

# A Crush Course On Cryptography

Yu Zhang

Harbin Institute of Technology

Cryptography, Autumn, 2020

# What cryptography is and is not

Cryptography is:

- A tremendous tool
- The basis for many security mechanisms
- Secure communication:
  - web traffic: HTTPS (SSL/TLS)
  - wireless traffic: 802.11i WPA2 (and WEP), GSM, Bluetooth
  - encrypting files on disk: EFS, TrueCrypt
  - content protection: DVD (CSS), Blu-ray (AACs)
  - user authentication

Cryptography is **NOT**:

- The solution to all security problems
- Reliable unless implemented and used properly
- Something you should try to invent yourself

# What cryptography can and can't do

“No one can guarantee 100% security. But we can work toward 100% risk acceptance. . . . Strong cryptography can withstand targeted attacks up to a point—the point at which it becomes easier to get the information some other way. . . . The good news about cryptography is that we already have the algorithms and protocols we need to secure our systems. The bad news is that that was the easy part; implementing the protocols successfully requires considerable expertise. . . . Security is different from any other design requirement, because functionality does not equal quality.”

– By Bruce Schneier 1997

# Rubber-hose Cryptanalysis

## A CRYPTO NERD'S IMAGINATION:

HIS LAPTOP'S ENCRYPTED.  
LET'S BUILD A MILLION-DOLLAR  
CLUSTER TO CRACK IT.

NO GOOD! IT'S  
4096-BIT RSA!

BLAST! OUR  
EVIL PLAN  
IS FOILED!



## WHAT WOULD ACTUALLY HAPPEN:

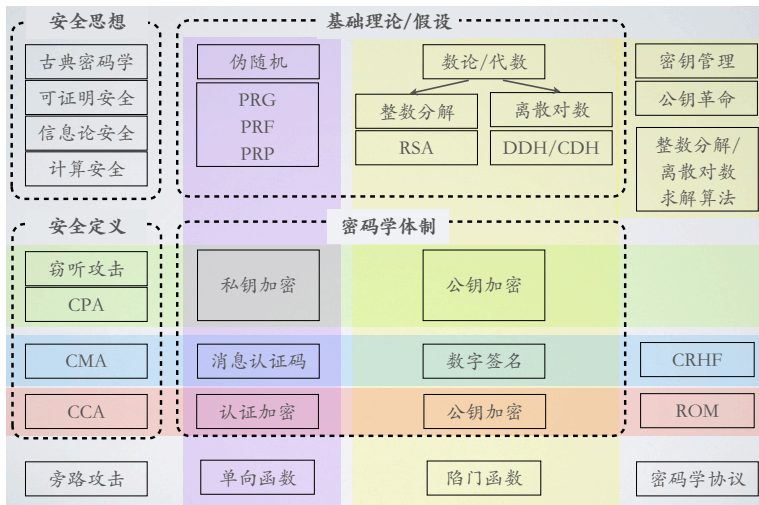
HIS LAPTOP'S ENCRYPTED.  
DRUG HIM AND HIT HIM WITH  
THIS \$5 WRENCH UNTIL  
HE TELLS US THE PASSWORD.

GOT IT.



- Classic cryptography, Perfect Secrets
- Private Key Encryption, MAC, Block Cipher, OWF
- Number Theory, Factoring and Discrete Log
- Key Management, Public Key, Digital Signature
- TPD, Random Oracle Model
- Cryptographic Protocols (Many magics here)

# Syllabus [in Chinese]



# We will learn from Turing Award recipients

- 1995 M. Blum
- 2000 A. Yao
- 2002 R. Rivest, A. Shamir, L. Adleman
- 2012 S. Micali, S. Goldwasser
- 2013 L. Lamport
- 2015 M. E. Hellman, W. Diffie

# Securing Key vs Obscuring Algorithm

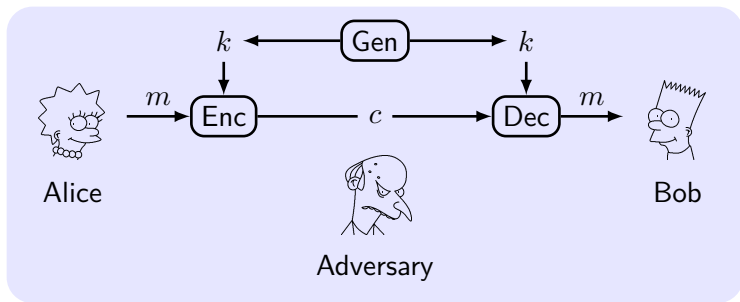
- Easier to maintain secrecy of a short key
- In case the key is exposed, easier for the honest parties to change the key
- In case many pairs of people, easier to use the same algorithm, but different keys

## Kerckhoffs's principle

*The cipher method must not be required to be secret, and it must be able to fall into the hands of the enemy without inconvenience.*



# The Syntax of Encryption



- key  $k \in \mathcal{K}$ , plaintext (or message)  $m \in \mathcal{M}$ , ciphertext  $c \in \mathcal{C}$
- **Key-generation** algorithm  $k \leftarrow \text{Gen}$
- **Encryption** algorithm  $c := \text{Enc}_k(m)$
- **Decryption** algorithm  $m := \text{Dec}_k(c)$
- **Encryption scheme:**  $\Pi = (\text{Gen}, \text{Enc}, \text{Dec})$
- **Basic correctness requirement:**  $\text{Dec}_k(\text{Enc}_k(m)) = m$

# One-Time Pad (Vernam's Cipher)

- $\mathcal{M} = \mathcal{K} = \mathcal{C} = \{0, 1\}^\ell$ .
- Gen chooses a  $k$  randomly with probability exactly  $2^{-\ell}$ .
- $c := \text{Enc}_k(m) = k \oplus m$ .
- $m := \text{Dec}_k(c) = k \oplus c$ .

## Theorem 1

*The one-time pad encryption scheme is perfectly-secret.*

# Definition of 'Perfect Secrecy'

**Intuition:** An adversary knows the probability distribution over  $\mathcal{M}$ .  $c$  should have no effect on the knowledge of the adversary; the *a posteriori* likelihood that some  $m$  was sent should be no different from the *a priori* probability that  $m$  would be sent.

## Definition 2

$\Pi$  over  $\mathcal{M}$  is **perfectly secret** if for every probability distribution over  $\mathcal{M}$ ,  $\forall m \in \mathcal{M}$  and  $\forall c \in \mathcal{C}$  for which  $\Pr[C = c] > 0$ :

$$\Pr[M = m|C = c] = \Pr[M = m].$$

**Simplify:** non-zero probabilities for  $\forall m \in \mathcal{M}$  and  $\forall c \in \mathcal{C}$ .

**Is the below scheme perfectly secret?**

For  $\mathcal{M} = \mathcal{K} = \{0, 1\}$ ,  $\text{Enc}_k(m) = m \oplus k$ .

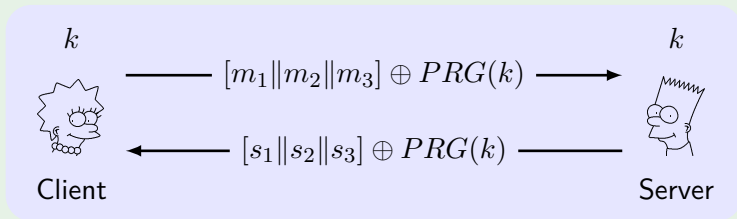
# Two Time Pad: Real World Cases

Only used once for the same key, otherwise

$$c \oplus c' = (m \oplus k) \oplus (m' \oplus k) = m \oplus m'.$$

Learn  $m$  from  $m \oplus m'$  due to the redundancy of language.

## MS-PPTP (Win NT)

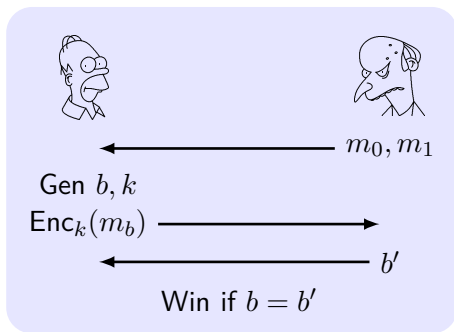


Improvement: use two keys for C-to-S and S-to-C separately.

# Eavesdropping Indistinguishability Experiment

The eavesdropping indistinguishability experiment  $\text{PrivK}_{\mathcal{A}, \Pi}^{\text{eav}}(n)$ :

- 1  $\mathcal{A}$  is given input  $1^n$ , outputs  $m_0, m_1$  of the same length
- 2  $k \leftarrow \text{Gen}(1^n)$ , a random bit  $b \leftarrow \{0, 1\}$  is chosen. Then  $c \leftarrow \text{Enc}_k(m_b)$  (challenge ciphertext) is given to  $\mathcal{A}$
- 3  $\mathcal{A}$  outputs  $b'$ . If  $b' = b$ ,  $\text{PrivK}_{\mathcal{A}, \Pi}^{\text{eav}} = 1$ , otherwise 0



# Defining Private-key Encryption Security

## Definition 3

$\Pi$  has **indistinguishable encryptions in the presence of an eavesdropper** if  $\forall$  PPT  $\mathcal{A}$ ,  $\exists$  a negligible function  $\text{negl}$  such that

$$\Pr \left[ \text{PrivK}_{\mathcal{A}, \Pi}^{\text{eav}}(n) = 1 \right] \leq \frac{1}{2} + \text{negl}(n),$$

where the probability is taken over the random coins used by  $\mathcal{A}$ .

