CCA-Secure and Authentication Encryption

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Outline

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Recall Security Against CCA

The CCA indistinguishability experiment $\mathsf{PrivK}^{\mathsf{cca}}_{\mathcal{A},\Pi}(n)$:

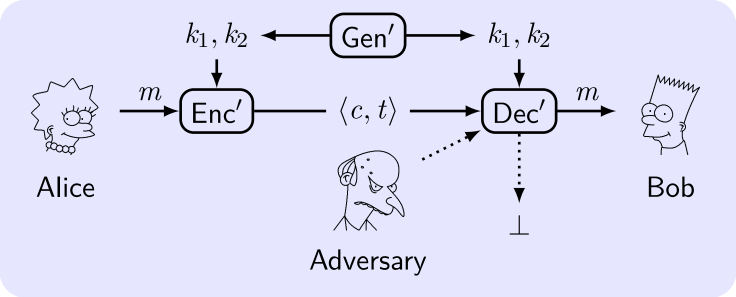
1. $k \leftarrow \mathsf{Gen}(1^n)$.
2. $\mathcal{A}$ is given input 1^n and oracle access $\mathcal{A}^{\mathsf{Enc}_k(\cdot)}$ and $\mathcal{A}^{\mathsf{Dec}_k(\cdot)}$, outputs m_0, m_1 of the same length.
3. a random bit $b \leftarrow \{0,1\}$ is chosen. Then $c \leftarrow \mathsf{Enc}_k(m_b)$ is given to $\mathcal{A}$.
4. $\mathcal{A}$ continues to have oracle access **except for** c, outputs b'.
5. If $b' = b$, $\mathcal{A}$ succeeded $\mathsf{PrivK}^{\mathsf{cca}}_{\mathcal{A},\Pi} = 1$, otherwise 0.

Definition 1

Π has **indistinguishable encryptions under a CCA (CCA-secure)** if $\forall$ PPT $\mathcal{A}$, $\exists$ negl such that

$$\Pr\left[\mathsf{PrivK}^{\mathsf{cca}}_{\mathcal{A},\Pi}(n) = 1\right] \le \frac{1}{2} + \mathsf{negl}(n).$$

Constructing CCA-Secure Encryption Schemes



Construction 2

$\Pi_E = (\mathsf{Gen}_E, \mathsf{Enc}, \mathsf{Dec})$, $\Pi_M = (\mathsf{Gen}_M, \mathsf{Mac}, \mathsf{Vrfy})$. Π':

- $\mathsf{Gen}'(1^n)$: $k_1 \leftarrow \mathsf{Gen}_E(1^n)$ *and* $k_2 \leftarrow \mathsf{Gen}_M(1^n)$.
- $\mathsf{Enc}'_{k_1,k_2}(m)$: $c \leftarrow \mathsf{Enc}_{k_1}(m)$, $t \leftarrow \mathsf{Mac}_{k_2}(c)$ *and output* $\langle c, t\rangle$.
- $\mathsf{Dec}'_{k_1,k_2}(\langle c, t\rangle)$: *If* $\mathsf{Vrfy}_{k_2}(c, t) \stackrel{?}{=} 1$, *output* $\mathsf{Dec}_{k_1}(c)$; *otherwise output "failure"* $\perp$.

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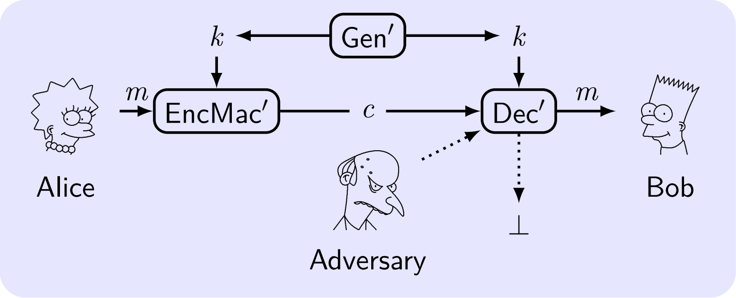
Message Transmission Scheme



- **Key-generation** algorithm outputs $k \leftarrow \mathsf{Gen}'(1^n)$.
  $k = (k_1, k_2)$. $k_1 \leftarrow \mathsf{Gen}_E(1^n)$, $k_2 \leftarrow \mathsf{Gen}_M(1^n)$.
- **Message transmission** algorithm is derived from $\mathsf{Enc}_{k_1}(\cdot)$ and $\mathsf{Mac}_{k_2}(\cdot)$, outputs $c \leftarrow \mathsf{EncMac}'_{k_1,k_2}(m)$.
- **Decryption** algorithm is derived from $\mathsf{Dec}_{k_1}(\cdot)$ and $\mathsf{Vrfy}_{k_2}(\cdot)$, outputs $m \leftarrow \mathsf{Dec}'_{k_1,k_2}(c)$ or $\perp$.
- **Correctness requirement**: $\mathsf{Dec}'_{k_1,k_2}(\mathsf{EncMac}'_{k_1,k_2}(m)) = m$.

