

# Inductive and Analytical Learning

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## **Inductive learning**

Hypothesis fits data

Statistical inference

Requires little prior knowledge

Syntactic inductive bias

## **Analytical learning**

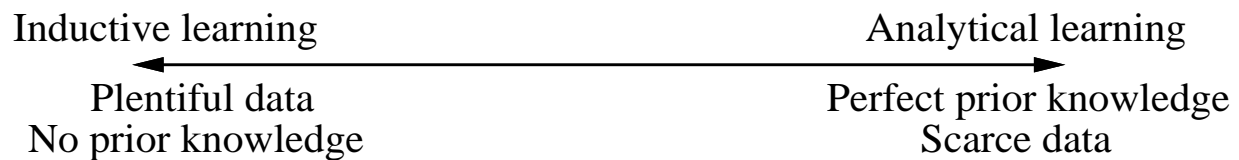
Hypothesis fits domain theory

Deductive inference

Learns from scarce data

Bias is domain theory

## What We Would Like



General purpose learning method:

- No domain theory  $\rightarrow$  learn as well as inductive methods
- Perfect domain theory  $\rightarrow$  learn as well as PROLOG-EBG
- Accomodate arbitrary and unknown errors in domain theory
- Accomodate arbitrary and unknown errors in training data

Domain theory:

Cup  $\leftarrow$  Stable, Lifiable, OpenVessel

Stable  $\leftarrow$  BottomIsFlat

Lifiable  $\leftarrow$  Graspable, Light

Graspable  $\leftarrow$  HasHandle

OpenVessel  $\leftarrow$  HasConcavity, ConcavityPointsUp

Training examples:

	Cups				Non-Cups				
BottomIsFlat	✓	✓	✓	✓	✓	✓	✓		✓
ConcavityPoints Up	✓	✓	✓	✓	✓		✓	✓	
Expensive	✓		✓				✓	✓	
Fragile	✓	✓			✓	✓		✓	✓
HandleOnTop					✓		✓		
HandleOnSide	✓			✓				✓	
HasConcavity	✓	✓	✓	✓	✓		✓	✓	✓
HasHandle	✓			✓	✓		✓	✓	
Light	✓	✓	✓	✓	✓	✓	✓	✓	
MadeOfCeramic	✓				✓		✓	✓	
MadeOfPaper				✓				✓	
MadeOfStyrofoam		✓	✓			✓			✓

# KBANN

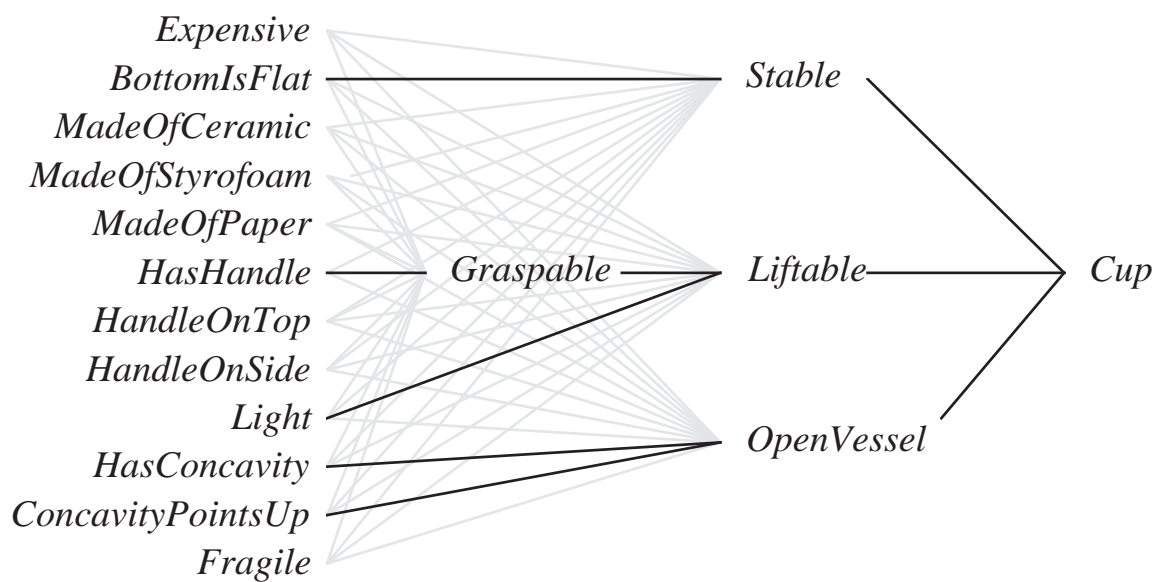
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KBANN (data  $D$ , domain theory  $B$ )