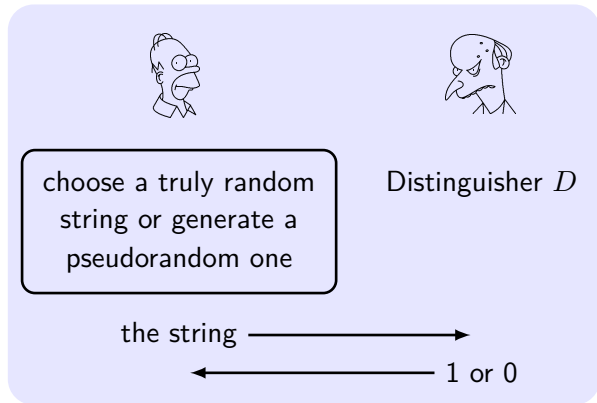
# Conceptual Points of Pseudorandomness

- True randomness can not be generated by a describable mechanism
- Pseudorandom looks truly random for the observers who don't know the mechanism
- No fixed string can be “pseudorandom” which refers to a distribution
- Q: is it possible to definitively prove randomness?



# Intuition for Defining Pseudorandom

**Intuition:** Generate a long string from a short truly random seed, and the pseudorandom string is indistinguishable from truly random strings.





# Definition of Pseudorandom Generators

## Definition 4

A deterministic polynomial-time algorithm  $G : \{0, 1\}^n \rightarrow \{0, 1\}^{\ell(n)}$  is a **pseudorandom generator (PRG)** if

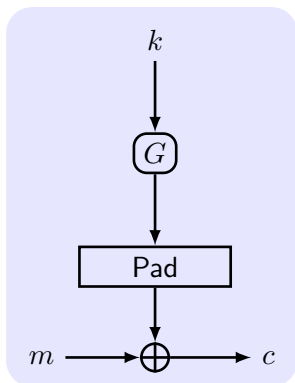
- 1 (Expansion:)  $\forall n, \ell(n) > n$ .
- 2 (Pseudorandomness):  $\forall$  PPT distinguishers  $D$ ,

$$|\Pr[D(r) = 1] - \Pr[D(G(s)) = 1]| \leq \text{negl}(n),$$

where  $r$  is chosen *u.a.r* from  $\{0, 1\}^{\ell(n)}$ , the **seed**  $s$  is chosen *u.a.r* from  $\{0, 1\}^n$ .  $\ell(\cdot)$  is the **expansion factor** of  $G$ .

- Pseudorandomness means being **next-bit unpredictable**,  
 $G$  passes all next bit tests  $\iff G$  passes all statistical tests.
- **Existence:** Under the weak assumption that *one-way functions* exists, or  $\mathcal{P} \neq \mathcal{NP}$

# A Secure Fixed-Length Encryption Scheme



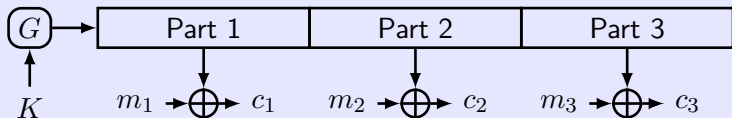
## Construction 5

- $|G(k)| = \ell(|k|)$ ,  $m \in \{0, 1\}^{\ell(n)}$ .
- Gen:  $k \in \{0, 1\}^n$ .
- Enc:  $c := G(k) \oplus m$ .
- Dec:  $m := G(k) \oplus c$ .

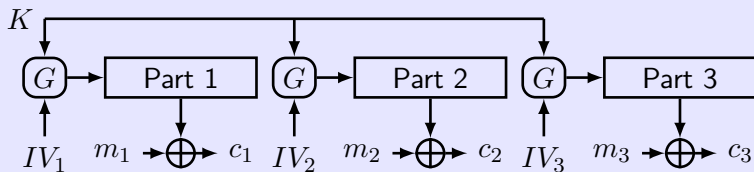
## Theorem 6

*This fixed-length encryption scheme has indistinguishable encryptions in the presence of an eavesdropper.*

# Secure Multiple Encryptions Using a Stream Cipher



*Synchronized Mode*



*Unsynchronized Mode*

Initial vector  $IV$  is chosen *u.a.r* and public

Q: which mode is better in your opinion?

Keys (the  $IV$ -key pair) for multiple enc. must be independent

### Attacks on 802.11b WEP

Unsynchronized mode:  $\text{Enc}(m_i) := \langle IV_i, G(IV_i \| k) \oplus m_i \rangle$

- Length of  $IV$  is 24 bits, repeat  $IV$  after  $2^{24} \approx 16\text{M}$  frames
- On some WiFi cards,  $IV$  resets to 0 after power cycle
- $IV_i = IV_{i-1} + 1$ . For RC4, recover  $k$  after 40,000 frames

# Chosen-Plaintext Attacks (CPA)

**CPA:** the adversary has the ability to obtain the encryption of plaintexts of its choice

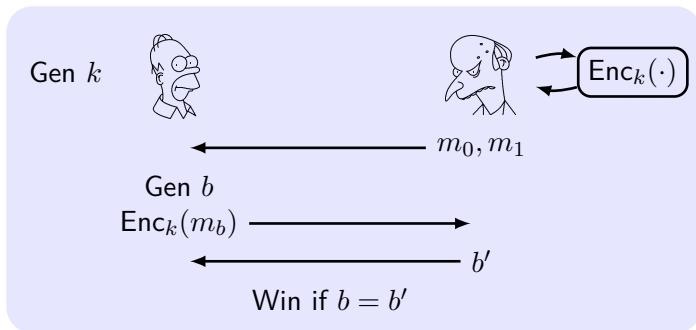
## A story in WWII

- Navy cryptanalysts believe the ciphertext “AF” means “Midway island” in Japanese messages
- But the general did not believe that Midway island would be attacked
- Navy cryptanalysts sent a plaintext that the freshwater supplies at Midway island were low
- Japanese intercepted the plaintext and sent a ciphertext that “AF” was low in water
- The US forces dispatched three aircraft carriers and won

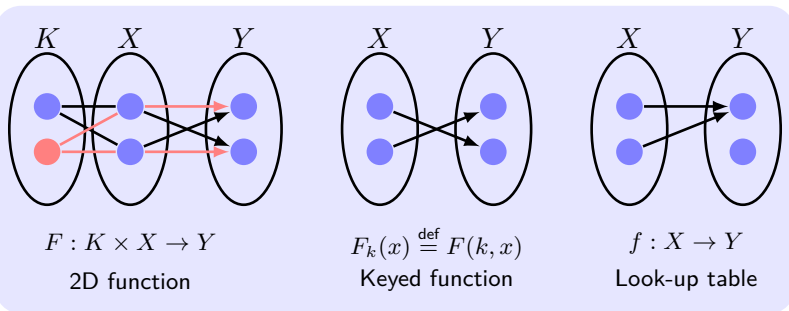
# Security Against CPA

The CPA indistinguishability experiment  $\text{PrivK}_{\mathcal{A}, \Pi}^{\text{cpa}}(n)$ :

- 1  $k \leftarrow \text{Gen}(1^n)$
- 2  $\mathcal{A}$  is given input  $1^n$  and **oracle access**  $\mathcal{A}^{\text{Enc}_k(\cdot)}$  to  $\text{Enc}_k(\cdot)$ , outputs  $m_0, m_1$  of the same length
- 3  $b \leftarrow \{0, 1\}$ . Then  $c \leftarrow \text{Enc}_k(m_b)$  is given to  $\mathcal{A}$
- 4  $\mathcal{A}$  **continues to have oracle access** to  $\text{Enc}_k(\cdot)$ , outputs  $b'$
- 5 If  $b' = b$ ,  $\mathcal{A}$  succeeded  $\text{PrivK}_{\mathcal{A}, \Pi}^{\text{cpa}} = 1$ , otherwise 0

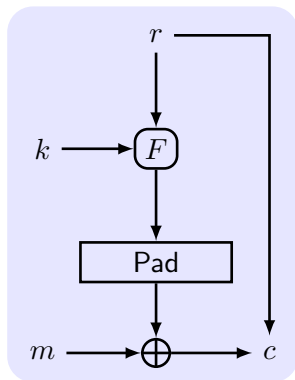


# Concepts on Pseudorandom Functions



- **Keyed function**  $F : \{0, 1\}^* \times \{0, 1\}^* \rightarrow \{0, 1\}^*$   
 $F_k : \{0, 1\}^* \rightarrow \{0, 1\}^*, F_k(x) \stackrel{\text{def}}{=} F(k, x)$
- **Look-up table**  $f : \{0, 1\}^n \rightarrow \{0, 1\}^n$  with size = ? bits
- **Function family**  $\text{Func}_n$ : all functions  $\{0, 1\}^n \rightarrow \{0, 1\}^n$ .  
 $|\text{Func}_n| = 2^{n \cdot 2^n}$
- **Length Preserving:**  $\ell_{\text{key}}(n) = \ell_{\text{in}}(n) = \ell_{\text{out}}(n)$

# CPA-Security from Pseudorandom Function



## Construction 7

- Fresh random string  $r$ .
- $F_k(r)$ :  $|k| = |m| = |r| = n$ .
- Gen:  $k \in \{0, 1\}^n$ .
- Enc:  $s := F_k(r) \oplus m$ ,  
 $c := \langle r, s \rangle$ .
- Dec:  $m := F_k(r) \oplus s$ .

