: (user, item, rating):



Beyond Rating Predictions

- In many other cases, we do NOT always have ratings (explicit feedback) from the users
- Instead, we would have **implicit feedback** from the users on the items
 - The user purchased an item
 - The user clicked on an advertisement
 - The user viewed the details of an item
- Implicit feedbacks can also be considered as (weaker) indications that the user is interested
 in the items
- We can still populate a user-item matrix using implicit feedbacks
- Ref: <u>Collaborative Filtering for Implicit Feedback Datasets</u> (Hu et al. 2008)

- Besides rating prediction using matrix factorization, recommendation can also be considered
 as a classification task
- Ultimately, we want to determine the **probability that a user is interested / likes / wants to purchase an item**
- Besides the explicit/implicit feedbacks, there are actually a lot of things we can consider as
 features
 - o date/time when the users visit the Website
 - the browsing history of the users
 - the various characteristics of the items (e.g. actors/actresses in a movie, storyline of a fiction)
 - Whether the user is using a PC or a smartphone
 - **interactions** between user and item features

- Recommendation can be considered as a binary classification problem
 - Whether the user will **click** on an advertisement
 - Whether the user will **purchase** the item
 - Whether the user will **download** the mobile app
- Common classification models can be used
 - Logistic regression
 - Support vector machines
 - Decision trees / Random forests
- The most important things in this approach are the features --> Feature Engineering

- To train a classifier, you need both **positive** and **negative** samples
- However, very often you don't know what the user DOES NOT like
- A user hasn't interacted with an item DOES NOT mean that he/she is not interested in an item
- Negative sampling
 - For each positive feedback you have, randomly sample items that the user has not interacted with
 - Use these items as **negative** samples
 - Can also weight each sample differently (how?)

End of Lecture 5