1. Create a feedforward network  $h$  equivalent to  $B$
2. Use BACKPROP to tune  $h$  to fit  $D$

# Neural Net Equivalent to Domain Theory

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# Creating Network Equivalent to Domain Theory

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Create one unit per horn clause rule (i.e., an AND unit)

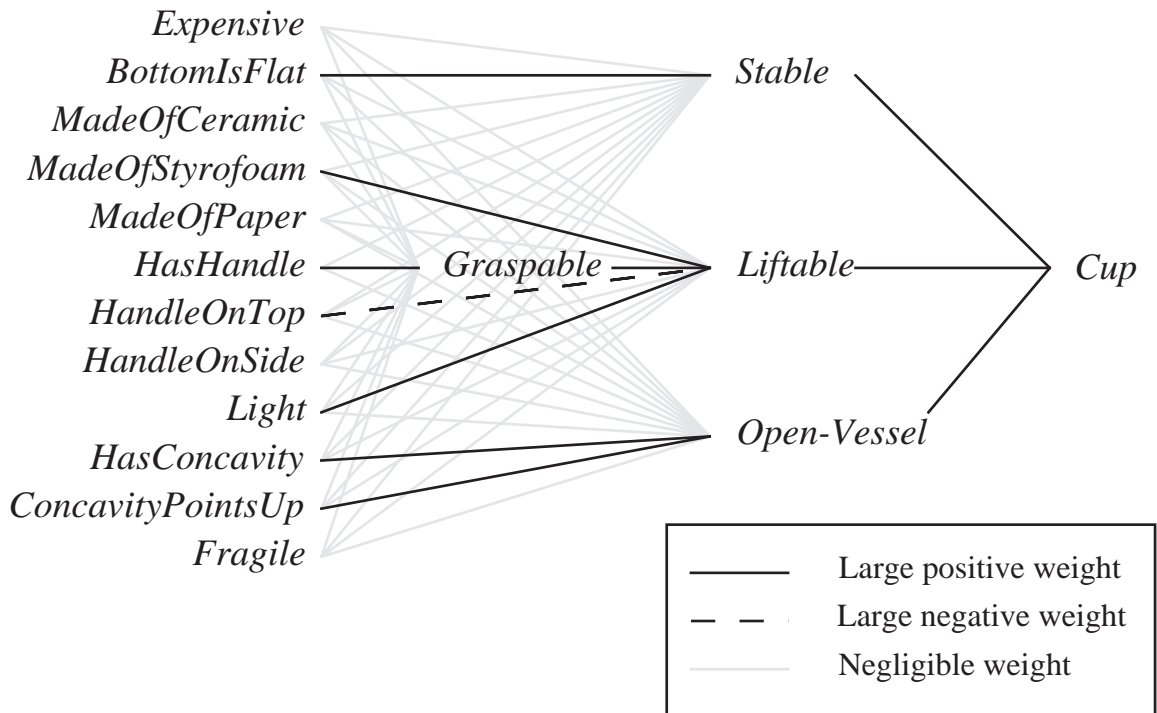
- Connect unit inputs to corresponding clause antecedents
- For each non-negated antecedent, corresponding input weight  $w \leftarrow W$ , where  $W$  is some constant
- For each negated antecedent, input weight  $w \leftarrow -W$
- Threshold weight  $w_0 \leftarrow -(n - .5)W$ , where  $n$  is number of non-negated antecedents