## Theorem 8

If  $F$  is a PRF, this fixed-length encryption scheme  $\Pi$  is CPA-secure.



# Pseudorandom Permutations

- **Bijection:**  $F$  is one-to-one and onto
- **Permutation:** A bijective function from a set to itself
- **Keyed permutation:**  $\forall k, F_k(\cdot)$  is permutation
- $F$  is a bijection  $\iff F^{-1}$  is a bijection

## Definition 9

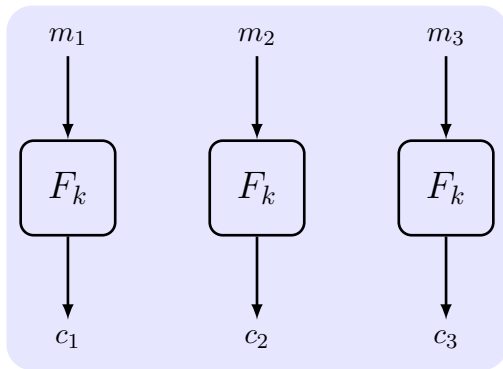
An efficient, keyed permutation  $F$  is a **strong pseudorandom permutation (PRP)** if  $\forall$  PPT distinguishers  $D$ ,

$$\left| \Pr[D^{F_k(\cdot), F_k^{-1}(\cdot)}(1^n) = 1] - \Pr[D^{f(\cdot), f^{-1}(\cdot)}(1^n) = 1] \right| \leq \text{negl}(n),$$

where  $f$  is chosen *u.a.r* from the set of permutations on  $n$ -bit strings.

**If  $F$  is a pseudorandom permutation then is it a PRF?**

# Electronic Code Book (ECB) Mode

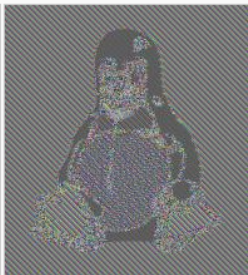


- Q: is it indistinguishable in the presence of an eavesdropper?
- Q: can  $F$  be any PRF?

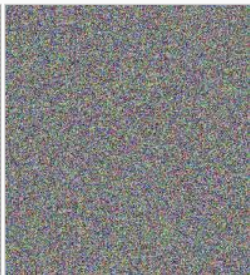
# Attack on ECB mode



Original image

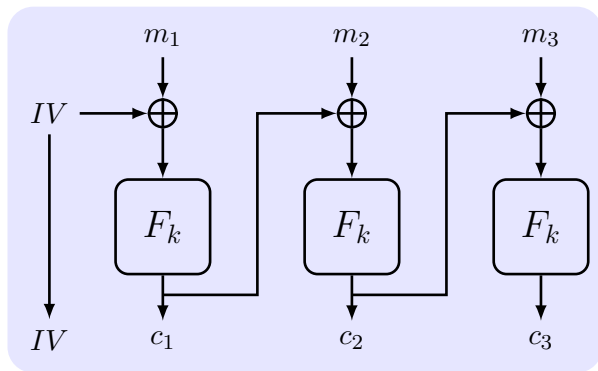


Encrypted using ECB mode



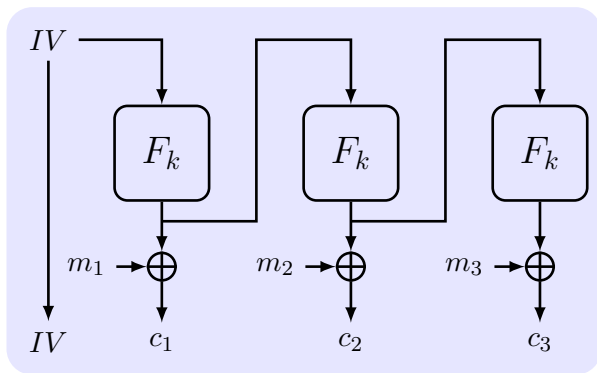
Modes other than ECB result in  
pseudo-randomness

# Cipher Block Chaining (CBC) Mode

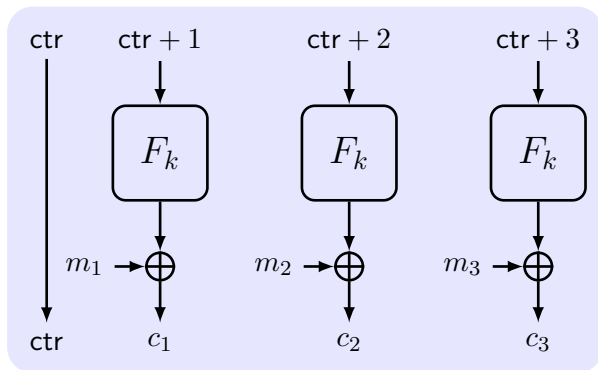


- $IV$ : initial vector, a fresh random string.

# Output Feedback (OFB) Mode



# Counter (CTR) Mode



# IV Should Not Be Predictable

If  $IV$  is predictable, then CBC/OFB/CTR mode is not CPA-secure.

## Bug in SSL/TLS 1.0

$IV$  for record  $\#i$  is last CT block of record  $\#(i - 1)$ .

## API in OpenSSL

```
void AES_cbc_encrypt (  
    const unsigned char *in,  
    unsigned char        *out,  
    size_t                length,  
    const AES_KEY         *key,  
    unsigned char        *ivec,    User supplies IV  
    AES_ENCRYPT or AES_DECRYPT);
```

# Security Against CCA

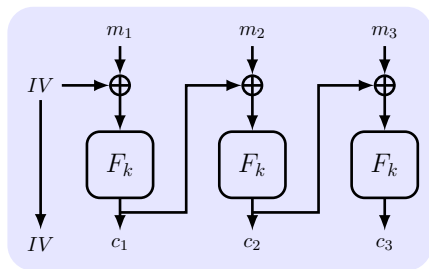
The CCA indistinguishability experiment  $\text{PrivK}_{\mathcal{A}, \Pi}^{\text{cca}}(n)$ :

- 1  $k \leftarrow \text{Gen}(1^n)$ .
  - 2  $\mathcal{A}$  is given input  $1^n$  and oracle access  $\mathcal{A}^{\text{Enc}_k(\cdot)}$  and  $\mathcal{A}^{\text{Dec}_k(\cdot)}$ , outputs  $m_0, m_1$  of the same length.
  - 3  $b \leftarrow \{0, 1\}$ .  $c \leftarrow \text{Enc}_k(m_b)$  is given to  $\mathcal{A}$ .
  - 4  $\mathcal{A}$  continues to have oracle access **except for  $c$** , outputs  $b'$ .
  - 5 If  $b' = b$ ,  $\mathcal{A}$  succeeded  $\text{PrivK}_{\mathcal{A}, \Pi}^{\text{cca}} = 1$ , otherwise 0.
- In real world, the adversary might conduct CCA by influencing what gets decrypted
    - If the communication is not authenticated, then an adversary may send certain ciphertexts on behalf of the honest party
  - CCA-security implies “**non-malleability**”
  - None of the above scheme is CCA-secure



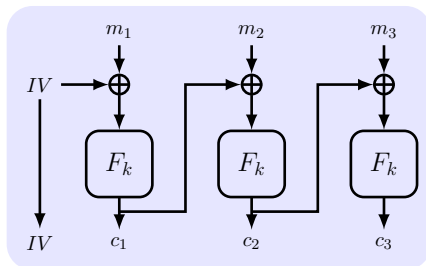
# Padding-Oracle Attacks

- In a one-block CBC, by modifying the 1st byte of  $IV$ , attacker can learn whether  $m$  is NULL. If yes, error will occur.



- append  $\{b\}^b$  as a dummy block if  $m$  is NULL
- change the 1st byte of  $IV$  from  $x$  to  $y$ , get decrypted block  $(x \oplus y \oplus b) || \{b\}^{b-1}$ , and trigger an error

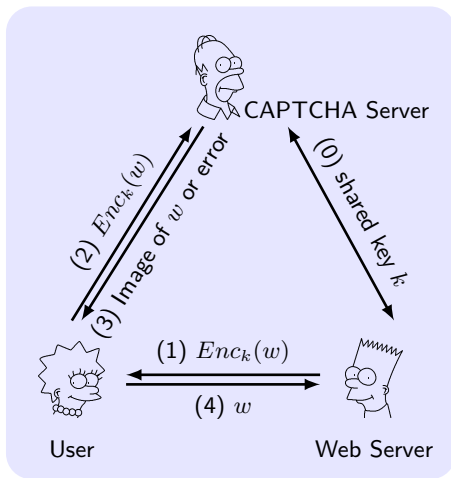
# Padding-Oracle Attacks (Cont.)



