## HIT — Cryptography — Homework 1

## September 4, 2014

**Problem 1.** Show that the shift, Mono-Alphabetic sub., and Vigenère ciphers are all trivial to break using a known-plaintext attack. How much known plaintext (how many characters) is needed to completely recover the key for each of the ciphers? (show how to break the cipher)

**Problem 2.** Show that the shift, Mono-Alphabetic sub., and Vigenère ciphers are all trivial to break using a chosen-plaintext attack. How much plaintext (how many characters) must be encrypted to completely recover the key? (show your chosen plaintext)

**Problem 3.** Prove or refute: For every encryption scheme that is perfectly secret it holds that for every distribution over the message space  $\mathcal{M}$ , every  $m, m' \in \mathcal{M}$ , and every  $c \in \mathcal{C}$ :

$$\Pr[M = m | C = c] = \Pr[M = m' | C = c].$$

**Problem 4.** Study conditions under which the shift, mono-alphabetic sub., and Vigenère cipher ciphers are perfectly secret:

- (a) Prove that if only a single character is encrypted, then the shift cipher is perfectly secret.
- (b) What is the largest plaintext space M you can find for which the mono-alphabetic sub. cipher provides perfect secrecy?
- (c) Show how to use the Vigenère cipher to encrypt any word of length t so that perfect secrecy is obtained (note: you can choose the length of the key). Prove your answer.