Finally, add many additional connections with near-zero weights

$$Liftable \leftarrow Graspable, \neg Heavy$$

# Result of refining the network

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# KBANN Results

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Classifying promoter regions in DNA  
leave one out testing:

- Backpropagation: error rate 8/106
- KBANN: 4/106

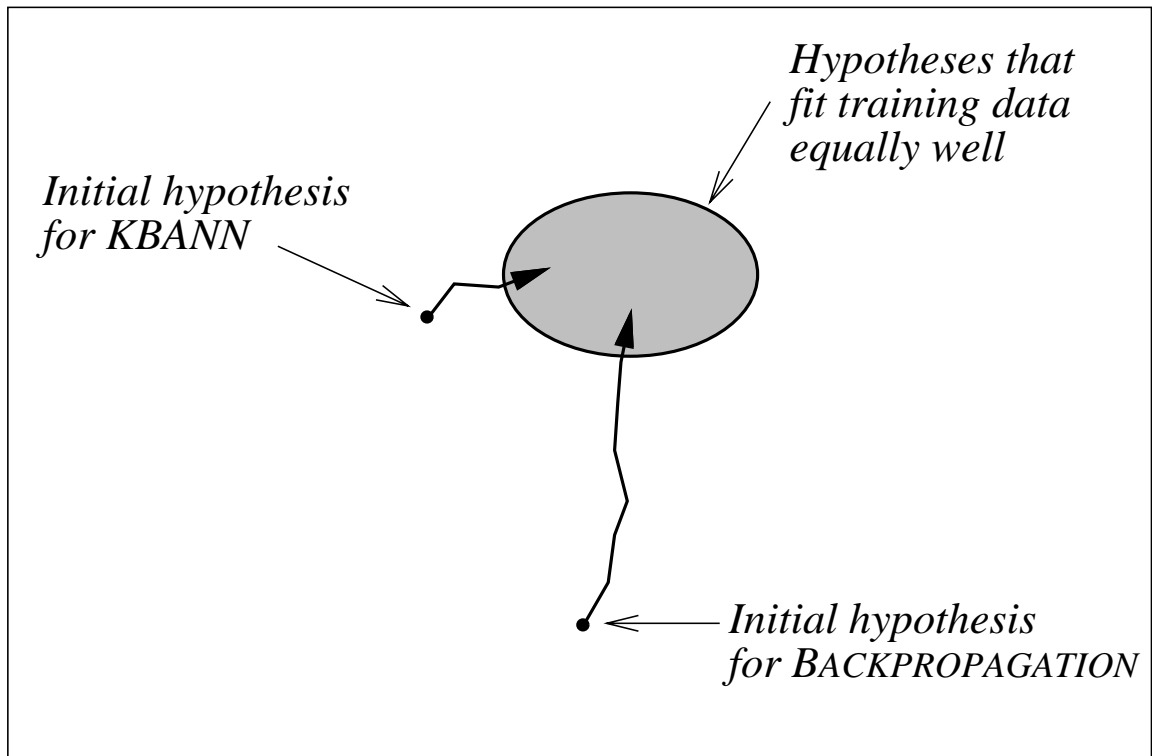
Similar improvements on other classification,  
control tasks.