- If no error, then learn whether  $m$  is 1 byte by modifying the 2nd byte of  $IV$  and so on (changing the ciphertext)
- Once learn the length of  $m$ , learn the last byte of  $m$  ( $s$ ) by modifying the one before the last block in the ciphertext
- $m_{last} = \dots s || \{b\}^b$ ,  $c_{last-1} = \dots t || \{\cdot\}^b$
- modify  $c_{last-1}$  to  $c'_{last-1} = \dots u || (\{\cdot\}^b \oplus \{b\}^b \oplus \{b+1\}^b)$
- Q: If no padding error, then  $s = ?$

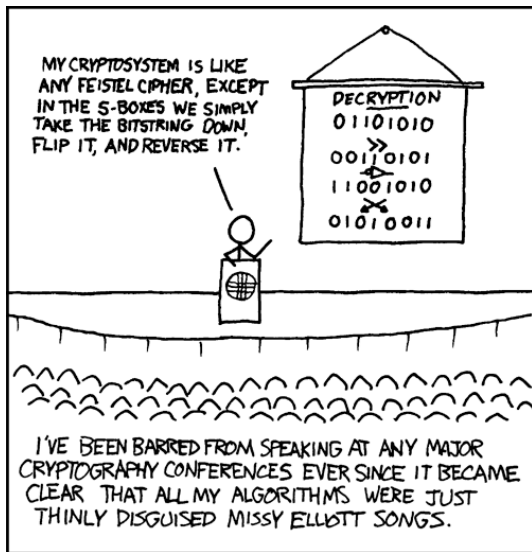
# Padding-Oracle Attacks: Real-world Case

CAPTCHA server will return an error when deciphering the CT of a CAPTCHA text received from a user.



# Comics on S-box [xkcd:153]

If you got a big keyspace, let me search it.



# Chronology of DES

- 1973** NBS (NIST) publishes a call for a standard.
- 1974** DES is published in the Federal Register.
- 1977** DES is published as FIPS PUB 46.
- 1990** Differential cryptanalysis with CPA of  $2^{47}$  plaintexts.
- 1997** DESCHALL Project breaks DES in public.
- 1998** EFF's Deep Crack breaks DES in 56hr at \$250,000.
- 1999** Triple DES.
- 2001** AES is published in FIPS PUB 197.
- 2004** FIPS PUB 46-3 is withdrawn.
- 2006** COPACOBANA breaks DES in 9 days at \$10,000.
- 2008** RIVYERA breaks DES within one day.

# AES – The Advanced Encryption Standard

- In 1997, NIST calls for AES.
- In 2001, Rijndael [J. Daemen & V. Rijmen] becomes AES.
- The first publicly accessible cipher for top secret information.
- Not only security, also efficiency and flexibility, etc.
- 128-bit block length and 128-, 192-, or 256-bit keys.
- Not a Feistel structure, but a SPN.
- Only non-trivial attacks are for reduced-round variants.
  - $2^{27}$  on 6-round of 10-round for 128-bit keys.
  - $2^{188}$  on 8-round of 12-round for 192-bit keys.
  - $2^{204}$  on 8-round of 14-round for 256-bit keys.

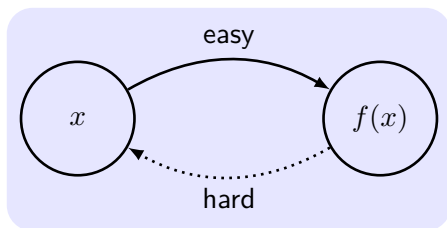
# Remarks on Block Ciphers

- **Block length** should be sufficiently large
- **Message tampering** is not with message confidentiality
- **Padding**: TLS: For  $n > 0$ ,  $n$  byte pad is  $n, n, \dots, n$  If no pad needed, add a dummy block
- **Stream ciphers vs. block ciphers**:
  - Stream ciphers are faster but have lower security
  - It is possible to use block ciphers in “stream-cipher mode”

## Performance: Crypto++ 5.6, AMD Opetron 2.2GHz

	Block/key size	Speed MB/sec
RC4		126
Salsa20/12		643
Sosemanuk		727
3DES	64/168	13
AES-128	128/128	109

# One-Way Functions (OWF)



The inverting experiment  $\text{Invert}_{\mathcal{A},f}(n)$ :

- 1 Choose input  $x \leftarrow \{0, 1\}^n$ . Compute  $y := f(x)$ .
- 2  $\mathcal{A}$  is given  $1^n$  and  $y$  as input, and outputs  $x'$ .
- 3  $\text{Invert}_{\mathcal{A},f}(n) = 1$  if  $f(x') = y$ , otherwise 0.



# Candidate One-Way Function

- **Multiplication and factoring:**

$f_{\text{mult}}(x, y) = (xy, \|x\|, \|y\|)$ ,  $x$  and  $y$  are equal-length primes.

- **Modular squaring and square roots:**

$f_{\text{square}}(x) = x^2 \bmod N$ .

- **Discrete exponential and logarithm:**

$f_{g,p}(x) = g^x \bmod p$ .

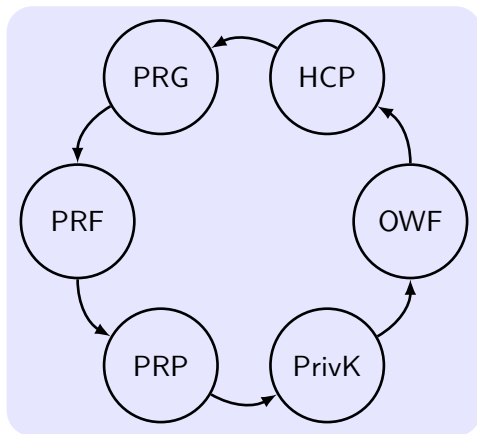
- **Subset sum problem:**

$f(x_1, \dots, x_n, J) = (x_1, \dots, x_n, \sum_{j \in J} x_j)$ .

- **Cryptographically secure hash functions:**

Practical solutions for one-way computation.

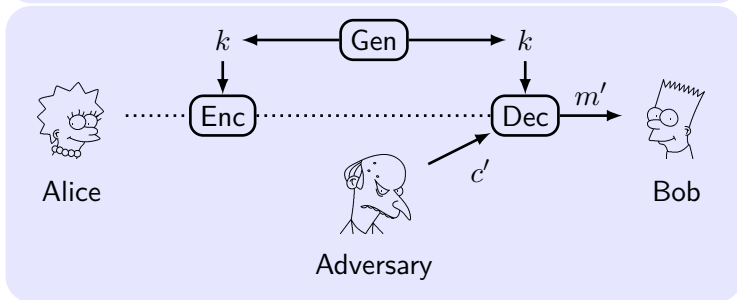
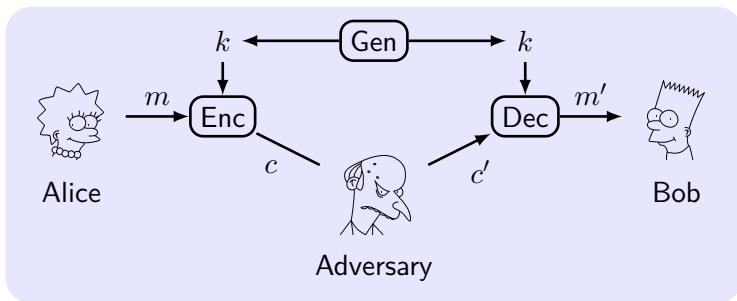
# Theoretical Constructions of Pseudorandom Objects



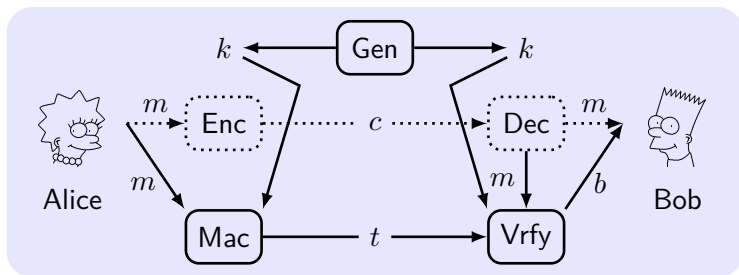
## One of contributions of modern cryptography

The existence of one-way functions is equivalent to the existence of all (non-trivial) private-key cryptography.

# Integrity and Authentication



# The Syntax of MAC



- key  $k$ , tag  $t$ , a bit  $b$  means valid if  $b = 1$ ; invalid if  $b = 0$ .
- **Key-generation** algorithm  $k \leftarrow \text{Gen}(1^n)$ ,  $|k| \geq n$ .
- **Tag-generation** algorithm  $t \leftarrow \text{Mac}_k(m)$ .
- **Verification** algorithm  $b := \text{Vrfy}_k(m, t)$ .
- **Message authentication code:**  $\Pi = (\text{Gen}, \text{Mac}, \text{Vrfy})$ .
- **Basic correctness requirement:**  $\text{Vrfy}_k(m, \text{Mac}_k(m)) = 1$ .

- **Intuition:** No adversary should be able to generate a **valid** tag on any “**new**” message<sup>1</sup> that was not previously sent.
- **Replay attack:** Copy a message and tag previously sent. (excluded by only considering “**new**” message)
  - Sequence numbers: receiver must store the previous ones.
  - Time-Stamps: sender/receiver maintain synchronized clocks.
- **Existential unforgeability:** **Not** be able to forge a valid tag on **any** message.
  - **Existential forgery:** *at least one* message.
  - **Selective forgery:** message chosen *prior* to the attack.
  - **Universal forgery:** *any* given message.
- **Adaptive chosen-message attack (CMA):** be able to obtain tags on *any* message chosen adaptively *during* its attack.

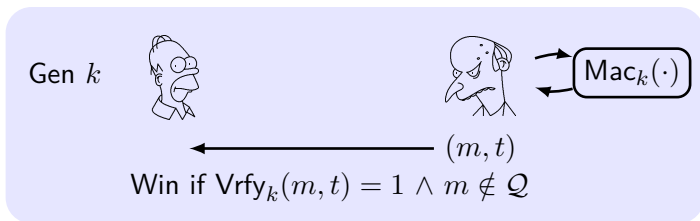
---

<sup>1</sup>A stronger requirement is concerning *new message/tag pair*.