Defining Secure Message Transmission

The secure message transmission experiment $\mathsf{Auth}_{\mathcal{A},\Pi'}(n)$:

1. $k = (k_1, k_2) \leftarrow \mathsf{Gen}'(1^n)$.
2. $\mathcal{A}$ is given input 1^n and oracle access to EncMac'_k, and outputs $c \leftarrow \mathsf{EncMac}'_k(m)$.
3. $m := \mathsf{Dec}'_k(c)$. $\mathsf{Auth}_{\mathcal{A},\Pi'}(n) = 1 \iff m \neq \perp \wedge\ m \notin \mathcal{Q}$.

Definition 3

Π' achieves **authenticated communication** if $\forall$ PPT $\mathcal{A}$, $\exists$ negl such that

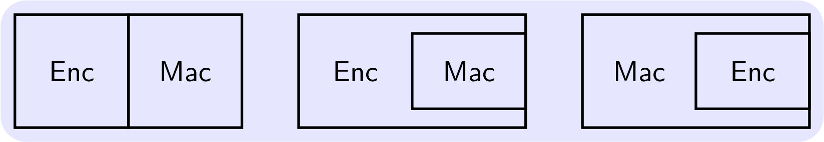
$$\Pr[\mathsf{Auth}_{\mathcal{A},\Pi'}(n) = 1] \leq \mathsf{negl}(n).$$

Definition 4

Π' is **secure (authenticated encryption)** if it is both CCA-secure and also achieves authenticated communication.[1]

[1] CPA security and integrity imply CCA security.

Combining Encryption and Authentication



- **Encrypt-and-authenticate** (e.g., SSH):

$$c \leftarrow \mathsf{Enc}_{k_1}(m),\ t \leftarrow \mathsf{Mac}_{k_2}(m).$$

- **Authenticate-then-encrypt** (e.g, SSL):

$$t \leftarrow \mathsf{Mac}_{k_2}(m),\ c \leftarrow \mathsf{Enc}_{k_1}(m\|t).$$

- **Encrypt-then-authenticate** (e.g, IPsec):

$$c \leftarrow \mathsf{Enc}_{k_1}(m),\ t \leftarrow \mathsf{Mac}_{k_2}(c).$$

Analyzing Security of Combinations

All-or-nothing: Reject any combination for which there exists even a single counterexample is insecure.

- **Encrypt-and-authenticate**: $\mathsf{Mac}'_k(m) = (m, \mathsf{Mac}_k(m))$.
- **Authenticate-then-encrypt**:
  - $\text{Trans} : 0 \to 00; 1 \to 10/01$; Enc' uses CTR mode; $c = \mathsf{Enc}'(\mathsf{Trans}(m \| \mathsf{Mac}(m)))$.
  - Flip the first two bits of c and verify whether the ciphertext is valid. $10/01 \to 01/10 \to 1$, $00 \to 11 \to \perp$.
  - If valid, the first bit of message is 1; otherwise 0.
  - For any MAC, this is not CCA-secure.
- **Encrypt-then-authenticate**:
  Decryption: If $\mathsf{Vrfy}(\cdot) = 1$, then $\mathsf{Dec}(\cdot)$; otherwise output $\perp$.

Remarks on Secure Message Transmission

- Authentication may leak the message.
- Secure message transmission implies CCA-security. The opposite direction is not necessarily true.
- Different security goals should always use different keys.
  - otherwise, the message may be leaked if $\mathsf{Mac}_k(c) = \mathsf{Dec}_k(c)$.
- Implementation may destroy the security proved by theory.
  - **Attack with padding oracle** (in TLS 1.0):
    Dec return two types of error: padding error, MAC error.
    Adv. learns last bytes if no padding error with guessed bytes.
  - **Attack non-atomic dec.** (in SSH Binary Packet Protocol):
    Dec (1)decrypt length field; (2)read packets as specified by the length; (3)check MAC.
    Adv. (1)send c; (2)send l packets until "MAC error" occurs; (3)learn $l = \mathsf{Dec}(c)$.