# Hypothesis space search in KBANN

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## Hypothesis Space



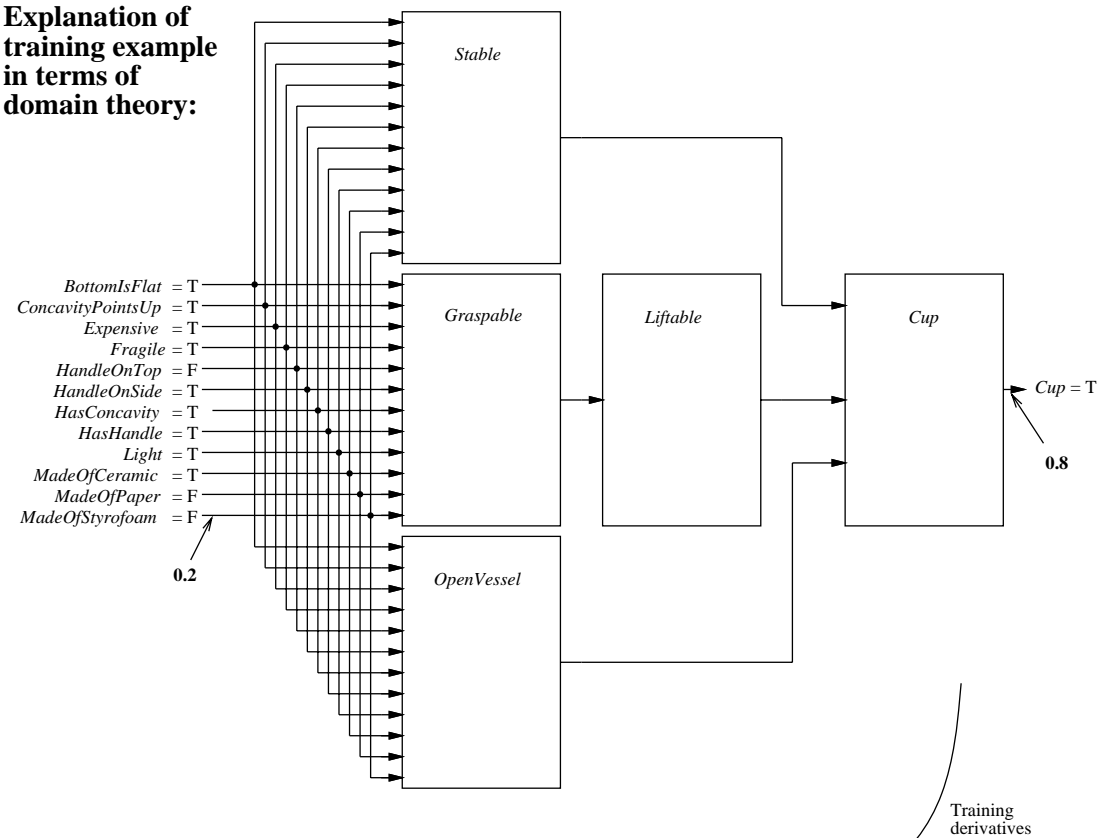
# EBNN

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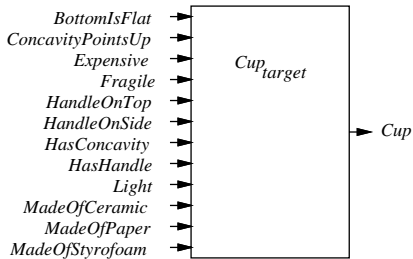
Key idea:

- Previously learned approximate domain theory
- Domain theory represented by collection of neural networks
- Learn target function as another neural network