# Definition of MAC Security

The message authentication experiment  $\text{Macforge}_{\mathcal{A}, \Pi}(n)$ :

- 1  $k \leftarrow \text{Gen}(1^n)$ .
- 2  $\mathcal{A}$  is given input  $1^n$  and oracle access to  $\text{Mac}_k(\cdot)$ , and outputs  $(m, t)$ .  $\mathcal{Q}$  is the set of queries to its oracle.
- 3  $\text{Macforge}_{\mathcal{A}, \Pi}(n) = 1 \iff \text{Vrfy}_k(m, t) = 1 \wedge m \notin \mathcal{Q}$ .

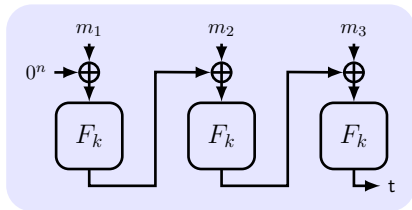
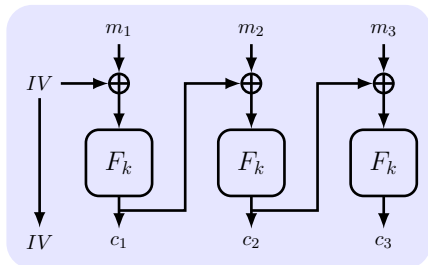


## Definition 10

A MAC  $\Pi$  is **existentially unforgeable under an adaptive CMA** if  $\forall$  PPT  $\mathcal{A}$ ,  $\exists$   $\text{negl}$  such that:

$$\Pr[\text{Macforge}_{\mathcal{A}, \Pi}(n) = 1] \leq \text{negl}(n).$$

# Constructing Fixed-Length CBC-MAC

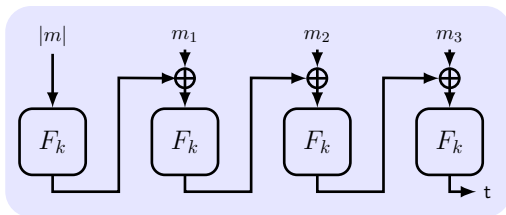


Modify CBC encryption into CBC-MAC:

- Change random  $IV$  to encrypted fixed  $0^n$ , *otherwise*:  
Q: query  $m_1$  and get  $(IV, t_1)$ ; output  $m'_1 = IV' \oplus IV \oplus m_1$  and  $t'_1 = \underline{\hspace{1cm}}$ .
- Tag only includes the output of the final block, *otherwise*:  
Q: query  $m_i$  and get  $t_i$ ; output  $m'_i = t'_{i-1} \oplus t_{i-1} \oplus m_i$  and  $t'_i = \underline{\hspace{1cm}}$ .

# Secure Variable-Length MAC

- **Input-length key separation:**  $k_\ell := F_k(\ell)$ , use  $k_\ell$  for CBC-MAC.
- **Length-prepend:** Prepend  $m$  with  $|m|$ , then use CBC-MAC.

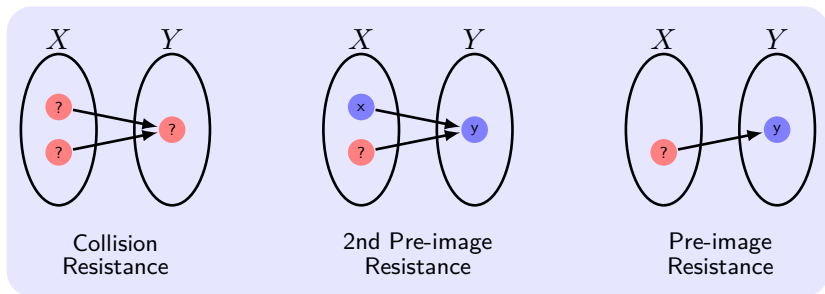


- **Encrypt last block (ECBC-MAC):** Use two keys  $k_1, k_2$ . Get  $t$  with  $k_1$  by CBC-MAC, then output  $\hat{t} := F_{k_2}(t)$ .

Q: To authenticate a voice stream, which approach do you prefer?



# Weaker Notions of Security for Hash Functions

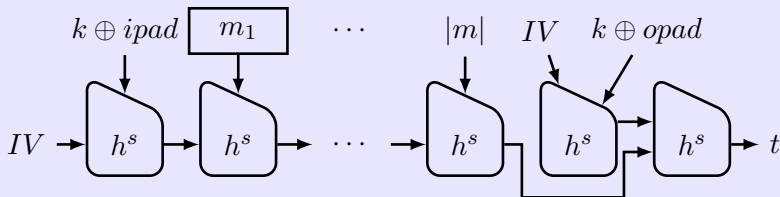


- **Collision resistance:** It is hard to find  $(x, x'), x' \neq x$  such that  $H(x) = H(x')$ .
- **Second pre-image resistance:** Given  $s$  and  $x$ , it is hard to find  $x' \neq x$  such that  $H^s(x') = H^s(x)$ .
- **Pre-image resistance:** Given  $s$  and  $y = H^s(x)$ , it is hard to find  $x'$  such that  $H^s(x') = y$ .

# Applications of Hash Functions

- **Fingerprinting and Deduplication:**  $H(\text{alargefile})$  for virus fingerprinting, deduplication, P2P file sharing
- **Merkle Trees:**  
 $H(H(H(\text{file1}), H(\text{file2})), H(H(\text{file3}), H(\text{file4})))$   
fingerprinting multiple files / parts of a file
- **Password Hashing:**  $(\text{salt}, H(\text{salt}, \text{pw}))$  mitigating the risk of leaking password stored in the clear
- **Key Derivation:**  $H(\text{secret})$  deriving a key from a high-entropy (but not necessarily uniform) shared secret
- **Commitment Schemes:**  $H(\text{info})$  hiding the committed info; binding the commitment to a info

# Hash-based MAC (HMAC)



## Construction 11

$(\widetilde{\text{Gen}}, h)$  is a fixed-length CRHF.  $(\widetilde{\text{Gen}}, H)$  is the Merkle-Damgård transform.  $IV$ ,  $opad$  ( $0 \times 36$ ),  $ipad$  ( $0 \times 5C$ ) are fixed constants of length  $n$ . HMAC:

- $\text{Gen}(1^n)$ : Output  $(s, k)$ .  $s \leftarrow \widetilde{\text{Gen}}, k \leftarrow \{0, 1\}^n$  u.a.r
- $\text{Mac}_{s,k}(m)$ :  $t := H_{IV}^s((k \oplus opad) \| H_{IV}^s((k \oplus ipad) \| m))$
- $\text{Vrfy}_{s,k}(m, t)$ :  $1 \iff t \stackrel{?}{=} \text{Mac}_{s,k}(m)$

## Theorem 12

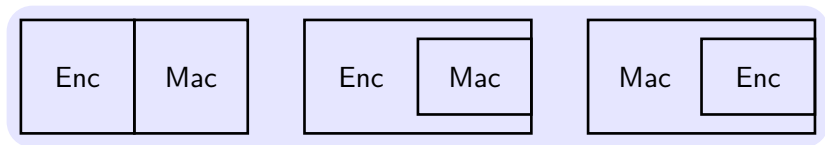
$G(k) \stackrel{\text{def}}{=} h^s(IV \parallel (k \oplus \text{opad})) \parallel h^s(IV \parallel (k \oplus \text{ipad})) = k_1 \parallel k_2$   
 $(\widetilde{\text{Gen}}, h)$  is CRHF. If  $G$  is a PRG, then HMAC is secure.

- HMAC is an industry standard (RFC2104)
- HMAC is faster than CBC-MAC
- Before HMAC, a common mistake was to use  $H^s(k \parallel x)$
- **Verification timing attacks: (Keyczar crypto library (Python))**  

```
def Verify(key, msg, sig_bytes):  
    return HMAC(key, msg) == sig_bytes
```

The problem: implemented as a byte-by-byte comparison
- *Don't implement it yourself*

# Combining Encryption and Authentication



- **Encrypt-and-authenticate** (e.g., SSH):

$$c \leftarrow \text{Enc}_{k_1}(m), t \leftarrow \text{Mac}_{k_2}(m).$$

- **Authenticate-then-encrypt** (e.g., SSL):

$$t \leftarrow \text{Mac}_{k_2}(m), c \leftarrow \text{Enc}_{k_1}(m||t).$$

- **Encrypt-then-authenticate** (e.g., IPsec):

$$c \leftarrow \text{Enc}_{k_1}(m), t \leftarrow \text{Mac}_{k_2}(c).$$

# Analyzing Security of Combinations

**All-or-nothing:** Reject any combination for which there exists even a single counterexample is insecure.

- **Encrypt-and-authenticate:**  $\text{Mac}'_k(m) = (m, \text{Mac}_k(m))$ .

- **Authenticate-then-encrypt:**

- $\text{Trans} : 0 \rightarrow 00; 1 \rightarrow 10/01$ ;  $\text{Enc}'$  uses CTR mode;  
 $c = \text{Enc}'(\text{Trans}(m \parallel \text{Mac}(m)))$ .
- Flip the first two bits of  $c$  and verify whether the ciphertext is valid.  $10/01 \rightarrow 01/10 \rightarrow 1$ ,  $00 \rightarrow 11 \rightarrow \perp$ .
- If valid, the first bit of message is 1; otherwise 0.
- For any MAC, this is not CCA-secure.