**Explanation of training example in terms of domain theory:**



**Target network:**



## Modified Objective for Gradient Descent

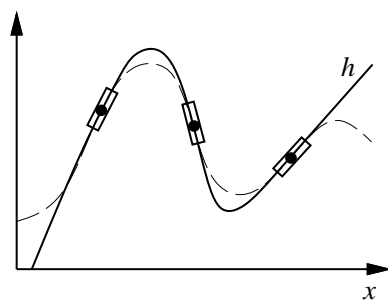
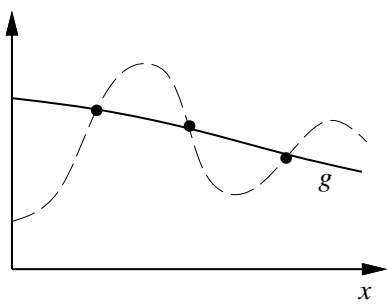
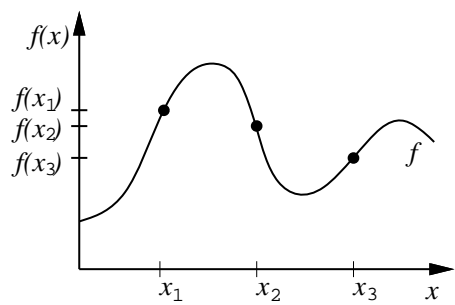
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$$E = \sum_i \left[ (f(x_i) - \hat{f}(x_i))^2 + \mu_i \sum_j \left( \frac{\partial A(x)}{\partial x^j} - \frac{\partial \hat{f}(x)}{\partial x^j} \right)^2_{(x=x_i)} \right]$$

where

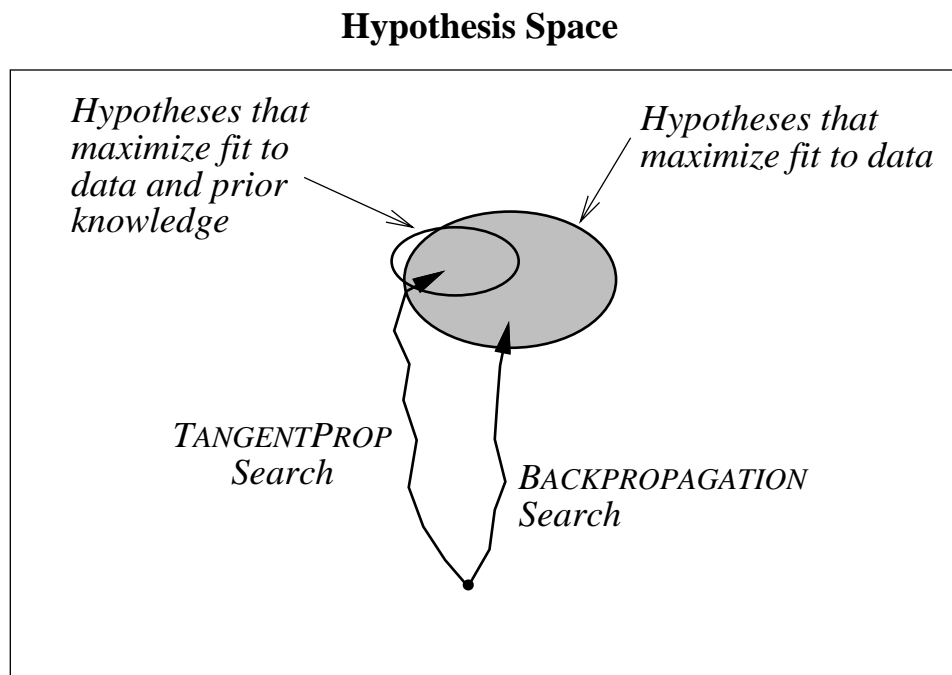
$$\mu_i \equiv 1 - \frac{|A(x_i) - f(x_i)|}{c}$$

- $f(x)$  is target function
- $\hat{f}(x)$  is neural net approximation to  $f(x)$
- $A(x)$  is domain theory approximation to  $f(x)$



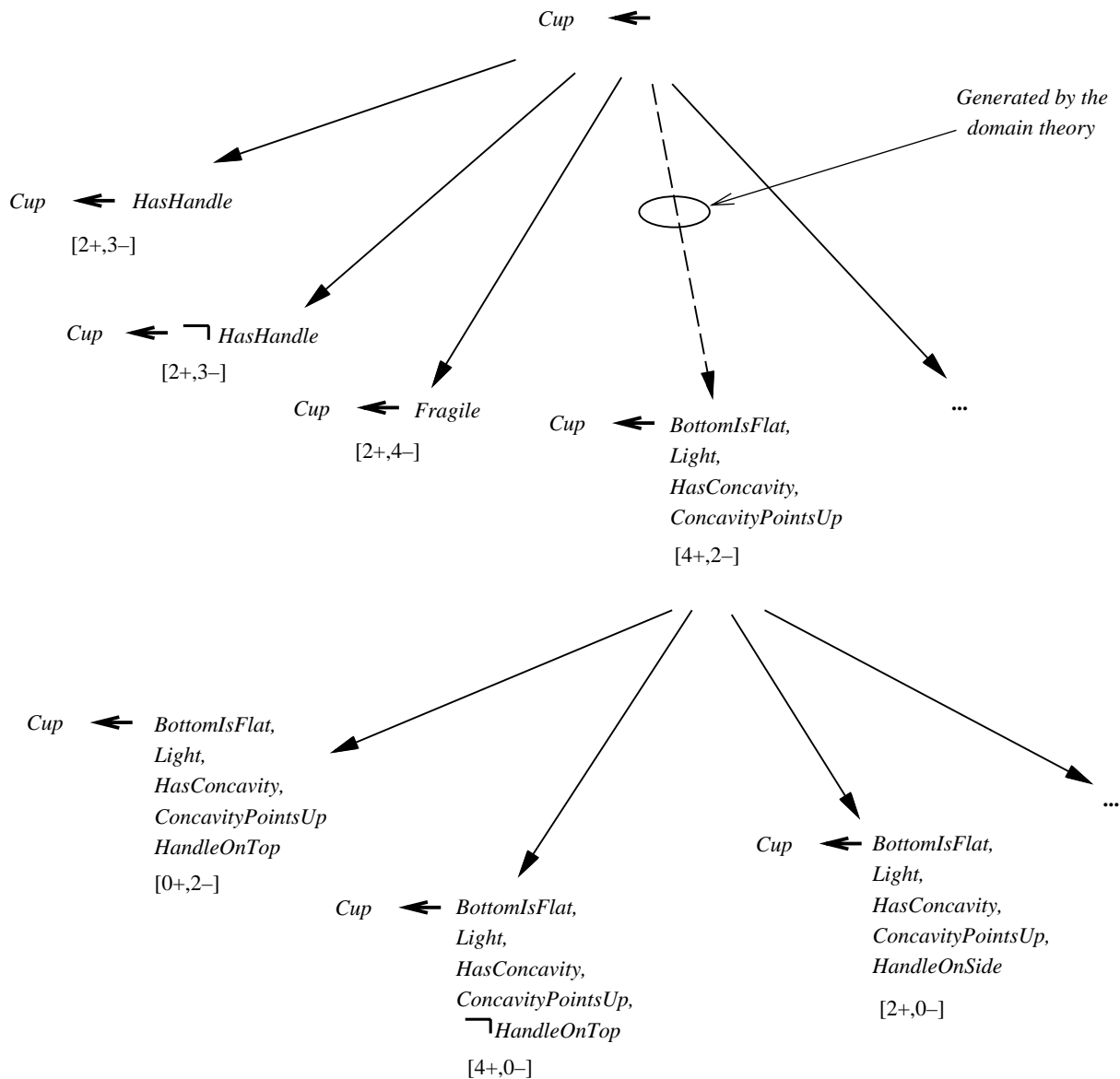
# Hypothesis Space Search in EBNN

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# Search in FOCL

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# FOCL Results

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Recognizing legal chess endgame positions:

- 30 positive, 30 negative examples
- FOIL: 86%
- FOCL: 94% (using domain theory with 76% accuracy)

NYNEX telephone network diagnosis

- 500 training examples
- FOIL: 90%
- FOCL: 98% (using domain theory with 95% accuracy)