- **Encrypt-then-authenticate:**

Decryption: If  $\text{Vrfy}(\cdot) = 1$ , then  $\text{Dec}(\cdot)$ ; otherwise output  $\perp$ .

## Theorem 13

$\Pi_E$  is CPA-secure and  $\Pi_E$  is a secure MAC with unique tags,  $\Pi'$  deriving from encrypt-then-authenticate approach is secure.

**GCM(Galois/Counter Mode):** CTR encryption then Galois MAC. (RFC4106/4543/5647/5288 on IPsec/SSH/TLS)

**EAX:** CTR encryption then CMAC.

## Proposition 14

*Authenticate-then-encrypt approach is secure if  $\Pi_E$  is rand-CTR mode or rand-CBC mode.*

**CCM (Counter with CBC-MAC):** CBC-MAC then CTR encryption. (802.11i, RFC3610)

**OCB (Offset Codebook Mode):** integrating MAC into ENC. (two times fast as CCM, EAX)

**All support AEAD (A.E. with associated data):** part of message is in clear, and all is authenticated

# Remarks on Secure Message Transmission

- Authentication may leak the message.
- Secure message transmission implies CCA-security. The opposite direction is not necessarily true.
- Different security goals should always use different keys.
  - otherwise, the message may be leaked if  $\text{Mac}_k(c) = \text{Dec}_k(c)$ .
- Implementation may destroy the security proved by theory.
  - **Attack with padding oracle** (in TLS 1.0):  
**Dec** return two types of error: padding error, MAC error.  
**Adv.** learns last bytes if no padding error with guessed bytes.
  - **Attack non-atomic dec.** (in SSH Binary Packet Protocol):  
**Dec** (1)decrypt length field; (2)read packets as specified by the length; (3)check MAC.  
**Adv.** (1)send  $c$ ; (2)send  $l$  packets until “MAC error” occurs; (3)learn  $l = \text{Dec}(c)$ .



# Password-Based KDF (PBKDF)

**Key stretching** increases the time of testing key (with slow hash function).

**Key strengthening** increases the length/randomness of key (with salt).

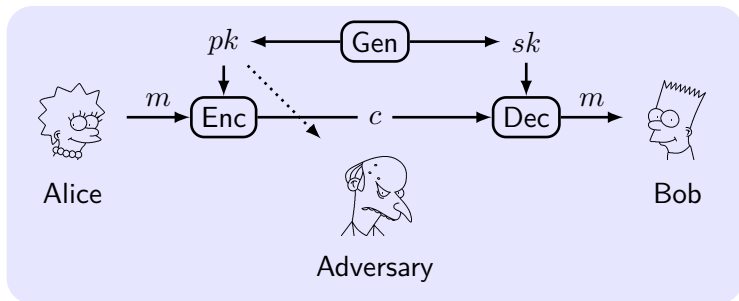
**PKCS#5 (PBKDF1):**  $H^{(c)}(pwd || salt)$ , iterate hash function  $c$  times.

**Attack:** either try the enhanced key (larger key space), or else try the initial key (longer time per key).

# Public-Key Revolution

- In 1976, Whitfield Diffie and Martin Hellman published “*New Directions in Cryptography*”.
- **Asymmetric** or **public-key** encryption schemes:
  - **Public key** as the encryption key.
  - **Private key** as the decryption key.
- **Public-key primitives:**
  - Public-key encryption.
  - Digital signatures. (non-repudiation)
  - Interactive key exchange.
- **Strength:**
  - Key distribution over public channels.
  - Reduce the need to store many keys.
  - Enable security in open system.
- **Weakness:** slow, active attack on public key distribution.

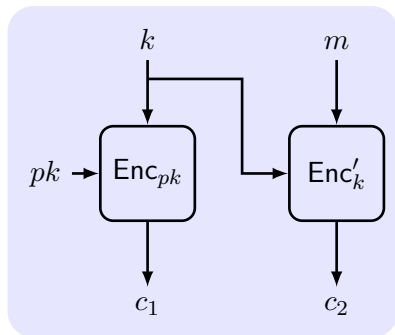
# Definitions



- **Key-generation** algorithm:  $(pk, sk) \leftarrow \text{Gen}$ , key length  $\geq n$ .
- **Plaintext space**  $\mathcal{M}$  is associated with  $pk$ .
- **Encryption** algorithm:  $c \leftarrow \text{Enc}_{pk}(m)$ .
- **Decryption** algorithm:  $m := \text{Dec}_{sk}(c)$ , or outputs  $\perp$ .
- **Requirement**:  $\Pr[\text{Dec}_{sk}(\text{Enc}_{pk}(m)) = m] \geq 1 - \text{negl}(n)$ .

# Construction of Hybrid Encryption

To speed up the encryption of long message, use private-key encryption  $\Pi'$  in tandem with public-key encryption  $\Pi$ .



## Construction 15

$\Pi^{\text{hy}} = (\text{Gen}^{\text{hy}}, \text{Enc}^{\text{hy}}, \text{Dec}^{\text{hy}})$ :

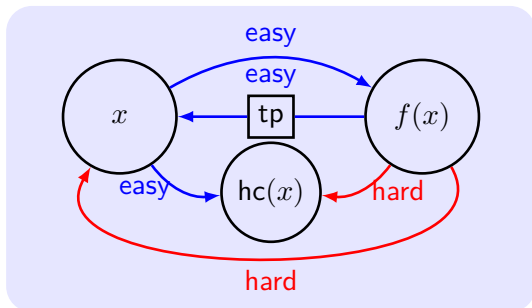
- $\text{Gen}^{\text{hy}}$ :  
 $(pk, sk) \leftarrow \text{Gen}(1^n)$ .
- $\text{Enc}^{\text{hy}}$ :  $pk$  and  $m$ .
  - 1  $k \leftarrow \{0, 1\}^n$ .
  - 2  $c_1 \leftarrow \text{Enc}_{pk}(k)$ ,  
 $c_2 \leftarrow \text{Enc}'_k(m)$ .
- $\text{Dec}^{\text{hy}}$ :  $sk$  and  $\langle c_1, c_2 \rangle$ .
  - 1  $k := \text{Dec}_{sk}(c_1)$ .
  - 2  $m := \text{Dec}'_k(c_2)$ .

Q: is hybrid encryption a public-key enc. or private-key enc. ?

# Trapdoor Permutations

**Trapdoor function:** is easy to compute, yet difficult to find its inverse without special info., the “trapdoor”. (One Way Function with the “trapdoor”)

A public-key encryption scheme can be constructed from any trapdoor permutation. (*“Theory and Applications of Trapdoor Functions”*, [Yao, 1982])



# Public-key Encryption Schemes from TDPs

## Construction 16

- Gen:  $(I, \text{td}) \leftarrow \widehat{\text{Gen}}$  output **public key**  $I$  and **private key**  $\text{td}$ .
- Enc: on input  $I$  and  $m \in \{0, 1\}^*$ , choose a random  $x \leftarrow \mathcal{D}_I$  and output  $\langle f_I(x), \text{hc}_I(x) \oplus m \rangle$ .
- Dec: on input  $\text{td}$  and  $\langle y, m' \rangle$ , compute  $x := f_I^{-1}(y)$  and output  $\text{hc}_I(x) \oplus m'$ .

## Theorem 17

If  $\widehat{\Pi} = (\widehat{\text{Gen}}, f)$  is TDP, and  $\text{hc}$  is HCP for  $\widehat{\Pi}$ , then Construction  $\Pi$  is CPA-secure.

**Is the following scheme is secure?**

$$\text{Enc}_I(m) = f_I(m), \text{Dec}_{\text{td}}(c) = f_I^{-1}(c).$$

# Scenarios of CCA in Public-Key Setting

- 1 An adversary  $\mathcal{A}$  observes the ciphertext  $c$  sent by  $\mathcal{S}$  to  $\mathcal{R}$ .
- 2  $\mathcal{A}$  send  $c'$  to  $\mathcal{R}$  in the name of  $\mathcal{S}$  or its own.
- 3  $\mathcal{A}$  infer  $m$  from the decryption of  $c'$  to  $m'$ .

## Scenarios

- **login to on-line bank with the password:** trial-and-error, learn info from the feedback of bank.
- **reply an e-mail with the quotation of decrypted text.**
- **malleability of ciphertexts:** e.g. doubling others' bids at an auction.

# State of the Art on CCA2-secure Encryption

- **Zero-Knowledge Proof**: complex, and impractical. (e.g., Dolev-Dwork-Naor)
- **Random Oracle** model: efficient, but not realistic (to consider CRHF as RO). (e.g., RSA-OAEP and Fujisaki-Okamoto)
- **DDH(Decisional Diffie-Hellman assumption) and UOWHF(Universal One-Way Hashs Function)**:  $\times 2$  expansion in size, but security proved w/o RO or ZKP (e.g., Cramer-Shoup system).

**CCA2-secure implies Plaintext-aware**: an adversary cannot produce a valid ciphertext without “knowing” the plaintext.

## Open problem

Constructing a CCA2-secure scheme based on RSA problem as efficient as “Textbook RSA”.



# Private Key Encryption vs. Public Key Encryption

	<b>Private Key</b>	<b>Public Key</b>
<b>Secret Key</b>	both parties	receiver
<b>Weakest Attack</b>	Eav	CPA
<b>Probabilistic</b>	CPA/CCA	always
<b>Assumption against CPA</b>	OWF	TDP
<b>Assumption against CCA</b>	OWF	TDP+RO
<b>Efficiency</b>	fast	slow

- **RSA**: Ron Rivest, Adi Shamir and Leonard Adleman, in 1977
- **RSA problem**: Given  $N = pq$  (two distinct big prime numbers) and  $y \in \mathbb{Z}_N^*$ , compute  $y^{-e}$ ,  $e^{\text{th}}$ -root of  $y$  modulo  $N$
- **Open problem**: RSA problem is easier than factoring  $N$ ?
- **Certification**: PKCS#1 (RFC3447), ANSI X9.31, IEEE 1363
- **Key sizes**: 1,024 to 4,096 bit
- **Best public cryptanalysis**: a 768 bit key has been broken
- **RSA Challenge**: break RSA-2048 to win \$200,000 USD

**Key lengths** with comparable security :

Symmetric	RSA
80 bits	1024 bits
128 bits	3072 bits
256 bits	15360 bits

## Construction 18

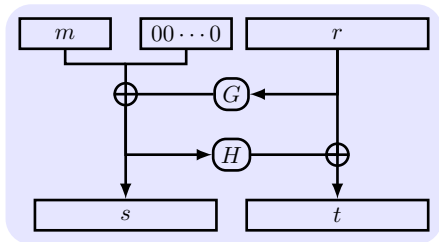
- Gen: on input  $1^n$  run  $\text{GenRSA}(1^n)$  to obtain  $N, e, d$ .  
 $pk = \langle N, e \rangle$  and  $sk = \langle N, d \rangle$ .
- Enc: on input  $pk$  and  $m \in \mathbb{Z}_N^*$ ,  $c := [m^e \bmod N]$ .
- Dec: on input  $sk$  and  $m \in \mathbb{Z}_N^*$ ,  $m := [c^d \bmod N]$ .

## Insecurity

Since the “textbook RSA” is deterministic, it is insecure with respect to any of the definitions of security we have proposed.

# PKCK #1 v2.1 (RSAES-OAEP) (Cont.)

RSA-OAEP is CCA-secure in Random Oracle model.<sup>2</sup> [RFC 3447]



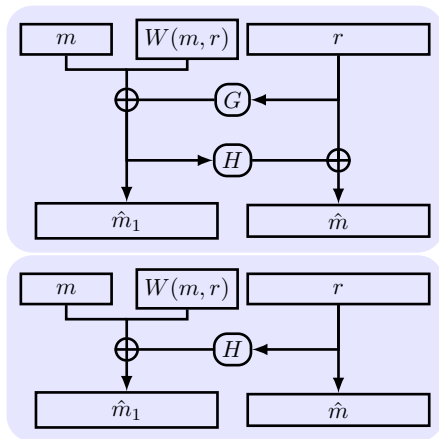
CPA: To learn  $r$ , attacker has to learn  $\hat{m}_1$  from  $(\hat{m}_1 || \hat{m})^e$

CCA: Effective decryption query is disabled by checking "00...0" in the plaintext before the response

---

<sup>2</sup>It may not be secure when RO is instantiated.

# OAEP Improvements



**OAEP+**:  $\forall$  trap-door permutation  $F$ , F-OAEP+ is CCA-secure.

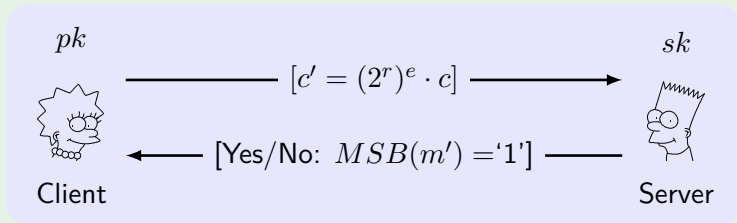
**SAEP+**: RSA ( $e=3$ ) is a trap-door permutation, RSA-SAEP+ is CCA-secure.

$W, G, H$  are Random Oracles.

# Implementation Attacks on RSA

## Simplified CCA on PKCS1 v1.5 in HTTPS [Bleichenbacher]

Server tells if the MSB of plaintext (Version Number) = '1' for a given ciphertext. Attacker sends  $c' = (2^r)^e \cdot c$ . If receiving *Yes*, then  $(r + 1)$ -th  $MSB(m) = ?$



**Defense:** treating incorrectly formatted message blocks in a manner indistinguishable from correctly formatted blocks. See [RFC 5246]

# Implementation Attacks on RSA (Cont.)

**Timing attack:** [Kocher et al. 1997] The time it takes to compute  $c^d$  can expose  $d$ . (require a high-resolution clock)

**Power attack:** [Kocher et al. 1999] The power consumption of a smartcard while it is computing  $c^d$  can expose  $d$ .

**Defense: Blinding** by choosing a random  $r$  and deciphering  $r^e \cdot c$ .

**Key generation trouble** (in OpenSSL RSA key generation):

Same  $p$  will be generated by multiple devices (due to poor entropy at startup), but different  $q$  (due to additional randomness).

Q:  $N_1, N_2$  from different devices,  $\gcd(N_1, N_2) = ?$

Experiment result: factor 0.4% of public HTTPS keys.

# Faults Attack on RSA

**Faults attack:** A computer error during  $c^d \bmod N$  can expose  $d$ .

Using Chinese Remainder Theory to speed up the decryption:

$$[c^d \bmod N] \leftrightarrow ([m_p \equiv c^d \pmod{p}], [m_q \equiv c^d \pmod{q}]).$$

**Suppose error occurs when computing  $m_q$ , but no error in  $m_p$ .**

Then output  $m' \equiv c^d \pmod{p}$ ,  $m' \not\equiv c^d \pmod{q}$ .

So  $(m')^e \equiv c \pmod{p}$ ,  $(m')^e \not\equiv c \pmod{q}$ .

$$\gcd((m')^e - c, N) = ?$$

**Defense:** check output. (but 10% slowdown)



# Diffie-Hellman Assumptions

- **Computational Diffie-Hellman (CDH) problem:**

$$\text{DH}_g(h_1, h_2) \stackrel{\text{def}}{=} g^{\log_g h_1 \cdot \log_g h_2}$$

- **Decisional Diffie-Hellman (DDH) problem:**

Distinguish  $\text{DH}_g(h_1, h_2)$  from a random group element  $h'$ .

## Definition 19

DDH problem is hard relative to  $\mathcal{G}$  if  $\forall$  PPT  $\mathcal{A}$ ,  $\exists$   $\text{negl}$  such that

$$|\Pr[\mathcal{A}(\mathbb{G}, q, g, g^x, g^y, g^z) = 1] - \Pr[\mathcal{A}(\mathbb{G}, q, g, g^x, g^y, g^{xy}) = 1]| \\ \leq \text{negl}(n).$$

## Intractability of DL, CDH and DDH

DDH is easier than CDH and DL.

# Diffie-Hellman Key-Exchange Protocol



$$(\mathbb{G}, q, g) \leftarrow \mathcal{G}$$

$$x \leftarrow \mathbb{Z}_q$$
$$h_1 := g^x \xrightarrow{\mathbb{G}, q, g, h_1}$$

$$y \leftarrow \mathbb{Z}_q$$
$$h_2 := g^y \xleftarrow{h_2}$$

$$k_A := h_2^x$$

$$k_B := h_1^y$$

Q:  $k_A = k_B = k = ?$

$\widehat{\text{KE}}_{\mathcal{A}, \Pi}^{\text{eav}}$  denote an experiment where if  $b = 0$  the adversary is given  $\hat{k} \leftarrow \mathbb{G}$ .

## Theorem 20

*If DDH problem is hard relative to  $\mathcal{G}$ , then DH key-exchange protocol  $\Pi$  is secure in the presence of an eavesdropper (with respect to the modified experiment  $\widehat{\text{KE}}_{\mathcal{A}, \Pi}^{\text{eav}}$ ).*

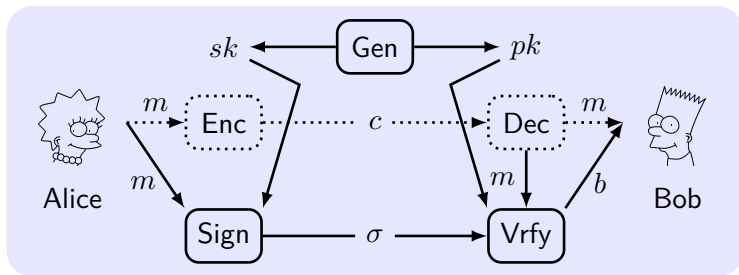
## Security

Insecurity against active adversaries (Man-In-The-Middle).

# Digital Signatures – An Overview

- **Digital signature scheme** is a mathematical scheme for demonstrating the authenticity/integrity of a digital message
- allow a **signer**  $S$  to “**sign**” a message with its own  $sk$ , anyone who knows  $S$ 's  $pk$  can **verify** the authenticity/integrity
- (Comparing to MAC) digital signature is:
  - publicly verifiable
  - transferable
  - non-repudiation
  - but slow
- Q: What are the differences between digital signatures and handwritten signatures?
- Digital signature is NOT the “inverse” of public-key encryption

# The Syntax of Digital Signature Scheme



- signature  $\sigma$ , a bit  $b$  means valid if  $b = 1$ ; invalid if  $b = 0$ .
- **Key-generation** algorithm  $(pk, sk) \leftarrow \text{Gen}(1^n), |pk|, |sk| \geq n$ .
- **Signing** algorithm  $\sigma \leftarrow \text{Sign}_{sk}(m)$ .
- **Verification** algorithm  $b := \text{Vrfy}_{pk}(m, \sigma)$ .
- **Basic correctness requirement:**  $\text{Vrfy}_{pk}(m, \text{Sign}_{sk}(m)) = 1$ .

# Defining of Signature Security

The signature experiment  $\text{Sigforge}_{\mathcal{A},\Pi}(n)$ :

- 1  $(pk, sk) \leftarrow \text{Gen}(1^n)$ .
- 2  $\mathcal{A}$  is given input  $1^n$  and oracle access to  $\text{Sign}_{sk}(\cdot)$ , and outputs  $(m, \sigma)$ .  $\mathcal{Q}$  is the set of queries to its oracle.
- 3  $\text{Sigforge}_{\mathcal{A},\Pi}(n) = 1 \iff \text{Vrfy}_{pk}(m, \sigma) = 1 \wedge m \notin \mathcal{Q}$ .

## Definition 21

A signature scheme  $\Pi$  is **existentially unforgeable under an adaptive CMA** if  $\forall$  PPT  $\mathcal{A}$ ,  $\exists$   $\text{negl}$  such that:

$$\Pr[\text{Sigforge}_{\mathcal{A},\Pi}(n) = 1] \leq \text{negl}(n).$$

**Q: What's the difference on the ability of adversary between MAC and digital signature? What if an adversary is not limited to PPT?**

# The “Hash-and-Sign” Paradigm

## Construction 22

$\Pi = (\text{Gen}_S, \text{Sign}, \text{Vrfy})$ ,  $\Pi_H = (\text{Gen}_H, H)$ . A signature scheme  $\Pi'$ :

- $\text{Gen}'$ : on input  $1^n$  run  $\text{Gen}_S(1^n)$  to obtain  $(pk, sk)$ , and run  $\text{Gen}_H(1^n)$  to obtain  $s$ . The public key is  $pk' = \langle pk, s \rangle$  and the private key is  $sk' = \langle sk, s \rangle$ .
- $\text{Sign}'$ : on input  $sk'$  and  $m \in \{0, 1\}^*$ ,  $\sigma \leftarrow \text{Sign}_{sk}(H^s(m))$ .
- $\text{Vrfy}'$ : on input  $pk'$ ,  $m \in \{0, 1\}^*$  and  $\sigma$ , output  $1 \iff \text{Vrfy}_{pk}(H^s(m), \sigma) = 1$ .

## Theorem 23

If  $\Pi$  is existentially unforgeable under an adaptive CMA and  $\Pi_H$  is collision resistant, then Construction is existentially unforgeable under an adaptive CMA.

# One-Time Signature (OTS)

**One-Time Signature (OTS):** Under a weaker attack scenario, sign only one message with one secret.

The OTS experiment  $\text{Sigforge}_{\mathcal{A}, \Pi}^{1\text{-time}}(n)$ :

- 1  $(pk, sk) \leftarrow \text{Gen}(1^n)$ .
- 2  $\mathcal{A}$  is given input  $1^n$  and a **single query**  $m'$  to  $\text{Sign}_{sk}(\cdot)$ , and outputs  $(m, \sigma)$ ,  $m \neq m'$ .
- 3  $\text{Sigforge}_{\mathcal{A}, \Pi}^{1\text{-time}}(n) = 1 \iff \text{Vrfy}_{pk}(m, \sigma) = 1$ .

## Definition 24

A signature scheme  $\Pi$  is **existentially unforgeable under a single-message attack** if  $\forall$  PPT  $\mathcal{A}$ ,  $\exists$   $\text{negl}$  such that:

$$\Pr[\text{Sigforge}_{\mathcal{A}, \Pi}^{1\text{-time}}(n) = 1] \leq \text{negl}(n).$$

**Idea:** OTS from OWF; one mapping per bit.

## Construction 25

*f is a one-way function.*

■ Gen: on input  $1^n$ , for  $i \in \{1, \dots, \ell\}$ :

1 choose random  $x_{i,0}, x_{i,1} \leftarrow \{0, 1\}^n$ .

2 compute  $y_{i,0} := f(x_{i,0})$  and  $y_{i,1} := f(x_{i,1})$ .

$$pk = \begin{pmatrix} y_{1,0} & y_{2,0} & \cdots & y_{\ell,0} \\ y_{1,1} & y_{2,1} & \cdots & y_{\ell,1} \end{pmatrix} \quad sk = \begin{pmatrix} x_{1,0} & x_{2,0} & \cdots & x_{\ell,0} \\ x_{1,1} & x_{2,1} & \cdots & x_{\ell,1} \end{pmatrix}.$$

■ Sign:  $m = m_1 \cdots m_\ell$ , output  $\sigma = (x_{1,m_1}, \dots, x_{\ell,m_\ell})$ .

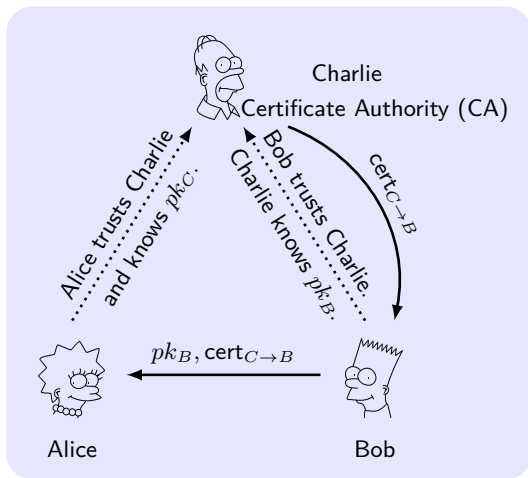
■ Vrfy:  $\sigma = (x_1, \dots, x_\ell)$ , output  $1 \iff f(x_i) = y_{i,m_i}$ , for all  $i$ .

## Theorem 26

*If f is OWF,  $\Pi$  is OTS for messages of length polynomial  $\ell$ .*



# Certificates



**Certificates**  $cert_{C \rightarrow B} \stackrel{\text{def}}{=} \text{Sign}_{sk_C}(\text{'Bob's key is } pk_B')$ .

# Public-Key Infrastructure (PKI)

- **A single CA:** is trusted by everybody.
  - Strength: simple
  - Weakness: single-point-of-failure
- **Multiple CAs:** are trusted by everybody.
  - Strength: robust
  - Weakness: cannikin law
- **Delegation and certificate chains:** The trust is transitive.
  - Strength: ease the burden on the root CA.
  - Weakness: difficult for management, cannikin law.
- **“Web of trust”:** No central points of trust, e.g., PGP.
  - Strength: robust, work at “grass-roots” level.
  - Weakness: difficult to manage/give a guarantee on trust.

# Invalidating Certificates

- **Expiration:** include an *expiry date* in the certificate.

$$\text{cert}_{C \rightarrow B} \stackrel{\text{def}}{=} \text{Sign}_{sk_C}(\text{'bob's key is } pk_B', \text{ date}).$$

- **Revocation:** explicitly revoke the certificate.

$$\text{cert}_{C \rightarrow B} \stackrel{\text{def}}{=} \text{Sign}_{sk_C}(\text{'bob's key is } pk_B', \text{ ###}).$$

“###” represents the serial number of this certificate.

**Cumulated Revocation:** CA generates *certificate revocation list* (CRL) containing the serial numbers of all revoked certificates, signs CRL with the current date.

- A proof of security never proves security in an absolute sense, it relates security to an unproven assumption that some computational problem is hard.
- The quality of a security reduction should not be ignored – it matters how tight it is, and how strong the underlying assumption is.
- A security reduction only proves something in a particular model specifying what the adversary has access to and can do.

Crypto deceptively simple

- Why does it so often fail?

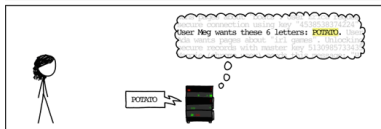
Important to distinguish various issues:

- 1 Bad cryptography/implementations/design, etc.
- 2 Good cryptography can be 'circumvented' by adversaries operating 'outside the model'
- 3 Even the best cryptography only shifts the weakest point of failure to elsewhere in your system
- 4 Systems are complex: key management; social engineering; insider attacks

Avoid the first; be aware of 2-4.

# Bad Implementation Example: Heartbleed

## HOW THE HEARTBEAT BUG WORKS:



# Crypto is difficult to get right

- Must be implemented correctly
- Must be integrated from the beginning, not added on “after the fact”
- Need expertise; “a little knowledge can be a dangerous thing”
- Can't be secured by Q/A, only (at best) through penetration testing and dedicated review of the code by security experts

# Beware of Snake Oil

**Snake Oil:** bogus commercial cryptographic products.

- **Secret system:** security through obscurity
- **Technobabble:** since cryptography is complicated
- **Unbreakable:** a sure sign of snake oil
- **One-time pads:** a flawed implementation
- **Unsubstantiated “bit” claims:** key lengths are not directly comparable



# General Recommendation

- Use only standardized algorithms and protocols
- No security through obscurity!
- Use primitives for their intended purpose
- Don't implement your own crypto
- If your system cannot use “off-the-shelf” crypto components, re-think your system
- If you really need something new, have it designed and/or evaluated by an expert
- Don't use the same key for multiple purposes
- Use good random-number generation

- Use existing, high-level crypto libraries: cryptlib, NaCl, Google's Keyczar, Mozilla's NSS, OpenSSL
- Avoid low-level libraries (like JCE, crypto++, GnuPG, OpenPGP) - too much possibility of mis-use
- Avoid writing your own low-level crypto